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Functions

## allanvar

Allan variance

## Syntax

```
[avar,tau] = allanvar(Omega)
[avar,tau] = allanvar(Omega,m)
[avar,tau] = allanvar(Omega,ptStr)
[avar,tau] = allanvar(
```

$\qquad$

``` ,fs)
```


## Description

Allan variance is used to measure the frequency stability of oscillation for a sequence of data in the time domain. It can also be used to determine the intrinsic noise in a system as a function of the averaging time. The averaging time series $\tau$ can be specified as $\tau=m / f s$. Here $f s$ is the sampling frequency of data, and $m$ is a list of ascending averaging factors (such as $1,2,4,8, \ldots$ ).
[avar,tau] = allanvar(Omega) returns the Allan variance avar as a function of averaging time tau. The default averaging time tau is an octave sequence given as $\left(1,2, \ldots, 2^{\text {flor }\left\{\log _{2}[(N-1) / 2]\right\}}\right)$, where $N$ is the number of samples in Omega. If Omega is specified as a matrix, allanvar operates over the columns of omega.
[avar,tau] = allanvar(Omega,m) returns the Allan variance avar for specific values of tau defined by m . Since the default frequency fs is assumed to be 1 , the output tau is exactly same with m.
[avar,tau] = allanvar(Omega,ptStr) sets averaging factor $m$ to the specified point specification, ptStr. Since the default frequency fs is 1 , the output tau is exactly equal to the specified $m$. ptStr can be specified as 'octave' or 'decade'.
[avar,tau] = allanvar( $\qquad$ , fs) also allows you to provide the sampling frequency fs of the input data omega in Hz . This input parameter can be used with any of the previous syntaxes.

## Examples

## Determine Allan Variance of Single Axis Gyroscope

Load gyroscope data from a MAT file, including the sample rate of the data in Hz. Calculate the Allan variance.

```
load('LoggedSingleAxisGyroscope','omega','Fs')
[avar,tau] = allanvar(omega,'octave',Fs);
```

Plot the Allan variance on a loglog plot.

```
loglog(tau,avar)
xlabel('\tau')
ylabel('\sigma^2(\tau)')
title('Allan Variance')
grid on
```



## Determine Allan Deviation at Specific Values of $\tau$

Generate sample gyroscope noise, including angle random walk and rate random walk.

```
numSamples = le6;
Fs = 100;
nStd = 1e-3;
kStd = 1e-7;
nNoise = nStd.*randn(numSamples,1);
kNoise = kStd.*cumsum(randn(numSamples,1));
omega = nNoise+kNoise;
```

Calculate the Allan deviation at specific values of $m=\tau$. The Allan deviation is the square root of the Allan variance.

```
m = 2.^(9:18);
[avar,tau] = allanvar(omega,m,Fs);
adev = sqrt(avar);
```

Plot the Allan deviation on a loglog plot.
loglog(tau, adev)
xlabel('\tau')
ylabel('\sigma(\tau)')
title('Allan Deviation')
grid on


## Input Arguments

## Omega - Input data

$N$-by-1 vector $\mid N$-by- $M$ matrix
Input data specified as an $N$-by- 1 vector or an $N$-by- $M$ matrix. $N$ is the number of samples, and $M$ is the number of sample sets. If specified as a matrix, allanvar operates over the columns of Omega.
Data Types: single | double
m - Averaging factor
scalar | vector
Averaging factor, specified as a scalar or vector with ascending integer values less than ( $N-1$ )/2, where $N$ is the number of samples in Omega.
Data Types: single | double
ptStr - Point specification of $m$
'octave' (default)|'decade'
Point specification of $m$, specified as 'octave' or 'decade'. Based on the value of ptStr, $m$ is specified as following:

- If $p t S t r$ is specified as 'octave ', $m$ is:

$$
\left.\left[2^{0}, 2^{1} \ldots 2^{\log _{2}\left(\frac{N-1}{2}\right)}\right]\right]
$$

- If $p t S t r$ is specified as 'decade ', $m$ is:

$$
\left.\left[10^{0}, 10^{1} \ldots 10^{\log _{10}\left(\frac{N-1}{2}\right)}\right)\right]
$$

$N$ is the number of samples in Omega.

## fs - Basic frequency of input data in Hz scalar

Basic frequency of the input data, Omega, in Hz , specified as a positive scalar.
Data Types: single | double

## Output Arguments

## avar - Allan variance of input data

vector | matrix
Allan variance of input data at tau, returned as a vector or matrix.
tau - Averaging time of Allan variance
vector | matrix
Averaging time of Allan variance, returned as a vector, or a matrix.

## See Also

gyroparams|imuSensor
Introduced in R2019a

## angdiff

Difference between two angles

## Syntax

```
delta = angdiff(alpha,beta)
delta = angdiff(alpha)
```


## Description

delta = angdiff(alpha,beta) calculates the difference between the angles alpha and beta. This function subtracts alpha from beta with the result wrapped on the interval [-pi, pi]. You can specify the input angles as single values or as arrays of angles that have the same number of values.
delta $=$ angdiff(alpha) returns the angular difference between adjacent elements of alpha along the first dimension whose size does not equal 1 . If alpha is a vector of length $n$, the first entry is subtracted from the second, the second from the third, etc. The output, delta, is a vector of length $n$-1. If alpha is an $m$-by- $n$ matrix with $m$ greater than 1 , the output, delta, will be a matrix of size $m-1$-by-n. If alpha is a scalar, delta returns as an empty vector.

## Examples

## Calculate Difference Between Two Angles

```
d = angdiff(pi,2*pi)
d = 3.1416
```


## Calculate Difference Between Two Angle Arrays

```
d = angdiff([pi/2 3*pi/4 0],[pi pi/2 -pi])
d = 1\times3
    1.5708 -0.7854 -3.1416
```


## Calculate Angle Differences of Adjacent Elements

angles = [pi pi/2 pi/4 pi/2];
d = angdiff(angles)
$\mathrm{d}=1 \times 3$

## Input Arguments

alpha - Angle in radians
scalar | vector | matrix | multidimensional array
Angle in radians, specified as a scalar, vector, matrix, or multidimensional array. This is the angle that is subtracted from beta when specified. If alpha is a scalar, delta returns as an empty vector.
Example: pi/2
beta - Angle in radians
scalar | vector | matrix | multidimensional array
Angle in radians, specified as a scalar, vector, matrix, or multidimensional array of the same size as alpha. This is the angle that alpha is subtracted from when specified.
Example: pi/2

## Output Arguments

delta - Difference between two angles
scalar | vector | matrix | multidimensional array
Angular difference between two angles, returned as a scalar, vector, or array. delta is wrapped to the interval [-pi, pi]. If alpha is a scalar, delta returns as an empty vector.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Introduced in R2015a

## axang2quat

Convert axis-angle rotation to quaternion

## Syntax

```
quat = axang2quat(axang)
```


## Description

quat = axang2quat(axang) converts a rotation given in axis-angle form, axang, to quaternion, quat.

## Examples

## Convert Axis-Angle Rotation to Quaternion

```
axang = [1 0 0 pi/2];
quat = axang2quat(axang)
quat = 1\times4
    0.7071 0.7071 0
```


## Input Arguments

axang - Rotation given in axis-angle form
$n$-by-4 matrix
Rotation given in axis-angle form, specified as an $n$-by- 4 matrix of $n$ axis-angle rotations. The first three elements of every row specify the rotation axis, and the last element defines the rotation angle (in radians).

Example: [1 00 pi/2]

## Output Arguments

quat - Unit quaternion
$n$-by-4 matrix
Unit quaternion, returned as an $n$-by-4 matrix containing $n$ quaternions. Each quaternion, one per row, is of the form $q=[w \times y z]$, with $w$ as the scalar number.
Example: [0.7071 0.7071 0 0]

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

quat2axang
Introduced in R2015a

## axang2rotm

Convert axis-angle rotation to rotation matrix

## Syntax

rotm $=$ axang $2 \operatorname{rotm}(a x a n g)$

## Description

rotm $=$ axang 2 rotm (axang) converts a rotation given in axis-angle form, axang, to an orthonormal rotation matrix, rotm. When using the rotation matrix, premultiply it with the coordinates to be rotated (as opposed to postmultiplying).

## Examples

## Convert Axis-Angle Rotation to Rotation Matrix

```
axang = [0 1 0 pi/2];
rotm = axang2rotm(axang)
rotm = 3×3
\begin{tabular}{rrr}
0.0000 & 0 & 1.0000 \\
0 & 1.0000 & 0 \\
1.0000 & 0 & 0.0000
\end{tabular}
```


## Input Arguments

## axang - Rotation given in axis-angle form

$n$-by-4 matrix
Rotation given in axis-angle form, specified as an $n$-by- 4 matrix of $n$ axis-angle rotations. The first three elements of every row specify the rotation axis, and the last element defines the rotation angle (in radians).
Example: [1 00 pi/2]

## Output Arguments

## rotm - Rotation matrix

3-by-3-by-n matrix
Rotation matrix, returned as a 3-by-3-by-n matrix containing $n$ rotation matrices. Each rotation matrix has a size of 3 -by- 3 and is orthonormal. When using the rotation matrix, premultiply it with the coordinates to be rotated (as opposed to postmultiplying).
Example: [0 0 1; 010 - 100 0]

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

rotm2axang

Introduced in R2015a

## axang2tform

Convert axis-angle rotation to homogeneous transformation

## Syntax

tform = axang2tform(axang)

## Description

tform = axang2tform(axang) converts a rotation given in axis-angle form, axang, to a homogeneous transformation matrix, t form. When using the transformation matrix, premultiply it with the coordinates to be transformed (as opposed to postmultiplying).

## Examples

## Convert Axis-Angle Rotation to Homogeneous Transformation

```
axang = [1 0 0 pi/2];
tform = axang2tform(axang)
tform = 4×4
```

| 1.0000 | 0 | 0 | 0 |
| ---: | ---: | ---: | ---: |
| 0 | 0.0000 | -1.0000 | 0 |
| 0 | 1.0000 | 0.0000 | 0 |
| 0 | 0 | 0 | 1.0000 |

## Input Arguments

## axang - Rotation given in axis-angle form

$n$-by-4 matrix
Rotation given in axis-angle form, specified as an $n$-by- 4 matrix of $n$ axis-angle rotations. The first three elements of every row specify the rotation axis, and the last element defines the rotation angle (in radians).
Example: [1 00 pi/2]

## Output Arguments

## tform - Homogeneous transformation

4-by-4-by-n matrix
Homogeneous transformation matrix, specified by a 4 -by-4-by-n matrix of $n$ homogeneous transformations. When using the transformation matrix, premultiply it with the coordinates to be formed (as opposed to postmultiplying).

```
Example:[0 0 1 0; 0 1 0 0; -1 0 0 0; 0 0 0 1]
```


## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

tform2axang

Introduced in R2015a

## buildMap

Build occupancy map from lidar scans

## Syntax

map $=$ buildMap(scans,poses,mapResolution,maxRange)

## Description

map = buildMap(scans,poses,mapResolution,maxRange) creates a occupancyMap map by inserting lidar scans at the given poses. Specify the resolution of the resulting map, mapResolution, and the maximum range of the lidar sensor, maxRange.

## Examples

## Build Occupancy Map from Lidar Scans and Poses

The buildMap function takes in lidar scan readings and associated poses to build an occupancy grid as lidarScan objects and associated [x y theta] poses to build an occupancyMap.

Load scan and pose estimates collected from sensors on a robot in a parking garage. The data collected is correlated using a lidarSLAM algorithm, which performs scan matching to associate scans and adjust poses over the full robot trajectory. Check to make sure scans and poses are the same length.

```
load scansAndPoses.mat
length(scans) == length(poses)
ans = logical
    1
```

Build the map. Specify the scans and poses in the buildMap function and include the desired map resolution (10 cells per meter) and the max range of the lidar ( 19.2 meters). Each scan is added at the associated poses and probability values in the occupancy grid are updated.

```
occMap = buildMap(scans,poses,10,19.2);
figure
show(occMap)
title('Occupancy Map of Garage')
```



## Perform SLAM Using Lidar Scans

Use a lidarSLAM object to iteratively add and compare lidar scans and build an optimized pose graph of the robot trajectory. To get an occupancy map from the associated poses and scans, use the buildMap function.

## Load Data and Set Up SLAM Algorithm

Load a cell array of lidarScan objects. The lidar scans were collected in a parking garage on a Husky ${ }_{\circledR}$ robot from ClearPath Robotics $®$. Typically, lidar scans are taken at a high frequency and each scan is not needed for SLAM. Therefore, down sample the scans by selecting only every 40th scan.

```
load garage_fl1_southend.mat scans
scans = scans(1:40:end);
```

To set up the SLAM algorithm, specify the lidar range, map resolution, loop closure threshold, and search radius. Tune these parameters for your specific robot and environment. Create the lidarSLAM object with these parameters.

```
maxRange = 19.2; % meters
resolution = 10; % cells per meter
slamObj = lidarSLAM(resolution,maxRange);
slamObj.LoopClosureThreshold = 360;
slam0bj.LoopClosureSearchRadius = 8;
```


## Add Scans Iteratively

Using a for loop, add scans to the SLAM object. The object uses scan matching to compare each added scan to previously added ones. To improve the map, the object optimizes the pose graph whenever it detects a loop closure. Every 10 scans, display the stored poses and scans.

```
for i = 1:numel(scans)
    addScan(slamObj,scans{i});
    if rem(i,10) == 0
        show(slamObj);
    end
end
```



## View Occupancy Map

After adding all the scans to the SLAM object, build an occupancyMap map by calling buildMap with the scans and poses. Use the same map resolution and max range you used with the SLAM object.

```
[scansSLAM,poses] = scansAndPoses(slamObj);
occMap = buildMap(scansSLAM,poses,resolution,maxRange);
figure
show(occMap)
title('Occupancy Map of Garage')
```



## Input Arguments

## scans - Lidar scans

cell array of lidarScan objects
Lidar scans used to build the map, specified as a cell array of lidarScan objects.

## poses - Poses of lidar scans

n-by-3 matrix
Poses of lidar scans, specified as an $n$-by-3 matrix. Each row is an [ $x$ y theta] vector representing the $x y$-position and orientation angle of a scan.

## mapResolution - Resolution of occupancy grid <br> positive integer

Resolution of the output occupancyMap map, specified as a positive integer in cells per meter.

## maxRange - Maximum range of lidar sensor

positive scalar
Maximum range of lidar sensor, specified as a positive scalar in meters. Points in the scans outside this range are ignored.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . , NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: ['MapWidth',10]

## MapWidth - Width of occupancy grid

positive scalar
Width of the occupancy grid, specified as the comma-separated pair consisting of 'MapWidth' and a positive scalar. If this value is not specified, the map is automatically scaled to fit all laser scans.

## MapHeight - Height of occupancy grid

positive scalar
Height of occupancy grid, specified as the comma-separated pair consisting of 'MapHeight ' and a positive scalar. If this value is not specified, the map is automatically scaled to fit all laser scans.

## Output Arguments

## map - Occupancy Map

occupancyMap object
Occupancy map, returned as a occupancyMap object.

## See Also

## Functions

matchScans|matchScansGrid|lidarScan|transformScan

## Classes

lidarSLAM | occupancyMap

## Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
"Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

## Introduced in R2019b

## cart2hom

Convert Cartesian coordinates to homogeneous coordinates

## Syntax

hom $=$ cart2hom(cart)

## Description

hom = cart2hom (cart) converts a set of points in Cartesian coordinates to homogeneous coordinates.

## Examples

## Convert 3-D Cartesian Points to Homogeneous Coordinates

```
\(c=[0.81470 .12700 .6324 ; 0.90580 .91340 .0975] ;\)
```

h = cart2hom(c)
$h=2 \times 4$

| 0.8147 | 0.1270 | 0.6324 | 1.0000 |
| :--- | :--- | :--- | :--- |
| 0.9058 | 0.9134 | 0.0975 | 1.0000 |

## Input Arguments

## cart - Cartesian coordinates

$n$-by-(k-1) matrix
Cartesian coordinates, specified as an $n$-by-( $k-1$ ) matrix, containing $n$ points. Each row of cart represents a point in ( $k-1$ )-dimensional space. $k$ must be greater than or equal to 2 .
Example: [0.8147 0.1270 0.6324; 0.9058 0.9134 0.0975]

## Output Arguments

## hom - Homogeneous points

n-by-k matrix
Homogeneous points, returned as an $n$-by-k matrix, containing $n$ points. $k$ must be greater than or equal to 2.
Example:[0.2785 0.9575 0.1576 0.5; 0.5469 0.9649 0.9706 0.5]

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

hom2cart

Introduced in R2015a

## connect

Connect poses for given connection type

## Syntax

```
[pathSegments,pathCosts] = connect(connectionObj,start,goal)
[pathSegments,pathCosts] = connect(connectionObj,start,
goal,'PathSegments','all')
```


## Description

[pathSegments,pathCosts] = connect(connectionObj,start,goal) connects the start and goal poses using the specified dubinsConnection object. The path segment object with the lowest cost is returned.
[pathSegments,pathCosts] = connect(connectionObj,start, goal,'PathSegments', 'all') returns all possible path segments as a cell array with their associated costs.

## Examples

## Connect Poses Using Dubins Connection Path

Create a dubinsConnection object.
dubConnObj = dubinsConnection;
Define start and goal poses as [x y theta] vectors.

```
startPose = [0 0 0];
goalPose = [1 1 pi];
```

Calculate a valid path segment to connect the poses.

```
[pathSegObj, pathCosts] = connect(dubConnObj,startPose,goalPose);
```

Show the generated path.

```
show(pathSegObj{1})
```



## Connect Poses Using ReedsShepp Connection Path

Create a reedsSheppConnection object.
reedsConnObj $=$ reedsSheppConnection;
Define start and goal poses as [x y theta] vectors.

```
startPose = [0 0 0];
```

goalPose = [1 1 pi];

Calculate a valid path segment to connect the poses.
[pathSeg0bj,pathCosts] = connect(reedsConnObj,startPose,goalPose);
Show the generated path.
show(pathSeg0bj\{1\})


## Input Arguments

connection0bj - Path connection type
dubinsPathSegment object| reedsSheppPathSegment object
Path connection type, specified as a dubinsConnection or reedsSheppConnection object. This object defines the parameters of the connection, including the minimum turning radius of the robot and the valid motion types.

## start - Initial pose of robot

$[x, y, \Theta]$ vector or matrix
This property is read-only.
Initial pose of the robot at the start of the path segment, specified as an $[x, y, \Theta]$ vector or matrix. Each row of the matrix corresponds to a different start pose.
$x$ and $y$ are in meters. $\Theta$ is in radians.
The connect function supports:

- Singular start pose with singular goal pose.
- Multiple start pose with singular goal pose.
- Singular start pose with multiple goal pose.
- Multiple start pose with multiple goal pose.

The output pathSegments cell array size reflects the singular or multiple pose options.

## goal - Goal pose of robot

$[x, y, \Theta]$ vector or matrix
This property is read-only.
Goal pose of the robot at the end of the path segment, specified as an $[x, y, \Theta]$ vector or matrix. Each row of the matrix corresponds to a different goal pose.
$x$ and $y$ are in meters. $\Theta$ is in radians.
The connect function supports:

- Singular start pose with singular goal pose.
- Multiple start pose with singular goal pose.
- Singular start pose with multiple goal pose.
- Multiple start pose with multiple goal pose.

The output pathSegments cell array size reflects the singular or multiple pose options.

## Output Arguments

## pathSegments - Path segments

cell array of objects
Path segments, specified as a cell array of objects. The type of object depends on the input connection0bj. The size of the cell array depends on whether you use singular or multiple start and goal poses. By default, the function returns the path with the lowest cost for each start and goal pose. When call connect using the 'PathSegments', 'all' name-value pair, the cell array contains all valid path segments between the specified start and goal poses.

## pathCosts - Cost of path segment

positive numeric scalar | positive numeric vector | positive numeric matrix
Cost of path segments, specified as a positive numeric scalar, vector, or matrix. Each element of the cost vector or matrix corresponds to a path segment in pathSegment. By default, the function returns the path with the lowest cost for each start and goal pose.

Example: [7.6484, 7.5122]

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® $\mathrm{Coder}^{\mathrm{TM}}$.

## See Also

## Functions

interpolate|show

```
Objects
dubinsConnection| dubinsPathSegment | reedsSheppConnection|
reedsSheppPathSegment
Introduced in R2019b
```


## createPlanningTemplate

Create sample implementation for path planning interface

## Syntax

createPlanningTemplate
createPlanningTemplate("StateValidator")

## Description

createPlanningTemplate creates a planning template for a subclass of the nav.StateSpace class. The function opens a file in the MATLAB ${ }^{\circledR}$ Editor. Save your custom implementation and ensure the file is available on the MATLAB path. Alternative syntax:
createPlanningTemplate("StateSpace")
createPlanningTemplate("StateValidator") creates a template for a subclass of the nav. StateValidator class.

## Examples

## Create Custom State Space for Path Planning

This example shows how to use the createPlanningTemplate function to generate a template for customizing your own state space definition and sampler to use with path planning algorithms. A simple implementation is provided with the template.

Call the create template function. This function generates a class definition file for you to modify for your own implementation.
createPlanningTemplate

## Class and Property Definition

The first part of the template specifies the class definition and any properties for the class. Derive from the nav.StateSpace class. For this example, create a property for the uniform and normal distributions. You can specify any additional user-defined properties here.

```
classdef MyCustomStateSpace < nav.StateSpace & ...
    matlabshared.planning.internal.EnforceScalarHandle
    properties
        UniformDistribution
        NormalDistribution
    % Specify additional properties here
end
```

Save your custom state space class and ensure your file name matches the class name.

## Class Constructor

Use the constructor to set the name of the state space, the number of state variables, and define its boundaries. Alternatively, you can add input arguments to the function and pass the variables in when you create an object.

- For each state variable, define the [min max] values for the state bounds.
- Call the constructor of the base class.
- For this example, you specify the normal and uniform distribution property values using predefined NormalDistribution and UniformDistribution classes.
- Specify any other user-defined property values here.
methods
function obj = MyCustomStateSpace
spaceName = "MyCustomStateSpace"; numStateVariables = 3; stateBounds = [-100 100; \% [min max] -100 100;
-100 100];
obj@nav.StateSpace(spaceName, numStateVariables, stateBounds);
obj.NormalDistribution = matlabshared.tracking.internal.NormalDistribution(numStateVarial obj.UniformDistribution = matlabshared.tracking.internal.UniformDistribution(numStateVar: \% User-defined property values here
end


## Copy Semantics

Specify the copy method definition. Copy all the values of your user-defined variables into a new object, so copyObj is a deep copy. The default behavior given in this example creates a new copy of the object with the same name, state bounds, and distributions.

```
function copyObj = copy(obj)
    copy0bj = feval(class(obj));
    copyObj.StateBounds = obj.StateBounds;
    copyObj.UniformDistribution = obj.UniformDistribution.copy;
    copyObj.NormalDistribution = obj.NormalDistribution.copy;
end
```


## Enforce State Bounds

Specify how to ensure states are always within the state bounds. For this example, the state values
get saturated at the minimum or maximum values for the state bounds.

```
function boundedState = enforceStateBounds(obj, state)
    nav.internal.validation.validateStateMatrix(state, nan, obj.NumStateVariables, "enforceState
    boundedState = state;
    boundedState = min(max(boundedState, obj.StateBounds(:,1)'), ...
        obj.StateBounds(:,2)');
end
```


## Sample Uniformly

Specify the behavior for sampling across a uniform distribution. support multiple syntaxes to constrain the uniform distribution to a nearby state within a certain distance and sample multiple states.

```
STATE = sampleUniform(OBJ)
STATE = sampleUniform(OBJ,NUMSAMPLES)
STATE = sampleUniform(OBJ,NEARSTATE,DIST)
STATE = sampleUniform(OBJ,NEARSTATE,DIST,NUMSAMPLES)
```

For this example, use a validation function to process a varargin input that handles the varying input arguments.

```
function state = sampleUniform(obj, varargin)
    narginchk(1,4);
    [numSamples, stateBounds] = obj.validateSampleUniformInput(varargin{:});
    obj.UniformDistribution.RandomVariableLimits = stateBounds;
    state = obj.UniformDistribution.sample(numSamples);
end
```


## Sample from Gaussian Distribution

Specify the behavior for sampling across a Gaussian distribution. Support multiple syntaxes for sampling a single state or multiple states.

```
STATE = sampleGaussian(OBJ, MEANSTATE, STDDEV)
STATE = sampleGaussian(OBJ, MEANSTATE, STDDEV, NUMSAMPLES)
```

function state $=$ sampleGaussian(obj, meanState, stdDev, varargin)
narginchk $(3,4)$;
[meanState, stdDev, numSamples] = obj.validateSampleGaussianInput(meanState, stdDev, varargi
obj.NormalDistribution.Mean = meanState;
obj.NormalDistribution.Covariance = diag(stdDev.^2);
state = obj.NormalDistribution.sample(numSamples);
state $=$ obj.enforceStateBounds(state);
end

## Interpolate Between States

Define how to interpolate between two states in your state space. Use an input, fraction, to determine how to sample along the path between two states. For this example, define a basic linear interpolation method using the difference between states.

```
function interpState = interpolate(obj, state1, state2, fraction)
    narginchk(4,4);
    [state1, state2, fraction] = obj.validateInterpolateInput(state1, state2, fraction);
    stateDiff = state2 - state1;
    interpState = statel + fraction' * stateDiff;
end
```


## Calculate Distance Between States

Specify how to calculate the distance between two states in your state space. Use the state1 and state 2 inputs to define the start and end positions. Both inputs can be a single state (row vector) or multiple states (matrix of row vectors). For this example, calculate the distance based on the Euclidean distance between each pair of state positions.

```
function dist = distance(obj, state1, state2)
```

    narginchk(3,3);
    nav.internal.validation.validateStateMatrix(state1, nan, obj.NumStateVariables, "distance",
    nav.internal.validation.validateStateMatrix(state2, size(state1,1), obj.NumStateVariables,
    stateDiff = bsxfun(@minus, state2, state1);
    dist = sqrt( sum( stateDiff.^2, 2 ) );
    end

Terminate the methods and class sections.
end
end
Save your state space class definition. You can now use the class constructor to create an object for your state space.

## Create Custom State Space Validator for Path Planning

This example shows how to use the createPlanningTemplate function to generate a template for customizing your own state validation class. State validation is used with path planning algorithms to ensure valid paths. The template function provides a basic implementation for example purposes.

Call the create template function. This function generates a class definition file for you to modify for your own implementation. Save this file.
createPlanningTemplate("StateValidator")

## Class and Property Definition

The first part of the template specifies the class definition and any properties for the class. Derive from the nav. StateValidator class. You can specify any additional user-defined properties here.

```
classdef MyCustomStateValidator < nav.StateValidator & ...
    matlabshared.planning.internal.EnforceScalarHandle
    properties
    % User-defined properties
    end
```

Save your custom state validator class and ensure your file name matches the class name.

## Class Constructor

Use the constructor to set the name of the state space validator and specify the state space object. Set a default value for the state space if one is not provided. Call the constructor of the base class. Initialize any other user-defined properties. This example uses a default of MyCustomStateSpace, which was illustrated in the previous example.

```
methods
```

```
function obj = MyCustomStateValidator(space)
    narginchk(0,1)
    if nargin == 0
        space = MyCustomStateSpace;
    end
    obj@nav.StateValidator(space);
    % Initialize user-defined properties
end
```


## Copy Semantics

Specify the copy method definition. Copy all the values of your user-defined variables into a new object, so copy0bj is a deep copy. The default behavior given in this example creates a new copy of the object with the same type.

```
function copyObj = copy(obj)
    copy0bj = feval(class(obj), obj.StateSpace);
end
```


## Check State Validity

Define how a given state is validated. The state input can either be a single row vector, or a matrix of row vectors for multiple states. Customize this function for any special validation behavior for your state space like collision checking against obstacles.

```
function isValid = isStateValid(obj, state)
    narginchk(2,2);
    nav.internal.validation.validateStateMatrix(state, nan, obj.StateSpace.NumStateVaria
        "isStateValid", "state");
    bounds = obj.StateSpace.StateBounds';
    inBounds = state >= bounds(1,:) & state <= bounds(2,:);
    isValid = all(inBounds, 2);
end
```


## Check Motion Validity

Define how to generate the motion between states and determine if it is valid. For this example, use linspace to evenly interpolate between states and check if these states are valid using isStateValid. Customize this function to sample between states or consider other analytical methods for determining if a vehicle can move between given states.

```
function [isValid, lastValid] = isMotionValid(obj, state1, state2)
    narginchk(3,3);
    statel = nav.internal.validation.validateStateVector(state1, ...
        obj.StateSpace.NumStateVariables, "isMotionValid", "state1");
    state2 = nav.internal.validation.validateStateVector(state2, ...
            obj.StateSpace.NumStateVariables, "isMotionValid", "state2");
    if (~obj.isStateValid(statel))
        error("statevalidator:StartStateInvalid", "The start state of the motion is inva
    end
```

```
    % Interpolate at a fixed interval between states and check state validity
    numInterpPoints = 100;
    interpStates = obj.StateSpace.interpolate(state1, state2, linspace(0,1,numInterpPoin
    interpValid = obj.isStateValid(interpStates);
    % Look for invalid states. Set lastValid state to index-1.
    firstInvalidIdx = find(~interpValid, 1);
    if isempty(firstInvalidIdx)
        isValid = true;
        lastValid = state2;
else
    isValid = false;
    lastValid = interpStates(firstInvalidIdx-1,:);
end
end
Terminate the methods and class sections.
```

end
end
Save your state space validator class definition. You can now use the class constructor to create an object for validation of states for a given state space.

## See Also

nav.StateSpace|nav.StateValidator| stateSpaceSE2| validator0ccupancyMap
Introduced in R2019b

## ecompass

Orientation from magnetometer and accelerometer readings

## Syntax

orientation = ecompass(accelerometerReading, magnetometerReading) orientation = ecompass(accelerometerReading,magnetometerReading, orientationFormat)
orientation = ecompass(accelerometerReading,magnetometerReading, orientationFormat,'ReferenceFrame', RF)

## Description

orientation = ecompass(accelerometerReading,magnetometerReading) returns a quaternion that can rotate quantities from a parent (NED) frame to a child (sensor) frame.
orientation = ecompass(accelerometerReading,magnetometerReading, orientationFormat) specifies the orientation format as quaternion or rotation matrix.
orientation = ecompass(accelerometerReading,magnetometerReading, orientationFormat, 'ReferenceFrame' , RF) also allows you to specify the reference frame RF of the orientation output. Specify RF as 'NED ' (North-East-Down) or 'ENU' (East-North-Up). The default value is 'NED'.

## Examples

## Determine Declination of Boston

Use the known magnetic field strength and proper acceleration of a device pointed true north in Boston to determine the magnetic declination of Boston.

Define the known acceleration and magnetic field strength in Boston.

```
magneticFieldStrength = [19.535 -5.109 47.930];
properAcceleration = [0 0 9.8];
```

Pass the magnetic field strength and acceleration to the ecompass function. The ecompass function returns a quaternion rotation operator. Convert the quaternion to Euler angles in degrees.

```
q = ecompass(properAcceleration,magneticFieldStrength);
e = eulerd(q,'ZYX','frame');
```

The angle, e, represents the angle between true north and magnetic north in Boston. By convention, magnetic declination is negative when magnetic north is west of true north. Negate the angle to determine the magnetic declination.

```
magneticDeclination0fBoston = -e(1)
magneticDeclination0fBoston = -14.6563
```


## Return Rotation Matrix

The ecompass function fuses magnetometer and accelerometer data to return a quaternion that, when used within a quaternion rotation operator, can rotate quantities from a parent (NED) frame to a child frame. The ecompass function can also return rotation matrices that perform equivalent rotations as the quaternion operator.

Define a rotation that can take a parent frame pointing to magnetic north to a child frame pointing to geographic north. Define the rotation as both a quaternion and a rotation matrix. Then, convert the quaternion and rotation matrix to Euler angles in degrees for comparison.

Define the magnetic field strength in microteslas in Boston, MA, when pointed true north.

```
m = [19.535 -5.109 47.930];
a = [0 0 9.8];
```

Determine the quaternion and rotation matrix that is capable of rotating a frame from magnetic north to true north. Display the results for comparison.

```
q = ecompass(a,m);
quaterionEulerAngles = eulerd(q,'ZYX','frame')
quaterionEulerAngles = 1\times3
    14.6563 0 0
r = ecompass(a,m,'rotmat');
theta = -asin(r(1,3));
psi = atan2(r(2,3)/cos(theta),r(3,3)/cos(theta));
rho = atan2(r(1,2)/cos(theta),r(1,1)/cos(theta));
rotmatEulerAngles = rad2deg([rho,theta,psi])
rotmatEulerAngles = 1\times3
    14.6563 0 0
```


## Determine Gravity Vector

Use ecompass to determine the gravity vector based on data from a rotating IMU.
Load the inertial measurement unit (IMU) data.
load 'rpy_9axis.mat' sensorData Fs
Determine the orientation of the sensor body relative to the local NED frame over time.
orientation = ecompass(sensorData.Acceleration,sensorData.MagneticField);
To estimate the gravity vector, first rotate the accelerometer readings from the sensor body frame to the NED frame using the orientation quaternion vector.

```
gravityVectors = rotatepoint(orientation,sensorData.Acceleration);
```

Determine the gravity vector as an average of the recovered gravity vectors over time.

```
gravityVectorEstimate = mean(gravityVectors,1)
gravityVectorEstimate = 1×3
    0.0000 -0.0000 10.2102
```


## Track Spinning Platform

Fuse modeled accelerometer and gyroscope data to track a spinning platform using both idealized and realistic data.

## Generate Ground-Truth Trajectory

Describe the ground-truth orientation of the platform over time. Use the kinematicTrajectory System object ${ }^{\mathrm{TM}}$ to create a trajectory for a platform that has no translation and spins about its $z$-axis.

```
duration = 12;
fs = 100;
numSamples = fs*duration;
```

accelerationBody $=$ zeros(numSamples,3);
angularVelocityBody = zeros(numSamples,3);

angularVelocityBody(:,3) = zAxisAngularVelocity;
trajectory $=$ kinematicTrajectory('SampleRate',fs);
[~,orientationNED,~,accelerationNED, angularVelocityNED] = trajectory(accelerationBody,angularVel

## Model Receiving IMU Data

Use an imuSensor System object to mimic data received from an IMU that contains an ideal magnetometer and an ideal accelerometer.

```
IMU = imuSensor('accel-mag','SampleRate',fs);
[accelerometerData,magnetometerData] = IMU(accelerationNED, ...
    angularVelocityNED, ...
    orientationNED);
```


## Fuse IMU Data to Estimate Orientation

Pass the accelerometer data and magnetometer data to the ecompass function to estimate orientation over time. Convert the orientation to Euler angles in degrees and plot the result.

```
orientation = ecompass(accelerometerData,magnetometerData);
orientationEuler = eulerd(orientation,'ZYX','frame');
timeVector = (0:numSamples-1).'/fs;
figure(1)
```

plot(timeVector,orientationEuler)
legend('z-axis','y-axis','x-axis')
xlabel('Time (s)')
ylabel('Rotation (degrees)')
title('Orientation from Ideal IMU')


## Repeat Experiment with Realistic IMU Sensor Model

Modify parameters of the IMU System object to approximate realistic IMU sensor data. Reset the IMU and then call it with the same ground-truth acceleration, angular velocity, and orientation. Use ecompass to fuse the IMU data and plot the results.

```
IMU.Accelerometer = accelparams( ...
    'MeasurementRange',20, ...
    'Resolution',0.0006, ...
    'ConstantBias',0.5, ...
    'AxesMisalignment',2, ...
    'NoiseDensity',0.004, ...
    'BiasInstability',0.5);
IMU.Magnetometer = magparams( ...
    'MeasurementRange',200, ...
    'Resolution',0.01);
reset(IMU)
[accelerometerData,magnetometerData] = IMU(accelerationNED,angularVelocityNED,orientationNED);
orientation = ecompass(accelerometerData,magnetometerData);
orientationEuler = eulerd(orientation,'ZYX','frame');
```

```
figure(2)
plot(timeVector,orientationEuler)
legend('z-axis','y-axis','x-axis')
xlabel('Time (s)')
ylabel('Rotation (degrees)')
title('Orientation from Realistic IMU')
```



## Input Arguments

## accelerometerReading - Accelerometer readings in sensor body coordinate system ( $\mathbf{m} / \mathbf{s}^{2}$ )

N -by-3 matrix
Accelerometer readings in sensor body coordinate system in $\mathrm{m} / \mathrm{s}^{2}$, specified as an N -by- 3 matrix. The columns of the matrix correspond to the $x-, y$-, and $z$-axes of the sensor body. The rows in the matrix, $N$, correspond to individual samples. The accelerometer readings are normalized before use in the function.

Data Types: single | double

## magnetometerReading - Magnetometer readings in sensor body coordinate system ( $\mu \mathrm{T}$ )

 $N$-by-3 matrixMagnetometer readings in sensor body coordinate system in $\mu \mathrm{T}$, specified as an $N$-by- 3 matrix. The columns of the matrix correspond to the $x$-, $y$-, and $z$-axes of the sensor body. The rows in the matrix, $N$, correspond to individual samples. The magnetometer readings are normalized before use in the function.

Data Types: single | double
orientationFormat - Format used to describe orientation
'quaternion' (default)|'rotmat'
Format used to describe orientation, specified as 'quaternion' or 'rotmat'.
Data Types: char|string

## Output Arguments

## orientation - Orientation that rotates quantities from global coordinate system to sensor body coordinate system

$N$-by-1 vector of quaternions (default) | 3 -by-3-by- $N$ array
Orientation that can rotate quantities from a global coordinate system to a body coordinate system, returned as a vector of quaternions or an array. The size and type of the orientation depends on the format used to describe orientation:

- 'quaternion' -- $N$-by-1 vector of quaternions with the same underlying data type as the input
- ' rotmat ' -- 3-by-3-by- $N$ array the same data type as the input

Data Types: quaternion | single | double

## Algorithms

The ecompass function returns a quaternion or rotation matrix that can rotate quantities from a parent (NED for example) frame to a child (sensor) frame. For both output orientation formats, the rotation operator is determined by computing the rotation matrix.

The rotation matrix is first calculated with an intermediary:

$$
R=[(a \times m) \times a a \times m a]
$$

and then normalized column-wise. $a$ and $m$ are the accelerometerReading input and the magnetometerReading input, respectively.

To understand the rotation matrix calculation, consider an arbitrary point on the Earth and its corresponding local NED frame. Assume a sensor body frame, $[x, y, z]$, with the same origin.


Recall that orientation of a sensor body is defined as the rotation operator (rotation matrix or quaternion) required to rotate a quantity from a parent (NED) frame to a child (sensor body) frame:

$$
[R]\left[p_{\text {parent }}\right]=\left[p_{\text {child }}\right]
$$

where

- $R$ is a 3-by-3 rotation matrix, which can be interpreted as the orientation of the child frame.
- $p_{\text {parent }}$ is a 3 -by- 1 vector in the parent frame.
- $p_{\text {child }}$ is a 3-by-1 vector in the child frame.

For a stable sensor body, an accelerometer returns the acceleration due to gravity. If the sensor body is perfectly aligned with the NED coordinate system, all acceleration due to gravity is along the $z$ axis, and the accelerometer reads $\left[\begin{array}{lll}0 & 1\end{array}\right]$. Consider the rotation matrix required to rotate a quantity from the NED coordinate system to a quantity indicated by the accelerometer.


$$
\left[\begin{array}{lll}
r_{11} & r_{21} & r_{31} \\
r_{12} & r_{22} & r_{32} \\
r_{13} & r_{23} & r_{33}
\end{array}\right]\left[\begin{array}{l}
0 \\
0 \\
1
\end{array}\right]=\left[\begin{array}{l}
a_{1} \\
a_{2} \\
a_{3}
\end{array}\right]
$$

The third column of the rotation matrix corresponds to the accelerometer reading:

$$
\left[\begin{array}{l}
r_{31} \\
r_{32} \\
r_{33}
\end{array}\right]=\left[\begin{array}{l}
a_{1} \\
a_{2} \\
a_{3}
\end{array}\right]
$$

A magnetometer reading points toward magnetic north and is in the $N-D$ plane. Again, consider a sensor body frame aligned with the NED coordinate system.


By definition, the $E$-axis is perpendicular to the $N$ - $D$ plane, therefore $N \times D=E$, within some amplitude scaling. If the sensor body frame is aligned with NED, both the acceleration vector from the accelerometer and the magnetic field vector from the magnetometer lie in the $N-D$ plane. Therefore $m \times a=y$, again with some amplitude scaling.

Consider the rotation matrix required to rotate NED to the child frame, $[x y z]$.


$$
\left[\begin{array}{lll}
r_{11} & r_{21} & r_{31} \\
r_{12} & r_{22} & r_{32} \\
r_{13} & r_{23} & r_{33}
\end{array}\right]\left[\begin{array}{l}
0 \\
1 \\
0
\end{array}\right]=\left[\begin{array}{l}
a_{1} \\
a_{2} \\
a_{3}
\end{array}\right] \times\left[\begin{array}{l}
m_{1} \\
m_{2} \\
m_{3}
\end{array}\right]
$$

The second column of the rotation matrix corresponds to the cross product of the accelerometer reading and the magnetometer reading:

$$
\left[\begin{array}{l}
r_{21} \\
r_{22} \\
r_{23}
\end{array}\right]=\left[\begin{array}{l}
a_{1} \\
a_{2} \\
a_{3}
\end{array}\right] \times\left[\begin{array}{l}
m_{1} \\
m_{2} \\
m_{3}
\end{array}\right]
$$

By definition of a rotation matrix, column 1 is the cross product of columns 2 and 3:

$$
\begin{aligned}
{\left[\begin{array}{l}
r_{11} \\
r_{12} \\
r_{13}
\end{array}\right] } & =\left[\begin{array}{l}
r_{21} \\
r_{22} \\
r_{23}
\end{array}\right] \times\left[\begin{array}{l}
r_{31} \\
r_{32} \\
r_{33}
\end{array}\right] \\
& =(a \times m) \times a
\end{aligned}
$$

Finally, the rotation matrix is normalized column-wise:

$$
R_{i j}=\frac{R_{i j}}{\sqrt{\sum_{i=1}^{3} R_{i j}^{2}}}, \forall j
$$

Note The ecompass algorithm uses magnetic north, not true north, for the NED coordinate system.

## References

[1] Open Source Sensor Fusion. https://github.com/memsindustrygroup/Open-Source-Sensor-Fusion/ tree/master/docs

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

ahrsfilter|imufilter
Introduced in R2018b

## enu2lla

Transform local east-north-up coordinates to geodetic coordinates

## Syntax

lla = enu2lla(xyzENU,lla0,method)

## Description

lla = enu2lla(xyzENU, lla0, method) transforms the local east-north-up (ENU) Cartesian coordinates xyzENU to geodetic coordinates lla. Specify the origin of the local ENU system as the geodetic coordinates lla0.

## Note

- The latitude and longitude values in the geodetic coordinate system use the World Geodetic System of 1984 (WGS84) standard.
- Specify altitude as height in meters above the WGS84 reference ellipsoid.


## Examples

## Transform ENU Coordinates to Geodetic Coordinates

Specify the geodetic coordinates of the local origin in Zermatt, Switzerland.
lla0 = [46.017 7.750 1673]; \% [lat0 lon0 alt0]
Specify the ENU coordinates of a point of interest, in meters. In this case, the point of interest is the Matterhorn.

```
xyzENU = [-7134.8 -4556.3 2852.4]; % [xEast yNorth zUp]
```

Transform the local ENU coordinates to geodetic coordinates using flat earth approximation.

```
lla = enu2lla(xyzENU,lla0,'flat')
lla = 1\times3
103 }
    0.0460 0.0077 4.5254
```


## Input Arguments

xyzENU - Local ENU Cartesian coordinates
three-element row vector | $n$-by-3 matrix

Local ENU Cartesian coordinates, specified as a three-element row vector or an $n$-by- 3 matrix. $n$ is the number of points to transform. Specify each point in the form [xEast yNorth $z U p$ ]. xEast, yNorth, and $z U p$ are the respective $x$-, $y$-, and $z$-coordinates, in meters, of the point in the local ENU system.
Data Types: double
lla0 - Origin of local ENU system in geodetic coordinates
three-element row vector | $n$-by-3 matrix
Origin of the local ENU system in the geodetic coordinates, specified as a three-element row vector or an $n$-by-3 matrix. $n$ is the number of origin points. Specify each point in the form [ lat0 lon0 alt0]. lat0 and lon0 specify the latitude and longitude of the origin, respectively, in degrees. alt0 specifies the altitude of the origin in meters.
Data Types: double
method - Transformation method
'flat'|'ellipsoid'
Transformation method, specified as 'flat' or 'ellipsoid'. This argument specifies whether the function assumes the planet is flat or ellipsoidal.

The flat Earth transformation method has these limitations:

- Assumes that the flight path and bank angle are zero.
- Assumes that the flat Earth $z$-axis is normal to the Earth at only the initial geodetic latitude and longitude. This method has higher accuracy over small distances from the initial geodetic latitude and longitude, and closer to the equator. The method calculates a longitude with higher accuracy when the variation in latitude is smaller.
- Latitude values of +90 and -90 may return unexpected values because of singularity at the poles.

Data Types: char|string

## Output Arguments

## lla - Geodetic coordinates

three-element row vector | $n$-by-3 matrix
Geodetic coordinates, returned as a three-element row vector or an $n$-by- 3 matrix. $n$ is the number of transformed points. Each point is in the form [lat lon alt]. lat and lon specify the latitude and longitude, respectively, in degrees. alt specifies the altitude in meters.
Data Types: double

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

Functions
lla2enu|lla2ned|ned2lla

Introduced in R2021a

## eul2quat

Convert Euler angles to quaternion

## Syntax

```
quat = eul2quat(eul)
quat = eul2quat(eul,sequence)
```


## Description

quat = eul2quat (eul) converts a given set of Euler angles, eul, to the corresponding quaternion, quat. The default order for Euler angle rotations is "ZYX".
quat $=$ eul2quat (eul, sequence) converts a set of Euler angles into a quaternion. The Euler angles are specified in the axis rotation sequence, sequence. The default order for Euler angle rotations is " ZYX ".

## Examples

## Convert Euler Angles to Quaternion

```
eul = [0 pi/2 0];
qZYX = eul2quat(eul)
qZYX = 1×4
```

$\begin{array}{llll}0.7071 & 0 & 0.7071 & 0\end{array}$

```
Convert Euler Angles to Quaternion Using Default ZYZ Axis Order
eul = [pi/2 0 0];
qZYZ = eul2quat(eul,'ZYZ')
qZYZ = 1×4
    0.7071 0 0 0.7071
```


## Input Arguments

## eul - Euler rotation angles

$n$-by-3 matrix
Euler rotation angles in radians, specified as an $n$-by- 3 array of Euler rotation angles. Each row represents one Euler angle set.

Example: [0 0 1.5708]

## sequence - Axis rotation sequence

"ZYX" (default) | "ZYZ" | "XYZ"
Axis rotation sequence for the Euler angles, specified as one of these string scalars:

- "ZYX" (default) - The order of rotation angles is $z$-axis, $y$-axis, $x$-axis.
- "ZYZ" - The order of rotation angles is $z$-axis, $y$-axis, $z$-axis.
- "XYZ" - The order of rotation angles is $x$-axis, $y$-axis, $z$-axis.

Data Types: string | char

## Output Arguments

quat - Unit quaternion
$n$-by-4 matrix
Unit quaternion, returned as an $n$-by-4 matrix containing $n$ quaternions. Each quaternion, one per row, is of the form $q=[w x y z]$, with $w$ as the scalar number.
Example: [0.7071 0.7071 0 0]

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

quat2eul | quaternion
Introduced in R2015a

## eul2rotm

Convert Euler angles to rotation matrix

## Syntax

```
rotm = eul2rotm(eul)
rotm = eul2rotm(eul,sequence)
```


## Description

rotm $=$ eul2rotm (eul) converts a set of Euler angles, eul, to the corresponding rotation matrix, rotm. When using the rotation matrix, premultiply it with the coordinates to be rotated (as opposed to postmultiplying). The default order for Euler angle rotations is "ZYX".
rotm $=$ eul2rotm(eul, sequence) converts Euler angles to a rotation matrix, rotm. The Euler angles are specified in the axis rotation sequence, sequence. The default order for Euler angle rotations is " ZYX ".

## Examples

## Convert Euler Angles to Rotation Matrix

```
eul = [0 pi/2 0];
rotmZYX = eul2rotm(eul)
rotmZYX = 3\times3
\begin{tabular}{rrr}
0.0000 & 0 & 1.0000 \\
0 & 1.0000 & 0 \\
-1.0000 & 0 & 0.0000
\end{tabular}
```


## Convert Euler Angles to Rotation Matrix Using ZYZ Axis Order

```
eul = [0 pi/2 pi/2];
rotmZYZ = eul2rotm(eul,'ZYZ')
rotmZYZ = 3\times3
\begin{tabular}{rrr}
0.0000 & -0.0000 & 1.0000 \\
1.0000 & 0.0000 & 0 \\
0.0000 & 1.0000 & 0.0000
\end{tabular}
```


## Input Arguments

## eul - Euler rotation angles

n-by-3 matrix
Euler rotation angles in radians, specified as an $n$-by- 3 array of Euler rotation angles. Each row represents one Euler angle set.
Example: [0 0 1.5708]

## sequence - Axis rotation sequence

"ZYX" (default) | "ZYZ" | "XYZ"
Axis rotation sequence for the Euler angles, specified as one of these string scalars:

- "ZYX" (default) - The order of rotation angles is $z$-axis, $y$-axis, $x$-axis.
- "ZYZ" - The order of rotation angles is $z$-axis, $y$-axis, $z$-axis.
- "XYZ" - The order of rotation angles is $x$-axis, $y$-axis, $z$-axis.

Data Types: string | char

## Output Arguments

## rotm - Rotation matrix

3-by-3-by-n matrix
Rotation matrix, returned as a 3-by-3-by-n matrix containing $n$ rotation matrices. Each rotation matrix has a size of 3 -by- 3 and is orthonormal. When using the rotation matrix, premultiply it with the coordinates to be rotated (as opposed to postmultiplying).
Example: [0 0 1; 01 0; -1 0 0]

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

rotm2eul

## Introduced in R2015a

## eul2tform

Convert Euler angles to homogeneous transformation

## Syntax

```
eul = eul2tform(eul)
tform = eul2tform(eul,sequence)
```


## Description

eul = eul2tform(eul) converts a set of Euler angles, eul, into a homogeneous transformation matrix, tform. When using the transformation matrix, premultiply it with the coordinates to be transformed (as opposed to postmultiplying). The default order for Euler angle rotations is "ZYX".
tform = eul2tform(eul, sequence) converts Euler angles to a homogeneous transformation. The Euler angles are specified in the axis rotation sequence, sequence. The default order for Euler angle rotations is "ZYX".

## Examples

## Convert Euler Angles to Homogeneous Transformation Matrix

eul = [0 pi/2 0];
tformZYX = eul2tform(eul)
tformZYX $=4 \times 4$

| 0.0000 | 0 | 1.0000 | 0 |
| ---: | ---: | ---: | ---: |
| 0 | 1.0000 | 0 | 0 |
| -1.0000 | 0 | 0.0000 | 0 |
| 0 | 0 | 0 | 1.0000 |

## Convert Euler Angles to Homogeneous Transformation Matrix Using ZYZ Axis Order

eul = [0 pi/2 pi/2];
tformZYZ = eul2tform(eul,'ZYZ')
tformZYZ $=4 \times 4$

| 0.0000 | -0.0000 | 1.0000 | 0 |
| ---: | ---: | ---: | ---: |
| 1.0000 | 0.0000 | 0 | 0 |
| -0.0000 | 1.0000 | 0.0000 | 0 |
| 0 | 0 | 0 | 1.0000 |

## Input Arguments

## eul - Euler rotation angles

n-by-3 matrix
Euler rotation angles in radians, specified as an $n$-by- 3 array of Euler rotation angles. Each row represents one Euler angle set.
Example: [0 0 1.5708]

## sequence - Axis rotation sequence

"ZYX" (default) | "ZYZ" | "XYZ"
Axis rotation sequence for the Euler angles, specified as one of these string scalars:

- "ZYX" (default) - The order of rotation angles is $z$-axis, $y$-axis, $x$-axis.
- "ZYZ" - The order of rotation angles is $z$-axis, $y$-axis, $z$-axis.
- "XYZ" - The order of rotation angles is $x$-axis, $y$-axis, $z$-axis.

Data Types: string | char

## Output Arguments

tform - Homogeneous transformation
4-by-4-by-n matrix
Homogeneous transformation matrix, specified by a 4-by-4-by-n matrix of $n$ homogeneous transformations. When using the rotation matrix, premultiply it with the coordinates to be rotated (as opposed to postmultiplying).
Example: [0 0 1 0; 010 0; -1 0 0 0; 0001$]$

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{Tm}}$.

## See Also

tform2eul
Introduced in R2015a

## exportOccupancyMap3D

Import an octree file as 3D occupancy map

## Syntax

export0ccupancyMap3D(map3D,filename)

## Description

export0ccupancyMap3D(map3D,filename) serializes the 3D occupancy map, map3D, into either an octree or binary tree file (.ot/bt) specified at the file location and name, filename

## Examples

## Create and Export 3-D Occupancy Map

Create an occupancyMap3D object.

```
map3D = occupancyMap3D;
```

Create a ground plane and set occupancy values to 0 .

```
[xGround,yGround,zGround] = meshgrid(0:100,0:100,0);
xyzGround = [xGround(:) yGround(:) zGround(:)];
occval = 0;
setOccupancy(map3D,xyzGround,occval)
```

Create obstacles in specific world locations of the map.

```
[xBuilding1,yBuilding1,zBuilding1] = meshgrid(20:30,50:60,0:30);
[xBuilding2,yBuilding2,zBuilding2] = meshgrid(50:60,10:30,0:40);
[xBuilding3,yBuilding3,zBuilding3] = meshgrid(40:60,50:60,0:50);
[xBuilding4,yBuilding4,zBuilding4] = meshgrid(70:80,35:45,0:60);
xyzBuildings = [xBuilding1(:) yBuilding1(:) zBuilding1(:);...
    xBuilding2(:) yBuilding2(:) zBuilding2(:);...
    xBuilding3(:) yBuilding3(:) zBuilding3(:);...
    xBuilding4(:) yBuilding4(:) zBuilding4(:)];
```

Update the obstacles with new probability values and display the map.

```
obs = 0.65;
update0ccupancy(map3D,xyzBuildings,obs)
show(map3D)
```


## Occupancy Map



Check if the map file named citymap. ot already exist in the current directory and delete it before creating the map file.

```
if exist("citymap.ot",'file')
    delete("citymap.ot")
end
```

Export the map as an octree file.
filePath = fullfile(pwd,"citymap.ot");
export0ccupancyMap3D(map3D,filePath)

## Input Arguments

map3D - 3-D occupancy map
occupancyMap3D object
3-D occupancy map, specified as a occupancyMap3D object.
filename - Absolute or relative path to octree file
string scalar | character vector
Absolute or relative path to octree file (.ot/bt), specified as a string scalar or character vector.
Example: "path/to/file/map.ot"
Data Types: char \| string

## See Also

## Classes

occupancyMap3D | lidarSLAM | occupancyMap
Functions
insertPointCloud |inflate | set0ccupancy | show
Introduced in R2020a

## extractNMEASentence

Verify and extract NMEA sentence data into string array

## Syntax

[isValid,splitString] = extractNMEASentence(unparsedData,'MessageID')

## Description

[isValid,splitString] = extractNMEASentence(unparsedData,'MessageID') verifies the checksum of an unparsed NMEA sentence, identified using its Message ID, and extracts the NMEA fields from NMEA sentence data into a string array, splitString.

## Examples

## Extract NMEA Fields of NMEA Sentence

Provide unparsed GGA, GSA, and RMC sentences as the input.

```
unparsedGGALine = '$GPGGA,111357.771,5231.364,N,01324.240,E,1,12,1.0,0.0,M,0.0,M, ,*69';
unparsedGSALine = '$GPGSA,A,3,01,02,03,04,05,06,07,08,09,10,11,12,1.0,1.0,1.0*30';
unparsedRMCLine = '$GPRMC,111357.771,A,5231.364,N,01324.240,E,10903,221.5,020620,000.0,W*44';
```

Create a string array to include the three sentences
unparsedNMEAData = [unparsedGGALine, newline,unparsedGSALine,newline,unparsedRMCLine]

```
unparsedNMEAData =
    '$GPGGA,111357.771,5231.364,N,01324.240,E,1,12,1.0,0.0,M,0.0,M, ,*69
    $GPGSA,A , 3,01,02,03,04,05,06,07,08,09,10,11,12,1.0,1.0,1.0*30
    $GPRMC,111357.771,A , 5231.364,N,01324.240, E, 10903,221.5,020620,000.0,W*44'
```

Specify GSA as the Message ID to extract the NMEA fields from the NMEA sentence into string array.

```
[isValid, splitString] = extractNMEASentence(unparsedNMEAData,'GSA')
isValid = logical
    1
splitString = 1x19 string
    Columns 1 through 10
        "GP" "GSA" "A" "3" "01" "02" "03" "04" "05" "06"
    Columns 11 through 19
        "07" "08" "09" "10" "11" "12" "1.0" "1.0" "1.0"
```


## Input Arguments

## unparsedData - Unparsed NMEA data from the device <br> string | character array

The unparsed NMEA data as obtained from the device.

## MessageID - Message ID of the unparsed NMEA sentence

string | character array
The Message ID to identify the unparsed NMEA sentence.

## Output Arguments

## isValid - Validity of unparsed NMEA sentence based on checksum 0|1

Determine the validity of unparsed NMEA sentence based on checksum. A value of 1 indicates that the checksum is valid. A value of 0 indicates that the checksum is invalid; however, the fields of NMEA sentence appear in the splitString output if the specified MessageID is matching.
Data Types: logical
splitString - Output data as split strings
string array
Output data as split strings based on the structure that you defined. If the specified MessageID is not found in the NMEA sentence, the function returns an empty splitString.
Data Types: string

## See Also

## Objects

nmeaParser

Introduced in R2021b

## flush

Flush all GPS data accumulated in the buffers and reset properties

## Syntax

```
flush(gps)
```


## Description

flush(gps) clears the buffers and resets the values of SamplesRead and SamplesAvailable properties.

## Examples

## Read Data from GPS Receiver as Matrix

Read data from the GPS receiver connected to the host computer using serialport object.

## Required Hardware

To run this example, you need:

- UBlox Neo-6M GPS module
- GPS antenna
- USB to UART module
- USB cable
- Connecting wires


## Hardware Connection



Connect the pins on the UBlox Neo-6M GPS module to the pins on your USB to UART module. The connections are:

- VCC -+5 V
- RX - TXO
- TX - RXI
- GND - GND

Connect the GPS antenna to the GPS module. Connect the USB to UART module to the host computer with a USB cable. GPS Fix can be easily acquired in locations that have a clear view of the sky. Wait for the GPS module to acquire satelite signals (Fix).This can be verified by checking the Fix LED (D1) of your GPS module.

## Create GPS Object

Connect to the GPS receiver using serialport object. Specify the port name and the baud rate. Specify the output format of the data as matrix.

```
s = serialport('COM4',9600);
gps = gpsdev(s,'OutputFormat',"matrix")
gps =
    gpsdev with properties:
        SerialPort: COM4
                        BaudRate: 9600 (bits/s)
        SamplesPerRead: 1
        ReadMode: "latest"
    SamplesRead: 0
Show all properties all functions
```


## Read the GPS data

Read the GPS data and return them as matrices.

```
[lla,speed,course,dops,gpsReceiverTime,timestamp,overruns] = read(gps)
lla = 1×3
    NaN NaN NaN
speed = NaN
course = NaN
dops = 1\times3
    NaN NaN NaN
gpsReceiverTime = datetime
    NaT
```

```
timestamp = datetime
    22-Mar-2021 03:41:00.274
overruns = 1
```

Display number of samples read and the samples available in the host buffer.

```
gps.SamplesRead
ans = 1
gps.SamplesAvailable
ans = 0
```

Flush all GPS data accumulated in the buffers and reset the SamplesRead and SamplesAvailable properties.

## flush(gps)

Display number of samples read and the samples available in the host buffer.

```
gps.SamplesRead
ans = 0
gps.SamplesAvailable
ans = 0
```


## Clean Up

When the connection is no longer needed, clear the associated object.

```
delete(gps);
clear gps;
clear s;
```


## Input Arguments

gps - GPS sensor
gpsdev object
The GPS sensor, specified as a gpsdev object.

## See Also

## Objects

gpsdev

## Functions <br> release|writeBytes | read |info

Introduced in R2020b

## gnssconstellation

Satellite locations at specified time

## Syntax

[satPos,satVel] = gnssconstellation(t)
[satPos,satVel,satID] = gnssconstellation(t,RINEXData=navData)

## Description

[satPos, satVel] = gnssconstellation(t) returns the satellite positions and velocities at the datetime $t$. The function returns positions and velocities in the Earth-centered Earth-fixed (ECEF) coordinate system in meters and meters per second, respectively.
[satPos,satVel,satID] = gnssconstellation(t,RINEXData=navData) returns the satellite positions, velocities, and IDs at time $t$ in the specified RINEX navigation message data navData.

## Examples

## Get Current Satellite Positions and Velocities

Get the current satellite positions and velocities from the GNSS satellites. Access the orbital parameters from IS-GPS-200K Interface Specification and calculate the position and velocities in ECEF coordinates for the given time. Display the satellite positions.

```
t = datetime('now','TimeZone','Local');
[satPos,satVel] = gnssconstellation(t);
disp(satPos)
1.0e+07 *
\begin{tabular}{rrr}
1.9000 & 1.5148 & 1.0723 \\
-0.1652 & -2.1753 & 1.5149 \\
-0.8193 & 1.4171 & -2.0916 \\
-1.5905 & 0.2721 & -2.1096 \\
0.5687 & -2.4543 & -0.8409 \\
-0.3208 & -2.0170 & -1.6979 \\
1.7950 & -0.7767 & 1.7969 \\
-1.4511 & 2.1755 & -0.4643 \\
1.4283 & 0.5443 & 2.1721 \\
2.6285 & -0.3116 & -0.2190 \\
-0.8123 & -1.4193 & -2.0928 \\
-2.0310 & -0.8994 & -1.4561 \\
-1.4030 & 1.3510 & 1.8058 \\
1.0114 & 2.3664 & 0.6569 \\
-1.7424 & -1.9241 & 0.5623 \\
-1.9381 & -1.1699 & 1.3891 \\
1.4515 & -0.5429 & -2.1570 \\
-0.0230 & 2.0737 & 1.6594 \\
-1.5580 & -0.2323 & 2.1385 \\
1.3006 & -2.3081 & -0.1874
\end{tabular}
```

| 0.3298 | 2.0098 | -1.7047 |
| ---: | ---: | ---: |
| 1.7620 | -1.5204 | -1.2798 |
| 1.2966 | -1.3829 | 1.8603 |
| 1.2930 | 1.2797 | -1.9351 |
| 2.1891 | 0.7733 | -1.2899 |
| -2.5692 | 0.4833 | -0.4690 |
| -2.5536 | -0.3104 | 0.6612 |

## Get Satellite Look Angles for Receiver Position

Use the lookangles function to get the azimuth and elevation angles of satellites for given satellite and receiver positions. Specify a mask angle of 5 degrees. Get the satellite positions using the gnssconstellation function.

Specify a receiver position in geodetic coordinates (latitude, longitude, altitude).

```
recPos = [42 -71 50];
```

Get the satellite positions for the current time.

```
t = datetime('now');
gpsSatPos = gnssconstellation(t);
```

Specify a mask angle of 5 degrees.

```
maskAngle = 5;
```

Get the azimuth and elevation look angles for the satellite positions. The vis output indicates which satellites are visible. Get the total using nnz.

```
[az,el,vis] = lookangles(recPos,gpsSatPos,maskAngle);
fprintf('%d satellites visible at %s.\n',nnz(vis),t);
9 ~ s a t e l l i t e s ~ v i s i b l e ~ a t ~ 2 7 - F e b - 2 0 2 2 ~ 0 3 : 0 3 : 2 3 . ~
```


## Retrieve Satellite Positions, Velocities, and IDs from RINEX File

Read one set of GPS satellites from the GPS navigation message in a RINEX file.

```
filename = "GODS00USA R 20211750000 01D GN.rnx";
data = rinexread(filename);
gpsData = data.GPS;
[~,satIdx] = unique(gpsData.SatelliteID);
gpsData = gpsData(satIdx,:);
```

Get the satellite positions, velocities, and IDs at the first time step.

```
t = gpsData.Time(1);
[satPos,satVel,satID] = gnssconstellation(t,RINEXData=gpsData)
satPos = 31\times3
107}
```

| -1.5630 | -0.1882 | 2.1186 |
| ---: | ---: | ---: |
| 1.3808 | 2.1970 | -0.4861 |
| -2.0061 | 0.7606 | 1.5492 |
| -2.5625 | -0.0140 | -0.7096 |
| 1.4896 | 0.5448 | -2.1487 |
| 0.6129 | 2.5407 | 0.4615 |
| -1.0081 | 1.3751 | -1.9877 |
| -2.5811 | -0.6135 | -0.3246 |
| -1.9289 | 0.8690 | -1.6134 |
| 0.9542 | -2.2526 | 1.0113 |

```
satVel = 31\times3
10}\mp@subsup{}{}{3}
\begin{tabular}{rrr}
-0.8888 & -2.5914 & -0.8416 \\
0.0362 & 0.7543 & 3.1043 \\
1.1203 & -1.6505 & 2.2591 \\
-0.8301 & -0.4385 & 2.9967 \\
-1.6023 & 2.1607 & -0.5493 \\
-0.3948 & -0.4708 & 3.1591 \\
-1.0322 & -2.4133 & -1.1748 \\
0.4370 & -0.1710 & -3.1339 \\
-1.9860 & -0.5032 & 2.1087 \\
0.9968 & -0.8308 & -2.8502
\end{tabular}
satID = 31\times1
```

    1
    2
    3
    4
    5
    6
    7
    8
    9
    10
    
## Input Arguments

t - Current time for satellite simulation
scalar datetime array
Current time for the satellite simulation, specified as a scalar datetime array.
The default time zone for a datetime array is UTC. For information on specifying a different time zone, see datetime.

GPS start time is Jan 6, 1980 midnight, UTC. Specifying any datetime prior to this time will use the GPS start time.

Example: datetime('now','TimeZone','Local');
Data Types: datetime
navData - RINEX navigation data
structure
RINEX navigation data, specified as a structure returned by the rinexread function. The contents of the struct vary depending on the type of satellite system. The gnssconstellation function supports only GPS or Galileo data read from a RINEX file. For more information on the contents of the structure, see the rinexread function "More About" on page 1-209 section.
Example: RINEXData=rinexread("GODS00USA_R_20211750000_01D_GN.rnx")

## Output Arguments

## satPos - Satellite positions

$N$-by-3 matrix of scalars
Satellite positions in the Earth-centered Earth-fixed (ECEF) coordinate system in meters, returned as an $N$-by- 3 matrix of scalars. $N$ is the number of satellites in the constellation.
Data Types: single | double

## satVel - Satellite velocities

$N$-by-3 matrix of scalar
Satellite velocities in the Earth-centered Earth-fixed (ECEF) coordinate system in meters per second, returned as an $N$-by- 3 matrix of scalars. $N$ is the number of satellites in the constellation.

Data Types: single | double

## satID - Satellite identification numbers

$N$-element column vector
Satellite identification numbers, returned as an $N$-element column vector. $N$ is the number of satellites in the constellation.
Data Types: single | double

## More About

## Orbital Parameters

The initial satellite positions and velocities are defined by orbital parameters in Table A.2-2 in GPS SPS Performance Standard, and are given in Earth-centered Earth-fixed (ECEF) coordinates.

Position calculations use equations from Table 30-II in the same IS-GPS-200K Interface Specification.
Velocity calculations use equations 8.21-8.27 in [1].

## References

[1] Groves, Paul D. Principles of GNSS, Inertial, and Multisensor Integrated Navigation Systems. Boston: Artech House, 2013.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Only MEX functions are supported for code generation.

## See Also

```
Objects
gnssSensor|gpsSensor|imuSensor
```


## Functions

skyplot | lookangles | pseudoranges | receiverposition| rinexread| rinexinfo
Topics
"Estimate GNSS Receiver Position with Simulated Satellite Constellations"
Introduced in R2021a

## hom2cart

Convert homogeneous coordinates to Cartesian coordinates

## Syntax

cart $=$ hom2cart(hom)

## Description

cart $=$ hom2cart (hom) converts a set of homogeneous points to Cartesian coordinates.

## Examples

```
Convert Homogeneous Points to 3-D Cartesian Points
h = [0.2785 0.9575 0.1576 0.5; 0.5469 0.9649 0.9706 0.5];
c = hom2cart(h)
c = 2 * 3
```

0.5570
1.9150
0.3152
$1.0938 \quad 1.9298 \quad 1.9412$

## Input Arguments

hom - Homogeneous points
$n$-by-k matrix
Homogeneous points, specified as an $n$-by- $k$ matrix, containing $n$ points. $k$ must be greater than or equal to 2 .
Example: [0.2785 0.9575 0.1576 0.5; 0.5469 0.9649 0.9706 0.5]

## Output Arguments

cart - Cartesian coordinates
$n$-by-( $k-1$ ) matrix
Cartesian coordinates, returned as an $n$-by- $(k-1)$ matrix, containing $n$ points. Each row of cart represents a point in ( $k-1$ )-dimensional space. $k$ must be greater than or equal to 2 .
Example: [0.8147 0.1270 0.6324; 0.9058 0.9134 0.0975]

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{Tm}}$.

## See Also <br> cart2hom <br> Introduced in R2015a

## importFactorGraph

Import factor graph from g2o log file

## Syntax

graph = importFactorGraph(filename)

## Description

graph = importFactorGraph(filename) imports a factor graph from the specified G2o file filename.

## Examples

## Import Factor Graph from G2o Log File

Import a factor graph from a G2o log file.
G = importFactorGraph("factorGraphLog.g2o");

## Input Arguments

## filename - Name of G2o log file

string scalar | character vector
Name of the G2o log file to import a factor graph from, specified as a string scalar or character vector. The specified G2o log file must contain either only 'EDGE_SE2' and 'VERTEX_SE2' tokens, or only 'EDGE_SE3:QUAT' and 'VERTEX_SE3:QUAT' tokens.

## Output Arguments

graph - Factor graph imported from G2o file
factorGraph object
Factor graph imported from the G2o file, returned as a factorGraph object.

## See Also

## Objects

factorGraph | factorGraphSolverOptions

Introduced in R2022a

## importOccupancyMap3D

Import an octree file as 3D occupancy map

## Syntax

map3D $=$ importOccupancyMap3D(mapPath)

## Description

map3D = importOccupancyMap3D(mapPath) imports the octree file (.ot/bt) specified at the relative or absolute file path, mapPath

## Examples

## Check Occupancy Status and Get Occupancy Values in 3-D Occupancy Map

Import a 3-D occupancy map.

```
map3D = import0ccupancyMap3D("citymap.ot")
map3D =
    occupancyMap3D with properties:
        ProbabilitySaturation: [1.0000e-03 0.9990]
            Resolution: 1
            OccupiedThreshold: 0.6500
            FreeThreshold: 0.2000
```

Display the map.
show(map3D)

## Occupancy Map



Check the occupancy statuses of different locations and get their occupancy values.

```
iOccVal1 = checkOccupancy(map3D,[50 15 0])
iOccVal1 = 0
OccVal1 = getOccupancy(map3D,[50 15 0])
OccVal1 = 0.0019
iOccVal2 = checkOccupancy(map3D,[50 15 15])
iOccVal2 = 1
OccVal2 = getOccupancy(map3D,[50 15 15])
OccVal2 = 0.6500
iOccVal3 = checkOccupancy(map3D,[50 15 45])
iOccVal3 = -1
OccVal3 = getOccupancy(map3D,[50 15 45])
OccVal3 = 0.5000
```


## Input Arguments

mapPath - Absolute or relative path to octree file
string scalar | character vector
Absolute or relative path to octree file (.ot/bt), specified as a string scalar or character vector.
Example: "path/to/file/map.ot"
Data Types: char|string

## Output Arguments

map3D - 3-D occupancy map
occupancyMap3D object
3-D occupancy map, specified as a occupancyMap3D object.

## See Also

## Classes

occupancyMap3D | lidarSLAM | occupancyMap
Functions
insertPointCloud |inflate | set0ccupancy | show
Introduced in R2020a

## info

Read update rate, GPS lock information and number of satellites in view for the GPS receiver

## Syntax

```
gpsInfo = info(gps)
```


## Description

gpsInfo $=$ info (gps) returns the update rate of the GPS receiver, GPS lock information and number of satellites from which the GPS can read signals. info gets updated after every execution of read command.

## Examples

## Read Information from GPS Receiver

Read information from the GPS receiver connected to the host computer on a specific serial port.

## Required Hardware

To run this example, you need:

- UBlox Neo-6M GPS module
- GPS antenna
- USB to UART module
- USB cable
- Connecting wires


## Hardware Connection



Connect the pins on the UBlox Neo-6M GPS module to the pins on your USB to UART module. The connections are:

- VCC - +5 V
- RX - TXO
- TX - RXI
- GND - GND

Connect the GPS antenna to the GPS module. Connect the USB to UART module to the host computer with a USB cable. GPS Fix can be easily acquired in locations that have a clear view of the sky. Wait for the GPS module to acquire satelite signals (Fix).This can be verified by checking the Fix LED (D1) of your GPS module.

## Create GPS Object

Create a gpsdev object for the GPS receiver connected to a specific port.

```
gps = gpsdev('COM4')
gps =
    gpsdev with properties:
                            SerialPort: COM4
                        BaudRate: 9600 (bits/s)
            SamplesPerRead: 1
            ReadMode: "latest"
            SamplesRead: 0
Show all properties all functions
```


## Read the GPS Module Information

Read the GPS module information and return them as a structure.

```
gpsInfo = info(gps)
gpsInfo = struct with fields:
    UpdateRate: []
        GPSLocked: 0
    SatellitesInView: 0
```


## Clean Up

When the connection is no longer needed, clear the associated object.

```
delete(gps);
clear gps;
```


## Input Arguments

```
gps - GPS sensor
```

gpsdev object
The GPS sensor, specified as a gpsdev object.

## Output Arguments

## gpsInfo - GPS module information

structure
GPS module information such as update rate, and number of satellites. The output has three fields:

- UpdateRate - Update Rate of the GPS Module in Hz. Update Rate of GPS receiver is estimated from the difference in time at which two RMC sentences are obtained. This value might be slightly varying from actual Update Rate of the module.
- GPSLocked - This property specifies if GPS has enough information to get valid data. GPS signals are acquired easily in locations that have a clear view of the sky. It can be either a 0 or 1 (logical). If GPSLocked is 0 , the GPS does not have the lock to compute location or time information. If GPSLocked is 1, GPS module has enough data to compute location or time information.
- NumberOfSatellitesInView - Number of satellites from which the GPS module can read the signals.

Data Types: struct

## See Also

## Objects

gpsdev

## Functions

flush|release|read|writeBytes
Introduced in R2020b

## insfilter

Create inertial navigation filter

## Syntax

filter = insfilter
filter = insfilter('ReferenceFrame',RF)

## Description

filter = insfilter returns an insfilterMARG inertial navigation filter object that estimates pose based on accelerometer, gyroscope, GPS, and magnetometer measurements. See insfilterMARG for more details.
filter = insfilter('ReferenceFrame',RF) returns an insfilterMARG inertial navigation filter object that estimates pose relative to a reference frame specified by RF. Specify RF as 'NED ' (North-East-Down) or 'ENU ' (East-North-Up). The default value is 'NED'. See insfilterMARG for more details.

## Examples

## Create Default INS Filter

The default INS filter is the insfilterMARG object. Call insfilter with no input arguments to create the default INS filter.

```
filter = insfilter
filter =
    insfilterMARG with properties:
            IMUSampleRate: 100 Hz
        ReferenceLocation: [0 0 0] [deg deg m]
            State: [22x1 double]
            StateCovariance: [22\times22 double]
    Multiplicative Process Noise Variances
                    GyroscopeNoise: [1e-09 1e-09 1e-09] (rad/s)2
            AccelerometerNoise: [0.0001 0.0001 0.0001] (m/s 2)}\mp@subsup{}{2}{2
            GyroscopeBiasNoise: [1e-10 1e-10 1e-10] (rad/s)2
        AccelerometerBiasNoise: [0.0001 0.0001 0.0001] (m/s2)2
    Additive Process Noise Variances
        GeomagneticVectorNoise: [1e-06 1e-06 1e-06] uT2
            MagnetometerBiasNoise: [0.1 0.1 0.1] uT2
```


## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

imufilter|ahrsfilter|insfilterErrorState|insfilterAsync| insfilterNonholonomic|insfilterMARG

Introduced in R2018b

## interpolate

Interpolate poses along path segment

## Syntax

```
poses = interpolate(pathSeg)
poses = interpolate(pathSeg,lengths)
[poses,directions] = interpolate(
```

$\qquad$

``` )
```


## Description

poses = interpolate(pathSeg) interpolates along the path segment at the transitions between motion types.
poses = interpolate(pathSeg,lengths) interpolates along the path segment at the specified lengths along the path. Transitions between motion types are always included.
[poses, directions] = interpolate ( __ ) also returns the direction of motion along the path for each section as a vector of 1 s (forward) and -1 s (reverse) using the previous inputs.

## Examples

## Interpolate Poses For Dubins Path

Create a dubinsConnection object.
dubConnObj = dubinsConnection;
Define start and goal poses as [x y theta] vectors.

```
startPose = [0 0 0];
goalPose = [1 1 pi];
```

Calculate a valid path segment to connect the poses.

```
[pathSegObj,pathCosts] = connect(dubConnObj,startPose,goalPose);
```

Show the generated path.

```
show(pathSegObj{1})
```



Interpolate poses along the path. Get a pose every 0.2 meters, including the transitions between turns.

```
length = pathSegObj{1}.Length;
poses = interpolate(pathSeg0bj{1},0:0.2:length)
poses = 32\times3
```

| 0 | 0 | 0 |
| ---: | ---: | ---: |
| 0.1987 | -0.0199 | 6.0832 |
| 0.3894 | -0.0789 | 5.8832 |
| 0.5646 | -0.1747 | 5.6832 |
| 0.7174 | -0.3033 | 5.4832 |
| 0.8309 | -0.4436 | 5.3024 |
| 0.8418 | -0.4595 | 5.3216 |
| 0.9718 | -0.6110 | 5.5216 |
| 1.1293 | -0.7337 | 5.7216 |
| 1.3081 | -0.8226 | 5.9216 |

Use the quiver function to plot these poses.
quiver(poses(:,1), poses(:,2), cos(poses(:,3)), $\sin (\operatorname{poses}(:, 3)), 0.5)$


## Input Arguments

pathSeg - Path segment
dubinsPathSegment object| reedsSheppPathSegment object
Path segment, specified as a dubinsPathSegment or reedsSheppPathSegment object.

## lengths - Lengths along path to interpolate at

positive numeric vector
Lengths along path to interpolate at, specified as a positive numeric vector. For example, specify [0:0.1:pathSegObj $\{1\}$. Length] to interpolate at every 0.1 meters along the path. Transitions between motion types are always included.

## Output Arguments

```
poses - Interpolated poses
```

$[x, y, \Theta]$ matrix
This property is read-only.
Interpolated poses along the path segment, specified as an $[x, y, \Theta]$ matrix. Each row of the matrix corresponds to a different interpolated pose along the path.
$x$ and $y$ are in meters. $\Theta$ is in radians.
directions - Directions of motion
vector of 1s (forward) and -1s (reverse)
Directions of motion for each segment of the interpolated path, specified as a vector of 1 s (forward) and -1 s (reverse).

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{Tm}}$.

## See Also

## Functions

connect \| show
Objects
dubinsConnection|dubinsPathSegment | reedsSheppConnection |
reedsSheppPathSegment
Introduced in R2019b

## Ila2enu

Transform geodetic coordinates to local east-north-up coordinates

## Syntax

xyzENU = lla2enu(lla,lla0,method)

## Description

xyzENU = lla2enu(lla, lla0, method) transforms the geodetic coordinates lla to local east-north-up (ENU) Cartesian coordinates xyzENU. Specify the origin of the local ENU system as the geodetic coordinates lla0.

## Note

- The latitude and longitude values in the geodetic coordinate system use the World Geodetic System of 1984 (WGS84) standard.
- Specify altitude as height in meters above the WGS84 reference ellipsoid.


## Examples

## Transform Geodetic Coordinates to ENU Coordinates

Specify the geodetic coordinates of the local origin in Zermatt, Switzerland.
lla0 = [46.017 7.750 1673]; \% [lat0 lon0 alt0]
Specify the geodetic coordinates of a point of interest. In this case, the point of interest is the Matterhorn.

```
lla = [45.976 7.658 4531]; % [lat lon alt]
```

Transform the geodetic coordinates to local ENU coordinates using flat earth approximation.

```
xyzENU = lla2enu(lla,lla0,'flat')
xyzENU = 1×3
103 x
    -7.1244 -4.5572 2.8580
```


## Input Arguments

## Lla - Geodetic coordinates

three-element row vector | $n$-by-3 matrix

Geodetic coordinates, specified as a three-element row vector or an $n$-by- 3 matrix. $n$ is the number of points to transform. Specify each point in the form [lat lon alt]. lat and lon specify the latitude and longitude respectively in degrees. alt specifies the altitude in meters.
Data Types: double

## lla0 - Origin of local ENU system in geodetic coordinates

three-element row vector | $n$-by-3 matrix
Origin of the local ENU system in the geodetic coordinates, specified as a three-element row vector or an $n$-by- 3 matrix. $n$ is the number of origin points. Specify each point in the form [ lat0 lon0 alt0]. lat0 and lon0 specify the latitude and longitude of the origin, respectively, in degrees. alt0 specifies the altitude of the origin in meters.
Data Types: double
method - Transformation method
'flat' | 'ellipsoid'
Transformation method, specified as 'flat' or 'ellipsoid'. This argument specifies whether the function assumes the planet is flat or ellipsoidal.

The flat Earth transformation method has these limitations:

- Assumes that the flight path and bank angle are zero.
- Assumes that the flat Earth $z$-axis is normal to the Earth at only the initial geodetic latitude and longitude. This method has higher accuracy over small distances from the initial geodetic latitude and longitude, and closer to the equator. The method calculates a longitude with higher accuracy when the variation in latitude is smaller.
- Latitude values of +90 and -90 may return unexpected values because of singularity at the poles.

Data Types: char|string

## Output Arguments

## xyzENU - Local ENU Cartesian coordinates

three-element row vector $\mid n$-by- 3 matrix
Local ENU Cartesian coordinates, returned as a three-element row vector or an $n$-by- 3 matrix. $n$ is the number of transformed points. Each point is in the form [xEast yNorth zUp]. xEast, yNorth, and $z U p$ are the respective $x-, y$-, and $z$-coordinates, in meters, of the point in the local ENU system.
Data Types: double

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® $\mathrm{Coder}^{\mathrm{TM}}$.

## See Also

Functions
enu2lla|lla2ned|ned2lla

Introduced in R2021a

## Ila2ned

Transform geodetic coordinates to local north-east-down coordinates

## Syntax

xyzNED = lla2ned(lla,lla0,method)

## Description

xyzNED = lla2ned(lla, lla0, method) transforms the geodetic coordinates lla to local north-east-down (NED) Cartesian coordinates xyzNED. Specify the origin of the local NED system as the geodetic coordinates lla0.

## Note

- The latitude and longitude values in the geodetic coordinate system use the World Geodetic System of 1984 (WGS84) standard.
- Specify altitude as height in meters above the WGS84 reference ellipsoid.


## Examples

## Transform Geodetic Coordinates to NED Coordinates

Specify the geodetic coordinates of the local origin in Zermatt, Switzerland.
lla0 $=$ [46.017 7.750 1673]; \% [lat0 lon0 alt0]
Specify the geodetic coordinates of a point of interest. In this case, the point of interest is the Matterhorn.

```
lla = [45.976 7.658 4531]; % [lat lon alt]
```

Transform the geodetic coordinates to local NED coordinates using flat earth approximation.

```
xyzNED = lla2ned(lla,lla0,'flat')
xyzNED = 1×3
103 x
    -4.5572 -7.1244 -2.8580
```


## Input Arguments

## Lla - Geodetic coordinates

three-element row vector | $n$-by-3 matrix

Geodetic coordinates, specified as a three-element row vector or an $n$-by- 3 matrix. $n$ is the number of points to transform. Specify each point in the form [lat lon alt]. lat and lon specify the latitude and longitude respectively in degrees. alt specifies the altitude in meters.

## Data Types: double

## lla0 - Origin of local NED system in geodetic coordinates

three-element row vector $\mid n$-by-3 matrix
Origin of the local NED system with the geodetic coordinates, specified as a three-element row vector or an $n$-by-3 matrix. $n$ is the number of origin points. Specify each point in the form [lat0 lon 0 alt0]. lat0 and lon0 specify the latitude and longitude respectively in degrees. alt0 specifies the altitude in meters.

Data Types: double
method - Transformation method
'flat'|'ellipsoid'
Transformation method, specified as 'flat' or 'ellipsoid'. This argument specifies whether the function assumes the planet is flat or ellipsoidal.

The flat Earth transformation method has these limitations:

- Assumes that the flight path and bank angle are zero.
- Assumes that the flat Earth $z$-axis is normal to the Earth at only the initial geodetic latitude and longitude. This method has higher accuracy over small distances from the initial geodetic latitude and longitude, and closer to the equator. The method calculates a longitude with higher accuracy when the variation in latitude is smaller.
- Latitude values of +90 and - 90 may return unexpected values because of singularity at the poles.

Data Types: char | string

## Output Arguments

## xyzNED - Local NED Cartesian coordinates

three-element row vector | $n$-by-3 matrix
Local NED Cartesian coordinates, returned as a three-element row vector or an $n$-by- 3 matrix. $n$ is the number of transformed points. Each point is in the form [xNorth yEast zDown]. xNorth, $y$ East, and $z$ Down are the respective $x$-, $y$-, and $z$-coordinates, in meters, of the point in the local NED system.

Data Types: double

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

## Functions

enu2lla|lla2enu|ned2lla

Introduced in R2021a

## lookangles

Satellite look angles from receiver and satellite positions

## Syntax

[az,el,vis] = lookangles(recPos,satPos)
[az,el,vis] = lookangles(recPos,satPos,maskAngle)

## Description

[az,el,vis] = lookangles(recPos,satPos) returns the look angles and visibilities of satellite positions for a given receiver position. The azimuth az and elevation el are the look angles in degrees in the Earth-centered Earth-fixed (ECEF) coordinate system. The visibility of the satellites vis is a logical array that the function calculates using the default receiver mask angle of 10 degrees.
[az,el,vis] = lookangles(recPos,satPos,maskAngle) returns the look angles and visibilities of satellites with a specified mask angle maskAngle in degrees.

## Examples

## Get Satellite Look Angles for Receiver Position

Use the lookangles function to get the azimuth and elevation angles of satellites for given satellite and receiver positions. Specify a mask angle of 5 degrees. Get the satellite positions using the gnssconstellation function.

Specify a receiver position in geodetic coordinates (latitude, longitude, altitude).

```
recPos = [42 -71 50];
```

Get the satellite positions for the current time.

```
t = datetime('now');
gpsSatPos = gnssconstellation(t);
```

Specify a mask angle of 5 degrees.

```
maskAngle = 5;
```

Get the azimuth and elevation look angles for the satellite positions. The vis output indicates which satellites are visible. Get the total using nnz.

```
[az,el,vis] = lookangles(recPos,gpsSatPos,maskAngle);
fprintf('%d satellites visible at %s.\n',nnz(vis),t);
9 satellites visible at 27-Feb-2022 03:03:23.
```


## Input Arguments

## recPos - Receiver position

three-element vector of the form [lat lon alt]
Receiver position in geodetic coordinates, specified as a three-element vector of the form [latitude longitude altitude]

Data Types: single|double

## satPos - Satellite positions

$N$-by-3 matrix of scalars
Satellite positions in the Earth-centered Earth-fixed (ECEF) coordinate system in meters, specified as an $N$-by- 3 matrix of scalars. $N$ is the number of satellites in the constellation.

Data Types: single | double

## maskAngle - Elevation mask angle

positive scalar
Elevation mask angle of the receiver, specified as a positive scalar in degrees.
Data Types: single | double

## Output Arguments

az - Azimuth angles for visible satellite positions
$n$-element vector of angles
Azimuth angles for visible satellite positions, returned as an $n$-element vector of angles. $n$ is the number of visible satellite positions in the plot. Azimuth angles are measured in degrees, clockwisepositive from the north direction looking down.
Example: [25 45182 356]
Data Types: double

## el - Elevation angles for visible satellite positions

$n$-element vector of angles
Elevation angles for visible satellite positions, returned as an $n$-element vector of angles. $n$ is the number of visible satellite positions in the plot. Elevation angles are measured from the horizon line with 90 degrees being directly up.

Example: [llllll 45027 74]
Data Types: double
vis - Satellite visibility
n-element logical array
Satellite visibility, returned as an $n$-element logical array. Each element indicates whether the satellite position given by az and el is visible.
Data Types: logical

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

## Objects

gnssSensor|gpsSensor|imuSensor
Functions
skyplot | gnssconstellation | pseudoranges | receiverposition
Introduced in R2021a

## ned2Ila

Transform local north-east-down coordinates to geodetic coordinates

## Syntax

lla = ned2lla(xyzNED,lla0,method)

## Description

lla $=$ ned2lla(xyzNED, lla0, method) transforms the local north-east-down (NED) Cartesian coordinates xyzNED to geodetic coordinates lla. Specify the origin of the local NED system as the geodetic coordinates lla0.

## Note

- The latitude and longitude values in the geodetic coordinate system use the World Geodetic System of 1984 (WGS84) standard.
- Specify altitude as height in meters above the WGS84 reference ellipsoid.


## Examples

## Transform NED Coordinates to Geodetic Coordinates

Specify the geodetic coordinates of the local origin in Zermatt, Switzerland.
lla0 $=$ [46.017 7.750 1673]; \% [lat0 lon0 alt0]
Specify the NED coordinates of a point of interest, in meters. In this case, the point of interest is the Matterhorn.

```
xyzNED = [-4556.3 -7134.8 -2852.4]; % [xNorth yEast zDown]
```

Transform the local NED coordinates to geodetic coordinates using flat earth approximation.

```
lla = ned2lla(xyzNED,lla0,'flat')
lla = 1×3
103 }
    0.0460 0.0077 4.5254
```


## Input Arguments

## xyzNED - Local NED Cartesian coordinates

three-element row vector $\mid n$-by- 3 matrix

Local NED Cartesian coordinates, specified as a three-element row vector or an $n$-by- 3 matrix. $n$ is the number of points to transform. Specify each point in the form [xNorth yEast zDown]. xNorth, $y$ East, and $z$ Down are the respective $x-, y$-, and $z$-coordinates, in meters, of the point in the local NED system.
Data Types: double

## lla0 - Origin of local NED system in geodetic coordinates

three-element row vector | $n$-by-3 matrix
Origin of the local NED system with the geodetic coordinates, specified as a three-element row vector or an $n$-by-3 matrix. $n$ is the number of origin points. Specify each point in the form [lat0 lon0 alt0]. lat0 and lon0 specify the latitude and longitude respectively in degrees. alt0 specifies the altitude in meters.

Data Types: double

## method - Transformation method <br> 'flat'|'ellipsoid'

Transformation method, specified as 'flat' or 'ellipsoid'. This argument specifies whether the function assumes the planet is flat or ellipsoidal.

The flat Earth transformation method has these limitations:

- Assumes that the flight path and bank angle are zero.
- Assumes that the flat Earth $z$-axis is normal to the Earth at only the initial geodetic latitude and longitude. This method has higher accuracy over small distances from the initial geodetic latitude and longitude, and closer to the equator. The method calculates a longitude with higher accuracy when the variation in latitude is smaller.
- Latitude values of +90 and -90 may return unexpected values because of singularity at the poles.

Data Types: char|string

## Output Arguments

## lla - Geodetic coordinates

three-element row vector | $n$-by-3 matrix
Geodetic coordinates, returned as a three-element row vector or an $n$-by- 3 matrix. $n$ is the number of transformed points. Each point is in the form [lat lon alt]. lat and lon specify the latitude and longitude, respectively, in degrees. alt specifies the altitude in meters.

## Data Types: double

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

Functions
enu2lla|lla2enu|lla2ned

Introduced in R2021a

## copy

Create copy of path object

## Syntax

path2 $=$ copy (path1)

## Description

path2 $=$ copy (path1) creates a copy of the path object, path2, from the path object, path1.

## Examples

## Create Copy of navPath Object

Create a navPath object.

```
path = navPath
path =
    navPath with properties:
        StateSpace: [1x1 stateSpaceSE2]
            States: [0x3 double]
        NumStates: 0
```

Create copy of navPath object.

```
pathNew = copy(path)
pathNew =
    navPath with properties:
        StateSpace: [1x1 stateSpaceSE2]
            States: [0x3 double]
        NumStates: 0
```


## Input Arguments

path1 - path object
navPath object
Path object, specified as a navPath object.
Data Types: object

## Output Arguments

path2 - path object
navPath object
Path object, returned as a navPath object.
Data Types: object

## See Also

navPath

Introduced in R2019b

## magcal

Magnetometer calibration coefficients

## Syntax

[A, b, expmfs] = magcal(D)
$[A, b$, expmfs $]=\operatorname{magcal}(D, f i t k i n d)$

## Description

$[A, b, \operatorname{expmfs}]=$ magcal(D) returns the coefficients needed to correct uncalibrated magnetometer data D.

To produce the calibrated magnetometer data C , use equation $\mathrm{C}=(\mathrm{D}-\mathrm{b}) * \mathrm{~A}$. The calibrated data C lies on a sphere of radius expmfs.
[A,b, expmfs] = magcal( $D, f i t k i n d)$ constrains the matrix $A$ to be the type specified by fitkind. Use this syntax when only the soft- or hard-iron effect needs to be corrected.

## Examples

## Correct Data Lying on Ellipsoid

Generate uncalibrated magnetometer data lying on an ellipsoid.

```
c = [-50; 20; 100]; % ellipsoid center
r = [30; 20; 50]; % semiaxis radii
[x,y,z] = ellipsoid(c(1),c(2),c(3),r(1),r(2),r(3),20);
D = [x(:),y(:),z(:)];
```

Correct the magnetometer data so that it lies on a sphere. The option for the calibration is set by default to 'auto'.

```
[A,b,expmfs] = magcal(D); % calibration coefficients
expmfs % Dipaly expected magnetic field strength in uT
expmfs = 31.0723
C = (D-b)*A; % calibrated data
```

Visualize the uncalibrated and calibrated magnetometer data.

```
figure(1)
plot3(x(:),y(:),z(:),'LineStyle','none','Marker','X','MarkerSize',8)
hold on
grid(gca,'on')
plot3(C(:,1),C(:,2),C(:,3),'LineStyle','none','Marker', ...
    'o','MarkerSize',8,'MarkerFaceColor','r')
axis equal
xlabel('uT')
```

```
ylabel('uT')
zlabel('uT')
legend('Uncalibrated Samples', 'Calibrated Samples','Location', 'southoutside')
title("Uncalibrated vs Calibrated" + newline + "Magnetometer Measurements")
hold off
```



## Input Arguments

## D - Raw magnetometer data

$N$-by-3 matrix (default)
Input matrix of raw magnetometer data, specified as a $N$-by-3 matrix. Each column of the matrix corresponds to the magnetometer measurements in the first, second and third axes, respectively. Each row of the matrix corresponds to a single three-axis measurement.
Data Types: single|double

## fitkind - Matrix output type

'auto' (default) | 'eye' | 'diag' | 'sym'
Matrix type for output A. The matrix type of A can be constrained to:

- 'eye' - identity matrix
- 'diag' - diagonal
- 'sym' - symmetric
- 'auto' - whichever of the previous options gives the best fit


## Output Arguments

## A - Correction matrix for soft-iron effect

3-by-3 matrix
Correction matrix for the soft-iron effect, returned as a 3-by-3 matrix.

## b - Correction vector for hard-iron effect

3-by-1 vector
Correction vector for the hard-iron effect, returned as a 3-by-1 array.

## expmfs - Expected magnetic field strength

scalar
Expected magnetic filed strength, returned as a scalar.

## More About

## Soft- and Hard-Iron Effects

Because a magnetometer usually rotates through a full range of 3-D rotation, the ideal measurements from a magnetometer should form a perfect sphere centered at the origin if the magnetic field is unperturbed. However, due to distorting magnetic fields from the sensor circuit board and the surrounding environment, the spherical magnetic measurements can be perturbed. In general, two effects exist.

1 The soft-iron effect is described as the distortion of the ellipsoid from a sphere and the tilt of the ellipsoid, as shown in the left figure. This effect is caused by disturbances that influence the magnetic field but may not generate their own magnetic field. For example, metals such as nickel and iron can cause this kind of distortion.
2 The hard-iron effect is described as the offset of the ellipsoid center from the origin. This effect is produced by materials that exhibit a constant, additive field to the earth's magnetic field. This constant additive offset is in addition to the soft-iron effect as shown in the figure on the right.


The underlying algorithm in magcal determines the best-fit ellipsoid to the raw sensor readings and attempts to "invert" the ellipsoid to produce a sphere. The goal is to generate a correction matrix A to
account for the soft-iron effect and a vector $b$ to account for the hard-iron effect. The three output options, 'eye', 'diag' and 'sym' correspond to three parameter-solving algorithms, and the 'auto' option chooses among these three options to give the best fit.

## References

[1] Ozyagcilar, T. "Calibrating an eCompass in the Presence of Hard and Soft-iron Interference." Freescale Semiconductor Ltd. 1992, pp. 1-17.

## See Also

## Classes

magparams
Objects
imuSensor

## Introduced in R2019a

## mapClutter

Generate map with randomly scattered obstacles

## Syntax

```
map = mapClutter
map = mapClutter(numObst)
map = mapClutter(numObst,shapes)
map = mapClutter(___,Name,Value)
```


## Description

map = mapClutter generates a 2-D occupancy map as a binary0ccupancyMap object map, with a width and height of 50 meters and a resolution of 5 cells per meter. The map contains 20 randomly distributed obstacles of types Box and Circle. Generated obstacles have random sizes.
map $=$ mapClutter(numObst) generates a 2-D occupancy map, of the default size and resolution, with a specified number of randomly distributed obstacles, num0bst, of default shapes.
map $=$ mapClutter(num0bst, shapes) generates a 2-D occupancy map, of the default size and resolution, with a specified number of obstacles, numObst, of specified shapes, shapes.
map = mapClutter( $\qquad$ ,Name, Value) specifies options using one or more name-value pair arguments in addition to any combination of input arguments from previous syntaxes. For example, 'MapSize', [50 30] generates a randomly distributed obstacle map with a width of 50 meters and height of 30 meters.

## Examples

## Generate Randomly Distributed Obstacle Map

Generate a 2-D occupancy map with ten randomly scattered obstacles of types Box, Circle, and Plus. Specify the size of the map as 50 meters wide and 30 meters high with a resolution of 5 cells per meters.
map = mapClutter(10,\{'Box','Plus','Circle'\},'MapSize',[50 30],'MapResolution',5);
Visualize the generated obstacle map.

```
show(map)
```



## Input Arguments

numObst - Number of obstacles
20 (default) | positive integer
Number of obstacles, specified as a positive integer.
Data Types: single|double

## shapes - Obstacle shapes

\{'Box','Circle'\} (default) | string scalar | vector of strings | cell array of character vectors
Obstacle shapes, specified as a string scalar, vector of strings, or cell array of character vectors. The only valid shapes are Box, Circle, and Plus.

When you specify a string scalar, the function generates a map with obstacles of only the specified shape.

Example: "Box"
When you specify a vector of strings or a cell array of character vectors, the function generates a map with obstacles of each specified shape.
Example: ["Box", "Plus"]
Example: \{'Box','Plus','Circle'\}

Data Types: cell | string

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, ... ,NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: 'MapSize', [50 40] generates a randomly distributed obstacle map with a width of 50 meters and height of 40 meters.

## MapSize - Width and height of generated map

[50 50] (default) |two-element vector of positive real finite numbers
Width and height of the generated map, specified as the comma-separated pair consisting of 'MapSize' and a two-element vector of positive real finite numbers of the form [Width,Height]. Specify both values in meters.
Example: 'MapSize',[50 30]
Data Types: single | double

## MapResolution - Resolution of generated map

5 (default) | positive real scalar
Resolution of the generated map, specified as the comma-separated pair consisting of 'MapResolution' and a positive real scalar in cells per meter.
Example: 'MapResolution',10
Data Types: single | double

## Output Arguments

map - Map with randomly scattered obstacles
binaryOccupancyMap object
A map with randomly scattered obstacles, returned as a binary0ccupancyMap object.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.

## See Also

mapMaze | binary0ccupancyMap | validatorOccupancyMap

Introduced in R2020b

## mapMaze

Generate random 2-D maze map

## Syntax

```
map = mapMaze
map = mapMaze(passageWidth)
map = mapMaze(passageWidth,wallThickness)
map = mapMaze(
```

$\qquad$

``` ,Name, Value)
```


## Description

map = mapMaze generates a random 2-D maze map, map, as a binary0ccupancyMap object with a width and height of 50 meters and a resolution of 5 cells per meter. The maze map contains straight passages, turns, and T-junctions with a passage width of 4 grid cells and wall thickness of 1 grid cell.
map = mapMaze(passageWidth) generates a binary0ccupancyMap of a maze of the default size and resolution with a specified passage width, passageWidth, in number of grid cells.
map $=$ mapMaze(passageWidth, wallThickness) specifies a wall thickness, wallThickness, in number of grid cells.
map = mapMaze( __ , Name, Value) specifies options using one or more name-value pair arguments in addition to any combination of input arguments from previous syntaxes. For example, 'MapSize' , [50 30] generates a random maze map with a width of 50 meters and height of 30 meters.

## Examples

## Generate Random Maze Map

Generate a random 2-D maze map with a passage width of 5 grid cells and wall thickness of 2 grid cells. Specify the size of the map as 50 meters wide and 30 meters high with a resolution of 5 cells per meter.

```
map = mapMaze(5,2,'MapSize',[50 30],'MapResolution',5);
```

Visualize the generated obstacle map.

```
show(map)
```



Input Arguments
passageWidth - Width of maze passage
4 (default) | positive integer
Width of maze passage, specified as a positive integer in number of grid cells.
Data Types: single | double
wallThickness - Thickness of maze wall
1 (default) | positive integer
Thickness of maze wall, specified as a positive integer in number of grid cells.
Data Types: single | double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, ... , NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: 'MapSize' , [50 40] generates a randomly distributed obstacle map with a width of 50 meters and height of 40 meters.

## MapSize - Width and height of generated map

[50 50] (default) | two-element vector of positive real finite numbers
Width and height of the generated map, specified as the comma-separated pair consisting of 'MapSize' and a two-element vector of positive real finite numbers of the form [Width Height]. Specify both values in meters.
Example: 'MapSize', [50 30]
Data Types: single | double

## MapResolution - Resolution of generated map

5 (default) | positive real scalar
Resolution of the generated map, specified as the comma-separated pair consisting of 'MapResolution' and a positive real scalar in cells per meter.
Example: 'MapResolution' , 10
Data Types: single|double

## Output Arguments

## map - Random maze map

binaryOccupancyMap object
Random maze map, returned as a binary0ccupancyMap object.

## Tips

- when the number of grid cells along map width could not accommodate given maze parameters, ceil (MapWidth*MapResolution) must be greater than or equal to (passageWidth +2*wallThickness).
- when the number of grid cells along map height could not accommodate given maze parameters, ceil(MapHeight*MapResolution) must be greater than or equal to (passageWidth +2*wallThickness).


## See Also

mapClutter | binary0ccupancyMap | validator0ccupancyMap

## Introduced in R2021a

## matchScans

Estimate pose between two laser scans

## Syntax

```
pose = matchScans(currScan,refScan)
pose = matchScans(currRanges,currAngles,refRanges,refAngles)
[pose,stats] = matchScans(
```

$\qquad$

```
[___] = matchScans(___ ,Name,Value)
```


## Description

pose $=$ matchScans(currScan, refScan) finds the relative pose between a reference lidarScan and a current lidarScan object using the normal distributions transform (NDT).
pose $=$ matchScans(currRanges,currAngles,refRanges,refAngles) finds the relative pose between two laser scans specified as ranges and angles.
[pose,stats] = matchScans(__ ) returns additional statistics about the scan match result using the previous input arguments.
[___ ] = matchScans (__ , Name, Value) specifies additional options specified by one or more Name, Value pair arguments.

## Examples

## Match Lidar Scans

Create a reference lidar scan using lidarScan. Specify ranges and angles as vectors.

```
refRanges = 5*ones(1,300);
refAngles = linspace(-pi/2,pi/2,300);
refScan = lidarScan(refRanges,refAngles);
```

Using the transformScan (Robotics System Toolbox) function, generate a second lidar scan at an $x, y$ offset of (0.5, 0.2).
currScan = transformScan(refScan,[0.5 0.2 0]);
Match the reference scan and the second scan to estimate the pose difference between them.

```
pose = matchScans(currScan,refScan);
```

Use the transformScan function to align the scans by transforming the second scan into the frame of the first scan using the relative pose difference. Plot both the original scans and the aligned scans.

```
currScan2 = transformScan(currScan,pose);
subplot(2,1,1);
hold on
```

```
plot(currScan)
plot(refScan)
title('Original Scans')
hold off
subplot(2,1,2);
hold on
plot(currScan2)
plot(refScan)
title('Aligned Scans')
xlim([0 5])
hold off
```



## Match Laser Scans

This example uses the 'fminunc' solver algorithm to perform scan matching. This solver algorithm requires an Optimization Toolbox ${ }^{\mathrm{TM}}$ license.

Specify a reference laser scan as ranges and angles.
refRanges $=5 *$ ones $(1,300)$;
refAngles $=$ linspace(-pi/2,pi/2,300);
Using the transformScan (Robotics System Toolbox) function, generate a second laser scan at an $x, y$ offset of (0.5,0.2).
[currRanges,currAngles] = transformScan(refRanges,refAngles,[0.5 0.2 0]);
Match the reference scan and the second scan to estimate the pose difference between them.

```
pose = matchScans(currRanges,currAngles,refRanges,refAngles,'SolverAlgorithm','fminunc');
```

Improve the estimate by giving an initial pose estimate.

```
pose = matchScans(currRanges,currAngles,refRanges,refAngles,...
    'SolverAlgorithm','fminunc','InitialPose',[-0.4 -0.1 0]);
```

Use the transformScan function to align the scans by transforming the second scan into the frame of the first scan using the relative pose difference. Plot both the original scans and the aligned scans.
[currRanges2,currAngles2] = transformScan(currRanges,currAngles,pose);
[x1, y1] = pol2cart(refAngles,refRanges);
[x2, y2] = pol2cart(currAngles,currRanges);
[x3, y3] = pol2cart(currAngles2,currRanges2);

```
subplot(1,2,1)
plot(x1,y1,'o',x2,y2,'*r')
title('Original Scans')
subplot(1,2,2)
plot(x1,y1,'o',x3,y3,'*r')
title('Aligned Scans')
```




## Input Arguments

## currScan - Current lidar scan readings <br> lidarScan object

Current lidar scan readings, specified as a lidarScan object.
Your lidar scan can contain Inf and NaN values, but the algorithm ignores them.

## refScan - Reference lidar scan readings

lidarScan object
Reference lidar scan readings, specified as a lidarScan object.
Your lidar scan can contain Inf and NaN values, but the algorithm ignores them.

## currRanges - Current laser scan ranges

vector in meters
Current laser scan ranges, specified as a vector. Ranges are given as distances to objects measured from the laser sensor.

Your laser scan ranges can contain Inf and NaN values, but the algorithm ignores them.

## currAngles - Current laser scan angles

vector in radians
Current laser scan angles, specified as a vector in radians. Angles are given as the orientations of the corresponding range measurements.

## refRanges - Reference laser scan ranges

vector in meters
Reference laser scan ranges, specified as a vector in meters. Ranges are given as distances to objects measured from the laser sensor.

Your laser scan ranges can contain Inf and NaN values, but the algorithm ignores them.

## refAngles - Reference laser scan angles

vector in radians
Reference laser scan angles, specified as a vector in radians. Angles are given as the orientations of the corresponding range measurements.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, ... , NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

```
Example: "InitialPose",[1 1 pi/2]
```


## SolverAlgorithm - Optimization algorithm

[^0]Optimization algorithm, specified as either "trust-region" or "fminunc". Using "fminunc" requires an Optimization Toolbox ${ }^{\mathrm{TM}}$ license.

## InitialPose - Initial guess of current pose <br> [000] (default) | [x y theta]

Initial guess of the current pose relative to the reference laser scan, specified as the commaseparated pair consisting of "InitialPose" and an [x y theta] vector. [ $\mathrm{x} y$ ] is the translation in meters and theta is the rotation in radians.

## CellSize - Length of cell side

1 (default) | numeric scalar
Length of a cell side in meters, specified as the comma-separated pair consisting of "CellSize" and a numeric scalar. matchScans uses the cell size to discretize the space for the NDT algorithm.

Tuning the cell size is important for proper use of the NDT algorithm. The optimal cell size depends on the input scans and the environment of your robot. Larger cell sizes can lead to less accurate matching with poorly sampled areas. Smaller cell sizes require more memory and less variation between subsequent scans. Sensor noise influences the algorithm with smaller cell sizes as well. Choosing a proper cell size depends on the scale of your environment and the input data.

## MaxIterations - Maximum number of iterations

400 (default) | scalar integer
Maximum number of iterations, specified as the comma-separated pair consisting of
"MaxIterations" and a scalar integer. A larger number of iterations results in more accurate pose estimates, but at the expense of longer execution time.

## ScoreTolerance - Lower bounds on the change in NDT score <br> 1e-6 (default) | numeric scalar

Lower bound on the change in NDT score, specified as the comma-separated pair consisting of "ScoreTolerance" and a numeric scalar. The NDT score is stored in the Score field of the output stats structure. Between iterations, if the score changes by less than this tolerance, the algorithm converges to a solution. A smaller tolerance results in more accurate pose estimates, but requires a longer execution time.

## Output Arguments

## pose - Pose of current scan

[x y theta]
Pose of current scan relative to the reference scan, returned as [ $x$ y theta], where [ $x y$ ] is the translation in meters and theta is the rotation in radians.

## stats - Scan matching statistics

structure
Scan matching statistics, returned as a structure with the following fields:

- Score - Numeric scalar representing the NDT score while performing scan matching. This score is an estimate of the likelihood that the transformed current scan matches the reference scan. Score is always nonnegative. Larger scores indicate a better match.
- Hessian - 3-by-3 matrix representing the Hessian of the NDT cost function at the given pose solution. The Hessian is used as an indicator of the uncertainty associated with the pose estimate.


## References

[1] Biber, P., and W. Strasser. "The Normal Distributions Transform: A New Approach to Laser Scan Matching." Intelligent Robots and Systems Proceedings. 2003.
[2] Magnusson, Martin. "The Three-Dimensional Normal-Distributions Transform -- an Efficient Representation for Registration, Surface Analysis, and Loop Detection." PhD Dissertation. Örebro University, School of Science and Technology, 2009.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder ${ }^{\mathrm{TM}}$.
Code generation is supported for the default SolverAlgorithm, "trust-region". You cannot use the "fminunc" algorithm in code generation.

## See Also

## Functions

matchScansGrid|matchScansLine|transformScan|lidarScan
Classes
occupancyMap | monteCarloLocalization
Topics
"Estimate Robot Pose with Scan Matching"
Introduced in R2019b

## matchScansGrid

Estimate pose between two lidar scans using grid-based search

## Syntax

```
pose = matchScansGrid(currScan,refScan)
[pose,stats] = matchScansGrid )
```

$\qquad$

``` ,Name, Value)
```

```
[
```

[
] = matchScansGrid

```
    ] = matchScansGrid
```


## Description

pose $=$ matchScansGrid(currScan, refScan) finds the relative pose between a reference lidarScan and a current lidarScan object using a grid-based search. matchScansGrid converts lidar scan pairs into probabilistic grids and finds the pose between the two scans by correlating their grids. The function uses a branch-and-bound strategy to speed up computation over large discretized search windows.
[pose,stats] = matchScansGrid( ___ ) returns additional statistics about the scan match result using the previous input arguments.
[__] = matchScansGrid (_, Name, Value) specifies options using one or more Name, Value pair arguments. For example, ' $\overline{\text { InitialPose' , [1 }} 11 \mathrm{pi} / 2]$ specifies an initial pose estimate for scan matching.

## Examples

## Match Scans Using Grid-Based Search

Perform scan matching using a grid-based search to estimate the pose between two laser scans. Generate a probabilistic grid from the scans and estimate the pose difference from those grids.

Load the laser scan data. These two scans are from an actual lidar sensor with changes in the robot pose and are stored as lidarScan objects.

```
load laserScans.mat scan scan2
plot(scan)
hold on
plot(scan2)
hold off
```



Use matchScansGrid to estimate the pose between the two scans.
relPose $=$ matchScansGrid(scan2,scan);
Using the estimated pose, transform the current scan back to the reference scan. The scans overlap closely when you plot them together.

```
scan2Tformed = transformScan(scan2,relPose);
plot(scan)
hold on
plot(scan2Tformed)
hold off
```


## LiDAR Scan



## Input Arguments

## currScan - Current lidar scan readings

lidarScan object
Current lidar scan readings, specified as a lidarScan object.
Your lidar scan can contain Inf and NaN values, but the algorithm ignores them.

## refScan - Reference lidar scan readings

lidarScan object
Reference lidar scan readings, specified as a lidarScan object.
Your lidar scan can contain Inf and NaN values, but the algorithm ignores them.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: 'InitialPose',[1 1 pi/2]

## InitialPose - Initial guess of current pose

[0 0 0] (default)|[x y theta]
Initial guess of the current pose relative to the reference laser scan, specified as the commaseparated pair consisting of 'InitialPose' and an [x y theta] vector. [x $y$ ] is the translation in meters and theta is the rotation in radians.

## Resolution - Grid cells per meter

20 (default) | positive integer
Grid cells per meter, specified as the comma-separated pair consisting of 'Resolution' and a positive integer. The accuracy of the scan matching result is accurate up to the grid cell size.

## MaxRange - Maximum range of lidar sensor

8 (default) | positive scalar
Maximum range of lidar sensor, specified as the comma-separated pair consisting of 'MaxRange ' and a positive scalar.

## TranslationSearchRange - Search range for translation

[4 4] (default) |[x y] vector
Search range for translation, specified as the comma-separated pair consisting of 'TranslationSearchRange' and an [x y] vector. These values define the search window in meters around the initial translation estimate given in InitialPose. If the InitialPose is given as [ $x 0 \mathrm{y} 0$ ], then the search window coordinates are [ $x 0-x \quad x 0+x$ ] and [ $y 0-y \quad y 0+y$ ]. This parameter is used only when InitialPose is specified.

## RotationSearchRange - Search range for rotation

## pi/4 (default) | positive scalar

Search range for rotation, specified as the comma-separated pair consisting of
'RotationSearchRange' and a positive scalar. This value defines the search window in radians around the initial rotation estimate given in InitialPose. If the InitialPose rotation is given as th0, then the search window is [th0-a th0+a], where a is the rotation search range. This parameter is used only when InitialPose is specified.

## Output Arguments

## pose - Pose of current scan

[x y theta] vector
Pose of current scan relative to the reference scan, returned as an [ x y theta] vector, where [ x $y$ ] is the translation in meters and theta is the rotation in radians.

## stats - Scan matching statistics

structure
Scan matching statistics, returned as a structure with the following field:

- Score - Numeric scalar representing the score while performing scan matching. This score is an estimate of the likelihood that the transformed current scan matches the reference scan. Score is always nonnegative. Larger scores indicate a better match, but values vary depending on the lidar data used.
- Covariance - Estimated covariance representing the confidence of the computed relative pose, returned as a 3-by-3 matrix.


## References

[1] Hess, Wolfgang, Damon Kohler, Holger Rapp, and Daniel Andor. "Real-Time Loop Closure in 2D LIDAR SLAM." 2016 IEEE International Conference on Robotics and Automation (ICRA). 2016.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

## Functions

matchScans|matchScansLine|lidarScan|transformScan
Classes
lidarSLAM

## Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
"Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
Introduced in R2019b

## matchScansLine

Estimate pose between two laser scans using line features

## Syntax

```
relpose = matchScansLine(currScan,refScan,initialRelPose)
[relpose,stats] = matchScansLine(
[relpose,stats,debugInfo] = matchScansLine(
```

$\qquad$

``` )
[___] = matchScansLine( ___ ,Name,Value)
```


## Description

relpose = matchScansLine(currScan,refScan,initialRelPose) estimates the relative pose between two scans based on matched line features identified in each scan. Specify an initial guess on the relative pose, initialRelPose.
[relpose,stats] = matchScansLine( __ ) returns additional information about the covariance and exit condition in stats as a structure using the previous inputs.
[relpose,stats,debugInfo] = matchScansLine( $\qquad$ ) returns additional debugging info, debugInfo, from the line-based scan matching result.
$\qquad$ ] = matchScansLine( $\qquad$ ,Name, Value) specifies options using one or more Name, Value pair arguments.

## Examples

## Estimate Pose of Scans with Line Features

This example shows how to use the matchScansLine function to estimate the relative pose between lidar scans given an initial estimate. The identified line features are visualized to show how the scanmatching algorithm associates features between scans.

Load a pair of lidar scans. The .mat file also contains an initial guess of the relative pose difference, initGuess, which could be based on odometry or other sensor data.

```
load tb3 scanPair.mat
plot(s1)
hold on
plot(s2)
hold off
```


## LiDAR Scan



Set parameters for line feature extraction and association. The noise of the lidar data determines the smoothness threshold, which defines when a line break occurs for a specific line feature. Increase this value for more noisy lidar data. The compatibility scale determines when features are considered matches. Increase this value for looser restrictions on line feature parameters.

```
smoothnessThresh = 0.2;
compatibilityScale = 0.002;
```

Call matchScansLine with the given initial guess and other parameters specified as name-value pairs. The function calculates line features for each scan, attempts to match them, and uses an overall estimate to get the difference in pose.

```
[relPose, stats, debugInfo] = matchScansLine(s2, s1, initGuess, ...
    'SmoothnessThreshold', smoothnessThresh, ...
    'CompatibilityScale', compatibilityScale);
```

After matching the scans, the debugInfo output gives you information about the detected line feature parameters, [rho alpha], and the hypothesis of which features match between scans.
debugInfo. MatchHypothesis states that the first, second, and sixth line feature in s1 match the fifth, second, and fourth features in s2.

```
debugInfo.MatchHypothesis
ans = 1\times6
    5
```

The provided helper function plots these two scans and the features extracted with labels. $\mathbf{s 2}$ is transformed to be in the same frame based on the initial guess for relative pose.

```
exampleHelperShowLineFeaturesInScan(s1, s2, debugInfo, initGuess);
```



Use the estimated relative pose from matchScansLine to transform s2. Then, plot both scans to show that the relative pose difference is accurate and the scans overlay to show the same environment.

```
s2t = transformScan(s2,relPose);
```

clf
plot(s1)
hold on
plot(s2t)
hold off


## Input Arguments

## currScan - Current lidar scan readings

lidarScan object
Current lidar scan readings, specified as a lidarScanobject.
Your lidar scan can contain Inf and NaN values, but the algorithm ignores them.
refScan - Reference lidar scan readings
lidarScan object
Reference lidar scan readings, specified as a lidarScan object.
Your lidar scan can contain Inf and NaN values, but the algorithm ignores them.
initialRelPose - Initial guess of relative pose
[x y theta]
Initial guess of the current pose relative to the reference laser scan frame, specified an [ $x y$ theta] vector. [ $x y$ ] is the translation in meters and theta is the rotation in radians.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: "LineMergeThreshold", [0.10 0.2]
SmoothnessThreshold - Threshold to detect line break points in scan
0.1 (default) | scalar

Threshold to detect line break points in scan, specified as a scalar. Smoothness is defined by calling diff(diff(scanData)) and assumes equally spaced scan angles. Scan points corresponding to smoothness values higher than this threshold are considered break points. For lidar scan data with a higher noise level, increase this threshold.

## MinPointsPerLine - Minimum number of scan points in each line feature <br> 10 (default) | positive integer greater than 3

Minimum number of scan points in each line feature, specified as a positive integer greater than 3.
A line feature cannot be identified from a set of scan points if the number of points in that set is below this threshold. When the lidar scan data is noisy, setting this property too small may result in low-quality line features being identified and skew the matching result. On the other hand, some key line features may be missed if this number is set too large.

## LineMergeThreshold - Threshold on line parameters to merge line features <br> [0.05 0.1] (default)|two-element vector [rho alpha]

Threshold on line parameters to merge line features, specified as a two-element vector [rho alpha]. A line is defined by two parameters:

- rho -- Distance from the origin to the line along a vector perpendicular to the line, specified in meters.
- alpha -- Angle between the $x$-axis and the rho vector, specified in radians.

If the difference between these parameters for two line features is below the given threshold, the line features are merged.

## MinCornerPromenance - Lower bound on prominence value to detect a corner 0.05 (default) | positive scalar

Lower bound on prominence value to detect a corner, specified as a positive scalar.
Prominence measures how much a local extrema stands out in the lidar data. Only values higher than this lower bound are considered a corner. Corners help identify line features, but are not part of the feature itself. For noisy lidar scan data, increase this lower bound.

## CompatibilityScale - Scale used to adjust the compatibility thresholds for feature association

0.0005 (default) | positive scalar

Scale used to adjust the compatibility thresholds for feature association, specified as a positive scalar. A lower scale means tighter compatibility threshold for associating features. If no features are found
in lidar data with obvious line features, increase this value. For invalid feature matches, reduce this value.

## Output Arguments

## relpose - Pose of current scan

[ x y theta]
Pose of current scan relative to the reference scan, returned as [ $x$ y theta], where [ $x y$ ] is the translation in meters and theta is the rotation in radians.

## stats - Scan matching information

structure
Scan matching information, returned as a structure with the following fields:

- Covariance -- 3-by-3 matrix representing the covariance of the relative pose estimation. The matScansLine function does not provide covariance between the ( $x, y$ ) and the theta components of the relative pose. Therefore, the matrix follows the pattern: [Cxx, Cxy 0; Cyx Cyy 0; 00 Ctheta].
- ExitFlag -- Scalar value indicating the exit condition of the solver:
- 0 -- No error.
- 1 -- Insufficient number of line features $(<2)$ are found in one or both of the scans. Consider using different scans with more line features.
- 2 -- Insufficient number of line feature matches are identified. This may indicate the initialRelPose is invalid or scans are too far apart.


## debugInfo - Debugging information for line-based scan matching result

structure
Debugging information for line-based scan matching result, returned as a structure with the following fields:

- ReferenceFeatures -- Line features extracted from the reference scan as an $n$-by-2 matrix. Each line feature is represented as [rho alpha] for the parametric equation, $r h o=x \cdot \cos (a l p h a)$ $+y \cdot \sin ($ alpha $)$.
- ReferenceScanMask -- Mask indicating which points in the reference scan are used for each line feature as an $n$-by- $p$ matrix. Each row corresponds to a row in ReferenceFeatures and contains zeros and ones for each point in refScan.
- CurrentFeatures -- Line features extracted from the current scan as an $n$-by- 2 matrix. Each line feature is represented as [rho alpha] for the parametric equation, $r h o=x \cdot \cos (a l p h a)+$ $y \cdot \sin (a l p h a)$.
- CurrentScanMask -- Mask indicating which points in the current scan are used for each line feature as an $n$-by- $p$ matrix. Each row corresponds to a row in ReferenceFeatures and contains zeros and ones for each point in refScan.
- MatchHypothesis -- Best line feature matching hypothesis as an $n$ element vector, where $n$ is the number of line features in CurrentFeatures. Each element represents the corresponding feature in ReferenceFeaturesand gives the index of the matched feature in ReferenceFeatures is an index match the
- MatchValue -- Scalar value indicating a score for each MatchHypothesis. A lower value is considered a better match. If two elements of MatchHypothesis have the same index, the feature with a lower score is used.


## References

[1] Neira, J., and J.d. Tardos. "Data Association in Stochastic Mapping Using the Joint Compatibility Test." IEEE Transactions on Robotics and Automation 17, no. 6 (2001): 890-97. https:// doi.org/10.1109/70.976019.
[2] Shen, Xiaotong, Emilio Frazzoli, Daniela Rus, and Marcelo H. Ang. "Fast Joint Compatibility Branch and Bound for Feature Cloud Matching." 2016 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS), 2016. https://doi.org/10.1109/iros.2016.7759281.

## See Also

matchScans|matchScansGrid|lidarSLAM

## Topics

"Estimate Robot Pose with Scan Matching"
"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
Introduced in R2020a

## optimizePath

Optimize path while maintaining safe distance from obstacle

## Syntax

```
optPath = optimizePath(path)
optPath = optimizePath(path,map)
optPath = optimizePath(path,options)
optPath = optimizePath(path,map,options)
[optPath,kineticInfo] = optimizePath( ___)
[optPath,kineticInfo,solutionInfo] = optimizePath(
```

$\qquad$

## Description

optPath = optimizePath(path) optimizes the travel time and smoothness of the specified path for car-like robots in an empty map for the default parameters. The number of states in the optPath can be different than in the path.
optPath = optimizePath(path,map) optimizes the path in the specified map for the default parameters. The returned optimized path optPath tries to maintain a safety margin to obstacles in the map map.
optPath = optimizePath(path,options) optimizes the path in an empty map by parameters specified in options. Parameters related to trajectory, obstacle, and solver, along with the weights of those parameters can be specified in options as an optimizePathOptions object.
optPath = optimizePath(path, map,options) optimizes the path in the specified map for by parameters specified in options.
[optPath, kineticInfo] = optimizePath( _ _ ) also returns kineticInfo as a structure that contains the kinetic information of the optimized path.
[optPath,kineticInfo,solutionInfo] = optimizePath( $\qquad$ ) also returns solutionInfo as a structure that contains the solution information of the optimized path.

## Examples

## Optimize Planned Path

## Setup Environment

Load a map into the workspace.

```
map = load("exampleMaps.mat").complexMap;
```

Create a binary occupancy map.

```
map = binaryOccupancyMap(map);
```

Create a state validator object.

```
stateValidator = validatorOccupancyMap;
```

Assign the map to the state validator object.

```
stateValidator.Map = map;
```

Set the validation distance for the validator.

```
stateValidator.ValidationDistance = 0.01;
```


## Plan Path

Initialize the plannerHybridAStar object with the state validator object. Specify the MinTurningRadius property of the planner as 2 meters.

```
planner = plannerHybridAStar(stateValidator,MinTurningRadius=2);
```

Define start and goal poses as [x y theta] vectors. $x$ and $y$ specify the position in meters, and theta specifies the orientation angle in radians.

```
start = [6 3 pi/2];
goal = [32 32 0];
```

Plan a path from the start pose to the goal pose.

```
path = plan(planner,start,goal);
inpath = path.States;
```


## Optimize Path

Configure options for optimization.

```
options = optimizePathOptions
options =
optimizePathOptions
```

    Trajectory Parameters
                MaxPathStates: 200
            ReferenceDeltaTime: 0.3000
            MinTurningRadius: 1
                    MaxVelocity: 0.4000
            MaxAngularVelocity: 0.3000
                    MaxAcceleration: 0.5000
        MaxAngularAcceleration: 0.5000
    Obstacle Parameters
            ObstacleSafetyMargin: 0.5000
            ObstacleCutOffDistance: 2.5000
        ObstacleInclusionDistance: 0.7500
    Solver Parameters
                            NumIteration: 4
            MaxSolverIteration: 15
    Weights
                WeightTime: 10
            WeightSmoothness: 1000
        WeightMinTurningRadius: 10
    $$
\begin{aligned}
\text { WeightVelocity: } & 100 \\
\text { WeightAngularVelocity: } & 10 \\
\text { WeightAcceleration: } & 10 \\
\text { WeightAngularAcceleration: } & 10 \\
\text { Weight0bstacles: } & 50
\end{aligned}
$$

Set the minimum turning radius value as same as in the planner.
options.MinTurningRadius = 2;
Specify the maximum number of poses allowed in the optimized path.
options.MaxPathStates = size(inpath,1) * 3;
Maintain a safe distance of 0.75 meters from the obstacles.
options.ObstacleSafetyMargin = 0.75;
Optimize the path generated by the planner.
optpath = optimizePath(inpath,map,options);

## Visualize

Visualize input path and optimized path in the map.

```
show(map)
hold on
quiver(inpath(:,1),inpath(:,2),cos(inpath(:,3)),sin(inpath(:,3)),0.1);
quiver(optpath(:,1),optpath(:,2),cos(optpath(:,3)),sin(optpath(:,3)),0.1);
legend("Input Path","Optimized Path")
```



## Input Arguments

## path - Path states

real-valued $M$-by-2 matrix of the form $[x y] \mid$ real-valued $M$-by-3 matrix of the form [x y theta]
Path states, specified as a real-valued $M$-by-2 matrix of the form [ $x y$ ] or $M$-by- 3 matrix of the form [ $x$ $y$ theta]. $x$ and $y$ specify the position in meters. theta specifies the orientation in radians. $M$ is the number of states in the path. The number of states in the path must be greater than or equal to 3 .
Data Types: single | double

## map - Map representation

binaryOccupancyMap object | occupancyMap object | vehicleCostMap object
Map representation, specified as a binary0ccupancyMap, occupancyMap, or vehicleCostmap object. This object represents the environment of the vehicle.

## options - Optimization options

optimizePathOptions object
Optimization options, specified as optimizePath0ptions object.

## Output Arguments

## optPath - Optimized path

real-valued $N$-by-2 matrix of the form $[x y] \mid$ real-valued $N$-by- 3 matrix of the form $[x$ y theta]

Path states, returned as a real-valued $N$-by-2 matrix of the form [ $x y$ ] or $N$-by-3 matrix of the form [xy theta]. $x$ and $y$ specify the position in meters. theta specifies the orientation in radians. $N$ is the number of states in the path. The number of states in the optPath can be different than in the path.

## kineticInfo - Kinetic Information

structure
Kinetic Information, returned as a structure. The fields of the structure are:
Fields of kineticInfo

| Fields | Description |
| :--- | :--- |
| TimeStamps | Time corresponding to the pose in the optimized <br> path. |
| Velocity | Velocity to travel between two consecutive poses. |
| AngularVelocity | Angular Velocity between two consecutive poses. |

Data Types: struct

## solutionInfo - Solution Information

structure
Solution Information, returned as a structure. The fields of the structure are:
Fields of solutionInfo

| Fields | Description |
| :--- | :--- |
| NumIterations | Number of iterations performed. |
| Cost | Final cost of the path. |

Data Types: struct

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.

See Also<br>optimizePathOptions

Introduced in R2022a

## optimizePoseGraph

Optimize nodes in pose graph

## Syntax

```
updatedGraph = optimizePoseGraph(poseGraph)
updatedGraph = optimizePoseGraph(poseGraph,solver)
[updatedGraph,solutionInfo] = optimizePoseGraph(___)
[
    ] = optimizePoseGraph(
```

$\qquad$

``` ,Name, Value)
```


## Description

updatedGraph = optimizePoseGraph(poseGraph) adjusts the poses based on their edge constraints defined in the specified graph to improve the overall graph. You optimize either a 2-D or 3-D pose graph. The returned pose graph has the same topology with updated nodes.

This pose graph optimization assumes all edge constraints and loop closures are valid. To consider trimming edges based on bad loop closures, see the trimLoopClosures function.
updatedGraph = optimizePoseGraph(poseGraph,solver) specifies the solver type for optimizing the pose graph.
[updatedGraph,solutionInfo] = optimizePoseGraph( __ ) returns additional statistics about the optimization process in solutionInfo using any of the previous syntaxes.
[___ ] = optimizePoseGraph (__ ,Name,Value) specifies additional options using one or more Name, Value pairs. For example, 'MaxIterations ' , 1000 increases the maximum number of iterations to 1000.

## Examples

## Optimize a 3-D Pose Graph

Optimize a pose graph based on the nodes and edge constraints. The pose graph used in this example is taken from the MIT Dataset and was generated using information extracted from a parking garage.

Load the pose graph from the MIT dataset. Inspect the poseGraph3D object to view the number of nodes and loop closures.

```
load parking-garage-posegraph.mat pg
disp(pg);
    poseGraph3D with properties:
            NumNodes: 1661
            NumEdges: 6275
    NumLoopClosureEdges: 4615
        LoopClosureEdgeIDs: [\begin{array}{lllllllllllll}{128}&{129}&{130}&{132}&{133}&{134}&{135}&{137}&{138}&{139}&{140... ]}\end{array}]
            LandmarkNodeIDs: [1x0 double]
```

Plot the pose graph with IDs off. Red lines indicate loop closures identified in the dataset.

```
title('Original Pose Graph')
show(pg,'IDs','off');
view(-30,45)
```



Optimize the pose graph. Nodes are adjusted based on the edge constraints and loop closures. Plot the optimized pose graph to see the adjustment of the nodes with loop closures.

```
updatedPG = optimizePoseGraph(pg);
figure
title('Updated Pose Graph')
show(updatedPG,'IDs','off');
view(-30,45)
```



## Input Arguments

## poseGraph - 2-D or 3-D pose graph

poseGraph object | poseGraph3D object | digraph object
2-D or 3-D pose graph, specified as a poseGraph, poseGraph3D, digraph object.
To use the digraph object, generate the pose graph using createPoseGraph from an imageviewset or pcviewset object. You must have Computer Vision Toolbox ${ }^{\mathrm{TM}}$ and the solver must be set to "builtin-trust-region". The 'LoopClosuresToIgnore' and
' FirstNodePose' name-value pairs are ignored if specified.
The edges of digraph object are described by affine3d or rigid3d objects.

## solver - Pose graph solver

"builtin-trust-region" (default) | "g2o-levenberg-marquardt"
Pose graph solver, specified as either "builtin-trust-region" or "g2o-levenbergmarquardt". To tune either solver, use the name-value pair arguments for that solver.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, ... NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: 'MaxTime', 300

Note Depending on the solver input, the function supports different name-value pairs.

## If the solver input is set to "builtin-trust-region":

MaxTime - Maximum time allowed
500 (default) | positive numeric scalar
Maximum time allowed, specified as the comma-separated pair consisting of 'MaxTime ' and a positive numeric scalar in seconds. The optimizer exits after it exceeds this time.

## GradientTolerance - Lower bound on norm of gradient

0.5e-8 (default) | scalar

Lower bound on the norm of the gradient, specified as the comma-separated pair consisting of 'GradientTolerance' and a scalar. The norm of the gradient is calculated based on the cost function of the optimization. If the norm falls below this value, the optimizer exits.

FunctionTolerance - Lower bound on change in cost function
1e-8 (default) | scalar
Lower bound on the change in the cost function, specified as the comma-separated pair consisting of 'FunctionTolerance ' and a scalar. If the cost function change falls below this value between optimization steps, the optimizer exits.

## StepTolerance - Lower bound on step size <br> 1e-12 (default) | scalar

Lower bound on the step size, specified as the comma-separated pair consisting of
'StepTolerance ' and a scalar. If the norm of the optimization step falls below this value, the optimizer exits.

## InitialTrustRegionRadius - Initial trust region radius <br> 100 (default) | scalar

Initial trust region radius, specified as a scalar.

## VerboseOutput - Display intermediate iteration information

'off' (default)|'on'
Display intermediate iteration information on the MATLAB command line, specified as the commaseparated pair consisting of 'VerboseOutput' and either 'off' or 'on'.

LoopClosuresToIgnore - IDs of loop closure edges in pose graph
vector
IDs of loop closure edges in poseGraph, specified as the comma-separated pair consisting of 'LoopClosuresToIgnore' and a vector. To get edge IDs from the pose graph, use findEdgeID.

FirstNodePose - Pose of first node
[0 0 0] or [0 0 0 1 0 0 0] (default)|[x y theta]|[x y z qw qx qy qz]

Pose of the first node in poseGraph, specified as the comma-separated pair consisting of 'FirstNodePose' and a pose vector.

For poseGraph (2-D), the pose is an [x y theta] vector, which defines the relative $x y$-position and orientation angle, theta.

For poseGraph3D, the pose is an [x y z qw qx qy qz] vector, which defines the relative xyzposition and quaternion orientation, [qw $q x$ qy qz].

Note Many other sources for 3-D pose graphs, including .g2o formats, specify the quaternion orientation in a different order, for example, [qx qy qz qw]. Check the source of your pose graph data before adding nodes to your poseGraph3D object.

## If the solver input is set to "g2o-levenberg-marquardt":

## MaxIterations - Maximum number of iterations

300 (default) | positive integer
Maximum number of iterations, specified as the comma-separated pair consisting of 'MaxIterations ' and a positive integer. The optimizer exits after it exceeds this number of iterations.

## MaxTime - Maximum time allowed

500 (default) | positive numeric scalar
Maximum time allowed, specified as the comma-separated pair consisting of 'MaxTime' and a positive numeric scalar in seconds. The optimizer exits after it exceeds this time.

## FunctionTolerance - Lower bound on change in cost function <br> 1e-8 (default) | scalar

Lower bound on the change in the cost function, specified as the comma-separated pair consisting of 'FunctionTolerance ' and a scalar. If the cost function change falls below this value between optimization steps, the optimizer exits.

## Verbose0utput - Display intermediate iteration information 'off' (default)|'on'

Display intermediate iteration information on the MATLAB command line, specified as the commaseparated pair consisting of 'Verbose0utput' and either 'off' or 'on'.

## LoopClosuresToIgnore - IDs of loop closure edges in pose graph

## vector

IDs of loop closure edges in poseGraph, specified as the comma-separated pair consisting of 'LoopClosuresToIgnore' and a vector. To get edge IDs from the pose graph, use findEdgeID.

## FirstNodePose - Pose of first node

[0 0 0] or [0 001000 ] (default)| 0 [x y theta]|[x y z qw qx qy qz]
Pose of the first node in poseGraph, specified as the comma-separated pair consisting of 'FirstNodePose' and a pose vector.

For poseGraph (2-D), the pose is an [ $\mathrm{x} y$ theta] vector, which defines the relative $x y$-position and orientation angle, theta.

For poseGraph3D, the pose is an [x y z qw qx qy qz] vector, which defines the relative xyzposition and quaternion orientation, [ $q \mathbf{q w} q \mathrm{qy} q \mathrm{z}$ ].

Note Many other sources for 3-D pose graphs, including .g2o formats, specify the quaternion orientation in a different order, for example, [qx qy qz qw]. Check the source of your pose graph data before adding nodes to your poseGraph3D object.

## Output Arguments

## updatedGraph - Optimized 2-D or 3-D pose graph

poseGraph object | poseGraph3D object
Optimized 2-D or 3-D pose graph, returned as a poseGraph or poseGraph3D object.

## solutionInfo - Statistics of optimization process

## structure

Statistics of optimization process, returned as a structure with these fields:

- Iterations - Number of iterations used in optimization.
- ResidualError - Value of cost function when optimizer exits.
- Exit Flag - Exit condition for optimizer:
- 1 - Local minimum found.
- 2 - Maximum number of iterations reached. See MaxIterations name-value pair argument.
- 3-Algorithm timed out during operation.
- 4 - Minimum step size. The step size is below the StepTolerance name-value pair argument.
- 5 - The change in error is below the minimum.
- 8 - Trust region radius is below the minimum set in InitialTrustRegionRadius.


## References

[1] Grisetti, G., R. Kummerle, C. Stachniss, and W. Burgard. "A Tutorial on Graph-Based SLAM." IEEE Intelligent Transportation Systems Magazine. Vol. 2, No. 4, 2010, pp. 31-43. doi:10.1109/ mits.2010.939925.
[2] Carlone, Luca, Roberto Tron, Kostas Daniilidis, and Frank Dellaert. "Initialization Techniques for 3D SLAM: a Survey on Rotation Estimation and its Use in Pose Graph Optimization." 2015 IEEE International Conference on Robotics and Automation (ICRA). 2015, pp. 4597-4604.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

- Use this syntax when constructing poseGraph or poseGraph3D objects for code generation:
poseGraph = poseGraph('MaxNumEdges', maxEdges,'MaxNumNodes', maxNodes) specifies an upper bound on the number of edges and nodes allowed in the pose graph when generating code. This limit is only required when generating code.
- The "g2o-levenberg-marquardt" solver input argument is not supported for code generation.


## See Also

## Functions

trimLoopClosures | addRelativePose | removeEdges | edgeNodePairs |edgeConstraints | findEdgeID|nodeEstimates

## Objects

poseGraph | poseGraph3D | lidarSLAM
Topics
"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
"Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

Introduced in R2019b

## plotTransforms

Plot 3-D transforms from translations and rotations

## Syntax

```
ax = plotTransforms(translations,rotations)
ax = plotTransforms(translations,rotations,Name,Value)
```


## Description

ax = plotTransforms(translations, rotations) draws transform frames in a 3-D figure window using the specified translations and rotations. The $z$-axis always points upward.
ax = plotTransforms(translations, rotations,Name,Value) specifies additional options using name-value pair arguments. Specify multiple name-value pairs to set multiple options.

## Input Arguments

## translations - xyz-positions

$\left[\begin{array}{lll}x & y & z\end{array}\right]$ vector | matrix of $[x y z]$ vectors
$x y z$-positions specified as a vector or matrix of $\left[\begin{array}{lll}x & y & z\end{array}\right]$ vectors. Each row represents a new frame to plot with a corresponding orientation in rotations.

```
Example: [1 1 1; 222 ]
```

rotations - Rotations of $\boldsymbol{x y z}$-positions
quaternion array | matrix of [w x y z] quaternion vectors
Rotations of $x y z$-positions specified as a array or $n$-by-4 matrix of [w $\left.\begin{array}{ll} & x \\ y & z\end{array}\right]$ quaternion vectors. Each element of the array or each row of the matrix represents the rotation of the $x y z$-positions specified in translations.
Example: [1 1 1 0; 1350$]$

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: 'FrameSize',5

## FrameSize - Size of frames and attached meshes

positive numeric scalar
Size of frame and attached meshes, specified as positive numeric scalar.

## InertialZDirection - Direction of positive $\boldsymbol{z}$-axis of inertial frame "up" (default) | "down"

Direction of the positive $z$-axis of inertial frame, specified as either "up" or "down". In the plot, the positive $z$-axis always points up.

## MeshFilePath - File path of mesh file attached to frames <br> character vector | string scalar

File path of mesh file attached to frames, specified as either a character vector or string scalar. The mesh is attached to each plotted frame at the specified position and orientation. Provided .stl are

- "fixedwing.stl"
- "multirotor.stl"
- "groundvehicle.stl"

Example: 'fixedwing.stl'

## MeshColor - Color of attached mesh

"red" (default) | RGB triplet | string scalar
Color of attached mesh, specified as an RGB triplet or string scalar.
Example: [0 0 1] or "green"

## Parent - Axes used to plot transforms

Axes object | UIAxes object
Axes used to plot the pose graph, specified as the comma-separated pair consisting of 'Parent ' and either an Axes or UIAxes object. See axes or uiaxes.

## Output Arguments

## ax - Axes used to plot transforms

Axes object | UIAxes object
Axes used to plot the pose graph, specified as the comma-separated pair consisting of 'Parent ' and either an Axes or UIAxesobject. See axes or uiaxes.

## See Also

quaternion | hom2cart | eul2quat | tform2quat | rotm2quat

## Introduced in R2018b

## poseGraphSolverOptions

Solver options for pose graph optimization

## Syntax

solverOptions = poseGraphSolverOptions(solverType)

## Description

solverOptions = poseGraphSolverOptions(solverType) returns the set of solver options with default values for the specified pose graph solver type.

## Examples

## Optimize and Trim Loop Closures For 2-D Pose Graphs

Optimize a pose graph based on the nodes and edge constraints. Trim loop closed based on their edge residual errors.

Load the data set that contains a 2-D pose graph. Inspect the poseGraph object to view the number of nodes and loop closures.

```
load grid-2d-posegraph.mat pg
disp(pg)
poseGraph with properties:
    NumNodes: 120
    NumEdges: 193
    NumLoopClosureEdges: 74
    LoopClosureEdgeIDs: [120 121 122 123 124 125 126 127 128 129 130 ... ]
            LandmarkNodeIDs: [1x0 double]
```

Plot the pose graph with IDs off. Red lines indicate loop closures identified in the dataset. The poses in the graph should follow a grid pattern, but show evidence of drift over time.

```
show(pg,'IDs','off');
title('Original Pose Graph')
```



Optimize the pose grap using the optimizePoseGraph function. By default, this function uses the "builtin-trust-region" solver. Because the pose graph contains some bad loop closures, the resulting pose graph is actual not desirable.
pgOptim $=$ optimizePoseGraph(pg);
figure;
show(pgOptim);


Look at the edge residual errors for the original pose graph. Large outlier error values at the end indicate bad loop closures.

```
resErrorVec = edgeResidualErrors(pg);
plot(resErrorVec);
title('Edge Residual Errors by Edge ID')
```



Certain loop closures should be trimmed from the pose graph based on their residual error. Use the trimLoopClosures function to trim therse bad loop closures. Set the maximum and truncation threshold for the trimmer parameters. This threshold is set based on the measurement accuracy and should be tuned for your system.
trimParams.MaxIterations $=100$;
trimParams.TruncationThreshold = 25;
solverOptions = poseGraphSolverOptions;
Use the trimLoopClosures function with the trimmer parameters and solver options.

```
[pgNew, trimInfo, debugInfo] = trimLoopClosures(pg,trimParams,solverOptions);
```

From the trimInfo output, plot the loop closures removed from the optimized pose graph. By plotting with the residual errors plot before, you can see the large error loop closures were removed.

```
removedLCs = trimInfo.LoopClosuresToRemove;
hold on
plot(removedLCs,zeros(length(removedLCs)),'or')
title('Edge Residual Errors and Removed Loop Closures')
legend('Residual Errors', 'Removed Loop Closures')
xlabel('Edge IDs')
ylabel('Edge Residual Error')
hold off
```



Show the new pose graph with the bad loop closures trimmed.
show(pgNew, "IDs", "off") ;


## Input Arguments

## solverType - Pose graph solver type

'builtin-trust-region' (default)|'g2o-levenberg-marquardt'
Pose graph sovler type, specified as 'builtin-trust-region' or 'g2o-levenberg-marquardt'.
The function generates a set of solver options with default values for the specified pose graph solver type:

```
pgSolverTrustRegion = poseGraphSolverOptions('builtin-trust-region')
pgSolverTrustRegion =
TrustRegion (builtin-trust-region-dogleg) options:
    MaxIterations: 300
            MaxTime: 10
        FunctionTolerance: 1.0000e-08
        GradientTolerance: 5.0000e-09
            StepTolerance: 1.0000e-12
    InitialTrustRegionRadius: 100
        VerboseOutput: 'off'
pgSolverG2o = poseGraphSolverOptions('g2o-levenberg-marquardt')
```

```
pgSolverG2o =
G2oLevenbergMarquardt (g2o-levenberg-marquardt) options:
    MaxIterations: 300
            MaxTime: 10
    FunctionTolerance: 1.0000e-09
    VerboseOutput: 'off'
Data Types: char|string
```


## Output Arguments

## solverOptions - Pose graph solver options

poseGraphSolver0ptions parameters
Pose graph solver options, specified as a set of parameters generated by calling the poseGraphSolverOptions function. The function generates a set of solver options with default values for the specified pose graph solver type.

If the solverType input is set to "builtin-trust-region":

|  | Default | Description |
| :--- | :--- | :--- |
| MaxIterations | 300 | Maximum number of iterations, <br> specified as a positive integer. <br> The optimizer exits after it <br> exceeds this number of <br> iterations. |
| MaxTime | 500 | Maximum time allowed, <br> specified as a positive numeric <br> scalar in seconds. The optimizer <br> exits after it exceeds this time. |
| FunctionTolerance | $1 \mathrm{e-8}$ | Lower bound on the change in <br> the cost function, specified as a <br> scalar. If the cost function <br> change falls below this value <br> between optimization steps, the <br> optimizer exits. |
| GradientTolerance | $0.5 \mathrm{e}-8$ | Lower bound on the norm of the <br> gradient, specified as a scalar. <br> The norm of the gradient is <br> calculated based on the cost <br> function of the optimization. If <br> the norm falls below this value, <br> the optimizer exits. |
| StepTolerance | $1 \mathrm{e}-12$ | Lower bound on the step size, <br> specified as a scalar. If the norm <br> of the optimization step falls <br> below this value, the optimizer <br> exits. |
| InitialTrustRegionRadius | 100 | Initial trust region radius, <br> specified as a scalar. |
| VerboseOutput | 'off' or ' on ' | Display intermediate iteration <br> information on the MATLAB <br> command line. |

If the solver input is set to "g2o-levenberg-marquardt":

|  | Default | Description |
| :--- | :--- | :--- |
| MaxIterations | 300 | Maximum number of iterations, <br> specified as a positive integer. <br> The optimizer exits after it <br> exceeds this number of <br> iterations. |
| MaxTime | 500 | Maximum time allowed, <br> specified as a positive numeric <br> scalar in seconds. The optimizer <br> exits after it exceeds this time. |
| FunctionTolerance | $1 \mathrm{e-8}$ | Lower bound on the change in <br> the cost function, specified as a <br> scalar. If the cost function <br> change falls below this value <br> between optimization steps, the <br> optimizer exits. |
| VerboseOutput | 'off' or ' on' | Display intermediate iteration <br> information on the MATLAB <br> command line. |

## See Also

## Functions

trimLoopClosures|edgeResidualErrors|edgeResidualErrors| removeEdges |
edgeNodePairs |edgeConstraints

## Objects

poseGraph | poseGraph3D | lidarSLAM

## Introduced in R2020b

## poseplot

3-D pose plot

## Syntax

```
poseplot
poseplot(quat)
poseplot(R)
poseplot(___,position)
poseplot(___,frame)
poseplot(___,Name=Value)
poseplot(ax,
```

$\qquad$

```
p = poseplot
```

$\qquad$

``` )
```


## Description

poseplot plots the pose (position and orientation) at the coordinate origin position with zero rotation. The default navigation frame is the north-east-down (NED) frame.
poseplot (quat) plots the pose with orientation specified by a quaternion quat. The position by default is [0 0 0].
poseplot (R) plots the pose with orientation specified by a rotation matrix $R$. The position by default is [0 0 0].
poseplot (__ , position) specifies the position of the pose plot.
poseplot (__ , frame) specifies the navigation frame of the pose plot.
poseplot (__, Name=Value) specifies pose patch properties using one or more name-value arguments. For example, poseplot (PatchFaceColor="r") plots the pose with red face color. For a list of properties, see PosePatch Properties.
poseplot(ax, $\qquad$ ) specifies the parent axes of the pose plot.
p = poseplot( $\qquad$ ) returns the PosePatch object. Use $p$ to modify properties of the pose patch after creation. For a list of properties, see PosePatch Properties.

## Examples

## Visualize Pose Using poseplot

Plot the default pose using the poseplot function with default settings.

```
poseplot
xlabel("North-x (m)")
ylabel("East-y (m)")
zlabel("Down-z (m)");
```



Next, plot a pose with specified orientation and position.

```
q = quaternion([35 10 50],"eulerd","ZYX","frame");
position = [1 1 1];
poseplot(q,position)
```



Then, plot a second pose on the figure and return the PosePatch object. Plot the second pose with a smaller size by using the ScaleFactor name-value argument.
hold on
p = poseplot(eye(3),[5 5 5],ScaleFactor=0.5)
p =
PosePatch with properties:
Orientation: [3x3 double]
Position: [5 5 5]
Show all properties
legend("First Pose","Second Pose")
hold off


| $\square$ |
| :--- |
| First Pose |
| $\square$ |
| Second Pose |

## Animate Pose Using poseplot

Animate a series of poses using the poseplot function. First, define the initial and final positions.
$\mathrm{ps}=\left[\begin{array}{lll}0 & 0 & 0\end{array}\right] ;$
$\mathrm{pf}=\left[\begin{array}{ccc}10 & 0 & 0\end{array}\right] ;$
Then, define the initial and final orientations using the quaternion object.

```
qs = quaternion([45,0,0],'eulerd','ZYX','frame');
qf = quaternion([-45,0,0],'eulerd','ZYX','frame');
```

Show the starting pose.

```
patch = poseplot(qs,ps);
ylim([-2 2])
xlim([-2 12])
xlabel("North-x (m)")
ylabel("East-y (m)")
zlabel("Down-z (m)");
```



Change the position and orientation continuously using coefficients, and update the pose using the set object function.

```
for coeff = 0:0.01:1
    q = slerp(qs,qf,coeff);
    position = ps + (pf - ps)*coeff;
    set(patch,Orientation=q,Position=position);
    drawnow
end
```



## Show Poses with Meshes

Plot orientations and positions in meshes using the poseplot function. First, plot a ground vehicle at the origin with zero rotation.

```
poseplot(ones("quaternion"),[0 0 0],MeshFileName="groundvehicle.stl",ScaleFactor=0.3);
xlabel("North-x (m)")
ylabel("East-y (m)")
zlabel("Down-z (m)")
```



Second, plot a rotor at the position [ 20 20 -20] with zero rotation.
hold on
poseplot(ones("quaternion"),[20 20-20],MeshFileName="multirotor.stl",ScaleFactor=0.2);


Lastly, plot a fixed-wing aircraft at the position [5 5 - 40 $]$ ] with zero rotation.
poseplot(ones("quaternion"),[5 5 -40],MeshFileName="fixedwing.stl",ScaleFactor=0.4); view([-37.8 28.4])
hold off


## Input Arguments

quat - Quaternion
quaternion object
Quaternion, specified as a quaternion object.

## R - Rotation matrix

3-by-3 orthonormal matrix
Rotation matrix, specified as a 3-by-3 orthonormal matrix.
Example: eye (3)

## position - Position of pose plot

three-element real-valued vector
Position of the pose plot, specified as a three-element real-valued vector.
Example: [1 3 4 4$]$

## frame - Navigation frame of pose plot

"NED" (default) | "ENU"
Navigation frame of the pose plot, specified as "NED" for the north-east-down frame or "ENU" for the east-north-up frame.

When the parent axes status is hold off, specifying the NED navigation frame reverses the $y$ - and $z$ axes in the figure by setting the YDir and ZDir properties of the parent axes.

## ax - Parent axes of pose plot

Axes object
Parent axes of the pose plot, specified as an Axes object. If you do not specify the axes, the poseplot function uses the current axes.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, . . . ,NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

The PosePatch properties listed here are only a subset. For a complete list, see PosePatch Properties.

Example: poseplot (PatchFaceAlpha=0.1)
Orientation - Orientation of pose plot
quaternion object (default) | rotation matrix
Orientation of the pose plot, specified as a quaternion object or a rotation matrix.

## Position - Position of pose plot

[0000] (default) | three-element real-valued vector
Position of the pose plot, specified as a three-element real-valued vector.

## MeshFileName - Name of STL mesh file

## string scalar | character vector

Name of Standard Triangle Language (STL) mesh file, specified as a string scalar or a character vector containing the name of the mesh file. When you specify this argument, the poseplot function plots the mesh instead of the orientation box.

## ScaleFactor - Scale factor of pose plot <br> 1 (default) | nonnegative scalar

Scale factor of the pose plot, specified as a nonnegative scalar. The scale factor controls the size of the orientation box. When you specify the MeshFileName argument, the scale factor also changes the scale of the mesh.

## PatchFaceColor - Patch face color

[000] (default) | RGB triplet | hexadecimal color code | "r" | "g" | "b" | ...
Patch face color, specified as an RGB triplet, a hexadecimal color code, a color name, or a short name.

- An RGB triplet is a three-element row vector whose elements specify the intensities of the red, green, and blue components of the color. The intensities must be in the range [0, 1]; for example, [0.4 0.6 0.7].
- A hexadecimal color code is a character vector or a string scalar that starts with a hash symbol (\#) followed by three or six hexadecimal digits, which can range from 0 to $F$. The values are not case sensitive. Thus, the color codes "\#FF8800", "\#ff8800", "\#F80", and "\#f80" are equivalent.

Here is a list of commonly used colors and their corresponding values.

| Color Name | Short Name | RGB Triplet | Hexadecimal <br> Color Code | Appearance |
| :--- | :--- | :--- | :--- | :--- |
| "red" | "r" | $\left[\begin{array}{lll}1 & 0 & 0\end{array}\right]$ | "\#FF0000" |  |
| "green" | "g" | $\left[\begin{array}{lll}0 & 1 & 0\end{array}\right]$ | "\#00FF00" |  |
| "blue" | "b" | $\left[\begin{array}{lll}0 & 0 & 1\end{array}\right]$ | $" \# 0000 F F "$ |  |
| "cyan" | "c" | $\left[\begin{array}{lll}0 & 1 & 1\end{array}\right]$ | $" \# 00 F F F F "$ |  |
| "magenta" | "m" | $\left[\begin{array}{lll}1 & 0 & 1\end{array}\right]$ | "\#FF00FF" |  |
| "yellow" | "y" | $\left[\begin{array}{lll}1 & 1 & 0\end{array}\right]$ | "\#FFFF00" |  |
| "black" | "k" | $\left[\begin{array}{lll}0 & 0 & 0\end{array}\right]$ | "\#000000" |  |
| "white" | "w" | $\left[\begin{array}{lll}1 & 1 & 1\end{array}\right]$ | "\#FFFFFF" | $\square$ |

## PatchFaceAlpha - Patch face transparency

0.1 (default) | scalar in range [0, 1]

Patch face transparency, specified as a scalar in range [0, 1]. A value of 1 is fully opaque and 0 is completely transparent.

## Output Arguments

## p - Pose patch object

PosePatch object
Pose patch object, returned as a PosePatch object. You can use the returned object to query and modify properties of the plotted pose. For a list of properties, see PosePatch Properties.

## See Also

PosePatch Properties

## Introduced in R2021b

## PosePatch Properties

Pose plot appearance and behavior

## Description

PosePatch properties control the appearance and behavior of a PosePatch object. By changing property values, you can modify certain aspects of the pose plot. Use dot notation to query and set properties. To create a PosePatch object, use the poseplot function.

```
p = poseplot;
c = p.PatchFaceColor;
p.PatchFaceColor = "red";
```


## Properties

## Position and Orientation

## Orientation - Orientation of pose plot

quaternion object (default) | rotation matrix
Orientation of the pose plot, specified as a quaternion object or a rotation matrix.

## Position - Position of pose plot

[0 0 0 0 ] (default) | three-element real-valued vector
Position of the pose plot, specified as a three-element real-valued vector.

## Color and Styling

## ScaleFactor - Scale factor of pose plot

1 (default) | nonnegative scalar
Scale factor of the pose plot, specified as a nonnegative scalar. The scale factor controls the size of the orientation box. When you specify the MeshFileName argument, the scale factor also changes the scale of the mesh.

## PatchFaceColor - Patch face color

[0 0 0] (default) | RGB triplet | hexadecimal color code | "r" | "g" | "b" | ...
Patch face color, specified as an RGB triplet, a hexadecimal color code, a color name, or a short name.

- An RGB triplet is a three-element row vector whose elements specify the intensities of the red, green, and blue components of the color. The intensities must be in the range [0, 1]; for example, $[0.4$ 0.6 0.7].
- A hexadecimal color code is a character vector or a string scalar that starts with a hash symbol (\#) followed by three or six hexadecimal digits, which can range from 0 to $F$. The values are not case sensitive. Thus, the color codes "\#FF8800", "\#ff8800", "\#F80", and "\#f80" are equivalent.

Here is a list of commonly used colors and their corresponding values.

| Color Name | Short Name | RGB Triplet | Hexadecimal <br> Color Code | Appearance |
| :--- | :--- | :--- | :--- | :--- |
| "red" | "r" | $\left[\begin{array}{lll}1 & 0 & 0\end{array}\right]$ | "\#FF0000" |  |
| "green" | "g" | $\left[\begin{array}{lll}0 & 1 & 0\end{array}\right]$ | $" \# 00 F F 00 "$ |  |
| "blue" | "b" | $\left[\begin{array}{lll}0 & 0 & 1\end{array}\right]$ | "\#0000FF" |  |
| "cyan" | "c" | $\left[\begin{array}{lll}0 & 1 & 1\end{array}\right]$ | $" \# 00 F F F F "$ |  |
| "magenta" | "m" | $\left[\begin{array}{lll}1 & 0 & 1\end{array}\right]$ | $" \# F F 00 F F "$ |  |
| "yellow" | "y" | $\left[\begin{array}{lll}1 & 1 & 0\end{array}\right]$ | "\#FFFF00" |  |
| "black" | "k" | $\left[\begin{array}{lll}0 & 0 & 0\end{array}\right]$ | "\#000000" |  |
| "white" | "w" | $\left[\begin{array}{lll}1 & 1 & 1\end{array}\right]$ | "\#FFFFFF" |  |

## MeshFileName - Name of STL mesh file

string scalar | character vector
Name of Standard Triangle Language (STL) mesh file, specified as a string scalar or a character vector containing the name of the mesh file. When you specify this argument, the poseplot function plots the mesh instead of the orientation box.

## PatchFaceAlpha - Patch face transparency

0.1 (default) | scalar in range [0, 1]

Patch face transparency, specified as a scalar in range [0, 1]. A value of 1 is fully opaque and 0 is completely transparent.

## Parent/Children

## Parent - Parent axes

Axes object
Parent axes, specified as an Axes object.

## Children - Children

empty GraphicsPlaceholder array | DataTip object array
Children, returned as an empty GraphicsPlaceholder array or a DataTip object array. Currently, this property is not used and is reserved for future use.

## Interactivity

## Visible - Pose plot visibility

"on" (default) | "off" | on/off logical value
Pose plot visibility, specified as "on" or "off", or as numeric or logical 1 (true) or 0 (false). A value of "on" is equivalent to true, and "off" is equivalent to false. Thus, you can use the value of this property as a logical value. The value is stored as an on/off logical value of type matlab.lang.OnOffSwitchState.

- "on" - Display the object.
- "off" - Hide the object without deleting it. You still can access the properties of an invisible object.


## HandleVisibility - Visibility of pose patch object handle <br> "on" (default)| "off" | "callback"

Visibility of the pose patch object handle in the Children property of the parent, specified as one of these values:

- "on" - Object handle is always visible.
- "off" - Object handle is invisible at all times. This option is useful for preventing unintended changes by another function. Set HandleVisibility to "off" to temporarily hide the handle during the execution of that function. Hidden object handles are still valid.
- "callback" - Object handle is visible from within callbacks or functions invoked by callbacks, but not from within functions invoked from the command line. This option blocks access to the object at the command line, but permits callback functions to access it.


## Standard Chart Properties

## DisplayName - Pose plot name to display in legend

string scalar | character vector
Pose plot name to display in the legend, specified as a string scalar or character vector. The legend does not display until you call the legend command. If you do not specify the display name, then legend sets the label using the format "dataN", where $N$ is the order of pose plots shown in the axes. You can also directly specify the legend. For example: legend("Pose1", "Pose2").

## Type - Type of pose plot object <br> 'PosePatch' (default)

This property is read-only.
Type of pose plot object, returned as 'PosePatch '. Use this property to find all objects of a given type within a plotting hierarchy, for example, searching for the type using the findobj function.

## Annotation - Control for including or excluding object from legend

## Annotation object

This property is read-only.
Control for including or excluding the object from a legend, returned as an Annotation object. Set the underlying IconDisplayStyle property to one of these values:

- "on" - Include the object in the legend (default).
- "off" - Do not include the object in the legend.

For example, to exclude a graphics object, go, from the legend, set the IconDisplayStyle property to "off".
go.Annotation.LegendInformation.IconDisplayStyle = "off";
Alternatively, you can control the items in a legend using the legend function.

## SeriesIndex - Pose plot series index

1 (default) | nonnegative integer
Pose plot series index, specified as a nonnegative integer. Use this property to reassign the marker colors of several PosePatch objects so that they match each other. By default, the SeriesIndex
property of a PosePatch object is a number that corresponds to the order of creation of the object, starting at 0.

MATLAB uses the number to calculate indices for assigning colors when you call plotting functions if you do not specify the color directly. The indices refer to the rows of the arrays stored in the ColorOrder property of the axes.

## See Also

poseplot

Introduced in R2021b

## pseudoranges

Pseudoranges between GNSS receiver and satellites

## Syntax

```
p = pseudoranges(recPos,satPos)
[p, pdot] = pseudoranges(___,recVel, satVel)
[p, pdot] = pseudoranges(___Name,Value)
```


## Description

p = pseudoranges(recPos, satPos) returns the pseudoranges between the receiver at position recPos and the satellites at positions satPos.
[p, pdot] = pseudoranges (__ , recVel, satVel) returns the pseudorange rates pdot between the receiver and satellites. Use this syntax with the input arguments in the previous syntax.
[ $\mathrm{p}, \mathrm{pdot}$ ] = pseudoranges ( __ Name, Value) specifies the measurement noise for the ranges and range rates using name-value arguments. For example, [p pdot] = pseudoranges(_, 'RangeAccuracy' ,2) sets the measurement noise in pseudoranges, specified as a scalar standard deviation in meters.

## Examples

## Get Satellite Pseudoranges for Receiver Position and Velocity

Use the pseudoranges function to get the pseudorange and pseudorange rate for given satellite and receiver positions and velocities. Get the satellte positions and velcoties using the gnssconstellation function.

Specify a receiver position in geodetic coordinates (latitude, longitude, altitude) and receiver velocity in the local navigation frame.

```
recPos = [42 -71 50];
recVel = [1 2 3];
```

Get the satellite positions for the current time.

```
t = datetime('now');
[gpsSatPos,gpsSatVel] = gnssconstellation(t);
```

Get the pseudoranges and pseudorange rates between the receiver and satellites.

```
[p,pdot] = pseudoranges(recPos,gpsSatPos,recVel,gpsSatVel);
```


## Input Arguments

## recPos - Receiver position

three-element vector of the form [lat lon alt]

Receiver position in geodetic coordinates, specified as a three-element vector of the form [latitude longitude altitude]
Data Types: single | double

## satPos - Satellite positions

N -by-3 matrix of scalars
Satellite positions in the Earth-centered Earth-fixed (ECEF) coordinate system in meters, specified as an $N$-by- 3 matrix of scalars. $N$ is the number of satellites in the constellation.
Data Types: single|double

## recVel - Receiver velocity

three-element vector of the form [vx vy vz]
Receiver velocity in the local navigation frame using north-east-down (NED) coordinates, specified as a three-element vector of the form [ $v x v y v z$ ].
Data Types: single | double

## satVel - Satellite velocities

$N$-by-3 matrix of scalars
Satellite velocities in the Earth-centered Earth-fixed (ECEF) coordinate system in meters per second, specified as an $N$-by-3 matrix of scalars. $N$ is the number of satellites in the constellation.

## Data Types: single|double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: 'RangeAccuracy', ' 0.5 ' sets the measurement noise of the pseudoranges to 0.5 meters.

## RangeAccuracy - Measurement noise in pseudoranges <br> 1 (default) | scalar

Measurement noise in pseudoranges, specified as a scalar standard deviation in meters.
Data Types: single | double

## RangeRateAccuracy - Measurement noise in pseudorange rates

0.02 (default) | scalar

Measurement noise in pseudorange rates, specified as a scalar standard deviation in meters per second.

Data Types: single | double

## Output Arguments

## p - Pseudoranges between satellites and receiver

$n$-element vector

Pseudoranges between the satellites and receiver, returned as an $n$-element vector in meters.
Data Types: single | double
pdot - Pseudorange rates between satellites and receiver
zeros( $\mathrm{n}, 1$ ) (default) | $n$-element vector
Pseudorange rates between the satellites and receiver, returned as an $n$-element vector in meters per second. If you do not provide velocity inputs, this output is zero.
Data Types: single | double

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

## Objects

gnssSensor | gpsSensor | imuSensor

## Functions

skyplot | gnssconstellation|lookangles | receiverposition
Introduced in R2021a

## quat2axang

Convert quaternion to axis-angle rotation

## Syntax

axang = quat2axang(quat)

## Description

axang = quat2axang(quat) converts a quaternion, quat, to the equivalent axis-angle rotation, axang.

## Examples

## Convert Quaternion to Axis-Angle Rotation

```
quat = [0.7071 0.7071 0 0];
axang = quat2axang(quat)
axang = 1×4
    1.0000 0 0 1.5708
```


## Input Arguments

## quat - Unit quaternion

n-by-4 matrix | n-element vector of quaternion objects
Unit quaternion, specified as an $n$-by-4 matrix or $n$-element vector of quaternion objects containing $n$ quaternions. If the input is a matrix, each row is a quaternion vector of the form $q=[w x y z]$, with $w$ as the scalar number.

Example: [0.7071 0.7071 0 0]

## Output Arguments

## axang - Rotation given in axis-angle form

n-by-4 matrix
Rotation given in axis-angle form, returned as an $n$-by-4 matrix of $n$ axis-angle rotations. The first three elements of every row specify the rotation axis, and the last element defines the rotation angle (in radians).

```
Example:[1 0 0 pi/2]
```


## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

axang2quat | quaternion
Introduced in R2015a

## quat2eul

Convert quaternion to Euler angles

## Syntax

```
eul = quat2eul(quat)
eul = quat2eul(quat,sequence)
```


## Description

eul = quat2eul(quat) converts a quaternion rotation, quat, to the corresponding Euler angles, eul. The default order for Euler angle rotations is "ZYX".
eul = quat2eul (quat, sequence) converts a quaternion into Euler angles. The Euler angles are specified in the axis rotation sequence, sequence. The default order for Euler angle rotations is "ZYX".

## Examples

## Convert Quaternion to Euler Angles

quat $=$ [0.7071 0.7071 0 0];

```
eulZYX = quat2eul(quat)
```

eulZYX $=1 \times 3$
$0 \quad 0 \quad 1.5708$

## Convert Quaternion to Euler Angles Using ZYZ Axis Order

```
quat = [0.7071 0.7071 0 0];
eulZYZ = quat2eul(quat,'ZYZ')
eulZYZ = 1\times3
    1.5708 -1.5708 -1.5708
```


## Input Arguments

## quat - Unit quaternion

$n$-by-4 matrix | $n$-element vector of quaternion objects
Unit quaternion, specified as an $n$-by- 4 matrix or $n$-element vector of quaternion objects containing $n$ quaternions. If the input is a matrix, each row is a quaternion vector of the form $q=[w x y z]$, with $w$ as the scalar number.

Example: [0.7071 0.7071 0 0]
sequence - Axis rotation sequence
"ZYX" (default) | "ZYZ" | "XYZ"
Axis rotation sequence for the Euler angles, specified as one of these string scalars:

- "ZYX" (default) - The order of rotation angles is $z$-axis, $y$-axis, $x$-axis.
- "ZYZ" - The order of rotation angles is $z$-axis, $y$-axis, $z$-axis.
- "XYZ" - The order of rotation angles is $x$-axis, $y$-axis, $z$-axis.

Data Types: string | char

## Output Arguments

## eul - Euler rotation angles

$n$-by-3 matrix
Euler rotation angles in radians, returned as an $n$-by- 3 array of Euler rotation angles. Each row represents one Euler angle set.
Example: [0 0 1.5708]

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

eul2quat | quaternion
Introduced in R2015a

## quat2rotm

Convert quaternion to rotation matrix

## Syntax

```
rotm = quat2rotm(quat)
```


## Description

rotm $=$ quat2 rotm(quat) converts a quaternion quat to an orthonormal rotation matrix, rotm. When using the rotation matrix, premultiply it with the coordinates to be rotated (as opposed to postmultiplying).

## Examples

## Convert Quaternion to Rotation Matrix

```
quat = [0.7071 0.7071 0 0];
rotm = quat2rotm(quat)
rotm = 3\times3
\begin{tabular}{rrr}
1.0000 & 0 & 0 \\
0 & -0.0000 & -1.0000
\end{tabular}
```


## Input Arguments

## quat - Unit quaternion

$n$-by-4 matrix | $n$-element vector of quaternion objects
Unit quaternion, specified as an $n$-by-4 matrix or $n$-element vector of objects containing $n$ quaternions. If the input is a matrix, each row is a quaternion vector of the form $q=[w x y z]$, with $w$ as the scalar number.
Example: [0.7071 0.7071 0 0]

## Output Arguments

## rotm - Rotation matrix

3-by-3-by-n matrix
Rotation matrix, returned as a 3-by-3-by- $n$ matrix containing $n$ rotation matrices. Each rotation matrix has a size of 3 -by- 3 and is orthonormal. When using the rotation matrix, premultiply it with the coordinates to be rotated (as opposed to postmultiplying).
Example: [0 0 1; $010 ;-100]$

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

rotm2quat | quaternion
Introduced in R2015a

## quat2tform

Convert quaternion to homogeneous transformation

## Syntax

tform = quat2tform(quat)

## Description

tform = quat2tform(quat) converts a quaternion, quat, to a homogeneous transformation matrix, tform. When using the transformation matrix, premultiply it with the coordinates to be transformed (as opposed to postmultiplying).

## Examples

## Convert Quaternion to Homogeneous Transformation

```
quat = [0.7071 0.7071 0 0];
tform = quat2tform(quat)
tform = 4×4
\begin{tabular}{rrrr}
1.0000 & 0 & 0 & 0 \\
0 & -0.0000 & -1.0000 & 0 \\
0 & 1.0000 & -0.0000 & 0 \\
0 & 0 & 0 & 1.0000
\end{tabular}
```


## Input Arguments

quat - Unit quaternion
$n$-by-4 matrix | $n$-element vector of quaternion objects
Unit quaternion, specified as an $n$-by-4 matrix or n-element vector of quaternion objects containing $n$ quaternions. If the input is a matrix, each row is a quaternion vector of the form $q=[w x y z]$, with $w$ as the scalar number.

Example: [0.7071 0.7071 0 0]

## Output Arguments

## tform - Homogeneous transformation

4-by-4-by-n matrix
Homogeneous transformation matrix, returned as a 4-by-4-by-n matrix of $n$ homogeneous transformations. When using the rotation matrix, premultiply it with the coordinates to be rotated (as opposed to postmultiplying).

```
Example:[0 0 1 0; 0 1 0 0; -1 0 0 0; 0 0 0 1]
```


## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

tform2quat | quaternion
Introduced in R2015a

## read

Read data from GPS receiver

## Syntax

[tt,overrun] = read(gps)
[lla,groundSpeed, course,dops,gpsReceiverTime,timestamp,overrun] = read(gps)

## Description

[tt, overrun] = read(gps) returns the GPS readings in timetable format. This is a non blocking read which returns $N$ data points in timetable format, where $N$ is specified by SamplesPerRead property and timetable is specified using OutputFormat property of gpsdev object.
[lla,groundSpeed, course,dops,gpsReceiverTime,timestamp,overrun] = read(gps) returns matrices of measurements from the GPS. This is a non blocking read which returns $N$ data points in matrix format, where $N$ is specified by SamplesPerRead property and matrix is specified using OutputFormat property of the gpsdev object.

## Examples

## Read Data from GPS Receiver as Timetable

Read data from the GPS receiver connected to the host computer on a specific serial port.

## Required Hardware

To run this example, you need:

- UBlox Neo-6M GPS module
- GPS antenna
- USB to UART module
- USB cable
- Connecting wires


## Hardware Connection



Connect the pins on the UBlox Neo-6M GPS module to the pins on your USB to UART module. The connections are:

- VCC - +5 V
- RX - TXO
- TX - RXI
- GND - GND

Connect the GPS antenna to the GPS module. Connect the USB to UART module to the host computer with a USB cable. GPS Fix can be easily acquired in locations that have a clear view of the sky. Wait for the GPS module to acquire satelite signals (Fix).This can be verified by checking the Fix LED (D1) of your GPS module.

## Create GPS Object

Create a gpsdev object for the GPS receiver connected to a specific port. Specify the output format of the data as a timetable.

```
gps = gpsdev('COM4','OutputFormat',"timetable")
gps =
    gpsdev with properties:
        SerialPort: COM4
        BaudRate: 9600 (bits/s)
        SamplesPerRead: 1
        ReadMode: "latest"
        SamplesRead: 0
Show all properties all functions
```


## Read the GPS data

Read the GPS data and return them as a timetable.

```
[tt,overruns] = read(gps)
tt=1\times5 timetable
    Time LLA GroundSpeed Course
    22-Mar-2021 15:31:15.190
        17.47
        78.343
        449.6
        GroundSpeed
        Course
        0.25619
    NaN
    9.31 1.
overruns = 0
```

Display number of samples read and the samples available in the host buffer.

```
gps.SamplesRead
ans = 1
gps.SamplesAvailable
ans = 0
```

Release the GPS object to configure the non tunable properties. The release function also clears the buffer and resets the SamplesRead and SamplesAvailable properties.

```
release(gps)
```

Specify the number of samples per read to 2 . Read the GPS data.

```
gps.SamplesPerRead = 2;
read(gps)
```



Display number of samples read and the samples available in the host buffer.

```
gps.SamplesRead
ans = 1
gps.SamplesAvailable
ans = 0
```


## Clean Up

When the connection is no longer needed, clear the associated object.

```
delete(gps);
```

clear gps;

## Read Data from GPS Receiver as Matrix

Read data from the GPS receiver connected to the host computer using serialport object.

## Required Hardware

To run this example, you need:

- UBlox Neo-6M GPS module
- GPS antenna
- USB to UART module
- USB cable
- Connecting wires


## Hardware Connection



Connect the pins on the UBlox Neo-6M GPS module to the pins on your USB to UART module. The connections are:

- VCC -+5 V
- RX - TXO
- TX - RXI
- GND - GND

Connect the GPS antenna to the GPS module. Connect the USB to UART module to the host computer with a USB cable. GPS Fix can be easily acquired in locations that have a clear view of the sky. Wait for the GPS module to acquire satelite signals (Fix).This can be verified by checking the Fix LED (D1) of your GPS module.

## Create GPS Object

Connect to the GPS receiver using serialport object. Specify the port name and the baud rate. Specify the output format of the data as matrix.

```
s = serialport('COM4',9600);
gps = gpsdev(s,'OutputFormat',"matrix")
gps =
    gpsdev with properties:
```

SerialPort: COM4
BaudRate: 9600 (bits/s)
SamplesPerRead: 1
ReadMode: "latest"
SamplesRead: 0
Show all properties all functions

## Read the GPS data

Read the GPS data and return them as matrices.

```
[lla,speed,course,dops,gpsReceiverTime,timestamp,overruns] = read(gps)
lla = 1\times3
    NaN NaN NaN
speed = NaN
course = NaN
dops = 1\times3
    NaN NaN NaN
gpsReceiverTime = datetime
    NaT
timestamp = datetime
    22-Mar-2021 03:41:00.274
overruns = 1
```

Display number of samples read and the samples available in the host buffer.

```
gps.SamplesRead
```

ans $=1$
gps.SamplesAvailable
ans $=0$

Flush all GPS data accumulated in the buffers and reset the SamplesRead and SamplesAvailable properties.

## flush(gps)

Display number of samples read and the samples available in the host buffer.

```
gps.SamplesRead
ans = 0
gps.SamplesAvailable
```

```
ans = 0
```


## Clean Up

When the connection is no longer needed, clear the associated object.

```
delete(gps);
clear gps;
clear s;
```


## Input Arguments

```
gps - GPS sensor
```

gpsdev object
The GPS sensor, specified as a gpsdev object.

## Output Arguments

tt - GPS data
timetable
GPS data, returned as a timetable. The timetable returned has the following fields:

- LLA (Latitude, Longitude, Altitude)
- Ground Speed
- Course over ground
- Dilution of Precisions(DOPs), VDOP,HDOP,PDOP
- GPS Receiver Time
- Time - System time when the data is read, in datetime or duration format

Data Types: timetable

## lla - Position in LLA coordinate system

$N$-by-3 matrix
Position of the GPS receiver in the geodetic latitude, longitude, and altitude (LLA), returned as a real finite $N$-by-3 array. Latitude and longitude are in degrees with North and East being positive. Altitude is in meters.

Data Types: double

## groundSpeed - Speed in m/s

N -by-1 vector
Speed over ground, returned as a real finite $N$-by- 1 vector.

## Data Types: double

## course - Course over ground

$N$-by-1 vector
Course over ground relative to true north, returned as a real finite $N$-by- 1 vector of values between 0 and 2pi radians.

## Data Types: double

## dops - Dilution of precisions

$N$-by-3 matrix
Dilution of precisions, returned as a real finite $N$-by-3 matrix of the form [PDOP , HDOP , VDOP].
Data Types: double
gpsReceiverTime - UTC time
$N$-by-1 vector
UTC time, returned as a $N$-by-1 vector.

## Data Types: datetime

## timestamp - Time at which GPS data is read

N -by-1 vector
Time at which GPS data is read, returned as a real finite $N$-by- 1 vector. This is the system time. If the TimeFormat is datetime, the timestamp will be datetime. If the TimeFormat is a duration, the timestamp will be duration

- datetime - Displays the date and time at which the data is read.
- duration - Displays the time elapsed in seconds after the first call of the read function or the last execution of the release function.

Note If the SamplesPerRead is greater than 1, an extrapolation is done on the time value. Hence it $\underline{\text { might not be precise. }}$

Data Types: datetime | duration

## overrun - Overrun

scalar
The number of samples lost between consecutive calls to read. The overrun is zero when ReadMode is set to oldest.

Data Types: double

## More About

## read Output

The gpsdev object expects GPRMC, GPGGA, and GPGSA sentences as outputs from the GPS receiver to get the required values. The read function errors out if these sentences are not available.

The read function outputs NaN and NaT in the following situations:

- If the GPS module does not receive valid data because there is no satellite lock or when GPS does not give a particular value.
- If there is a checksum failure, corresponding data points will be NaN for numeric outputs (lla, speed, course, dops) and NaT for gpsRecieverTime. lla is taken from GPGGA sentence,
speed, course, and gpsRecieverTime is taken GPRMC sentence and dops are taken from GPGSA sentence.

Because read function is non blocking, the following is expected:

- If no new data is available, the output of read is the previous data. For example, if the delay between subsequent reads is less than the UpdateRate of the GPS receiver.

Because GPS data is validated in the first read operation, it might take more time compared to the subsequent read operations.

## See Also

## Objects

gpsdev

## Functions

flush|release|info|writeBytes

## Introduced in R2020b

## readBinaryOccupancyGrid

Read binary occupancy grid

## Syntax

```
map = readBinary0ccupancyGrid(msg)
map = readBinary0ccupancyGrid(msg,thresh)
map = readBinaryOccupancyGrid(msg,thresh,val)
```


## Description

map $=$ readBinary0ccupancyGrid(msg) returns a binary0ccupancyMap object by reading the data inside a ROS message, msg, which must be a 'nav_msgs/OccupancyGrid' message. All message data values greater than or equal to the occupancy threshold are set to occupied, 1 , in the map. All other values, including unknown values ( -1 ) are set to unoccupied, 0 , in the map.

Note The msg input is an 'nav_msgs/OccupancyGrid' ROS message. For more info, see OccupancyGrid.
map = readBinaryOccupancyGrid(msg,thresh) specifies a threshold, thresh, for occupied values. All values greater than or equal to the threshold are set to occupied, 1 . All other values are set to unoccupied, 0 .
map = readBinary0ccupancyGrid(msg,thresh, val) specifies a value to set for unknown values (-1). By default, all unknown values are set to unoccupied, 0.

## Input Arguments

msg - 'nav_msgs/OccupancyGrid' ROS message
OccupancyGrid object handle
'nav_msgs/OccupancyGrid' ROS message, specified as a OccupancyGrid object handle.

## thresh - Threshold for occupied values

50 (default) | scalar
Threshold for occupied values, specified as a scalar. Any value greater than or equal to the threshold is set to occupied, 1 . All other values are set to unoccupied, 0 .
Data Types: double
val - Value to replace unknown values
0 (default) | 1
Value to replace unknown values, specified as either 0 or 1 . Unknown message values ( -1 ) are set to the given value.
Data Types: double | logical

## Output Arguments

## map - Binary occupancy grid

binary0ccupancyMap object handle
Binary occupancy grid, returned as a binary0ccupancyMap object handle. map is converted from a 'nav_msgs/OccupancyGrid' message on the ROS network. The object is a grid of binary values, where 1 indicates an occupied location and 0 indications an unoccupied location.

## See Also

## Objects

OccupancyGrid | occupancyMap | binary0ccupancyMap

## Functions

rosReadOccupancyGrid | rosWriteBinary0ccupancyGrid| rosWriteOccupancyGrid

## Introduced in R2015a

## readOccupancyGrid

Read occupancy grid message

## Syntax

map $=$ readOccupancyGrid(msg)

## Description

map = readOccupancyGrid(msg) returns an occupancyMap object by reading the data inside a ROS message, msg, which must be a 'nav_msgs/OccupancyGrid' message. All message data values are converted to probabilities from 0 to 1 . The unknown values ( -1 ) in the message are set as 0.5 in the map.

Note The msg input is an 'nav_msgs/OccupancyGrid' ROS message. For more info, see OccupancyGrid.

## Input Arguments

msg - 'nav_msgs/OccupancyGrid' ROS message
OccupancyGrid object handle
'nav_msgs/OccupancyGrid' ROS message, specified as an OccupancyGrid ROS message object handle.

## Output Arguments

## map - Occupancy map

occupancyMap object handle
Occupancy map, returned as an occupancyMap object handle.

## See Also

## Functions

rosReadBinary0ccupancyGrid| rosRead0ccupancyMap3D | rosWriteBinary0ccupancyGrid | rosWriteOccupancyGrid

Introduced in R2016b

## readOccupancyMap3D

Read 3-D map from Octomap ROS message

## Syntax

map $=$ readOccupancyMap3D(msg)

## Description

map $=$ read0ccupancyMap3D(msg) reads the data inside a ROS 'octomap_msgs/Octomap' message to return an occupancyMap3D object. All message data values are converted to probabilities from 0 to 1 .

## Input Arguments

msg - Octomap ROS message
structure
Octomap ROS message, specified as a structure of message type 'octomap_msgs/0ctomap '. Get this message by subscribing to an 'octomap_msgs/Octomap' topic using rossubscriber on a live ROS network or by creating your own message using rosmessage.

## Output Arguments

## map - 3-D occupancy map

occupancyMap3D object handle
3-D occupancy map, returned as an occupancyMap3D object handle.

## See Also

occupancyMap3D | rosmessage | rossubscriber
Introduced in R2021a

## receiverposition

Estimate GNSS receiver position and velocity

## Syntax

```
recPos = receiverposition(p,satPos)
[recPos,recVel] = receiverposition(___,pdot,satVel)
[recPos,recVel,hdop,vdop] = receiverposition(
```

$\qquad$

``` )
```


## Description

recPos $=$ receiverposition( $p$, satPos) returns the receiver position estimated from the pseudoranges and satellite positions.
[recPos,recVel] = receiverposition( $\qquad$ , pdot, satVel) also returns the receiver velocity estimated from the pseudorange rates pdot and satellite velocities satVel.
[recPos,recVel,hdop,vdop] = receiverposition( $\qquad$ ) also returns the horizontal dilution of precision hdop and vertical dilution of precision vdop associated with the position estimate.

## Examples

## Estimate Receiver Position from Pseudoranges and Satellite Positions

Use the receiverposition function to estimate a GNSS receiver position. Get the satellte positiions and velocities using the gnssconstellation function. Generate pseudoranges from these positions using the pseudoranges function.

Specify a receiver position in geodetic coordinates (latitude, longitude, altitude) and a receiver velocity in the local navigation frame.

```
recPos = [42 -71 50];
recVel = [ll 2 3];
```

Get the satellite positions for the current time.

```
t = datetime('now');
[gpsSatPos,gpsSatVel] = gnssconstellation(t);
```

Get the pseudoranges and pseudorange rates between the GNSS receiver and the satellites.

```
[p,pdot] = pseudoranges(recPos,gpsSatPos,recVel,gpsSatVel);
```

Use the pseudoranges to estimate the receiver position and velocity. The values close to your original receiver position and velocity used to generate the satellite position and pseudoranges.
[lla,gnssVel] = receiverposition(p,gpsSatPos,pdot,gpsSatVel)
lla $=1 \times 3$

```
gnssVel = 1\times3
```

$1.0067 \quad 2.0094 \quad 3.0080$

## Input Arguments

## p - Pseudoranges between satellites and receiver

n-element vector
Pseudoranges between the satellites and receiver, specified as an $n$-element vector in meters.
Data Types: single | double

## satPos - Satellite positions

N -by-3 matrix of scalars
Satellite positions in the Earth-centered Earth-fixed (ECEF) coordinate system in meters, specified as an $N$-by- 3 matrix of scalars. $N$ is the number of satellites in the constellation.
Data Types: single | double
pdot - Pseudorange rates between satellites and receiver
$n$-element vector
Pseudorange rates between the satellites and receiver, specified as an $n$-element vector in meters per second.

Data Types: single | double

## satVel - Velocity readings in local navigation coordinate system (m/s)

$N$-by-3 matrix of scalar
Velocity readings of the GNSS receiver in the local navigation coordinate system in meters per second, specified as an $N$-by- 3 matrix of scalars. $N$ is the number of satellites in the constellation.

Data Types: single | double

## Output Arguments

## recPos - Receiver position

three-element vector of the form [lat lon alt]
Receiver position in geodetic coordinates, returned as a three-element vector of the form [latitude longitude altitude]

## Data Types: single | double

## recVel - Receiver velocity

three-element vector of the form [ vx vy vz ]
Receiver velocity in the local navigation frame using north-east-down (NED) coordinates, returned as a three-element vector of the form [vx vy vz].

Data Types: single | double
hdop - Horizontal dilution of precision
scalar
Horizontal dilution of precision, returned as a scalar.
Data Types: double
vdop - Vertical dilution of precision scalar

Vertical dilution of precision, returned as a scalar.
Data Types: double

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.

## See Also

Objects
gnssSensor|gpsSensor|imuSensor
Functions
skyplot|gnssconstellation|lookangles|pseudoranges
Introduced in R2021a

## release

## Release the GPS object

## Syntax

```
release(gps)
```


## Description

release(gps) release the system objects, allows configuration of non tunable properties, clear the buffers, and resets the values of SamplesRead and SamplesAvailable properties.

## Examples

## Read Data from GPS Receiver as Timetable

Read data from the GPS receiver connected to the host computer on a specific serial port.

## Required Hardware

To run this example, you need:

- UBlox Neo-6M GPS module
- GPS antenna
- USB to UART module
- USB cable
- Connecting wires


## Hardware Connection



Connect the pins on the UBlox Neo-6M GPS module to the pins on your USB to UART module. The connections are:

- $\mathrm{VCC}-+5 \mathrm{~V}$
- RX - TXO
- TX - RXI
- GND - GND

Connect the GPS antenna to the GPS module. Connect the USB to UART module to the host computer with a USB cable. GPS Fix can be easily acquired in locations that have a clear view of the sky. Wait for the GPS module to acquire satelite signals (Fix).This can be verified by checking the Fix LED (D1) of your GPS module.

## Create GPS Object

Create a gpsdev object for the GPS receiver connected to a specific port. Specify the output format of the data as a timetable.

```
gps = gpsdev('COM4','OutputFormat',"timetable")
gps =
    gpsdev with properties:
    SerialPort: COM4
    BaudRate: 9600 (bits/s)
        SamplesPerRead: 1
            ReadMode: "latest"
        SamplesRead: 0
Show all properties all functions
```


## Read the GPS data

Read the GPS data and return them as a timetable.
[tt,overruns] $=\operatorname{read}(g p s)$
tt=1×5 timetable

| Time | LLA |  |  | GroundSpeed | Course |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 22-Mar-2021 15:31:15.190 | 17.47 | 78.343 | 449.6 | 0.25619 | NaN |

```
overruns = 0
```

Display number of samples read and the samples available in the host buffer.

```
gps.SamplesRead
ans = 1
gps.SamplesAvailable
ans = 0
```

Release the GPS object to configure the non tunable properties. The release function also clears the buffer and resets the SamplesRead and SamplesAvailable properties.

```
release(gps)
```

Specify the number of samples per read to 2 . Read the GPS data.

```
gps.SamplesPerRead = 2;
```

read(gps)
ans=2×5 timetable
Time LLA
22-Mar-2021 15:31:17.178 17.47 78.343 450 0.063791 NaN
22-Mar-2021 15:31:17.178 17.47 78.343 450 NaN 0.063791 1.

Display number of samples read and the samples available in the host buffer.

```
gps.SamplesRead
```

ans = 1
gps.SamplesAvailable
ans $=0$

## Clean Up

When the connection is no longer needed, clear the associated object.

```
delete(gps);
```

clear gps;

## Input Arguments

```
gps - GPS sensor
```

gpsdev object
The GPS sensor, specified as a gpsdev object.

## See Also

## Objects

gpsdev
Functions
flush|writeBytes|read|info
Introduced in R2020b

## removelnvalidData

Remove invalid range and angle data

## Syntax

```
validScan = removeInvalidData(scan)
validScan = removeInvalidData(scan,Name,Value)
```


## Description

validScan = removeInvalidData(scan)returns a new lidarScan object with all Inf and NaN values from the input scan removed. The corresponding angle readings are also removed.
validScan = removeInvalidData(scan,Name,Value) provides additional options specified by one or more Name, Value pairs.

## Examples

## Plot Lidar Scan and Remove Invalid Points

Specify lidar data as vectors of ranges and angles. These values include readings outside of the sensors range.

```
x = linspace(-2,2);
ranges = abs((1.5).*x.^2 + 5);
ranges(45:55) = 3.5;
angles = linspace(-pi/2,pi/2,numel(ranges));
```

Create a lidar scan by specifying the ranges and angles. Plot all points of the lidar scan.

```
scan = lidarScan(ranges,angles);
plot(scan)
```



Remove invalid points based on a specified minimum and maximum range.

```
minRange = 0.1;
maxRange = 7;
scan2 = removeInvalidData(scan,'RangeLimits',[minRange maxRange]);
hold on
plot(scan2)
legend('All Points','Valid Points')
```



## Input Arguments

## scan - Lidar scan readings

lidarScan object
Lidar scan readings, specified as a lidarScan object.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: ["RangeLimits", [0.05 2]
RangeLimits - Range reading limits
two-element vector
Range reading limits, specified as a two-element vector, [minRange maxRange], in meters. All range readings and corresponding angles outside these range limits are removed
Data Types: single | double

## AngleLimits - Angle limits

two-element vector
Angle limits, specified as a two-element vector, [minAngle maxAngle] in radians. All angles and corresponding range readings outside these angle limits are removed.

Angles are measured counter-clockwise around the positivez-axis.
Data Types: single | double

## Output Arguments

## validScan - Lidar scan readings

lidarScan object
Lidar scan readings, specified as a lidarScan object. All invalid lidar scan readings are removed.

## See Also

lidarScan|transformScan | matchScans
Introduced in R2019b

## rinexinfo

Get information about RINEX file

## Syntax

fileinfo = rinexinfo(filename)

## Description

fileinfo $=$ rinexinfo(filename) gets information about the specified RINEX version 3 file filename, and returns it as a structure, fileinfo. The contents of fileinfo depend on the RINEX file type and the satellite system in the file.

## Examples

Query Navigation And Observation Messages From RINEX File

## GPS Navigation Message Info

```
filename = "GODS00USA_R_20211750000_01D_GN.rnx";
info = rinexinfo(fileñame)
info = struct with fields:
    FileVersion: 3.0400
    FileSatelliteSystem: 'G'
            FileType: 'N'
            Comments: [3x1 string]
    LeapSecondParameters: [1x1 struct]
            PGM: "JPS2RIN v.2.0.191"
            RunBy: "JAVAD GNSS"
        CreationDate: 25-Jun-2021 00:06:25
            FileName: "GODS00USA_R_20211750000_01D_GN.rnx"
            FileSize: 109092
```


## Galileo Navigation Message Info

```
filename = "GODS00USA_R_20211750000_01D_EN.rnx";
info = rinexinfo(filename)
info = struct with fields:
    FileVersion: 3.0400
    FileSatelliteSystem: 'E'
                            FileType: 'N'
                            Comments: [3x1 string]
    IonosphericCorrections: [1x1 struct]
        LeapSecondParameters: [1x1 struct]
                            PGM: "JPS2RIN v.2.0.191"
                            RunBy: "JAVAD GNSS"
            CreationDate: 25-Jun-2021 00:06:25
            FileName: "GODS00USA R 20211750000 01D EN.rnx"
```


## GLONASS Navigation Message Info

```
filename = "GODS00USA_R_20211750000_01D_RN.rnx";
info = rinexinfo(filename)
info = struct with fields:
            FileVersion: 3.0400
    FileSatelliteSystem: 'R'
        FileType: 'N'
        Comments: [3x1 string]
    LeapSecondParameters: [1x1 struct]
                    PGM: "JPS2RIN v.2.0.191"
            RunBy: "JAVAD GNSS"
        CreationDate: 25-Jun-2021 00:06:25
            FileName: "GODS00USA_R_20211750000_01D RN.rnx"
            FileSize: 141452
```


## BeiDou Navigation Message Info

```
filename = "GODS00USA_R_20211750000_01D_CN.rnx";
info = rinexinfo(fileñame)
info = struct with fields:
            FileVersion: 3.0400
        FileSatelliteSystem: 'C'
            FileType: 'N'
            Comments: [3x1 string]
        LeapSecondParameters: [1x1 struct]
            PGM: "JPS2RIN v.2.0.191"
            RunBy: "JAVAD GNSS"
        CreationDate: 25-Jun-2021 00:06:26
    TimeSystemCorrections: [1x1 struct]
            FileName: "GODS00USA_R_20211750000_01D_CN.rnx"
            FileSize: 155431
```


## NavIC/IRNSS Navigation Message Info

```
filename = "ARHT00ATA_R_20211750000_01D_IN.rnx";
```

info = rinexinfo(filename)
info = struct with fields:
FileVersion: 3.0400
FileSatelliteSystem: 'I'
FileType: 'N'
Comments: [3x1 string]
LeapSecondParameters: [1x1 struct]
PGM: "JPS2RIN v.2.0.191"
RunBy: "JAVAD GNSS"
CreationDate: 25-Jun-2021 00:03:18
FileName: "ARHT00ATA R 20211750000 01D IN.rnx"
FileSize: 74322

## QZSS Navigation Message Info

```
filename = "ARHT00ATA R 20211750000 01D JN.rnx";
info = rinexinfo(filename)
info = struct with fields:
    FileVersion: 3.0400
    FileSatelliteSystem: 'J'
    FileType: 'N'
    Comments: [3x1 string]
    LeapSecondParameters: [1x1 struct]
                    PGM: "JPS2RIN v.2.0.191"
            RunBy: "JAVAD GNSS"
        CreationDate: 25-Jun-2021 00:03:18
            FileName: "ARHT00ATA R 20211750000 01D JN.rnx"
            FileSize: 22970
```


## SBAS Navigation Message Info

filename = "G0P600CZE_R_20211750000_01D_SN.rnx"; info = rinexinfo(filename)
info = struct with fields:
FileVersion: 3.0400
FileSatelliteSystem: 'S'
FileType: 'N'
Comments: "SBAS NAVIGATION DATA FROM STATION GOP6 (RIGTC, GO PECNY)
PGM: "sbf2rin-13.4.5"
RunBy: "RIGTC, GO PECNY"
CreationDate: 25-Jun-2021 00:26:37
FileName: "GOP600CZE R 20211750000 01D SN.rnx"
FileSize: 1083132

## Mixed Observation Info

```
filename = "GODS00USA R 20211750000 01H 30S MO.rnx";
info = rinexinfo(filename)
info = struct with fields:
    FileVersion: 3.0400
    FileSatelliteSystem: 'M'
            FileType: '0
        ObservationTypes: [4x1 struct]
            NumSatellites: 44
            AntennaNumber: "02083"
                AntennaType: "JAVRINGANT DM SCIS"
            AntennaDeltaHEN: [0.0083 0 0]
            ApproxPosition: [1.1308e+06 -4.8313e+06 3.9941e+06]
    GLONASSFrequencyNumbers: [1x1 struct]
            Interval: 30
        LeapSecondParameters: [1x1 struct]
            MarkerName: "GODS"
            MarkerNumber: "40451M128"
            Observer: "GGN"
                    Agency: "NASA GODDARD SPACE FLIGHT CENTER"
                PGM: "JPS2RIN v.2.0.191"
                    RunBy: "JAVAD GNSS"
```

CreationDate: 24-Jun-2021 01:05:22
TotalObservations: [44×1 struct]
ReceiverNumber: "02704"
ReceiverType: "JAVAD TRE_3 DELTA"
ReceiverVersion: "4.0.02"
PhaseShift: [22x1 struct]
FirstObsTime: 23-Jun-2021 23:59:42
LastObsTime: 24-Jun-2021 00:59:12
FileName: "GODS00USA_R_20211750000_01H_30S_M0.rnx"
FileSize: 1240462

## Input Arguments

## filename - Name of RINEX version 3 file

string scalar | character vector
Name of the RINEX version 3 file to read data from, specified as a string scalar or character vector.
Example: "GODS00USA_R_20211750000_01D_GN.rnx"
Data Types: string|char

## Output Arguments

## fileinfo - RINEX file contents

structure
RINEX file contents, returned as a structure. The structure has different fields depending on the type of RINEX file and the header entries in the file. See the "Output for Navigation Message Files" on page 1-194 and "Output for Observation Message Files" on page 1-197 sections for more information about the output structure.

## More About

## Output for Navigation Message Files

If the specified RINEX file is a navigation message file, the fileinfo output is a structure with these fields:

| Field | Type | Description |
| :--- | :--- | :--- |
| FileName | string | Name of file |
| FileSize | double | File size in bytes |
| SatelliteSyste <br> m | string | "GPS", "Galileo", "GLONASS", "BeiDou", "NavIC", <br> "QZSS", "SBAS", or "Mixed" |
| Version | double | Format Version |
| FileType | char | File type, specified as either 'N' for navigation message <br> files and '0' for observation data files. |
| PGM | string | Name of the program that created the file |
| RunBy | string | Name of the agency that created the file |


| Field | Type | Description |
| :---: | :---: | :---: |
| CreationDate | string | Date and time of file creation |
| Comments <br> (Optional) | string | Comment lines from file header |
| IonosphericCor rections (Optional) | structure array | An array of structures with a number of elements equal to the number of IONOSPHERIC CORR header lines in the file. Each structure has the CorrectionType, Parameters, TimeMark, and SVID fields. <br> TimeMark and SVID are optional for all satellite systems except BeiDou. <br> Correction type: <br> - GAL - Galileo ai0 to ai2 <br> - GPSA - GPS alpha0 to alpha3 <br> - GPSB - GPS beta0 to beta3 <br> - QZSA - QZS alpha0 to alpha3 <br> - QZSB - QZS beta0 to beta3 <br> - BDSA - BDS alpha0 to alpha3 <br> - BDSB - BDS beta0 to beta3 <br> - IRNA - NavIC/IRNSS alpha0 to alpha3 <br> - IRNB - NavIC/IRNSS beta0 to beta3 <br> Parameters: <br> - GAL - ai0, ai1, ai2, Blank <br> - GPS - alpha0 to alpha3 or beta0 to beta3 <br> - QZS - alpha0 to alpha3 or beta0 to beta3 <br> - BDS - alpha0 to alpha3 or beta0 to beta3 <br> - IRN - alpha0 to alpha3 or beta0 to beta3 <br> - Time mark, Transmission Time (seconds of week) converted to hours of day and then to A-X. A is $00 \mathrm{~h}-$ $01 \mathrm{~h}, \mathrm{~B}$ is $01 \mathrm{~h}-02 \mathrm{~h}, \ldots, \mathrm{X}$ is $23-24 \mathrm{~h}$ satellite system time. <br> - SV ID, identify which satellite provided the ionospheric parameters |


| Field | Type | Description |
| :---: | :---: | :---: |
| TimeSystemCorr ections | structure | An array of structures with a number of elements equal to the number of TIME SYSTEM CORR header lines in the file. Each structure has the CorrectionType, Parameters, ReferenceTime, ReferenceWeekNumber, SVID, and UTCID fields. <br> Correction type: <br> - $\quad$ GPUT $=$ GPS - UTC (a0, a1) <br> - GLUT $=$ GLO - UTC (a0 = -TauC, a1 = zero $)$ <br> - GAUT = GAL - UTC ( a0, a1) <br> - $\operatorname{BDUT}=$ BDS - UTC (a0 = A0UTC, $\mathrm{a} 1=$ A1UTC $)$ <br> - QZUT = QZS - UTC (a0, a1) <br> - IRUT $=$ IRN - UTC ( $\mathrm{a} 0=$ A0UTC, $\mathrm{a} 1=$ A1UTC $)$ <br> - SBUT = SBAS - UTC (a0, a1) <br> - GLGP = GLO - GPS (a0 = -TauGPS, a1 = zero) <br> - GAGP $=$ GAL - GPS ( $\mathrm{a} 0=\mathrm{A} 0 \mathrm{G}, \mathrm{a} 1=\mathrm{A} 1 \mathrm{G}$ for GAL INAV/ FNAV; a0 = -A0GGTO, a1 = -A1 GGTO for GPS CNAV) <br> - QZGP = QZS - GPS (a0, a1) <br> - $\operatorname{IRGP}=\operatorname{IRN}-\operatorname{GPS}(\mathrm{a} 0=\mathrm{A} 0, \mathrm{a} 1=\mathrm{A} 1)$ <br> Parameters: <br> - a0, a1 coefficients of linear polynomial $\Delta t=a 0+a 1 \cdot(t-$ tref) for fractional part (excluding leap seconds) of time system difference (a0; sec, a1; sec/sec) <br> - Reference time (T) for polynomial (Seconds into GPS/GAL/BDS/QZS/IRN/SBAS week) <br> - Reference week number (W) <br> - GPS/GAL/QZS/IRN/SBAS week aligned to GPS, continuous number from 6-Jan-1980 <br> - GLONASS T and W zero. <br> - BDS week, continuous from: 1-Jan-2006 <br> - SV ID, System identifier and PRN/slot number 'snn' of the GNSS satellite broadcasting the time system difference or SBAS satellite broadcasting the MT12. Use EGNOS, WAAS, or MSAS for SBAS time differences from MT17. <br> - UTC Identifier <br> - 0 if unknown <br> - $1=$ UTC(NIST) <br> - $2=$ UTC(USNO) <br> - $3=$ UTC(SU) <br> - $4=\mathrm{UTC}(\mathrm{BIPM})$ |


| Field | Type | Description |
| :---: | :---: | :---: |
|  |  | - 5 = UTC(Europe Lab) <br> - $6=$ UTC(CRL) <br> - 7 = UTC(NTSC) (BDS) <br> - $>7=$ not assigned yet. |
| LeapSecondPara meters (Optional) | structure | Leap second parameters in a structure with fields LeapSeconds, DeltaTimeLeapSeconds, WeekNumber, DayNumber, and TimeSystemID . <br> - LeapSeconds - Current number of leap seconds. <br> - DeltaTimeLeapSeconds - Future or past leap seconds. For example, it is future leap seconds if the week and day numbers are in the future. <br> - WeekNumber - For GPS, GAL, QZS, and IRN, number of weeks since January 6,1980 . For BDS, it is number of weeks since January 1, 2006. <br> - DayNumber - The day number is the GPS or BeiDou day before the leap second. For GPS, this number is in the range [1, 7]. For Beidou, this number is in the range [0, 6]. <br> - TimeSystemID - Only "GPS" and "BDT" are valid values. If blank the field defaults to "GPS". |

Note that optional fields are not present in the structure unless specified in the RINEX file.

## Output for Observation Message Files

If the specified RINEX file is an observation message file, the output is a structure with these fields:

| Field | Type | Entry |
| :--- | :--- | :--- |
| FileName | string | Name of file |
| FileSize | double | File size in bytes |
| SatelliteSyste <br> m | string | "GPS", "Galileo", "GLONASS", "BeiDou", "NavIC", <br> "QZSS", "SBAS", or "Mixed" |
| Version | double | Format Version |
| FileType | char | File type, specified as either 'N' for navigation message <br> files and '0' for observation data files. |
| PGM | string | Name of the program that created the file |
| RunBy | string | Name of the agency that created the file |
| CreationDate | string | Date and time of file creation |
| Comments <br> (Optional) | string | Comment lines from file header |
| MarkerName | string | Name of antenna marker |
| MarkerNumber <br> (Optional) | string | Number of antenna marker |


| Field | Type | Entry |
| :--- | :--- | :--- |
| MarkerType <br> (Optional for <br> GEODETIC and <br> NON_GEODETIC <br> marker types) | string | Type of marker |
| Observer | string | Name of observer |
| Agency | string | Name of agency |
| ReceiverNumber | string | Receiver number |
| ReceiverType | string | Receiver type |
| ReceiverVersio <br> n | string | Receiver version |
| AntennaNumber | string | Antenna number |
| AntennaType | string | Antenna type |
| ApproxPosition | double | Approximate marker position in meters. |
| AntennaDeltaHE <br> N | double | Height of the antenna reference point (ARP) above marker, <br> and horizontal eccentricity of ARP relative to marker (East/ <br> North) in meters. |
| AntennaDeltaXY <br> Z | double | Position of antenna reference point for antenna on vehicle <br> in meters. |
| AntennaPhaseCe <br> nter <br> (Optional) | structure array | A structure array with number of elements equal to the <br> number of ANTENNA: PHASECENTER header lines in the <br> file. Each structure has SatelliteSystem, <br> ObservationCode, and PhaseCenterfields. Where: <br> Satel liteSystem - The specified satellite system. |
| AntennaZeroDir <br> XYZ (Optional) | double | ObservationCode - The observation code. See the |
| "Observation Type Descriptors" on page 1-201 section for |  |  |
| more information. |  |  |
| PhaseCenter - The average phase center position with |  |  |
| respect to the antenna reference point, in meters, North/ |  |  |
| East/Up for fixed station, XYZbody-fixed system for a |  |  |
| vehicle. |  |  |


| Field | Type | Entry |
| :---: | :---: | :---: |
| ```CenterOfMassXY Z``` | double | Current center of mass of the vehicle in a body-fixed coordinate system, in meters. |
| ObservationTyp es | structure array | A structure array with number of elements equal to the number of satellite systems in the file. Each structure has SatelliteSystem and Descriptors fields. Where: <br> SatelliteSystem - String specifying the satellite system. <br> Descriptors - String array of 3-element observation descriptors. The first element is the Type, the second is the Band, and the third is the Attribute. See the "Observation Type Descriptors" on page 1-201 section for more information. |
| SignalStrength Unit (Optional) | string | Unit of the carrier to noise ratio observables SNN (if present) DBHZ: S/N given in dbHz. |
| Interval (Optional) | double | Observation interval in seconds. |
| First0bsTime (Optional, unless RINEX file is a mixed GNSS file) | datetime | Time of first observation record. Time systems are: <br> - GPS - GPS time system <br> - GLO - UTC time system <br> - GAL - Galileo time system <br> - QZS - QZSS time system <br> - BDT - BDS time system <br> - IRN - NavIC/IRNSS time system |
| HasReceiverClo ckOffset (Optional, unless, the epoch lines of the data section reports clock offsets) | logical | Epoch, code, and phase are corrected by applying the real-time-derived receiver clock offset. |
| DCBS (Optional) | structure array | An array with number of elements equal to number of satellite systems in the file. Each structure has SatelliteSystem, Program, and Source fields. Where: <br> SatelliteSystem - String specifying satellite system <br> Program - String specifying the program used to apply differential code bias corrections (DCBS) <br> Source - String URL of source of corrections |


| Field | Type | Entry |
| :---: | :---: | :---: |
| PCVS (Optional) | structure array | An array with number of elements equal to number of satellite systems in the file. Each structure has SatelliteSystem, Program, and Source fields. Where: <br> SatelliteSystem - String specifying satellite system <br> Program - String specifying the program used to apply phase center variation corrections (PCVS) <br> Source - String URL of source of corrections |
| ScaleFactor | structure array | An array with number of elements equal to number of "SYS / SCALE FACTOR" header lines in the file. Each structure has SatelliteSystem, Factor, and ObservationTypes fields. Where: <br> SatelliteSystem - String specifying satellite system <br> Factor - is a factor to divide stored observations with before use <br> ObservationTypes - is a list of observation types |
| PhaseShift (Optional) | structure array | An array with number of elements equal to number of "SYS / PHASE SHIFT" header lines in the file. Each structure has SatelliteSystem, ObservationType, Correction, SatelliteIDs fields. Where: <br> SatelliteSystem - String specifying the satellite system. <br> ObservationType - String specifying carrier phase observation code. <br> Correction - Value of correction applied (cycles). <br> SatelliteIDs - String array of satellites where correction is applied. |
| GLONASSFrequen <br> cyNumbers <br> (Optional unless using files with GLONASS satellites) | structure | A structure with fields Slot and FrequencyNumber. Where: <br> Slot - String array of satellite numbers (system code (R), slot) <br> FrequencyNumber - Vector of integer doubles. |
| GLONASSCodePha seBias | structure | A structure with fields ObservationTypes and Bias. Where: <br> ObservationTypes - String array of observation types. Valid values are "C1C", "C1P", "C2C", or "C2P". <br> Bias - Vector of code phase bias corrections in meters. |


| Field | Type | Entry |
| :--- | :--- | :--- |
| LeapSecondPara <br> meters (Optional) | structure | Leap second parameters in a structure with fields <br> LeapSeconds, DeltaTimeLeapSeconds, WeekNumber, <br> DayNumber, and TimeSystemID . <br> - LeapSeconds - Current number of leap seconds. <br> - <br> DeltaTimeLeapSeconds - Future or past leap <br> seconds. For example, it is future leap seconds if the <br> week and day numbers are in the future. <br> WeekNumber - For GPS, GAL, QZS, and IRN, number of <br> weeks since January 6, 1980. For BDS, it is number of <br> weeks since January 1, 2006. <br> DayNumber - The day number is the GPS or BeiDou <br> day before the leap second. For GPS, this number is in <br> the range [1, 7]. For Beidou, this number is in the range <br> [0, 6]. |
| TimeSystemID - Only "GPS" and "BDT" are valid <br> values. If blank the field defaults to "GPS". |  |  |
| NumSatellites <br> (Optional) | double | Number of satellites, for which observations are stored in <br> the file. |
| TotalObservati <br> ons (Optional) | structure array | An array of structure with the number of elements equal to <br> the number of PRN / \# OF OBS header lines in the file. <br> Each structure has a SatelliteID and <br> NumObservations field. |

Note that optional fields are not present in the structure unless specified in the RINEX file.

## Observation Type Descriptors

Observation type descriptors is a string comprised of three parts. The first part is the observation type, the second is the frequency band, and the third is the attribute which indicates the tracking mode or channel.

The observation type can be one of five types.

## Type

- C - Code or pseudorange, is the distance, in meters, between the receiver antenna and the satellite antenna including delays and other biases.
- L - Phase is the carrier phase range from the antenna to the satellite, measured in whole cycles.
- D - Doppler shift indicating the approach of satellites, where a positive value indicates an approaching satellite.
- S - Raw signal strength (carrier to noise ratio) as an integer in the range [1, 9].
- X - Receiver channel numbers.

You can identify the frequency band code number given a frequency band and a satellite system.

## Frequency Band vs Satellite System

| Frequency <br> Band Code <br> Number | GPS | QZSS | SBAS | BDS | GLO | GAL | NavIC/ <br> IRNSS |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | L1 | L1 | L1 | L1 | G1 | E1 | - |
| 2 | L2 | L2 | - | B1 | G2 | - | - |
| 3 | - | - | - | - | G3 | - | - |
| 4 | L5 | - | L5 | L5 | B2a | - | G1a |
| 5 | - | - | - | B3 or B3A | G2a | E6 | - |
| 6 | - | - | B2 or B2b | - | E5b | - |  |
| 7 | - | - | B2a and | - | E5a and | - |  |
| 8 | B2b | - | E5b |  |  |  |  |
| 9 |  | - | - | - | S |  |  |

[^1]
## Attribute vs Satellite System

| Attribute Letter | GPS | QZSS | SBAS | BDS | GLO | GAL | NavIC/ IRNSS |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A | - | - | - | - | A channel | A channel | A channel |
| B | - | - | - | - | A channel | A channel | A channel |
| C | C codebased | C codebased | C codebased | - | C codebased | C channel | C channel |
| D | Semicodeless | Semicodeless | - | Data channel | - | - | - |
| E | - | E channel | - | - | - | - | - |
| I | I channel | I channel | - | I channel | - | I channel | - |
| L | L channel (L2C GPS) <br> P channel | L channel <br> P channel | - | - | - | - | - |
| M | M-based code | - | - | - | - | - | - |
| N | Codeless | - | - | - | - | - | - |
| P | P codebased | - | - | Pilot channel | P codebased | - | - |
| Q | Q channel | Q channel | - | Q channel | - | Q channel | - |
| S | D channel <br> M channel (L2C GPS) | D channel <br> M channel | - | - | - | - | - |
| W | Based on Ztracking | - | - | - | - | - | - |
| X | I and Q channels <br> M and L channels <br> D and $P$ channels | I and Q channels <br> M and L channels <br> D and $P$ channels | - | I and Q channels <br> D and P channels | - | B and C channels <br> I and Q channels | B and C channels |
| Y | Y codebased | - | - | - | - | - | - |
| Z | - | I and Q channels <br> D and E channels | - | D and P channels | - | A, B, and C channels | - |

These are examples of codes:

- C1M - L1 pseudorange derived from the M channel for a GPS satellite.
- L5X - E5a carrier phase derived from the B and C channels for a Galileo satellite.
- S3I - G3 signal strength derived from the I channels for a GLONASS satellite.


## References

[1] International GNSS Service (for Daily 30-Second GPS Broadcast Ephemeris Data, NASA Crustal Dynamics Data Information System (CDDIS), Greenbelt, MD, USA, Jun. 24, 2021; accessed June 25, 2021). https://dx.doi.org/10.5067/GNSS/gnss_daily_n_001.
[2] International GNSS Service (for Daily 30-Second Galileo Broadcast Ephemeris Data, NASA Crustal Dynamics Data Information System (CDDIS), Greenbelt, MD, USA, Jun. 24, 2021; accessed June 25, 2021). https://dx.doi.org/10.5067/GNSS/gnss_daily_l_001.
[3] International GNSS Service (for Daily 30-Second GLONASS Broadcast Ephemeris Data, NASA Crustal Dynamics Data Information System (CDDIS), Greenbelt, MD, USA, Jun. 24, 2021; accessed August 19, 2021). https://dx.doi.org/10.5067/GNSS/gnss_daily_g_001.
[4] International GNSS Service (for Daily 30-Second BeiDou Broadcast Ephemeris Data, NASA Crustal Dynamics Data Information System (CDDIS), Greenbelt, MD, USA, Jun. 24, 2021; accessed August 19, 2021). https://dx.doi.org/10.5067/GNSS/gnss_daily_f_001.
[5] International GNSS Service (for Daily 30-Second NavIC/IRNSS Broadcast Ephemeris Data, NASA Crustal Dynamics Data Information System (CDDIS), Greenbelt, MD, USA, Jun. 24, 2021; accessed August 19, 2021). https://dx.doi.org/10.5067/GNSS/gnss_daily_i_001.
[6] International GNSS Service (for Daily 30-Second QZSS Broadcast Ephemeris Data, NASA Crustal Dynamics Data Information System (CDDIS), Greenbelt, MD, USA, Jun. 24, 2021; accessed August 19, 2021). https://dx.doi.org/10.5067/GNSS/gnss_daily_q_001.
[7] International GNSS Service (for Daily 30-Second SBAS Broadcast Ephemeris Data, NASA Crustal Dynamics Data Information System (CDDIS), Greenbelt, MD, USA, Jun. 24, 2021; accessed August 19, 2021). https://dx.doi.org/10.5067/GNSS/gnss_daily_h_001.
[8] International GNSS Service (for Hourly 30-Second Observation Data, NASA Crustal Dynamics Data Information System (CDDIS), Greenbelt, MD, USA, Jun. 24, 2021; accessed August 19, 2021). https://dx.doi.org/10.5067/GNSS/gnss_hourly_o_001.
[9] Romero, Ignacio, ed. RINEX The Receiver Independent Exchange Format Version 3.05. Darmstadt, Germany: IGS/RTCM ESA/ESOC/Navigation Support Office. December, 2020. Accessed on: Dec. 22, 2021. https://files.igs.org/pub/data/format/rinex305.pdf .

## See Also

## Functions

rinexread | gnssconstellation | pseudoranges

## Introduced in R2022a

## rinexread

Read data from RINEX file

## Syntax

data $=$ rinexread(filename)

## Description

data $=$ rinexread(filename) reads data from the RINEX version 3 file filename and returns a structure, data. The content of data depends on the RINEX file type and the satellite system in the file.

## Examples

## Read Navigation and Observation Data from RINEX File

Read navigation data from a RINEX file that contains GPS navigation message data.

```
filename = "GODS00USA_R_20211750000_01D_GN.rnx";
data = rinexread(file\overline{name)}
data = struct with fields:
    GPS: [178x32 timetable]
```

View the GPS data read from the RINEX file.


Read navigation data from a RINEX file that contains Galileo navigation message data.

```
filename = "GODS00USA_R_20211750000_01D_EN.rnx";
data = rinexread(fileñame)
data = struct with fields:
    Galileo: [1798\times32 timetable]
```

View the Galileo data read from the RINEX file.

```
data.Galileo(1:4,:)
```

| Time | SatelliteID | SVClockBias | SVClockDrift | SVClockDriftRate |
| :---: | :---: | :---: | :---: | :---: |
| 23-Jun-2021 23:50:00 | 12 | 0.0051451 | -1.8929e-11 | 0 |
| 23-Jun-2021 23:50:00 | 12 | 0.0051451 | -1.8929e-11 | 0 |
| 23-Jun-2021 23:50:00 | 18 | -0.0016176 | -1.4765e-11 | 0 |
| 23-Jun-2021 23:50:00 | 18 | -0.0016176 | -1.4765e-11 | 0 |

Read navigation data from a RINEX file that contains GLONASS navigation message data.

```
filename = "GODS00USA R 20211750000 01D RN.rnx";
data = rinexread(filename)
data = struct with fields:
    GLONASS: [435x20 timetable]
```

View the GLONASS data read from the RINEX file.

| ans $=4 \times 20$ timetable Time | SatelliteID | SVClockBias | SVFrequencyBias | MessageFrameTime |
| :---: | :---: | :---: | :---: | :---: |
| 24-Jun-2021 00:15:00 | 1 | 8.1313e-05 | 0 | $3.4563 e+05$ |
| 24-Jun-2021 00:15:00 | 6 | 0.00020024 | 0 | $3.4563 \mathrm{e}+05$ |
| 24-Jun-2021 00:15:00 | 7 | -4.2243e-05 | 0 | $3.4563 e+05$ |
| 24-Jun-2021 00:15:00 | 8 | -5.9644e-05 | 0 | $3.4563 e+05$ |

Read navigation data from a RINEX file that contains BeiDou navigation message data.

```
filename = "GODS00USA R 20211750000 01D CN.rnx";
data = rinexread(filename)
data = struct with fields:
    BeiDou: [262\times32 timetable]
```

View the BeiDou data read from the RINEX file.


Read navigation data from a RINEX file that contains NavIC/IRNSS navigation message data.

```
filename = "ARHT00ATA_R_20211750000_01D_IN.rnx";
data = rinexread(file\overline{name)}
```

```
data = struct with fields:
    NavIC: [121\times32 timetable]
```

View the NavIC data read from the RINEX file.
data. $\operatorname{NavIC(1:4,:)~}$
ans=4×32 timetable
Time

Read navigation data from a RINEX file that contains QZSS navigation message data.

```
filename = "ARHT00ATA_R_20211750000_01D_JN.rnx";
data = rinexread(filename)
data = struct with fields:
    QZSS: [38x32 timetable]
```

View the GPS data read from the RINEX file.

```
data.QZSS(1:4,:)
```

| Time | SatelliteID | SVClockBias | SVClockDrift | SVClockDriftRate |
| :---: | :---: | :---: | :---: | :---: |
| 24-Jun-2021 03:00:00 | 2 | -3.9348e-07 | -2.2737e-13 | 0 |
| 24-Jun-2021 03:00:00 | 7 | -3.4459e-08 | 0 | 0 |
| 24-Jun-2021 04:00:00 | 2 | -3.9442e-07 | -2.2737e-13 | 0 |
| 24-Jun-2021 04:00:00 | 7 | -3.3993e-08 | 0 | 0 |

Read navigation data from a RINEX file that contains SBAS navigation message data.

```
filename = "G0P600CZE_R_20211750000_01D_SN.rnx";
data = rinexread(filename)
data = struct with fields:
    SBAS: [3342x16 timetable]
```

View the SBAS data read from the RINEX file.

```
data.SBAS(1:4,:)
ans=4\times16 timetable
    Time SatelliteID SVClockBias SVFrequencyBias TransmissionTime
    -Jun-2021 23:57:36
\(\qquad\)

0

SVFrequencyBias TransmissionTime
\(\qquad\)
0
\(3.4548 \mathrm{e}+05\)
\begin{tabular}{llrlr}
\(23-J u n-2021\) & \(23: 59: 44\) & 48 & 0 & 0 \\
\(24-J u n-2021\) & \(00: 00: 16\) & 36 & 0 & 0 \\
\(24-J u n-2021\) & \(00: 00: 00\) & 44 & \(-4.0373 e-07\) & 0
\end{tabular}

\section*{Mixed Observation Data}

Read mixed observation data from a RINEX file that contains GPS, GLONASS, Galileo, and BeiDou observation message data.
```

filename = "GODS00USA_R_20211750000_01H_30S_MO.rnx";
data = rinexread(filename)
data = struct with fields:
GPS: [1245x45 timetable]
GLONASS: [1102\times38 timetable]
Galileo: [859x38 timetable]
BeiDou: [1303x45 timetable]

```

View the GPS, GLONASS, Galileo, and BeiDou data read from the RINEX file.
```

data.GPS(1:4,:)

| Time | SatelliteID | EpochFlag | ReceiverClock0ffset | C1C | C1C_SSI |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 24-Jun-2021 | 5 | 0 | -0.00047787 | $2.266 \mathrm{e}+07$ | NaN |
| 24-Jun-2021 | 10 | 0 | -0.00047787 | $2.4266 e+07$ | NaN |
| 24-Jun-2021 | 13 | 0 | -0.00047787 | $2.1788 \mathrm{e}+07$ | NaN |
| 24-Jun-2021 | 15 | 0 | -0.00047787 | $2 \mathrm{e}+07$ | NaN |

data.GLONASS(1:4,:)
ans=4\times38 timetable

| Time | SatelliteID |  | EpochFlag |  | ReceiverClock0ffset |  | C1C |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |

data.Galileo(1:4,:)
ans=4\times38 timetable
Time SatelliteID
EpochFlag
ReceiverClockOffset
C1X
-0.00047787
2.375e+07
2.1663e+07
2.2857e+07
C1X_SSI
24-Jun-2021 11
4 0
0
-0.00047787
-0.00047787
-0.00047787
0
24-Jun-2021 12
12

```

```

| $2.4922 \mathrm{e}+07$ |  |  |
| ---: | :--- | :--- |
|  |  | NaN |
| $2.375 \mathrm{e}+07$ |  | NaN |
| $2.1663 \mathrm{e}+07$ |  | NaN |
| $2.2857 \mathrm{e}+07$ |  | NaN |

    24-Jun-2021 18
    EpochFlag
_

```
data.BeiDou(1:4,:)
ans \(=4 \times 45\) timetable
\begin{tabular}{|c|c|c|c|c|c|}
\hline Time & SatelliteID & EpochFlag & ReceiverClock0ffset & C2I & C2I_SSI \\
\hline 24-Jun-2021 & 19 & 0 & -0.00047787 & 2.2728e+07 & NaN \\
\hline 24-Jun-2021 & 20 & 0 & -0.00047787 & 2.2033e+07 & NaN \\
\hline 24-Jun-2021 & 23 & 0 & -0.00047787 & \(2.6024 \mathrm{e}+07\) & NaN \\
\hline 24-Jun-2021 & 29 & 0 & -0.00047787 & \(2.243 \mathrm{e}+07\) & NaN \\
\hline
\end{tabular}

\section*{Input Arguments}

\section*{filename - Name of RINEX version 3 file}
string scalar | character vector

Name of the RINEX version 3 file to read data from, specified as a string scalar or character vector.
Example: "GODS00USA_R_20211750000_01D_GN.rnx"
Data Types: string | char

\section*{Output Arguments}

\section*{data - Satellite system data from RINEX version 3 file}
structure
Satellite system data from the RINEX version 3 file, returned as a structure. The structure has a timetable containing different fields depending on the type of RINEX file and the header entries in the file. For for more details on the fields in each navigation and observation files type, see the corresponding "More About" on page 1-209 section:
- "GPS Navigation Message" on page 1-209
- "Galileo Navigation Message" on page 1-211
- "GLONASS Navigation Message" on page 1-213
- "BeiDou Navigation Message" on page 1-214
- "NavIC/IRNSS Navigation Message" on page 1-215
- "QZSS Navigation Message" on page 1-217
- "SBAS Navigation Message" on page 1-218
- "Mixed Observation Data" on page 1-219

Data Types: struct

\section*{More About}

GPS Navigation Message
\begin{tabular}{|l|l|l|}
\hline Field & Data Type & Description \\
\hline Time & datetime & GPS clock time \\
\hline SatelliteID & double & Satellite system (G) number (PRN) \\
\hline SVClockBias & double & SV clock bias in seconds \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|}
\hline Field & Data Type & Description \\
\hline SVClockDrift & double & SV clock drift in seconds per second \\
\hline SVClockDriftRa te & double & SV clock drift rate in seconds per second squared \\
\hline IODE & double & Issue number of the satellite ephemeris data set, Issue of Data, Ephemeris (IODE) \\
\hline Crs & double & Amplitude of the sine harmonic correction term to the orbit radius, in meters \\
\hline Delta_n & double & Mean motion difference from the computed value at reference time, in radians per second. \\
\hline M0 & double & Mean anomaly at the reference time, in radians \\
\hline Cuc & double & Amplitude of the cosine harmonic correction term to the argument of latitude, in radians \\
\hline sqrtA & double & Square root of the semimajor axis (sqrt (m)) \\
\hline Toe & double & Time of ephemeris (seconds of respective satellite week) \\
\hline Cic & double & Amplitude of the cosine harmonic correction term to the angle of inclination, in radians \\
\hline i0 & double & Inclination angle at reference time, in radians \\
\hline Crc & double & Amplitude of the cosine harmonic correction term to the orbit radius, in meters \\
\hline omega & double & Argument of perigee, in radians \\
\hline OMEGA_DOT & double & Reference rate of right ascension, in radians per second \\
\hline IDOT & double & Rate of inclination angle, in radians per second \\
\hline L2ChannelCodes & double & Codes on L2 channel \\
\hline GPSWeek & double & GPS week number, with time of ephemeris. This is a continuous number, not mod (1024) \\
\hline L2PDataFlag & double & L2P data flag \\
\hline SVAccuracy & double & SV accuracy in meters \\
\hline SVHealth & double & SV health indicated by bits 17-22 (See GPS ICD Section 20.3.3.3.1.4) \\
\hline TGD & double & Timing group delay in seconds \\
\hline IODC & double & Issue number of the satellite clock data set, Issue of Data, Clock (IODC). (See GPS ICD Section 20.3.3.3.1.5) \\
\hline TransmissionTi me & double & Transmission time of the message \\
\hline FitInterval & double & Fit interval in hours. Bit 17 w 10 sf \(2+\) IODC and Table 20XII of the GPS ICD. \\
\hline ```
BRDCOrbit7Spar
``` & double & Spare entry. May be used in a future version. \\
\hline \[
\begin{aligned}
& \text { BRDCOrbit7Spar } \\
& \text { e4 }
\end{aligned}
\] & double & Spare entry. May be used in a future version. \\
\hline
\end{tabular}

\section*{Galileo Navigation Message}
\begin{tabular}{|l|l|l|}
\hline Field & Data Type & Description \\
\hline Time & datetime & Galileo (GAL) clock time \\
\hline SatelliteID & double & Satellite system (E) number \\
\hline SVClockBias & double & SV clock bias in seconds \\
\hline SVClockDrift & double & SV clock drift in seconds per second \\
\hline \begin{tabular}{l} 
SVClockDriftRa \\
te
\end{tabular} & double & SV clock drift rate in seconds per second squared \\
\hline IODnav & double & Issue of data of the navigation batch \\
\hline Crs & double & \begin{tabular}{l} 
Amplitude of the sine harmonic correction term to the orbit \\
radius, in meters
\end{tabular} \\
\hline Delta_n & \begin{tabular}{l} 
Mean motion difference from the computed value at \\
reference time, in radians per second.
\end{tabular} \\
\hline M0 & double & Mean anomaly at the reference time, in radians \\
\hline Cuc & \begin{tabular}{l} 
Amplitude of the cosine harmonic correction term to the \\
argument of latitude, in radians
\end{tabular} \\
\hline Eccentricity & double & Eccentricity \\
\hline Cus & double & \begin{tabular}{l} 
Amplitude of the sine harmonic correction term to the \\
argument of latitude, in radians
\end{tabular} \\
\hline sqrtA & Square root of the semimajor axis (sqrt (m)) \\
\hline Toe & double & \begin{tabular}{l} 
Amp of ephemeris (seconds of respective satellite week) \\
angle of inclination, in radians
\end{tabular} \\
\hline Cic & double & \begin{tabular}{l} 
Longitude of ascending node of orbit plane at weekly epoch, \\
in radians.
\end{tabular} \\
\hline OMEGA0 & \begin{tabular}{l} 
Amplitude of the sine harmonic correction term to the angle \\
of inclination, in radians.
\end{tabular} \\
\hline Cis & double & Inclination angle at reference time, in radians \\
\hline i0 & \begin{tabular}{l} 
Amplitude of the cosine harmonic correction term to the \\
orbit radius, in meters
\end{tabular} \\
\hline Crc & Argument of perigee, in radians \\
\hline Reference rate of right ascension, in radians per second \\
\hline OMega & Rate of inclination angle, in radians per second \\
\hline IDOT & dot & double \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|}
\hline Field & Data Type & Description \\
\hline DataSources & double & \begin{tabular}{l}
Data sources \\
- Bit 0 set: I/NAV E1-B \\
- Bit 1 set: F/NAV E5a-I \\
- Bit 2 set: I/NAV E5b-I \\
- Bits 0 and 2 : Both can be set if the navigation messages were merged, however, bits 0-2 cannot all be set, as the I/NAV and F/NAV messages contain different information. \\
- Bit 3 reserved for Galileo internal use \\
- Bit 4 reserved for Galileo internal use \\
- Bit 8 set: af0-af2, Toc, SISA are for E5a,E1 \\
- Bit 9 set: af0-af2, Toc, SISA are for E5b,E1 \\
- Bits 8-9 : exclusive (only one bit can be set)
\end{tabular} \\
\hline GALWeek & double & GAL week number, with Toe. Continuous number, not \(\bmod (1024)\). \\
\hline BRDCOrbit5Spar e4 & double & Spare entry. May be used in a future version. \\
\hline SISAccuracy & double & Signal in space accuracy in meters (-1.0 - no accuracy prediction available (NAPA) or unknown) \\
\hline SVHealth & double & \begin{tabular}{l}
SV health (See Galileo ICD Section 5.1.9.3) \\
- Bit 0: E1B DVS \\
- Bits 1-2: E1B HS \\
- Bit 3: E5a DVS \\
- Bits 4-5 :E5a HS \\
- Bit 6: E5b DVS \\
- Bits 7-8: E5b HS
\end{tabular} \\
\hline BGDE5aE1 & double & BGD E5a/E1 in seconds \\
\hline BGDE5bE1 & double & BGD E5b/E1 in seconds \\
\hline TransmissionTi me & double & Transmission time of the message \\
\hline \[
\begin{aligned}
& \text { BRDCOrbit7Spar } \\
& \text { e2 }
\end{aligned}
\] & double & Spare entry. May be used in a future version. \\
\hline BRDCOrbit7Spar e3 & double & Spare entry. May be used in a future version. \\
\hline BRDCOrbit7Spar e4 & double & Spare entry. May be used in a future version. \\
\hline
\end{tabular}

GLONASS Navigation Message
\begin{tabular}{|c|c|c|}
\hline Field & Data Type & Description \\
\hline Time & datetime & UTC clock time \\
\hline SatelliteID & double & Satellite system (R) number \\
\hline SVClockBias & double & SV clock bias in seconds \\
\hline SVFrequencyBia s & double & SV relative frequency bias in hertz \\
\hline MessageFrameTi me & double & Message frame time in seconds of the UTC week \\
\hline PositionX & double & Satellite position X in kilometers \\
\hline VelocityX & double & Satellite velocity X dot in kilometers per second \\
\hline AccelerationX & double & Satellite acceleration X in kilometers per second squared \\
\hline Health & double & Satellite health ( \(0=\) healthy, \(1=\) unhealthy) \\
\hline PositionY & double & Satellite position Y in kilometers \\
\hline VelocityY & double & Satellite velocity Y dot in kilometers per second \\
\hline AccelerationY & double & Satellite acceleration Y in kilometers per second squared \\
\hline FrequencyNumbe r & double & Frequency number (ICD 5.1) \\
\hline PositionZ & double & Satellite position Z in kilometers \\
\hline VelocityZ & double & Satellite velocity Z dot in kilometers per second \\
\hline AccelerationZ & double & Satellite acceleration Z in kilometers per second squared \\
\hline ```
AgeOperationIn
fo
``` & double & Age of operation information in days \\
\hline StatusFlags & double & \begin{tabular}{l}
Status flags, 9-bit binary number: \\
- M ; bit 7-8, GLO type indicator ( \(00=\) GLO, \(01=\) GLO-M/K) \\
- P4 ; bit \(6, \mathrm{GLO}-\mathrm{M} / \mathrm{K}\) only, \(1=\) data updated, \(0=\) data not updated \\
- P3 ; bit 5, num of satellites in current frame almanac (0 \(=4\) sats, \(1=5\) sats) \\
- P2 ; bit 4 , indicate even ( 0 ) or odd (1) of time interval \\
- P1 ; bit 2-3, update and validity interval ( \(00=0 \mathrm{~min}, 01\) \(=30 \mathrm{~min}, 10=45 \mathrm{~min}, 11=60 \mathrm{~min}\) ) \\
- P ; bit 0-1, GLO-M/K only, time offset parameters tc, tGPS source ( \(00=\) ground, \(01=\) tc ground, tGPS onboard, \(10=\) tc on-board, tGPS ground, \(11=\) on-board)
\end{tabular} \\
\hline GroupDelay & double & L1/L2 group delay difference in seconds \\
\hline URAI & double & Raw accuracy index \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|}
\hline Field & Data Type & Description \\
\hline HealthFlags & double & \begin{tabular}{l}
Health flags, 3-bit binary number \\
- l(3) ; bit 2, GLO-M/K only, health bit of string 3 \\
- AC ; bit 1, 1 = almanac health reported in ephemerides record, \(0=\) not reported \\
- C ; bit 0 , almanac health bit ( \(1=\) healthy, \(0=\) not healthy)
\end{tabular} \\
\hline
\end{tabular}

\section*{BeiDou Navigation Message}
\begin{tabular}{|l|l|l|}
\hline Field & Data Type & Description \\
\hline Time & datetime & \begin{tabular}{l} 
BeiDou (BDT) time. This is a combination of entries from \\
the record (Time of clock year, month, day, hour, minute, \\
second).
\end{tabular} \\
\hline SatelliteID & double & Satellite system (C) number \\
\hline SVClockBias & double & SV clock bias in seconds \\
\hline SVClockDrift & double & SV clock drift in seconds per second \\
\hline \begin{tabular}{l} 
SVClockDriftRa \\
te
\end{tabular} & double & SV clock drift rate in seconds per second squared \\
\hline AODE & double & \begin{tabular}{l} 
Age of satellite ephemeris data, Age of Data, Ephemeris \\
(AODE). See BeiDou ICD Table Section 5.2.4.11 Table 5-8) \\
and field range is: 0-31.
\end{tabular} \\
\hline Crs & double & \begin{tabular}{l} 
Amplitude of the sine harmonic correction term to the orbit \\
radius, in meters
\end{tabular} \\
\hline Delta_n & \begin{tabular}{l} 
Mean motion difference from the computed value at \\
reference time, in radians per second.
\end{tabular} \\
\hline M0 & double & \begin{tabular}{l} 
Mean anomaly at the reference time, in radians \\
Amplitude of the cosine harmonic correction term to the \\
argument of latitude, in radians
\end{tabular} \\
\hline Cuc & double & Eccentricity \\
\hline Eccentricity & double & \begin{tabular}{l} 
Amplitude of the sine harmonic correction term to the \\
argument of latitude, in radians
\end{tabular} \\
\hline Cus & double & Square root of the semimajor axis (sqrt (m)) \\
\hline Time of ephemeris (seconds of respective satellite week) \\
\hline SqrtA & double & \begin{tabular}{l} 
Amplitude of the cosine harmonic correction term to the \\
angle of inclination, in radians
\end{tabular} \\
\hline Cic & \begin{tabular}{l} 
Longitude of ascending node of orbit plane at weekly epoch, \\
in radians.
\end{tabular} \\
\hline omEGA0 & \begin{tabular}{l} 
Amplitude of the sine harmonic correction term to the angle \\
of inclination, in radians.
\end{tabular} \\
\hline Cis & Inclination angle at reference time, in radians \\
\hline i0 & double & double
\end{tabular}
\begin{tabular}{|l|l|l|}
\hline Field & Data Type & Description \\
\hline CrC & double & \begin{tabular}{l} 
Amplitude of the cosine harmonic correction term to the \\
orbit radius, in meters
\end{tabular} \\
\hline omega & double & Argument of perigee, in radians \\
\hline OMEGA_DOT & double & Reference rate of right ascension, in radians per second \\
\hline ID0T & double & Rate of inclination angle, in radians per second \\
\hline \begin{tabular}{l} 
BRDCOrbit5Spar \\
e2
\end{tabular} & double & Spare entry. May be used in a future version. \\
\hline BDTWeek & double & BDT week number \\
\hline \begin{tabular}{l} 
BRDCOrbit5Spar \\
e4
\end{tabular} & double & Spare entry. May be used in a future version. \\
\hline SVAccuracy & double & SV accuracy in meters (See BDS ICD Section 5.2.4) \\
\hline SatH1 & double & SatH1 \\
\hline TGD1 & double & TGD1 B1/B3 in seconds \\
\hline TGD2 & double & \begin{tabular}{l} 
TGD2 B2/B3 in seconds \\
\hline \begin{tabular}{l} 
TransmissionTi \\
me
\end{tabular} \\
double satellite clock data, Age of Data, Clock (AODC). See \\
BeiDou ICD Table Section 5.2.4.9 Table 5-6) and field range \\
is: 0-31.
\end{tabular} \\
\hline AODC & Spare entry. May be used in a future version. \\
\hline \begin{tabular}{l} 
BRDCOrbit7Spar \\
e3
\end{tabular} & double & Spare entry. May be used in a future version. \\
\hline \begin{tabular}{l} 
BRDCOrbit7Spar \\
e4
\end{tabular} & double & Transmission time of the message \\
\hline
\end{tabular}

\section*{NavIC/IRNSS Navigation Message}
\begin{tabular}{|l|l|l|}
\hline Field & Data Type & Description \\
\hline Time & datetime & NavIC/IRNSS clock time (same as GPS time) \\
\hline SatelliteID & double & Satellite system (I) number (PRN) \\
\hline SVClockBias & double & SV clock bias in seconds \\
\hline SVClockDrift & double & SV clock drift in seconds per second \\
\hline \begin{tabular}{l} 
SVClockDriftRa \\
te
\end{tabular} & double & SV clock drift rate in seconds per second squared \\
\hline IODEC & double & \begin{tabular}{l} 
Issue number of the satellite ephemeris and clock data sets, \\
Issue of Data, Ephemeris and Clock (IODEC)
\end{tabular} \\
\hline Crs & double & \begin{tabular}{l} 
Amplitude of the sine harmonic correction term to the orbit \\
radius, in meters
\end{tabular} \\
\hline Delta_n & \begin{tabular}{l} 
Mean motion difference from the computed value at \\
reference time, in radians per second.
\end{tabular} \\
\hline M0 & double & Mean anomaly at the reference time, in radians \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|}
\hline Field & Data Type & Description \\
\hline Cuc & double & Amplitude of the cosine harmonic correction term to the argument of latitude, in radians \\
\hline Eccentricity & double & Eccentricity \\
\hline Cus & double & Amplitude of the sine harmonic correction term to the argument of latitude, in radians \\
\hline sqrtA & double & Square root of the semimajor axis (sqrt (m)) \\
\hline Toe & double & Time of ephemeris (seconds of respective satellite week) \\
\hline Cic & double & Amplitude of the cosine harmonic correction term to the angle of inclination, in radians \\
\hline OMEGA0 & double & Longitude of ascending node of orbit plane at weekly epoch, in radians. \\
\hline Cis & double & Amplitude of the sine harmonic correction term to the angle of inclination, in radians. \\
\hline i0 & double & Inclination angle at reference time, in radians \\
\hline Crc & double & Amplitude of the cosine harmonic correction term to the orbit radius, in meters \\
\hline omega & double & Argument of perigee, in radians \\
\hline OMEGA_DOT & double & Reference rate of right ascension, in radians per second \\
\hline IDOT & double & Rate of inclination angle, in radians per second \\
\hline \[
\begin{aligned}
& \text { BRDCOrbit5Spar } \\
& \text { e2 }
\end{aligned}
\] & double & Spare entry. May be used in a future version. \\
\hline IRNWeek & double & IRN week number, with Toe. Continuous number, not \(\bmod (1024)\), counted from 1980 (same as GPS) \\
\hline BRDCOrbit5Spar e4 & double & Spare entry. May be used in a future version. \\
\hline UserRangeAccur acy & double & User range accuracy in meters. See NavIC/IRNSS ICD Section 6.2.1.4 \\
\hline HealthFlags & double & Health (Sub frame 1, bits 155 (most significant) and 156(least significant)), where \(0=\mathrm{L} 5\) and S healthy, \(1=\mathrm{L} 5\) healthy and S unhealthy, \(2=\) L5 unhealthy and S healthy, 3= both L5 and S unhealthy \\
\hline TGD & double & Timing group delay in seconds \\
\hline BRDCOrbit6Spar
e4 & double & Spare entry. May be used in a future version. \\
\hline TransmissionTi me & double & Transmission time of the message \\
\hline \[
\begin{aligned}
& \text { BRDCOrbit7Spar } \\
& \text { e2 }
\end{aligned}
\] & double & Spare entry. May be used in a future version. \\
\hline ```
#BRDCOrbit7Spar
``` & double & Spare entry. May be used in a future version. \\
\hline
\end{tabular}
\begin{tabular}{|l|l|l|}
\hline Field & Data Type & Description \\
\hline \begin{tabular}{l} 
BRDCOrbit7Spar \\
e4
\end{tabular} & double & Spare entry. May be used in a future version. \\
\hline
\end{tabular}

QZSS Navigation Message
\begin{tabular}{|c|c|c|}
\hline Field & Data Type & Description \\
\hline Time & datetime & QZSS clock time \\
\hline SatelliteID & double & Satellite system (J) Satellite PRN-192 \\
\hline SVClockBias & double & SV clock bias in seconds \\
\hline SVClockDrift & double & SV clock drift in seconds per second \\
\hline SVClockDriftRa te & double & SV clock drift rate in seconds per second squared \\
\hline IODE & double & Issue number of the satellite ephemeris data set, Issue of Data, Ephemeris (IODE) \\
\hline Crs & double & Amplitude of the sine harmonic correction term to the orbit radius, in meters \\
\hline Delta_n & double & Mean motion difference from the computed value at reference time, in radians per second. \\
\hline M0 & double & Mean anomaly at the reference time, in radians \\
\hline Cuc & double & Amplitude of the cosine harmonic correction term to the argument of latitude, in radians \\
\hline Eccentricity & double & Eccentricity \\
\hline Cus & double & Amplitude of the sine harmonic correction term to the argument of latitude, in radians \\
\hline sqrtA & double & Square root of the semimajor axis (sqrt (m)) \\
\hline Toe & double & Time of ephemeris (seconds of respective satellite week) \\
\hline Cic & double & Amplitude of the cosine harmonic correction term to the angle of inclination, in radians \\
\hline OMEGA0 & double & Longitude of ascending node of orbit plane at weekly epoch, in radians. \\
\hline Cis & double & Amplitude of the sine harmonic correction term to the angle of inclination, in radians. \\
\hline i0 & double & Inclination angle at reference time, in radians \\
\hline Crc & double & Amplitude of the cosine harmonic correction term to the orbit radius, in meters \\
\hline omega & double & Argument of perigee, in radians \\
\hline OMEGA_DOT & double & Reference rate of right ascension, in radians per second \\
\hline IDOT & double & Rate of inclination angle, in radians per second \\
\hline L2ChannelCodes & double & Codes on L2 channel (fixed to 2, see IS-QZSS-PNT 4.1.2.7) \\
\hline GPSWeek & double & GPS week number, with Toe. Continuous number, not \(\bmod (1024)\). \\
\hline
\end{tabular}
\begin{tabular}{|l|l|l|}
\hline Field & Data Type & Description \\
\hline L2PDataFlag & double & L2 P data flag set to 1 since QZSS does not track L2P \\
\hline SVAccuracy & double & SV accuracy (m) (See IS-QZSS-PNT Section 5.4.3.1) \\
\hline SVHealth & double & SV health (bits 17-22 w 3 sf 1) (See IS-QZSS-PNT 5.4.1) \\
\hline TGD & double & \begin{tabular}{l} 
Timing group delay (s) (The QZSS ICD specifies a do not \\
use bit pattern "1000000", this condition is represented by \\
a blank field.)
\end{tabular} \\
\hline IODC & \begin{tabular}{l} 
Issue number of the satellite clock data set, Issue of Data, \\
Clock (IODC)
\end{tabular} \\
\hline \begin{tabular}{l} 
TransmissionTi \\
me
\end{tabular} & double & Transmission time of the message \\
\hline \begin{tabular}{l} 
FitIntervalFla \\
g
\end{tabular} & double & \begin{tabular}{l} 
Fit interval flag (0/1) (See IS-QZSS-PNT, 4.1.2.4(3) 0 - two \\
hours), 1 - more than 2 hours.
\end{tabular} \\
\hline \begin{tabular}{l} 
BRDCOrbit7Spar \\
e3
\end{tabular} & double & Spare entry. May be used in a future version. \\
\hline \begin{tabular}{l} 
BRDCOrbit7Spar \\
e4
\end{tabular} & double & Spare entry. May be used in a future version. \\
\hline
\end{tabular}

\section*{SBAS Navigation Message}
\begin{tabular}{|l|l|l|}
\hline Field & Data Type & Description \\
\hline Time & datetime & SBAS clock time \\
\hline SatelliteID & double & Satellite system (S) number \\
\hline SVClockBias & double & SV clock bias in seconds \\
\hline \begin{tabular}{l} 
SVFrequencyBia \\
s
\end{tabular} & double & SV relative frequency bias in hertz \\
\hline \begin{tabular}{l} 
TransmissionTi \\
me
\end{tabular} & double & Transmission time of the message \\
\hline PositionX & double & Satellite position X in kilometers \\
\hline VelocityX & double & Satellite velocity X dot in kilometers per second \\
\hline AccelerationX & double & Satellite acceleration X in kilometers per second squared \\
\hline Health & double & \begin{tabular}{l} 
Health: SBAS: See RINEX 3.05 Standard section 5.4.4 for: \\
health, health availability and User Range Accuracy.
\end{tabular} \\
\hline PositionY & double & Satellite position Y in kilometers \\
\hline VelocityY & double & Satellite velocity Y dot in kilometers per second \\
\hline AccelerationY & double & Satellite acceleration Y in kilometers per second squared \\
\hline AccuracyCode & double & Accuracy code (URA, m) \\
\hline PositionZ & double & Satellite position Z in kilometers \\
\hline VelocityZ & double & Satellite velocity Z dot in kilometers per second \\
\hline AccelerationZ & double & Satellite acceleration Z in kilometers per second squared \\
\hline
\end{tabular}
\begin{tabular}{|l|l|l|}
\hline Field & Data Type & Description \\
\hline IODN & double & \begin{tabular}{l} 
Issue number of the satellite navigation data set, Issue of \\
Data, Navigation (IODN). See reference RTCA DO-229, 8 \\
first bits after Message Type if MT9
\end{tabular} \\
\hline
\end{tabular}

\section*{Mixed Observation Data}

Mixed observation data may have multiple timetables in the output structure. Unlike the navigation messages, the most of the fields of the mixed observation files change depending on the observation types in the observation data. However, all observation data contains the same first fields.

\section*{Main Observation Data Fields}
\begin{tabular}{|l|l|l|}
\hline Field & Data Type & Description \\
\hline Time & datetime & Satellite clock time. \\
\hline SatelliteID & double & Satellite system number. \\
\hline EpochFlag & \begin{tabular}{l} 
nonnegative \\
integer
\end{tabular} & \begin{tabular}{l} 
Epoch flag indicating the status of the satellite system. \\
\(0-\) OK. \\
\(1-\) Power failure between previous epoch and current \\
epoch. \\
\(>1-\) Special event. See RINEX Version 3.05 File \\
Section 5.3.2 for more information.
\end{tabular} \\
\hline \begin{tabular}{l} 
ReceiverClock0 \\
ffset
\end{tabular} & double & Receiver clock offset in seconds \\
\hline
\end{tabular}

The rest of the headers are observation codes comprised of three digits that represent type, band, and attribute. See "Observation Type Descriptors" on page 1-219 for more information about the possible types, bands, and attributes.

Each descriptor code has corresponding field for signal strength indicator (SSI) and, if the observation type is phase (L), a field for loss-of-lock indicator (LLI). For example, type L, band 1, and attribute X has the field L1X and has two additional fields, L1X_SSI and L1X_LLI.

The SSI fields are ratios specified as an integer in the range [1, 9]. A ratio of 1 is considered unreliable, above 5 is considered good, and 9 is the maximum possible signal strength.

The LLI fields are three-bit codes that are specified as an integer in the range [0, 7]. A value of 0 indicates no loss of lock or unknown. The least significant bit indicates a lost lock between the previous and current observations, the second bit indicates half-cycle ambiguity or slip is possible, and the most significant bit indicates binary offset carrier (BOC) tracking of a multiplexed BOC (MBOC) modulated signal.

\section*{Observation Type Descriptors}

Observation type descriptors is a string comprised of three parts. The first part is the observation type, the second is the frequency band, and the third is the attribute which indicates the tracking mode or channel.

The observation type can be one of five types.

\section*{Type}
- C - Code or pseudorange, is the distance, in meters, between the receiver antenna and the satellite antenna including delays and other biases.
- L - Phase is the carrier phase range from the antenna to the satellite, measured in whole cycles.
- D - Doppler shift indicating the approach of satellites, where a positive value indicates an approaching satellite.
- S - Raw signal strength (carrier to noise ratio) as an integer in the range [1, 9].
- X - Receiver channel numbers.

You can identify the frequency band code number given a frequency band and a satellite system.

\section*{Frequency Band vs Satellite System}
\begin{tabular}{|l|l|l|l|l|l|l|l|}
\hline \begin{tabular}{l} 
Frequency \\
Band Code \\
Number
\end{tabular} & GPS & QZSS & SBAS & BDS & GLO & GAL & \begin{tabular}{l} 
NavIC/ \\
IRNSS
\end{tabular} \\
\hline 1 & L1 & L1 & L1 & L1 & G1 & E1 & - \\
\hline 2 & L2 & L2 & - & B1 & G2 & - & - \\
\hline 3 & - & - & - & - & G3 & - & - \\
\hline 4 & - & - & - & - & G1a & - & - \\
\hline 5 & L5 & L5 & L5 & B2a & - & E5a & L5 \\
\hline 6 & - & L6 & - & B3 or B3A & G2a & E6 & - \\
\hline 7 & - & - & - & B2 or B2b & - & E5b & - \\
\hline 8 & - & - & - & \begin{tabular}{l} 
B2a and \\
B2b
\end{tabular} & - & \begin{tabular}{l} 
E5a and \\
E5b
\end{tabular} & - \\
\hline 9 & - & - & - & - & - & - & S \\
\hline
\end{tabular}

You can identify the attribute letter given a channel or code and a satellite system.

\section*{Attribute vs Satellite System}
\(\left.\begin{array}{|l|l|l|l|l|l|l|l|}\hline \begin{array}{l}\text { Attribute } \\ \text { Letter }\end{array} & \text { GPS } & \text { QZSS } & \text { SBAS } & \text { BDS } & \text { GLO } & \text { GAL } & \begin{array}{l}\text { NavIC/ } \\ \text { IRNSS }\end{array} \\ \hline \text { A } & - & - & - & - & \text { A channel } & \text { A channel } & \text { A channel } \\ \hline \text { B } & - & - & - & - & \text { A channel } & \text { A channel } & \text { A channel } \\ \hline \text { C } & \begin{array}{l}\text { C code- } \\ \text { based }\end{array} & \begin{array}{l}\text { C code- } \\ \text { based }\end{array} & \begin{array}{l}\text { C code- } \\ \text { based }\end{array} & - & \begin{array}{l}\text { C code- } \\ \text { based }\end{array} & \text { C channel } & \text { C channel } \\ \hline \text { D } & \begin{array}{l}\text { Semi- } \\ \text { codeless }\end{array} & \begin{array}{l}\text { Semi- } \\ \text { codeless }\end{array} & - & \begin{array}{l}\text { Data } \\ \text { channel }\end{array} & - & - & - \\ \hline \text { E } & - & \text { E channel } & - & - & - & - & - \\ \hline \text { I channel } & \text { I channel } & - & \text { I channel } & - & \text { I channel } & - \\ \hline \text { L } & \begin{array}{l}\text { L channel } \\ \text { (L2C GPS) } \\ \text { P channel }\end{array} & \begin{array}{l}\text { L channel } \\ \text { P channel }\end{array} & - & - & - & - & - \\ \hline \text { M } & \begin{array}{l}\text { M-based } \\ \text { code }\end{array} & - & - & - & - & - & - \\ \hline \text { P } & \begin{array}{l}\text { Codeless } \\ \text { P code- } \\ \text { based }\end{array} & - & - & - & - & - & - \\ \hline \text { Q } & \text { Q channel } \\ \text { channel }\end{array}\right)\)

These are examples of codes:
- C1M - L1 pseudorange derived from the M channel for a GPS satellite.
- L5X - E5a carrier phase derived from the B and C channels for a Galileo satellite.
- S3I - G3 signal strength derived from the I channels for a GLONASS satellite.

\section*{References}
[1] International GNSS Service (for Daily 30-Second GPS Broadcast Ephemeris Data, NASA Crustal Dynamics Data Information System (CDDIS), Greenbelt, MD, USA, Jun. 24, 2021; accessed June 25, 2021). https://dx.doi.org/10.5067/GNSS/gnss_daily_n_001.
[2] International GNSS Service (for Daily 30-Second Galileo Broadcast Ephemeris Data, NASA Crustal Dynamics Data Information System (CDDIS), Greenbelt, MD, USA, Jun. 24, 2021; accessed June 25, 2021). https://dx.doi.org/10.5067/GNSS/gnss daily_l 001.
[3] International GNSS Service (for Daily 30-Second GLONASS Broadcast Ephemeris Data, NASA Crustal Dynamics Data Information System (CDDIS), Greenbelt, MD, USA, Jun. 24, 2021; accessed August 19, 2021). https://dx.doi.org/10.5067/GNSS/gnss_daily_g_001.
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[7] International GNSS Service (for Daily 30-Second SBAS Broadcast Ephemeris Data, NASA Crustal Dynamics Data Information System (CDDIS), Greenbelt, MD, USA, Jun. 24, 2021; accessed August 19, 2021). https://dx.doi.org/10.5067/GNSS/gnss_daily_h_001.
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[9] Romero, Ignacio, ed. RINEX The Receiver Independent Exchange Format Version 3.05. Darmstadt, Germany: IGS/RTCM ESA/ESOC/Navigation Support Office. December, 2020. Accessed on: Dec. 22, 2021. https://files.igs.org/pub/data/format/rinex305.pdf .

\section*{See Also}

Functions
rinexinfo|gnssconstellation|pseudoranges
Topics
"Ground Vehicle Pose Estimation for Tightly Coupled IMU and GNSS"
Introduced in R2022a

\section*{rotm2axang}

Convert rotation matrix to axis-angle rotation

\section*{Syntax}
axang \(=\) rotm2axang (rotm)

\section*{Description}
axang = rotm2axang (rotm) converts a rotation given as an orthonormal rotation matrix, rotm, to the corresponding axis-angle representation, axang. The input rotation matrix must be in the premultiply form for rotations.

\section*{Examples}

\section*{Convert Rotation Matrix to Axis-Angle Rotation}
```

rotm = [1 0 0 ; 0 -1 0; 0 0 -1];
axang = rotm2axang(rotm)
axang = 1×4

```
1.0000
0
0
3.1416

\section*{Input Arguments}

\section*{rotm - Rotation matrix}

3-by-3-by-n matrix
Rotation matrix, specified as a 3-by-3-by-n matrix containing \(n\) rotation matrices. Each rotation matrix has a size of 3-by-3 and must be orthonormal. The input rotation matrix must be in the premultiply form for rotations.

Note Rotation matrices that are slightly non-orthonormal can give complex outputs. Consider validating your matrix before inputting to the function.

Example: [0 0 1; 0 1 0; -1 0 0]

\section*{Output Arguments}

\section*{axang - Rotation given in axis-angle form}
\(n\)-by-4 matrix

Rotation given in axis-angle form, returned as an \(n\)-by-4 matrix of \(n\) axis-angle rotations. The first three elements of every row specify the rotation axis, and the last element defines the rotation angle (in radians).
Example: [1 00 pi/2]

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).

\section*{See Also}
axang2rotm
Introduced in R2015a

\section*{rotm2eul}

Convert rotation matrix to Euler angles

\section*{Syntax}
```

eul = rotm2eul(rotm)
eul = rotm2eul(rotm,sequence)

```

\section*{Description}
eul \(=\) rotm2eul (rotm) converts a rotation matrix, rotm, to the corresponding Euler angles, eul. The input rotation matrix must be in the premultiply form for rotations. The default order for Euler angle rotations is " ZYX ".
eul = rotm2eul(rotm, sequence) converts a rotation matrix to Euler angles. The Euler angles are specified in the axis rotation sequence, sequence. The default order for Euler angle rotations is "ZYX".

\section*{Examples}

\section*{Convert Rotation Matrix to Euler Angles}
```

rotm = [0 0 1; 0 1 0; -1 0 0];
eulZYX = rotm2eul(rotm)
eulZYX = 1\times3

```
    \(0 \quad 1.5708 \quad 0\)

\section*{Convert Rotation Matrix to Euler Angles Using ZYZ Axis Order}
```

rotm = [0 0 1; 0 1 0; -1 0 0];
eulZYZ = rotm2eul(rotm,'ZYZ')
eulZYZ = 1\times3
-3.1416 -1.5708 -3.1416

```

\section*{Input Arguments}

\section*{rotm - Rotation matrix}

3-by-3-by-n matrix

Rotation matrix, specified as a 3-by-3-by- \(n\) matrix containing \(n\) rotation matrices. Each rotation matrix has a size of 3-by-3 and is orthonormal. The input rotation matrix must be in the premultiply form for rotations.

Note Rotation matrices that are slightly non-orthonormal can give complex outputs. Consider validating your matrix before inputting to the function.

Example: [0 0 1; 0 1 0; -1 0 0]
sequence - Axis rotation sequence
"ZYX" (default) | "ZYZ" | "XYZ"
Axis rotation sequence for the Euler angles, specified as one of these string scalars:
- "ZYX" (default) - The order of rotation angles is \(z\)-axis, \(y\)-axis, \(x\)-axis.
- "ZYZ" - The order of rotation angles is \(z\)-axis, \(y\)-axis, \(z\)-axis.
- "XYZ" - The order of rotation angles is \(x\)-axis, \(y\)-axis, \(z\)-axis.

Data Types: string | char

\section*{Output Arguments}
eul - Euler rotation angles
\(n\)-by-3 matrix
Euler rotation angles in radians, returned as an \(n\)-by- 3 array of Euler rotation angles. Each row represents one Euler angle set.
Example: [0 0 1.5708]

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder \({ }^{\mathrm{TM}}\).

\section*{See Also}
eul2rotm

\section*{Introduced in R2015a}

\section*{rotm2quat}

Convert rotation matrix to quaternion

\section*{Syntax}
quat \(=\) rotm2quat(rotm)

\section*{Description}
quat \(=\) rotm2quat \((\) rotm \()\) converts a rotation matrix, rotm, to the corresponding unit quaternion representation, quat. The input rotation matrix must be in the premultiply form for rotations.

\section*{Examples}

\section*{Convert Rotation Matrix to Quaternion}
```

rotm = [0 0 1; 0 1 0; -1 0 0];
quat = rotm2quat(rotm)
quat = 1×4
0.7071 0 0.7071 0

```

\section*{Input Arguments}
rotm - Rotation matrix
3-by-3-by-n matrix
Rotation matrix, specified as a 3-by-3-by-n matrix containing \(n\) rotation matrices. Each rotation matrix has a size of 3-by-3 and is orthonormal. The input rotation matrix must be in the premultiply form for rotations.

Note Rotation matrices that are slightly non-orthonormal can give complex outputs. Consider validating your matrix before inputting to the function.

Example: [0 0 1; 0 1 0; -1 0 0]

\section*{Output Arguments}
quat - Unit quaternion
\(n\)-by-4 matrix
Unit quaternion, returned as an \(n\)-by- 4 matrix containing \(n\) quaternions. Each quaternion, one per row, is of the form \(q=[w \times y z]\), with \(w\) as the scalar number.

Example: [0.7071 0.7071 0 0]

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{Tm}}\).

\section*{See Also}
quat2rotm

Introduced in R2015a

\section*{rotm2tform}

Convert rotation matrix to homogeneous transformation

\section*{Syntax}
tform = rotm2tform(rotm)

\section*{Description}
tform = rotm2tform(rotm) converts the rotation matrix, rotm, into a homogeneous transformation matrix, tform. The input rotation matrix must be in the premultiply form for rotations. When using the transformation matrix, premultiply it with the coordinates to be transformed (as opposed to postmultiplying).

\section*{Examples}

\section*{Convert Rotation Matrix to Homogeneous Transformation}
```

rotm = [1 0 0 ; 0 -1 0; 0 0 -1];
tform = rotm2tform(rotm)
tform = 4×4

| 1 | 0 | 0 | 0 |
| ---: | ---: | ---: | ---: |
| 0 | -1 | 0 | 0 |
| 0 | 0 | -1 | 0 |
| 0 | 0 | 0 | 1 |

```

\section*{Input Arguments}
rotm - Rotation matrix
3-by-3-by-n matrix
Rotation matrix, specified as a 3 -by-3-by-n matrix containing \(n\) rotation matrices. Each rotation matrix has a size of 3-by-3 and is orthonormal. The input rotation matrix must be in the premultiply form for rotations.

Note Rotation matrices that are slightly non-orthonormal can give complex outputs. Consider validating your matrix before inputting to the function.

Example: [0 0 1; 010 ; -1 0 0]

\section*{Output Arguments}

\section*{tform - Homogeneous transformation}

4-by-4-by-n matrix
Homogeneous transformation matrix, specified by a 4-by-4-by-n matrix of \(n\) homogeneous transformations. When using the rotation matrix, premultiply it with the coordinates to be rotated (as opposed to postmultiplying).
Example: [0 0 1 0; \(0100 ;-1000 ; 0001]\)

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}
tform2rotm

Introduced in R2015a

\section*{show}

Visualize path segment

\section*{Syntax}
show(pathSeg)
show (pathSeg, Name, Value)

\section*{Description}
show(pathSeg) plots the path segment with start and goal positions and their headings.
show (pathSeg, Name, Value) also specifies Name, Value pairs to control display settings.

\section*{Examples}

\section*{Connect Poses Using Dubins Connection Path}

Create a dubinsConnection object.
dubConnObj = dubinsConnection;
Define start and goal poses as [x y theta] vectors.
startPose = [0 0 0];
goalPose = [1 1 pi];
Calculate a valid path segment to connect the poses.
```

[pathSegObj, pathCosts] = connect(dubConnObj,startPose,goalPose);

```

Show the generated path.
```

show(pathSegObj{1})

```


\section*{Modify Connection Types for Reeds-Shepp Path}

Create a reedsSheppConnection object.
reedsConnObj \(=\) reedsSheppConnection;
Define start and goal poses as [x y theta] vectors.
```

startPose = [0 0 0];

```
goalPose = [1 1 pi];

Calculate a valid path segment to connect the poses.
[pathSeg0bj, pathCosts] = connect(reedsConnObj,startPose,goalPose);
Show the generated path. Notice the direction of the turns.
```

show(pathSegObj{1})

```

```

pathSegObj{1}.MotionDirections

```
ans \(=1 \times 5\)
    \(\begin{array}{lllll}1 & -1 & 1 & 1 & 1\end{array}\)

Disable this specific motion sequence in a new connection object. Reduce the MinTurningRadius if the robot is more maneuverable. Increase the reverse cost to reduce the likelihood of reverse directions being used. Connect the poses again to get a different path.
```

reedsConnObj = reedsSheppConnection('DisabledPathTypes',{'LpRnLp'});
reedsConnObj.MinTurningRadius = 0.5;
reedsConnObj.ReverseCost = 5;
[pathSegObj,pathCosts] = connect(reedsConnObj,startPose,goalPose);
pathSegObj{1}.MotionTypes
ans = 1x5 cell
{'L'} {'S'} {'L'} {'N'} {'N'}

```
```

show(pathSeg0bj{1})
xlim([0 1.5])
ylim([0 1.5])

```


\section*{Interpolate Poses For Dubins Path}

Create a dubinsConnection object.
dubConnObj = dubinsConnection;
Define start and goal poses as [x y theta] vectors.
startPose = [0 0 0];
goalPose = [1 1 pi];
Calculate a valid path segment to connect the poses.
[pathSeg0bj,pathCosts] = connect(dubConn0bj,startPose,goalPose);
Show the generated path.
show(pathSegObj\{1\})


Interpolate poses along the path. Get a pose every 0.2 meters, including the transitions between turns.
```

length = pathSegObj{1}.Length;
poses = interpolate(pathSegObj{1},0:0.2:length)
poses = 32\times3

```
\begin{tabular}{rrr}
0 & 0 & 0 \\
0.1987 & -0.0199 & 6.0832 \\
0.3894 & -0.0789 & 5.8832 \\
0.5646 & -0.1747 & 5.6832 \\
0.7174 & -0.3033 & 5.4832 \\
0.8309 & -0.4436 & 5.3024 \\
0.8418 & -0.4595 & 5.3216 \\
0.9718 & -0.6110 & 5.5216 \\
1.1293 & -0.7337 & 5.7216 \\
1.3081 & -0.8226 & 5.9216
\end{tabular}

Use the quiver function to plot these poses.
quiver(poses(:,1), poses(:,2), cos(poses(:,3)), \(\sin (\operatorname{poses}(:, 3)), 0.5)\)


\section*{Input Arguments}
pathSeg - Path segment
dubinsPathSegment object | reedsSheppPathSegment object
Path segment, specified as a dubinsPathSegment or reedsSheppPathSegment object.

\section*{Name-Value Pair Arguments}

Specify optional pairs of arguments as Namel=Value1, ... ,NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: 'Headings', \{'transitions'\}

\section*{Parent - Axes to plot path onto}

Axes handle
Axes to plot path onto, specified as an Axes handle.

\section*{Headings - Heading angles to display}
cell array of character vector or string scalars

Heading angles to display, specified as a cell array of character vector or string scalars. Options are any combination of 'start','goal', and 'transitions'. To disable all heading displays, specify \{' '\}.

\section*{Positions - Positions to display}
'both' (default)|'start'|'goal' | 'none'
Positions to display, specified as 'both', 'start', 'goal', or ' none'. The start position is marked with green, and the goal position is marked with red.

\section*{HeadingLength - Length of heading}
positive numeric scalar
Length of heading, specified as positive numeric scalar. By default the value is calculated according to the \(x\) - and \(y\)-axis limits of the plot.
Data Types: double

\section*{See Also}

\section*{Functions}
interpolate |connect

\section*{Objects}
dubinsConnection|dubinsPathSegment | reedsSheppConnection| reedsSheppPathSegment

Introduced in R2019b

\section*{skyplot}

Plot satellite azimuth and elevation data

\section*{Syntax}
skyplot(azdata,eldata)
skyplot(azdata,eldata, labeldata)
skyplot(status)
skyplot (__, Name, Value)
skyplot(parent, \(\qquad\) )
h = skyplot( \(\qquad\) )

\section*{Description}
skyplot (azdata, eldata) creates a sky plot using the azimuth and elevation data specified as vectors in degrees. Azimuth angles are measured in degrees, clockwise-positive from the North direction. Elevation angles are measured from the horizon line with 90 degrees being directly up. For details about the sky plot figure elements, see "Main Sky Plot Elements" on page 1-244.
skyplot(azdata,eldata,labeldata) specifies data labels as a string array with elements corresponding to each data point in the azdata and eldata inputs.
skyplot(status) specifies the azimuth and elevation data in a structure with fields SatelliteAzimuth and SatelliteElevation.
skyplot (__, ,Name, Value) specifies options using one or more name-value arguments in addition to the input arguments in previous syntaxes. The name-value arguments are properties of the SkyPlotChart object. For a list of properties, see SkyPlotChart Properties.
skyplot (parent, ___ ) creates the sky plot in the figure, panel, or tab specified by parent.
h = skyplot (__ ) returns the sky plot as a SkyPlotChart object, h. Use h to modify the properties of the chart after creating it. For a list of properties, see SkyPlotChart Properties.

\section*{Examples}

\section*{View Satellite Positions from GNSS Sensor}

Create a GNSS sensor model as a gnssSensor System Object \({ }^{\mathrm{TM}}\).
gnss = gnssSensor;
Specify the position and velocity of the sensor. Simulate the sensor readings and get status from visible satellites. Store the azimuth and elevation angles as vectors.
```

pos = [0 0 0];
vel = [0 0 0];
[~, ~, status] = gnss(pos, vel);

```
```

satAz = status.SatelliteAzimuth;
satEl = status.SatelliteElevation;

```

Plot the satellite postions.
skyplot(satAz,satEl)


\section*{Plot Series of Satellite Positions Over Time}

Animate the trajectory of satellite positions over time from a GNSS sensor.
Initialize the sky plot figure. Specify the relevant time-stepping information.
skyplotHandle \(=\) skyplot(0,0);

```

numHours = 12;
dt = 100;
numSeconds = numHours * 60 * 60;
numSimSteps = numSeconds/dt;

```

Create a GNSS sensor model as a gnssSensor System Object \({ }^{\text {TM }}\).
```

gnss = gnssSensor('SampleRate', 1/dt);

```

Iterate through the time steps and do the following:
- Simulate the sensor readings. Specify the zero postion and velocity for the stationary sensor.
- Store the azimuth and elevation angles as vectors.
- Set the AzimuthData and ElevationData properties of the SkyPlotChart handle directly.
for \(i=1: n u m S i m S t e p s\)
[~, ~, status] = gnss([00 0 0],[0000]);
satAz = status.SatelliteAzimuth;
satEl = status.SatelliteElevation;
set(skyplotHandle, 'AzimuthData',satAz,'ElevationData',satEl);
drawnow
end


\section*{View Satellite Positions For Different Groups}

Load the azimuth and elevation data from a logfile generated by an Adafruit® GPS satellite sensor. The data provided in this example contains the azimuth and elevation of each satellite and the pseudorandom noise (PRN) codes. Store these values as vectors.
```

load('gpsHWInfo','hwInfo')
satAz = hwInfo.SatelliteAzimuths;
satEl = hwInfo.SatelliteElevations;
prn = hwInfo.SatellitePRNs;

```

Separate the satellites based on the PRN codes. To correlate each position with a group, create a categorical array. For this set of satellites, only the ones with PRNs less than 32 are used in the positioning solution.
```

isUnused = (prn > 32);

```
group = categorical(isUnused,[false true],["Used in Positioning Solution" "Unused"]);

Visualize the satellites and specify the categorical groups in the GroupData name-value argument. Specify the PRN as the label for each point. Show the legend.
```

skyplot(satAz,satEl,prn,GroupData=group)
legend('Used','Unused')

```


\section*{Input Arguments}

\section*{azdata - Azimuth angles for visible satellite positions}
\(n\)-element vector of angles
Azimuth angles for visible satellite positions, specified as an \(n\)-element vector of angles. \(n\) is the number of visible satellite positions in the plot. Azimuth angles are measured in degrees, clockwisepositive from the North direction.
Example: [25 45182 356]
Data Types: double
eldata - Elevation angles for visible satellite positions
\(n\)-element vector of angles
Elevation angles for visible satellite positions, specified as an \(n\)-element vector of angles. \(n\) is the number of visible satellite positions in the plot. Elevation angles are measured from the horizon line with 90 degrees being directly up.

Example: [45 9027 74]
Data Types: double

\section*{labeldata - Labels for visible satellite positions}
\(n\)-element string array

Labels for visible satellite positions, specified as an \(n\)-element string array. \(n\) is the number of visible satellite positions in the plot.

Example: ["G1" "G11" "G7" "G3"]
Data Types: string

\section*{status - Satellite status}
structure array
Satellite status, specified as a structure array with fields SatelliteAzimuth and SatelliteElevation. Typically, this status structure comes from a gnssSensor object, which simulates satellite positions and velocities.
Example: gnss = gnssSensor; [~,~,status] = gnss(position,velocity)
Data Types: struct
parent - Parent container
Figure object | Panel object| Tab object | TiledChartLayout object| GridLayout object
Parent container, specified as a Figure, Panel, Tab, TiledChartLayout, or GridLayout object.

\section*{Output Arguments}
h - Sky plot chart
SkyplotChart object
Sky plot chart, returned as a SkyplotChart object, which is a standalone visualization on page 1244. Use h to set properties on the sky plot chart. For more information, see SkyPlotChart Properties.

\section*{More About}

\section*{Main Sky Plot Elements}


The main elements of the figure are:
- Azimuth axes - Specified by the azdata input argument, azimuth angle positions are measured clockwise-positive from the North direction.
- Elevation axes -Specified by the eldata input argument, elevation angle positions are measured from the horizon line with 90 degrees being directly up.
- Labels - Specified by the labeldata input argument as a string array with an element for each point in the azdata and eldata vectors.
- Groups - Specified by the GroupData property, a categorical array defines the group for each satellite position.

\section*{Standalone Visualization}

A standalone visualization is a chart designed for a special purpose that works independently from other charts. Unlike other charts such as plot and surf, a standalone visualization has a preconfigured axes object built into it, and some customizations are not available. A standalone visualization also has these characteristics:
- It cannot be combined with other graphics elements, such as lines, patches, or surfaces. Thus, the hold command is not supported.
- The gca function can return the chart object as the current axes.
- You can pass the chart object to many MATLAB functions that accept an axes object as an input argument. For example, you can pass the chart object to the title function.

\section*{See Also}

\section*{Functions}
polarscatter
Properties
SkyPlotChart Properties

\author{
Objects \\ gnssSensor|nmeaParser
}

\section*{Introduced in R2021a}

\section*{tform2axang}

Convert homogeneous transformation to axis-angle rotation

\section*{Syntax}
axang \(=\) tform2axang(tform)

\section*{Description}
axang = tform2axang(tform) converts the rotational component of a homogeneous
transformation, tform, to an axis-angle rotation, axang. The translational components of tform are ignored. The input homogeneous transformation must be in the premultiply form for transformations.

\section*{Examples}

\section*{Convert Homogeneous Transformation to Axis-Angle Rotation}
```

tform = [1 0 0 0; 0 0 -1 0; 0 1 0 0; 0 0 0 1];
axang = tform2axang(tform)
axang = 1\times4
1.0000 0 0 1.5708

```

\section*{Input Arguments}

\section*{tform - Homogeneous transformation}

4-by-4-by-n matrix
Homogeneous transformation, specified by a 4-by-4-by-n matrix of \(n\) homogeneous transformations. The input homogeneous transformation must be in the premultiply form for transformations.

Example: [0 0 1 0; \(0100 ;-1000 ; 0001]\)

\section*{Output Arguments}

\section*{axang - Rotation given in axis-angle form}
n-by-4 matrix
Rotation given in axis-angle form, specified as an \(n\)-by- 4 matrix of \(n\) axis-angle rotations. The first three elements of every row specify the rotation axes, and the last element defines the rotation angle (in radians).
Example: [1 00 pi/2]

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}
axang2tform
Introduced in R2015a

\section*{tform2eul}

Extract Euler angles from homogeneous transformation

\section*{Syntax}
```

eul = tform2eul(tform)
eul = tform2eul(tform, sequence)

```

\section*{Description}
eul = tform2eul(tform) extracts the rotational component from a homogeneous transformation, tform, and returns it as Euler angles, eul. The translational components of tform are ignored. The input homogeneous transformation must be in the premultiply form for transformations. The default order for Euler angle rotations is "ZYX".
eul = tform2eul(tform, sequence) extracts the Euler angles, eul, from a homogeneous transformation, tform, using the specified rotation sequence, sequence. The default order for Euler angle rotations is "ZYX".

\section*{Examples}

\section*{Extract Euler Angles from Homogeneous Transformation Matrix}
```

tform = [1 0 0 0.5; 0 -1 0 5; 0 0 -1 -1.2; 0 0 0 1];
eulZYX = tform2eul(tform)
eulZYX = 1×3
0 0 3.1416

```

\section*{Extract Euler Angles from Homogeneous Transformation Matrix Using ZYZ Rotation}
```

tform = [1 0 0 0.5; 0 -1 0 5; 0 0 -1 -1.2; 0 0 0 1];

```
eulZYZ = tform2eul(tform,'ZYZ')
eulZYZ \(=1 \times 3\)
    \(\begin{array}{lll}0 & -3.1416 & 3.1416\end{array}\)

\section*{Input Arguments}

\section*{tform - Homogeneous transformation}

4-by-4-by-n matrix

Homogeneous transformation, specified by a 4-by-4-by-n matrix of \(n\) homogeneous transformations. The input homogeneous transformation must be in the premultiply form for transformations.

sequence - Axis rotation sequence
"ZYX" (default) | "ZYZ" | "XYZ"
Axis rotation sequence for the Euler angles, specified as one of these string scalars:
- "ZYX" (default) - The order of rotation angles is \(z\)-axis, \(y\)-axis, \(x\)-axis.
- "ZYZ" - The order of rotation angles is \(z\)-axis, \(y\)-axis, \(z\)-axis.
- "XYZ" - The order of rotation angles is \(x\)-axis, \(y\)-axis, \(z\)-axis.

Data Types: string | char

\section*{Output Arguments}

\section*{eul - Euler rotation angles}
n-by-3 matrix
Euler rotation angles in radians, returned as an \(n\)-by- 3 array of Euler rotation angles. Each row represents one Euler angle set.
Example: [0 0 1.5708]

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder \(^{\text {TM }}\).

\section*{See Also}
eul2tform

Introduced in R2015a

\section*{tform2quat}

Extract quaternion from homogeneous transformation

\section*{Syntax}
quat \(=\) tform2quat(tform)

\section*{Description}
quat \(=\) tform2quat(tform) extracts the rotational component from a homogeneous transformation, tform, and returns it as a quaternion, quat. The translational components of tform are ignored. The input homogeneous transformation must be in the premultiply form for transformations.

\section*{Examples}

\section*{Extract Quaternion from Homogeneous Transformation}
```

tform = [1 0 0 0; 0 -1 0 0; 0 0 -1 0; 0 0 0 1];
quat = tform2quat(tform)
quat = 1\times4
0 1 0 0

```

\section*{Input Arguments}

\section*{tform - Homogeneous transformation}

4-by-4-by-n matrix
Homogeneous transformation, specified by a 4-by-4-by-n matrix of \(n\) homogeneous transformations. The input homogeneous transformation must be in the premultiply form for transformations.
Example: [0 0 1 0; \(0100 ;-1000 ; 0001]\)

\section*{Output Arguments}

\section*{quat - Unit quaternion}
\(n\)-by-4 matrix
Unit quaternion, returned as an \(n\)-by-4 matrix containing \(n\) quaternions. Each quaternion, one per row, is of the form \(q=[w \times y z]\), with \(w\) as the scalar number.

Example: [0.7071 0.7071 0 0]

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).

\section*{See Also}
quat2tform
Introduced in R2015a

\section*{tform2rotm}

Extract rotation matrix from homogeneous transformation

\section*{Syntax}
rotm \(=\) tform2rotm(tform)

\section*{Description}
rotm \(=\) tform2rotm(tform) extracts the rotational component from a homogeneous transformation, tform, and returns it as an orthonormal rotation matrix, rotm. The translational components of tform are ignored. The input homogeneous transformation must be in the pre-
multiply form for transformations. When using the rotation matrix, premultiply it with the coordinates to be rotated (as opposed to postmultiplying).

\section*{Examples}

\section*{Convert Homogeneous Transformation to Rotation Matrix}
```

tform = [1 0 0 0; 0 -1 0 0; 0 0 -1 0; 0 0 0 1];
rotm = tform2rotm(tform)
rotm = 3x3

| 1 | 0 | 0 |
| ---: | ---: | ---: |
| 0 | -1 | 0 |
| 0 | 0 | -1 |

```

\section*{Input Arguments}

\section*{tform - Homogeneous transformation}

4-by-4-by-n matrix
Homogeneous transformation matrix, specified by a 4-by-4-by-n matrix of \(n\) homogeneous transformations. The input homogeneous transformation must be in the pre-multiply form for transformations.
Example: [0 0 1 0; 010 0; -1 \(000 ; 0001]\)

\section*{Output Arguments}

\section*{rotm - Rotation matrix}

3-by-3-by-n matrix
Rotation matrix, returned as a 3-by-3-by-n matrix containing \(n\) rotation matrices. Each rotation matrix has a size of 3 -by- 3 and is orthonormal. When using the rotation matrix, premultiply it with the coordinates to be rotated (as opposed to postmultiplying).

Example: [0 0 1; 0 1 0; -1 0 0]

\section*{Extended Capabilities}
\(\mathbf{C} / \mathbf{C}++\) Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® \(\mathrm{Coder}^{\mathrm{TM}}\).

\section*{See Also}
rotm2tform

Introduced in R2015a

\section*{tform2trvec}

Extract translation vector from homogeneous transformation

\section*{Syntax}
trvec \(=\) tform2trvec(tform)

\section*{Description}
trvec \(=\) tform2trvec(tform) extracts the Cartesian representation of translation vector, trvec, from a homogeneous transformation, tform. The rotational components of tform are ignored. The input homogeneous transformation must be in the premultiply form for transformations.

\section*{Examples}

\section*{Extract Translation Vector from Homogeneous Transformation}
```

tform = [1 0 0 0.5; 0 -1 0 5; 0 0 -1 -1.2; 0 0 0 1];
trvec = tform2trvec(tform)
trvec = 1\times3
0.5000 5.0000 -1.2000

```

\section*{Input Arguments}

\section*{tform - Homogeneous transformation}

4-by-4-by-n matrix
Homogeneous transformation, specified by a 4 -by-4-by-n matrix of \(n\) homogeneous transformations. The input homogeneous transformation must be in the premultiply form for transformations.

Example: [0 0 1 0; 010 0; -1 \(000 ; 0001]\)

\section*{Output Arguments}

\section*{trvec - Cartesian representation of a translation vector}
\(n\)-by-3 matrix
Cartesian representation of a translation vector, returned as an \(n\)-by- 3 matrix containing \(n\) translation vectors. Each vector is of the form \(t=[x y z]\).
Example: [0.5 6 100]

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).

\section*{See Also}
trvec2tform
Introduced in R2015a

\section*{transformMotion}

Compute motion quantities between two relatively fixed frames

\section*{Syntax}
```

[posS,orientS,velS,accS,angvelS] = transformMotion(posSFromP,orientSFromP,
posP)
[___] = transformMotion(posSFromP,orientSFromP,posP,orientP)
[___ ] = transformMotion(posSFromP,orientSFromP,posP,orientP,velP)
[___] = transformMotion(posSFromP,orientSFromP,posP,orientP,velP,accP)
[___] = transformMotion(posSFromP,orientSFromP,posP,orientP,velP,accP,
angvelP)

```

\section*{Description}
[posS,orientS,velS,accS,angvelS] = transformMotion(posSFromP,orientSFromP, posP) computes motion quantities of the sensor frame relative to the navigation frame (posS, orientS, velS, accS, and angvelS) using the position of sensor frame relative to the platform frame, posSFromP, the orientation of the sensor frame relative to the platform frame, orientSFromP, and the position of the platform frame relative to the navigation frame, posP. Note that the position and orientation between the sensor frame and the platform frame are assumed to be fixed. Also, the unspecified quantities between the navigation frame and the platform frame (such as orientation, velocity, and acceleration) are assumed to be zero.
[___] = transformMotion(posSFromP,orientSFromP,posP,orientP) additionally specifies the orientation of the platform frame relative to the navigation frame, orientP. The output arguments are the same as those of the previous syntax.
[ ___ ] = transformMotion(posSFromP,orientSFromP, posP,orientP, velP) additionally specifies the velocity of the platform frame relative to the navigation frame, velP. The output arguments are the same as those of the previous syntax.
[__ ] = transformMotion(posSFromP,orientSFromP, posP,orientP, velP,accP) additionally specifies the acceleration of the platform frame relative to the navigation frame, accP. The output arguments are the same as those of the previous syntax.
[___] = transformMotion(posSFromP,orientSFromP, posP, orientP, velP,accP, angvelP) additionally specifies the angular velocity of the platform frame relative to the navigation frame, angvelP. The output arguments are the same as those of the previous syntax.

\section*{Examples}

\section*{Transform State to Sensor Frame}

Define the pose, velocity, and acceleration of the platform frame relative to the navigation frame.
```

posPlat = [20 -1 0];
orientPlat = quaternion(1, 0, 0, 0);
velPlat = [0 0 0];

```
```

accPlat = [0 0 0];
angvelPlat = [0 0 1];

```

Define the position and orientation offset of IMU sensor frame relative to the platform frame.
```

posPlat2IMU = [ll 2 3];
orientPlat2IMU = quaternion([45 0 0], 'eulerd', 'ZYX', 'frame');

```

Calculate the motion quantities of the sensor frame relative to the navigation frame and print the results.
```

[posIMU, orientIMU, velIMU, accIMU, angvelIMU] ...
= transformMotion(posPlat2IMU, orientPlat2IMU, ...
posPlat, orientPlat, velPlat, accPlat, angvelPlat);
fprintf('IMU position is:\n');
IMU position is:
fprintf('%.2f %.2f %.2f\n', posIMU);
21.00 1.00 3.00
orientIMU
orientIMU = quaternion
0.92388 + 0i + 0j + 0.38268k
velIMU
velIMU = 1\times3
-2 1 0
accPlat
accPlat = 1\times3
0 0 0

```

\section*{Input Arguments}
posSFromP - Position of sensor frame relative to platform frame
1-by-3 vector of real scalars
Position of the sensor frame relative to the platform frame, specified as a 1-by-3 vector of real scalars.
Example: \(\left[\begin{array}{lll}1 & 2 & 3\end{array}\right]\)
orientSFromP - Orientation of sensor frame relative to platform frame
quaternion | 3-by-3 rotation matrix
Orientation of the sensor frame relative to the platform frame, specified as a quaternion or a 3-by-3 rotation matrix.

Example: quaternion ( \(1,0,0,0\) )

\section*{posP - Position of platform frame relative to navigation frame}
\(N\)-by-3 matrix of real scalars
Position of platform frame relative to navigation frame, specified as an N -by-3 matrix of real scalars. \(N\) is the number of position quantities.
Example: [lll 12 3]
orientP - Orientation of platform frame relative to navigation frame
\(N\)-by-1 array of quaternion | 3 -by-3-by- \(N\) array of scalars
Orientation of platform frame relative to navigation frame, specified as an \(N\)-by- 1 array of quaternions, or a 3-by-3-by- \(N\) array of scalars. Each 3-by-3 matrix must be a rotation matrix. \(N\) is the number of orientation quantities.
Example: quaternion ( \(1,0,0,0\) )

\section*{velP - Velocity of platform frame relative to navigation frame}
\(N\)-by-3 matrix of real scalars
Velocity of platform frame relative to navigation frame, specified as an \(N\)-by- 3 matrix of real scalars. \(N\) is the number of velocity quantities.
Example: [ \(\left.\begin{array}{lll}4 & 8 & 6\end{array}\right]\)

\section*{accP - Acceleration of platform frame relative to navigation frame \\ \(N\)-by-3 matrix of real scalars}

Acceleration of platform frame relative to navigation frame, specified as an \(N\)-by- 3 matrix of real scalars. \(N\) is the number of acceleration quantities.
Example: [ 48 6 8 ]
angvelP - Angular velocity of platform frame relative to navigation frame
\(N\)-by-3 matrix of real scalars
Angular velocity of platform frame relative to navigation frame, specified as an \(N\)-by- 3 matrix of real scalars. \(N\) is the number of angular velocity quantities.
Example: [4 2 3]

\section*{Output Arguments}

\section*{posS - Position of sensor frame relative to navigation frame}
\(N\)-by-3 matrix of real scalars
Position of sensor frame relative to navigation frame, returned as an \(N\)-by- 3 matrix of real scalars. \(N\) is the number of position quantities specified by the posP input.

\section*{orientS - Orientation of sensor frame relative to navigation frame}
\(N\)-by-1 array of quaternion | 3 -by-3-by- \(N\) array of scalars
Orientation of sensor frame relative to navigation frame, returned as an \(N\)-by- 1 array of quaternions, or a 3-by-3-by- \(N\) array of scalars. \(N\) is the number of orientation quantities specified by the orientP input. The returned orientation quantity type is same with the orientP input.

\section*{velS - Velocity of sensor frame relative to navigation frame}
\(N\)-by-3 matrix of real scalars
Velocity of sensor frame relative to navigation frame, returned as an \(N\)-by-3 matrix of real scalars. \(N\) is the number of position quantities specified by the velP input.

\section*{accS - Acceleration of sensor frame relative to navigation frame}
\(N\)-by-3 matrix of real scalars
Acceleration of sensor frame relative to navigation frame, returned as an \(N\)-by- 3 matrix of real scalars. \(N\) is the number of position quantities specified by the accP input.

\section*{angvelS - Angular velocity of sensor frame relative to navigation frame}
\(N\)-by-3 matrix of real scalars
Angular velocity of sensor frame relative to navigation frame, returned as an \(N\)-by- 3 matrix of real scalars. \(N\) is the number of position quantities specified by the angvelP input.

\section*{More About}

\section*{Motion Quantities Used in transformMotion}

The transformMotion function calculates the motion quantities of the sensor frame ( \(S\) ), which is fixed on a rigid platform, relative to the navigation frame ( \(N\) ) using the mounting information of the sensor on the platform and the motion information of the platform frame \((P)\).

As shown in the figure, the position and orientation of the platform frame and the sensor frame are fixed on the platform. The position of the sensor frame relative to the platform frame is \(p_{S P}\), and the orientation of the sensor frame relative to the platform frame is \(r_{S P}\). Since the two frames are both fixed, \(p_{S P}\) and \(r_{S P}\) are constant.

To compute the motion quantities of the sensor frame relative to the navigation frame, the quantities describing the motion of the platform frame relative to the navigation frame are required. These quantities include: the platform position ( \(p_{P N}\) ), orientation ( \(r_{P N}\) ), velocity, acceleration, angular velocity, and angular acceleration relative to the navigation frame. You can specify these quantities through the function input arguments except the angular acceleration, which is always assumed to be zero in the function. The unspecified quantities are also assumed to be zero.

\section*{See Also}
quaternion | rotvec
Introduced in R2020a

\section*{transformScan}

Transform laser scan based on relative pose

\section*{Syntax}
transScan \(=\) transformScan(scan,relPose)
[transRanges,transAngles] = transformScan(ranges,angles,relPose)

\section*{Description}
transScan = transformScan(scan, relPose) transforms the laser scan specified in scan by using the specified relative pose, relPose.
[transRanges,transAngles] = transformScan(ranges,angles, relPose) transforms the laser scan specified in ranges and angles by using the specified relative pose, relPose.

\section*{Examples}

\section*{Transform Laser Scans}

Create a lidarScan object. Specify the ranges and angles as vectors.
```

refRanges = 5*ones(1,300);
refAngles = linspace(-pi/2,pi/2,300);
refScan = lidarScan(refRanges,refAngles);

```

Translate the laser scan by an \([x y]\) offset of ( \(0.5,0.2\) ).
transformedScan \(=\) transformScan(refScan,[0.5 0.2 0]) ;
Rotate the laser scan by 20 degrees.
```

rotateScan = transformScan(refScan,[0,0,deg2rad(20)]);

```

\section*{Use Scan Matching to Transform Scans}

Use the matchScans function to find the relative transformation between two lidar scans. Then, transform the second scan into the coordinate frame of the first scan.

Load a pair of lidar scans as a pair of lidarScan objects. They are two scans of the same scene with a change in relative pose.
```

load tb3 scanPair.mat
plot(s1)
hold on
plot(s2)
hold off

```


The relative pose is estimated from an odometry sensor and provided as a variable, initGuess, as [x y theta]. disp(initGuess)
```

    -0.7000 0.1500 -0.3254
    ```

Use scan matching to find the relative pose between the two laser scans and specify the initial guess for the pose.
```

pose = matchScans(s2,s1,"InitialPose",initGuess);
disp(pose)
-0.7213 0.1160 -0.2854

```

Transform the second scan to the coordinate frame of the first scan. Plot the two scans to see that they now overlap.
```

s2Transformed = transformScan(s2,pose);
plot(s1)
hold on
plot(s2Transformed)
hold off

```


\section*{Input Arguments}

\section*{scan - Lidar scan readings}
lidarScan object
Lidar scan readings, specified as a lidarScan object.
ranges - Range values from scan data
vector
Range values from scan data, specified as a vector in meters. These range values are distances from a sensor at specified angles. The vector must be the same length as the corresponding angles vector.

\section*{angles - Angle values from scan data}
vector
Angle values from scan data, specified as a vector in radians. These angle values are the specific angles of the specified ranges. The vector must be the same length as the corresponding ranges vector.
relPose - Relative pose of current scan
[ x y theta]
Relative pose of current scan, specified as [ \(x y\) theta], where [ \(x y\) ] is the translation in meters and theta is the rotation in radians.

\section*{Output Arguments}

\section*{transScan - Transformed lidar scan readings}
lidarScan object
Transformed lidar scan readings, specified as a lidarScan object.

\section*{transRanges - Range values of transformed scan \\ vector}

Range values of transformed scan, returned as a vector in meters. These range values are distances from a sensor at specified transAngles. The vector is the same length as the corresponding transAngles vector.

\section*{transAngles - Angle values from scan data}
vector
Angle values of transformed scan, returned as a vector in radians. These angle values are the specific angles of the specified transRanges. The vector is the same length as the corresponding ranges vector.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and C++ code using MATLAB® Coder \(^{\text {TM }}\).

\section*{See Also}
matchScans|transformScan | controllerVFH|monteCarloLocalization

\section*{Topics}
"Estimate Robot Pose with Scan Matching"
Introduced in R2017a

\section*{trimLoopClosures}

Optimize pose graph and remove bad loop closures

\section*{Syntax}
poseGraphUpdated \(=\) trimLoopClosures(poseGraphObj,trimParams, solverOptions) [poseGraphUpdated,trimInfo] = trimLoopClosures(poseGraphObj,trimParams, solverOptions)

\section*{Description}
poseGraphUpdated \(=\) trimLoopClosures(poseGraphObj,trimParams, solverOptions) optimizes the pose graph to best satisfy the edge constrains and removes any bad loop closure edges based on the residual error parameters specified in trimParams. Create the solverOptions input using the poseGraphSolverOptions function.

The function implements the graduated non-convexity (GNC) method with truncated least squares (TLS) robust cost in combination with the non-minimal pose graph solver [1] on page 1-270.
[poseGraphUpdated,trimInfo] = trimLoopClosures(poseGraphObj,trimParams, solverOptions) returns additional information related to the trimming process.

\section*{Examples}

\section*{Optimize and Trim Loop Closures For 2-D Pose Graphs}

Optimize a pose graph based on the nodes and edge constraints. Trim loop closed based on their edge residual errors.

Load the data set that contains a 2-D pose graph. Inspect the poseGraph object to view the number of nodes and loop closures.
```

load grid-2d-posegraph.mat pg
disp(pg)
poseGraph with properties:
NumNodes: 120
NumEdges: 193
NumLoopClosureEdges: 74
LoopClosureEdgeIDs: [120 121 122 123 124 125 126 127 128 129 130 ... ]
LandmarkNodeIDs: [1x0 double]

```

Plot the pose graph with IDs off. Red lines indicate loop closures identified in the dataset. The poses in the graph should follow a grid pattern, but show evidence of drift over time.
```

show(pg,'IDs','off');
title('Original Pose Graph')

```


Optimize the pose grap using the optimizePoseGraph function. By default, this function uses the "builtin-trust-region" solver. Because the pose graph contains some bad loop closures, the resulting pose graph is actual not desirable.
pgOptim \(=\) optimizePoseGraph(pg);
figure;
show(pgOptim);


Look at the edge residual errors for the original pose graph. Large outlier error values at the end indicate bad loop closures.
```

resErrorVec = edgeResidualErrors(pg);
plot(resErrorVec);
title('Edge Residual Errors by Edge ID')

```


Certain loop closures should be trimmed from the pose graph based on their residual error. Use the trimLoopClosures function to trim therse bad loop closures. Set the maximum and truncation threshold for the trimmer parameters. This threshold is set based on the measurement accuracy and should be tuned for your system.
trimParams.MaxIterations = 100;
trimParams.TruncationThreshold = 25;
solverOptions = poseGraphSolverOptions;
Use the trimLoopClosures function with the trimmer parameters and solver options.
[pgNew, trimInfo, debugInfo] = trimLoopClosures(pg,trimParams,solverOptions);
From the trimInfo output, plot the loop closures removed from the optimized pose graph. By plotting with the residual errors plot before, you can see the large error loop closures were removed.
```

removedLCs = trimInfo.LoopClosuresToRemove;
hold on
plot(removedLCs,zeros(length(removedLCs)),'or')
title('Edge Residual Errors and Removed Loop Closures')
legend('Residual Errors', 'Removed Loop Closures')
xlabel('Edge IDs')
ylabel('Edge Residual Error')
hold off

```


Show the new pose graph with the bad loop closures trimmed.
show(pgNew, "IDs", "off") ;


\section*{Input Arguments}
poseGraph0bj - Pose graph
poseGraph object | poseGraph3D object
Pose graph, specified as a poseGraph or poseGraph3D object.

\section*{trimParams - Residual error parameters for trimming}
structure
Residual error parameters for trimming loop closures, specified as a structure with fields:
- MaxIterations - Maximum number of iterations allowed for loop closure trimming, specified as a positive integer. In one trimming iteration, the pose graph is optimized based on the solver options and any edges outside the TruncationThreshold are trimmed.
- TruncationThreshold - Maximum allowed residual error for an edge. This value depends heavily on the pose graph you specify in poseGraphObj. To find a proper threshold based on all the errors, use the edgeResidualErrors function for the pose graph.

Example: struct('MaxIterations',10,'TruncationThreshold', 20)
Data Types: struct

\section*{solverOptions - Pose graph solver options}
poseGraphSolverOptions parameters

Pose graph solver options, specified as a set of parameters generated by calling the poseGraphSolverOptions function. The function generates a set of solver options with default values for the specified pose graph solver type:
```

pgSolverTrustRegion = poseGraphSolverOptions('builtin-trust-region')
pgSolverTrustRegion =
TrustRegion (builtin-trust-region-dogleg) options:
MaxIterations: 300
MaxTime: 10
FunctionTolerance: 1.0000e-08
GradientTolerance: 5.0000e-09
StepTolerance: 1.0000e-12
InitialTrustRegionRadius: 100
VerboseOutput: 'off'
pgSolverG2o = poseGraphSolverOptions('g2o-levenberg-marquardt')
pgSolverG2o =
G2oLevenbergMarquardt (g2o-levenberg-marquardt) options:
MaxIterations: 300
MaxTime: 10
FunctionTolerance: 1.0000e-09
VerboseOutput: 'off'

```

Modify the options to tune the solver parameters using dot notation.
```

pgSolverG2o.MaxIterations = 200;

```

\section*{Output Arguments}

\section*{poseGraphUpdated - Pose graph with trimmed looped closures}
poseGraph object | poseGraph3D object
Pose graph with trimmed looped closures, specified as a poseGraph or poseGraph3D object.

\section*{trimInfo - Information from trimming process \\ structure}

Information from trimming process, returned as a structure with fields:
- LoopClosuresToRemove - Loop closure edge IDs to remove from the input poseGraph0bj. These loop closures are removed in the output poseGraphUpdated.
- Iterations - Number of trimming iterations performed.

\section*{References}
[1] Yang, Heng, et al. "Graduated Non-Convexity for Robust Spatial Perception: From Non-Minimal Solvers to Global Outlier Rejection." IEEE Robotics and Automation Letters, vol. 5, no. 2, Apr. 2020, pp. 1127-34. DOI.org (Crossref), doi:10.1109/LRA.2020.2965893.

\section*{See Also}

\section*{Functions}
poseGraphSolverOptions |edgeResidualErrors|removeEdges |edgeNodePairs | edgeConstraints

\section*{Objects}
poseGraph | poseGraph3D | lidarSLAM

Introduced in R2020b

\section*{trvec2tform}

Convert translation vector to homogeneous transformation

\section*{Syntax}
tform = trvec2tform(trvec)

\section*{Description}
tform = trvec2tform(trvec) converts the Cartesian representation of a translation vector, trvec, to the corresponding homogeneous transformation, tform. When using the transformation matrix, premultiply it with the coordinates to be transformed (as opposed to postmultiplying).

\section*{Examples}

\section*{Convert Translation Vector to Homogeneous Transformation}
trvec \(=\) [0.5 6 100];
tform = trvec2tform(trvec)
tform \(=4 \times 4\)
\begin{tabular}{rrrr}
1.0000 & 0 & 0 & 0.5000 \\
0 & 1.0000 & 0 & 6.0000 \\
0 & 0 & 1.0000 & 100.0000 \\
0 & 0 & 0 & 1.0000
\end{tabular}

\section*{Input Arguments}
trvec - Cartesian representation of a translation vector
\(n\)-by-3 matrix
Cartesian representation of a translation vector, specified as an \(n\)-by- 3 matrix containing \(n\) translation vectors. Each vector is of the form \(t=[x y z]\).
Example: [0.5 6 100]

\section*{Output Arguments}

\section*{tform - Homogeneous transformation}

4-by-4-by-n matrix
Homogeneous transformation matrix, returned as a 4-by-4-by-n matrix of \(n\) homogeneous transformations. When using the rotation matrix, premultiply it with the coordinates to be rotated (as opposed to postmultiplying).
```

Example:[0 0 1 0; 0 1 0 0; -1 0 0 0; 0 0 0 1]

```

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder \(^{\text {TM }}\).

\section*{See Also}
tform2trvec

\section*{Introduced in R2015a}

\section*{tunernoise}

Noise structure of fusion filter

\section*{Syntax}
```

noiseStruct = tunernoise(filterName)
noiseStruct = tunernoise(filter)

```

\section*{Description}
noiseStruct = tunernoise(filterName) returns the measurement noise structure for the filter with name specified by the filterName input.
noiseStruct = tunernoise(filter) returns the measurement noise structure for the filter object.

\section*{Examples}

\section*{Obtain Measurement Noise Structure of insfilterAsync}

Obtain the measurement noise structure of the insfilterAsync object.
```

noiseStruct = tunernoise('insfilterAsync')
noiseStruct = struct with fields:
AccelerometerNoise: 1
GyroscopeNoise: 1
MagnetometerNoise: 1
GPSPositionNoise: 1
GPSVelocityNoise: 1

```

\section*{Tune insfilterAsync to Optimize Pose Estimate}

Load the recorded sensor data and ground truth data.
load('insfilterAsyncTuneData.mat');
Create timetables for the sensor data and the truth data.
```

sensorData = timetable(Accelerometer, Gyroscope, ...
Magnetometer, GPSPosition, GPSVelocity, 'SampleRate', 100);
groundTruth = timetable(Orientation, Position, ...
'SampleRate', 100);

```

Create an insfilterAsync filter object that has a few noise properties.
filter = insfilterAsync('State', initialState, ...
'StateCovariance', initialStateCovariance, ...
```

'AccelerometerBiasNoise', le-7, ...
'GyroscopeBiasNoise', 1e-7, ...
'MagnetometerBiasNoise', 1e-7, ...
'GeomagneticVectorNoise', 1e-7);

```

Create a tuner configuration object for the filter. Set the maximum iterations to two. Also, set the tunable parameters as the unspecified properties.
```

config = tunerconfig('insfilterAsync','MaxIterations',8);
config.TunableParameters = setdiff(config.TunableParameters, ...
{'GeomagneticVectorNoise', 'AccelerometerBiasNoise', ...
'GyroscopeBiasNoise', 'MagnetometerBiasNoise'});
config.TunableParameters
ans = 1\times10 string
"AccelerationNoise" "AccelerometerNoise" "AngularVelocityNoise" "GPSPositionNoise"

```

Use the tuner noise function to obtain a set of initial sensor noises used in the filter.
```

measNoise = tunernoise('insfilterAsync')
measNoise = struct with fields:
AccelerometerNoise: 1
GyroscopeNoise: 1
MagnetometerNoise: 1
GPSPositionNoise: 1
GPSVelocityNoise: 1

```

Tune the filter and obtain the tuned parameters.
\begin{tabular}{lll} 
tunedParams \(=\) tune(filter, measNoise, sensorData,groundTruth, config); \\
Iteration & Parameter & Metric \\
\cline { 1 - 1 } 1 & & \\
1 & AccelerationNoise & 2.1345 \\
1 & AccelerometerNoise & 2.1264 \\
1 & AngularVelocityNoise & 1.9659 \\
1 & GPSPositionNoise & 1.9341 \\
1 & GPSVelocityNoise & 1.8420 \\
1 & GyroscopeNoise & 1.7589 \\
1 & MagnetometerNoise & 1.7362 \\
1 & PositionNoise & 1.7362 \\
1 & QuaternionNoise & 1.7218 \\
2 & VelocityNoise & 1.7218 \\
2 & AccelerationNoise & 1.7190 \\
2 & AccelerometerNoise & 1.7170 \\
2 & AngularVelocityNoise & 1.6045 \\
2 & GPSPositionNoise & 1.5948 \\
2 & GPSVelocityNoise & 1.5323 \\
2 & GyroscopeNoise & 1.4803 \\
2 & MagnetometerNoise & 1.4703 \\
2 & PositionNoise & 1.4703 \\
2 & QuaternionNoise & 1.4632 \\
3 & VelocityNoise & 1.4632 \\
3 & AccelerationNoise & 1.4596 \\
3 & AccelerometerNoise & 1.4548 \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|}
\hline 3 & GPSPositionNoise & 1.3810 \\
\hline 3 & GPSVelocityNoise & 1.3322 \\
\hline 3 & GyroscopeNoise & 1.2998 \\
\hline 3 & MagnetometerNoise & 1.2976 \\
\hline 3 & PositionNoise & 1.2976 \\
\hline 3 & QuaternionNoise & 1.2943 \\
\hline 3 & VelocityNoise & 1.2943 \\
\hline 4 & AccelerationNoise & 1.2906 \\
\hline 4 & AccelerometerNoise & 1.2836 \\
\hline 4 & AngularVelocityNoise & 1.2491 \\
\hline 4 & GPSPositionNoise & 1.2258 \\
\hline 4 & GPSVelocityNoise & 1.1880 \\
\hline 4 & GyroscopeNoise & 1.1701 \\
\hline 4 & MagnetometerNoise & 1.1698 \\
\hline 4 & PositionNoise & 1.1698 \\
\hline 4 & QuaternionNoise & 1.1688 \\
\hline 4 & VelocityNoise & 1.1688 \\
\hline 5 & AccelerationNoise & 1.1650 \\
\hline 5 & AccelerometerNoise & 1.1569 \\
\hline 5 & AngularVelocityNoise & 1.1454 \\
\hline 5 & GPSPositionNoise & 1.1100 \\
\hline 5 & GPSVelocityNoise & 1.0778 \\
\hline 5 & GyroscopeNoise & 1.0709 \\
\hline 5 & MagnetometerNoise & 1.0675 \\
\hline 5 & PositionNoise & 1.0675 \\
\hline 5 & QuaternionNoise & 1.0669 \\
\hline 5 & VelocityNoise & 1.0669 \\
\hline 6 & AccelerationNoise & 1.0634 \\
\hline 6 & AccelerometerNoise & 1.0549 \\
\hline 6 & AngularVelocityNoise & 1.0549 \\
\hline 6 & GPSPositionNoise & 1.0180 \\
\hline 6 & GPSVelocityNoise & 0.9866 \\
\hline 6 & GyroscopeNoise & 0.9810 \\
\hline 6 & MagnetometerNoise & 0.9775 \\
\hline 6 & PositionNoise & 0.9775 \\
\hline 6 & QuaternionNoise & 0.9768 \\
\hline 6 & VelocityNoise & 0.9768 \\
\hline 7 & AccelerationNoise & 0.9735 \\
\hline 7 & AccelerometerNoise & 0.9652 \\
\hline 7 & AngularVelocityNoise & 0.9652 \\
\hline 7 & GPSPositionNoise & 0.9283 \\
\hline 7 & GPSVelocityNoise & 0.8997 \\
\hline 7 & GyroscopeNoise & 0.8947 \\
\hline 7 & MagnetometerNoise & 0.8920 \\
\hline 7 & PositionNoise & 0.8920 \\
\hline 7 & QuaternionNoise & 0.8912 \\
\hline 7 & VelocityNoise & 0.8912 \\
\hline 8 & AccelerationNoise & 0.8885 \\
\hline 8 & AccelerometerNoise & 0.8811 \\
\hline 8 & AngularVelocityNoise & 0.8807 \\
\hline 8 & GPSPositionNoise & 0.8479 \\
\hline 8 & GPSVelocityNoise & 0.8238 \\
\hline 8 & GyroscopeNoise & 0.8165 \\
\hline 8 & MagnetometerNoise & 0.8165 \\
\hline 8 & PositionNoise & 0.8165 \\
\hline 8 & QuaternionNoise & 0.8159 \\
\hline 8 & VelocityNoise & 0.8159 \\
\hline
\end{tabular}

Fuse the sensor data using the tuned filter.
```

dt = seconds(diff(groundTruth.Time));
N = size(sensorData,1);
qEst = quaternion.zeros(N,1);
posEst = zeros(N,3);
% Iterate the filter for prediction and correction using sensor data.
for ii=1:N
if ii ~= 1
predict(filter, dt(ii-1));
end
if all(~isnan(Accelerometer(ii,:)))
fuseaccel(filter,Accelerometer(ii,:), ...
tunedParams.AccelerometerNoise);
end
if all(~isnan(Gyroscope(ii,:)))
fusegyro(filter, Gyroscope(ii,:), ...
tunedParams.GyroscopeNoise);
end
if all(~isnan(Magnetometer(ii,1)))
fusemag(filter, Magnetometer(ii,:), ...
tunedParams.MagnetometerNoise);
end
if all(~isnan(GPSPosition(ii,1)))
fusegps(filter, GPSPosition(ii,:), ...
tunedParams.GPSPositionNoise, GPSVelocity(ii,:), ...
tunedParams.GPSVelocityNoise);
end
[posEst(ii,:), qEst(ii,:)] = pose(filter);
end

```

Compute the RMS errors.
```

orientationError = rad2deg(dist(qEst, Orientation));

```
rmsorientationError \(=\operatorname{sqrt}(\) mean(orientationError.^2))
rmsorientationError = 2.7801
positionError = sqrt(sum((posEst - Position).^2, 2));
rmspositionError \(\left.=\operatorname{sqrt(mean(~positionError.}{ }^{\wedge} 2\right)\) )
rmspositionError \(=0.5966\)

Visualize the results.
figure();
\(\mathrm{t}=(0: \mathrm{N}-1) . /\) groundTruth.Properties.SampleRate;
subplot \((2,1,1)\)
plot(t, positionError, 'b');
title("Tuned insfilterAsync" + newline + "Euclidean Distance Position Error")
xlabel('Time (s)');
ylabel('Position Error (meters)')
subplot \((2,1,2)\)
plot(t, orientationError, 'b');
title("Orientation Error")
xlabel('Time (s)');
ylabel('Orientation Error (degrees)');

Tuned insfilterAsync Euclidean Distance Position Error



\section*{Input Arguments}

\section*{filterName - Name of fusion filter}
'insfilterAsync' | 'ahrs10filter'|'insfilterMARG'| 'insfilterNonholonomic' |
'insfitlerErrorState'
Name of fusion filter, specified as specified as one of these:
- 'ahrs10filter'
- 'insfilterAsync'
- 'insfilterMARG'
- 'insfitlerErrorState'
- 'insfilterNonholonomic'
filter - Fusion filter
fusion filter object
Fusion filter, specified as one of these fusion filter objects:
- insEKF
- ahrs10filter
- insfilterAsync
- insfilterMARG
- insfilterErrorState
- insfilterNonholonomic

\section*{Output Arguments}

\section*{noiseStruct - Structure of measurement noise}
structure
Structure of measurement noise, returned as a structure. The exact fields of structure depend on the filter object.

For example, the structure contains these fields for the insfilterAsync object.
\begin{tabular}{|l|l|l|}
\hline Field & Description & Default \\
\hline AccelerometerNoise & \begin{tabular}{l} 
Variance of accelerometer noise, \\
specified as a scalar in \(\left(\mathrm{m}^{2} / \mathrm{s}\right)^{2}\)
\end{tabular} & 1 \\
\hline GyroscopeNoise & \begin{tabular}{l} 
Variance of gyroscope noise, \\
specified as a scalar in \((\mathrm{rad} / \mathrm{s})^{2}\)
\end{tabular} & 1 \\
\hline MagnetometerNoise & \begin{tabular}{l} 
Variance of magnetometer \\
noise, specified as a scalar in \\
\((\mu \mathrm{T})^{2}\).
\end{tabular} & 1 \\
\hline GPSPositionNoise & \begin{tabular}{l} 
Variance of GPS position noise, \\
specified as a scalar in \(\mathrm{m}^{2}\)
\end{tabular} & 1 \\
\hline GPSVelocityNoise & \begin{tabular}{l} 
Standard deviation of GPS \\
velocity noise, specified as a \\
scalar in \((\mathrm{m} / \mathrm{s})^{2}\)
\end{tabular} & 1 \\
\hline
\end{tabular}

To use this structure with a tune function, change the values of the noise to proper values as initial guesses for tuning the noise. When the function tunes the measurement noise, it tunes all the elements in each field together. For example, if the AccelerometerNoise is specified as diag ( [ 1 0.1 1]), then the tune function varies AccelerometerNoise as the product of a scalar and the original diag([1 0.1 1]).

\section*{See Also}

\section*{Introduced in R2020b}

\section*{tunerPlotPose}

Plot filter pose estimates during tuning

\section*{Syntax}
stopTuning = tunerPlotPose(params,tunerValues)

\section*{Description}
stopTuning = tunerPlotPose(params,tunerValues) plots the current pose estimate, consisting of orientation (and possibly position, depending on the filter), and the ground truth values. params contains the best estimates of the filter parameters during the current tuning iteration. tunerValues contains information on the tuner configuration, sensor data, and ground truth data. Use this function as the value for the OutputFcn property of the tunerconfig object to plot the tuning results during iterations.

\section*{Examples}

\section*{Visualize Tuning Results Using tunerPlotPose}

Create a tunerconfiguration object. Set the tunerPlotPose function as the output function of the object.
```

tc = tunerconfig('imufilter','OutputFcn',@tunerPlotPose)
tc =
tunerconfig with properties:
Filter: "imufilter"
TunableParameters: ["AccelerometerNoise" "GyroscopeNoise" ... ]
StepForward: 1.1000
StepBackward: 0.5000
MaxIterations: 20
ObjectiveLimit: 0.1000
FunctionTolerance: 0
Display: iter
Cost: RMS
OutputFcn: @tunerPlotPose

```

Load prerecorded sensor data.
ld = load('imufilterTuneData.mat');
Tune an imufilter object using the sensor data. The truth data and the estimates are shown in a figure.
```

tune(imufilter,ld.sensorData,ld.groundTruth,tc)

```

\section*{Iteration \\ 1}

\section*{Parameter \\ AccelerometerNoise}




Metric
0.0857

Iteration: 1
RMS Orientation Error (deg): 4.9107
-Ground Truth
——Filter Estimale

\section*{Input Arguments}

\section*{params - Estimates of filter parameters}
structure
Estimates of filter parameters during the current iteration of the tuning process, specified as a structure. The structure contains one field for every public property of the filter and additional fields for any required measurement noise. The exact field names vary depending on the filter being tuned.

\section*{tunerValues - Tuner values}
structure

Tuner values, specified as a structure. The structure has these fields:
\begin{tabular}{|l|l|}
\hline Field Name & Description \\
\hline Iteration & \begin{tabular}{l} 
Iteration count of the tuner, specified as a \\
positive integer
\end{tabular} \\
\hline SensorData & Sensor data input to the tune function \\
\hline GroundTruth & Ground truth input to the tune function \\
\hline Configuration & tunerconfig object used for tuning \\
\hline Cost & Tuning cost at the end of the current iteration \\
\hline
\end{tabular}

\section*{Output Arguments}

\section*{stopTuning - Stop tuning process}
false
Stop the tuning process, returned as false. As a result, using the tunerPlotPose function as the output function of a tunerconfig object never terminates the tuning process of a fusion filter.

\section*{See Also}
tunerconfig|tunernoise |imufilter|ahrsfilter|ahrs10filter|insfilterMARG| insfilterAsync|insfilterErrorState|insfilterNonholonomic

Introduced in R2021a

\section*{writeBinaryOccupancyGrid}

Write values from grid to ROS message

\section*{Syntax}
writeBinary0ccupancyGrid(msg,map)

\section*{Description}
writeBinaryOccupancyGrid(msg,map) writes occupancy values and other information to the ROS message, msg, from the binary occupancy grid, map.

\section*{Input Arguments}

\section*{map - Binary occupancy grid}
binary0ccupancyMap object handle
Binary occupancy grid, specified as a binary0ccupancyMap object handle. map is converted to a ' nav_msgs/OccupancyGrid' message on the ROS network. map is an object with a grid of binary values, where 1 indicates an occupied location and 0 indications an unoccupied location.
msg - 'nav_msgs/OccupancyGrid' ROS message
OccupancyGrid object handle
'nav_msgs/OccupancyGrid' ROS message, specified as a OccupancyGrid object handle.

\section*{See Also}

\section*{Functions}
rosReadBinaryOccupancyGrid| rosRead0ccupancyMap3D | rosReadOccupancyGrid |
rosWriteOccupancyGrid
Introduced in R2015a

\section*{writeBytes}

Write raw commands to the GPS receiver

\section*{Syntax}
writeBytes(gps,cmdArray)

\section*{Description}
writeBytes (gps,cmdArray) writes raw commands specified by cmdArray to configure the GPS module.

\section*{Examples}

\section*{Write Configuration Commands to GPS Receiver}

Write configuration commands to the GPS receiver connected to the host computer using serialport object.

\section*{Required Hardware}

To run this example, you need:
- UBlox Neo-6M GPS module
- GPS antenna
- USB to UART module
- USB cable
- Connecting wires

\section*{Hardware Connection}


Connect the pins on the UBlox Neo-6M GPS module to the pins on your USB to UART module. The connections are:
- VCC -+5 V
- RX - TXO
- TX - RXI
- GND - GND

Connect the GPS antenna to the GPS module. Connect the USB to UART module to the host computer with a USB cable. GPS Fix can be easily acquired in locations that have a clear view of the sky. Wait for the GPS module to acquire satelite signals (Fix).This can be verified by checking the Fix LED (D1) of your GPS module.

\section*{Create GPS Object}

Connect to the GPS receiver using serialport object. Specify the port name and the baud rate.
```

s = serialport('COM4',9600)
s =
Serialport with properties:
Port: "COM4"
BaudRate: 9600
NumBytesAvailable: 0
Show all properties, functions
gps = gpsdev(s)
gps =
gpsdev with properties:
SerialPort: COM4
BaudRate: 9600 (bits/s)
SamplesPerRead: 1
ReadMode: "latest"
SamplesRead: 0
Show all properties all functions

```

\section*{Write Configuration Commands}

In the default configuration the GPS receiver returns the following NMEA messages: GPRMC, GPVTG, GPGGA, GPGSA, GPGSV, and GPGLL. The receiver can be configured to have a user defined set of output messages.

Read few lines of default messages from the serial port the GPS receiver is connected.
```

for i = 1:10
data = readline(s);
disp(data);
end
\$GPRMC, ,V, , , , , , , , , ,N*53
\$GPVTG, , , , , , , , ,N*30

```
```

\$GPGGA, , , , , 0,00,99.99, , , , , ,*48
\$GPGSA, A ,1, , , , , , , , , , , , 99.99,99.99,99.99*30
\$GPGSV,2,1,08,01, , ,18,08, , ,12,09, ,,12,15, , ,19*77
\$GPGSV,2,2,08,23,,,13,24,, ,09,25,,,10,27, , ,25*79
\$GPGLL, , , , , V,N*64
\$GPRMC, ,V, , , , , , , , , N*53
\$GPVTG, , , , , , , , ,N*30
\$GPGGA, , , , , 0,00,99.99, , , , , ,*48

```

Write the version monitor command to the GPS receiver to return the software and hardware version of the GPS receiver.
```

configCMD = [0xB5 0x62 0x0A 0x04 0x00 0x00 0x0E 0x34];
% writeBytes(gps,cfg)
write(s,configCMD,'uint8')

```

Read few lines of messages again to verify the version message.
```

for i = 1:10
data = readline(s);
disp(data);
end
\$GPGSA,A,1, , , , , , , , , , , ,99.99,99.99,99.99*30
\$GPGSV,2,1,05,01, , ,13,09, , ,11,15, , ,16,23, , , 12*74
\$GPGSV, 2, 2,05,25,, ,10*7A
$GPGLL, , , , , V,N*64
\mub
( 7.03 (45969) 00040007 `$GPRMC,,V,,,,,,,,,, ,N*53
\$GPVTG, , , , , , , , ,N*30
\$GPGGA, , , , ,0,00,99.99, , , , , ,*48
\$GPGSA,A,1, , , , , , , , , , , ,99.99,99.99,99.99*30
\$GPGSV,2,1,06,01, , ,11,09, , ,11,23, ,,14,24, , ,21*75

```

It can be observed from the output, 7.03 (45969) is the software version and 00040007 is the hardware version.

\section*{Clean Up}

When the connection is no longer needed, clear the associated object.
```

delete(gps);
clear gps;
clear s;

```

\section*{Input Arguments}

\section*{gps - GPS sensor}
gpsdev object
The GPS sensor, specified as a gpsdev object.

\section*{cmdArray - Raw command to configure GPS module}
hexadecimal array
Raw command to configure the GPS module, specified as an hexadecimal array.
```

Example:[0xB5 0x62 0x06 0x01 0x08 0x00 0xF0 0x08 0x00 0x01 0x00 0x00 0x00 0x00
0x08 0x60]
Data Types: uint8

```

\section*{See Also}

Objects
gpsdev
Functions
flush|release|read|info
Introduced in R2020b

\section*{writeOccupancyGrid}

Write values from grid to ROS message

\section*{Syntax}
writeOccupancyGrid(msg,map)

\section*{Description}
write0ccupancyGrid(msg,map) writes occupancy values and other information to the ROS message, msg, from the occupancy grid, map.

\section*{Input Arguments}
```

msg - 'nav_msgs/OccupancyGrid' ROS message
OccupancyGrid object handle

```
'nav_msgs/0ccupancyGrid' ROS message, specified as an OccupancyGrid ROS message object handle.
map - Occupancy map
occupancyMap object handle
Occupancy map, specified as an occupancyMap object handle.

\section*{See Also}

\section*{Functions}
rosReadBinary0ccupancyGrid | rosRead0ccupancyMap3D | rosRead0ccupancyGrid |
rosWriteOccupancyGrid
Introduced in R2016b

Classes

\section*{accelparams}

Accelerometer sensor parameters

\section*{Description}

The accelparams class creates an accelerometer sensor parameters object. You can use this object to model an accelerometer when simulating an IMU with imuSensor. See the "Algorithms" on page 2-477 section of imuSensor for details of accelparams modeling.

\section*{Creation}

\section*{Syntax}
params = accelparams
params = accelparams(Name,Value)

\section*{Description}
params = accelparams returns an ideal accelerometer sensor parameters object with default values.
params = accelparams(Name, Value) configures an accelerometer sensor parameters object properties using one or more Name-Value pair arguments. Name is a property name and Value is the corresponding value. Name must appear inside single quotes (' ' ). You can specify several namevalue pair arguments in any order as (Name1,Value1, ... , NameN, ValueN). Any unspecified properties take default values.

\section*{Properties}

\section*{MeasurementRange - Maximum sensor reading (m/s²)}
inf (default) | real positive scalar
Maximum sensor reading in \(\mathrm{m} / \mathrm{s}^{2}\), specified as a real positive scalar.

\section*{Data Types: single | double}

\section*{Resolution - Resolution of sensor measurements ((m/s \(\left.\left.{ }^{2}\right) / L S B\right)\)}

0 (default) | real nonnegative scalar
Resolution of sensor measurements in \(\left(\mathrm{m} / \mathrm{s}^{2}\right) / \mathrm{LSB}\), specified as a real nonnegative scalar. Here, LSB is the acronym for least significant bit. Resolution is often referred to as Scale Factor for accelerometer.
Data Types: single | double

\section*{ConstantBias - Constant sensor offset bias (m/s \(\mathbf{s}^{\mathbf{2}}\) )}
[0000] (default) | real scalar | real 3-element row vector
Constant sensor offset bias in \(\mathrm{m} / \mathrm{s}^{2}\), specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3 -element row vector where each element has the input scalar value.

\section*{Data Types: single |double}

\section*{AxesMisalignment - Sensor axes skew (\%)}
diag([100 100 100]) (default)| scalar in the range [0,100]|3-element row vector in the range \([0,100] \mid 3\)-by-3 matrix in the range \([0,100]\)

Sensor axes skew in percentage, specified as a scalar, a 3-element row vector, or a 3-by-3 matrix with values ranging from 0 to 100. The diagonal elements of the matrix account for the misalignment effects for each axes. The off-diagonal elements account for the cross-axes misalignment effects. The measured state \(v_{\text {measure }}\) is obtained from the true state \(v_{\text {true }}\) via the misalignment matrix as:
\[
v_{\text {measure }}=\frac{1}{100} M v_{\text {true }}=\frac{1}{100}\left[\begin{array}{lll}
m_{11} & m_{12} & m_{13} \\
m_{21} & m_{22} & m_{23} \\
m_{31} & m_{32} & m_{33}
\end{array}\right] v_{\text {true }}
\]
- If you specify the property as a scalar, then all the off-diagonal elements of the matrix take the value of the specified scalar and all the diagonal elements are 100.
- If you specify the property as a vector \([a b c]\), then \(m_{21}=m_{31}=a, m_{12}=m_{32}=b\), and \(m_{13}=m_{23}=\) c. All the diagonal elements are 100 .

Data Types: single | double

\section*{NoiseDensity - Power spectral density of sensor noise ( \(\mathrm{m} / \mathrm{s}^{2} / \sqrt{ } \mathrm{Hz}\) )}
[0 0000\(]\) (default) |real scalar | real 3-element row vector
Power spectral density of sensor noise in \(\left(\mathrm{m} / \mathrm{s}^{2} / \sqrt{ } \mathrm{Hz}\right)\), specified as a real scalar or 3-element row vector. This property corresponds to the velocity random walk (VRW). Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.
Data Types: single | double

\section*{BiasInstability - Instability of the bias offset (m/s \({ }^{\mathbf{2}}\) )}
[0 0 0 0 \(]\) (default) | real scalar | real 3-element row vector
Instability of the bias offset in \(\mathrm{m} / \mathrm{s}^{2}\), specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.
Data Types: single|double

\section*{}
[0 00 0 \(]\) (default) | real scalar | real 3-element row vector
Integrated white noise of sensor in \(\left(\mathrm{m} / \mathrm{s}^{2}\right)(\sqrt{\mathrm{Hz}})\), specified as a real scalar or 3 -element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.
Data Types: single | double

\section*{TemperatureBias - Sensor bias from temperature ( \(\left.\left(\mathbf{m} / \mathbf{s}^{2}\right) /{ }^{\circ} \mathbf{C}\right)\)}
[0 0 0 0 \(]\) (default) | real scalar | real 3-element row vector
Sensor bias from temperature in \(\left(\mathrm{m} / \mathrm{s}^{2}\right) /{ }^{\circ} \mathrm{C}\), specified as a real scalar or 3 -element row vector. Any scalar input is converted into a real 3 -element row vector where each element has the input scalar value.

Data Types: single | double

\section*{TemperatureScaleFactor - Scale factor error from temperature (\%/ \({ }^{\circ} \mathrm{C}\) )}
[ \(\left.\begin{array}{lll}0 & 0 & 0\end{array}\right]\) (default) | real scalar in the range \([0,100] \mid\) real 3 -element row vector in the range \([0,100]\)
Scale factor error from temperature in \(\% /{ }^{\circ} \mathrm{C}\), specified as a real scalar or real 3-element row vector with values ranging from 0 to 100. Any scalar input is converted into a real 3 -element row vector where each element has the input scalar value.

Data Types: single | double

\section*{Examples}

\section*{Generate Accelerometer Data from Stationary Inputs}

Generate accelerometer data for an imuSensor object from stationary inputs.
Generate an accelerometer parameter object with a maximum sensor reading of \(19.6 \mathrm{~m} / \mathrm{s}^{2}\) and a resolution of \(0.598\left(\mathrm{~mm} / \mathrm{s}^{2}\right) / \mathrm{LSB}\). The constant offset bias is \(0.49 \mathrm{~m} / \mathrm{s}^{2}\). The sensor has a power spectral density of \(3920\left(\mu \mathrm{~m} / \mathrm{s}^{2}\right) / \sqrt{\mathrm{Hz}}\). The bias from temperature is \(0.294\left(\mathrm{~m} / \mathrm{s}^{2}\right) / 0 \mathrm{C}\). The scale factor error from temperature is \(0.02 \% / 0 \mathrm{C}\). The sensor axes are skewed by \(2 \%\).
```

params = accelparams('MeasurementRange',19.6,'Resolution',0.598e-3,'ConstantBias',0.49,'NoiseDen:

```

Use a sample rate of 100 Hz spaced out over 1000 samples. Create the imuSensor object using the accelerometer parameter object.
```

Fs = 100;
numSamples = 1000;
t = 0:1/Fs:(numSamples-1)/Fs;
imu = imuSensor('SampleRate', Fs, 'Accelerometer', params);

```

Generate accelerometer data from the imuSensor object.
```

orient = quaternion.ones(numSamples, 1);
acc = zeros(numSamples, 3);
angvel = zeros(numSamples, 3);
accelData = imu(acc, angvel, orient);

```

Plot the resultant accelerometer data.
```

plot(t, accelData)
title('Accelerometer')
xlabel('s')
ylabel('m/s^2')

```


\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder \(^{\text {TM }}\).

\section*{See Also}
imuSensor | gyroparams | magparams
Introduced in R2018b

\section*{ahrs10filter}

Height and orientation from MARG and altimeter readings

\section*{Description}

The ahrs10filter object fuses MARG and altimeter sensor data to estimate device height and orientation. MARG (magnetic, angular rate, gravity) data is typically derived from magnetometer, gyroscope, and accelerometer sensors. The filter uses an 18-element state vector to track the orientation quaternion, vertical velocity, vertical position, MARG sensor biases, and geomagnetic vector. The ahrs10filter object uses an extended Kalman filter to estimate these quantities.

\section*{Creation}

\section*{Syntax}
```

FUSE = ahrs10filter
FUSE = ahrsl0filter('ReferenceFrame',RF)
FUSE = ahrs10filter(

```
\(\qquad\)
``` ,Name, Value)
```


## Description

FUSE = ahrs10filter returns an extended Kalman filter object, FUSE, for sensor fusion of MARG and altimeter readings to estimate device height and orientation.

FUSE = ahrs10filter('ReferenceFrame', RF) returns an extended Kalman filter object that estimates device height and orientation relative to the reference frame RF. Specify RF as 'NED ' (North-East-Down) or 'ENU ' (East-North-Up). The default value is 'NED'.

FUSE = ahrs10filter( __ , Name, Value) sets each property Name to the specified Value. Unspecified properties have default values.

## Properties

IMUSampleRate - Sample rate of the IMU (Hz)
100 (default) | positive scalar
Sample rate of the IMU in Hz , specified as a positive scalar.
Data Types: single | double
GyroscopeNoise - Multiplicative process noise variance from gyroscope ((rad/s) ${ }^{\mathbf{2}}$ )
[1e-9,1e-9,1e-9] (default) | scalar | three-element row vector
Multiplicative process noise variance from the gyroscope in (rad/s) ${ }^{2}$, specified as positive real finite numbers.
Data Types: single | double

AccelerometerNoise - Multiplicative process noise variance from accelerometer ((m/s²) [1e-4,1e-4,1e-4] (default) | scalar | three-element row vector

Multiplicative process noise variance from the accelerometer in $\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}$, specified as positive real finite numbers.

Data Types: single | double
GyroscopeBiasNoise - Multiplicative process noise variance from gyroscope bias ((rad/
$\left.\mathbf{s}^{2}\right)^{2}$ )
[1e-10,1e-10,1e-10] (default) | scalar | three-element row vector
Multiplicative process noise variance from the gyroscope bias in $\left(\mathrm{rad} / \mathrm{s}^{2}\right)^{2}$, specified as positive real finite numbers.

Data Types: single | double
AccelerometerBiasNoise - Multiplicative process noise variance from accelerometer bias ( $\left.\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}\right)$
[1e-4,1e-4,1e-4] (default) | scalar | three-element row vector
Multiplicative process noise variance from the accelerometer bias in $\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}$, specified as positive real finite numbers.
Data Types: single | double

## GeomagneticVectorNoise - Additive process noise for geomagnetic vector ( $\mu \mathrm{T}^{\mathbf{2}}$ )

[1e-6,1e-6,1e-6] (default) | scalar | three-element row vector
Additive process noise for geomagnetic vector in $\mu \mathrm{T}^{2}$, specified as positive real finite numbers.
Data Types: single| double
MagnetometerBiasNoise - Additive process noise for magnetometer bias ( $\boldsymbol{\mu} \mathbf{T}^{\mathbf{2}}$ )
[0.1,0.1,0.1] (default)| scalar | three-element row vector
Additive process noise for magnetometer bias in $\mu \mathrm{T}^{2}$, specified as positive real finite numbers.
Data Types: single|double

## State - State vector of extended Kalman filter

18-element column vector
State vector of the extended Kalman filter. The state values represent:

| State | Units | Index |
| :--- | :--- | :--- |
| Orientation (quaternion parts) | $\mathrm{N} / \mathrm{A}$ | $1: 4$ |
| Altitude (NED or ENU) | m | 5 |
| Vertical Velocity (NED or ENU) | $\mathrm{m} / \mathrm{s}$ | 6 |
| Delta Angle Bias (XYZ) | $\mathrm{rad} / \mathrm{s}$ | $7: 9$ |
| Delta Velocity Bias (XYZ) | $\mathrm{m} / \mathrm{s}$ | $10: 12$ |
| Geomagnetic Field Vector (NED <br> or ENU) | $\mu \mathrm{T}$ | $13: 15$ |
| Magnetometer Bias (XYZ) | $\mu \mathrm{T}$ | $16: 18$ |

The default initial state corresponds to an object at rest located at [0000] in geodetic LLA coordinates.

Data Types: single | double
StateCovariance - State error covariance for extended Kalman filter
eye(18)*1e-6 (default) | 18-by-18 matrix
State error covariance for the Kalman filter, specified as an 18-by-18-element matrix of real numbers.
Data Types: single | double

## Object Functions

predict
fusemag
fusealtimeter
correct
residual
residualmag
residualaltimeter
pose
reset
stateinfo
tune
copy

Update states using accelerometer and gyroscope data for ahrs10filter
Correct states using magnetometer data for ahrs10filter
Correct states using altimeter data for ahrs10filter
Correct states using direct state measurements for ahrs10filter
Residuals and residual covariances from direct state measurements for ahrs10filter
Residuals and residual covariance from magnetometer measurements for ahrs10filter
Residuals and residual covariance from altimeter measurements for ahrs10filter Current orientation and position estimate for ahrs10filter Reset internal states for ahrs10filter
Display state vector information for ahrs10filter
Tune ahrs10filter parameters to reduce estimation error
Create copy of ahrs10filter

## Examples

## Estimate Pose of UAV

Load logged sensor data, ground truth pose, and initial state and initial state covariance. Calculate the number of IMU samples per altimeter sample and the number of IMU samples per magnetometer sample.

```
load('fuse10exampledata.mat', ...
    'imuFs','accelData','gyroData', ...
    'magnetometerFs','magData', ...
    'altimeterFs','altData', ...
    'expectedHeight','expectedOrient', ...
    'initstate','initcov');
imuSamplesPerAlt = fix(imuFs/altimeterFs);
imuSamplesPerMag = fix(imuFs/magnetometerFs);
```

Create an AHRS filter that fuses MARG and altimeter readings to estimate height and orientation. Set the sampling rate and measurement noises of the sensors. The values were determined from datasheets and experimentation.

```
filt = ahrs10filter('IMUSampleRate',imuFs, ...
    'AccelerometerNoise',0.1, ...
    'State',initstate, ...
    'StateCovariance',initcov);
```

```
Ralt = 0.24;
Rmag = 0.9;
```

Preallocate variables to log height and orientation.

```
numIMUSamples = size(accelData,1);
estHeight = zeros(numIMUSamples,1);
estOrient = zeros(numIMUSamples,1,'quaternion');
```

Fuse accelerometer, gyroscope, magnetometer and altimeter data. The outer loop predicts the filter forward at the fastest sample rate (the IMU sample rate).

```
for ii = 1:numIMUSamples
    % Use predict to estimate the filter state based on the accelometer and
    % gyroscope data.
    predict(filt,accelData(ii,:),gyroData(ii,:));
    % Magnetometer data is collected at a lower rate than IMU data. Fuse
    % magnetometer data at the lower rate.
    if ~mod(ii,imuSamplesPerMag)
        fusemag(filt,magData(ii,:),Rmag);
    end
    % Altimeter data is collected at a lower rate than IMU data. Fuse
    % altimeter data at the lower rate.
    if ~mod(ii, imuSamplesPerAlt)
        fusealtimeter(filt,altData(ii),Ralt);
    end
    % Log the current height and orientation estimate.
    [estHeight(ii),estOrient(ii)] = pose(filt);
end
```

Calculate the RMS errors between the known true height and orientation and the output from the AHRS filter.

```
pErr = expectedHeight - estHeight;
qErr = rad2deg(dist(expectedOrient,estOrient));
pRMS = sqrt(mean(pErr.^2));
qRMS = sqrt(mean(qErr.^2));
fprintf('Altitude RMS Error\n');
Altitude RMS Error
fprintf('\t%.2f (meters)\n\n',pRMS);
    0.38 (meters)
```

Visualize the true and estimated height over time.

```
t = (0:(numIMUSamples-1))/imuFs;
plot(t,expectedHeight);hold on
plot(t,estHeight);hold off
legend('Ground Truth','Estimated Height','location','best')
ylabel('Height (m)')
```

xlabel('Time (s)')
grid on

fprintf('Quaternion Distance RMS Error\n');
Quaternion Distance RMS Error
fprintf('\t\%.2f (degrees) \n\n',qRMS);
2.93 (degrees)

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

ahrsfilter|insfilter
Introduced in R2019a

## correct

Correct states using direct state measurements for ahrs10filter

## Syntax

```
correct(FUSE,idx,measurement,measurementCovariance)
```


## Description

correct(FUSE,idx, measurement, measurementCovariance) corrects the state and state estimation error covariance based on the measurement and measurement covariance. The measurement maps directly to the state specified by the indices idx.

## Input Arguments

FUSE - ahrs10filter object
object
Object of ahrs10filter.

## idx - State vector index of measurement to correct

N -element vector of increasing integers in the range $[1,18]$
State vector index of measurement to correct, specified as an $N$-element vector of increasing integers in the range $[1,18]$.

The state values represent:

| State | Units | Index |
| :--- | :--- | :--- |
| Orientation (quaternion parts) | $\mathrm{N} / \mathrm{A}$ | $1: 4$ |
| Altitude (NED) | m | 5 |
| Vertical Velocity (NED) | $\mathrm{m} / \mathrm{s}$ | 6 |
| Delta Angle Bias (XYZ) | $\mathrm{rad} / \mathrm{s}$ | $7: 9$ |
| Delta Velocity Bias (XYZ) | $\mathrm{m} / \mathrm{s}$ | $10: 12$ |
| Geomagnetic Field Vector (NED) | $\mu \mathrm{T}$ | $13: 15$ |
| Magnetometer Bias (XYZ) | $\mu \mathrm{T}$ | $16: 18$ |

Data Types: single | double
measurement - Direct measurement of state
$N$-element vector
Direct measurement of state, specified as a $N$-element vector. $N$ is the number of elements of the index argument, idx.
Data Types: single | double

## measurementCovariance - Covariance of measurement

scalar | $N$-element vector | $N$-by- $N$ matrix
Covariance of measurement, specified as a scalar, $N$-element vector, or $N$-by- $N$ matrix. $N$ is the number of elements of the index argument, idx.

Data Types: single | double

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® $\mathrm{Coder}^{\mathrm{TM}}$.

## See Also

ahrs10filter|insfilter
Introduced in R2019a

## copy

Create copy of ahrs10filter

## Syntax

newFilter $=$ copy(filter)

## Description

newFilter $=$ copy(filter) returns a copy of the ahrs10filter, filter, with the exactly same property values.

## Input Arguments

filter - Filter to be copied ahrs10filter

Filter to be copied, specified as an ahrs10filter object.

## Output Arguments

newFilter - New copied filter
ahrs10filter
New copied filter, returned as an ahrs10filter object.

## See Also

ahrs10filter
Introduced in R2020b

## fusealtimeter

Correct states using altimeter data for ahrs10filter

## Syntax

[res,resCov] = fusealtimeter(FUSE,altimeterReadings, altimeterReadingsCovariance)

## Description

[res,resCov] = fusealtimeter(FUSE,altimeterReadings, altimeterReadingsCovariance) fuses altimeter data to correct the state estimate.

## Input Arguments

FUSE - ahrs10filter object
object
Object of ahrs10filter.
altimeterReadings - Altimeter readings (m)
real scalar
Altimeter readings in meters, specified as a real scalar.
Data Types: single | double
altimeterReadingsCovariance - Altimeter readings error covariance (m²)
real scalar
Altimeter readings error covariance in $\mathrm{m}^{2}$, specified as a real scalar.
Data Types: single | double

## Output Arguments

res - Measurement residual
scalar
Measurement residual, returned as a scalar in meters.
resCov - Residual covariance
nonnegative scalar
Residual covariance, returned as a nonnegative scalar in $\mathrm{m}^{2}$.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.

## See Also

ahrs10filter|insfilter

Introduced in R2019a

## fusemag

Correct states using magnetometer data for ahrs10filter

## Syntax

[res,resCov] = fusemag(FUSE,magReadings,magReadingsCovariance)

## Description

[res,resCov] = fusemag(FUSE,magReadings,magReadingsCovariance) fuses magnetometer data to correct the state estimate.

## Input Arguments

FUSE - ahrs10filter object
object
Object of ahrs10filter.
magReadings - Magnetometer readings ( $\mu \mathrm{T}$ )
3-element row vector
Magnetometer readings in $\mu \mathrm{T}$, specified as a 3-element row vector of finite real numbers.
Data Types: single | double
magReadingsCovariance - Magnetometer readings error covariance ( $\boldsymbol{\mu} \mathbf{T}^{\mathbf{2}}$ )
scalar | 3-element row vector | 3-by-3 matrix
Magnetometer readings error covariance in $\mu \mathrm{T}^{2}$, specified as a scalar, 3-element row vector, or 3-by-3 matrix.
Data Types: single | double

## res - Residual

1-by-3 vector of real values
Residual, returned as a 1-by-3 vector of real values in $\mu \mathrm{T}$.
Data Types: single | double
resCov - Residual covariance
3-by-3 matrix of real values
Residual covariance, returned a 3-by-3 matrix of real values in $(\mu \mathrm{T})^{2}$.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

ahrs10filter|insfilter
Introduced in R2019a

## pose

Current orientation and position estimate for ahrs10filter

## Syntax

[position, orientation, velocity] = pose(FUSE)
[position, orientation, velocity] = pose(FUSE,format)

## Description

[position, orientation, velocity] = pose(FUSE) returns the current estimate of the pose.
[position, orientation, velocity] = pose(FUSE,format) returns the current estimate of the pose with orientation in the specified orientation format.

## Input Arguments

FUSE - ahrs10filter object
object
Object of ahrs10filter.

## format - Output orientation format

'quaternion' (default) | 'rotmat'
Output orientation format, specified as either 'quaternion' for a quaternion or 'rotmat' for a rotation matrix.
Data Types: char | string

## Output Arguments

position - Position estimate expressed in the local coordinate system (m)
3 -element row vector
Position estimate expressed in the local coordinate system of the filter in meters, returned as a 3element row vector.
Data Types: single | double

## orientation - Orientation estimate expressed in the local coordinate system

quaternion (default) | 3-by-3 rotation matrix
Orientation estimate expressed in the local coordinate system of the filter, returned as a scalar quaternion or 3-by-3 rotation matrix. The quaternion or rotation matrix represents a frame rotation from the local reference frame of the filter to the body reference frame.
Data Types: single|double | quaternion
velocity - Velocity estimate expressed in local coordinate system (m/s)
3-element row vector

Velocity estimate expressed in the local coordinate system of the filter in $\mathrm{m} / \mathrm{s}$, returned as a 3-element row vector.

Data Types: single | double

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

ahrs10filter|insfilter
Introduced in R2019a

## predict

Update states using accelerometer and gyroscope data for ahrs10filter

## Syntax

predict(FUSE, accelReadings,gyroReadings)

## Description

predict(FUSE, accelReadings, gyroReadings) fuses accelerometer and gyroscope data to update the state estimate.

## Input Arguments

```
FUSE - ahrs10Filter object
object
```

Object of ahrs10filter.
accelReadings - Accelerometer readings in the sensor body coordinate system ( $\mathbf{m} / \mathbf{s}^{\mathbf{2}}$ )
N -by-3 matrix
Accelerometer readings in local sensor body coordinate system in $\mathrm{m} / \mathrm{s}^{2}$, specified as an $N$-by- 3 matrix. $N$ is the number of samples, and the three columns of accelReadings represent the [ $x y z$ ] measurements. Accelerometer readings are assumed to correspond to the sample rate specified by the IMUSampleRate property.
Data Types: single | double
gyroReadings - Gyroscope readings in the sensor body coordinate system (rad/s)
$N$-by-3 matrix
Gyroscope readings in the sensor body coordinate system in rad/s, specified as an $N$-by- 3 matrix. $N$ is the number of samples, and the three columns of gyroReadings represent the $[x y z]$ measurements. Gyroscope readings are assumed to correspond to the sample rate specified by the IMUSampleRate property.
Data Types: single | double

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

ahrs10filter|insfilter
Introduced in R2019a

## reset

Reset internal states for ahrs10filter

## Syntax

reset (FUSE)

## Description

reset (FUSE) resets the State, StateCovariance, and internal integrators to their default values.

## Input Arguments

FUSE - ahrs10filter object
object
Object of ahrs10filter.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

ahrs10filter|insfilter
Introduced in R2019a

## residual

Residuals and residual covariances from direct state measurements for ahrs10filter

## Syntax

[res, resCov]= residual(FUSE,idx,measurement,measurementCovariance)

## Description

[res, resCov]= residual(FUSE,idx,measurement,measurementCovariance) computes the residual, res, and the residual covariance, resCov, based on the direct state measurement and measurement covariance. The measurement maps directly to the states specified by indices, idx.

## Input Arguments

FUSE - ahrs10filter
ahrs10filter|object
ahrs10filter, specified as an object.

## idx - State vector index of measurement to correct

$N$-element vector of increasing integers in the range $[1,18]$
State vector index of measurement to correct, specified as an $N$-element vector of increasing integers in the range $[1,18]$.

The state values represent:

| State | Units | Index |
| :--- | :--- | :--- |
| Orientation (quaternion parts) | $\mathrm{N} / \mathrm{A}$ | $1: 4$ |
| Altitude (NED) | m | 5 |
| Vertical Velocity (NED) | $\mathrm{m} / \mathrm{s}$ | 6 |
| Delta Angle Bias (XYZ) | $\mathrm{rad} / \mathrm{s}$ | $7: 9$ |
| Delta Velocity Bias (XYZ) | $\mathrm{m} / \mathrm{s}$ | $10: 12$ |
| Geomagnetic Field Vector (NED) | $\mu \mathrm{T}$ | $13: 15$ |
| Magnetometer Bias (XYZ) | $\mu \mathrm{T}$ | $16: 18$ |

## measurement - Direct measurement of state

$N$-element vector
Direct measurement of state, specified as a $N$-element vector. $N$ is the number of elements of the index argument, idx.

## measurementCovariance - Covariance of measurement

$N$-by- $N$ matrix
Covariance of measurement, specified as an $N$-by- $N$ matrix. $N$ is the number of elements of the index argument, idx.

## Output Arguments

res - Measurement residual
1 -by- $N$ vector of real values
Measurement residual, returned as a 1-by- $N$ vector of real values.
resCov - Residual covariance
$N$-by- $N$ matrix of real values
Residual covariance, returned as a $N$-by- $N$ matrix of real values.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® $\operatorname{Coder}^{\text {™ }}$.

## See Also

ahrs10filter

Introduced in R2020a

## residualaltimeter

Residuals and residual covariance from altimeter measurements for ahrs10filter

## Syntax

[res,resCov] = residualaltimeter(FUSE,altimeterReadings, altimeterReadingsCovariance)

## Description

[res,resCov] = residualaltimeter(FUSE,altimeterReadings,
altimeterReadingsCovariance) computes the residual, res, and the innovation covariance, resCov, based on the magnetometer readings and the corresponding covariance.

## Input Arguments

FUSE - ahrs10filter
ahrs10filter|object
ahrs10filter, specified as an object.
altimeterReadings - Altimeter readings (m)
real scalar
Altimeter readings in meters, specified as a real scalar.
Data Types: single | double
altimeterReadingsCovariance - Altimeter readings error covariance ( $\mathbf{m}^{\mathbf{2}}$ )
real scalar
Altimeter readings error covariance in $\mathrm{m}^{2}$, specified as a real scalar.
Data Types: single | double

## Output Arguments

## res - Measurement residual

scalar
Measurement residual, returned as a scalar in meters.
resCov - Residual covariance
nonnegative scalar
Residual covariance, returned as a nonnegative scalar in $\mathrm{m}^{2}$.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

ahrs10filter|insfilter
Introduced in R2020a

## residualmag

Residuals and residual covariance from magnetometer measurements for ahrs10filter

## Syntax

[res,resCov] = residualmag(FUSE,magReadings,magReadingsCovariance)

## Description

[res,resCov] = residualmag(FUSE,magReadings,magReadingsCovariance) computes the residual, residual, and the residual covariance, resCov, based on the magnetometer readings and the corresponding covariance.

## Input Arguments

FUSE - ahrs10filter
ahrs10filter|object
ahrs10filter, specified as an object.
magReadings - Magnetometer readings ( $\mu \mathrm{T}$ )
3-element row vector
Magnetometer readings in $\mu \mathrm{T}$, specified as a 3-element row vector of finite real numbers.
Data Types: single | double
magReadingsCovariance - Magnetometer readings error covariance ( $\boldsymbol{\mu} \mathbf{T}^{\mathbf{2}}$ )
scalar | 3-element row vector | 3-by-3 matrix
Magnetometer readings error covariance in $\mu \mathrm{T}^{2}$, specified as a scalar, 3 -element row vector, or 3-by-3 matrix.

Data Types: single | double

## Output Arguments

## res - Residual

1-by-3 vector of real values
Residual, returned as a 1-by-3 vector of real values in $\mu \mathrm{T}$.
Data Types: single | double

## resCov - Residual covariance

3-by-3 matrix of real values
Residual covariance, returned a 3-by-3 matrix of real values in $(\mu \mathrm{T})^{2}$.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

ahrs10filter
Introduced in R2020a

## stateinfo

Display state vector information for ahrs10filter

## Syntax

stateinfo(FUSE)
info = stateinfo(FUSE)

## Description

stateinfo(FUSE) displays the meaning of each index of the State property and the associated units.
info = stateinfo(FUSE) returns a structure with fields containing descriptions of the elements of the state vector of the filter, FUSE.

## Examples

## State information of ahrs10filter

Create an ahrs10filter object.

```
filter = ahrs10filter;
```

Display the state information of the created filter.

```
stateinfo(filter)
```

| States | Units | Index |
| :--- | :--- | :--- |
| Orientation (quaternion parts) |  | $1: 4$ |
| Altitude (NAV) | m | 5 |
| Vertical Velocity (NAV) | $\mathrm{m} / \mathrm{s}$ | 6 |
| Delta Angle Bias (XYZ) | rad | $7: 9$ |
| Delta Velocity Bias (XYZ) | $\mathrm{m} / \mathrm{s}$ | $10: 12$ |
| Geomagnetic Field Vector (NAV) | $\mu \mathrm{T}$ | $13: 15$ |
| Magnetometer Bias (XYZ) | $\mu \mathrm{T}$ | $16: 18$ |

Output the state information of the filter as a structure.

```
info = stateinfo(filter)
info = struct with fields:
    Orientation: [1 2 3 4]
                        Altitude: 5
        VerticalVelocity: 6
        DeltaAngleBias: [7 8 9]
        DeltaVelocityBias: [10 11 12]
    GeomagneticFieldVector: [13 14 15 15
        MagnetometerBias: [lllll
```


## Input Arguments

FUSE - ahrs10filter object
object
Object of ahrs10filter.

## Output Arguments

info - State information
structure
State information, returned as a structure. The field names of the structure are names of the elements of the state vector in the filter. The values of each field are the corresponding indices of the state vector.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

See Also<br>ahrs10filter|insfilter

Introduced in R2019a

## tune

Tune ahrs10filter parameters to reduce estimation error

## Syntax

tunedMeasureNoise = tune(filter, measureNoise,sensorData, groundTruth) tunedMeasureNoise = tune( $\qquad$ , config)

## Description

tunedMeasureNoise = tune(filter,measureNoise, sensorData, groundTruth) adjusts the properties of the ahrs10filter filter object, filter, and measurement noises to reduce the root-mean-squared (RMS) state estimation error between the fused sensor data and the ground truth. The function also returns the tuned measurement noise, tunedMeasureNoise. The function uses the property values in the filter and the measurement noise provided in the measureNoise structure as the initial estimate for the optimization algorithm.
tunedMeasureNoise = tune( $\qquad$ , config) specifies the tuning configuration based on a tunerconfig object, config.

## Examples

## Tune ahrs10filter to Optimize Pose Estimate

Load the recorded sensor data and ground truth data.

```
load('ahrs10filterTuneData.mat');
```

Create tables for the sensor data and the truth data.

```
sensorData = table(Accelerometer,Gyroscope,...
    Magnetometer,Altimeter);
groundTruth = table(Orientation, Altitude);
```

Create an ahrs10filter filter object.

```
filter = ahrs10filter('State', initialState, ...
    'StateCovariance', initialStateCovariance);
```

Create a tuner configuration object for the filter. Set the maximum iterations to ten and set the objective limit to 0.001 .

```
cfg = tunerconfig('ahrs10filter','MaxIterations',10,...
    'ObjectiveLimit',1e-3);
```

Use the tuner noise function to obtain a set of initial sensor noises used in the filter.

```
measNoise = tunernoise('ahrs10filter')
measNoise = struct with fields:
    MagnetometerNoise: 1
```

AltimeterNoise: 1

Tune the filter and obtain the tuned parameters.

```
tunedNoise = tune(filter, measNoise, sensorData, ...
    groundTruth, cfg);
```

| Iteration | Parameter | Metric |
| :---: | :---: | :---: |
| 1 | AccelerometerNoise | $\overline{0.0526}$ |
| 1 | GyroscopeNoise | 0.0526 |
| 1 | MagnetometerNoise | 0.0523 |
| 1 | AltimeterNoise | 0.0515 |
| 1 | AccelerometerBiasNoise | 0.0510 |
| 1 | GyroscopeBiasNoise | 0.0510 |
| 1 | GeomagneticVectorNoise | 0.0510 |
| 1 | MagnetometerBiasNoise | 0.0508 |
| 2 | AccelerometerNoise | 0.0508 |
| 2 | GyroscopeNoise | 0.0508 |
| 2 | MagnetometerNoise | 0.0504 |
| 2 | AltimeterNoise | 0.0494 |
| 2 | AccelerometerBiasNoise | 0.0490 |
| 2 | GyroscopeBiasNoise | 0.0490 |
| 2 | GeomagneticVectorNoise | 0.0490 |
| 2 | MagnetometerBiasNoise | 0.0487 |
| 3 | AccelerometerNoise | 0.0487 |
| 3 | GyroscopeNoise | 0.0487 |
| 3 | MagnetometerNoise | 0.0482 |
| 3 | AltimeterNoise | 0.0472 |
| 3 | AccelerometerBiasNoise | 0.0467 |
| 3 | GyroscopeBiasNoise | 0.0467 |
| 3 | GeomagneticVectorNoise | 0.0467 |
| 3 | MagnetometerBiasNoise | 0.0463 |
| 4 | AccelerometerNoise | 0.0463 |
| 4 | GyroscopeNoise | 0.0463 |
| 4 | MagnetometerNoise | 0.0456 |
| 4 | AltimeterNoise | 0.0446 |
| 4 | AccelerometerBiasNoise | 0.0442 |
| 4 | GyroscopeBiasNoise | 0.0442 |
| 4 | GeomagneticVectorNoise | 0.0442 |
| 4 | MagnetometerBiasNoise | 0.0437 |
| 5 | AccelerometerNoise | 0.0437 |
| 5 | GyroscopeNoise | 0.0437 |
| 5 | MagnetometerNoise | 0.0428 |
| 5 | AltimeterNoise | 0.0417 |
| 5 | AccelerometerBiasNoise | 0.0413 |
| 5 | GyroscopeBiasNoise | 0.0413 |
| 5 | GeomagneticVectorNoise | 0.0413 |
| 5 | MagnetometerBiasNoise | 0.0408 |
| 6 | AccelerometerNoise | 0.0408 |
| 6 | GyroscopeNoise | 0.0408 |
| 6 | MagnetometerNoise | 0.0397 |
| 6 | AltimeterNoise | 0.0385 |
| 6 | AccelerometerBiasNoise | 0.0381 |
| 6 | GyroscopeBiasNoise | 0.0381 |
| 6 | GeomagneticVectorNoise | 0.0381 |
| 6 | MagnetometerBiasNoise | 0.0375 |


| 7 | AccelerometerNoise | 0.0375 |
| :--- | :--- | :--- |
| 7 | GyroscopeNoise | 0.0375 |
| 7 | MagnetometerNoise | 0.0363 |
| 7 | AltimeterNoise | 0.0351 |
| 7 | AccelerometerBiasNoise | 0.0347 |
| 7 | GyroscopeBiasNoise | 0.0347 |
| 7 | GeomagneticVectorNoise | 0.0347 |
| 7 | MagnetometerBiasNoise | 0.0342 |
| 8 | AccelerometerNoise | 0.0342 |
| 8 | GyroscopeNoise | 0.0342 |
| 8 | MagnetometerNoise | 0.0331 |
| 8 | AltimeterNoise | 0.0319 |
| 8 | AccelerometerBiasNoise | 0.0316 |
| 8 | GyroscopeBiasNoise | 0.0316 |
| 8 | GeomagneticVectorNoise | 0.0316 |
| 8 | MagnetometerBiasNoise | 0.0313 |
| 9 | AccelerometerNoise | 0.0313 |
| 9 | GyroscopeNoise | 0.0313 |
| 9 | MagnetometerNoise | 0.0313 |
| 9 | AltimeterNoise | 0.0301 |
| 9 | AccelerometerBiasNoise | 0.0298 |
| 9 | GyroscopeBiasNoise | 0.0298 |
| 9 | GeomagneticVectorNoise | 0.0298 |
| 9 | MagnetometerBiasNoise | 0.0296 |
| 10 | AccelerometerNoise | 0.0296 |
| 10 | GyroscopeNoise | 0.0296 |
| 10 | MagnetometerNoise | 0.0296 |
| 10 | AltimeterNoise | 0.0285 |
| 10 | AccelerometerBiasNoise | 0.0283 |
| 10 | GyroscopeBiasNoise | 0.0283 |
| 10 | GeomagneticVectorNoise | 0.0283 |
| 10 | MagnetometerBiasNoise | 0.0282 |

Fuse the sensor data using the tuned filter.

```
N = size(sensorData,1);
qEstTuned = quaternion.zeros(N,1);
altEstTuned = zeros(N,1);
for ii=1:N
    predict(filter,Accelerometer(ii,:),Gyroscope(ii,:));
    if all(~isnan(Magnetometer(ii,1)))
        fusemag(filter, Magnetometer(ii,:),tunedNoise.MagnetometerNoise);
    end
    if ~isnan(Altimeter(ii))
        fusealtimeter(filter, Altimeter(ii),tunedNoise.AltimeterNoise);
    end
    [altEstTuned(ii), qEstTuned(ii)] = pose(filter);
end
```

Compute the RMS errors.
orientationErrorTuned = rad2deg(dist(qEstTuned, Orientation));
rmsOrientationErrorTuned $=$ sqrt(mean(orientationErrorTuned.^2))
rmsOrientationErrorTuned $=2.2899$
positionErrorTuned = altEstTuned - Altitude;
rmsPositionErrorTuned $=$ sqrt(mean( positionErrorTuned.^2))
rmsPositionErrorTuned $=0.0199$
Visualize the results.
figure;
t = (0:N-1)./ filter.IMUSampleRate;
subplot $(2,1,1)$
plot(t, positionErrorTuned, 'b');

```
title("Tuned ahrsl0filter" + newline + ...
```

"Altitude Error")
xlabel('Time (s)');
ylabel('Position Error (meters)')
subplot(2,1,2)
plot(t, orientationErrorTuned, 'b');
title("Orientation Error")
xlabel('Time (s)');
ylabel('Orientation Error (degrees)');


## Input Arguments

## filter - Filter object

ahrs10filter object
Filter object, specified as an ahrs10filter object.

## measureNoise - Measurement noise

## structure

Measurement noise, specified as a structure. The function uses the measurement noise input as the initial guess for tuning the measurement noise. The structure must contain these fields:

| Field name | Description |
| :--- | :--- |
| MagnetometerNoise | Variance of magnetometer noise, specified as a <br> scalar in $(\mu \mathrm{T})^{2}$ |
| AltimeterNoise | Variance of altimeter noise, specified as a scalar <br> $\mathrm{in}^{2}$ |

## sensorData - Sensor data

## table

Sensor data, specified as a table. In each row, the sensor data is specified as:

- Accelerometer - Accelerometer data, specified as a 1-by-3 vector of scalars in $\mathrm{m}^{2} / \mathrm{s}$.
- Gyroscope- Gyroscope data, specified as a 1-by-3 vector of scalars in rad/s.
- Magnetometer - Magnetometer data, specified as a 1-by-3 vector of scalars in $\mu \mathrm{T}$.
- Altimeter - Altimeter data, specified as a scalar in meters.

If the magnetometer does not produce measurements, specify the corresponding entry as NaN . If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the sensorData input based on your choice.

## groundTruth - Ground truth data

table
Ground truth data, specified as a table. In each row, the table can optionally contain any of these variables:

- Orientation - Orientation from the navigation frame to the body frame, specified as a quaternion or a 3-by-3 rotation matrix.
- Altitude - Altitude, specified as a scalar in meters.
- VertialVelocity - Velocity in the vertical direction, specified as a scalar in m/s.
- DeltaAngleBias - Delta angle bias, specified as a 1-by-3 vector of scalars in radians.
- DeltaVelocityBias - Delta velocity bias, specified as a 1-by-3 vector of scalars in m/s.
- GeomagneticFieldVector - Geomagnetic field vector in navigation frame, specified as a 1-by-3 vector of scalars.
- MagnetometerBias - Magnetometer bias in body frame, specified as a 1-by-3 vector of scalars in $\mu \mathrm{T}$.

The function processes each row of the sensorData and groundTruth tables sequentially to calculate the state estimate and RMS error from the ground truth. State variables not present in groundTruth input are ignored for the comparison. The sensorData and the groundTruth tables must have the same number of rows.

If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the groundTruth input based on your choice.

## config - Tuner configuration

tunerconfig object
Tuner configuration, specified as a tunerconfig object.

## Output Arguments

## tunedMeasureNoise - Tuned measurement noise

structure
Tuned measurement noise, returned as a structure. The structure contains these fields.

| Field name | Description |
| :--- | :--- |
| MagnetometerNoise | Variance of magnetometer noise, specified as a <br> scalar in $(\mu \mathrm{T})^{2}$ |
| AltimeterNoise | Variance of altimeter noise, specified as a scalar <br> ${\text { in } \mathrm{m}^{2}}$ |

## References

[1] Abbeel, P., Coates, A., Montemerlo, M., Ng, A.Y. and Thrun, S. Discriminative Training of Kalman Filters. In Robotics: Science and systems, Vol. 2, pp. 1, 2005.

See Also<br>tunerconfig|tunernoise<br>Introduced in R2021a

## ahrsfilter

Orientation from accelerometer, gyroscope, and magnetometer readings

## Description

The ahrsfilter System object ${ }^{\text {TM }}$ fuses accelerometer, magnetometer, and gyroscope sensor data to estimate device orientation.

To estimate device orientation:
1 Create the ahrsfilter object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

FUSE = ahrsfilter
FUSE = ahrsfilter('ReferenceFrame',RF)
FUSE = ahrsfilter( __, Name,Value)
Description
FUSE $=$ ahrsfilter returns an indirect Kalman filter System object, FUSE, for sensor fusion of accelerometer, gyroscope, and magnetometer data to estimate device orientation and angular velocity. The filter uses a 12 -element state vector to track the estimation error for the orientation, the gyroscope bias, the linear acceleration, and the magnetic disturbance.

FUSE = ahrsfilter('ReferenceFrame',RF) returns an ahrsfilter System object that fuses accelerometer, gyroscope, and magnetometer data to estimate device orientation relative to the reference frame RF. Specify RF as 'NED' (North-East-Down) or 'ENU' (East-North-Up). The default value is 'NED'.

FUSE = ahrsfilter( __ , Name, Value) sets each property Name to the specified Value. Unspecified properties have default values.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## SampleRate - Input sample rate of sensor data (Hz)

100 (default) | positive scalar
Input sample rate of the sensor data in Hz , specified as a positive scalar.
Tunable: No
Data Types: single | double

## DecimationFactor - Decimation factor

1 (default) | positive integer
Decimation factor by which to reduce the input sensor data rate as part of the fusion algorithm, specified as a positive integer.

The number of rows of the inputs -- accelReadings, gyroReadings, and magReadings -- must be a multiple of the decimation factor.

Data Types: single | double
AccelerometerNoise - Variance of accelerometer signal noise ((m/s $\left.\mathbf{s}^{\mathbf{2}} \mathbf{2}^{\mathbf{2}}\right)$
0.00019247 (default) | positive real scalar

Variance of accelerometer signal noise in $\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}$, specified as a positive real scalar.
Tunable: Yes
Data Types: single | double
MagnetometerNoise - Variance of magnetometer signal noise ( $\boldsymbol{\mu} \mathbf{T}^{\mathbf{2}}$ )
0.1 (default) | positive real scalar

Variance of magnetometer signal noise in $\mu \mathrm{T}^{2}$, specified as a positive real scalar.
Tunable: Yes
Data Types: single | double
GyroscopeNoise - Variance of gyroscope signal noise ((rad/s) ${ }^{\mathbf{2}}$ )
9.1385e-5 (default) | positive real scalar

Variance of gyroscope signal noise in (rad/s) ${ }^{2}$, specified as a positive real scalar.
Tunable: Yes
Data Types: single | double
GyroscopeDriftNoise - Variance of gyroscope offset drift ((rad/s) ${ }^{\mathbf{2}}$ )
3.0462e-13 (default) | positive real scalar

Variance of gyroscope offset drift in (rad/s) ${ }^{2}$, specified as a positive real scalar.
Tunable: Yes
Data Types: single | double
LinearAccelerationNoise - Variance of linear acceleration noise (m/s $\mathbf{s}^{\mathbf{2}}$
0.0096236 (default) | positive real scalar

Variance of linear acceleration noise in $\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}$, specified as a positive real scalar. Linear acceleration is modeled as a lowpass-filtered white noise process.

Tunable: Yes
Data Types: single | double

## LinearAccelerationDecayFactor - Decay factor for linear acceleration drift

0.5 (default) | scalar in the range [0,1)

Decay factor for linear acceleration drift, specified as a scalar in the range [0,1). If linear acceleration is changing quickly, set LinearAcclerationDecayFactor to a lower value. If linear acceleration changes slowly, set LinearAcclerationDecayFactor to a higher value. Linear acceleration drift is modeled as a lowpass-filtered white noise process.

Tunable: Yes
Data Types: single | double

## MagneticDisturbanceNoise - Variance of magnetic disturbance noise ( $\mu \mathrm{T}^{\mathbf{2}}$ )

0.5 (default) | real finite positive scalar

Variance of magnetic disturbance noise in $\mu \mathrm{T}^{2}$, specified as a real finite positive scalar.
Tunable: Yes
Data Types: single | double
MagneticDisturbanceDecayFactor - Decay factor for magnetic disturbance
0.5 (default) | positive scalar in the range [0,1]

Decay factor for magnetic disturbance, specified as a positive scalar in the range [0,1]. Magnetic disturbance is modeled as a first order Markov process.

Tunable: Yes
Data Types: single | double
InitialProcessNoise - Covariance matrix for process noise
12-by-12 matrix
Covariance matrix for process noise, specified as a 12-by-12 matrix. The default is:

| Columns 1 through 6 |  |  |  |
| ---: | ---: | ---: | ---: |
| 0.000006092348396 | 0 | 0 | 0 |
| 0 | 0.000006092348396 | 0 | 0 |
| 0 | 0 | 0.000006092348396 | 0 |
| 0 | 0 | 0 | 0.000076154354947 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
|  | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |

Columns 7 through 12

| 0 | 0 | 0 | 0 |
| ---: | ---: | ---: | ---: |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0.00962361000000 | 0 | 0 | 0 |
| 0 | 0.009623610000000 | 0 | 0 |
| 0 | 0 | 0.009623610000000 | 0 |
| 0 | 0 | 0 | 0.600000000000000 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |

The initial process covariance matrix accounts for the error in the process model.
Data Types: single | double

## ExpectedMagneticFieldStrength - Expected estimate of magnetic field strength ( $\mu \mathbf{T}$ )

50 (default) | real positive scalar
Expected estimate of magnetic field strength in $\mu \mathrm{T}$, specified as a real positive scalar. The expected magnetic field strength is an estimate of the magnetic field strength of the Earth at the current location.

Tunable: Yes
Data Types: single|double
OrientationFormat - Output orientation format
'quaternion' (default)|'Rotation matrix'
Output orientation format, specified as 'quaternion' or 'Rotation matrix'. The size of the output depends on the input size, $N$, and the output orientation format:

- 'quaternion' -- Output is an $N$-by-1 quaternion.
- 'Rotation matrix' -- Output is a 3-by-3-by-N rotation matrix.

Data Types: char|string

## Usage

## Syntax

[orientation,angularVelocity] = FUSE(accelReadings,gyroReadings,magReadings)

## Description

[orientation, angularVelocity] = FUSE(accelReadings, gyroReadings,magReadings)
fuses accelerometer, gyroscope, and magnetometer data to compute orientation and angular velocity measurements. The algorithm assumes that the device is stationary before the first call.

## Input Arguments

## accelReadings - Accelerometer readings in sensor body coordinate system (m/s $\mathbf{s}^{\mathbf{2}}$ )

$N$-by-3 matrix
Accelerometer readings in the sensor body coordinate system in $\mathrm{m} / \mathrm{s}^{2}$, specified as an N -by- 3 matrix. $N$ is the number of samples, and the three columns of accelReadings represent the [xyz] measurements. Accelerometer readings are assumed to correspond to the sample rate specified by the SampleRate property.

## Data Types: single | double

## gyroReadings - Gyroscope readings in sensor body coordinate system (rad/s) <br> $N$-by-3 matrix

Gyroscope readings in the sensor body coordinate system in rad/s, specified as an $N$-by- 3 matrix. $N$ is the number of samples, and the three columns of gyroReadings represent the $[x y z]$ measurements. Gyroscope readings are assumed to correspond to the sample rate specified by the SampleRate property.

## Data Types: single | double

## magReadings - Magnetometer readings in sensor body coordinate system ( $\mu \mathrm{T}$ )

$N$-by-3 matrix
Magnetometer readings in the sensor body coordinate system in $\mu \mathrm{T}$, specified as an $N$-by- 3 matrix. $N$ is the number of samples, and the three columns of magReadings represent the $[x y z]$ measurements. Magnetometer readings are assumed to correspond to the sample rate specified by the SampleRate property.

## Data Types: single |double

## Output Arguments

orientation - Orientation that rotates quantities from local navigation coordinate system to sensor body coordinate system
M-by-1 array of quaternions (default) | 3-by-3-by-M array
Orientation that can rotate quantities from the local navigation coordinate system to a body coordinate system, returned as quaternions or an array. The size and type of orientation depends on whether the OrienationFormat property is set to 'quaternion' or 'Rotation matrix':

- 'quaternion' -- the output is an $M$-by-1 vector of quaternions, with the same underlying data type as the inputs
- 'Rotation matrix' -- the output is a 3-by-3-by-M array of rotation matrices the same data type as the inputs

The number of input samples, $N$, and the DecimationFactor property determine $M$.
You can use orientation in a rotateframe function to rotate quantities from a local navigation system to a sensor body coordinate system.
Data Types: quaternion | single | double

## angularVelocity - Angular velocity in sensor body coordinate system (rad/s) <br> $M$-by-3 array (default)

Angular velocity with gyroscope bias removed in the sensor body coordinate system in rad/s, returned as an $M$-by- 3 array. The number of input samples, $N$, and the DecimationFactor property determine $M$.

## Data Types: single | double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to ahrsfilter

tune Tune ahrsfilter parameters to reduce estimation error

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Estimate Orientation Using ahrsfilter

Load the rpy_9axis file, which contains recorded accelerometer, gyroscope, and magnetometer sensor data from a device oscillating in pitch (around $y$-axis), then yaw (around $z$-axis), and then roll (around $x$-axis). The file also contains the sample rate of the recording.

```
load 'rpy 9axis' sensorData Fs
accelerometerReadings = sensorData.Acceleration;
gyroscopeReadings = sensorData.AngularVelocity;
magnetometerReadings = sensorData.MagneticField;
```

Create an ahrsfilter System object ${ }^{T M}$ with SampleRate set to the sample rate of the sensor data. Specify a decimation factor of two to reduce the computational cost of the algorithm.

```
decim = 2;
fuse = ahrsfilter('SampleRate',Fs,'DecimationFactor',decim);
```

Pass the accelerometer readings, gyroscope readings, and magnetometer readings to the ahrsfilter object, fuse, to output an estimate of the sensor body orientation over time. By default, the orientation is output as a vector of quaternions.

```
q = fuse(accelerometerReadings,gyroscopeReadings,magnetometerReadings);
```

Orientation is defined by angular displacement required to rotate a parent coordinate system to a child coordinate system. Plot the orientation in Euler angles in degrees over time.
ahrsfilter correctly estimates the change in orientation over time, including the south-facing initial orientation.

```
time = (0:decim:size(accelerometerReadings,1)-1)/Fs;
plot(time,eulerd(q,'ZYX','frame'))
title('Orientation Estimate')
legend('z-axis', 'y-axis', 'x-axis')
ylabel('Rotation (degrees)')
```

Orientation Estimate


## Simulate Magnetic Jamming on ahrsFilter

This example shows how performance of the ahrsfilter System object ${ }^{T M}$ is affected by magnetic jamming.

Load StationaryIMUReadings, which contains accelerometer, magnetometer, and gyroscope readings from a stationary IMU.
load 'StationaryIMUReadings.mat' accelReadings magReadings gyroReadings SampleRate numSamples = size(accelReadings,1);

The ahrsfilter uses magnetic field strength to stabilize its orientation against the assumed constant magnetic field of the Earth. However, there are many natural and man-made objects which output magnetic fields and can confuse the algorithm. To account for the presence of transient magnetic fields, you can set the MagneticDisturbanceNoise property on the ahrsfilter object.

Create an ahrsfilter object with the decimation factor set to 2 and note the default expected magnetic field strength.

```
decim = 2;
FUSE = ahrsfilter('SampleRate',SampleRate,'DecimationFactor',decim);
```

Fuse the IMU readings using the attitude and heading reference system (AHRS) filter, and then visualize the orientation of the sensor body over time. The orientation fluctuates at the beginning and stabilizes after approximately 60 seconds.

```
orientation = FUSE(accelReadings,gyroReadings,magReadings);
orientationEulerAngles = eulerd(orientation,'ZYX','frame');
time = (0:decim:(numSamples-1))'/SampleRate;
figure(1)
plot(time,orientationEulerAngles(:,1), ...
    time,orientationEulerAngles(:,2), ...
    time,orientationEulerAngles(:,3))
xlabel('Time (s)')
ylabel('Rotation (degrees)')
legend('z-axis','y-axis','x-axis')
title('Filtered IMU Data')
```

Filtered IMU Data


Mimic magnetic jamming by adding a transient, strong magnetic field to the magnetic field recorded in the magReadings. Visualize the magnetic field jamming.

```
jamStrength = [10,5,2];
startStop = (50*SampleRate):(150*SampleRate);
jam = zeros(size(magReadings));
jam(startStop,:) = jamStrength.*ones(numel(startStop),3);
magReadings = magReadings + jam;
figure(2)
plot(time,magReadings(1:decim:end,:))
xlabel('Time (s)')
ylabel('Magnetic Field Strength (\mu T)')
title('Simulated Magnetic Field with Jamming')
legend('z-axis','y-axis','x-axis')
```



Run the simulation again using the magReadings with magnetic jamming. Plot the results and note the decreased performance in orientation estimation.

```
reset(FUSE)
orientation = FUSE(accelReadings,gyroReadings,magReadings);
orientationEulerAngles = eulerd(orientation,'ZYX','frame');
figure(3)
plot(time,orientationEulerAngles(:,1), ...
    time,orientationEulerAngles(:,2), ...
    time,orientationEulerAngles(:,3))
xlabel('Time (s)')
ylabel('Rotation (degrees)')
```

```
legend('z-axis','y-axis','x-axis')
title('Filtered IMU Data with Magnetic Disturbance and Default Properties')
```



The magnetic jamming was misinterpreted by the AHRS filter, and the sensor body orientation was incorrectly estimated. You can compensate for jamming by increasing the MagneticDisturbanceNoise property. Increasing the MagneticDisturbanceNoise property increase the assumed noise range for magnetic disturbance, and the entire magnetometer signal is weighted less in the underlying fusion algorithm of ahrsfilter.

Set the MagneticDisturbanceNoise to 200 and run the simulation again.
The orientation estimation output from ahrsfilter is more accurate and less affected by the magnetic transient. However, because the magnetometer signal is weighted less in the underlying fusion algorithm, the algorithm may take more time to restabilize.

```
reset(FUSE)
FUSE.MagneticDisturbanceNoise = 20;
orientation = FUSE(accelReadings,gyroReadings,magReadings);
orientationEulerAngles = eulerd(orientation,'ZYX','frame');
figure(4)
plot(time,orientationEulerAngles(:,1), ...
    time,orientationEulerAngles(:,2), ...
    time,orientationEulerAngles(:,3))
xlabel('Time (s)')
```

```
ylabel('Rotation (degrees)')
legend('z-axis','y-axis','x-axis')
title('Filtered IMU Data with Magnetic Disturbance and Modified Properties')
```

Filtered IMU Data with Magnetic Disturbance and Modified Properties


## Track Shaking 9-Axis IMU

This example uses the ahrsfilter System object ${ }^{\text {TM }}$ to fuse 9-axis IMU data from a sensor body that is shaken. Plot the quaternion distance between the object and its final resting position to visualize performance and how quickly the filter converges to the correct resting position. Then tune parameters of the ahrsfilter so that the filter converges more quickly to the ground-truth resting position.

Load IMUReadingsShaken into your current workspace. This data was recorded from an IMU that was shaken then laid in a resting position. Visualize the acceleration, magnetic field, and angular velocity as recorded by the sensors.

```
load 'IMUReadingsShaken' accelReadings gyroReadings magReadings SampleRate
numSamples = size(accelReadings,1);
time = (0:(numSamples-1))'/SampleRate;
figure(1)
subplot(3,1,1)
plot(time,accelReadings)
title('Accelerometer Reading')
ylabel('Acceleration (m/s^2)')
```

```
subplot(3,1,2)
plot(time,magReadings)
title('Magnetometer Reading')
ylabel('Magnetic Field (\muT)')
subplot(3,1,3)
plot(time,gyroReadings)
title('Gyroscope Reading')
ylabel('Angular Velocity (rad/s)')
xlabel('Time (s)')
```





Create an ahrsfilter and then fuse the IMU data to determine orientation. The orientation is returned as a vector of quaternions; convert the quaternions to Euler angles in degrees. Visualize the orientation of the sensor body over time by plotting the Euler angles required, at each time step, to rotate the global coordinate system to the sensor body coordinate system.

```
fuse = ahrsfilter('SampleRate',SampleRate);
orientation = fuse(accelReadings,gyroReadings,magReadings);
orientationEulerAngles = eulerd(orientation,'ZYX','frame');
figure(2)
plot(time,orientationEulerAngles(:,1), ...
    time,orientationEulerAngles(:,2), ...
    time,orientationEulerAngles(:,3))
xlabel('Time (s)')
```

```
ylabel('Rotation (degrees)')
title('Orientation over Time')
legend('Rotation around z-axis', ...
    'Rotation around y-axis', ...
    'Rotation around x-axis')
```



In the IMU recording, the shaking stops after approximately six seconds. Determine the resting orientation so that you can characterize how fast the ahrsfilter converges.

To determine the resting orientation, calculate the averages of the magnetic field and acceleration for the final four seconds and then use the ecompass function to fuse the data.

Visualize the quaternion distance from the resting position over time.

```
restingOrientation = ecompass(mean(accelReadings(6*SampleRate:end,:)), ...
    mean(magReadings(6*SampleRate:end,:)));
figure(3)
plot(time,rad2deg(dist(resting0rientation,orientation)))
hold on
xlabel('Time (s)')
ylabel('Quaternion Distance (degrees)')
```



Modify the default ahrsfilter properties so that the filter converges to gravity more quickly. Increase the GyroscopeDriftNoise to le-2 and decrease the LinearAccelerationNoise to le-4. This instructs the ahrsfilter algorithm to weigh gyroscope data less and accelerometer data more. Because the accelerometer data provides the stabilizing and consistent gravity vector, the resulting orientation converges more quickly.

Reset the filter, fuse the data, and plot the results.

```
fuse.LinearAccelerationNoise = 1e-4;
fuse.GyroscopeDriftNoise = 1e-2;
reset(fuse)
orientation = fuse(accelReadings,gyroReadings,magReadings);
figure(3)
plot(time,rad2deg(dist(resting0rientation,orientation)))
legend('Default AHRS Filter','Tuned AHRS Filter')
```



## Algorithms

Note: The following algorithm only applies to an NED reference frame.
The ahrsfilter uses the nine-axis Kalman filter structure described in [1]. The algorithm attempts to track the errors in orientation, gyroscope offset, linear acceleration, and magnetic disturbance to output the final orientation and angular velocity. Instead of tracking the orientation directly, the indirect Kalman filter models the error process, $x$, with a recursive update:

$$
x_{k}=\left[\begin{array}{l}
\theta_{k} \\
b_{k} \\
a_{k} \\
d_{k}
\end{array}\right]=F_{k}\left[\begin{array}{c}
\theta_{k-1} \\
b_{k-1} \\
a_{k-1} \\
d_{k}-1
\end{array}\right]+w_{k}
$$

where $x_{\mathrm{k}}$ is a 12 -by- 1 vector consisting of:

- $\theta_{k}--3$-by-1 orientation error vector, in degrees, at time $k$
- $b_{k}$-- 3-by-1 gyroscope zero angular rate bias vector, in deg/s, at time $k$
- $a_{k}--3$-by-1 acceleration error vector measured in the sensor frame, in $g$, at time $k$
- $d_{k}--3$-by-1 magnetic disturbance error vector measured in the sensor frame, in $\mu \mathrm{T}$, at time $k$ and where $w_{\mathrm{k}}$ is a 12 -by- 1 additive noise vector, and $F_{\mathrm{k}}$ is the state transition model.

Because $\chi_{\mathrm{k}}$ is defined as the error process, the a priori estimate is always zero, and therefore the state transition model, $F_{k}$, is zero. This insight results in the following reduction of the standard Kalman equations:

Standard Kalman equations:

$$
\begin{aligned}
& x_{k}^{-}=F_{k} x_{k-1}^{+} \\
& P_{k}^{-}=F_{k} P_{k-1}^{+} F_{k}^{T}+Q_{k} \\
& y_{k}=z_{k}-H_{k} x_{\bar{k}}^{-} \\
& S_{k}=R_{k}+H_{k} P_{k}^{-} H_{k} T \\
& K_{k}=P_{k}^{-} H_{k}^{T}\left(S_{k}\right)^{-1} \\
& x_{k}^{+}=x_{k}^{-}+K_{k} y_{k} \\
& P_{k}^{+}=P_{k}^{-}-K_{k} H_{k} P_{k}^{-}
\end{aligned}
$$

Kalman equations used in this algorithm:

$$
\begin{aligned}
& x_{k}^{-}=0 \\
& P_{k}^{-}=Q_{k} \\
& y_{k}=z_{k} \\
& S_{k}=R_{k}+H_{k} P_{k}^{-} H_{k} T \\
& K_{k}=P_{k}^{-} H_{k}^{T}\left(S_{k}\right)^{-1} \\
& x_{k}^{+}=K_{k} y_{k} \\
& P_{k}^{+}=P_{k}^{--} K_{k} H_{k} P_{k}^{-}
\end{aligned}
$$

where:

- $x_{k}{ }^{-}$-- predicted (a priori) state estimate; the error process
- $P_{k}{ }^{-}$-- predicted (a priori) estimate covariance
- $y_{k}$-- innovation
- $S_{k}$-- innovation covariance
- $K_{k}-$ Kalman gain
- $x_{k}{ }^{+}$-- updated (a posteriori) state estimate
- $P_{k}{ }^{+}$-- updated (a posteriori) estimate covariance
$k$ represents the iteration, the superscript ${ }^{+}$represents an a posteriori estimate, and the superscript ${ }^{-}$ represents an a priori estimate.

The graphic and following steps describe a single frame-based iteration through the algorithm.


Before the first iteration, the accelReadings, gyroReadings, and magReadings inputs are chunked into DecimationFactor-by-3 frames. For each chunk, the algorithm uses the most current accelerometer and magnetometer readings corresponding to the chunk of gyroscope readings.

## Detailed Overview

Walk through the algorithm for an explanation of each stage of the detailed overview.


## Model

The algorithm models acceleration and angular change as linear processes.


## Predict Orientation

The orientation for the current frame is predicted by first estimating the angular change from the previous frame:

$$
\Delta \varphi_{N \times 3}=\frac{\left(\text { gyroReadings }_{N \times 3}-\text { gyroOffset }_{1 \times 3}\right)}{f s}
$$

where $N$ is the decimation factor specified by the DecimationFactor property and $f s$ is the sample rate specified by the SampleRate property.

The angular change is converted into quaternions using the rotvec quaternion construction syntax:

$$
\Delta Q_{N \times 1}=\text { quaternion }\left(\Delta \varphi_{N \times 3}, \text { 'rotvec' }^{\prime}\right)
$$

The previous orientation estimate is updated by rotating it by $\Delta Q$ :

$$
q_{1 \times 1}^{-}=\left(q_{1}^{+} \times 1\right)\left(\prod_{n=1}^{N} \Delta Q_{n}\right)
$$

During the first iteration, the orientation estimate, $q^{-}$, is initialized by ecompass.

## Estimate Gravity from Orientation

The gravity vector is interpreted as the third column of the quaternion, $q^{-}$, in rotation matrix form:

$$
g_{1 \times 3}=(r \operatorname{Prior}(:, 3))^{T}
$$

See [1] for an explanation of why the third column of rPrior can be interpreted as the gravity vector.

## Estimate Gravity from Acceleration

A second gravity vector estimation is made by subtracting the decayed linear acceleration estimate of the previous iteration from the accelerometer readings:

$$
\text { gAccel }_{1 \times 3}=\text { accelReadings }_{1 \times 3}-\text { linAccelprior }_{1 \times 3}
$$

## Estimate Earth's Magnetic Vector

Earth's magnetic vector is estimated by rotating the magnetic vector estimate from the previous iteration by the a priori orientation estimate, in rotation matrix form:

$$
m \text { Gyro }_{1 \times 3}=\left((r \text { Prior })\left(m^{T}\right)\right)^{T}
$$

## Error Model



The error model combines two differences:

- The difference between the gravity estimate from the accelerometer readings and the gravity estimate from the gyroscope readings: $z_{g}=g-g A c c e l$
- The difference between the magnetic vector estimate from the gyroscope readings and the magnetic vector estimate from the magnetometer: $z_{m}=m G y r o-m a g R e a d i n g s$


## Magnetometer Correct

The magnetometer correct estimates the error in the magnetic vector estimate and detects magnetic jamming.


## Magnetometer Disturbance Error

The magnetic disturbance error is calculated by matrix multiplication of the Kalman gain associated with the magnetic vector with the error signal:

$$
\text { merror }_{3 \times 1}=\left(\left(K(10: 12,:)_{3 \times 6}\right)\left(z_{1 \times 6}\right)^{T}\right)^{T}
$$

The Kalman gain, $K$, is the Kalman gain calculated in the current iteration.

## Magnetic Jamming Detection

Magnetic jamming is determined by verifying that the power of the detected magnetic disturbance is less than or equal to four times the power of the expected magnetic field strength:

$$
t f=\left\{\begin{array}{l}
\text { true if } \\
\text { false else }
\end{array}|m E r r o r|^{2}>(4)(\text { ExpectedMagneticFieldStrength })^{2}\right.
$$

ExpectedMagneticFieldStrength is a property of ahrsfilter.

## Kalman Equations

The Kalman equations use the gravity estimate derived from the gyroscope readings, $g$, the magnetic vector estimate derived from the gyroscope readings, mGyro, and the observation of the error process, $z$, to update the Kalman gain and intermediary covariance matrices. The Kalman gain is applied to the error signal, $z$, to output an a posteriori error estimate, $\chi^{+}$.


## Observation Model

The observation model maps the 1-by-3 observed states, $g$ and mGyro, into the 6-by-12 true state, $H$.
The observation model is constructed as:

$$
H_{3 \times 9}=\left[\begin{array}{cccccccccccc}
0 & g_{z} & -g_{y} & 0 & -\kappa g_{z} & \kappa g_{y} & 1 & 0 & 0 & 0 & 0 & 0 \\
-g_{z} & 0 & g_{x} & \kappa g_{z} & 0 & -\kappa g_{x} & 0 & 1 & 0 & 0 & 0 & 0 \\
g_{y} & -g_{x} & 0 & -\kappa g_{y} & \kappa g_{x} & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\
0 & m_{z} & -m_{y} & 0 & -\kappa m_{z} & -\kappa m_{y} & 0 & 0 & 0 & -1 & 0 & 0 \\
-m_{z} & 0 & m_{x} & \kappa m_{z} & 0 & -\kappa m_{x} & 0 & 0 & 0 & 0 & -1 & 0 \\
m_{y} & -m_{x} & 0 & -\kappa m_{y} & \kappa m_{x} & 0 & 0 & 0 & 0 & 0 & 0 & -1
\end{array}\right]
$$

where $g_{\mathrm{x}}, g_{\mathrm{y}}$, and $g_{\mathrm{z}}$ are the $x$-, $y$-, and $z$-elements of the gravity vector estimated from the a priori orientation, respectively. $m_{x}, m_{y}$, and $m_{z}$ are the $x$-, $y$-, and $z$-elements of the magnetic vector estimated from the a priori orientation, respectively. $\kappa$ is a constant determined by the SampleRate and DecimationFactor properties: $\kappa=$ DecimationFactor/SampleRate.

See sections 7.3 and 7.4 of [1] for a derivation of the observation model.

## Innovation Covariance

The innovation covariance is a 6 -by- 6 matrix used to track the variability in the measurements. The innovation covariance matrix is calculated as:

$$
S_{6 \times 6}=R_{6 \times 6}+\left(H_{6 \times 12}\right)\left(P_{12 \times 12}^{-}\right)\left(H_{6 \times 12}\right)^{T}
$$

where

- $H$ is the observation model matrix
- $P^{-}$is the predicted (a priori) estimate of the covariance of the observation model calculated in the previous iteration
- $R$ is the covariance of the observation model noise, calculated as:

$$
R_{6 \times 6}=\left[\begin{array}{cccccc}
a^{a c c e l} \\
0 & 0 & 0 & 0 & 0 & 0 \\
0 & a c c e l_{\text {noise }} & 0 & 0 & 0 & 0 \\
0 & 0 & a c c e l_{\text {noise }} & 0 & 0 & 0 \\
0 & 0 & 0 & \text { mag }_{\text {noise }} & 0 & 0 \\
0 & 0 & 0 & 0 & \text { mag }_{\text {noise }} & 0 \\
0 & 0 & 0 & 0 & 0 & \text { mag }_{\text {noise }}
\end{array}\right]
$$

where

$$
a^{c c e l_{\text {noise }}}=\text { AccelerometerNoise }+ \text { LinearAccelerationNoise }+\kappa^{2}
$$

(GyroscopeDriftNoise + GyroscopeNoise)
and

$$
\begin{aligned}
& \text { mag }_{\text {noise }}=\text { MagnetometerNoise }+ \text { MagneticDisturbanceNoise }+\kappa^{2} \\
& \text { (GyroscopeDriftNoise }+ \text { GyroscopeNoise })
\end{aligned}
$$

The following properties define the observation model noise variance:

- к -- DecimationFactor/SampleRate
- AccelerometerNoise
- LinearAccelerationNoise
- GyroscopeDriftNoise
- GyroscopeNoise
- MagneticDisturbanceNoise
- MagnetometerNoise


## Update Error Estimate Covariance

The error estimate covariance is a 12-by-12 matrix used to track the variability in the state.
The error estimate covariance matrix is updated as:

$$
P_{12 \times 12}^{+}=P_{12 \times 12}^{-}-\left(K_{12 \times 6}\right)\left(H_{6 \times 12}\right)\left(P_{12 \times 12}^{-}\right)
$$

where $K$ is the Kalman gain, $H$ is the measurement matrix, and $P^{-}$is the error estimate covariance calculated during the previous iteration.

## Predict Error Estimate Covariance

The error estimate covariance is a 12-by-12 matrix used to track the variability in the state. The $a$ priori error estimate covariance, $P^{-}$, is set to the process noise covariance, $Q$, determined during the previous iteration. $Q$ is calculated as a function of the a posteriori error estimate covariance, $P^{+}$. When calculating $Q$, it is assumed that the cross-correlation terms are negligible compared to the autocorrelation terms, and are set to zero:

$$
Q=
$$

$\left[\begin{array}{ccccc}P^{+}(1)+K^{2} P^{+}(40)+\beta+\eta & 0 & 0 & -K\left(P^{+}(40)+\beta\right) & 0 \\ 0 & P^{+}(14)+K^{2} P^{+}(53)+\beta+\eta & 0 & 0 & -K\left(P^{+}(53)+\right. \\ 0 & 0 & P^{+}(27)+K^{2} P^{+}(66)+\beta+\eta & 0 & 0 \\ -K\left(P^{+}(40)+\beta\right) & 0 & 0 & P^{+}(40)+\beta & 0 \\ 0 & -K\left(P^{+}(53)+\beta\right) & 0 & 0 & P^{+}(53)+\beta \\ 0 & 0 & -K\left(P^{+}(66)+\beta\right) & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0\end{array}\right.$
where

- $P^{+}$-- is the updated (a posteriori) error estimate covariance
- $\kappa$-- DecimationFactor/SampleRate
- $\beta$-- GyroscopeDriftNoise
- $\eta$-- GyroscopeNoise
- $\nu$-- LinearAcclerationDecayFactor
- $\xi$-- LinearAccelerationNoise
- $\sigma$-- MagneticDisturbanceDecayFactor
- $\gamma$-- MagneticDisturbanceNoise

See section 10.1 of [1] for a derivation of the terms of the process error matrix.

## Kalman Gain

The Kalman gain matrix is a 12 -by-6 matrix used to weight the innovation. In this algorithm, the innovation is interpreted as the error process, $z$.

The Kalman gain matrix is constructed as:

$$
K_{12 \times 6}=\left(P_{12 \times 12}^{-}\right)\left(H_{6 \times 12}\right)^{T}\left(\left(S_{6 \times 6}\right)^{T}\right)^{-1}
$$

where

- $P^{-}$-- predicted error covariance
- H -- observation model
- $S$-- innovation covariance


## Update a Posteriori Error

The a posterior error estimate is determined by combining the Kalman gain matrix with the error in the gravity vector and magnetic vector estimations:

$$
x_{12 \times 1}=\left(K_{12 \times 6}\right)\left(z_{1 \times 6}\right)^{T}
$$

If magnetic jamming is detected in the current iteration, the magnetic vector error signal is ignored, and the a posterior error estimate is calculated as:

$$
x_{9 \times 1}=\left(K(1: 9,1: 3)\left(z_{g}\right)^{T}\right.
$$

## Correct



## Estimate Orientation

The orientation estimate is updated by multiplying the previous estimation by the error:

$$
q^{+}=\left(q^{-}\right)\left(\theta^{+}\right)
$$

## Estimate Linear Acceleration

The linear acceleration estimation is updated by decaying the linear acceleration estimation from the previous iteration and subtracting the error:

$$
\text { linAccelPrior }=\left(\text { linAccelPrior }_{k-1}\right) \nu-b^{+}
$$

where

- $\quad \nu$-- LinearAcclerationDecayFactor


## Estimate Gyroscope Offset

The gyroscope offset estimation is updated by subtracting the gyroscope offset error from the gyroscope offset from the previous iteration:

$$
\text { gyroOffset }=\text { gyroOffset }_{k-1}-a^{+}
$$

## Compute Angular Velocity

To estimate angular velocity, the frame of gyroReadings are averaged and the gyroscope offset computed in the previous iteration is subtracted:

$$
\text { angularVelocity }_{1 \times 3}=\frac{\sum \text { gyroReadings }_{N \times 3}}{N}-\text { gyroOffset }_{1 \times 3}
$$

where $N$ is the decimation factor specified by the DecimationFactor property.
The gyroscope offset estimation is initialized to zeros for the first iteration.

## Update Magnetic Vector

If magnetic jamming was not detected in the current iteration, the magnetic vector estimate, $m$, is updated using the a posteriori magnetic disturbance error and the a posteriori orientation.

The magnetic disturbance error is converted to the navigation frame:

$$
m E r r o r N E D_{1 \times 3}=\left(\left(\text { rPost }_{3 \times 3}\right)^{T}\left(\text { mError }_{1 \times 3}\right)^{T}\right)^{T}
$$

The magnetic disturbance error in the navigation frame is subtracted from the previous magnetic vector estimate and then interpreted as inclination:

$$
M=m-m E r r o r N E D
$$

$$
\text { inclination }=\operatorname{atan} 2(M(3), M(1))
$$

The inclination is converted to a constrained magnetic vector estimate for the next iteration:

$$
\begin{aligned}
& m(1)=(\text { ExpectedMagneticFieldStrength })(\cos (\text { inclination })) \\
& m(2)=0 \\
& m(3)=(\text { ExpectedMagneticFieldStrength })(\sin (\text { inclination }))
\end{aligned}
$$

ExpectedMagneticFieldStrength is a property of ahrsfilter.

## References

[1] Open Source Sensor Fusion. https://github.com/memsindustrygroup/Open-Source-Sensor-Fusion/ tree/master/docs
[2] Roetenberg, D., H.J. Luinge, C.T.M. Baten, and P.H. Veltink. "Compensation of Magnetic Disturbances Improves Inertial and Magnetic Sensing of Human Body Segment Orientation." IEEE Transactions on Neural Systems and Rehabilitation Engineering. Vol. 13. Issue 3, 2005, pp. 395-405.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

ecompass|imufilter|imuSensor|gpsSensor

## Introduced in R2018b

## tune

Tune ahrsfilter parameters to reduce estimation error

## Syntax

```
tune(filter,sensorData,groundTruth)
tune(
```

$\qquad$

``` , config)
```


## Description

tune(filter, sensorData, groundTruth) adjusts the properties of the ahrsfilter filter object, filter, to reduce the root-mean-squared (RMS) quaternion distance error between the fused sensor data and the ground truth. The function uses the property values in the filter as the initial estimate for the optimization algorithm.
tune ( $\qquad$ , config) specifies the tuning configuration based on a tunerconfig object, config.

## Examples

## Tune ahrsfilter to Improve Orientation Estimate

Load recorded sensor data and ground truth data.

```
ld = load('ahrsfilterTuneData.mat');
qTrue = ld.groundTruth.Orientation; % true orientation
Create an arhsfitler object.
fuse = ahrsfilter;
```

Fuse the sensor data using the default, untuned filter.

```
qEstUntuned = fuse(ld.sensorData.Accelerometer, ...
    ld.sensorData.Gyroscope, ld.sensorData.Magnetometer);
```

Create a tunerconfig object. Tune the ahrsfilter object to improve the orientation estimation based on the configuration.

```
config = tunerconfig('ahrsfilter');
tune(fuse,ld.sensorData,ld.groundTruth,config);
\begin{tabular}{llll} 
Iteration & & Parameter & \\
\cline { 1 - 1 } & & & AccelerometerNoise \\
1 & & GyroscopeNoise & 0.1345 \\
1 & & MagnetometerNoise & 0.1342 \\
1 & GyroscopeDriftNoise & 0.1341 \\
1 & & LinearAccelerationNoise & 0.1341 \\
1 & & MagneticDisturbanceNoise & 0.1332 \\
1 & & LinearAccelerationDecayFactor & 0.1324 \\
1 & & MagneticDisturbanceDecayFactor & 0.1317 \\
& & & 0.1316
\end{tabular}
```

| AccelerometerNoise | 0.1316 |
| :---: | :---: |
| GyroscopeNoise | 0.1312 |
| MagnetometerNoise | 0.1311 |
| GyroscopeDriftNoise | 0.1311 |
| LinearAccelerationNoise | 0.1300 |
| MagneticDisturbanceNoise | 0.1292 |
| LinearAccelerationDecayFactor | 0.1285 |
| MagneticDisturbanceDecayFactor | 0.1285 |
| AccelerometerNoise | 0.1285 |
| GyroscopeNoise | 0.1280 |
| MagnetometerNoise | 0.1279 |
| GyroscopeDriftNoise | 0.1279 |
| LinearAccelerationNoise | 0.1267 |
| MagneticDisturbanceNoise | 0.1258 |
| LinearAccelerationDecayFactor | 0.1253 |
| MagneticDisturbanceDecayFactor | 0.1253 |
| AccelerometerNoise | 0.1252 |
| GyroscopeNoise | 0.1247 |
| MagnetometerNoise | 0.1246 |
| GyroscopeDriftNoise | 0.1246 |
| LinearAccelerationNoise | 0.1233 |
| MagneticDisturbanceNoise | 0.1224 |
| LinearAccelerationDecayFactor | 0.1220 |
| MagneticDisturbanceDecayFactor | 0.1220 |
| AccelerometerNoise | 0.1220 |
| GyroscopeNoise | 0.1213 |
| MagnetometerNoise | 0.1212 |
| GyroscopeDriftNoise | 0.1212 |
| LinearAccelerationNoise | 0.1200 |
| MagneticDisturbanceNoise | 0.1190 |
| LinearAccelerationDecayFactor | 0.1187 |
| MagneticDisturbanceDecayFactor | 0.1187 |
| AccelerometerNoise | 0.1187 |
| GyroscopeNoise | 0.1180 |
| MagnetometerNoise | 0.1178 |
| GyroscopeDriftNoise | 0.1178 |
| LinearAccelerationNoise | 0.1167 |
| MagneticDisturbanceNoise | 0.1156 |
| LinearAccelerationDecayFactor | 0.1155 |
| MagneticDisturbanceDecayFactor | 0.1155 |
| AccelerometerNoise | 0.1155 |
| GyroscopeNoise | 0.1147 |
| MagnetometerNoise | 0.1145 |
| GyroscopeDriftNoise | 0.1145 |
| LinearAccelerationNoise | 0.1137 |
| MagneticDisturbanceNoise | 0.1126 |
| LinearAccelerationDecayFactor | 0.1125 |
| MagneticDisturbanceDecayFactor | 0.1125 |
| AccelerometerNoise | 0.1125 |
| GyroscopeNoise | 0.1117 |
| MagnetometerNoise | 0.1116 |
| GyroscopeDriftNoise | 0.1116 |
| LinearAccelerationNoise | 0.1112 |
| MagneticDisturbanceNoise | 0.1100 |
| LinearAccelerationDecayFactor | 0.1099 |
| MagneticDisturbanceDecayFactor | 0.1099 |
| AccelerometerNoise | 0.1099 |
| GyroscopeNoise | 0.1091 |


| 9 | MagnetometerNoise | 0.1090 |
| :--- | :--- | ---: |
| 9 | GyroscopeDriftNoise | 0.1090 |
| 9 | LinearAccelerationNoise | 0.1090 |
| 9 | MagneticDisturbanceNoise | 0.1076 |
| 9 | LinearAccelerationDecayFactor | 0.1075 |
| 9 | MagneticDisturbanceDecayFactor | 0.1075 |
| 10 | AccelerometerNoise | 0.1075 |
| 10 | GyroscopeNoise | 0.1066 |
| 10 | MagnetometerNoise | 0.1064 |
| 10 | GyroscopeDriftNoise | 0.1064 |
| 10 | LinearAccelerationNoise | 0.1064 |
| 10 | MagneticDisturbanceNoise | 0.1049 |
| 10 | LinearAccelerationDecayFactor | 0.1047 |
| 10 | MagneticDisturbanceDecayFactor | 0.1047 |
| 11 | AccelerometerNoise | 0.1047 |
| 11 | GyroscopeNoise | 0.1038 |
| 11 | GygnetometerNoise | 0.1036 |
| 11 | LinearAccelerationNoise | 0.1036 |
| 11 | MagneticDisturbanceNoise | 0.1036 |
| 11 | LinearAccelerationDecayFactor | 0.1016 |
| 11 | MagneticDisturbanceDecayFactor | 0.1014 |
| 11 | AccelerometerNoise | 0.1014 |
| 12 | GyroscopeNoise | 0.1014 |
| 12 | MagnetometerNoise | 0.1005 |
| 12 | GyroscopeDriftNoise | 0.1002 |
| 12 | LinearAccelerationNoise | 0.1002 |
| 12 | MagneticDisturbanceNoise | 0.1002 |
| 12 |  | 0.0978 |

Fuse the sensor data using the tuned filter.
qEstTuned = fuse(ld.sensorData.Accelerometer, ...
ld.sensorData.Gyroscope, ld.sensorData.Magnetometer);
Compare the tuned and untuned RMS error performances.

```
dUntuned = rad2deg(dist(qEstUntuned, qTrue));
dTuned = rad2deg(dist(qEstTuned, qTrue));
rmsUntuned = sqrt(mean(dUntuned.^2))
rmsUntuned = 7.7088
rmsTuned = sqrt(mean(dTuned.^2))
rmsTuned = 5.6033
```

Visualize the errors with respect to time.

```
N = numel(dUntuned);
t = (0:N-1)./ fuse.SampleRate;
plot(t, dUntuned, 'r', t, dTuned, 'b');
legend('Untuned', 'Tuned');
title('ahrsfilter - Tuned vs Untuned Error')
xlabel('Time (s)');
ylabel('Orientation Error (degrees)');
```



## Input Arguments

filter - Filter object
ahrsfilter object
Filter object, specified as an ahrsfilter object.

## sensorData - Sensor data <br> table

Sensor data, specified as a table. In each row, the sensor data is specified as:

- Accelerometer - Accelerometer data, specified as a 1 -by-3 vector of scalars in $\mathrm{m}^{2} / \mathrm{s}$.
- Gyroscope - Gyroscope data, specified as a 1-by-3 vector of scalars in rad/s.
- Magnetometer - Magnetometer data, specified as a 1-by-3 vector of scalars in $\mu \mathrm{T}$.

If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the sensorData input based on your choice.

## groundTruth - Ground truth data

timetable
Ground truth data, specified as a table. The table has only one column of Orientation data. In each row, the orientation is specified as a quaternion object or a 3-by-3 rotation matrix.

The function processes each row of the sensorData and groundTruth tables sequentially to calculate the state estimate and RMS error from the ground truth. Each row of the sensorData and the groundTruth tables must correspond to each other.

If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the groundTruth input based on your choice.

## config - Tuner configuration

tunerconfig object
Tuner configuration, specified as a tunerconfig object.

## References

[1] Abbeel, P., Coates, A., Montemerlo, M., Ng, A.Y. and Thrun, S. Discriminative Training of Kalman Filters. In Robotics: Science and systems, Vol. 2, pp. 1, 2005.

## See Also

Introduced in R2020b

## altimeterSensor

Altimeter simulation model

## Description

The altimeterSensor System object models receiving data from an altimeter sensor.
To model an altimeter:
1 Create the altimeterSensor object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

altimeter = altimeterSensor
altimeter = altimeterSensor('ReferenceFrame',RF)
altimeter $=$ altimeterSensor $\qquad$ ,Name, Value)

## Description

altimeter = altimeterSensor returns an altimeterSensor System object that simulates altimeter readings.
altimeter = altimeterSensor('ReferenceFrame',RF) returns an altimeterSensor System object that simulates altimeter readings relative to the reference frame RF. Specify RF as 'NED ' (North-East-Down) or 'ENU' (East-North-Up). The default value is 'NED'.
altimeter = altimeterSensor( $\qquad$ ,Name, Value) sets each property Name to the specified Value. Unspecified properties have default values.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## SampleRate - Update rate of sensor (Hz)

1 (default) | positive scalar
Update rate of sensor in Hz , specified as a positive scalar.

Data Types: single | double

## ConstantBias - Constant offset bias (m)

0 (default) | scalar
Constant offset bias in meters, specified as a scalar.
Tunable: Yes
Data Types: single | double

## NoiseDensity - Power spectral density of sensor noise ( $\mathbf{m} / \sqrt{ } \mathrm{Hz}$ )

0 (default) | nonnegative scalar
Power spectral density of sensor noise in $\mathrm{m} / \sqrt{ } \mathrm{Hz}$, specified as a nonnegative scalar.
Tunable: Yes
Data Types: single | double

## BiasInstability - Instability of bias offset (m)

0 (default) | nonnegative scalar
Instability of the bias offset in meters, specified as a nonnegative scalar.
Tunable: Yes
Data Types: single | double

## DecayFactor - Bias instability noise decay factor

0 (default) | scalar in the range [0,1]
Bias instability noise decay factor, specified as a scalar in the range [0,1]. A decay factor of 0 models the bias instability noise as a white noise process. A decay factor of 1 models the bias instability noise as a random walk process.

Tunable: Yes
Data Types: single | double

## RandomStream - Random number source

'Global stream' (default)|'mt19937ar with seed'
Random number source, specified as a character vector or string:

- 'Global stream' -- Random numbers are generated using the current global random number stream.
- 'mt19937ar with seed' -- Random numbers are generated using the mt19937ar algorithm with the seed specified by the Seed property.

Data Types: char \| string

## Seed - Initial seed

67 (default) | nonnegative integer scalar
Initial seed of an mt19937ar random number generator algorithm, specified as a nonnegative integer scalar.

## Dependencies

To enable this property, set RandomStream to 'mt19937ar with seed'.
Data Types: single | double
Usage

## Syntax

altimeterReadings = altimeter(position)

## Description

altimeterReadings = altimeter(position) generates an altimeter sensor altitude reading from the position input.

## Input Arguments

## position - Position of sensor in local navigation coordinate system (m)

$N$-by-3 matrix
Position of sensor in the local navigation coordinate system, specified as an $N$-by-3 matrix with elements measured in meters. $N$ is the number of samples in the current frame.

```
Data Types: single|double
```


## Output Arguments

## altimeterReadings - Altitude of sensor relative to local navigation coordinate system (m)

$N$-element column vector
Altitude of sensor relative to the local navigation coordinate system in meters, returned as an N element column vector. $N$ is the number of samples in the current frame.
Data Types: single|double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:
release(obj)

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Generate Noisy Altimeter Readings from Stationary Input

Create an altimeterSensor System object ${ }^{\text {TM }}$ to model receiving altimeter sensor data. Assume a typical one Hz sample rate and a 10 minute simulation time. Set ConstantBias to 0.01, NoiseDensity to 0.05, BiasInstability to 0.05, and DecayFactor to 0.5.

```
Fs = 1;
```

duration = 60*10;
numSamples = duration*Fs;
altimeter = altimeterSensor('SampleRate',Fs, ...
'ConstantBias',0.01, ...
'NoiseDensity',0.05, ...
'BiasInstability',0.05, ...
'DecayFactor',0.5) ;
truePosition = zeros(numSamples,3);

Call altimeter with the specified truePosition to model noisy altimeter readings from a stationary platform.
altimeterReadings = altimeter(truePosition);
Plot the true position and the altimeter sensor readings for height.

```
t = (0:(numSamples-1))/Fs;
plot(t,altimeterReadings)
hold on
plot(t,truePosition(:,3),'LineWidth',2)
hold off
title('Altimeter Readings')
xlabel('Time (s)')
ylabel('Height (m)')
legend('Altimeter Readings','Ground Truth')
```



## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

gpsSensor|imuSensor
Introduced in R2019a

## complementaryFilter

Orientation estimation from a complementary filter

## Description

The complementaryFilter System object fuses accelerometer, gyroscope, and magnetometer sensor data to estimate device orientation and angular velocity.

To estimate orientation using this object:
1 Create the complementaryFilter object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

FUSE = complementaryFilter
FUSE = complementaryFilter('ReferenceFrame',RF)
FUSE = complementaryFilter( $\qquad$ ,Name, Value)

Description
FUSE = complementaryFilter returns a complementaryFilter System object, FUSE, for sensor fusion of accelerometer, gyroscope, and magnetometer data to estimate device orientation and angular velocity.

FUSE = complementaryFilter('ReferenceFrame',RF) returns a complementaryFilter System object that fuses accelerometer, gyroscope, and magnetometer data to estimate device orientation relative to the reference frame RF. Specify RF as 'NED ' (North-East-Down) or 'ENU' (East-North-Up). The default value is 'NED '.

FUSE = complementaryFilter $\qquad$ ,Name, Value) sets each property Name to the specified Value. Unspecified properties have default values.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## SampleRate - Input sample rate of sensor data (Hz)

## 100 (default) | positive scalar

Input sample rate of the sensor data in Hz , specified as a positive scalar.
Tunable: No
Data Types: single | double

## AccelerometerGain - Accelerometer gain

0.01 (default) | real scar in [0, 1]

Accelerometer gain, specified as a real scalar in the range of [0,1]. The gain determines how much the accelerometer measurement is trusted over the gyroscope measurement for orientation estimation. This property is tunable.
Data Types: single | double

## MagnetometerGain - Magnetometer gain

0.01 (default) | real scar in [0, 1]

Magnetometer gain, specified as a real scalar in the range of $[0,1]$. The gain determines how much the magnetometer measurement is trusted over the gyroscope measurement for orientation estimation. This property is tunable.
Data Types: single | double

## HasMagnetometer - Enable magnetometer input

true (default) | false
Enable magnetometer input, specified as true or false.
Data Types: logical

## OrientationFormat - Output orientation format

'quaternion' (default)|'Rotation matrix'
Output orientation format, specified as 'quaternion' or 'Rotation matrix'. The size of the output depends on the output orientation format:

- 'quaternion' -- Output is an $N$-by-1 quaternion.
- 'Rotation matrix' -- Output is a 3 -by- 3 -by- $N$ rotation matrix.
$N$ is the number of samples.
Data Types: char | string


## Usage

## Syntax

[orientation, angularVelocity] = FUSE(accelReadings,gyroReadings,magReadings) [orientation,angularVelocity] = FUSE(accelReadings,gyroReadings)

## Description

[orientation,angularVelocity] = FUSE(accelReadings,gyroReadings,magReadings) fuses accelerometer, gyroscope, and magnetometer data to compute orientation and angular velocity. To use this syntax, set the HasMagnetometer property as true.
[orientation,angularVelocity] = FUSE(accelReadings,gyroReadings) fuses accelerometer and gyroscope data to compute orientation and angular velocity. To use this syntax, set the HasMagnetometer property as false.

## Input Arguments

## accelReadings - Accelerometer readings in sensor body coordinate system (m/s $\mathbf{s}^{\mathbf{2}}$ )

$N$-by-3 matrix
Accelerometer readings in the sensor body coordinate system in $\mathrm{m} / \mathrm{s}^{2}$, specified as an N -by- 3 matrix. $N$ is the number of samples, and the three columns of accelReadings represent the $[x y z]$ measurements. Accelerometer readings are assumed to correspond to the sample rate specified by the SampleRate property. In the filter, the gravity constant $g$ is assumed to be $9.81 \mathrm{~m} / \mathrm{s}^{2}$.

## Data Types: single | double

## gyroReadings - Gyroscope readings in sensor body coordinate system (rad/s)

$N$-by-3 matrix
Gyroscope readings in the sensor body coordinate system in rad/s, specified as an $N$-by- 3 matrix. $N$ is the number of samples, and the three columns of gyroReadings represent the $[x y z]$ measurements. Gyroscope readings are assumed to correspond to the sample rate specified by the SampleRate property.
Data Types: single | double

## magReadings - Magnetometer readings in sensor body coordinate system ( $\mu \mathrm{T}$ )

$N$-by-3 matrix
Magnetometer readings in the sensor body coordinate system in $\mu \mathrm{T}$, specified as an $N$-by- 3 matrix. $N$ is the number of samples, and the three columns of magReadings represent the [ $x y z$ ] measurements. Magnetometer readings are assumed to correspond to the sample rate specified by the SampleRate property.

## Data Types: single | double

## Output Arguments

orientation - Orientation that rotates quantities from local navigation coordinate system to sensor body coordinate system
$N$-by-1 array of quaternions (default) | 3 -by-3-by- $N$ array
Orientation that rotates quantities from the local navigation coordinate system to the body coordinate system, returned as quaternions or an array. The size and type of orientation depends on whether the OrienationFormat property is set to 'quaternion' or 'Rotation matrix':

- 'quaternion' -- the output is an $N$-by-1 vector of quaternions, where $N$ is the number of samples.
- 'Rotation matrix' -- the output is a 3-by-3-by- $N$ array of rotation matrices, where $N$ is the number of samples.


## Data Types: quaternion|single|double

## angularVelocity - Angular velocity in sensor body coordinate system (rad/s)

$N$-by-3 array (default)
Angular velocity expressed in the sensor body coordinate system in rad/s, returned as an N -by-3 array, where $N$ is the number of samples.

Data Types: single | double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:
release(obj)

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object
clone Create duplicate System object
isLocked Determine if System object is in use

## Examples

## Estimate Orientation from Recorded IMU Data

Load the rpy_9axis file, which contains recorded accelerometer, gyroscope, and magnetometer sensor data from a device oscillating in pitch (around $y$-axis), then yaw (around $z$-axis), and then roll (around $x$-axis). The file also contains the sample rate of the recording.

```
ld = load('rpy_9axis.mat');
accel = ld.sensorData.Acceleration;
gyro = ld.sensorData.AngularVelocity;
mag = ld.sensorData.MagneticField;
```

Create a complementary filter object with sample rate equal to the frequency of the data.

```
Fs = ld.Fs; % Hz
fuse = complementaryFilter('SampleRate', Fs);
```

Fuse accelerometer, gyroscope, and magnetometer data using the filter.

```
q = fuse(accel, gyro, mag);
```

Visualize the results.

```
plot(eulerd( q, 'ZYX', 'frame'));
title('Orientation Estimate');
legend('Z-rotation', 'Y-rotation', 'X-rotation');
ylabel('Degrees');
```



## References

[1] Valenti, R., I. Dryanovski, and J. Xiao. "Keeping a good attitude: A quaternion-based orientation filter for IMUs and MARGs." Sensors. Vol. 15, Number 8, 2015, pp. 19302-19330.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

ahrsfilter|imufilter
Introduced in R2019b

## insfilterAsync

Estimate pose from asynchronous MARG and GPS data

## Description

The insfilterAsync object implements sensor fusion of MARG and GPS data to estimate pose in the NED (or ENU) reference frame. MARG (magnetic, angular rate, gravity) data is typically derived from magnetometer, gyroscope, and accelerometer data, respectively. The filter uses a 28 -element state vector to track the orientation quaternion, velocity, position, MARG sensor biases, and geomagnetic vector. The insfilterAsync object uses a continuous-discrete extended Kalman filter to estimate these quantities.

## Creation

## Syntax

```
filter = insfilterAsync
filter = insfilterAsync('ReferenceFrame',RF)
filter = insfilterAsync( ___,Name,Value)
Description
```

filter = insfilterAsync creates an insfilterAsync object to fuse asynchronous MARG and GPS data with default property values.
filter $=$ insfilterAsync('ReferenceFrame',RF) allows you to specify the reference frame, RF, of the filter. Specify RF as 'NED' (North-East-Down) or 'ENU' (East-North-Up). The default value is 'NED'.
filter = insfilterAsync( $\qquad$ , Name, Value) also allows you set properties of the created filter using one or more name-value pairs. Enclose each property name in single quotes.

## Properties

## ReferenceLocation - Reference location (deg, deg, meters)

[0 0 0] (default) | three-element positive row vector
Reference location, specified as a three-element row vector in geodetic coordinates (latitude, longitude, and altitude). Altitude is the height above the reference ellipsoid model, WGS84. The reference location units are [degrees degrees meters].
Data Types: single | double
QuaternionNoise - Additive quaternion process noise variance
[1e-6 le-6 le-6 le-6] (default)| scalar |four-element row vector
Additive quaternion process noise variance, specified as a scalar or four-element vector of quaternion parts.

Data Types: single | double

## AngularVelocityNoise - Additive angular velocity process noise in local navigation coordinate system ((rad/s) ${ }^{2}$ ) <br> [0.005 0.005 0.005] (default) | scalar | three-element row vector

Additive angular velocity process noise in the local navigation coordinate system in (rad/s) ${ }^{2}$, specified as a scalar or three-element row vector of positive real finite numbers.

- If AngularVelocityNoise is a row vector, the elements correspond to the noise in the $x, y$, and $z$ axes of the local navigation coordinate system, respectively.
- If AngularVelocityNoise is a scalar, the single element is applied to each axis.

Data Types: single | double
PositionNoise - Additive position process noise variance in local navigation coordinate system ( $\mathrm{m}^{2}$ )
[1e-6 le-6 1e-6] (default)| scalar | three-element row vector
Additive position process noise in the local navigation coordinate system in $\mathrm{m}^{2}$, specified as a scalar or three-element row vector of positive real finite numbers.

- If PositionNoise is a row vector, the elements correspond to the noise in the $x, y$, and $z$ axes of the local navigation coordinate system, respectively.
- If PositionNoise is a scalar, the single element is applied to each axis.


## Data Types: single | double

## VelocityNoise - Additive velocity process noise variance in local navigation coordinate system (( $\mathrm{m} / \mathrm{s})^{2}$ )

[1e-6 1e-6 1e-6] (default)| scalar | three-element row vector
Additive velocity process noise in the local navigation coordinate system in $\left(\mathrm{m} / \mathrm{s}^{2}\right.$, specified as a scalar or three-element row vector of positive real finite numbers.

- If VelocityNoise is a row vector, the elements correspond to the noise in the $x, y$, and $z$ axes of the local navigation coordinate system, respectively.
- If VelocityNoise is a scalar, the single element is applied to each axis.

Data Types: single | double

## AccelerationNoise - Additive acceleration process noise variance in local navigation coordinate system ((m/s $\left.\mathbf{s}^{\mathbf{2}}\right)^{\mathbf{2}}$ ) <br> [50 50 50] (default) | scalar | three-element row vector

Additive acceleration process noise in $\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}$, specified as a scalar or three-element row vector of positive real finite numbers.

- If AccelerationNoise is a row vector, the elements correspond to the noise in the $x, y$, and $z$ axes of the local navigation coordinate system, respectively.
- If AccelerationNoise is a scalar, the single element is applied to each axis.

Data Types: single|double

## GyroscopeBiasNoise - Additive process noise variance from gyroscope bias ((rad/s) ${ }^{\mathbf{2}}$ )

[1e-10 1e-10 1e-10] (default)| scalar|three-element row vector
Additive process noise variance from the gyroscope bias in (rad/s) ${ }^{2}$, specified as a scalar or threeelement row vector of positive real finite numbers.

- If GyroscopeBiasNoise is a row vector, the elements correspond to the noise in the $x, y$, and $z$ axes of the gyroscope, respectively.
- If GyroscopeBiasNoise is a scalar, the single element is applied to each axis.

Data Types: single|double

## AccelerometerBiasNoise - Additive process noise variance from accelerometer bias ((m/s $\left.\left.{ }^{2}\right)^{2}\right)$ <br> [le-4 le-4 1e-4] (default) | positive scalar| three-element row vector

Additive process noise variance from accelerometer bias in $\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}$, specified as a scalar or threeelement row vector of positive real numbers.

- If AccelerometerBiasNoise is a row vector, the elements correspond to the noise in the $x, y$, and $z$ axes of the accelerometer, respectively.
- If AccelerometerBiasNoise is a scalar, the single element is applied to each axis.


## GeomagneticVectorNoise - Additive process noise variance of geomagnetic vector in local navigation coordinate system ( $\mu \mathrm{T}^{\mathbf{2}}$ ) <br> [1e-6 le-6 le-6] (default) | positive scalar| three-element row vector

Additive process noise variance of geomagnetic vector in $\mu \mathrm{T}^{2}$, specified as a scalar or three-element row vector of positive real numbers.

- If GeomagneticVectorNoise is a row vector, the elements correspond to the noise in the $x, y$, and $z$ axes of the local navigation coordinate system, respectively.
- If GeomagneticVectorNoise is a scalar, the single element is applied to each axis.


## MagnetometerBiasNoise - Additive process noise variance from magnetometer bias ( $\mu \mathrm{T}^{\mathbf{2}}$ )

[0.1 0.1 0.1] (default) | positive scalar \| three-element row vector
Additive process noise variance from magnetometer bias in $\mu \mathrm{T}^{2}$, specified as a scalar or three-element row vector of positive real numbers.

- If MagnetometerBiasNoise is a row vector, the elements correspond to the noise in the $x, y$, and $z$ axes of the magnetometer, respectively.
- If MagnetometerBiasNoise is a scalar, the single element is applied to each axis.


## State - State vector of extended Kalman filter

28-element column vector
State vector of the extended Kalman filter. The state values represent:

| State | Units | Index |
| :--- | :--- | :--- |
| Orientation (quaternion parts) | $\mathrm{N} / \mathrm{A}$ | $1: 4$ |
| Angular Velocity (XYZ) | $\mathrm{rad} / \mathrm{s}$ | $5: 7$ |


| State | Units | Index |
| :--- | :--- | :--- |
| Position (NED or ENU) | m | $8: 10$ |
| Velocity (NED or ENU) | $\mathrm{m} / \mathrm{s}$ | $11: 13$ |
| Acceleration (NED or ENU) | $\mathrm{m} / \mathrm{s}^{2}$ | $14: 16$ |
| Accelerometer Bias (XYZ) | $\mathrm{m} / \mathrm{s}^{2}$ | $17: 19$ |
| Gyroscope Bias (XYZ) | $\mathrm{rad} / \mathrm{s}$ | $20: 22$ |
| Geomagnetic Field Vector (NED $\mu \mathrm{T}$ <br> or ENU)  <br> Magnetometer Bias (XYZ) $\mu \mathrm{T}$ | $23: 25$ |  |
|  |  | $26: 28$ |

The default initial state corresponds to an object at rest located at [0 0 0] in geodetic LLA coordinates.
Data Types: single | double

## StateCovariance - State error covariance for extended Kalman filter eye(28) (default) | 28 -by-28 matrix

State error covariance for the extended Kalman filter, specified as a 28 -by-28-element matrix of real numbers.
Data Types: single | double

## Object Functions

predict Update states based on motion model for insfilterAsync fuseaccel Correct states using accelerometer data for insfilterAsync
fusegyro Correct states using gyroscope data for insfilterAsync
fusemag Correct states using magnetometer data for insfilterAsync
fusegps Correct states using GPS data for insfilterAsync
correct Correct states using direct state measurements for insfilterAsync
residual Residuals and residual covariances from direct state measurements for insfilterAsync
residualaccel Residuals and residual covariance from accelerometer measurements for insfilterAsync
residualgps Residuals and residual covariance from GPS measurements for insfilterAsync
residualmag Residuals and residual covariance from magnetometer measurements for insfilterAsync
residualgyro Residuals and residual covariance from gyroscope measurements for insfilterAsync
pose Current position, orientation, and velocity estimate for insfilterAsync
reset $\quad$ Reset internal states for insfilterAsync
stateinfo Display state vector information for insfilterAsync
copy Create copy of insfilterAsync
tune Tune insfilterAsync parameters to reduce estimation error
tunernoise Noise structure of fusion filter

## Examples

## Estimate Pose of UAV

Load logged sensor data and ground truth pose.

```
load('uavshort.mat','refloc','initstate','imuFs', ...
    'accel','gyro','mag','lla','gpsvel', ...
    'trueOrient','truePos')
```

Create an INS filter to fuse asynchronous MARG and GPS data to estimate pose.

```
filt = insfilterAsync;
```

filt.ReferenceLocation = refloc;
filt.State $=$ [initstate(1:4);0;0;0;initstate(5:10);0;0;0;initstate(11:end)];

Define sensor measurement noises. The noises were determined from datasheets and experimentation.

```
Rmag = 80;
Rvel = 0.0464;
Racc = 800;
Rgyro = 1e-4;
Rpos = 34;
```

Preallocate variables for position and orientation. Allocate a variable for indexing into the GPS data.

```
N = size(accel,1);
p = zeros(N,3);
q = zeros(N,1,'quaternion');
gpsIdx = 1;
```

Fuse accelerometer, gyroscope, magnetometer, and GPS data. The outer loop predicts the filter forward one time step and fuses accelerometer and gyroscope data at the IMU sample rate.

```
for ii = 1:N
    % Predict the filter forward one time step
    predict(filt,1./imuFs);
    % Fuse accelerometer and gyroscope readings
    fuseaccel(filt,accel(ii,:),Racc);
    fusegyro(filt,gyro(ii,:),Rgyro);
    % Fuse magnetometer at 1/2 the IMU rate
    if ~mod(ii, fix(imuFs/2))
        fusemag(filt,mag(ii,:),Rmag);
    end
    % Fuse GPS once per second
    if ~mod(ii,imuFs)
        fusegps(filt,lla(gpsIdx,:),Rpos,gpsvel(gpsIdx,:),Rvel);
        gpsIdx = gpsIdx + 1;
    end
    % Log the current pose estimate
    [p(ii,:),q(ii)] = pose(filt);
end
```

Calculate the RMS errors between the known true position and orientation and the output from the asynchronous IMU filter.

```
posErr = truePos - p;
qErr = rad2deg(dist(trueOrient,q));
pRMS = sqrt(mean(posErr.^2));
qRMS = sqrt(mean(qErr.^2));
fprintf('Position RMS Error\n');
Position RMS Error
fprintf('\tX: %.2f, Y: %.2f, Z: %.2f (meters)\n\n',pRMS(1),pRMS(2),pRMS(3));
    X: 0.55, Y: 0.71, Z: 0.74 (meters)
fprintf('Quaternion Distance RMS Error\n');
Quaternion Distance RMS Error
fprintf('\t%.2f (degrees)\n\n', qRMS);
    4.72 (degrees)
```

Visualize the true position and the estimated position.

```
plot3(truePos(:,1),truePos(:,2),truePos(:,3),'LineWidth',2)
hold on
plot3(p(:,1),p(:,2),p(:,3),'r:','LineWidth',2)
grid on
xlabel('N (m)')
ylabel('E (m)')
zlabel('D (m)')
```



## Algorithms

## Dynamic Model Used in insfilterAsync

Note: The following algorithm only applies to an NED reference frame.
insfilterAsync implements a 28 -axis continuous-discrete extended Kalman filter using sequential fusion. The filter relies on the assumption that individual sensor measurements are uncorrelated. The filter uses an omnidirectional motion model and assumes constant angular velocity and constant acceleration. The state is defined as:

where

- $q_{0}, q_{1}, q_{2}, q_{3}$-- Parts of orientation quaternion. The orientation quaternion represents a frame rotation from the platform's current orientation to the local NED coordinate system.
- angVel ${ }_{\mathrm{X}}$, angVel $_{\mathrm{Y}}$, angVel $_{\mathrm{Z}}--$ Angular velocity relative to the platform's body frame. $^{\text {a }}$
- position ${ }_{N}$, position $_{E}$, position $_{\mathrm{D}}$-- Position of the platform in the local NED coordinate system.
- $\nu_{\mathrm{N}}, \nu_{\mathrm{E}}, \nu_{\mathrm{D}}$-- Velocity of the platform in the local NED coordinate system.

- accelbias ${ }_{\mathrm{X}}$, accelbias $_{\mathrm{Y}}$, accelbias $_{\mathrm{Z}}$-- Bias in the accelerometer reading.
- gyrobias $_{\mathrm{X}}$, gyrobias $_{\mathrm{Y}}$, gyrobias $_{\mathrm{Z}}$-- Bias in the gyroscope reading.
- geomagneticFieldVector ${ }_{\mathrm{N}}$, geomagneticFieldVector ${ }_{\mathrm{E}}$, geomagneticFieldVector $_{\mathrm{D}}$-- Estimate of the geomagnetic field vector at the reference location.
- magbias ${ }_{\mathrm{X}}$, magbias $_{\mathrm{Y}}$, magbias $_{\mathrm{Z}}$-- Bias in the magnetometer readings.

Given the conventional formation of the process equation, $\dot{x}=f(x)+w, w$ is the process noise, $\dot{x}$ is the derivative of $x$, and:
$f(x)=\left[\begin{array}{c}\frac{-\left(q_{1}\right)\left(\text { angVel }_{\mathrm{X}}\right)-\left(q_{2}\right)\left(\text { angVel }_{\mathrm{Y}}\right)-\left(q_{3}\right)\left(\text { angVel }_{\mathrm{Z}}\right)}{2} \\ \frac{\left(q_{0}\right)\left(a n g V e l_{\mathrm{X}}\right)-\left(q_{3}\right)\left(a n g V e l_{\mathrm{Y}}\right)+\left(q_{1}\right)\left(\text { angVel }_{\mathrm{Z}}\right)}{2} \\ \frac{\left(q_{3}\right)\left(\text { angVel }_{\mathrm{X}}\right)+\left(q_{0}\right)\left(a n g V e l_{\mathrm{Y}}\right)-\left(q_{1}\right)\left(\text { angVel }_{\mathrm{Z}}\right)}{2} \\ \frac{\left(q_{1}\right)\left(\text { angVel }_{\mathrm{X}}\right)-\left(q_{2}\right)\left(\text { angVel }_{\mathrm{Y}}\right)+\left(q_{0}\right)\left(\text { angVel }_{\mathrm{Z}}\right)}{2} \\ 0 \\ 0 \\ 0 \\ \nu_{\mathrm{N}} \\ \nu_{\mathrm{E}} \\ \nu_{\mathrm{D}} \\ a c c e l_{\mathrm{N}} \\ a c c e l_{\mathrm{E}} \\ a c c e l_{\mathrm{D}} \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ \end{array}\right]$

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also <br> insfilterErrorState|insfilterNonholonomic|insfilterMARG Introduced in R2019a

## correct

Correct states using direct state measurements for insfilterAsync

## Syntax

correct(FUSE,idx,measurement, measurementCovariance)

## Description

correct(FUSE, idx, measurement, measurementCovariance) corrects the state and state estimation error covariance based on the measurement and measurement covariance. The measurement maps directly to the state specified by the indices idx.

## Input Arguments

FUSE - insfilterAsync object
object
insfilterAsync, specified as an object.
idx - State vector index of measurement to correct
$N$-element vector of increasing integers in the range [1,28]
State vector index of measurement to correct, specified as an $N$-element vector of increasing integers in the range [1, 28].

The state values represent:

| State | Units | Index |
| :--- | :--- | :--- |
| Orientation (quaternion parts) | $\mathrm{N} / \mathrm{A}$ | $1: 4$ |
| Angular Velocity (XYZ) | $\mathrm{rad} / \mathrm{s}$ | $5: 7$ |
| Position (NED) | m | $8: 10$ |
| Velocity (NED) | $\mathrm{m} / \mathrm{s}$ | $11: 13$ |
| Acceleration (NED) | $\mathrm{m} / \mathrm{s}^{2}$ | $14: 16$ |
| Accelerometer Bias (XYZ) | $\mathrm{m} / \mathrm{s}^{2}$ | $17: 19$ |
| Gyroscope Bias (XYZ) | $\mathrm{rad} / \mathrm{s}$ | $20: 22$ |
| Geomagnetic Field Vector (NED) | $\mu \mathrm{T}$ | $23: 25$ |
| Magnetometer Bias (XYZ) | $\mu \mathrm{T}$ | $26: 28$ |

Data Types: single | double

## measurement - Direct measurement of state

$N$-element vector
Direct measurement of state, specified as an $N$-element vector. $N$ is the number of elements of the index argument, idx.

Data Types: single | double
measurementCovariance - Covariance of measurement
scalar | $N$-element vector | $N$-by- $N$ matrix
Covariance of measurement, specified as a scalar, $N$-element vector, or $N$-by- $N$ matrix. $N$ is the number of elements of the index argument, idx.
Data Types: single | double

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

insfilterAsync|insfilter
Introduced in R2019a

## copy

Create copy of insfilterAsync

## Syntax

newFilter $=$ copy(filter)

## Description

newFilter = copy(filter) returns a copy of the insfilterAsync, filter, that has exactly the same property values.

## Input Arguments

filter - Filter to be copied
insfilterAsync
Filter to be copied, specified as an insfilterAsync object.

## Output Arguments

newFilter - New copied filter
insfilterAsync
New copied filter, returned as an insfilterAsync object.

## See Also

insfilterAsync
Introduced in R2020b

## fuseaccel

Correct states using accelerometer data for insfilterAsync

## Syntax

[res,resCov] = fuseaccel(FUSE,acceleration,accelerationCovariance)

## Description

[res,resCov] = fuseaccel(FUSE,acceleration,accelerationCovariance) fuses accelerometer data to correct the state estimate.

## Input Arguments

FUSE - insfilterAsync object
object
insfilterAsync, specified as an object.
acceleration - Accelerometer readings in local sensor body coordinate system (m/s)
3-element row vector
Accelerometer readings in local sensor body coordinate system in $\mathrm{m} / \mathrm{s}^{2}$, specified as a 3 -element row vector

Data Types: single | double
accelerationCovariance - Acceleration error covariance of accelerometer measurement ( $\left.\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}\right)$
scalar | 3-element row vector | 3-by-3 matrix
Acceleration error covariance of the accelerometer measurement in $\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}$, specified as a scalar, 3element row vector, or 3-by-3 matrix.
Data Types: single | double

## Output Arguments

## res - Residual

1-by-3 vector of real values
Residual, returned a 1-by-3 vector of real values in $\mathrm{m} / \mathrm{s}^{2}$.

## resCov - Residual covariance

3-by-3 matrix of real values
Residual covariance, returned as a 3-by-3 matrix of real values in $\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}$.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

insfilterAsync|insfilter
Introduced in R2019a

## fusegps

Correct states using GPS data for insfilterAsync

## Syntax

[res,resCov] = fusegps(FUSE,position,positionCovariance)
[res,resCov] = fusegps(FUSE,position, positionCovariance,velocity, velocityCovariance)

## Description

[res, resCov] = fusegps(FUSE, position, positionCovariance) fuses GPS position data to correct the state estimate.
[res, resCov] = fusegps(FUSE, position, positionCovariance, velocity,
velocityCovariance) fuses GPS position and velocity data to correct the state estimate.

## Input Arguments

FUSE - insfilterAsync object
object
insfilterAsync, specified as an object.
position - Position of GPS receiver (LLA)
3-element row vector
Position of GPS receiver in geodetic latitude, longitude, and altitude (LLA) specified as a real finite 3element row vector. Latitude and longitude are in degrees with north and east being positive. Altitude is in meters.
Data Types: single | double
positionCovariance - Position measurement covariance of GPS receiver ( $\mathbf{m}^{\mathbf{2}}$ )
3-by-3 matrix
Position measurement covariance of GPS receiver in $\mathrm{m}^{2}$, specified as a 3-by-3 matrix.
Data Types: single | double

## velocity - Velocity of GPS receiver in local NED coordinate system ( $\mathrm{m} / \mathrm{s}$ )

3-element row vector
Velocity of the GPS receiver in the local NED coordinate system in $\mathrm{m} / \mathrm{s}$, specified as a 3-element row vector.

## Data Types: single | double

velocityCovariance - Velocity measurement covariance of GPS receiver ( $\mathrm{m} / \mathrm{s}^{\mathbf{2}}$ )
3-by-3 matrix

Velocity measurement covariance of the GPS receiver in the local NED coordinate system in $\mathrm{m} / \mathrm{s}^{2}$, specified as a 3-by-3 matrix.

Data Types: single|double

## Output Arguments

## res - Position and velocity residual

1 -by- 6 vector of real values
Position and velocity residual, returned as a 1-by-6 vector of real values in $m$ and $m / s$, respectively.
resCov - Residual covariance
6 -by-6 matrix of real values
Residual covariance, returned as a 6-by-6 matrix of real values.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

insfilterAsync|insfilter|insfilterMARG
Introduced in R2019a

## fusegyro

Correct states using gyroscope data for insfilterAsync

## Syntax

[res,resCov] = fusegyro(FUSE,gyroReadings,gyroCovariance)

## Description

[res,resCov] = fusegyro(FUSE,gyroReadings,gyroCovariance) fuses gyroscope data to correct the state estimate.

## Input Arguments

FUSE - insfilterAsync object
object
insfilterAsync, specified as an object.
gyroReadings - Gyroscope readings in local sensor body coordinate system (rad/s)
3-element row vector
Gyroscope readings in local sensor body coordinate system in rad/s, specified as a 3 -element row vector.

Data Types: single | double
gyroCovariance - Covariance of gyroscope measurement error ((rad/s) ${ }^{\mathbf{2}}$ )
scalar | 3-element row vector | 3-by-3 matrix
Covariance of gyroscope measurement error in $(\mathrm{rad} / \mathrm{s})^{2}$, specified as a scalar, 3-element row vector, or 3-by-3 matrix.
Data Types: single | double

## Output Arguments

## res - Residual

1-by-3 vector of real values
Residual, returned as a 1-by-3 vector of real values in rad/s.

## resCov - Residual covariance

3-by-3 matrix of real values
Residual covariance, returned as a 3-by-3 matrix of real values in $(\mathrm{rad} / \mathrm{s})^{2}$.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

insfilterAsync|insfilter
Introduced in R2019a

## fusemag

Correct states using magnetometer data for insfilterAsync

## Syntax

[res,resCov] = fusemag(FUSE,magReadings,magReadingsCovariance)

## Description

[res,resCov] = fusemag(FUSE,magReadings,magReadingsCovariance) fuses magnetometer data to correct the state estimate.

## Input Arguments

FUSE - insfilterAsync object
object
insfilterAsync, specified as an object.
magReadings - Magnetometer readings ( $\mu \mathrm{T}$ )
3-element row vector
Magnetometer readings in $\mu \mathrm{T}$, specified as a 3 -element row vector of finite real numbers.
Data Types: single | double
magReadingsCovariance - Magnetometer readings error covariance ( $\boldsymbol{\mu} \mathbf{T}^{\mathbf{2}}$ )
scalar | 3-element row vector | 3-by-3 matrix
Magnetometer readings error covariance in $\mu \mathrm{T}^{2}$, specified as a scalar, 3-element row vector, or 3-by-3 matrix.
Data Types: single | double

## Output Arguments

res - Residual
1-by-3 vector of real values
Residual, returned a 1 -by- 3 vector of real values in $\mu \mathrm{T}$.
Data Types: single | double

## resCov - Residual covariance

3 -by-3 matrix of real values
Residual covariance, returned a 3-by-3 matrix of real values in $(\mu \mathrm{T})^{2}$.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

insfilterAsync|insfilter
Introduced in R2019a

## pose

Current position, orientation, and velocity estimate for insfilterAsync

## Syntax

[position,orientation, velocity] = pose(FUSE)
[position,orientation, velocity] = pose(FUSE,format)

## Description

[position,orientation, velocity] = pose(FUSE) returns the current estimate of the pose.
[position,orientation, velocity] = pose(FUSE,format) returns the current estimate of the pose with orientation in the specified orientation format.

## Input Arguments

FUSE - insfilterAsync object
object
insfilterAsync, specified as an object.

## format - Output orientation format

'quaternion' (default) | 'rotmat'
Output orientation format, specified as either 'quaternion' for a quaternion or 'rotmat' for a rotation matrix.
Data Types: char | string

## Output Arguments

## position - Position estimate expressed in the local coordinate system (m)

3-element row vector
Position estimate expressed in the local coordinate system of the filter in meters, returned as a 3element row vector.

Data Types: single | double
orientation - Orientation estimate expressed in the local coordinate system
quaternion (default) | 3-by-3 rotation matrix
Orientation estimate expressed in the local coordinate system of the filter, returned as a scalar quaternion or 3-by-3 rotation matrix. The quaternion or rotation matrix represents a frame rotation from the local reference frame of the filter to the body reference frame.
Data Types: single | double | quaternion
velocity - Velocity estimate expressed in local coordinate system (m/s)
3 -element row vector

Velocity estimate expressed in the local coordinate system of the filter in $\mathrm{m} / \mathrm{s}$, returned as a 3-element row vector.

Data Types: single | double

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

insfilterAsync|insfilter
Introduced in R2019a

## predict

Update states based on motion model for insfilterAsync

## Syntax

predict(FUSE,dt)

## Description

predict(FUSE, dt) updates states based on the motion model.

## Input Arguments

FUSE - insfilterAsync object
object
insfilterAsync, specified as an object.
dt - Delta time to propagate forward (s)
scalar
Delta time to propagate forward in seconds, specified as a positive scalar.
Data Types: single | double

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

insfilterAsync|insfilter
Introduced in R2019a

## reset

Reset internal states for insfilterAsync

## Syntax

reset (FUSE)

## Description

reset (FUSE) resets the State and StateCovariance properties of the insfilterAsync object to their default values.

## Input Arguments

FUSE - insfilterAsync object
object
insfilterAsync, specified as an object.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
See Also
insfilterAsync|insfilter

Introduced in R2019a

## residual

Residuals and residual covariances from direct state measurements for insfilterAsync

## Syntax

[res, resCov]= residual(FUSE,idx,measurement,measurementCovariance)

## Description

[res, resCov]= residual(FUSE,idx,measurement,measurementCovariance) computes the residual, res, and the residual covariance, resCov, based on the direct state measurement and measurement covariance. The measurement maps directly to the states specified by indices, idx.

## Input Arguments

FUSE - insfilterAsync
ahrs10filter|object
insfilterAsync, specified as an object.

## idx - State vector index of measurement to correct

$N$-element vector of increasing integers in the range [1, 28]
State vector index of measurement to correct, specified as an $N$-element vector of increasing integers in the range [1, 28].

The state values represent:

| State | Units | Index |
| :--- | :--- | :--- |
| Orientation (quaternion parts) | $\mathrm{N} / \mathrm{A}$ | $1: 4$ |
| Angular Velocity (XYZ) | $\mathrm{rad} / \mathrm{s}$ | $5: 7$ |
| Position (NED) | m | $8: 10$ |
| Velocity (NED) | $\mathrm{m} / \mathrm{s}$ | $11: 13$ |
| Acceleration (NED) | $\mathrm{m} / \mathrm{s}^{2}$ | $14: 16$ |
| Accelerometer Bias (XYZ) | $\mathrm{m} / \mathrm{s}^{2}$ | $17: 19$ |
| Gyroscope Bias (XYZ) | $\mathrm{rad} / \mathrm{s}$ | $20: 22$ |
| Geomagnetic Field Vector (NED) | $\mu \mathrm{T}$ | $23: 25$ |
| Magnetometer Bias (XYZ) | $\mu \mathrm{T}$ | $26: 28$ |

Data Types: single | double

## measurement - Direct measurement of state

$N$-element vector
Direct measurement of state, specified as a $N$-element vector. $N$ is the number of elements of the index argument, idx.

## measurementCovariance - Covariance of measurement

$N$-by- $N$ matrix
Covariance of measurement, specified as an $N$-by- $N$ matrix. $N$ is the number of elements of the index argument, idx.

## Output Arguments

## res - Measurement residual

1 -by- $N$ vector of real values
Measurement residual, returned as a 1-by- $N$ vector of real values.

## resCov - Residual covariance

$N$-by- $N$ matrix of real values
Residual covariance, returned as a $N$-by- $N$ matrix of real values.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

insfilterAsync
Introduced in R2020a

## residualaccel

Residuals and residual covariance from accelerometer measurements for insfilterAsync

## Syntax

[res,resCov] = residualaccel(FUSE,acceleration,accelerationCovariance)

## Description

[res,resCov] = residualaccel(FUSE,acceleration,accelerationCovariance) computes the residual, res, and the residual covariance, resCov, based on the acceleration readings and the corresponding covariance.

## Input Arguments

FUSE - insfilterAsync
ahrs10filter|object
insfilterAsync, specified as an object.
acceleration - Accelerometer readings in local sensor body coordinate system (m/s)
3 -element row vector
Accelerometer readings in local sensor body coordinate system in $\mathrm{m} / \mathrm{s}^{2}$, specified as a 3 -element row vector

Data Types: single | double
accelerationCovariance - Acceleration error covariance of accelerometer measurement ( $\left.\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}\right)$
scalar | 3-element row vector | 3-by-3 matrix
Acceleration error covariance of the accelerometer measurement in $\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}$, specified as a scalar, 3element row vector, or 3-by-3 matrix.
Data Types: single | double

## Output Arguments

## res - Residual

1-by-3 vector of real values
Residual, returned a 1-by-3 vector of real values in $\mathrm{m} / \mathrm{s}^{2}$.
resCov - Residual covariance
3-by-3 matrix of real values
Residual covariance, returned a 3-by-3 matrix of real values in $\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}$.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

insfilterAsync|insfilter
Introduced in R2020a

## residualgps

Residuals and residual covariance from GPS measurements for insfilterAsync

## Syntax

[res,resCov] = residualgps(FUSE,position,positionCovariance)
[res,resCov] = residualgps(FUSE,position, positionCovariance,velocity, velocityCovariance)

## Description

[res,resCov] = residualgps(FUSE, position, positionCovariance) computes the residual, res, and the residual covariance, resCov, based on the GPS position measurement and covariance.
[res,resCov] = residualgps(FUSE,position, positionCovariance, velocity, velocityCovariance) computes the residual, res, and the residual covariance, resCov, based on the GPS position measurement and covariance.

## Input Arguments

FUSE - insfilterAsync
ahrs10filter|object
insfilterAsync, specified as an object.
position - Position of GPS receiver (LLA)
3 -element row vector
Position of GPS receiver in geodetic latitude, longitude, and altitude (LLA) specified as a real finite 3element row vector. Latitude and longitude are in degrees with north and east being positive. Altitude is in meters.

## Data Types: single | double

positionCovariance - Position measurement covariance of GPS receiver ( $\mathbf{m}^{\mathbf{2}}$ )
3-by-3 matrix
Position measurement covariance of GPS receiver in $\mathrm{m}^{2}$, specified as a 3 -by- 3 matrix.
Data Types: single | double

## velocity - Velocity of GPS receiver in local NED coordinate system (m/s)

3-element row vector
Velocity of the GPS receiver in the local NED coordinate system in $\mathrm{m} / \mathrm{s}$, specified as a 3 -element row vector.

Data Types: single | double
velocityCovariance - Velocity measurement covariance of GPS receiver ( $\mathbf{m} / \mathbf{s}^{\mathbf{2}}$ )
3-by-3 matrix

Velocity measurement covariance of the GPS receiver in the local NED coordinate system in $\mathrm{m} / \mathrm{s}^{2}$, specified as a 3-by-3 matrix.

Data Types: single|double

## Output Arguments

## res - Position and velocity residual

1 -by- 3 vector of real values | 1 -by-6 vector of real values
Position and velocity residual, returned as a 1-by-3 vector of real values if the inputs only contain position information, and returned as 1-by-6 vector of real values if the inputs also contain velocity information.

## resCov - Residual covariance

3-by-3 matrix of real values | 6-by-6 matrix of real values
Residual covariance, returned as a 3-by-3 matrix of real values if the inputs only contain position information, and a 6 -by- 6 matrix of real values if the inputs also contain velocity information.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

insfilterAsync
Introduced in R2020a

## residualgyro

Residuals and residual covariance from gyroscope measurements for insfilterAsync

## Syntax

[res,resCov] = residualgyro(FUSE,gyroReadings,gyroCovariance)

## Description

[res,resCov] = residualgyro(FUSE,gyroReadings,gyroCovariance) computes the residual, res, and the innovation covariance, resCov, based on the gyroscope readings and the corresponding covariance.

## Input Arguments

FUSE - insfilterAsync
ahrs10filter|object
insfilterAsync, specified as an object.
gyroReadings - Gyroscope readings in local sensor body coordinate system (rad/s)
3-element row vector
Gyroscope readings in local sensor body coordinate system in rad/s, specified as a 3 -element row vector.

Data Types: single | double
gyroCovariance - Covariance of gyroscope measurement error ((rad/s) ${ }^{\mathbf{2}}$ )
scalar | 3-element row vector | 3-by-3 matrix
Covariance of gyroscope measurement error in (rad/s) ${ }^{2}$, specified as a scalar, 3-element row vector, or 3-by-3 matrix.
Data Types: single | double

## Output Arguments

## res - Residual

1-by-3 vector of real values
Residual, returned as a 1-by-3 vector of real values in rad/s.

## resCov - Residual covariance

3 -by-3 matrix of real values
Residual covariance, returned as a 3-by-3 matrix of real values in (rad/s) ${ }^{2}$.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

insfilterAsync|insfilter
Introduced in R2020a

## residualmag

Residuals and residual covariance from magnetometer measurements for insfilterAsync

## Syntax

[res,resCov] = residualmag(FUSE,magReadings,magReadingsCovariance)

## Description

[res,resCov] = residualmag(FUSE,magReadings,magReadingsCovariance) computes the residual, residual, and the residual covariance, resCov, based on the magnetometer readings and the corresponding covariance.

## Input Arguments

FUSE - insfilterAsync
ahrs10filter|object
insfilterAsync, specified as an object.
magReadings - Magnetometer readings ( $\mu \mathrm{T}$ )
3-element row vector
Magnetometer readings in $\mu \mathrm{T}$, specified as a 3-element row vector of finite real numbers.
Data Types: single | double
magReadingsCovariance - Magnetometer readings error covariance ( $\boldsymbol{\mu} \mathbf{T}^{\mathbf{2}}$ )
scalar | 3-element row vector | 3-by-3 matrix
Magnetometer readings error covariance in $\mu \mathrm{T}^{2}$, specified as a scalar, 3 -element row vector, or 3-by-3 matrix.

Data Types: single | double

## Output Arguments

## res - Residual

1-by-3 vector of real values
Residual, returned as a 1 -by- 3 vector of real values in $\mu \mathrm{T}$.
Data Types: single | double

## resCov - Residual covariance

3-by-3 matrix of real values
Residual covariance, returned a 3-by-3 matrix of real values in $(\mu \mathrm{T})^{2}$.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

insfilterAsync
Introduced in R2020a

## stateinfo

Display state vector information for insfilterAsync

## Syntax

stateinfo(FUSE)
info = stateinfo(FUSE)

## Description

stateinfo(FUSE) displays the description of each index of the State property of the insfilterAsync object and the associated units.
info = stateinfo(FUSE) returns a structure with fields containing descriptions of the elements of the state vector of the filter, FUSE.

## Examples

## State Information of insfilterAsync

Create an insfilterAsync object.
filter = insfilterAsync;
Display the state information of the created filter.

```
stateinfo(filter)
States Units Index
Orientation (quaternion parts) 1:4
Angular Velocity (XYZ) rad/s 5:7
Position (NAV) m 8:10
Velocity (NAV) m/s 11:13
Acceleration (NAV) m/s^2 14:16
Accelerometer Bias (XYZ) m/s^2 17:19
Gyroscope Bias (XYZ) rad/s 20:22
Geomagnetic Field Vector (NAV) \muT 23:25
Magnetometer Bias (XYZ) 晅 26:28
```

Output the state information of the filter as a structure.

```
info = stateinfo(filter)
info = struct with fields:
                            Orientation: [lllll
        AngularVelocity: [5 6 7]
            Position: [8 9 10]
            Velocity: [11 12 13]
            Acceleration: [14 15 16]
    AccelerometerBias: [17 18 19]
        GyroscopeBias: [20 21 22]
```


## Input Arguments

FUSE - insfilterAsync object
object
insfilterAsync, specified as an object.

## Output Arguments

info - State information
structure
State information, returned as a structure. The field names of the structure are names of the elements of the state vector in the filter. The values of each field are the corresponding indices of the state vector.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

insfilterAsync|insfilter
Introduced in R2019a

## tune

Tune insfilterAsync parameters to reduce estimation error

## Syntax

tunedMeasureNoise = tune(filter, measureNoise, sensorData, groundTruth) tunedMeasureNoise = tune( $\qquad$ , config)

## Description

tunedMeasureNoise = tune(filter, measureNoise, sensorData, groundTruth) adjusts the properties of the insfilterAsync filter object, filter, and measurement noises to reduce the root-mean-squared (RMS) state estimation error between the fused sensor data and the ground truth. The function also returns the tuned measurement noise, tunedMeasureNoise. The function uses the property values in the filter and the measurement noise provided in the measureNoise structure as the initial estimate for the optimization algorithm.
tunedMeasureNoise = tune( $\qquad$ , config) specifies the tuning configuration based on a tunerconfig object, config.

## Examples

## Tune insfilterAsync to Optimize Pose Estimate

Load the recorded sensor data and ground truth data.
load('insfilterAsyncTuneData.mat');
Create timetables for the sensor data and the truth data.

```
sensorData = timetable(Accelerometer, Gyroscope, ...
    Magnetometer, GPSPosition, GPSVelocity, 'SampleRate', 100);
groundTruth = timetable(Orientation, Position, ...
    'SampleRate', 100);
```

Create an insfilterAsync filter object that has a few noise properties.

```
filter = insfilterAsync('State', initialState, ...
    'StateCovariance', initialStateCovariance, ...
    'AccelerometerBiasNoise', le-7, ...
    'GyroscopeBiasNoise', le-7, ...
    'MagnetometerBiasNoise', le-7, ...
    'GeomagneticVectorNoise', 1e-7);
```

Create a tuner configuration object for the filter. Set the maximum iterations to two. Also, set the tunable parameters as the unspecified properties.

```
config = tunerconfig('insfilterAsync','MaxIterations',8);
config.TunableParameters = setdiff(config.TunableParameters, ...
    {'GeomagneticVectorNoise', 'AccelerometerBiasNoise', ...
```

```
    'GyroscopeBiasNoise', 'MagnetometerBiasNoise'});
config.TunableParameters
ans = 1\times10 string
    "AccelerationNoise" "AccelerometerNoise" "AngularVelocityNoise" "GPSPositionNoise"
```

Use the tuner noise function to obtain a set of initial sensor noises used in the filter.

```
measNoise = tunernoise('insfilterAsync')
measNoise = struct with fields:
    AccelerometerNoise: 1
            GyroscopeNoise: 1
        MagnetometerNoise: 1
        GPSPositionNoise: 1
        GPSVelocityNoise: 1
```

Tune the filter and obtain the tuned parameters.

| tunedParams $=$ tune(filter,measNoise, sensorData, groundTruth, config); |  |  |
| :---: | :--- | :--- |
| Iteration | Parameter | Metric |
| 1 |  |  |
| 1 | AccelerationNoise | 2.1345 |
| 1 | AccelerometerNoise | 2.1264 |
| 1 | AngularVelocityNoise | 1.9659 |
| 1 | GPSPositionNoise | 1.9341 |
| 1 | GPSVelocityNoise | 1.8420 |
| 1 | GyroscopeNoise | 1.7589 |
| 1 | MagnetometerNoise | 1.7362 |
| 1 | PositionNoise | 1.7362 |
| 1 | QuaternionNoise | 1.7218 |
| 2 | VelocityNoise | 1.7218 |
| 2 | AccelerationNoise | 1.7190 |
| 2 | AccelerometerNoise | 1.7170 |
| 2 | AngularVelocityNoise | 1.6045 |
| 2 | GPSPositionNoise | 1.5948 |
| 2 | GPSVelocityNoise | 1.5323 |
| 2 | GyroscopeNoise | 1.4803 |
| 2 | MagnetometerNoise | 1.4703 |
| 2 | PositionNoise | 1.4703 |
| 2 | QuaternionNoise | 1.4632 |
| 3 | VelocityNoise | 1.4632 |
| 3 | AccelerationNoise | 1.4596 |
| 3 | AccelerometerNoise | 1.4548 |
| 3 | AngularVelocityNoise | 1.3923 |
| 3 | GPSPositionNoise | 1.3810 |
| 3 | GPSVelocityNoise | 1.3322 |
| 3 | GyroscopeNoise | 1.2998 |
| 3 | MagnetometerNoise | 1.2976 |
| 3 | PositionNoise | 1.2976 |
| 3 | QuaternionNoise | 1.2943 |
| 4 | VelocityNoise | 1.2943 |
| 4 | AccelerationNoise | 1.2906 |
| 4 | AngularVelocityNoise | 1.2836 |
| 4 | GPSPositionNoise | 1.2491 |
|  |  | 1.2258 |


| 4 | GPSVelocityNoise | 1.1880 |
| :---: | :---: | :---: |
| 4 | GyroscopeNoise | 1.1701 |
| 4 | MagnetometerNoise | 1.1698 |
| 4 | PositionNoise | 1.1698 |
| 4 | QuaternionNoise | 1.1688 |
| 4 | VelocityNoise | 1.1688 |
| 5 | AccelerationNoise | 1.1650 |
| 5 | AccelerometerNoise | 1.1569 |
| 5 | AngularVelocityNoise | 1.1454 |
| 5 | GPSPositionNoise | 1.1100 |
| 5 | GPSVelocityNoise | 1.0778 |
| 5 | GyroscopeNoise | 1.0709 |
| 5 | MagnetometerNoise | 1.0675 |
| 5 | PositionNoise | 1.0675 |
| 5 | QuaternionNoise | 1.0669 |
| 5 | VelocityNoise | 1.0669 |
| 6 | AccelerationNoise | 1.0634 |
| 6 | AccelerometerNoise | 1.0549 |
| 6 | AngularVelocityNoise | 1.0549 |
| 6 | GPSPositionNoise | 1.0180 |
| 6 | GPSVelocityNoise | 0.9866 |
| 6 | GyroscopeNoise | 0.9810 |
| 6 | MagnetometerNoise | 0.9775 |
| 6 | PositionNoise | 0.9775 |
| 6 | QuaternionNoise | 0.9768 |
| 6 | VelocityNoise | 0.9768 |
| 7 | AccelerationNoise | 0.9735 |
| 7 | AccelerometerNoise | 0.9652 |
| 7 | AngularVelocityNoise | 0.9652 |
| 7 | GPSPositionNoise | 0.9283 |
| 7 | GPSVelocityNoise | 0.8997 |
| 7 | GyroscopeNoise | 0.8947 |
| 7 | MagnetometerNoise | 0.8920 |
| 7 | PositionNoise | 0.8920 |
| 7 | QuaternionNoise | 0.8912 |
| 7 | VelocityNoise | 0.8912 |
| 8 | AccelerationNoise | 0.8885 |
| 8 | AccelerometerNoise | 0.8811 |
| 8 | AngularVelocityNoise | 0.8807 |
| 8 | GPSPositionNoise | 0.8479 |
| 8 | GPSVelocityNoise | 0.8238 |
| 8 | GyroscopeNoise | 0.8165 |
| 8 | MagnetometerNoise | 0.8165 |
| 8 | PositionNoise | 0.8165 |
| 8 | QuaternionNoise | 0.8159 |
| 8 | VelocityNoise | 0.8159 |

Fuse the sensor data using the tuned filter.

```
dt = seconds(diff(groundTruth.Time));
N = size(sensorData,1);
qEst = quaternion.zeros(N,1);
posEst = zeros(N,3);
% Iterate the filter for prediction and correction using sensor data.
for ii=1:N
    if ii ~= 1
        predict(filter, dt(ii-1));
    end
```

```
    if all(~isnan(Accelerometer(ii,:)))
    fuseaccel(filter,Accelerometer(ii,:), ...
        tunedParams.AccelerometerNoise);
    end
    if all(~isnan(Gyroscope(ii,:)))
    fusegyro(filter, Gyroscope(ii,:), ...
        tunedParams.GyroscopeNoise);
    end
    if all(~isnan(Magnetometer(ii,1)))
    fusemag(filter, Magnetometer(ii,:), ...
        tunedParams.MagnetometerNoise);
    end
    if all(~isnan(GPSPosition(ii,1)))
        fusegps(filter, GPSPosition(ii,:), ...
            tunedParams.GPSPositionNoise, GPSVelocity(ii,:), ...
            tunedParams.GPSVelocityNoise);
    end
    [posEst(ii,:), qEst(ii,:)] = pose(filter);
end
Compute the RMS errors.
```

```
orientationError = rad2deg(dist(qEst, Orientation));
```

orientationError = rad2deg(dist(qEst, Orientation));
rmsorientationError = sqrt(mean(orientationError.^2))
rmsorientationError = 2.7801
positionError = sqrt(sum((posEst - Position).^2, 2));
rmspositionError = sqrt(mean( positionError.^2))
rmspositionError = 0.5966

```

Visualize the results.
```

figure();
t = (0:N-1)./ groundTruth.Properties.SampleRate;
subplot(2,1,1)
plot(t, positionError, 'b');
title("Tuned insfilterAsync" + newline + "Euclidean Distance Position Error")
xlabel('Time (s)');
ylabel('Position Error (meters)')
subplot(2,1,2)
plot(t, orientationError, 'b');
title("Orientation Error")
xlabel('Time (s)');
ylabel('Orientation Error (degrees)');

```


\section*{Input Arguments}

\section*{filter - Filter object}
infilterAsync object
Filter object, specified as an insfilterAsync object.

\section*{measureNoise - Measurement noise}
structure
Measurement noise, specified as a structure. The function uses the measurement noise input as the initial guess for tuning the measurement noise. The structure must contain these fields:
\begin{tabular}{|l|l|}
\hline Field name & Description \\
\hline AccelerometerNoise & \begin{tabular}{l} 
Variance of accelerometer noise, specified as a \\
scalar in \(\left(\mathrm{m}^{2} / \mathrm{s}\right)\)
\end{tabular} \\
\hline GyroscopeNoise & \begin{tabular}{l} 
Variance of gyroscope noise, specified as a scalar \\
in \((\mathrm{rad} / \mathrm{s})^{2}\)
\end{tabular} \\
\hline MagnetometerNoise & \begin{tabular}{l} 
Variance of magnetometer noise, specified as a \\
scalar in \((\mu \mathrm{T})^{2}\)
\end{tabular} \\
\hline GPSPositionNoise & \begin{tabular}{l} 
Variance of GPS position noise, specified as a \\
scalar in \(\mathrm{m}^{2}\)
\end{tabular} \\
\hline
\end{tabular}

Field name
GPSVelocityNoise

Description
Variance of GPS velocity noise, specified as a scalar in \((\mathrm{m} / \mathrm{s})^{2}\)

\section*{sensorData - Sensor data}
duration
Sensor data, specified as a timetable. In each row, the time and sensor data is specified as:
- Time - Time at which the data is obtained, specified as a scalar in seconds.
- Accelerometer - Accelerometer data, specified as a 1-by-3 vector of scalars in \(\mathrm{m}^{2} / \mathrm{s}\).
- Gyroscope - Gyroscope data, specified as a 1-by-3 vector of scalars in rad/s.
- Magnetometer - Magnetometer data, specified as a 1-by-3 vector of scalars in \(\mu \mathrm{T}\).
- GPSPosition - GPS position data, specified as a 1-by-3 vector of scalars in meters.
- GPSVelocity - GPS velocity data, specified as a 1-by-3 vector of scalars in m/s.

If a sensor does not produce measurements, specify the corresponding entry as NaN . If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the sensorData input based on your choice.

\section*{groundTruth - Ground truth data}

\section*{duration}

Ground truth data, specified as a timetable. In each row, the table can optionally contain any of these variables:
- Orientation - Orientation from the navigation frame to the body frame, specified as a quaternion or a 3-by-3 rotation matrix.
- AngularVelocity - Angular velocity in body frame, specified as a 1-by-3 vector of scalars in rad/s.
- Position - Position in navigation frame, specified as a 1-by-3 vector of scalars in meters.
- Velocity - Velocity in navigation frame, specified as a 1-by-3 vector of scalars in m/s.
- Acceleration - Acceleration in navigation frame, specified as a 1-by-3 vector of scalars in \(\mathrm{m}^{2} / \mathrm{s}\).
- AccelerometerBias - Accelerometer delta angle bias in body frame, specified as a 1-by-3 vector of scalars in \(\mathrm{m}^{2} / \mathrm{s}\).
- GyroscopeBias - Gyroscope delta angle bias in body frame, specified as a 1-by-3 vector of scalars in rad/s.
- GeomagneticFieldVector - Geomagnetic field vector in navigation frame, specified as a 1-by-3 vector of scalars.
- MagnetometerBias - Magnetometer bias in body frame, specified as a 1-by-3 vector of scalars in \(\mu \mathrm{T}\).

The function processes each row of the sensorData and groundTruth tables sequentially to calculate the state estimate and RMS error from the ground truth. State variables not present in groundTruth input are ignored for the comparison. The sensorData and the groundTruth tables must have the same time steps.

If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the groundTruth input based on your choice.

\section*{config - Tuner configuration}
tunerconfig object
Tuner configuration, specified as a tunerconfig object.

\section*{Output Arguments}

\section*{tunedMeasureNoise - Tuned measurement noise}
structure
Tuned measurement noise, returned as a structure. The structure contains these fields.
\begin{tabular}{|l|l|}
\hline Field name & Description \\
\hline AccelerometerNoise & \begin{tabular}{l} 
Variance of accelerometer noise, specified as a \\
scalar in \(\left(\mathrm{m}^{2} / \mathrm{s}\right)^{2}\)
\end{tabular} \\
\hline GyroscopeNoise & \begin{tabular}{l} 
Variance of gyroscope noise, specified as a scalar \\
in \((\mathrm{rad} / \mathrm{s})^{2}\)
\end{tabular} \\
\hline MagnetometerNoise & \begin{tabular}{l} 
Variance of magnetometer noise, specified as a \\
scalar in \((\mu \mathrm{T})^{2}\)
\end{tabular} \\
\hline GPSPositionNoise & \begin{tabular}{l} 
Variance of GPS position noise, specified as a \\
scalar in \(\mathrm{m}^{2}\)
\end{tabular} \\
\hline GPSVelocityNoise & \begin{tabular}{l} 
Variance of GPS velocity noise, specified as a \\
scalar in \((\mathrm{m} / \mathrm{s})^{2}\)
\end{tabular} \\
\hline
\end{tabular}

\section*{References}
[1] Abbeel, P., Coates, A., Montemerlo, M., Ng, A.Y. and Thrun, S. Discriminative Training of Kalman Filters. In Robotics: Science and systems, Vol. 2, pp. 1, 2005.

\section*{See Also}
tunerconfig|tunernoise

\section*{Introduced in R2020b}

\section*{binaryOccupancyMap}

Create occupancy grid with binary values

\section*{Description}

The binary0ccupancyMap creates a 2-D occupancy map object, which you can use to represent and visualize a robot workspace, including obstacles. The integration of sensor data and position estimates create a spatial representation of the approximate locations of the obstacles.

Occupancy grids are used in robotics algorithms such as path planning. They are also used in mapping applications, such as for finding collision-free paths, performing collision avoidance, and calculating localization. You can modify your occupancy grid to fit your specific application.

Each cell in the occupancy grid has a value representing the occupancy status of that cell. An occupied location is represented as true (1) and a free location is represented as false (0).

The object keeps track of three reference frames: world, local, and, grid. The world frame origin is defined by GridLocationInWorld, which defines the bottom-left corner of the map relative to the world frame. The LocalOriginInWorld property specifies the location of the origin of the local frame relative to the world frame. The first grid location with index \((1,1)\) begins in the top-left corner of the grid.

Note This object was previously named robotics.Binary0ccupancyGrid.

\section*{Creation}

\section*{Syntax}
```

map = binaryOccupancyMap
map = binary0ccupancyMap(width,height)
map = binary0ccupancyMap(width,height,resolution)
map = binary0ccupancyMap(rows,cols,resolution,"grid")
map = binary0ccupancyMap(p)
map = binary0ccupancyMap(p,resolution)
map = binaryOccupancyMap(sourcemap)
map = binaryOccupancyMap(sourcemap,resolution)

```

\section*{Description}
map = binary0ccupancyMap creates a 2-D binary occupancy grid with a width and height of 10 m . The default grid resolution is one cell per meter.
map = binary0ccupancyMap(width, height) creates a 2-D binary occupancy grid representing a work space of width and height in meters. The default grid resolution is one cell per meter.
map \(=\) binary0ccupancyMap(width, height, resolution) creates a grid with the Resolution property specified in cells per meter. The map is in world coordinates by default.
map \(=\) binary0ccupancyMap(rows, cols, resolution, "grid") creates a 2-D binary occupancy grid of size (rows,cols).
map \(=\) binary0ccupancyMap ( \(p\) ) creates a grid from the values in matrix \(p\). The size of the grid matches the size of the matrix, with each cell value interpreted from its location in the matrix. \(p\) contains any numeric or logical type with zeros (0) and ones (1).
map \(=\) binary0ccupancyMap( \(p\), resolution) creates a map from a matrix with the Resolution property specified in cells per meter.
map \(=\) binary0ccupancyMap(sourcemap) creates an object using values from another binary0ccupancyMap object.
map = binary0ccupancyMap(sourcemap, resolution) creates an object using values from another binary0ccupancyMap object, but resamples the matrix to have the specified resolution.

\section*{Input Arguments}

\section*{width - Map width}
positive scalar
Map width, specified as a positive scalar in meters.

\section*{height - Map height}
positive scalar
Map height, specified as a positive scalar in meters.

\section*{p - Map grid values}
matrix
Map grid values, specified as a matrix.

\section*{sourcemap - Occupancy map object}
binary0ccupancyMap object
Occupancy map object, specified as a binary0ccupancyMap object.

\section*{Properties}

\section*{GridSize - Number of rows and columns in grid}
two-element horizontal vector
This property is read-only.
Number of rows and columns in grid, stored as a two-element horizontal vector of the form [ rows cols].

\section*{Resolution - Grid resolution}

1 (default) | scalar in cells per meter
This property is read-only.

Grid resolution, stored as a scalar in cells per meter.
XLocalLimits - Minimum and maximum values of \(x\)-coordinates in local frame two-element vector

This property is read-only.
Minimum and maximum values of \(x\)-coordinates in local frame, stored as a two-element horizontal vector of the form [min max]. Local frame is defined by LocalOriginInWorld property.

YLocalLimits - Minimum and maximum values of \(\boldsymbol{y}\)-coordinates in local frame two-element vector

This property is read-only.
Minimum and maximum values of \(y\)-coordinates in local frame, stored as a two-element horizontal vector of the form [min max]. Local frame is defined by LocalOriginInWorld property.

XWorldLimits - Minimum and maximum values of \(\boldsymbol{x}\)-coordinates in world frame
two-element vector
This property is read-only.
Minimum and maximum values of \(x\)-coordinates in world frame, stored as a two-element horizontal vector of the form [min max]. These values indicate the world range of the \(x\)-coordinates in the grid.

\section*{YWorldLimits - Minimum and maximum values of \(\boldsymbol{y}\)-coordinates}
two-element vector
This property is read-only.
Minimum and maximum values of \(y\)-coordinates, stored as a two-element vector of the form [min \(\max ]\). These values indicate the world range of the \(y\)-coordinates in the grid.

GridLocationInWorld - Location of the grid in world coordinates
[0 0] (default) | two-element vector | [xGrid yGrid]
Location of the bottom-left corner of the grid in world coordinates, specified as a two-element vector, [xGrid yGrid].

\section*{LocalOriginInWorld - Location of the local frame in world coordinates}
[0 0] (default) | two-element vector | [xWorld yWorld]
Location of the origin of the local frame in world coordinates, specified as a two-element vector, [xLocal yLocal]. Use the move function to shift the local frame as your vehicle moves.

GridOriginInLocal - Location of the grid in local coordinates
[0 0] (default) | two-element vector | [xLocal yLocal]
Location of the bottom-left corner of the grid in local coordinates, specified as a two-element vector, [xLocal yLocal].

DefaultValue - Default value for unspecified map locations
0 (default) | 1
Default value for unspecified map locations including areas outside the map, specified as 0 or 1.

\section*{Object Functions}
\begin{tabular}{ll} 
checkOccupancy & Check occupancy values for locations \\
getOccupancy & Get occupancy value of locations \\
grid2local & Convert grid indices to local coordinates \\
grid2world & Convert grid indices to world coordinates \\
inflate & Inflate each occupied grid location \\
insertRay & Insert ray from laser scan observation \\
local2grid & Convert local coordinates to grid indices \\
local2world & Convert local coordinates to world coordinates \\
move & Move map in world frame \\
occupancyMatrix & Convert occupancy grid to matrix \\
raycast & Compute cell indices along a ray \\
rayIntersection & Find intersection points of rays and occupied map cells \\
setOccupancy & Set occupancy value of locations \\
show & Show occupancy grid values \\
syncWith & Sync map with overlapping map \\
world2grid & Convert world coordinates to grid indices \\
world2local & Convert world coordinates to local coordinates
\end{tabular}

\section*{Examples}

\section*{Create and Modify Binary Occupancy Grid}

Create a \(10 \mathrm{~m} \times 10 \mathrm{~m}\) empty map.
```

map = binaryOccupancyMap(10,10,10);

```

Set occupancy of world locations and show map.
```

x = [1.2; 2.3; 3.4; 4.5; 5.6];
y = [5.0; 4.0; 3.0; 2.0; 1.0];
set0ccupancy(map, [x y], ones(5,1))
figure
show(map)

```


Inflate occupied locations by a given radius.
inflate(map, 0.5)
figure
show (map)


Get grid locations from world locations.
ij = world2grid(map, [x y]);
Set grid locations to free locations.
```

setOccupancy(map, ij, zeros(5,1), 'grid')

```
figure
show(map)


\section*{Image to Binary Occupancy Grid Example}

This example shows how to convert an image to a binary occupancy grid for using with mapping and path planning.

Import image.
image = imread('imageMap.png');
Convert to grayscale and then black and white image based on given threshold value.
grayimage = rgb2gray(image);
bwimage = grayimage < 0.5;
Use black and white image as matrix input for binary occupancy grid.
grid = binary0ccupancyMap(bwimage);
show(grid)


\section*{Convert PGM Image to Map}

This example shows how to convert a .pgm file into a binaryOccupancyMap object for use in MATLAB.

Import image using imread. The image is quite large and should be cropped to the relevant area.
image = imread('playpen map.pgm');
imageCropped = image(750:1250,750:1250);
imshow(imageCropped)


Unknown areas (gray) should be removed and treated as free space. Create a logical matrix based on a threshold. Depending on your image, this value could be different. Occupied space should be set as 1 (white in image).
```

imageBW = imageCropped < 100;

```
imshow(imageBW)


Create binary0ccupancyMap object using adjusted map image.
map = binary0ccupancyMap(imageBW);
show(map)


\section*{Compatibility Considerations}
binary0ccupancyMap was renamed
Behavior change in future release
The binary0ccupancyMap object was renamed from robotics.BinaryOccupancyGrid. Use binary0ccupancyMap for all object creation.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

As of MATLAB R2022a, default map behavior during code generation has changed, which may result in backwards compatibility issues. Maps such as binary0ccupancyMap now support fixed-size code generation (DynamicMemoryAllocation="off").

1 Maps that are either default-constructed or constructed with compile-time constant size information (or matrices that are of compile-time constant size) produce fixed-size maps.
2 To restore the previous behavior, use the coder.ignoreConst function when specifying size inputs, or coder . varsize matrix variable name specified as a string scalar or character vector, prior to constructing the map.

\section*{See Also}
controllerPurePursuit

\section*{Topics}
"Occupancy Grids"

\section*{Introduced in R2015a}

\section*{checkOccupancy}

Check occupancy values for locations

\section*{Syntax}
```

occVal = checkOccupancy(map,xy)
occVal = checkOccupancy(map,xy,"local")
occVal = checkOccupancy(map,ij,"grid")
[occVal,validPts] = checkOccupancy(___)
occMatrix = checkOccupancy(map)
occMatrix = checkOccupancy(map,bottomLeft,matSize)
occMatrix = checkOccupancy(map,bottomLeft,matSize,"local")
occMatrix = checkOccupancy(map,topLeft,matSize,"grid")

```

\section*{Description}
occVal = checkOccupancy (map, xy) returns an array of occupancy values at the \(x y\) locations in the world frame. Obstacle-free cells return 0, occupied cells return 1. Unknown locations, including outside the map, return -1 .
occVal = check0ccupancy(map,xy,"local") returns an array of occupancy values at the xy locations in the local frame. The local frame is based on the LocalOriginInWorld property of the map.
occVal = checkOccupancy(map,ij,"grid") specifies ij grid cell indices instead of xy locations. Grid indices start at \((1,1)\) from the top left corner.
[occVal, validPts] = checkOccupancy (__ ) also outputs an n-element vector of logical values indicating whether input coordinates are within the map limits.
occMatrix \(=\) check0ccupancy (map) returns a matrix that contains the occupancy status of each location. Obstacle-free cells return 0 , occupied cells return 1 . Unknown locations, including outside the map, return - 1 .
occMatrix = checkOccupancy(map, bottomLeft,matSize) returns a matrix of occupancy values by specifying the bottom-left corner location in world coordinates and the matrix size in meters.
occMatrix = check0ccupancy(map,bottomLeft,matSize,"local") returns a matrix of occupancy values by specifying the bottom-left corner location in local coordinates and the matrix size in meters.
occMatrix = checkOccupancy(map,topLeft,matSize,"grid") returns a matrix of occupancy values by specifying the top-left cell index in grid coordinates and the matrix size.

\section*{Examples}

\section*{Get Occupancy Values and Check Occupancy Status}

Access occupancy values and check their occupancy status based on the occupied and free thresholds of the occupancyMap object.

Create a matrix and populate it with values. Use this matrix to create an occupancy map.
```

p = zeros(20,20);
p(11:20,11:20) = ones(10,10);
map = binary0ccupancyMap(p,10);
show(map)

```


Get the occupancy of different locations and check their occupancy statuses. The occupancy status returns 0 for free space and 1 for occupied space. Unknown values return -1 .
```

pocc = getOccupancy(map,[1.5 1]);
occupied = checkOccupancy(map,[1.5 1]);
pocc2 = getOccupancy(map,[5 5],'grid');

```

\section*{Input Arguments}
map - Map representation
binary0ccupancyMap object
Map representation, specified as a binary0ccupancyMap object.
xy - Coordinates in the map
n-by-2 matrix
Coordinates in the map, specified as an \(n\)-by- 2 matrix of \(\left[\begin{array}{ll}x & y\end{array}\right]\) pairs, where \(n\) is the number of coordinates. Coordinates can be world or local coordinates depending on the syntax.
Data Types: double
ij - Grid locations in the map
\(n\)-by-2 matrix
Grid locations in the map, specified as an \(n\)-by-2 matrix of [ \(i j\) ] pairs, where \(n\) is the number of locations. Grid locations are given as [row col].
Data Types: double
bottomLeft - Location of output matrix in world or local
two-element vector | [xCoord yCoord]
Location of bottom left corner of output matrix in world or local coordinates, specified as a twoelement vector, [xCoord yCoord]. Location is in world or local coordinates based on syntax.
Data Types: double
matSize - Output matrix size
two-element vector | [xLength yLength] |[gridRow gridCol]
Output matrix size, specified as a two-element vector, [xLength yLength], or [gridRow gridCol]. Size is in world, local, or grid coordinates based on syntax.

Data Types: double

\section*{topLeft - Location of grid}
two-element vector | [iCoord jCoord]
Location of top left corner of grid, specified as a two-element vector, [iCoord jCoord].
Data Types: double

\section*{Output Arguments}

\section*{occVal - Occupancy values}
n-by-1 column vector
Occupancy values, returned as an \(n\)-by- 1 column vector equal in length to xy or ij input. Occupancy values can be obstacle free (0), occupied (1), or unknown ( -1 ).

\section*{validPts - Valid map locations}
\(n\)-by-1 column vector
Valid map locations, returned as an \(n\)-by- 1 column vector equal in length to xy or ij. Locations inside the map return a value of 1 . Locations outside the map limits return a value of 0 .

\section*{occMatrix - Matrix of occupancy values}
matrix

Matrix of occupancy values, returned as matrix with size equal to matSize or the size of your map. Occupancy values can be obstacle free (0), occupied (1), or unknown (-1).

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}
binary0ccupancyMap | getOccupancy | occupancyMap

Introduced in R2019b

\section*{getOccupancy}

Get occupancy value of locations

\section*{Syntax}
```

occVal = getOccupancy(map,xy)
occVal = getOccupancy(map,xy,"local")
occVal = get0ccupancy(map,ij,"grid")
[occVal,validPts] = getOccupancy(

```
\(\qquad\)
```

occMatrix = get0ccupancy(map)
occMatrix = get0ccupancy(map,bottomLeft,matSize)
occMatrix = getOccupancy(map,bottomLeft,matSize,"local")
occMatrix = getOccupancy(map,topLeft,matSize,"grid")

```

\section*{Description}
occVal = getOccupancy (map, xy) returns an array of occupancy values at the \(x y\) locations in the world frame. Unknown locations, including outside the map, return map. DefaultValue.
occVal = getOccupancy(map,xy,"local") returns an array of occupancy values at the \(x y\) locations in the local frame.
occVal = getOccupancy(map,ij, "grid") specifies ij grid cell indices instead of xy locations.
[occVal,validPts] = getOccupancy( \(\qquad\) ) additionally outputs an \(n\)-element vector of logical values indicating whether input coordinates are within the map limits.
occMatrix = get0ccupancy(map) returns all occupancy values in the map as a matrix.
occMatrix = getOccupancy(map, bottomLeft, matSize) returns a matrix of occupancy values by specifying the bottom-left corner location in world coordinates and the matrix size in meters.
occMatrix = get0ccupancy(map,bottomLeft,matSize,"local") returns a matrix of occupancy values by specifying the bottom-left corner location in local coordinates and the matrix size in meters.
occMatrix = get0ccupancy(map,topLeft,matSize,"grid") returns a matrix of occupancy values by specifying the top-left cell index in grid indices and the matrix size.

\section*{Examples}

\section*{Insert Laser Scans into Binary Occupancy Map}

Create an empty binary occupancy grid map.
map = binary0ccupancyMap(10,10,20);
Input pose of the vehicle, ranges, angles, and the maximum range of the laser scan.
```

pose = [5,5,0];
ranges = 3*ones(100,1);
angles = linspace(-pi/2,pi/2,100);
maxrange = 20;

```

Create a lidarScan object with the specified ranges and angles.
scan \(=\) lidarScan(ranges,angles);
Insert the laser scan data into the occupancy map.
insertRay(map, pose,scan,maxrange);
Show the map to see the results of inserting the laser scan.
show (map)

Binary Occupancy Grid


Check the occupancy of the spot directly in front of the vehicle.
```

getOccupancy(map,[8 5])
ans = logical
1

```

\section*{Get Occupancy Values and Check Occupancy Status}

Access occupancy values and check their occupancy status based on the occupied and free thresholds of the occupancyMap object.

Create a matrix and populate it with values. Use this matrix to create an occupancy map.
```

p = zeros(20,20);
p(11:20,11:20) = ones(10,10);
map = binary0ccupancyMap(p,10);
show(map)

```


Get the occupancy of different locations and check their occupancy statuses. The occupancy status returns 0 for free space and 1 for occupied space. Unknown values return -1 .
```

pocc = getOccupancy(map,[1.5 1]);
occupied = checkOccupancy(map,[1.5 1]);
pocc2 = getOccupancy(map,[5 5],'grid');

```

\section*{Input Arguments}

\section*{map - Map representation}
binary0ccupancyMap object
Map representation, specified as a binary0ccupancyMap object. This object represents the environment of the vehicle.
xy - Coordinates in the map
n-by-2 matrix
Coordinates in the map, specified as an \(n\)-by- 2 matrix of \(\left[\begin{array}{ll}x & y\end{array}\right]\) pairs, where \(n\) is the number of coordinates. Coordinates can be world or local coordinates depending on the syntax.
Data Types: double
ij - Grid locations in the map
\(n\)-by-2 matrix
Grid locations in the map, specified as an \(n\)-by-2 matrix of [ \(i j\) ] pairs, where \(n\) is the number of locations. Grid locations are given as [row col].

Data Types: double
bottomLeft - Location of output matrix in world or local
two-element vector | [xCoord yCoord]
Location of bottom left corner of output matrix in world or local coordinates, specified as a twoelement vector, [xCoord yCoord]. Location is in world or local coordinates based on syntax.
Data Types: double
matSize - Output matrix size
two-element vector|[xLength yLength]|[gridRow gridCol]
Output matrix size, specified as a two-element vector, [xLength yLength] or [gridRow gridCol]. The size is in world coordinates, local coordinates, or grid indices based on syntax.
Data Types: double
topLeft - Location of grid
two-element vector | [iCoord jCoord]
Location of top left corner of grid, specified as a two-element vector, [iCoord jCoord].
Data Types: double

\section*{Output Arguments}

\section*{occVal - Occupancy values}
n-by-1 column vector
Occupancy values, returned as an \(n\)-by- 1 column vector equal in length to xy or ij . Occupancy values can be obstacle free (0) or occupied (1).

\section*{validPts - Valid map locations}
\(n\)-by-1 column vector
Valid map locations, returned as an \(n\)-by- 1 column vector equal in length to xy or ij. Locations inside the map return a value of 1 . Locations outside the map limits return a value of 0 .

\section*{occMatrix - Matrix of occupancy values}
matrix
Matrix of occupancy values, returned as matrix with size equal to matSize or the size of map.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).

\section*{See Also}
binary0ccupancyMap | set0ccupancy
Topics
"Occupancy Grids"

Introduced in R2015a

\section*{grid2local}

Convert grid indices to local coordinates

\section*{Syntax}
\(x y=\) grid2local(map,ij)

\section*{Description}
\(\mathrm{xy}=\mathrm{grid} 2 l o c a l(m a p, i j)\) converts a [row col] array of grid indices, ij , to an array of local coordinates, \(x y\).

\section*{Input Arguments}

\section*{map - Map representation}
binary0ccupancyMap object
Map representation, specified as a binary0ccupancyMap object. This object represents the environment of the robot. The object contains a matrix grid with binary values indicating obstacles as true (1) and free locations as false (0).

\section*{ij - Grid positions \\ \(n\)-by-2 vertical array}

Grid positions, specified as an \(n\)-by-2 vertical array of [i \(j\) ] pairs in [rows cols] format, where \(n\) is the number of grid positions.

\section*{Output Arguments}

\section*{xy - Local coordinates}
\(n\)-by-2 vertical array
Local coordinates, specified as an \(n\)-by-2 vertical array of [ \(x\) y] pairs, where \(n\) is the number of local coordinates.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}
binaryOccupancyMap | world2grid
Introduced in R2019b

\section*{grid2world}

Convert grid indices to world coordinates

\section*{Syntax}
xy = grid2world(map,ij)

\section*{Description}
xy = grid2world(map,ij) converts a [row col] array of grid indices, ij , to an array of world coordinates, \(x y\).

\section*{Input Arguments}

\section*{map - Map representation}
binary0ccupancyMap object
Map representation, specified as a binary0ccupancyMap object. This object represents the environment of the robot. The object contains a matrix grid with binary values indicating obstacles as true (1) and free locations as false (0).

\section*{ij - Grid positions \\ \(n\)-by-2 vertical array}

Grid positions, specified as an \(n\)-by-2 vertical array of [i \(j\) ] pairs in [rows cols] format, where \(n\) is the number of grid positions.

\section*{Output Arguments}
xy - World coordinates
\(n\)-by-2 vertical array
World coordinates, specified as an \(n\)-by-2 vertical array of [ \(x y\) ] pairs, where \(n\) is the number of world coordinates.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}
binary0ccupancyMap | world2grid | grid2local
Introduced in R2015a

\section*{inflate}

Inflate each occupied grid location

\section*{Syntax}
```

inflate(map,radius)
inflate(map,gridradius,'grid')

```

\section*{Description}
inflate(map,radius) inflates each occupied position of the map by the radius given in meters. radius is rounded up to the nearest cell equivalent based on the resolution of the map. Every cell within the radius is set to true (1).
inflate(map,gridradius,'grid') inflates each occupied position by the radius given in number of cells.

\section*{Examples}

\section*{Create and Modify Binary Occupancy Grid}

Create a \(10 \mathrm{~m} \times 10 \mathrm{~m}\) empty map.
```

map = binary0ccupancyMap(10,10,10);

```

Set occupancy of world locations and show map.
```

x = [1.2; 2.3; 3.4; 4.5; 5.6];
y = [5.0; 4.0; 3.0; 2.0; 1.0];
setOccupancy(map, [x y], ones(5,1))
figure
show(map)

```


Inflate occupied locations by a given radius.
inflate(map, 0.5)
figure
show (map)


Get grid locations from world locations.
ij = world2grid(map, [x y]);
Set grid locations to free locations.
```

setOccupancy(map, ij, zeros(5,1), 'grid')

```
figure
show(map)


\section*{Input Arguments}

\section*{map - Map representation}
binaryOccupancyMap object
Map representation, specified as a binary0ccupancyMap object. This object represents the environment of the robot. The object contains a matrix grid with binary values indicating obstacles as true (1) and free locations as false (0).

\section*{radius - Dimension the defines how much to inflate occupied locations}
scalar
Dimension that defines how much to inflate occupied locations, specified as a scalar. radius is rounded up to the nearest cell value.

Data Types: double
gridradius - Dimension the defines how much to inflate occupied locations
positive scalar
Dimension that defines how much to inflate occupied locations, specified as a positive scalar. gridradius is the number of cells to inflate the occupied locations.
Data Types: double

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).

\section*{See Also}
binary0ccupancyMap | set0ccupancy
Topics
"Occupancy Grids"

Introduced in R2015a

\section*{insertRay}

Insert ray from laser scan observation

\section*{Syntax}
```

insertRay(map,pose,scan,maxrange)
insertRay(map, pose,ranges,angles,maxrange)
insertRay(map,startpt,endpoints)

```

\section*{Description}
insertRay (map, pose, scan, maxrange) inserts one or more lidar scan sensor observations in the occupancy grid, map, using the input lidarScan object, scan, to get ray endpoints. End point locations are updated with an occupied value. If the ranges are above maxrange, the ray endpoints are considered free space. All other points along the ray are treated as obstacle-free.
insertRay (map, pose, ranges, angles, maxrange) specifies the range readings as vectors defined by the input ranges and angles.
insertRay (map, startpt, endpoints) inserts observations between the line segments from the start point to the end points. The endpoints are updated are occupied space and other points along the line segments are updated as free space.

\section*{Examples}

\section*{Insert Laser Scans into Binary Occupancy Map}

Create an empty binary occupancy grid map.
```

map = binaryOccupancyMap(10,10,20);

```

Input pose of the vehicle, ranges, angles, and the maximum range of the laser scan.
```

pose = [5,5,0];
ranges = 3*ones(100,1);
angles = linspace(-pi/2,pi/2,100);
maxrange = 20;

```

Create a lidarScan object with the specified ranges and angles.
```

scan = lidarScan(ranges,angles);

```

Insert the laser scan data into the occupancy map.
```

insertRay(map,pose,scan,maxrange);

```

Show the map to see the results of inserting the laser scan.
```

show(map)

```


Check the occupancy of the spot directly in front of the vehicle.
```

get0ccupancy(map,[8 5])

```
ans = logical
    1

\section*{Input Arguments}
map - Map representation
binary0ccupancyMap object
Map representation, specified as a binary0ccupancyMap object. This object represents the environment of the robot. The object contains a matrix grid with binary values indicating obstacles as true (1) and free locations as false (0).

\section*{pose - Position and orientation of vehicle}
three-element vector
Position and orientation of vehicle, specified as an [x y theta] vector. The vehicle pose is an \(x\) and \(y\) position with angular orientation theta (in radians) measured from the \(x\)-axis.

\section*{scan - Lidar scan readings}
lidarScan object

Lidar scan readings, specified as a lidarScan object.

\section*{ranges - Range values from scan data}
vector
Range values from scan data, specified as a vector of elements measured in meters. These range values are distances from a sensor at given angles. The vector must be the same length as the corresponding angles vector.

\section*{angles - Angle values from scan data}
vector
Angle values from scan data, specified as a vector of elements measured in radians. These angle values correspond to the given ranges. The vector must be the same length as the corresponding ranges vector.

\section*{maxrange - Maximum range of sensor}
scalar
Maximum range of laser range sensor, specified as a scalar in meters. Range values greater than or equal to maxrange are considered free along the whole length of the ray, up to maxrange.

\section*{startpt - Start point for rays}
two-element vector
Start point for rays, specified as a two-element vector, \([x y\) ], in the world coordinate frame. All rays are line segments that originate at this point.

\section*{endpoints - Endpoints for rays}
\(n\)-by-2 matrix
Endpoints for rays, specified as an \(n\)-by-2 matrix of \([x y]\) pairs in the world coordinate frame, where \(n\) is the length of ranges or angles. All rays are line segments that originate at startpt.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}
occupancyMap | binary0ccupancyMap | lidarScan | lidarScan

\section*{Topics}
"Occupancy Grids" (Robotics System Toolbox)

\section*{Introduced in R2019b}

\section*{local2grid}

Convert local coordinates to grid indices

\section*{Syntax}
ij \(=\) local2grid(map, \(x y\) )

\section*{Description}
ij = local2grid(map, \(x y\) ) converts an array of local coordinates, \(x y\), to an array of grid indices, ij in [row col] format.

\section*{Input Arguments}

\section*{map - Map representation}
binaryOccupancyMap object
Map representation, specified as a binary0ccupancyMap object. This object represents the environment of the vehicle.
xy - Local coordinates
\(n\)-by-2 matrix
Local coordinates, specified as an \(n\)-by-2 matrix of \([x y]\) pairs, where \(n\) is the number of local coordinates.

Data Types: double

\section*{Output Arguments}

\section*{ij - Grid positions}
\(n\)-by-2 matrix
Grid positions, returned as an \(n\)-by-2 matrix of [i j] pairs in [row col] format, where \(n\) is the number of grid positions. The grid cell locations are counted from the top left corner of the grid.
Data Types: double

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).

\section*{See Also}
binary0ccupancyMap | occupancyMap | grid2world | grid2world

\section*{Topics}
"Occupancy Grids"

Introduced in R2019b

\section*{local2world}

Convert local coordinates to world coordinates

\section*{Syntax}
xyWorld \(=\) local2world(map,xy)

\section*{Description}
xyWorld \(=\) local2world(map,xy) converts an array of local coordinates to world coordinates.

\section*{Input Arguments}
map - Map representation
binaryOccupancyMap object
Map representation, specified as a binary0ccupancyMap object. This object represents the environment of the vehicle.
xy - Local coordinates
\(n\)-by-2 matrix
Local coordinates, specified as an \(n\)-by-2 matrix of \([x y]\) pairs, where \(n\) is the number of local coordinates.

Data Types: double

\section*{Output Arguments}
xyWorld - World coordinates
\(n\)-by-2 matrix
World coordinates, specified as an \(n\)-by-2 matrix of [ \(x y\) ] pairs, where \(n\) is the number of world coordinates.

Data Types: double

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{Tm}}\).

\section*{See Also}

Topics
"Occupancy Grids"
Introduced in R2019b

\section*{move}

Move map in world frame

\section*{Syntax}
move(map, moveValue)
move(map, moveValue, Name, Value)

\section*{Description}
move(map, moveValue) moves the local origin of the map to an absolute location, moveValue, in the world frame, and updates the map limits. Move values are truncated based on the resolution of the map. By default, newly revealed regions are set to map. DefaultValue.
move (map, moveValue, Name, Value) specifies additional options specified by one or more namevalue pair arguments.

\section*{Examples}

\section*{Move Local Map and Sync with World Map}

This example shows how to move a local egocentric map and sync it with a larger world map. This process emulates a vehicle driving in an environment and getting updates on obstacles in the new areas.

Load example maps. Create a binary occupancy map from the complexMap.
```

load exampleMaps.mat
map = binary0ccupancyMap(complexMap);
show(map)

```


Create a smaller local map.
mapLocal = binary0ccupancyMap(complexMap(end-20:end,1:20)); show(mapLocal)


Follow a path planned in the world map and update the local map as you move your local frame. Specify path locations and plot on the map.
```

path = [5 2
82
8 8
30 8];
show(map)
hold on
plot(path(:,1),path(:,2))
hold off

```

Binary Occupancy Grid


Create a loop for moving between points by the map resolution. Divide the difference between points by the map resolution to see how many incremental moves you can make.
```

for i = 1:length(path)-1
moveAmount = (path(i+1,:)-path(i,:))/map.Resolution;
for j = 1:abs(moveAmount(1)+moveAmount(2))
moveValue = sign(moveAmount).*map.Resolution;
move(mapLocal,moveValue, ...
"MoveType", "relative", "SyncWith", map)
show(mapLocal)
drawnow limitrate
pause(0.2)
end
end

```


\section*{Input Arguments}

\section*{map - Map representation}
binary0ccupancyMap object
Map representation, specified as a binary0ccupancyMap object. This object represents the environment of the vehicle.

\section*{moveValue - Local map origin move value}
[ \(\mathrm{x} y\) ] vector
Local map origin move value, specified as an [ \(\mathrm{x} y\) ] vector. By default, the value is an absolute location to move the local origin to in the world frame. Use the MoveType name-value pair to specify a relative move.

\section*{Name-Value Pair Arguments}

Specify optional pairs of arguments as Namel=Value1, ...,NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: 'MoveType','relative'

\section*{MoveType - Type of move}
'absolute' (default)|'relative'
Type of move, specified as 'absolute' or 'relative'. For relative moves, specify a relative [x y] vector for moveValue based on your current local frame.

FillValue - Fill value for revealed locations
0 (default) | 1
Fill value for revealed locations because of the shifted map limits, specified as 0 or 1 .
SyncWith - Secondary map to sync with
binaryOccupancyMap object
Secondary map to sync with, specified as a binary0ccupancyMap object. Any revealed locations based on the move are updated with values in this map using the world coordinates.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).

\section*{See Also}
binary0ccupancyMap | occupancyMap | occupancyMatrix
Introduced in R2019b

\section*{occupancyMatrix}

Convert occupancy grid to matrix

\section*{Syntax}
mat = occupancyMatrix(map)

\section*{Description}
mat = occupancyMatrix(map) returns occupancy values stored in the occupancy grid object as a matrix.

\section*{Input Arguments}
map - Map representation
binary0ccupancyMap object
Map representation, specified as a binary0ccupancyMap object. This object represents the environment of the robot. The object contains a matrix grid with binary values indicating obstacles as true (1) and free locations as false (0).

\section*{Output Arguments}
mat - Occupancy values
matrix
Occupancy values, returned as an \(h\)-by- \(w\) matrix, where \(h\) and \(w\) are defined by the two elements of the GridSize property of the occupancy grid object.
Data Types: double

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and C++ code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}
binaryOccupancyMap | occupancyMap
Topics
"Occupancy Grids"
Introduced in R2016b

\section*{raycast}

Compute cell indices along a ray

\section*{Syntax}
[endpoints,midpoints] = raycast(map,pose,range,angle)
[endpoints,midpoints] = raycast(map,p1,p2)

\section*{Description}
[endpoints,midpoints] = raycast(map, pose, range, angle) returns cell indices of the specified map for all cells traversed by a ray originating from the specified pose at the specified angle and range values. endpoints contains all indices touched by the end of the ray, with all other points included in midpoints.
[endpoints,midpoints] = raycast(map, p1, p2) returns the cell indices of the line segment between the two specified points.

\section*{Input Arguments}

\section*{map - Map representation}
binaryOccupancyMap object
Map representation, specified as a binary0ccupancyMap object. This object represents the environment of the robot. The object contains a matrix grid with binary values indicating obstacles as true (1) and free locations as false (0).

\section*{pose - Position and orientation of sensor}
three-element vector
Position and orientation of sensor, specified as an [x y theta] vector. The sensor pose is an \(x\) and \(y\) position with angular orientation theta (in radians) measured from the \(x\)-axis.

\section*{range - Range of ray}
scalar
Range of ray, specified as a scalar in meters.

\section*{angle - Angle of ray}
scalar
Angle of ray, specified as a scalar in radians. The angle value is for the corresponding range.

\section*{p1 - Starting point of ray}
two-element vector
Starting point of ray, specified as an \(\left[\begin{array}{ll}x & y\end{array}\right]\) two-element vector. Points are defined with respect to the world-frame.

\section*{p2 - Endpoint of ray}
two-element vector

Endpoint of ray, specified as an \(\left[\begin{array}{ll}x & y\end{array}\right]\) two-element vector. Points are defined with respect to the world-frame.

\section*{Output Arguments}

\section*{endpoints - Endpoint grid indices \\ \(n\)-by-2 matrix}

Endpoint indices, returned as an \(n\)-by-2 matrix of [ \(i \quad j\) ] pairs, where \(n\) is the number of grid indices. The endpoints are where the range value hits at the specified angle. Multiple indices are returned when the endpoint lies on the boundary of multiple cells.

\section*{midpoints - Midpoint grid indices}
n-by-2 matrix
Midpoint indices, returned as an \(n\)-by- 2 matrix of \(\left[\begin{array}{ll}i & j\end{array}\right]\) pairs, where \(n\) is the number of grid indices. This argument includes all grid indices the ray intersects, excluding the endpoint.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and \(\mathrm{C}++\) code using MATLAB® \(\operatorname{Coder}^{\text {™ }}\).

\section*{See Also}
binary0ccupancyMap|insertRay|occupancyMap

\section*{Topics}
"Occupancy Grids" (Robotics System Toolbox)
"Occupancy Grids"

Introduced in R2019b

\section*{rayIntersection}

Find intersection points of rays and occupied map cells

\section*{Syntax}
```

intersectionPts = rayIntersection(map,pose,angles,maxrange)

```

\section*{Description}
intersectionPts = rayIntersection(map, pose, angles, maxrange) returns intersection points of rays and occupied cells in the specified map. Rays emanate from the specified pose and angles. Intersection points are returned in the world coordinate frame. If there is no intersection up to the specified maxrange, [ NaN NaN ] is returned.

\section*{Examples}

\section*{Get Ray Intersection Points on Occupancy Map}

Create a binary occupancy grid map. Add obstacles and inflate them. A lower resolution map is used to illustrate the importance of the size of your grid cells. Show the map.
```

map = binary0ccupancyMap(10,10,2);
obstacles = [4 10; 3 5; 7 7];
set0ccupancy(map,obstacles,ones(length(obstacles),1))
inflate(map,0.25)
show(map)

```

Binary Occupancy Grid


Find the intersection points of occupied cells and rays that emit from the given vehicle pose. Specify the max range and angles for these rays. The last ray does not intersect with an obstacle within the max range, so it has no collision point.
```

maxrange = 6;
angles = [pi/4,-pi/4,0,-pi/8];
vehiclePose = [4,4,pi/2];
intsectionPts = rayIntersection(map,vehiclePose,angles,maxrange)
intsectionPts = 4×2
3.5000 4.5000
6.0000 6.0000
4.0000 9.0000
NaN NaN

```

Plot the intersection points and rays from the pose.
```

hold on
plot(intsectionPts(:,1),intsectionPts(:,2),'*r') % Intersection points
plot(vehiclePose(1),vehiclePose(2),'ob') % Vehicle pose
for i = 1:3
plot([vehiclePose(1),intsectionPts(i,1)],...
[vehiclePose(2),intsectionPts(i,2)],'-b') % Plot intersecting rays
end
plot([vehiclePose(1),vehiclePose(1)-6*sin(angles(4))],...
[vehiclePose(2),vehiclePose(2)+6*cos(angles(4))],'-b') % No intersection ray

```


\section*{Input Arguments}

\section*{map - Map representation}
binaryOccupancyMap object
Map representation, specified as a binary0ccupancyMap object. This object represents the environment of the robot. The object contains a matrix grid with binary values indicating obstacles as true (1) and free locations as false (0).

\section*{pose - Position and orientation of sensor}
three-element vector
Position and orientation of the sensor, specified as an [x y theta] vector. The sensor pose is an \(x\) and \(y\) position with angular orientation theta (in radians) measured from the \(x\)-axis.

\section*{angles - Ray angles emanating from sensor}
vector
Ray angles emanating from the sensor, specified as a vector with elements in radians. These angles are relative to the specified sensor pose.

\section*{maxrange - Maximum range of sensor}
scalar

Maximum range of laser range sensor, specified as a scalar in meters. Range values greater than or equal to maxrange are considered free along the whole length of the ray, up to maxrange.

\section*{Output Arguments}

\section*{intersectionPts - Intersection points \\ n-by-2 matrix}

Intersection points, returned as \(n\)-by-2 matrix of \([x y]\) pairs in the world coordinate frame, where \(n\) is the length of angles.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}
binary0ccupancyMap | occupancyMap
Topics
"Occupancy Grids" (Robotics System Toolbox)
"Occupancy Grids" (Robotics System Toolbox)
Introduced in R2019b

\section*{setOccupancy}

Set occupancy value of locations

\section*{Syntax}
```

set0ccupancy(map,xy,occval)
setOccupancy(map,xy,occval,"local")
set0ccupancy(map,ij,occval,"grid")
validPts = setOccupancy(

```
\(\qquad\)
```

setOccupancy(map,bottomLeft,inputMatrix)
set0ccupancy(map,bottomLeft,inputMatrix,"local")
setOccupancy(map,topLeft,inputMatrix,"grid")

```

\section*{Description}
setOccupancy (map, xy, occval) assigns occupancy values, occval, to the input array of world coordinates, \(x y\) in the occupancy grid, map. Each row of the array, \(x y\), is a point in the world and is represented as an [ \(x y\) ] coordinate pair. occval is either a scalar or a single column array of the same length as \(x y\). An occupied location is represented as true (1), and a free location is represented as false (0).
setOccupancy (map, xy, occval, "local") assigns occupancy values, occval, to the input array of local coordinates, \(x y\), as local coordinates.
setOccupancy(map,ij, occval,"grid") assigns occupancy values, occval, to the input array of grid indices, ij, as [rows cols].
validPts = setOccupancy( \(\qquad\) ) outputs an \(n\)-element vector of logical values indicating whether input coordinates are within the map limits.
set0ccupancy (map, bottomLeft,inputMatrix) assigns a matrix of occupancy values by specifying the bottom-left corner location in world coordinates.
setOccupancy(map, bottomLeft,inputMatrix, "local") assigns a matrix of occupancy values by specifying the bottom-left corner location in local coordinates.
set0ccupancy(map,topLeft,inputMatrix, "grid") assigns a matrix of occupancy values by specifying the top-left cell index in grid indices and the matrix size.

\section*{Examples}

\section*{Create and Modify Binary Occupancy Grid}

Create a \(10 \mathrm{~m} \times 10 \mathrm{~m}\) empty map.
```

map = binaryOccupancyMap(10,10,10);

```

Set occupancy of world locations and show map.
\(x=[1.2 ; 2.3 ; 3.4 ; 4.5 ; 5.6]\);
\(y=[5.0 ; 4.0 ; 3.0 ; 2.0 ; 1.0] ;\)
set0ccupancy(map, [x y], ones \((5,1)\) )
figure
show (map)


Inflate occupied locations by a given radius.
inflate(map, 0.5)
figure
show(map)


Get grid locations from world locations.
ij = world2grid(map, [x y]);
Set grid locations to free locations.
```

setOccupancy(map, ij, zeros(5,1), 'grid')

```
figure
show(map)


\section*{Input Arguments}

\section*{map - Map representation}
binary0ccupancyMap object
Map representation, specified as a binary0ccupancyMap object. This object represents the environment of the robot. The object contains a matrix grid with binary values indicating obstacles as true (1) and free locations as false (0).

\section*{xy - World coordinates}
n-by-2 vertical array
World coordinates, specified as an \(n\)-by-2 vertical array of [ \(x y\) ] pairs, where \(n\) is the number of world coordinates.

Data Types: double
ij - Grid positions
n-by-2 vertical array
Grid positions, specified as an \(n\)-by-2 vertical array of [i j] pairs in [rows cols] format, where \(n\) is the number of grid positions.
Data Types: double

\section*{occval - Occupancy values}
\(n\)-by-1 vertical array
Occupancy values of the same length as either xy or ij , returned as an \(n\)-by- 1 vertical array, where \(n\) is the same \(n\) in either xy or ij . Values are given between 0 and 1 inclusively.

\section*{inputMatrix - Occupancy values \\ matrix}

Occupancy values, specified as a matrix. Values are given between 0 and 1 inclusively.

\section*{bottomLeft - Location of output matrix in world or local}
two-element vector | [xCoord yCoord]
Location of bottom left corner of output matrix in world or local coordinates, specified as a twoelement vector, [xCoord yCoord]. Location is in world or local coordinates based on syntax.

Data Types: double

\section*{topLeft - Location of grid}
two-element vector | [iCoord jCoord]
Location of top left corner of grid, specified as a two-element vector, [iCoord jCoord].
Data Types: double

\section*{Output Arguments}

\section*{validPts - Valid map locations}
\(n\)-by-1 column vector
Valid map locations, returned as an \(n\)-by- 1 column vector equal in length to xy or ij . Locations inside the map return a value of 1 . Locations outside the map limits return a value of 0 .

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{Tm}}\).

\section*{See Also}
binary0ccupancyMap | get0ccupancy | occupancyMap

\section*{Introduced in R2015a}

\section*{show}

Show occupancy grid values

\section*{Syntax}
show (map)
show(map, "local")
show(map, "grid")
show (__ , Name, Value)
mapImage \(=\) show (___)

\section*{Description}
show(map) displays the binary occupancy grid map in the current axes, with the axes labels representing the world coordinates.
show(map, "local") displays the binary occupancy grid map in the current axes, with the axes labels representing the local coordinates instead of world coordinates.
show(map, "grid") displays the binary occupancy grid map in the current axes, with the axes labels representing the grid coordinates.
show (__ , Name, Value) specifies additional options specified by one or more name-value pair arguments.
mapImage \(=\) show( \(\qquad\) ) returns the handle to the image object created by show.

\section*{Examples}

\section*{Move Local Map and Sync with World Map}

This example shows how to move a local egocentric map and sync it with a larger world map. This process emulates a vehicle driving in an environment and getting updates on obstacles in the new areas.

Load example maps. Create a binary occupancy map from the complexMap.
```

load exampleMaps.mat
map = binary0ccupancyMap(complexMap);
show(map)

```


Create a smaller local map.
mapLocal = binary0ccupancyMap(complexMap(end-20:end,1:20)); show(mapLocal)


Follow a path planned in the world map and update the local map as you move your local frame. Specify path locations and plot on the map.
```

path = [5 2
8
8
30 8];
show(map)
hold on
plot(path(:,1),path(:,2))
hold off

```

Binary Occupancy Grid


Create a loop for moving between points by the map resolution. Divide the difference between points by the map resolution to see how many incremental moves you can make.
```

for i = 1:length(path)-1
moveAmount = (path(i+1,:)-path(i,:))/map.Resolution;
for j = 1:abs(moveAmount(1)+moveAmount(2))
moveValue = sign(moveAmount).*map.Resolution;
move(mapLocal,moveValue, ...
"MoveType", "relative", "SyncWith", map)
show(mapLocal)
drawnow limitrate
pause(0.2)
end
end

```


\section*{Input Arguments}

\section*{map - Map representation}
binary0ccupancyMap object
Map representation, specified as a binary0ccupancyMap object. This object represents the environment of the vehicle.

\section*{Name-Value Pair Arguments}

Specify optional pairs of arguments as Namel=Value1, ... , NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: 'Parent', axHandle

\section*{Parent - Axes to plot the map}

Axes object | UIAxes object
Axes to plot the map specified as either an Axes or UIAxesobject. See axes or uiaxes.

\section*{FastUpdate - Update existing map plot}

0 (default) | 1

Update existing map plot, specified as 0 or 1. If you previously plotted your map on your figure, set to 1 for a faster update to the figure. This is useful for updating the figure in a loop for fast animations.

\author{
See Also \\ binary0ccupancyMap | occupancyMap \\ Introduced in R2015a
}

\section*{syncWith}

Sync map with overlapping map

\section*{Syntax}
```

mat = syncWith(map,sourcemap)

```

\section*{Description}
mat = syncWith(map, sourcemap) updates map with data from another binaryOccupancyMap object, sourcemap. Locations in map that are also found in sourcemap are updated. All other cells in map are set to map. DefaultValue.

\section*{Examples}

\section*{Sync Map With an Overlapping Map}

This example shows how to sync two overlapping maps using the syncWith function.
2-D occupancy maps are used to represent and visualize robot workspaces. In this example 2-D occupancy maps are created using existing map grid values stored inside exampleMaps.mat.
```

load('exampleMaps.mat');

```

Create and display a new empty 2-D occupancy map object using binary0ccupancyMap function.
map1 = binary0ccupancyMap (70,70);
show(map1)
title('New Map')


Create and display 2-D occupancy map using the map grid values stored in complexMap.
map2 = binary0ccupancyMap(complexMap); show(map2)
title('Complex Map')


Now update map1 with map2 using the syncWith function.
syncWith(map1,map2);
show(map1)


\section*{Input Arguments}
map - Map representation
binary0ccupancyMap object
Map representation, specified as a binary0ccupancyMap object.
sourcemap - Map representation
binary0ccupancyMap object
Map representation, specified as a binary0ccupancyMap object.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and C++ code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}
binary0ccupancyMap | occupancyMap

\section*{Topics}
"Occupancy Grids"

Introduced in R2019b

\section*{world2grid}

Convert world coordinates to grid indices

\section*{Syntax}
ij \(=\) world2grid(map, xy)

\section*{Description}
ij = world2grid(map, xy) converts an array of world coordinates, \(x y\), to a [rows cols] array of grid indices, ij.

\section*{Input Arguments}
map - Map representation
binary0ccupancyMap object
Map representation, specified as a binary0ccupancyMap object.
xy - World coordinates
\(n\)-by-2 vertical array
World coordinates, specified as an \(n\)-by-2 vertical array of [ \(x y\) ] pairs, where \(n\) is the number of world coordinates.

\section*{Output Arguments}
ij - Grid indices
\(n\)-by-2 vertical array
Grid indices, specified as an \(n\)-by-2 vertical array of [ \(i \operatorname{j}\) ] pairs in [rows cols] format, where \(n\) is the number of grid positions.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}
binary0ccupancyMap|grid2world

Introduced in R2015a

\section*{world2local}

Convert world coordinates to local coordinates

\section*{Syntax}
xyLocal \(=\) world2local (map, xy)

\section*{Description}
xyLocal \(=\) world2local(map,xy) converts an array of world coordinates to local coordinates.

\section*{Input Arguments}

\section*{map - Map representation}
binaryOccupancyMap object
Map representation, specified as a binary0ccupancyMap object.
xy - World coordinates
\(n\)-by-2 vertical array
World coordinates, specified as an \(n\)-by-2 vertical array of [ \(\mathrm{x} y\) ] pairs, where \(n\) is the number of world coordinates.

\section*{Output Arguments}
xyLocal - Local coordinates
n-by-2 vertical array
Local coordinates, specified as an \(n\)-by-2 vertical array of [ \(x\) y] pairs, where \(n\) is the number of local coordinates.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and C++ code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}
binary0ccupancyMap | grid2world | local2world

\section*{Introduced in R2019b}

\section*{controllerVFH}

Avoid obstacles using vector field histogram

\section*{Description}

The controllerVFH System object enables your vehicle to avoid obstacles based on range sensor data using vector field histograms (VFH). Given laser scan readings and a target direction to drive toward, the object computes an obstacle-free steering direction.
controllerVFH specifically uses the VFH+ algorithm to compute an obstacle-free direction. First, the algorithm takes the ranges and angles from laser scan data and builds a polar histogram for obstacle locations. Then, the input histogram thresholds are used to calculate a binary histogram that indicates occupied and free directions. Finally, the algorithm computes a masked histogram, which is computed from the binary histogram based on the minimum turning radius of the vehicle.

The algorithm selects multiple steering directions based on the open space and possible driving directions. A cost function, with weights corresponding to the previous, current, and target directions, calculates the cost of different possible directions. The object then returns an obstaclefree direction with minimal cost. Using the obstacle-free direction, you can input commands to move your vehicle in that direction.

To use this object for your own application and environment, you must tune the properties of the algorithm. Property values depend on the type of vehicle, the range sensor, and the hardware you use.

To find an obstacle-free steering direction:
1 Create the controllerVFH object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

\section*{Creation}

\section*{Syntax}

VFH = controllerVFH
VFH = controllerVFH(Name,Value)

\section*{Description}

VFH = controllerVFH returns a vector field histogram object that computes the obstacle-free steering direction using the VFH+ algorithm.

VFH = controllerVFH(Name, Value) returns a vector field histogram object with additional options specified by one or more Name, Value pairs. Name is the property name and Value is the corresponding value. Name must appear inside single quotes (' '). You can specify several name-
value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN. Properties not specified retain their default values.

\section*{Properties}

\section*{NumAngularSectors - Number of angular sectors in histogram \\ 180 (default) | positive integer}

Number of angular sectors in the vector field histogram, specified as a scalar. This property defines the number of bins used to create the histograms. This property is non-tunable. You can only set this when the object is initialized.

\section*{DistanceLimits - Limits for range readings}
[0.05 2] (default)| 2 -element vector
Limits for range readings, specified as a 2 -element vector with elements measured in meters. The range readings specified when calling the object are considered only if they fall within the distance limits. Use the lower distance limit to ignore false positives from poor sensor performance at lower ranges. Use the upper limit to ignore obstacles that are too far from the vehicle.

\section*{RobotRadius - Radius of vehicle}
0.1 (default) | scalar

Radius of the vehicle in meters, specified as a scalar. This dimension defines the smallest circle that can circumscribe your vehicle. The vehicle radius is used to account for vehicle size when computing the obstacle-free direction.

\section*{SafetyDistance - Safety distance around vehicle}
0.1 (default) | scalar

Safety distance around the vehicle, specified as a scalar in meters. This is a safety distance to leave around the vehicle position in addition to the value of the RobotRadius parameter. The sum of the vehicle radius and the safety distance is used to compute the obstacle-free direction.

\section*{MinTurningRadius - Minimum turning radius at current speed}
0.1 (default) | scalar

Minimum turning radius in meters for the vehicle moving at its current speed, specified as a scalar.

\section*{TargetDirectionWeight - Cost function weight for target direction \\ 5 (default) | scalar}

Cost function weight for moving toward the target direction, specified as a scalar. To follow a target direction, set this weight to be higher than the sum of the CurrentDirectionWeight and PreviousDirectionWeight properties. To ignore the target direction cost, set this weight to zero.

\section*{CurrentDirectionWeight - Cost function weight for current direction}

2 (default) | scalar
Cost function weight for moving the robot in the current heading direction, specified as a scalar. Higher values of this weight produce efficient paths. To ignore the current direction cost, set this weight to zero.

PreviousDirectionWeight - Cost function weight for previous direction
2 (default) | scalar

Cost function weight for moving in the previously selected steering direction, specified as a scalar. Higher values of this weight produces smoother paths. To ignore the previous direction cost, set this weight to zero.

\section*{HistogramThresholds - Thresholds for binary histogram computation \\ [3 10] (default) | 2 -element vector}

Thresholds for binary histogram computation, specified as a 2 -element vector. The algorithm uses these thresholds to compute the binary histogram from the polar obstacle density. Polar obstacle density values higher than the upper threshold are represented as occupied space (1) in the binary histogram. Values smaller than the lower threshold are represented as free space (0). Values that fall between the limits are set to the values in the previous binary histogram, with the default being free space (0).

\section*{UseLidarScan - Use lidarScan object as scan input \\ false (default) | true}

Use lidarScan object as scan input, specified as either true or false.

\section*{Usage}

\section*{Syntax}
```

steeringDir = vfh(scan,targetDir)
steeringDir = vfh(ranges,angles,targetDir)

```

\section*{Description}
steeringDir = vfh(scan,targetDir) finds an obstacle-free steering direction using the VFH + algorithm for the input lidarScan object, scan. A target direction is given based on the target location.

To enable this syntax, you must set the UseLidarScan property to true. For example:
```

mcl = monteCarloLocalization('UseLidarScan',true);
[isUpdated,pose,covariance] = mcl(odomPose,scan);
steeringDir = vfh(ranges,angles,targetDir) defines the lidar scan with two vectors:
ranges and angles.

```

\section*{Input Arguments}

\section*{scan - Lidar scan readings}
```

lidarScan object

```

Lidar scan readings, specified as a lidarScan object.

\section*{Dependencies}

To use this argument, you must set the UseLidarScan property to true.
mcl.UseLidarScan = true;

\section*{ranges - Range values from scan data}
vector
Range values from scan data, specified as a vector in meters. These range values are distances from a sensor at given angles. The vector must be the same length as the corresponding angles vector.

\section*{angles - Angle values from scan data}
vector
Angle values from scan data, specified as a vector in radians. These angle values are the specific angles of the given ranges. The vector must be the same length as the corresponding ranges vector.

\section*{targetDir - Target direction for vehicle \\ scalar}

Target direction for the vehicle, specified as a scalar in radians. The forward direction of the vehicle is considered zero radians, with positive angles measured counterclockwise.

\section*{Output Arguments}

\section*{steeringDir - Steering direction for vehicle}
scalar
Steering direction for the vehicle, specified as a scalar in radians. This obstacle-free direction is calculated based on the VFH+ algorithm. The forward direction of the vehicle is considered zero radians, with positive angles measured counterclockwise.

\section*{Object Functions}

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:
```

release(obj)

```

\section*{Specific to controllerVFH}
show Display VectorFieldHistogram information in figure window

\section*{Common to All System Objects}
step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

\section*{Examples}

\section*{Create a Vector Field Histogram Object and Visualize Data}

This example shows how to calculate a steering direction based on input laser scan data.
Create a controllerVFH object. Set the UseLidarScan property to true.
```

vfh = controllerVFH;
vfh.UseLidarScan = true;

```

Input laser scan data and target direction.
```

ranges = 10*ones(1,500);
ranges(1,225:275) = 1.0;
angles = linspace(-pi,pi,500);
targetDir = 0;

```

Create a lidarScan object by specifying the ranges and angles.
scan = lidarScan(ranges,angles);
Compute an obstacle-free steering direction.
steeringDir = vfh(scan,targetDir);
Visualize the VectorFieldHistogram computation.
h = figure;
set(h,'Position',[50 50800 400])
show(vfh)



\section*{References}
[1] Borenstein, J., and Y. Koren. "The Vector Field Histogram - Fast Obstacle Avoidance for Mobile Robots." IEEE Journal of Robotics and Automation. Vol. 7, Number 3, 1991, pp.278-88.
[2] Ulrich, I., and J. Borenstein. "VFH : Reliable Obstacle Avoidance for Fast Mobile Robots." Proceedings. 1998 IEEE International Conference on Robotics and Automation. (1998): 15721577.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and C++ code using MATLAB® Coder \(^{\text {TM }}\).
Usage notes and limitations:
Use in a MATLAB Function block is not supported.
Lidar scans require a limited size in code generation. The lidar scans, scan, are limited to 4000 points (range and angles) as a maximum.

For additional information about code generation for System objects, see "System Objects in MATLAB Code Generation" (MATLAB Coder)

\section*{See Also}
lidarScan|show

\section*{Topics}
"Obstacle Avoidance with TurtleBot and VFH"
"Vector Field Histogram"
Introduced in R2019b

\section*{show}

Display VectorFieldHistogram information in figure window

\section*{Syntax}
show(vfh)
show(vfh,'Parent', parent)
h = show( \(\qquad\) )

\section*{Description}
show (vfh) shows histograms calculated by the VFH + algorithm in a figure window. The figure also includes the parameters of the controllerVFH object and range values from the last object call.
show(vfh,' Parent', parent) sets the specified axes handle, parent, to the axes.
h = show ( \(\qquad\) ) returns the figure object handle created by show using any of the arguments from the previous syntaxes.

\section*{Examples}

\section*{Create a Vector Field Histogram Object and Visualize Data}

This example shows how to calculate a steering direction based on input laser scan data.
Create a controllerVFH object. Set the UseLidarScan property to true.
```

vfh = controllerVFH;

```
vfh.UseLidarScan = true;

Input laser scan data and target direction.
```

ranges = 10*ones(1,500);
ranges(1,225:275) = 1.0;
angles = linspace(-pi,pi,500);
targetDir = 0;

```

Create a lidarScan object by specifying the ranges and angles.
scan = lidarScan(ranges,angles);
Compute an obstacle-free steering direction.
```

steeringDir = vfh(scan,targetDir);

```

Visualize the VectorFieldHistogram computation.
```

h = figure;
set(h,'Position',[50 50 800 400])
show(vfh)

```


\section*{Input Arguments}
vfh - Vector field histogram algorithm
controllerVFH object
Vector field histogram algorithm, specified as a controllerVFH object. This object contains all the parameters for tuning the VFH+ algorithm.
```

parent - Axes properties
handle

```

Axes properties, specified as a handle.

\section*{Output Arguments}
h - Axes handles for VFH algorithm display
Axes array
Axes handles for VFH algorithm display, specified as an Axes array. The VFH histogram and HistogramThresholds are shown in the first axes. The binary histogram, range sensor readings, target direction, and steering directions are shown in the second axes.

\section*{See Also}
controllerVFH

\section*{Introduced in R2019b}

\section*{controllerPurePursuit}

Create controller to follow set of waypoints

\section*{Description}

The controllerPurePursuit System object creates a controller object used to make a differentialdrive vehicle follow a set of waypoints. The object computes the linear and angular velocities for the vehicle given the current pose. Successive calls to the object with updated poses provide updated velocity commands for the vehicle. Use the MaxAngularVelocity and DesiredLinearVelocity properties to update the velocities based on the vehicle's performance.

The LookaheadDistance property computes a look-ahead point on the path, which is a local goal for the vehicle. The angular velocity command is computed based on this point. Changing LookaheadDistance has a significant impact on the performance of the algorithm. A higher lookahead distance results in a smoother trajectory for the vehicle, but can cause the vehicle to cut corners along the path. A low look-ahead distance can result in oscillations in tracking the path, causing unstable behavior. For more information on the pure pursuit algorithm, see "Pure Pursuit Controller".

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, \(x\) ) and \(y=o b j(x)\) perform equivalent operations.

To compute linear and angular velocity control commands:
1 Create the controllerPurePursuit object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

\section*{Creation}

\section*{Syntax}
controller = controllerPurePursuit
controller = controllerPurePursuit(Name,Value)

\section*{Description}
controller = controllerPurePursuit creates a pure pursuit object that uses the pure pursuit algorithm to compute the linear and angular velocity inputs for a differential drive vehicle.
controller \(=\) controllerPurePursuit(Name, Value) creates a pure pursuit object with additional options specified by one or more Name, Value pairs. Name is the property name and Value is the corresponding value. Name must appear inside single quotes (' '). You can specify several
name-value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN. Properties not specified retain their default values.

Example: controller = controllerPurePursuit('DesiredLinearVelocity', 0.5)

\section*{Properties}

\section*{DesiredLinearVelocity - Desired constant linear velocity}
0.1 (default) | scalar in meters per second

Desired constant linear velocity, specified as a scalar in meters per second. The controller assumes that the vehicle drives at a constant linear velocity and that the computed angular velocity is independent of the linear velocity.

Data Types: double

\section*{LookaheadDistance - Look-ahead distance}

\section*{1.0 (default) | scalar in meters}

Look-ahead distance, specified as a scalar in meters. The look-ahead distance changes the response of the controller. A vehicle with a higher look-ahead distance produces smooth paths but takes larger turns at corners. A vehicle with a smaller look-ahead distance follows the path closely and takes sharp turns, but potentially creating oscillations in the path.
Data Types: double

\section*{MaxAngularVelocity - Maximum angular velocity}
1.0 (default) | scalar in radians per second

Maximum angular velocity, specified a scalar in radians per second. The controller saturates the absolute angular velocity output at the given value.
Data Types: double

\section*{Waypoints - Waypoints}
[ ] (default) | \(n\)-by-2 array
Waypoints, specified as an \(n\)-by- 2 array of [ \(x\) y] pairs, where \(n\) is the number of waypoints. You can generate the waypoints from the mobileRobotPRM class or from another source.
Data Types: double

\section*{Usage}

\section*{Syntax}
[vel,angvel] = controller(pose)
[vel,angvel,lookaheadpoint] = controller(pose)

\section*{Description}
[vel, angvel] = controller(pose) processes the vehicle's position and orientation, pose, and outputs the linear velocity, vel, and angular velocity, angvel.
[vel, angvel,lookaheadpoint] = controller(pose) returns the look-ahead point, which is a location on the path used to compute the velocity commands. This location on the path is computed using the LookaheadDistance property on the controller object.

\section*{Input Arguments}
pose - Position and orientation of vehicle
3 -by-1 vector in the form [x y theta]
Position and orientation of vehicle, specified as a 3-by-1 vector in the form [ \(x\) y theta]. The vehicle pose is an \(x\) and \(y\) position with angular orientation \(\theta\) (in radians) measured from the \(x\)-axis.

\section*{Output Arguments}

\section*{vel - Linear velocity}
scalar in meters per second
Linear velocity, specified as a scalar in meters per second.
Data Types: double

\section*{angvel - Angular velocity}
scalar in radians per second
Angular velocity, specified as a scalar in radians per second.
Data Types: double

\section*{lookaheadpoint - Look-ahead point on path}
[ \(x\) y] vector
Look-ahead point on the path, returned as an \([x y]\) vector. This value is calculated based on the LookaheadDistance property.

\section*{Object Functions}

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:
```

release(obj)

```

\section*{Specific to controllerPurePursuit}
info Characteristic information about controllerPurePursuit object

\section*{Common to All System Objects}
step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

\section*{Examples}

\section*{Get Additional Pure Pursuit Object Information}

Use the info method to get more information about a controllerPurePursuit object. The info function returns two fields, RobotPose and LookaheadPoint, which correspond to the current position and orientation of the robot and the point on the path used to compute outputs from the last call of the object.

Create a controllerPurePursuit object.
pp = controllerPurePursuit;
Assign waypoints.
pp.Waypoints = [0 0;1 1];
Compute control commands using the pp object with the initial pose [x y theta] given as the input.
```

[v,w] = pp([0 0 0]);

```

Get additional information.
```

s = info(pp)

```
s = struct with fields:
    RobotPose: [0 0 0]
    LookaheadPoint: [0.7071 0.7071]

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).
Usage notes and limitations:
Use in a MATLAB Function block is not supported.
For additional information about code generation for System objects, see "System Objects in MATLAB Code Generation" (MATLAB Coder)
```

See Also
binaryOccupancyMap | occupancyMap | binaryOccupancyMap | occupancyMap |
controllerVFH
Topics
"Pure Pursuit Controller"
Introduced in R2019b

```

\section*{info}

Characteristic information about controllerPurePursuit object

\section*{Syntax}
```

controllerInfo = info(controller)

```

\section*{Description}
controllerInfo = info(controller) returns a structure, controllerInfo, with additional information about the status of the controllerPurePursuit object, controller. The structure contains the fields, RobotPose and LookaheadPoint.

\section*{Examples}

\section*{Get Additional Pure Pursuit Object Information}

Use the info method to get more information about a controllerPurePursuit object. The info function returns two fields, RobotPose and LookaheadPoint, which correspond to the current position and orientation of the robot and the point on the path used to compute outputs from the last call of the object.

Create a controllerPurePursuit object.
pp = controllerPurePursuit;
Assign waypoints.
pp.Waypoints = [0 0;1 1];
Compute control commands using the pp object with the initial pose [ \(\mathrm{x} y\) theta] given as the input.
```

[v,w] = pp([0 0 0]);

```

Get additional information.
```

s = info(pp)
s = struct with fields:
RobotPose: [0 0 0]
LookaheadPoint: [0.7071 0.7071]

```

\section*{Input Arguments}
controller - Pure pursuit controller
controllerPurePursuit object
Pure pursuit controller, specified as a controllerPurePursuit object.

\section*{Output Arguments}

\section*{controllerInfo - Information on the controllerPurePursuit object \\ structure}

Information on the controllerPurePursuit object, returned as a structure. The structure contains two fields:
- RobotPose - A three-element vector in the form [x y theta] that corresponds to the \(x\) - \(y\) position and orientation of the vehicle. The angle, theta, is measured in radians with positive angles measured counterclockwise from the \(x\)-axis.
- LookaheadPoint-A two-element vector in the form [x y]. The location is a point on the path that was used to compute outputs of the last call to the object.

\section*{See Also}
controllerPurePursuit

\section*{Topics}
"Pure Pursuit Controller"
Introduced in R2019b

\section*{dubinsConnection}

Dubins path connection type

\section*{Description}

The dubinsConnection object holds information for computing a dubinsPathSegment path segment to connect between poses. A Dubins path segment connects two poses as a sequence of three motions. The motion options are:
- Straight
- Left turn at maximum steer
- Right turn at maximum steer

A Dubins path segment only allows motion in the forward direction.
Use this connection object to define parameters for a robot motion model, including the minimum turning radius and options for path types. To generate a path segment between poses using this connection type, call the connect function.

\section*{Creation}

\section*{Syntax}
```

dubConnObj = dubinsConnection
dubConnObj = dubinsConnection(Name,Value)
Description

```
dubConnObj = dubinsConnection creates an object using default property values.
dubConnObj = dubinsConnection(Name,Value) specifies property values using name-value
pairs. To set multiple properties, specify multiple name-value pairs.

\section*{Properties}

\section*{MinTurningRadius - Minimum turning radius of the vehicle}

1 (default) | positive scalar in meters
Minimum turning radius of the vehicle, specified as a positive scalar in meters. The minimum turning radius is for the smallest circle the vehicle can make with maximum steer in a single direction.
Data Types: double

\section*{DisabledPathTypes - Path types to disable}
\{\} (default) | cell array of three-element character vectors | vector of three-element string scalars

Dubins path types to disable, specified as a cell array of three-element character vectors or vector of string scalars. The cell array defines three sequences of motions that are prohibited by the vehicle motion model.
\begin{tabular}{|l|l|}
\hline Motion Type & Description \\
\hline "S" & Straight \\
\hline "L" & \begin{tabular}{l} 
Left turn at the maximum steering angle of the \\
vehicle
\end{tabular} \\
\hline "R" & \begin{tabular}{l} 
Right turn at the maximum steering angle of the \\
vehicle
\end{tabular} \\
\hline
\end{tabular}

To see all available path types, see the AllPathTypes property.
For Dubins connections, the available path types are: \{"LSL"\} \{"LSR"\} \{"RSL"\} \{"RSR"\} \{"RLR"\} \{"LRL"\}.
Example: ["LSL","LSR"]
Data Types: string|cell
AllPathTypes - All possible path types
cell array of character vectors
This property is read-only.
All possible path types, returned as a cell array of character vectors. This property lists all types. To disable certain types, specify types from this list in DisabledPathTypes.

For Dubins connections, the available path types are: \{'LSL'\} \{'LSR'\} \{'RSL'\} \{'RSR'\} \{'RLR'\} \{'LRL'\}.
Data Types: cell

\section*{Object Functions}
connect Connect poses for given connection type

\section*{Examples}

\section*{Connect Poses Using Dubins Connection Path}

Create a dubinsConnection object.
dubConnObj = dubinsConnection;
Define start and goal poses as [x y theta] vectors.
```

startPose = [0 0 0];
goalPose = [1 1 pi];

```

Calculate a valid path segment to connect the poses.
```

[pathSegObj, pathCosts] = connect(dubConnObj,startPose,goalPose);

```

Show the generated path.
show(pathSeg0bj\{1\})


\section*{Modify Connection Types for Dubins Path}

Create a dubinsConnection object.
dubConnObj = dubinsConnection;
Define start and goal poses as [x y theta] vectors.
startPose = [0 0 0];
goalPose = [1 1 pi];
Calculate a valid path segment to connect the poses.
pathSegObj = connect(dubConnObj,startPose,goalPose);
Show the generated path. Notice the direction of the turns.
show(pathSeg0bj\{1\})

pathSeg0bj\{1\}.MotionTypes
ans \(=1 \times 3\) cell
\{'R'\} \{'L'\} \{'R'\}

Disable this specific motion sequence in a new connection object. Reduce the MinTurningRadius if the robot is more maneuverable. Connect the poses again to get a different path.
```

dubConnObj = dubinsConnection('DisabledPathTypes',{'RLR'});
dubConnObj.MinTurningRadius = 0.5;
[pathSegObj, pathCosts] = connect(dubConnObj,startPose,goalPose);
pathSegObj{1}.MotionTypes
ans = 1x3 cell
{'L'} {'S'} {'L'}

```
show(pathSeg0bj\{1\})


\section*{References}
[1] Shkel, Andrei M., and Vladimir Lumelsky. "Classification of the Dubins set." Robotics and Autonomous Systems. Vol. 34, No. 4, 2001, pp. 179-202.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and C++ code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}

\section*{Objects}
dubinsPathSegment|reedsSheppConnection | reedsSheppPathSegment

\section*{Functions}
connect | interpolate | show

\section*{Introduced in R2019b}

\section*{dubinsPathSegment}

Dubins path segment connecting two poses

\section*{Description}

The dubinsPathSegment object holds information for a Dubins path segment that connects two poses as a sequence of three motions. The motion options are:
- Straight
- Left turn at maximum steer
- Right turn at maximum steer

\section*{Creation}

To generate a dubinsPathSegment object, use the connect function with a dubinsConnection object:
dubPathSeg = connect(connection0bj, start,goal) connects the start and goal pose using the specified connection type object.

To specifically define a path segment:
dubPathSeg = dubinsPathSegment (connectionObj,start,goal,motionLengths, motionTypes) specifies the Dubins connection type, the start and goal poses, and the corresponding motion lengths and types. These values are set to the corresponding properties in the object.

\section*{Properties}

\section*{MinTurningRadius - Minimum turning radius of vehicle \\ positive scalar}

This property is read-only.
Minimum turning radius of the vehicle, specified as a positive scalar in meters. This value corresponds to the radius of the turning circle at the maximum steering angle of the vehicle.
Data Types: double

\section*{StartPose - Initial pose of the vehicle}
\([x, y, \Theta]\) vector
This property is read-only.
Initial pose of the vehicle at the start of the path segment, specified as an \([x, y, \Theta]\) vector. \(x\) and \(y\) are in meters. \(\Theta\) is in radians.
Data Types: double

\section*{GoalPose - Goal pose of the vehicle}
\([x, y, \Theta]\) vector
This property is read-only.
Goal pose of the vehicle at the end of the path segment, specified as an \([x, y, \Theta]\) vector. \(x\) and \(y\) are in meters. \(\Theta\) is in radians.

Data Types: double

\section*{MotionLengths - Length of each motion}
three-element numeric vector
This property is read-only.
Length of each motion in the path segment, in world units, specified as a three-element numeric vector. Each motion length corresponds to a motion type specified in MotionTypes.

Data Types: double
MotionTypes - Type of each motion
three-element string cell array
This property is read-only.
Type of each motion in the path segment, specified as a three-element string cell array.
\begin{tabular}{|l|l|}
\hline Motion Type & Description \\
\hline "S" & Straight \\
\hline "L" & \begin{tabular}{l} 
Left turn at the maximum steering angle of the \\
vehicle
\end{tabular} \\
\hline "R" & \begin{tabular}{l} 
Right turn at the maximum steering angle of the \\
vehicle
\end{tabular} \\
\hline
\end{tabular}

Each motion type corresponds to a motion length specified in MotionLengths.
For Dubins connections, the available path types are: \{"LSL"\} \{"LSR"\} \{"RSL"\} \{"RSR"\} \{"RLR"\} \{"LRL"\}.
Example: \{"R" "S" "R"\}
Data Types: cell

\section*{Length - Length of path segment}
positive scalar
This property is read-only.
Length of the path segment, specified as a positive scalar in meters. This length is just a sum of the elements in MotionLengths.
Data Types: double

\section*{Object Functions}
interpolate Interpolate poses along path segment
show
Visualize path segment

\section*{Examples}

\section*{Connect Poses Using Dubins Connection Path}

Create a dubinsConnection object.
dubConnObj = dubinsConnection;
Define start and goal poses as [x y theta] vectors.
startPose = [0 0 0];
goalPose = [1 1 pi];
Calculate a valid path segment to connect the poses.
[pathSegObj, pathCosts] = connect(dubConnObj,startPose,goalPose);
Show the generated path.
show(pathSeg0bj\{1\})


\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).

\section*{See Also}

\section*{Objects}
dubinsConnection| reedsSheppConnection| reedsSheppPathSegment

\section*{Functions}
connect | interpolate | show
Introduced in R2019b

\section*{dynamicCapsuleList}

Dynamic capsule-based obstacle list

\section*{Description}

The dynamicCapsuleList object manages two lists of capsule-based collision objects in 2-D space. Collision objects are separated into two lists, ego bodies and obstacles. For ego bodies and obstacles in 3-D, see the dynamicCapsuleList3D object.

Each collision object in the two lists has three key elements:
- ID -- Integer that identifies each object, stored in the EgoIDs property for ego bodies and the ObstacleIDs property for obstacles.
- States -- Location and orientation of the object as an \(M\)-by-3 matrix, where each row is of form [ x \(y\) theta] and \(M\) is the number of states along the path of the object in the world frame. The list of states assumes each state is separated by a fixed time interval. \(x y\)-positions are in meters, and theta is in radians. The default local origin is located at the center of the left semicircle of the capsule.
- Geometry -- Size of the capsule-based object based on a specified length and radius. The radius applies to the semicircle end caps, and the length applies to the central rectangle length. To shift the capsule geometry and local origin relative to the default origin point, specify a fixed transform relative to the local frame of the capsule.


Use the object functions to dynamically add, remove, and update the geometries and states of the various objects in your environment. To add an ego body, see the addEgo object function. To add an obstacle, see the addObstacle object function.

After specifying all of the object states, validate the ego-body paths and check for collisions with obstacles at every step using the checkCollision object function. The function only checks if an ego body collides with an obstacle, ignoring collisions between only obstacles or only ego bodies.

\section*{Creation}

\section*{Syntax}
obstacleList = dynamicCapsuleList

\section*{Description}
obstacleList \(=\) dynamicCapsuleList creates a dynamic capsule-based obstacle list with no ego bodies or obstacles. To begin building an obstacle list, use the addEgo or addObstacle object functions.

\section*{Properties}

MaxNumSteps - Maximum number of time steps in obstacle list
31 (default) | positive integer
Maximum number of time steps in the obstacle list, specified as a positive integer. The number of steps determines to the maximum length of the States field for a specific ego body or obstacle.
Data Types: double

\section*{EgoIDs - List of IDs for ego bodies}
vector of positive integers
This property is read-only.
List of identifiers for ego bodies, returned as a vector of positive integers.
Data Types: double

\section*{ObstacleIDs - IDs for obstacles}
vector of positive integers
This property is read-only.
List of identifiers for obstacles, returned as a vector of positive integers.

\section*{Data Types: double}

\section*{NumObstacles - Number of obstacles in list}
integer
This property is read-only.
Number of obstacles in list, returned as an integer.
Data Types: double
NumEgos - Number of ego bodies in list
integer

This property is read-only.
Number of ego bodies in list, returned as an integer.
Data Types: double

\section*{Object Functions}
addEgo addObstacle checkCollision egoGeometry egoPose obstacleGeometry obstaclePose removeEgo removeObstacle show updateEgoGeometry updateEgoPose updateObstacleGeometry updateObstaclePose

Add ego bodies to capsule list
Add obstacles to 2-D capsule list
Check for collisions between ego bodies and obstacles
Geometric properties of ego bodies
Poses of ego bodies
Geometric properties of obstacles
Poses of obstacles
Remove ego bodies from capsule list
Remove obstacles from capsule list
Display ego bodies and obstacles in environment
Update geometric properties of ego bodies
Update states of ego bodies
Update geometric properties of obstacles
Update states of obstacles

\section*{Examples}

\section*{Build Ego Body Paths and Check for Collisions with Obstacles}

Build an ego body path and maintain obstacle states using the dynamicCapsuleList object. Visualize the states of all objects in the environment at different timestamps. Validate the path of the ego body by checking for collisions with obstacles in the environment.

Create the dynamicCapsuleList object. Extract the maximum number of steps to use as the number of time stamps for your object paths.
```

obsList = dynamicCapsuleList;
numSteps = obsList.MaxNumSteps;

```

\section*{Add Ego Body}

Define an ego body by specifying the ID, geometry, and state together in a structure. The capsule geometry has a length of 3 m and radius of 1 m . Specify the state as a linear path from \(x=0 \mathrm{~m}\) to \(x=\) 100 m .
```

egoID1 = 1;
geom = struct("Length",3,"Radius",1,"FixedTransform",eye(3));
states = linspace(0,1,obsList.MaxNumSteps)'.*[100 0 0];
egoCapsule1 = struct('ID',egoID1,'States',states,'Geometry',geom);
addEgo(obsList,egoCapsule1);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])

```


\section*{Add Obstacles}

Specify states for two obstacles that are separated from the ego body by 5 m in opposite directions on the \(y\)-axis.. Assume the obstacles have the same geometry geom as the ego body.
```

obsStatel = states + [0 5 0];
obsState2 = states + [0 -5 0];
obsCapsule1 = struct('ID',1,'States',obsState1,'Geometry',geom);
obsCapsule2 = struct('ID',2,'States',obsState2,'Geometry',geom);
addObstacle(obsList,obsCapsule1);
addObstacle(obsList,obsCapsule2);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])

```


\section*{Update Obstacles}

Alter your obstacle locations and geometry dimensions over time. Use the previously generated structure, modify the fields, and update the obstacles using the update0bstacleGeometry and update0bstaclePose object functions. Reduces the radius of the first obstacle to 0.5 m , and change the path to move it towards the ego body.
```

obsCapsule1.Geometry.Radius = 0.5;
obsCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
linspace(5,-4,numSteps)' ... % y
zeros(numSteps,1)]; % theta
updateObstacleGeometry(obsList,1,obsCapsule1);
updateObstaclePose(obsList,1,obsCapsule1);

```

\section*{Check for Collisions}

Visualize the new paths. Show where collisions between the ego body and an obstacle, which the display highlights in red. Notice that collisions between the obstacles are not checked.
```

show(obsList,"TimeStep",[1:numSteps],"ShowCollisions",1);
ylim([-20 20])
xlabel("X (m)")
ylabel("Y (m)")

```


Programmatically check for collisions by using the checkCollision object function. The function returns a vector of logical values that indicates the status of each time step. The vector is transposed for display purposes.
```

collisions = checkCollision(obsList)'
collisions = 1x31 logical array

```
\begin{tabular}{lllllllllllllllllllllllll}
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 0
\end{tabular}

To validate paths with a large number of steps, use the any function on the vector of collision values.
```

if any(collisions)
disp("Collision detected.")
end
Collision detected.

```

\section*{Update Ego Path}

Specify a new path for the ego body. Visualize the paths again, displaying collisions.
```

egoCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
3*sin(linspace(0,2*pi,numSteps))' ... % y
zeros(numSteps,1)]; % theta

```
updateEgoPose(obsList,1,egoCapsule1);
show(obsList,"TimeStep", [1:numSteps],"ShowCollisions",1); ylim([-20 20])


\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}

\section*{Objects}
dynamicCapsuleList3D

\section*{Functions}
addEgo | addObstacle | checkCollision | egoGeometry | egoPose | obstacleGeometry | obstaclePose | removeEgo | removeObstacle | show | updateEgoGeometry |updateEgoPose | updateObstacleGeometry|updateObstaclePose

Topics
"Highway Trajectory Planning Using Frenet Reference Path"
Introduced in R2020b

\section*{addEgo}

Add ego bodies to capsule list

\section*{Syntax}
addEgo(capsuleListObj,egoStruct)
status = addEgo(capsuleListObj,egoStruct)

\section*{Description}
addEgo(capsuleListObj, egoStruct) adds one or more ego bodies to the 2-D dynamic capsule list with the specified ID, state, and geometry values given in egoStruct.
status = addEgo(capsuleListObj, egoStruct) additionally returns an indicator of whether each specified ego body was added, updated, or a duplicate.

\section*{Examples}

\section*{Build Ego Body Paths and Check for Collisions with Obstacles}

Build an ego body path and maintain obstacle states using the dynamicCapsuleList object. Visualize the states of all objects in the environment at different timestamps. Validate the path of the ego body by checking for collisions with obstacles in the environment.

Create the dynamicCapsuleList object. Extract the maximum number of steps to use as the number of time stamps for your object paths.
```

obsList = dynamicCapsuleList;
numSteps = obsList.MaxNumSteps;

```

\section*{Add Ego Body}

Define an ego body by specifying the ID, geometry, and state together in a structure. The capsule geometry has a length of 3 m and radius of 1 m . Specify the state as a linear path from \(x=0 \mathrm{~m}\) to \(x=\) 100 m .
```

egoID1 = 1;
geom = struct("Length",3,"Radius",1,"FixedTransform",eye(3));
states = linspace(0,1,obsList.MaxNumSteps)'.*[100 0 0];
egoCapsule1 = struct('ID',egoID1,'States',states,'Geometry',geom);
addEgo(obsList,egoCapsule1);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])

```


\section*{Add Obstacles}

Specify states for two obstacles that are separated from the ego body by 5 m in opposite directions on the \(y\)-axis.. Assume the obstacles have the same geometry geom as the ego body.
```

obsStatel = states + [0 5 0];
obsState2 = states + [0 -5 0];
obsCapsule1 = struct('ID',1,'States',obsState1,'Geometry',geom);
obsCapsule2 = struct('ID',2,'States',obsState2,'Geometry',geom);
addObstacle(obsList,obsCapsule1);
addObstacle(obsList,obsCapsule2);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])

```


\section*{Update Obstacles}

Alter your obstacle locations and geometry dimensions over time. Use the previously generated structure, modify the fields, and update the obstacles using the updateObstacleGeometry and updateObstaclePose object functions. Reduces the radius of the first obstacle to 0.5 m , and change the path to move it towards the ego body.
```

obsCapsule1.Geometry.Radius = 0.5;
obsCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
linspace(5,-4,numSteps)' ... % y
zeros(numSteps,1)]; % theta
updateObstacleGeometry(obsList,1,obsCapsule1);
updateObstaclePose(obsList,1,obsCapsule1);

```

\section*{Check for Collisions}

Visualize the new paths. Show where collisions between the ego body and an obstacle, which the display highlights in red. Notice that collisions between the obstacles are not checked.
```

show(obsList,"TimeStep",[1:numSteps],"ShowCollisions",1);
ylim([-20 20])
xlabel("X (m)")
ylabel("Y (m)")

```


Programmatically check for collisions by using the checkCollision object function. The function returns a vector of logical values that indicates the status of each time step. The vector is transposed for display purposes.
```

collisions = checkCollision(obsList)'
collisions = 1x31 logical array

```
```

if any(collisions)

```
if any(collisions)
    disp("Collision detected.")
    disp("Collision detected.")
end
end
Collision detected.
```

Collision detected.

```
    \(\begin{array}{lllllllllllllllllllllllll}0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 0\end{array}\)

To validate paths with a large number of steps, use the any function on the vector of collision values.

\section*{Update Ego Path}

Specify a new path for the ego body. Visualize the paths again, displaying collisions.
```

egoCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
3*sin(linspace(0,2*pi,numSteps))' ... % y
zeros(numSteps,1)]; % theta

```
```

updateEgoPose(obsList,1,egoCapsule1);
show(obsList,"TimeStep",[1:numSteps],"ShowCollisions",1);
ylim([-20 20])

```


\section*{Input Arguments}

\section*{capsuleListObj - Dynamic capsule list}
dynamicCapsuleList object
Dynamic capsule list, specified as a dynamicCapsuleList object.

\section*{egoStruct - Ego body parameters}
structure | \(N\)-element structure array
Ego body parameters, specified as an \(N\)-element structure or a structure array, where \(N\) is the number of added ego bodies. The fields of each structure define the ID, geometry, and states of an ego body:
- ID -- Integer that identifies each object. Stored in the EgoIDs property of the dynamicCapsuleList object specified by the capsuleList0bj argument.
- States -- Location and orientation of the object as an \(M\)-by- 3 matrix, where each row is of form [ \(x y\) theta], and \(M\) is the number of states for the specified ego body in the world frame. The list of states assumes each state is separated by a fixed time interval. xy-positions are in meters and theta is in radians.
- Geometry -- Structure with fields Length, Radius, and FixedTransform. These fields define the size of the capsule-based object using the specified length for the cylinder and semicircle radius for the end caps. To shift the capsule geometry from the default origin, specify the FixedTransform field as a fixed transform relative to the local frame of the capsule. To keep the default capsule origin, specify the transform as eye (3).


\section*{Output Arguments}

\section*{status - Result of adding ego bodies}
\(N\)-element column vector
Result of adding ego bodies, returned as a \(N\)-element column vector of ones, zeros, and negative ones. \(N\) is the number of ego bodies specified in the egoStruct argument. Each value indicates whether the associated body is added (1), updated (0), or a duplicate ( -1 ). While adding ego bodies, if multiple structures with the same body ID are found in the structure array egoStruct, then the function marks the previous entry as duplicate and ignores it.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).

\section*{See Also}

Objects
dynamicCapsuleList|dynamicCapsuleList3D

\author{
Functions \\ addObstacle|checkCollision | egoGeometry| egoPose|obstacleGeometry| \\ obstaclePose|removeEgo| removeObstacle| show|updateEgoGeometry|updateEgoPose| \\ update0bstacleGeometry|update0bstaclePose \\ \section*{Topics} \\ "Highway Trajectory Planning Using Frenet Reference Path" \\ Introduced in R2020b
}

\section*{addObstacle}

Add obstacles to 2-D capsule list

\section*{Syntax}
addObstacle(capsuleListObj,obstacleStruct)
status = addObstacle(capsuleListObj,obstacleStruct)

\section*{Description}
addObstacle(capsuleListObj, obstacleStruct) adds one or more obstacles to the 2-D dynamic capsule list with the specified ID, state, and geometry values given in obstacleStruct.
status = addObstacle(capsuleListObj,obstacleStruct) additionally returns an indicator of whether each specified obstacle was added, updated, or a duplicate.

\section*{Examples}

\section*{Build Ego Body Paths and Check for Collisions with Obstacles}

Build an ego body path and maintain obstacle states using the dynamicCapsuleList object. Visualize the states of all objects in the environment at different timestamps. Validate the path of the ego body by checking for collisions with obstacles in the environment.

Create the dynamicCapsuleList object. Extract the maximum number of steps to use as the number of time stamps for your object paths.
```

obsList = dynamicCapsuleList;
numSteps = obsList.MaxNumSteps;

```

\section*{Add Ego Body}

Define an ego body by specifying the ID, geometry, and state together in a structure. The capsule geometry has a length of 3 m and radius of 1 m . Specify the state as a linear path from \(x=0 \mathrm{~m}\) to \(x=\) 100 m .
```

egoID1 = 1;
geom = struct("Length",3,"Radius",1,"FixedTransform",eye(3));
states = linspace(0,1,obsList.MaxNumSteps)'.*[100 0 0];
egoCapsule1 = struct('ID',egoID1,'States',states,'Geometry',geom);
addEgo(obsList,egoCapsule1);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])

```


\section*{Add Obstacles}

Specify states for two obstacles that are separated from the ego body by 5 m in opposite directions on the \(y\)-axis.. Assume the obstacles have the same geometry geom as the ego body.
```

obsStatel = states + [0 5 0];
obsState2 = states + [0 -5 0];
obsCapsule1 = struct('ID',1,'States',obsState1,'Geometry',geom);
obsCapsule2 = struct('ID',2,'States',obsState2,'Geometry',geom);
addObstacle(obsList,obsCapsule1);
addObstacle(obsList,obsCapsule2);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])

```


\section*{Update Obstacles}

Alter your obstacle locations and geometry dimensions over time. Use the previously generated structure, modify the fields, and update the obstacles using the update0bstacleGeometry and update0bstaclePose object functions. Reduces the radius of the first obstacle to 0.5 m , and change the path to move it towards the ego body.
```

obsCapsule1.Geometry.Radius = 0.5;
obsCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
linspace(5,-4,numSteps)' ... % y
zeros(numSteps,1)]; % theta
updateObstacleGeometry(obsList,1,obsCapsule1);
updateObstaclePose(obsList,1,obsCapsule1);

```

\section*{Check for Collisions}

Visualize the new paths. Show where collisions between the ego body and an obstacle, which the display highlights in red. Notice that collisions between the obstacles are not checked.
```

show(obsList,"TimeStep",[1:numSteps],"ShowCollisions",1);
ylim([-20 20])
xlabel("X (m)")
ylabel("Y (m)")

```


Programmatically check for collisions by using the checkCollision object function. The function returns a vector of logical values that indicates the status of each time step. The vector is transposed for display purposes.
```

collisions = checkCollision(obsList)'
collisions = 1x31 logical array

```
\begin{tabular}{lllllllllllllllllllllllll}
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 0
\end{tabular}

To validate paths with a large number of steps, use the any function on the vector of collision values.
```

if any(collisions)
disp("Collision detected.")
end
Collision detected.

```

\section*{Update Ego Path}

Specify a new path for the ego body. Visualize the paths again, displaying collisions.
```

egoCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
3*sin(linspace(0,2*pi,numSteps))' ... % y
zeros(numSteps,1)]; % theta

```
```

updateEgoPose(obsList,1,egoCapsule1);
show(obsList,"TimeStep",[1:numSteps],"ShowCollisions",1);
ylim([-20 20])

```


\section*{Input Arguments}

\section*{capsuleListObj - Dynamic capsule list}
dynamicCapsuleList object
Dynamic capsule list, specified as a dynamicCapsuleList object.

\section*{obstacleStruct - Obstacle parameters}
structure | \(N\)-element structure array
Obstacle parameters, specified as an \(N\)-element structure or a structure array, where \(N\) is the number of added obstacles. The fields of each structure define the ID, geometry, and states of an obstacle:
- ID -- Integer that identifies each object. Stored in the ObstacleIDs property of the dynamicCapsuleList object specified by the capsuleList0bj argument.
- States -- Location and orientation of the object as an \(M\)-by-3 matrix, where each row is of form [ \(\mathrm{x} y\) theta], and \(M\) is the number of states for the specified obstacle in the world frame. The list of states assumes each state is separated by a fixed time interval. xy-positions are in meters and theta is in radians.
- Geometry -- Structure with fields Length, Radius, and FixedTransform. These fields define the size of the capsule-based object using the specified length for the cylinder and semicircle radius for the end caps. To shift the capsule geometry from the default origin, specify the FixedTransform field as a fixed transform relative to the local frame of the capsule. To keep the default capsule origin, specify the transform as eye (3).


\section*{Output Arguments}

\section*{status - Result of adding obstacles}
\(N\)-element column vector
Result of adding obstacles, returned as a \(N\)-element column vector of ones, zeros, and negative ones. \(N\) is the number of obstacles specified in the obstacleStruct argument. Each value indicates whether the associated body is added (1), updated (0), or a duplicate ( -1 ). While adding obstacles, if multiple structures with the same body ID are found in the structure array obstaclesStruct, then the function marks the previous entry as duplicate and ignores it.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder \({ }^{\mathrm{TM}}\).

\section*{See Also}

Objects
dynamicCapsuleList|dynamicCapsuleList3D

\author{
Functions \\ addEgo | checkCollision | egoGeometry |egoPose| obstacleGeometry|obstaclePose| removeEgo | removeObstacle | show \| updateEgoGeometry |updateEgoPose | \\ updateObstacleGeometry|updateObstaclePose \\ \section*{Topics} \\ "Highway Trajectory Planning Using Frenet Reference Path" \\ Introduced in R2020b
}

\section*{checkCollision}

Check for collisions between ego bodies and obstacles

\section*{Syntax}
collisionFound \(=\) checkCollision(capsuleListObj)
[fullResults,distance] = checkCollision(capsuleListObj,options)

\section*{Description}
collisionFound = checkCollision(capsuleListObj) checks each ego body for collisions with obstacles in the environment. The function indicates whether each ego body is in collision at each time step..
[fullResults,distance] = checkCollision(capsuleListObj,options) checks each ego body for collisions with obstacles in the environment, and returns the results using additional specified collision detection options options.

\section*{Examples}

\section*{Build Ego Body Paths and Check for Collisions with Obstacles}

Build an ego body path and maintain obstacle states using the dynamicCapsuleList object. Visualize the states of all objects in the environment at different timestamps. Validate the path of the ego body by checking for collisions with obstacles in the environment.

Create the dynamicCapsuleList object. Extract the maximum number of steps to use as the number of time stamps for your object paths.
```

obsList = dynamicCapsuleList;
numSteps = obsList.MaxNumSteps;

```

\section*{Add Ego Body}

Define an ego body by specifying the ID, geometry, and state together in a structure. The capsule geometry has a length of 3 m and radius of 1 m . Specify the state as a linear path from \(x=0 \mathrm{~m}\) to \(x=\) 100 m .
```

egoID1 = 1;
geom = struct("Length",3,"Radius",1,"FixedTransform",eye(3));
states = linspace(0,1,obsList.MaxNumSteps)'.*[100 0 0];
egoCapsule1 = struct('ID',egoID1,'States',states,'Geometry',geom);
addEgo(obsList,egoCapsule1);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])

```


\section*{Add Obstacles}

Specify states for two obstacles that are separated from the ego body by 5 m in opposite directions on the \(y\)-axis.. Assume the obstacles have the same geometry geom as the ego body.
```

obsStatel = states + [0 5 0];
obsState2 = states + [0 -5 0];
obsCapsule1 = struct('ID',1,'States',obsState1,'Geometry',geom);
obsCapsule2 = struct('ID',2,'States',obsState2,'Geometry',geom);
addObstacle(obsList,obsCapsule1);
addObstacle(obsList,obsCapsule2);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])

```


\section*{Update Obstacles}

Alter your obstacle locations and geometry dimensions over time. Use the previously generated structure, modify the fields, and update the obstacles using the updateObstacleGeometry and updateObstaclePose object functions. Reduces the radius of the first obstacle to 0.5 m , and change the path to move it towards the ego body.
```

obsCapsule1.Geometry.Radius = 0.5;
obsCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
linspace(5,-4,numSteps)' ... % y
zeros(numSteps,1)]; % theta
updateObstacleGeometry(obsList,1,obsCapsule1);
updateObstaclePose(obsList,1,obsCapsule1);

```

\section*{Check for Collisions}

Visualize the new paths. Show where collisions between the ego body and an obstacle, which the display highlights in red. Notice that collisions between the obstacles are not checked.
```

show(obsList,"TimeStep",[1:numSteps],"ShowCollisions",1);
ylim([-20 20])
xlabel("X (m)")
ylabel("Y (m)")

```


Programmatically check for collisions by using the checkCollision object function. The function returns a vector of logical values that indicates the status of each time step. The vector is transposed for display purposes.
```

collisions = checkCollision(obsList)'
collisions = 1x31 logical array

```
\begin{tabular}{lllllllllllllllllllllllll}
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 0
\end{tabular}

To validate paths with a large number of steps, use the any function on the vector of collision values.
```

if any(collisions)
disp("Collision detected.")
end
Collision detected.

```

\section*{Update Ego Path}

Specify a new path for the ego body. Visualize the paths again, displaying collisions.
```

egoCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
3*sin(linspace(0,2*pi,numSteps))' ... % y
zeros(numSteps,1)]; % theta

```
updateEgoPose(obsList,1,egoCapsule1);
show(obsList,"TimeStep", [1:numSteps],"ShowCollisions",1);
ylim([-20 20])


\section*{Input Arguments}

\section*{capsuleListObj - Dynamic capsule list}
dynamicCapsuleList object | dynamicCapsuleList3D object
Dynamic capsule list, specified as a dynamicCapsuleList or dynamicCapsuleList3D object.

\section*{options - Collision detection options}
structure
Collision detection options, specified as a structure with these fields:
- FullResults -- Return the collision results for each obstacle separately , specified as a logical 0 (false) or 1 (true). See the fullResults output argument.
- ReturnDistance -- Return the distance calculation from collision checking, specified as a logical 0 (false) or 1 (true). See the distance output argument.

Data Types: struct

\section*{Output Arguments}

\section*{collisionFound - Collision checking results}
n-by-e matrix of logical values
Collision checking results, returned as an \(n\)-by-e matrix of logical values. By default, the function checks for any collision between any object, which returns an \(n\)-by-e matrix, where \(n\) is the maximum number of states for ego bodies in the specified capsuleListobj object, and \(e\) is the number of ego bodies.

\section*{Data Types: logical}

\section*{fullResults - Full collision checking results for each obstacle}
\(n\)-by-o-by-e array of logical values
Full collision checking results for each obstacle, returned as an \(n\)-by- \(o\)-by-e array of logical values. \(n\) is the maximum number of states for ego bodies in the specified capsuleListobj argument, \(o\) is the number of obstacles, and \(e\) is the number of ego bodies.

\section*{Dependencies}

To return the fullResults output argument, specify the options input argument with the FullResults field set to true.

Data Types: logical

\section*{distance - Distance from obstacles}
\(n\)-by-e numeric matrix | \(n\)-by-oby-e numeric array
Distance from obstacles, returned as an \(n\)-by-e numeric matrix or \(n\)-by-oby-e numeric array. The dimensions and behavior of the distance argument depend on the value of the FullResults field of the options argument
\begin{tabular}{|l|l|l|}
\hline distance Dimensions & \begin{tabular}{l} 
FullResults \\
Value
\end{tabular} & Behavior \\
\hline\(n\)-by-e numeric matrix & false & \begin{tabular}{l} 
Returns the distance between each ego body and the \\
closest obstacle at each time step. \(n\) is the maximum \\
number of states for ego bodies specified in the \\
capsuleList0bj argument, and \(e\) is the number of \\
ego bodies.
\end{tabular} \\
\hline\(n\)-by-oby-e numeric array & true & \begin{tabular}{l} 
Returns the distance between each ego body and \\
each obstacle at each time step. \(o\) is the number of \\
obstacles.
\end{tabular} \\
\hline
\end{tabular}

\section*{Dependencies}

To return the distance output argument, specify the options input argument with the ReturnDistance field set to true.
Data Types: single | double

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{Tm}}\).

\section*{See Also}

\section*{Objects}
dynamicCapsuleList|dynamicCapsuleList3D

\section*{Functions}
addEgo | addObstacle | egoGeometry | egoPose | obstacleGeometry |obstaclePose | removeEgo | removeObstacle | show | updateEgoGeometry |updateEgoPose |
updateObstacleGeometry|updateObstaclePose

\section*{Topics}
"Highway Trajectory Planning Using Frenet Reference Path"
Introduced in R2020b

\section*{egoGeometry}

Geometric properties of ego bodies

\section*{Syntax}
```

[egoIDs,geomStruct] = egoGeometry(capsuleListObj)
[egoIDs,geomStruct] = egoGeometry(capsuleListObj,selectEgoIDs)
[egoIDs,geomStruct,status] = egoGeometry(capsuleListObj,selectEgoIDs)

```

\section*{Description}
[egoIDs, geomStruct] = egoGeometry(capsuleList0bj) returns the ego ID and the geometry parameters for each ego body in the capsule list.
[egoIDs,geomStruct] = egoGeometry(capsuleListObj,selectEgoIDs) specifies which ego bodies to return the ID and geometry parameters for.
[egoIDs,geomStruct,status] = egoGeometry(capsuleListObj, selectEgoIDs) returns an indicator of whether each ID in selectEgoIDs exists.

\section*{Examples}

\section*{Create and Modify Capsule-Based Ego Bodies}

Add ego bodies to an environment using the dynamicCapsuleList object. Modify the properties of the ego bodies. Remove an ego body from the environment. Visualize the states of all objects in the environment at different timestamps.

Create the dynamicCapsuleList object. Extract the maximum number of steps to use as the number of time stamps for the object paths.
```

capsuleList = dynamicCapsuleList;
numSteps = capsuleList.MaxNumSteps;

```

\section*{Add Ego Bodies}

Specify the states for the two ego bodies as a linear path from \(x=0 \mathrm{~m}\) to \(x=100 \mathrm{~m}\). The two ego bodies are separated by 5 m in opposite directions on the \(y\)-axis.
```

egoState = linspace(0,1,numSteps)'.*[100 0 0];
egoStatel = egoState+[0 5 0];
egoState2 = egoState+[0 -5 0];

```

Generate default poses and geometric structures for the two ego bodies using ego IDs.
```

[egoIDs,egoPoseStruct] = egoPose(capsuleList,[1 2]);
[egoIDs,egoGeomStruct] = egoGeometry(capsuleList,egoIDs);

```

\section*{Update Ego Bodies}

Assign the states to the ego bodies.
```

egoPoseStruct(1).States = egoState1;
egoPoseStruct(2).States = egoState2;

```

Increase the radius of the first ego body to 2 m .
egoGeomStruct(1).Geometry.Radius = 2;
update the ego bodies using the updateEgoPose and updateEgoGeometry object functions.
updateEgoPose(capsuleList,egoIDs,egoPoseStruct);
updateEgoGeometry (capsuleList, egoIDs, egoGeomStruct);
Visualize the ego bodies.
show(capsuleList, 'TimeStep',1:numSteps); axis equal


\section*{Remove Ego Body}

Remove the first ego body from the capsule list by specifying its ID.
```

removeEgo(capsuleList,1);

```

Visualize the ego bodies again.
show(capsuleList,'TimeStep',1:numSteps);
axis equal


\section*{Input Arguments}
capsuleListObj - Dynamic capsule list
dynamicCapsuleList object| dynamicCapsuleList3D object
Dynamic capsule list, specified as a dynamicCapsuleList or dynamicCapsuleList3D object.

\section*{selectEgoIDs - Ego body IDs}
vector of positive integers
Ego body IDs, specified as a vector of positive integers. The function returns the ego IDs and geometry parameters for only the ego bodies specified in this vector.

\section*{Output Arguments}
egoIDs - IDs of ego bodies
vector of positive integers
IDs of ego bodies, returned as a vector of positive integers.

\section*{geomStruct - Geometry parameters for ego bodies}
structure | structure array
Geometry parameters for ego bodies, returned as a structure or structure array where each structure contains the fields from the structure in the Geometry field of the associated ego body. The fields of
this structure depend on whether you are using a dynamicCapsuleList or dynamicCapsuleList3D object.

\section*{status - Indication of ego body existence}
\(N\)-element column vector
Indication of ego body existence, returned as a \(N\)-element column vector of ones, zeros, and negative ones. Each value indicates whether the associated body exists (1), updated (0), or a duplicate (-1). If you specify the same ego body ID more than once in the selectEgoIDs argument, then the function marks all instances of that ID after the first as duplicates and ignores them.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and C++ code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).

\section*{See Also}

\section*{Objects}
dynamicCapsuleList|dynamicCapsuleList3D

\section*{Functions}
addEgo| addObstacle |checkCollision |egoPose |obstacleGeometry |obstaclePose | removeEgo | removeObstacle | show | updateEgoGeometry |updateEgoPose |
updateObstacleGeometry|updateObstaclePose

\section*{Topics}
"Highway Trajectory Planning Using Frenet Reference Path"

\section*{Introduced in R2020b}

\section*{egoPose}

Poses of ego bodies

\section*{Syntax}
[egoIDs,poseStruct] = egoPose(capsuleListObj)
[egoIDs, poseStruct] = egoPose(capsuleListObj,selectEgoIDs)
[egoIDs,poseStruct,status] = egoPose(capsuleListObj,selectEgoIDs)

\section*{Description}
[egoIDs, poseStruct] = egoPose(capsuleListObj) returns the ego ID and the states for each ego body in the specified capsule list.
[egoIDs,poseStruct] = egoPose(capsuleListObj,selectEgoIDs) specifies which ego bodies to return the ID and states for.
[egoIDs,poseStruct,status] = egoPose(capsuleListObj,selectEgoIDs) returns an indicator of whether each ID in selectEgoIDs exists.

\section*{Examples}

\section*{Create and Modify Capsule-Based Ego Bodies}

Add ego bodies to an environment using the dynamicCapsuleList object. Modify the properties of the ego bodies. Remove an ego body from the environment. Visualize the states of all objects in the environment at different timestamps.

Create the dynamicCapsuleList object. Extract the maximum number of steps to use as the number of time stamps for the object paths.
```

capsuleList = dynamicCapsuleList;
numSteps = capsuleList.MaxNumSteps;

```

\section*{Add Ego Bodies}

Specify the states for the two ego bodies as a linear path from \(x=0 \mathrm{~m}\) to \(x=100 \mathrm{~m}\). The two ego bodies are separated by 5 m in opposite directions on the \(y\)-axis.
```

egoState = linspace(0,1,numSteps)'.*[100 0 0];
egoStatel = egoState+[0 5 0];
egoState2 = egoState+[0 -5 0];

```

Generate default poses and geometric structures for the two ego bodies using ego IDs.
```

[egoIDs,egoPoseStruct] = egoPose(capsuleList,[1 2]);
[egoIDs,egoGeomStruct] = egoGeometry(capsuleList,egoIDs);

```

\section*{Update Ego Bodies}

Assign the states to the ego bodies.
```

egoPoseStruct(1).States = egoState1;
egoPoseStruct(2).States = egoState2;

```

Increase the radius of the first ego body to 2 m .
egoGeomStruct(1).Geometry.Radius = 2;
update the ego bodies using the updateEgoPose and updateEgoGeometry object functions.
updateEgoPose(capsuleList,egoIDs,egoPoseStruct);
updateEgoGeometry (capsuleList, egoIDs, egoGeomStruct);
Visualize the ego bodies.
show(capsuleList, 'TimeStep',1:numSteps); axis equal


\section*{Remove Ego Body}

Remove the first ego body from the capsule list by specifying its ID.
```

removeEgo(capsuleList,1);

```

Visualize the ego bodies again.
show(capsuleList,'TimeStep',1:numSteps);
axis equal


\section*{Input Arguments}
capsuleListObj - Dynamic capsule list
dynamicCapsuleList object| dynamicCapsuleList3D object
Dynamic capsule list, specified as a dynamicCapsuleList or dynamicCapsuleList3D object.
```

selectEgoIDs - Ego body IDs

```
vector of positive integers
Ego body IDs, specified as a vector of positive integers. The function returns the ego IDs and states for only the ego bodies specified in this vector.

\section*{Output Arguments}
egoIDs - IDs of ego bodies
vector of positive integers
IDs of ego bodies, returned as a vector of positive integers.
poseStruct - States for ego bodies
structure | structure array

States for ego bodies, returned as a structure or structure array. Each structure contains a matrix of states for each ego body. The state matrix size depends on whether you are using a dynamicCapsuleList or dynamicCapsuleList3D object.
Data Types: struct

\section*{status - Indication of ego body existence}
\(N\)-element column vector
Indication of ego body existence, returned as a \(N\)-element column vector of ones, zeros, and negative ones. Each value indicates whether the associated body exists (1), updated (0), or a duplicate ( -1 ). If you specify the same ego body ID more than once in the selectEgoIDs argument, then the function marks all instances of that ID after the first as duplicates and ignores them.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).

\section*{See Also}

\section*{Objects}
dynamicCapsuleList|dynamicCapsuleList3D

\section*{Functions}
addEgo|addObstacle | checkCollision | egoGeometry| obstaclePose | removeEgo|
removeObstacle | show | updateEgoGeometry | updateEgoPose | updateObstacleGeometry |
updateObstaclePose

\section*{Topics}
"Highway Trajectory Planning Using Frenet Reference Path"

\section*{Introduced in R2020b}

\section*{obstacleGeometry}

Geometric properties of obstacles

\section*{Syntax}
```

[obstacleIDs,geomStruct] = obstacleGeometry(capsuleListObj)
[obstacleIDs,geomStruct] = obstacleGeometry(capsuleListObj,selectObstacleIDs)
[obstacleIDs,geomStruct,status] = obstacleGeometry(capsuleListObj,
selectObstacleIDs)

```

\section*{Description}
[obstacleIDs,geomStruct] = obstacleGeometry(capsuleListObj) returns the obstacle ID and the geometry parameters for each obstacle in the capsule list.
[obstacleIDs,geomStruct] = obstacleGeometry(capsuleList0bj,select0bstacleIDs) specifies which obstacle to return the ID and geometry parameters for.
[obstacleIDs,geomStruct,status] = obstacleGeometry(capsuleListObj, selectObstacleIDs) returns an indicator of whether each ID in selectobstacleIDs exists.

\section*{Examples}

\section*{Create and Modify Capsule-Based Obstacles}

Add obstacles to an environment using the dynamicCapsuleList object. Modify the properties of the obstacles. Remove an obstacle from the environment. Visualize the states of all objects in the environment at different timestamps.

Create the dynamicCapsuleList object. Extract the maximum number of steps to use as the number of time stamps for the object paths.
```

capsuleList = dynamicCapsuleList;
numSteps = capsuleList.MaxNumSteps;

```

\section*{Add Obstacles}

Specify the states for the two obstacles as a linear path from \(x=0 \mathrm{~m}\) to \(x=100 \mathrm{~m}\). The two obstacles are separated by 10 m in opposite directions on the \(y\)-axis.
```

obsState = linspace(0,1,numSteps)'.*[100 0 0];
obsState1 = obsState+[0 10 0];
obsState2 = obsState+[0 -10 0];

```

Generate default poses and geometric structures for the two obstacles using obstacle IDs.
```

[obsIDs,obsPoseStruct] = obstaclePose(capsuleList,[1 2]);
[obsIDs,obsGeomStruct] = obstacleGeometry(capsuleList,obsIDs);

```

\section*{Update Obstacles}

Assign the states to the obstacles.
```

obsPoseStruct(1).States = obsState1;
obsPoseStruct(2).States = obsState2;

```

Increase the radius of the first obstacle to 2 m .
obsGeomStruct(1).Geometry.Radius = 2;
update the obstacles using the updateObstaclePose and updateObstacleGeometry object functions.
updateObstaclePose(capsuleList,obsIDs,obsPoseStruct);
updateObstacleGeometry(capsuleList,obsIDs,obsGeomStruct);
Visualize the obstacles.
show(capsuleList,'TimeStep',1:numSteps);
axis equal


\section*{Remove Obstacles}

Remove the first obstacle from the capsule list by specifying its ID.
```

removeObstacle(capsuleList,1);

```

Visualize the obstacles again.
```

show(capsuleList,'TimeStep',1:numSteps);
axis equal

```


\section*{Input Arguments}
capsuleListObj - Dynamic capsule list
dynamicCapsuleList object| dynamicCapsuleList3D object
Dynamic capsule list, specified as a dynamicCapsuleList or dynamicCapsuleList3D object.

\section*{selectObstacleIDs - Obstacle IDs}
vector of positive integers
Obstacle IDs, specified as a vector of positive integers. The function returns the obstacle IDs and geometry parameters for only the obstacles specified in this vector.

\section*{Output Arguments}

\section*{obstacleIDs - IDs of obstacles}
vector of positive integers
IDs of obstacles, returned as a vector of positive integers.

\section*{geomStruct - Geometry parameters for obstacles}
structure | structure array

Geometry parameters for obstacles, returned as a structure or structure array where each structure contains the fields from the structure in the Geometry field of the associated obstacle. The fields of this structure depend on whether you are using a dynamicCapsuleList or dynamicCapsuleList3D object.

\section*{status - Indication of obstacle existence}
vector of ones, zeros, and negative ones
Indication of obstacle existence, returned as a \(N\)-element column vector of ones, zeros, and negative ones. Each value indicates whether the associated obstacle exists (1), updated (0), or a duplicate (-1). If you specify the same ego body ID more than once in the select0bstacleIDs argument, then the function marks all instances of that ID after the first as duplicates and ignores them.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® \({ }^{\circledR}\) Coder \(^{\text {TM }}\).

\section*{See Also}

\section*{Objects}
dynamicCapsuleList|dynamicCapsuleList3D

\section*{Functions}
addEgo|addObstacle | checkCollision | egoGeometry|egoPose|obstaclePose|
removeEgo | removeObstacle | show \| updateEgoGeometry | updateEgoPose |
updateObstacleGeometry|updateObstaclePose

\section*{Topics}
"Highway Trajectory Planning Using Frenet Reference Path"

\section*{Introduced in R2020b}

\section*{obstaclePose}

Poses of obstacles

\section*{Syntax}
```

[obstacleIDs,poseStruct] = obstaclePose(capsuleListObj)
[obstacleIDs,poseStruct] = obstaclePose(capsuleListObj,selectObstacleIDs)
[obstacleIDs,poseStruct,status] = obstaclePose(capsuleListObj,
selectObstacleIDs)

```

\section*{Description}
[obstacleIDs,poseStruct] = obstaclePose(capsuleListObj) returns the obstacle ID and states for each obstacle in the specified capsule list.
[obstacleIDs,poseStruct] = obstaclePose(capsuleList0bj, select0bstacleIDs) specifies which obstacles to return the ID and states for.
[obstacleIDs,poseStruct,status] = obstaclePose(capsuleListObj, selectObstacleIDs) returns an indicator of whether each ID in select0bstacleIDs exists.

\section*{Examples}

\section*{Create and Modify Capsule-Based Obstacles}

Add obstacles to an environment using the dynamicCapsuleList object. Modify the properties of the obstacles. Remove an obstacle from the environment. Visualize the states of all objects in the environment at different timestamps.

Create the dynamicCapsuleList object. Extract the maximum number of steps to use as the number of time stamps for the object paths.
```

capsuleList = dynamicCapsuleList;
numSteps = capsuleList.MaxNumSteps;

```

\section*{Add Obstacles}

Specify the states for the two obstacles as a linear path from \(x=0 \mathrm{~m}\) to \(x=100 \mathrm{~m}\). The two obstacles are separated by 10 m in opposite directions on the \(y\)-axis.
```

obsState = linspace(0,1,numSteps)'.*[100 0 0];
obsState1 = obsState+[0 10 0];
obsState2 = obsState+[0 -10 0];

```

Generate default poses and geometric structures for the two obstacles using obstacle IDs.
```

[obsIDs,obsPoseStruct] = obstaclePose(capsuleList,[1 2]);
[obsIDs,obsGeomStruct] = obstacleGeometry(capsuleList,obsIDs);

```

\section*{Update Obstacles}

Assign the states to the obstacles.
```

obsPoseStruct(1).States = obsState1;
obsPoseStruct(2).States = obsState2;

```

Increase the radius of the first obstacle to 2 m .
obsGeomStruct(1).Geometry.Radius = 2;
update the obstacles using the updateObstaclePose and updateObstacleGeometry object functions.
updateObstaclePose(capsuleList,obsIDs,obsPoseStruct);
updateObstacleGeometry(capsuleList,obsIDs,obsGeomStruct);
Visualize the obstacles.
show(capsuleList,'TimeStep',1:numSteps);
axis equal


\section*{Remove Obstacles}

Remove the first obstacle from the capsule list by specifying its ID.
```

removeObstacle(capsuleList,1);

```

Visualize the obstacles again.
```

show(capsuleList,'TimeStep',1:numSteps);
axis equal

```


\section*{Input Arguments}
capsuleListObj - Dynamic capsule list
dynamicCapsuleList object| dynamicCapsuleList3D object
Dynamic capsule list, specified as a dynamicCapsuleList or dynamicCapsuleList3D object.

\section*{selectObstacleIDs - Obstacle IDs}
vector of positive integers
Obstacle IDs, specified as a vector of positive integers. The function returns the obstacle IDs and states for only the obstacles specified in this vector.

\section*{Output Arguments}

\section*{obstacleIDs - IDs of obstacles}
vector of positive integers
IDs of obstacles, specified as a vector of positive integers.

\section*{poseStruct - States for ego bodies}
structure | structure array

States for obstacles, returned as a structure or structure array. Each structure contains a matrix of states for each obstacle. The state matrix size depends on whether you are using a dynamicCapsuleList or dynamicCapsuleList3D object.
Data Types: struct

\section*{status - Indication of obstacle existence}
\(N\)-element column vector
Indication of obstacle existence, returned as a \(N\)-element column vector of ones, zeros, and negative ones. Each value indicates whether the associated obstacle exists (1), updated (0), or a duplicate (-1). If you specify the same obstacle ID more than once in the select0bstacleIDs argument, then the function marks all instances of that ID after the first as duplicates and ignores them.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).

\section*{See Also}

\section*{Objects}
dynamicCapsuleList|dynamicCapsuleList3D

\section*{Functions}
addEgo | addObstacle | checkCollision | egoGeometry | egoPose | obstacleGeometry | removeEgo | removeObstacle | show | updateEgoGeometry | updateEgoPose |
updateObstacleGeometry|updateObstaclePose

\section*{Topics}
"Highway Trajectory Planning Using Frenet Reference Path"

\section*{Introduced in R2020b}

\section*{removeEgo}

Remove ego bodies from capsule list

\section*{Syntax}
removeEgo(capsuleListObj,egoIDs)
status = removeEgo(capsuleList0bj,egoIDs)

\section*{Description}
removeEgo(capsuleListObj, egoIDs) removes ego bodies with the specified IDs from the dynamic capsule list.
status = removeEgo(capsuleListObj,egoIDs) additionally returns an indicator of whether an ego body is removed, not found, or a duplicate.

\section*{Examples}

\section*{Create and Modify Capsule-Based Ego Bodies}

Add ego bodies to an environment using the dynamicCapsuleList object. Modify the properties of the ego bodies. Remove an ego body from the environment. Visualize the states of all objects in the environment at different timestamps.

Create the dynamicCapsuleList object. Extract the maximum number of steps to use as the number of time stamps for the object paths.
```

capsuleList = dynamicCapsuleList;
numSteps = capsuleList.MaxNumSteps;

```

\section*{Add Ego Bodies}

Specify the states for the two ego bodies as a linear path from \(x=0 \mathrm{~m}\) to \(x=100 \mathrm{~m}\). The two ego bodies are separated by 5 m in opposite directions on the \(y\)-axis.
```

egoState = linspace(0,1,numSteps)'.*[100 0 0];
egoState1 = egoState+[0 5 0];
egoState2 = egoState+[0 -5 0];

```

Generate default poses and geometric structures for the two ego bodies using ego IDs.
```

[egoIDs,egoPoseStruct] = egoPose(capsuleList,[1 2]);
[egoIDs,egoGeomStruct] = egoGeometry(capsuleList,egoIDs);

```

Update Ego Bodies
Assign the states to the ego bodies.
```

egoPoseStruct(1).States = egoState1;
egoPoseStruct(2).States = egoState2;

```

Increase the radius of the first ego body to 2 m .
egoGeomStruct(1).Geometry.Radius \(=2\);
update the ego bodies using the updateEgoPose and updateEgoGeometry object functions.
updateEgoPose(capsuleList,egoIDs,egoPoseStruct);
updateEgoGeometry(capsuleList,egoIDs,egoGeomStruct);
Visualize the ego bodies.
show(capsuleList,'TimeStep',1:numSteps);
axis equal


\section*{Remove Ego Body}

Remove the first ego body from the capsule list by specifying its ID.
```

removeEgo(capsuleList,1);

```

Visualize the ego bodies again.
```

show(capsuleList,'TimeStep',1:numSteps);
axis equal

```


\section*{Input Arguments}
capsuleListObj - Dynamic capsule list
dynamicCapsuleList object | dynamicCapsuleList3D object
Dynamic capsule list, specified as a dynamicCapsuleList or dynamicCapsuleList3D object.

\section*{egoIDs - IDs of ego bodies}
vector of positive integers
IDs of ego bodies to remove, specified as a vector of positive integers.

\section*{Output Arguments}

\section*{status - Result of removing ego bodies}
\(N\)-element column vector
Result of removing ego bodies, specified as \(N\)-element column vector of ones, zeros, and negative ones. \(N\) is the number of ego bodies specified in the egoIDs argument. Each value indicates whether the body is removed (1), not found (0), or a duplicate ( -1 ). If you specify the same ego ID multiple times in the egoIDs input argument, then all entries besides the last are marked as a duplicate.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).

\section*{See Also}

\section*{Objects}
dynamicCapsuleList|dynamicCapsuleList3D
Functions
addEgo | addObstacle | checkCollision | egoGeometry|egoPose |obstacleGeometry| obstaclePose | removeObstacle | show | updateEgoGeometry | updateEgoPose | updateObstacleGeometry|updateObstaclePose

\section*{Topics}
"Highway Trajectory Planning Using Frenet Reference Path"

\section*{Introduced in R2020b}

\section*{removeObstacle}

Remove obstacles from capsule list

\section*{Syntax}
removeObstacle(capsuleListObj,obstacleIDs)
status = removeObstacle(capsuleListObj,obstacleIDs)

\section*{Description}
removeObstacle(capsuleListObj,obstacleIDs) removes obstacles with the specified IDs from the dynamic capsule list.
status = removeObstacle(capsuleListObj,obstacleIDs) additionally returns an indicator of whether an obstacles is removed, not found, or a duplicate.

\section*{Examples}

\section*{Create and Modify Capsule-Based Obstacles}

Add obstacles to an environment using the dynamicCapsuleList object. Modify the properties of the obstacles. Remove an obstacle from the environment. Visualize the states of all objects in the environment at different timestamps.

Create the dynamicCapsuleList object. Extract the maximum number of steps to use as the number of time stamps for the object paths.
```

capsuleList = dynamicCapsuleList;
numSteps = capsuleList.MaxNumSteps;

```

\section*{Add Obstacles}

Specify the states for the two obstacles as a linear path from \(x=0 \mathrm{~m}\) to \(x=100 \mathrm{~m}\). The two obstacles are separated by 10 m in opposite directions on the \(y\)-axis.
```

obsState = linspace(0,1,numSteps)'.*[100 0 0];
obsState1 = obsState+[0 10 0];
obsState2 = obsState+[0 -10 0];

```

Generate default poses and geometric structures for the two obstacles using obstacle IDs.
```

[obsIDs,obsPoseStruct] = obstaclePose(capsuleList,[1 2]);
[obsIDs,obsGeomStruct] = obstacleGeometry(capsuleList,obsIDs);

```

Update Obstacles
Assign the states to the obstacles.
```

obsPoseStruct(1).States = obsStatel;
obsPoseStruct(2).States = obsState2;

```

Increase the radius of the first obstacle to 2 m .
obsGeomStruct(1).Geometry.Radius = 2;
update the obstacles using the updateObstaclePose and updateObstacleGeometry object functions.
updateObstaclePose(capsuleList,obsIDs,obsPoseStruct);
updateObstacleGeometry (capsuleList,obsIDs, obsGeomStruct);
Visualize the obstacles.
```

show(capsuleList,'TimeStep',1:numSteps);

```
axis equal


\section*{Remove Obstacles}

Remove the first obstacle from the capsule list by specifying its ID.
```

removeObstacle(capsuleList,1);

```

Visualize the obstacles again.
```

show(capsuleList,'TimeStep',1:numSteps);
axis equal

```


\section*{Input Arguments}

\section*{capsuleListObj - Dynamic capsule list}
dynamicCapsuleList object| dynamicCapsuleList3D object
Dynamic capsule list, specified as a dynamicCapsuleList or dynamicCapsuleList3D object.

\section*{obstacleIDs - IDs of obstacles}
vector of positive integers
IDs of obstacles to remove, specified as a vector of positive integers.

\section*{Output Arguments}

\section*{status - Result of removing obstacles}
\(N\)-element column vector
Result of removing obstacles, specified as \(N\)-element column vector of ones, zeros, and negative ones. \(N\) is the number of obstacles specified in the obstacleIDs argument. Each value indicates whether the obstacle is removed (1), not found (0), or a duplicate ( -1 ). If you specify the same obstacle ID multiple times in the obstacleIDs input argument, then all entries besides the last are marked as a duplicate.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).

\section*{See Also}

\section*{Objects}
dynamicCapsuleList|dynamicCapsuleList3D

\section*{Functions}
addEgo | addObstacle | checkCollision | egoGeometry | egoPose | obstacleGeometry | obstaclePose | removeEgo | show | updateEgoGeometry | updateEgoPose |
updateObstacleGeometry|updateObstaclePose

\section*{Topics}
"Highway Trajectory Planning Using Frenet Reference Path"

\section*{Introduced in R2020b}

\section*{show}

Display ego bodies and obstacles in environment

\section*{Syntax}
```

ax = show(capsuleListObj)
ax = show(capsuleListObj,Name,Value)

```

\section*{Description}
ax = show(capsuleList0bj) displays the initial state of all ego bodies and obstacles in the specified capsule list, and returns the axes handle of the plot.
ax = show(capsuleListObj,Name, Value) specifies options using name-value pair arguments on page 2-265. For example, 'FastUpdate', true enables fast updates to an existing plot.

\section*{Examples}

\section*{Build Ego Body Paths and Check for Collisions with Obstacles}

Build an ego body path and maintain obstacle states using the dynamicCapsuleList object. Visualize the states of all objects in the environment at different timestamps. Validate the path of the ego body by checking for collisions with obstacles in the environment.

Create the dynamicCapsuleList object. Extract the maximum number of steps to use as the number of time stamps for your object paths.
```

obsList = dynamicCapsuleList;
numSteps = obsList.MaxNumSteps;

```

\section*{Add Ego Body}

Define an ego body by specifying the ID, geometry, and state together in a structure. The capsule geometry has a length of 3 m and radius of 1 m . Specify the state as a linear path from \(x=0 \mathrm{~m}\) to \(x=\) 100 m .
```

egoID1 = 1;
geom = struct("Length",3,"Radius",1,"FixedTransform",eye(3));
states = linspace(0,1,obsList.MaxNumSteps)'.*[100 0 0];
egoCapsule1 = struct('ID',egoID1,'States',states,'Geometry',geom);
addEgo(obsList,egoCapsule1);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])

```


\section*{Add Obstacles}

Specify states for two obstacles that are separated from the ego body by 5 m in opposite directions on the \(y\)-axis.. Assume the obstacles have the same geometry geom as the ego body.
```

obsStatel = states + [0 5 0];
obsState2 = states + [0 -5 0];
obsCapsule1 = struct('ID',1,'States',obsState1,'Geometry',geom);
obsCapsule2 = struct('ID',2,'States',obsState2,'Geometry',geom);
addObstacle(obsList,obsCapsule1);
addObstacle(obsList,obsCapsule2);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])

```


\section*{Update Obstacles}

Alter your obstacle locations and geometry dimensions over time. Use the previously generated structure, modify the fields, and update the obstacles using the update0bstacleGeometry and update0bstaclePose object functions. Reduces the radius of the first obstacle to 0.5 m , and change the path to move it towards the ego body.
```

obsCapsule1.Geometry.Radius = 0.5;
obsCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
linspace(5,-4,numSteps)' ... % y
zeros(numSteps,1)]; % theta
updateObstacleGeometry(obsList,1,obsCapsule1);
updateObstaclePose(obsList,1,obsCapsule1);

```

\section*{Check for Collisions}

Visualize the new paths. Show where collisions between the ego body and an obstacle, which the display highlights in red. Notice that collisions between the obstacles are not checked.
```

show(obsList,"TimeStep",[1:numSteps],"ShowCollisions",1);
ylim([-20 20])
xlabel("X (m)")
ylabel("Y (m)")

```


Programmatically check for collisions by using the checkCollision object function. The function returns a vector of logical values that indicates the status of each time step. The vector is transposed for display purposes.
```

collisions = checkCollision(obsList)'
collisions = 1x31 logical array

```
\begin{tabular}{lllllllllllllllllllllllll}
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 0
\end{tabular}

To validate paths with a large number of steps, use the any function on the vector of collision values.
```

if any(collisions)
disp("Collision detected.")
end
Collision detected.

```

\section*{Update Ego Path}

Specify a new path for the ego body. Visualize the paths again, displaying collisions.
```

egoCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
3*sin(linspace(0,2*pi,numSteps))' ... % y
zeros(numSteps,1)]; % theta

```
```

updateEgoPose(obsList,1,egoCapsule1);
show(obsList,"TimeStep",[1:numSteps],"ShowCollisions",1);
ylim([-20 20])

```


\section*{Input Arguments}
capsuleListObj - Dynamic capsule list
dynamicCapsuleList object| dynamicCapsuleList3D object
Dynamic capsule list, specified as a dynamicCapsuleList or dynamicCapsuleList3D object.

\section*{Name-Value Pair Arguments}

Specify optional pairs of arguments as Namel=Value1, ... ,NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: 'FastUpdate' , true enables the option for fast updates in an existing plot.

\section*{Parent - Parent axes to plot on}
gca (default) | Axes handle
Parent axes to plot on, specified as the comma-separated pair consisting of 'Parent ' and an Axes handle.

\section*{FastUpdate - Perform fast update to existing plot false or 0 (default) | true or 1}

Perform a fast update to an existing plot, specified as the comma-separated pair consisting of ' FastUpdate' and a logical 0 (false) or 1 (true). You must use the show object function to initially display your capsule list before you can specify it with this argument.

Data Types: logical

\section*{TimeStep - Time steps to display}

1 (default) | numeric vector
Time steps to display, specified as the comma-separated pair consisting of 'TimeStep ' and numeric vector of values in the range \([1, N]\), where \(N\) is the value of the MaxNumSteps property of the object specified in the capsuleList0bj argument. Each time step corresponds to a row of the state matrix for each ego body and obstacle.

\section*{ShowCollisions - Check for and highlight collisions in display \\ false or 0 (default) | true or 1}

Check for and highlight collisions in the display, specified as the comma-separated pair consisting of 'ShowCollisions ' and a logical 0 (false) or 1 (true).
Data Types: logical

\section*{EgoIDs - Ego IDs to display}
vector of positive integers
Ego IDs to display, specified as the comma-separated pair consisting of 'EgoIDs ' and a vector of positive integers. By default, the object function displays all ego bodies.

\section*{ObstacleIDs - Obstacle IDs to display}
vector of positive integers
Obstacle IDs to display, specified as the comma-separated pair consisting of 'ObstacleIDs ' and a vector of positive integers. By default, the function displays all obstacles.

\section*{Output Arguments}
ax - Parent axes of dynamic capsule list plot
Axes handle
Parent axes of the dynamic capsule list plot, returned as anAxes handle.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder \(^{\text {TM }}\).

\section*{See Also}

\section*{Objects}
dynamicCapsuleList|dynamicCapsuleList3D

\author{
Functions \\ addEgo| addObstacle | checkCollision | egoGeometry | egoPose |obstacleGeometry| obstaclePose|removeEgo| removeObstacle|updateEgoGeometry|updateEgoPose| updateObstacleGeometry|updateObstaclePose \\ \section*{Topics} \\ "Highway Trajectory Planning Using Frenet Reference Path" \\ Introduced in R2020b
}

\section*{updateEgoGeometry}

Update geometric properties of ego bodies

\section*{Syntax}
updateEgoGeometry(capsuleListObj, egoIDs, geomStruct)
status = updateEgoGeometry(capsuleList0bj, egoIDs,geomStruct)

\section*{Description}
updateEgoGeometry(capsuleListObj, egoIDs, geomStruct) updates geometry parameters for the specified ego bodies in the capsule list. If a specified ego ID does not already exist, the function adds a new ego body with that ID to the list.
status = updateEgoGeometry(capsuleList0bj,egoIDs,geomStruct) additionally returns an indicator of whether an ego body is added, updated, or a duplicate.

\section*{Examples}

\section*{Create and Modify Capsule-Based Ego Bodies}

Add ego bodies to an environment using the dynamicCapsuleList object. Modify the properties of the ego bodies. Remove an ego body from the environment. Visualize the states of all objects in the environment at different timestamps.

Create the dynamicCapsuleList object. Extract the maximum number of steps to use as the number of time stamps for the object paths.
```

capsuleList = dynamicCapsuleList;
numSteps = capsuleList.MaxNumSteps;

```

\section*{Add Ego Bodies}

Specify the states for the two ego bodies as a linear path from \(x=0 \mathrm{~m}\) to \(x=100 \mathrm{~m}\). The two ego bodies are separated by 5 m in opposite directions on the \(y\)-axis.
```

egoState = linspace(0,1,numSteps)'.*[100 0 0];
egoState1 = egoState+[0 5 0];
egoState2 = egoState+[0 -5 0];

```

Generate default poses and geometric structures for the two ego bodies using ego IDs.
```

[egoIDs,egoPoseStruct] = egoPose(capsuleList,[1 2]);
[egoIDs,egoGeomStruct] = egoGeometry(capsuleList,egoIDs);

```

\section*{Update Ego Bodies}

Assign the states to the ego bodies.
```

egoPoseStruct(1).States = egoState1;
egoPoseStruct(2).States = egoState2;

```

Increase the radius of the first ego body to 2 m .
```

egoGeomStruct(1).Geometry.Radius = 2;

```
update the ego bodies using the updateEgoPose and updateEgoGeometry object functions.
```

updateEgoPose(capsuleList,egoIDs,egoPoseStruct);

```
updateEgoGeometry(capsuleList,egoIDs,egoGeomStruct);

Visualize the ego bodies.
show(capsuleList, 'TimeStep',1:numSteps);
axis equal


\section*{Remove Ego Body}

Remove the first ego body from the capsule list by specifying its ID.
```

removeEgo(capsuleList,1);

```

Visualize the ego bodies again.
```

show(capsuleList,'TimeStep',1:numSteps);
axis equal

```


\section*{Input Arguments}
capsuleListObj - Dynamic capsule list
dynamicCapsuleList object| dynamicCapsuleList3D object
Dynamic capsule list, specified as a dynamicCapsuleList or dynamicCapsuleList3D object.
egoIDs - IDs of ego bodies to update
vector of positive integers
IDs of ego bodies to update, specified as a vector of positive integers.

\section*{geomStruct - Geometry parameters for ego bodies}
structure | structure array
Geometry parameters for ego bodies, specified as a structure or structure array, where each structure contains the fields of the structure in the Geometry field of the ego body to be updated. The fields of this structure depend on whether you are using a dynamicCapsuleList or dynamicCapsuleList3D object.
Data Types: struct

\section*{Output Arguments}

\section*{status - Result of updating ego bodies}
\(N\)-element column vector

Result of updating ego bodies, specified as \(N\)-element column vector of ones, zeros, and negative ones. \(N\) is the number of ego bodies specified in the egoIDs argument. Each value indicates whether the body is removed (1), not found (0), or a duplicate ( -1 ). If you specify the same ego ID multiple times in the egoIDs input argument, then all entries besides the last are marked as a duplicate.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).

\section*{See Also}

\section*{Objects}
dynamicCapsuleList|dynamicCapsuleList3D

\section*{Functions}
addEgo |addObstacle | checkCollision | egoGeometry | egoPose | obstacleGeometry | obstaclePose | removeEgo | removeObstacle | show | updateEgoPose|
updateObstacleGeometry|updateObstaclePose

\section*{Topics}
"Highway Trajectory Planning Using Frenet Reference Path"
Introduced in R2020b

\section*{updateEgoPose}

Update states of ego bodies

\section*{Syntax}
updateEgoPose(capsuleList0bj, egoIDs, poseStruct)
status = updateEgoPose(capsuleList0bj,egoIDs,poseStruct)

\section*{Description}
updateEgoPose(capsuleListObj, egoIDs, poseStruct) updates the states of the specified ego bodies in the capsule list. If a specified ego ID does not already exist, the function adds a new ego body with that ID to the list.
status = updateEgoPose(capsuleListObj,egoIDs,poseStruct) returns an indicator of whether an ego body is added, updated, or a duplicate.

\section*{Examples}

\section*{Build Ego Body Paths and Check for Collisions with Obstacles}

Build an ego body path and maintain obstacle states using the dynamicCapsuleList object. Visualize the states of all objects in the environment at different timestamps. Validate the path of the ego body by checking for collisions with obstacles in the environment.

Create the dynamicCapsuleList object. Extract the maximum number of steps to use as the number of time stamps for your object paths.
```

obsList = dynamicCapsuleList;
numSteps = obsList.MaxNumSteps;

```

\section*{Add Ego Body}

Define an ego body by specifying the ID, geometry, and state together in a structure. The capsule geometry has a length of 3 m and radius of 1 m . Specify the state as a linear path from \(x=0 \mathrm{~m}\) to \(x=\) 100 m .
```

egoID1 = 1;
geom = struct("Length",3,"Radius",1,"FixedTransform",eye(3));
states = linspace(0,1,obsList.MaxNumSteps)'.*[100 0 0];
egoCapsule1 = struct('ID',egoID1,'States',states,'Geometry',geom);
addEgo(obsList,egoCapsule1);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])

```


\section*{Add Obstacles}

Specify states for two obstacles that are separated from the ego body by 5 m in opposite directions on the \(y\)-axis.. Assume the obstacles have the same geometry geom as the ego body.
```

obsStatel = states + [0 5 0];
obsState2 = states + [0 -5 0];
obsCapsule1 = struct('ID',1,'States',obsState1,'Geometry',geom);
obsCapsule2 = struct('ID',2,'States',obsState2,'Geometry',geom);
addObstacle(obsList,obsCapsule1);
addObstacle(obsList,obsCapsule2);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])

```


\section*{Update Obstacles}

Alter your obstacle locations and geometry dimensions over time. Use the previously generated structure, modify the fields, and update the obstacles using the updateObstacleGeometry and updateObstaclePose object functions. Reduces the radius of the first obstacle to 0.5 m , and change the path to move it towards the ego body.
```

obsCapsule1.Geometry.Radius = 0.5;
obsCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
linspace(5,-4,numSteps)' ... % y
zeros(numSteps,1)]; % theta
updateObstacleGeometry(obsList,1,obsCapsule1);
updateObstaclePose(obsList,1,obsCapsule1);

```

\section*{Check for Collisions}

Visualize the new paths. Show where collisions between the ego body and an obstacle, which the display highlights in red. Notice that collisions between the obstacles are not checked.
```

show(obsList,"TimeStep",[1:numSteps],"ShowCollisions",1);
ylim([-20 20])
xlabel("X (m)")
ylabel("Y (m)")

```


Programmatically check for collisions by using the checkCollision object function. The function returns a vector of logical values that indicates the status of each time step. The vector is transposed for display purposes.
```

collisions = checkCollision(obsList)'
collisions = 1x31 logical array
0

```

To validate paths with a large number of steps, use the any function on the vector of collision values.
```

if any(collisions)
disp("Collision detected.")
end
Collision detected.

```

\section*{Update Ego Path}

Specify a new path for the ego body. Visualize the paths again, displaying collisions.
```

egoCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
3*sin(linspace(0,2*pi,numSteps))' ... % y
zeros(numSteps,1)]; % theta

```
updateEgoPose(obsList,1,egoCapsule1);
show(obsList,"TimeStep", [1:numSteps],"ShowCollisions",1);
ylim([-20 20])


\section*{Input Arguments}

\section*{capsuleListObj - Dynamic capsule list}
dynamicCapsuleList object| dynamicCapsuleList3D object
Dynamic capsule list, specified as a dynamicCapsuleList or dynamicCapsuleList3D object.

\section*{egoIDs - IDs of ego bodies to update}
vector of positive integers
IDs of ego bodies to update, specified as a vector of positive integers.

\section*{poseStruct - States for ego bodies}
structure | structure array
States for ego bodies, specified as a structure array or structure array, where each structure contains the fields of the structure in the Geometry field of the ego body to be updated. Each element of the structure array contains a matrix of states for each ego body. The state matrix size depends on whether you are using a dynamicCapsuleList or dynamicCapsuleList3D object.

Data Types: struct

\section*{Output Arguments}

\section*{status - Result of updating ego bodies}
\(N\)-element column vector
Result of updating ego bodies, specified as \(N\)-element column vector of ones, zeros, and negative ones. \(N\) is the number of ego bodies specified in the egoIDs argument. Each value indicates whether the body is updated (1), not found (0), or a duplicate ( -1 ). If you specify the same ego ID multiple times in the egoIDs input argument, then all entries besides the last are marked as a duplicate.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and C++ code using MATLAB® \({ }^{\circledR}\) Coder \(^{\text {TM }}\).

\section*{See Also}

\section*{Objects}
dynamicCapsuleList|dynamicCapsuleList3D

\section*{Functions}
addEgo |addObstacle | checkCollision | egoGeometry | egoPose | obstacleGeometry | obstaclePose | removeEgo | removeObstacle | show | updateEgoGeometry| updateObstacleGeometry|updateObstaclePose

\section*{Topics}
"Highway Trajectory Planning Using Frenet Reference Path"
Introduced in R2020b

\section*{updateObstacleGeometry}

Update geometric properties of obstacles

\section*{Syntax}
updateObstacleGeometry(capsuleListObj,obstacleIDs, geomStruct)
status = updateObstacleGeometry(capsuleListObj,obstacleIDs,geomStruct)

\section*{Description}
updateObstacleGeometry (capsuleListObj, obstacleIDs,geomStruct) updates geometry parameters for the specified obstacles in the capsule list. If a specified obstacle ID does not already exist, the function adds a new obstacle with that ID to the list.
status = updateObstacleGeometry(capsuleListObj,obstacleIDs,geomStruct) returns an indicator of whether an obstacle is added, updated, or a duplicate.

\section*{Examples}

\section*{Build Ego Body Paths and Check for Collisions with Obstacles}

Build an ego body path and maintain obstacle states using the dynamicCapsuleList object. Visualize the states of all objects in the environment at different timestamps. Validate the path of the ego body by checking for collisions with obstacles in the environment.

Create the dynamicCapsuleList object. Extract the maximum number of steps to use as the number of time stamps for your object paths.
```

obsList = dynamicCapsuleList;
numSteps = obsList.MaxNumSteps;

```

\section*{Add Ego Body}

Define an ego body by specifying the ID, geometry, and state together in a structure. The capsule geometry has a length of 3 m and radius of 1 m . Specify the state as a linear path from \(x=0 \mathrm{~m}\) to \(x=\) 100 m .
```

egoID1 = 1;
geom = struct("Length",3,"Radius",1,"FixedTransform",eye(3));
states = linspace(0,1,obsList.MaxNumSteps)'.*[100 0 0];
egoCapsule1 = struct('ID',egoID1,'States',states,'Geometry',geom);
addEgo(obsList,egoCapsule1);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])

```


\section*{Add Obstacles}

Specify states for two obstacles that are separated from the ego body by 5 m in opposite directions on the \(y\)-axis.. Assume the obstacles have the same geometry geom as the ego body.
```

obsStatel = states + [0 5 0];
obsState2 = states + [0 -5 0];
obsCapsule1 = struct('ID',1,'States',obsState1,'Geometry',geom);
obsCapsule2 = struct('ID',2,'States',obsState2,'Geometry',geom);
addObstacle(obsList,obsCapsule1);
addObstacle(obsList,obsCapsule2);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])

```


\section*{Update Obstacles}

Alter your obstacle locations and geometry dimensions over time. Use the previously generated structure, modify the fields, and update the obstacles using the updateObstacleGeometry and updateObstaclePose object functions. Reduces the radius of the first obstacle to 0.5 m , and change the path to move it towards the ego body.
```

obsCapsule1.Geometry.Radius = 0.5;
obsCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
linspace(5,-4,numSteps)' ... % y
zeros(numSteps,1)]; % theta
updateObstacleGeometry(obsList,1,obsCapsule1);
updateObstaclePose(obsList,1,obsCapsule1);

```

\section*{Check for Collisions}

Visualize the new paths. Show where collisions between the ego body and an obstacle, which the display highlights in red. Notice that collisions between the obstacles are not checked.
```

show(obsList,"TimeStep",[1:numSteps],"ShowCollisions",1);
ylim([-20 20])
xlabel("X (m)")
ylabel("Y (m)")

```


Programmatically check for collisions by using the checkCollision object function. The function returns a vector of logical values that indicates the status of each time step. The vector is transposed for display purposes.
```

collisions = checkCollision(obsList)'
collisions = 1x31 logical array

```
\begin{tabular}{lllllllllllllllllllllllll}
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 0
\end{tabular}

To validate paths with a large number of steps, use the any function on the vector of collision values.
```

if any(collisions)
disp("Collision detected.")
end
Collision detected.

```

\section*{Update Ego Path}

Specify a new path for the ego body. Visualize the paths again, displaying collisions.
```

egoCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
3*sin(linspace(0,2*pi,numSteps))' ... % y
zeros(numSteps,1)]; % theta

```
updateEgoPose(obsList,1,egoCapsule1);
show(obsList,"TimeStep", [1:numSteps],"ShowCollisions",1);
ylim([-20 20])


\section*{Input Arguments}

\section*{capsuleListObj - Dynamic capsule list}
dynamicCapsuleList object| dynamicCapsuleList3D object
Dynamic capsule list, specified as a dynamicCapsuleList or dynamicCapsuleList3D object.

\section*{obstacleIDs - IDs of obstacles to update}
vector of positive integers
IDs of obstacles to update, specified as a vector of positive integers.

\section*{geomStruct - Geometry parameters for ego bodies}
structure | structure array
Geometry parameters for ego bodies, specified as a structure or structure array, where each structure contains the fields of the structure in the Geometry field of the obstacle to be updated.. The fields of this structure depend on whether you are using a dynamicCapsuleList or dynamicCapsuleList3D object.

Data Types: struct

\section*{Output Arguments}

\section*{status - Result of updating obstacles}
\(N\)-element column vector
Result of updating obstacles, specified as \(N\)-element column vector of ones, zeros, and negative ones. \(N\) is the number of obstacles specified in the obstacleIDs argument. Each value indicates whether the obstacle is removed (1), not found (0), or a duplicate ( -1 ). If you specify the same obstacle ID multiple times in the obstacleIDs input argument, then all entries besides the last are marked as a duplicate.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and C++ code using MATLAB® Coder \(^{\text {TM }}\).

\section*{See Also}

\section*{Objects}
dynamicCapsuleList|dynamicCapsuleList3D

\section*{Functions}
addEgo | addObstacle | checkCollision | egoGeometry | egoPose | obstacleGeometry | obstaclePose | removeEgo | removeObstacle | show \| updateEgoGeometry |updateEgoPose | updateObstaclePose

Topics
"Highway Trajectory Planning Using Frenet Reference Path"
Introduced in R2020b

\section*{updateObstaclePose}

\author{
Update states of obstacles
}

\section*{Syntax}
updateObstaclePose(capsuleListObj,obstacleIDs, poseStruct)
status = updateObstaclePose(capsuleList0bj,obstacleIDs,poseStruct)

\section*{Description}
updateObstaclePose(capsuleListObj, obstacleIDs, poseStruct) updates the states of the specified obstacles in the capsule list. If a specified obstacle ID does not already exist, the function adds a new ego body with that ID to the list.
status = updateObstaclePose(capsuleListObj,obstacleIDs, poseStruct) returns an indicator of whether an obstacle is added, updated, or a duplicate.

\section*{Examples}

\section*{Build Ego Body Paths and Check for Collisions with Obstacles}

Build an ego body path and maintain obstacle states using the dynamicCapsuleList object. Visualize the states of all objects in the environment at different timestamps. Validate the path of the ego body by checking for collisions with obstacles in the environment.

Create the dynamicCapsuleList object. Extract the maximum number of steps to use as the number of time stamps for your object paths.
```

obsList = dynamicCapsuleList;
numSteps = obsList.MaxNumSteps;

```

\section*{Add Ego Body}

Define an ego body by specifying the ID, geometry, and state together in a structure. The capsule geometry has a length of 3 m and radius of 1 m . Specify the state as a linear path from \(x=0 \mathrm{~m}\) to \(x=\) 100 m .
```

egoID1 = 1;
geom = struct("Length",3,"Radius",1,"FixedTransform",eye(3));
states = linspace(0,1,obsList.MaxNumSteps)'.*[100 0 0];
egoCapsule1 = struct('ID',egoID1,'States',states,'Geometry',geom);
addEgo(obsList,egoCapsule1);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])

```


\section*{Add Obstacles}

Specify states for two obstacles that are separated from the ego body by 5 m in opposite directions on the \(y\)-axis.. Assume the obstacles have the same geometry geom as the ego body.
```

obsStatel = states + [0 5 0];
obsState2 = states + [0 -5 0];
obsCapsule1 = struct('ID',1,'States',obsState1,'Geometry',geom);
obsCapsule2 = struct('ID',2,'States',obsState2,'Geometry',geom);
addObstacle(obsList,obsCapsule1);
addObstacle(obsList,obsCapsule2);
show(obsList,"TimeStep",[1:numSteps]);
ylim([-20 20])

```


\section*{Update Obstacles}

Alter your obstacle locations and geometry dimensions over time. Use the previously generated structure, modify the fields, and update the obstacles using the updateObstacleGeometry and updateObstaclePose object functions. Reduces the radius of the first obstacle to 0.5 m , and change the path to move it towards the ego body.
```

obsCapsule1.Geometry.Radius = 0.5;
obsCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
linspace(5,-4,numSteps)' ... % y
zeros(numSteps,1)]; % theta
updateObstacleGeometry(obsList,1,obsCapsule1);
updateObstaclePose(obsList,1,obsCapsule1);

```

\section*{Check for Collisions}

Visualize the new paths. Show where collisions between the ego body and an obstacle, which the display highlights in red. Notice that collisions between the obstacles are not checked.
```

show(obsList,"TimeStep",[1:numSteps],"ShowCollisions",1);
ylim([-20 20])
xlabel("X (m)")
ylabel("Y (m)")

```


Programmatically check for collisions by using the checkCollision object function. The function returns a vector of logical values that indicates the status of each time step. The vector is transposed for display purposes.
```

collisions = checkCollision(obsList)'
collisions = 1x31 logical array

```
\begin{tabular}{lllllllllllllllllllllllll}
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 0
\end{tabular}

To validate paths with a large number of steps, use the any function on the vector of collision values.
```

if any(collisions)
disp("Collision detected.")
end
Collision detected.

```

\section*{Update Ego Path}

Specify a new path for the ego body. Visualize the paths again, displaying collisions.
```

egoCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
3*sin(linspace(0,2*pi,numSteps))' ... % y
zeros(numSteps,1)]; % theta

```
updateEgoPose(obsList,1,egoCapsule1);
show(obsList,"TimeStep", [1:numSteps],"ShowCollisions",1);
ylim([-20 20])


\section*{Input Arguments}

\section*{capsuleListObj - Dynamic capsule list}
dynamicCapsuleList object| dynamicCapsuleList3D object
Dynamic capsule list, specified as a dynamicCapsuleList or dynamicCapsuleList3D object.

\section*{obstacleIDs - IDs of obstacles to update}
vector of positive integers
IDs of obstacles to update, specified as a vector of positive integers.

\section*{poseStruct - States for obstacles}
structure | structure array
States for ego bodies, specified as a structure or structure array, where each structure contains the fields of the structure in the Geometry field of the obstacle to be updated. Each element of the structure array contains a matrix of states for each ego body. The state matrix size depends on whether you are using a dynamicCapsuleList or dynamicCapsuleList3D object.

Data Types: struct

\section*{Output Arguments}

\section*{status - Result of updating obstacles}
\(N\)-element column vector
Result of updating obstacles, specified as \(N\)-element column vector of ones, zeros, and negative ones. \(N\) is the number of obstacles specified in the obstacleIDs argument. Each value indicates whether the obstacle is removed (1), not found (0), or a duplicate ( -1 ). If you specify the same obstacle ID multiple times in the obstacleIDs input argument, then all entries besides the last are marked as a duplicate.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and C++ code using MATLAB® Coder \(^{\text {TM }}\).

\section*{See Also}

\section*{Objects}
dynamicCapsuleList|dynamicCapsuleList3D

\section*{Functions}
addEgo | addObstacle | checkCollision | egoGeometry | egoPose | obstacleGeometry | obstaclePose | removeEgo | removeObstacle | show | updateEgoGeometry |updateEgoPose | updateObstacleGeometry

\section*{Topics}
"Highway Trajectory Planning Using Frenet Reference Path"
Introduced in R2020b

\section*{dynamicCapsuleList3D}

Dynamic capsule-based obstacle list

\section*{Description}

The dynamicCapsuleList3D object manages two lists of capsule-based collision objects in 3-D space. Collision objects are separated into two lists, ego bodies and obstacles. For ego bodies and obstacles in 2-D, see the dynamicCapsuleList object.

Each collision object in the two lists has three key elements:
- ID -- Integer that identifies each object, stored in the EgoIDs property for ego bodies and the ObstacleIDs property for obstacles.
- States -- Location and orientation of the object as an \(M\)-by-6 matrix, where each row is of form [x y z qW qX qY qZ], and \(M\) is the number of states along the path of the object in the world frame. The list of states assumes each state is separated by a fixed time interval. xyz-positions are in meters, and the orientation is a four-element quaternion vector. The default local origin is located at the center of the left hemisphere of the capsule.
- Geometry -- Size of the capsule-based object based on the specified length and radius. The radius applies to the spherical ends, and the length applies to the cylinder length. To shift the capsule geometry and local origin relative to the default origin point, specify a 4 -by- 4 transform relative to the local frame of the capsule. To keep the default transform, specify eye (4).


States: \(\quad[x y z q W q X q Y q Z]\)
Geometry: Radius
Length
FixedTransform*
* \(=\) Not Pictured

Use the object functions to dynamically add, remove, and update the geometries and states of the various objects in your environment. To add an ego body, see the addEgo object function. To add an obstacle, see the addObstacle object function.

After specifying all the object paths, validate the ego-body paths and check for collisions with obstacles at every step using the checkCollision object function. The function only checks if an ego body collides with an obstacle, ignoring collisions between only obstacles or only ego bodies.

\section*{Creation}

\section*{Syntax}
obstacleList \(=\) dynamicCapsuleList3D

\section*{Description}
obstacleList = dynamicCapsuleList3D creates a dynamic capsule-based obstacle list with no ego bodies or obstacles. To begin building an obstacle list, use the addEgo or addObstacle object functions.

\section*{Properties}

MaxNumSteps - Maximum number of time steps in obstacle list
31 (default) | positive integer
Maximum number of time steps in the obstacle list, specified as a positive integer. The number of steps determines to the maximum length of the States field for a specific ego body or obstacle.
Data Types: double

\section*{EgoIDs - List of IDs for ego bodies}
vector of positive integers
This property is read-only.
List of identifiers for ego bodies, returned as a vector of positive integers.
Data Types: double

\section*{ObstacleIDs - IDs for obstacles}
vector of positive integers
This property is read-only.
List of identifiers for obstacles, returned as a vector of positive integers.

\section*{Data Types: double}

\section*{NumObstacles - Number of obstacles in list}
integer
This property is read-only.
Number of obstacles in list, returned as an integer.
Data Types: double
NumEgos - Number of ego bodies in list
integer

This property is read-only.
Number of ego bodies in list, returned as an integer.
Data Types: double

\section*{Object Functions}
addEgo
addObstacle
checkCollision
egoGeometry
egoPose
obstacleGeometry
obstaclePose
removeEgo
removeObstacle
show
updateEgoGeometry
updateEgoPose
updateObstacleGeometry
updateObstaclePose

Add ego bodies to 3D capsule list
Add obstacles to 3-D capsule list
Check for collisions between ego bodies and obstacles
Geometric properties of ego bodies
Poses of ego bodies
Geometric properties of obstacles
Poses of obstacles
Remove ego bodies from capsule list
Remove obstacles from capsule list
Display ego bodies and obstacles in environment
Update geometric properties of ego bodies
Update states of ego bodies
Update geometric properties of obstacles
Update states of obstacles

\section*{Examples}

\section*{Build 3-D Ego Body Paths and Check for Collisions with 3-D Obstacles}

Build an ego body path and maintain obstacle states using the dynamicCapsuleList3D object. Visualize the states of all objects in the environment at different timestamps. Validate the path of the ego body by checking for collisions with obstacles in the environment.

Create the dynamicCapsuleList3D object. Extract the maximum number of steps to use as the number of time stamps for your object paths.
```

obsList = dynamicCapsuleList3D;
numSteps = obsList.MaxNumSteps;

```

\section*{Add Ego Body}

Define an ego body by specifying the ID, geometry, and state together in a structure. The capsule geometry has a length of 3 m and radius of 1 m . Specify the state as a linear path from \(x=0 \mathrm{~m}\) to \(x=\) 100 m .
```

egoID1 = 1;
geom = struct("Length",3,"Radius",1,"FixedTransform",eye(4));
states = linspace(0,1,obsList.MaxNumSteps)'.*[100 0 0];
states = [states ones(numSteps,2) zeros(numSteps,2)];
egoCapsule1 = struct('ID',egoID1,'States',states,'Geometry',geom);
addEgo(obsList,egoCapsule1);
show(obsList,"TimeStep",1:numSteps);
ylim([-20 20])
zlim([-5 20])

```
view(-45,25)
hold on


\section*{Add Obstacles}

Specify states for two obstacles that are separated from the ego body by 5 m in opposite directions on the \(y\)-axis. Assume the obstacles have the same geometry geom as the ego body.
```

obsState1 = states + [0 5 0 0 0 0 0];
obsState2 = states + [0 -5 0 0 0 0 0];
obsCapsule1 = struct('ID',1,'States',obsState1,'Geometry',geom);
obsCapsule2 = struct('ID',2,'States',obsState2,'Geometry',geom);
addObstacle(obsList,obsCapsule1);
addObstacle(obsList,obsCapsule2);
cla
show(obsList,"TimeStep",1:numSteps);

```


\section*{Update Obstacles}

Alter your obstacle locations and geometry dimensions over time. Use the previously generated structure, modify the fields, and update the obstacles using the updateObstacleGeometry and updateObstaclePose object functions. Reduce the radius of the first obstacle to 0.5 m , and change the path to move it towards the ego body.
```

obsCapsule1.Geometry.Radius = 0.5;
obsCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
linspace(5,-4,numSteps)' ... % y
zeros(numSteps,1) ... % z

```
    ones(numSteps,2) zeros(numSteps,2)]; \% quaternion \% quaternioı
updateObstacleGeometry(obsList,1,obsCapsule1);
updateObstaclePose(obsList,1,obsCapsule1);

\section*{Check for Collisions}

Visualize the new paths. Show where collisions between the ego body and an obstacle occur, which the display highlights in red. Notice that collisions between the obstacles are not checked.
```

cla
show(obsList,"TimeStep",1: numSteps,"ShowCollisions",1);

```


Programmatically check for collisions bu using the checkCollision object function. The function returns a vector of logical values that indicates the collision status at each time step. The vector is transposed for display purposes.
```

collisions = checkCollision(obsList)'
collisions = 1x31 logical array

```
\begin{tabular}{lllllllllllllllllllllllll}
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 0
\end{tabular}

To validate paths with a large number of steps, use the any function on the vector of collision values.
```

if any(collisions)
disp("Collision detected.")
end
Collision detected.

```

\section*{Update Ego Path}

Specify a new path for the ego body. Visualize the paths again, displaying collisions.
```

egoCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
3*sin(linspace(0,2*pi,numSteps))' ... % y
zeros(numSteps,1)... % z

```
    ones(numSteps,2) zeros(numSteps,2)]; \%quaternion \% quaterni
updateEgoPose(obsList,1,egoCapsule1);
cla
show(obsList,"TimeStep",1:numSteps,"ShowCollisions",1);


\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and C++ code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{Tm}}\).

\section*{See Also}

\section*{Objects}
dynamicCapsuleList

\section*{Functions}
addEgo | addObstacle | checkCollision | egoGeometry | egoPose | obstacleGeometry | obstaclePose | removeEgo | removeObstacle | show | updateEgoGeometry |updateEgoPose | updateObstacleGeometry|updateObstaclePose

\section*{Topics}
"Highway Trajectory Planning Using Frenet Reference Path"

Introduced in R2020b

\section*{addEgo}

Add ego bodies to 3D capsule list

\section*{Syntax}
```

addEgo(capsuleListObj,egoStruct)
status = addEgo(capsuleListObj,egoStruct)

```

\section*{Description}
addEgo( capsuleListObj, egoStruct) adds one or more ego bodies to the 3-D dynamic capsule list with the specified ID, state, and geometry values given in egoStruct.
status = addEgo(capsuleListObj, egoStruct) additionally returns an indicator of whether each specified ego body was added, updated, or a duplicate.

\section*{Examples}

\section*{Build 3-D Ego Body Paths and Check for Collisions with 3-D Obstacles}

Build an ego body path and maintain obstacle states using the dynamicCapsuleList3D object. Visualize the states of all objects in the environment at different timestamps. Validate the path of the ego body by checking for collisions with obstacles in the environment.

Create the dynamicCapsuleList3D object. Extract the maximum number of steps to use as the number of time stamps for your object paths.
```

obsList = dynamicCapsuleList3D;
numSteps = obsList.MaxNumSteps;

```

\section*{Add Ego Body}

Define an ego body by specifying the ID, geometry, and state together in a structure. The capsule geometry has a length of 3 m and radius of 1 m . Specify the state as a linear path from \(x=0 \mathrm{~m}\) to \(x=\) 100 m .
```

egoID1 = 1;
geom = struct("Length",3,"Radius",1,"FixedTransform",eye(4));
states = linspace(0,1,obsList.MaxNumSteps)'.*[100 0 0];
states = [states ones(numSteps,2) zeros(numSteps,2)];
egoCapsule1 = struct('ID',egoID1,'States',states,'Geometry',geom);
addEgo(obsList,egoCapsule1);
show(obsList,"TimeStep",1:numSteps);
ylim([-20 20])
zlim([-5 20])
view(-45,25)
hold on

```


\section*{Add Obstacles}

Specify states for two obstacles that are separated from the ego body by 5 m in opposite directions on the \(y\)-axis. Assume the obstacles have the same geometry geom as the ego body.
```

obsStatel = states + [0 5 0 0 0 0 0];
obsState2 = states + [0 -5 0 0 0 0 0];
obsCapsule1 = struct('ID',1,'States',obsState1,'Geometry',geom);
obsCapsule2 = struct('ID',2,'States',obsState2,'Geometry',geom);
addObstacle(obsList,obsCapsule1);
addObstacle(obsList,obsCapsule2);
cla
show(obsList,"TimeStep",1:numSteps);

```


\section*{Update Obstacles}

Alter your obstacle locations and geometry dimensions over time. Use the previously generated structure, modify the fields, and update the obstacles using the updateObstacleGeometry and updateObstaclePose object functions. Reduce the radius of the first obstacle to 0.5 m , and change the path to move it towards the ego body.
```

obsCapsule1.Geometry.Radius = 0.5;
obsCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
linspace(5,-4,numSteps)' ... % y
zeros(numSteps,1) ... % z

```
    ones(numSteps,2) zeros(numSteps,2)]; \% quaternion \% quaternioı
updateObstacleGeometry(obsList,1,obsCapsule1);
updateObstaclePose(obsList,1,obsCapsule1);

\section*{Check for Collisions}

Visualize the new paths. Show where collisions between the ego body and an obstacle occur, which the display highlights in red. Notice that collisions between the obstacles are not checked.
```

cla
show(obsList,"TimeStep",1: numSteps,"ShowCollisions",1);

```


Programmatically check for collisions bu using the checkCollision object function. The function returns a vector of logical values that indicates the collision status at each time step. The vector is transposed for display purposes.
```

collisions = checkCollision(obsList)'
collisions = 1x31 logical array

```
\begin{tabular}{lllllllllllllllllllllllll}
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 0
\end{tabular}

To validate paths with a large number of steps, use the any function on the vector of collision values.
```

if any(collisions)
disp("Collision detected.")
end
Collision detected.

```

\section*{Update Ego Path}

Specify a new path for the ego body. Visualize the paths again, displaying collisions.
```

egoCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
3*sin(linspace(0,2*pi,numSteps))' ... % y
zeros(numSteps,1)... % z

```
    ones(numSteps,2) zeros(numSteps,2)]; \%quaternion \% quaterni
```

updateEgoPose(obsList,1,egoCapsule1);
cla
show(obsList,"TimeStep",1:numSteps,"ShowCollisions",1);

```


\section*{Input Arguments}

\section*{capsuleListObj - Dynamic capsule list}
dynamicCapsuleList3D object
Dynamic capsule list, specified as a dynamicCapsuleList3D object.

\section*{egoStruct - Ego body parameters}
structure | structure array
Ego body parameters, specified as an \(N\)-element structure or a structure array, where \(N\) is the number of added ego bodies. The fields of each structure define the ID, geometry, and states of an ego body:
- ID -- Integer that identifies each object. Stored in the EgoIDs property of the dynamicCapsuleList3D object specified by the capsuleListObj argument.
- States -- Location and orientation of the object as an \(M\)-by- 6 matrix, where each row is of form [x y z qW qX qY qZ], and \(M\) is the number of states along the path of the object in the world frame. The list of states assumes each state is separated by a fixed time interval. xyz-positions are
in meters, and the orientation is a four-element quaternion vector. The default local origin is located at the center of the left hemisphere of the capsule.
- Geometry -- Structure with fields Length, Radius, and FixedTransform. These fields define the size of the capsule-based object using the specified length for the cylinder and hemisphere radius for the end caps. To shift the capsule geometry from the default origin, specify the FixedTransform field as a fixed transform relative to the local frame of the capsule. To keep the default capsule origin, specify the transform as eye (4).

\(\begin{array}{ll}\text { States: } & {[x y z q W \text { qX qY qZ] }} \\ \text { Geometry: } & \text { Radius } \\ & \text { Length } \\ & \text { FixedTransform* } \\ & *=\text { NotPictured }\end{array}\)

\section*{Output Arguments}

\section*{status - Result of adding ego bodies}
\(N\)-element column vector
Result of adding ego bodies, returned as a \(N\)-element column vector of ones, zeros, and negative ones. \(N\) is the number of ego bodies specified in the egoStruct argument. Each value indicates whether the associated body is added (1), updated (0), or a duplicate ( -1 ). While adding ego bodies, if multiple structures with the same body ID are found in the structure array egoStruct, then the function marks the previous entry as duplicate and ignores it.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).

\section*{See Also}

\section*{Objects}
dynamicCapsuleList|dynamicCapsuleList3D

\author{
Functions \\ addObstacle|checkCollision | egoGeometry | egoPose| obstacleGeometry| \\ obstaclePose|removeEgo| removeObstacle| show|updateEgoGeometry|updateEgoPose| \\ update0bstacleGeometry|update0bstaclePose \\ \section*{Topics} \\ "Highway Trajectory Planning Using Frenet Reference Path" \\ Introduced in R2020b
}

\section*{addObstacle}

Add obstacles to 3-D capsule list

\section*{Syntax}
addObstacle(capsuleList0bj, obstacleStruct)
status = addObstacle(capsuleListObj,obstacleStruct)

\section*{Description}
addObstacle(capsuleListObj, obstacleStruct) adds one or more obstacles to the 3-D dynamic capsule list with the specified ID, state, and geometry values given in obstacleStruct.
status = addObstacle(capsuleListObj,obstacleStruct) additionally returns an indicator of whether each specified obstacle was added, updated, or a duplicate.

\section*{Examples}

\section*{Build 3-D Ego Body Paths and Check for Collisions with 3-D Obstacles}

Build an ego body path and maintain obstacle states using the dynamicCapsuleList3D object. Visualize the states of all objects in the environment at different timestamps. Validate the path of the ego body by checking for collisions with obstacles in the environment.

Create the dynamicCapsuleList3D object. Extract the maximum number of steps to use as the number of time stamps for your object paths.
```

obsList = dynamicCapsuleList3D;
numSteps = obsList.MaxNumSteps;

```

\section*{Add Ego Body}

Define an ego body by specifying the ID, geometry, and state together in a structure. The capsule geometry has a length of 3 m and radius of 1 m . Specify the state as a linear path from \(x=0 \mathrm{~m}\) to \(x=\) 100 m .
```

egoID1 = 1;
geom = struct("Length",3,"Radius",1,"FixedTransform",eye(4));
states = linspace(0,1,obsList.MaxNumSteps)'.*[100 0 0];
states = [states ones(numSteps,2) zeros(numSteps,2)];
egoCapsule1 = struct('ID',egoID1,'States',states,'Geometry',geom);
addEgo(obsList,egoCapsule1);
show(obsList,"TimeStep",1:numSteps);
ylim([-20 20])
zlim([-5 20])
view(-45,25)
hold on

```


\section*{Add Obstacles}

Specify states for two obstacles that are separated from the ego body by 5 m in opposite directions on the \(y\)-axis. Assume the obstacles have the same geometry geom as the ego body.
```

obsState1 = states + [0 5 0 0 0 0 0];
obsState2 = states + [0 -5 0 0 0 0 0];
obsCapsule1 = struct('ID',1,'States',obsState1,'Geometry',geom);
obsCapsule2 = struct('ID',2,'States',obsState2,'Geometry',geom);
addObstacle(obsList,obsCapsule1);
addObstacle(obsList,obsCapsule2);
cla
show(obsList,"TimeStep",1:numSteps);

```


\section*{Update Obstacles}

Alter your obstacle locations and geometry dimensions over time. Use the previously generated structure, modify the fields, and update the obstacles using the updateObstacleGeometry and updateObstaclePose object functions. Reduce the radius of the first obstacle to 0.5 m , and change the path to move it towards the ego body.
```

obsCapsule1.Geometry.Radius = 0.5;
obsCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
linspace(5,-4,numSteps)' ... % y
zeros(numSteps,1) ... % z
updateObstacleGeometry(obsList,1,obsCapsule1);
updateObstaclePose(obsList,1,obsCapsule1);

```

\section*{Check for Collisions}
```

Visualize the new paths. Show where collisions between the ego body and an obstacle occur, which the display highlights in red. Notice that collisions between the obstacles are not checked.

```
```

cla

```
cla
show(obsList,"TimeStep",1: numSteps,"ShowCollisions",1);
```

show(obsList,"TimeStep",1: numSteps,"ShowCollisions",1);

```
    ones(numSteps,2) zeros(numSteps,2)]; \% quaternion \% quaternioı


Programmatically check for collisions bu using the checkCollision object function. The function returns a vector of logical values that indicates the collision status at each time step. The vector is transposed for display purposes.
```

collisions = checkCollision(obsList)'
collisions = 1x31 logical array

```
\begin{tabular}{lllllllllllllllllllllllll}
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 0
\end{tabular}

To validate paths with a large number of steps, use the any function on the vector of collision values.
```

if any(collisions)
disp("Collision detected.")
end
Collision detected.

```

\section*{Update Ego Path}

Specify a new path for the ego body. Visualize the paths again, displaying collisions.
```

egoCapsule1.States = ...
[linspace(0,100,numSteps)' ... % x
3*sin(linspace(0,2*pi,numSteps))' ... % y
zeros(numSteps,1)... % z

```
    ones(numSteps,2) zeros(numSteps,2)]; \%quaternion \% quaterni
```

updateEgoPose(obsList,1,egoCapsule1);
cla
show(obsList,"TimeStep",1:numSteps,"ShowCollisions",1);

```


\section*{Input Arguments}
capsuleListObj - Dynamic capsule-list
dynamicCapsuleList3D object
Dynamic capsule-list, specified as a dynamicCapsuleList3D object.

\section*{Output Arguments}

\section*{obstacleStruct - Obstacle parameters}
structure | structure array
Obstacle parameters, specified as an \(N\)-element structure or a structure array, where \(N\) is the number of added ego bodies. The fields of each structure define the ID, geometry, and states of an obstacle:
- ID -- Integer that identifies each object. Stored in the ObstacleIDs property of the dynamicCapsuleList3D object specified by the capsuleListObj argument.
- States -- Location and orientation of the object as an \(M\)-by-6 matrix, where each row is of form [x y z qW qX qY qZ], and \(M\) is the number of states along the path of the object in the world
frame. The list of states assumes each state is separated by a fixed time interval. \(x y z\)-positions are in meters, and the orientation is a four-element quaternion vector. The default local origin is located at the center of the left hemisphere of the capsule.
- Geometry -- Structure with fields Length, Radius, and FixedTransform. These fields define the size of the capsule-based object using the specified length for the cylinder and hemisphere radius for the end caps. To shift the capsule geometry from the default origin, specify the FixedTransform field as a fixed transform relative to the local frame of the capsule. To keep the default capsule origin, specify the transform as eye(4).


States: \(\quad[x y z q W q X q Y q Z]\)
Geometry: Radius
Length
FixedTransform*
* \(=\) Not Pictured

\section*{status - Result of adding obstacles}
\(N\)-element column vector
Result of adding obstacles, returned as a \(N\)-element column vector of ones, zeros, and negative ones. \(N\) is the number of obstacles specified in the obstacleStruct argument. Each value indicates whether the associated body is added (1), updated ( 0 ), or a duplicate ( -1 ). While adding obstacles, if multiple structures with the same body ID are found in the structure array obstaclesStruct, then the function marks the previous entry as duplicate and ignores it.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}

Objects
dynamicCapsuleList| dynamicCapsuleList3D

\author{
Functions \\ addEgo | checkCollision | egoGeometry |egoPose| obstacleGeometry|obstaclePose| removeEgo | removeObstacle | show \| updateEgoGeometry |updateEgoPose | \\ updateObstacleGeometry|updateObstaclePose \\ \section*{Topics} \\ "Highway Trajectory Planning Using Frenet Reference Path" \\ Introduced in R2020b
}

\section*{ekfSLAM}

Perform simultaneous localization and mapping using extended Kalman filter

\section*{Description}

The ekfSLAM object performs simultaneous localization and mapping (SLAM) using an extended Kalman filter (EKF). It takes in observed landmarks from the environment and compares them with known landmarks to find associations and new landmarks. Use the associations to correct the state and state covariance. The new landmarks are augmented in the state vector.

\section*{Creation}

\section*{Syntax}
```

slamObj = ekfSLAM
slamObj = ekfSLAM(Name,Value)
slamObj = ekfSLAM('MaxNumLandmark',N,Name,Value)
slamObj = ekfSLAM('MaxNumLandmark',N,`MaxNumPoseStored',M,Name,Value)
Description

```
slam0bj = ekfSLAM creates an EKF SLAM object with default properties.
slamObj = ekfSLAM(Name,Value) sets properties using one or more name-value pair arguments in addition to any combination of input arguments from previous syntaxes. Any unspecified properties have default values.
slam0bj = ekfSLAM('MaxNumLandmark',N,Name,Value) specifies an upper bound on the number of landmarks \(N\) allowed in the state vector when generating code. This limit on the number of landmarks applies only when generating code.
slamObj = ekfSLAM('MaxNumLandmark',N,‘MaxNumPoseStored’,M,Name,Value) specifies the maximum size of the pose history M along with the maximum number of landmarks N in the state vector while generating code. These limits apply only when generating code.

\section*{Properties}

You cannot change the value of the properties State, StateCovariance, StateTransitionFcn, and MaxNumLandmark after the object is created. Set the value of these properties as a default or while creating the object.

\section*{State - State vector}
[0; 0; 0] (default) | \(M\)-element column vector
State vector, specified as an \(M\)-element column vector.
Data Types: single | double

\section*{StateCovariance - State estimation error covariance}
eye(3) (default) | \(M\)-by- \(M\) matrix
State estimation error covariance, specified as an \(M\)-by- \(M\) matrix. \(M\) is the number of states in the state vector.

Data Types: single | double

\section*{StateTransitionFcn - State transition function}
nav.algs.velocityMotionModel (default) | function handle
State transition function, specified as a function handle. This function calculates the state vector at time step k from the state vector at time step \(\mathrm{k}-1\). The function can take additional input parameters, such as control inputs or time step size.

The function also calculates the Jacobians with respect to the current pose and controller input. If not specified, the Jacobians are computed using numerical differencing at each call to the predict function. This computation can increase processing time and numerical inaccuracy.

The function considers nonadditive process noise, and should have this signature:
[pose(k),jacPose,jacControl] =
StateTransitionFcn(pose(k-1), controlInput, parameters)
- pose( \(k\) ) is the estimated pose at time \(k\).
- jacPose is the Jacobian of StateTransitionFcn with respect to pose( \(k-1\) ).
- jacControl is the Jacobian of StateTransitionFen with respect to controlInput.
- controlInput is the input for propagating the state.
- parameters are any additional arguments required by the state transition function.

Data Types: function_handle

\section*{MeasurementFcn - Measurement function}
nav.algs.rangeBearingMeasurement (default) | function handle
Measurement function, specified as a function handle. This function calculates an \(N\)-element measurement vector for an \(M\)-element state vector.

The function also calculates the Jacobians with respect to the current pose and landmark position. If not specified, the Jacobians are computed using numerical differencing at each call to the correct function. This computation can increase processing time and numerical inaccuracy.

The function considers additive measurement noise, and should have this signature:

> [measurements(k),jacPose,jacLandmarks] = MeasurementFcn(pose(k),landmarks)
- pose( \(k\) ) is the estimated pose at time \(k\).
- measurements \((k)\) is the estimated measurement at time \(k\).
- landmarks are the positions of the landmarks.
- jacPose is the Jacobian of MeasurementFcn with respect to pose( \(k\) ).
- jacLandmarks is the Jacobian of MeasurementFcn with respect to landmarks.

Data Types: function_handle

\section*{InverseMeasurementFcn - Inverse measurement function}
nav.algs.rangeBearingInverseMeasurement (default) | function handle
Inverse measurement function, specified as a function handle. This function calculates the landmark position as an \(M\)-element state vector for an \(N\)-element measurement vector.

The function also calculates the Jacobians with respect to the current pose and measurement. If not specified, the Jacobians are computed using numerical differencing at each call to the correct function. This computation can increase processing time and numerical inaccuracy.

The function should have this signature:
[landmarks(k),jacPose,jacMeasurements] =
InverseMeasurementFcn(pose(k), measurements)
- pose( \(k\) ) is the estimated pose at time \(k\).
- landmarks ( k ) is the landmark position at time k .
- measurements are the observed landmarks at time k .
- jacPose is the Jacobian of InverseMeasurementFcn with respect to pose(k).
- jacMeasurements is the Jacobian of InverseMeasurementFcn with respect to measurements.

Data Types: function_handle

\section*{DataAssociationFen - Data association function}
nav.algs.associateMaxLikelihood (default) | function handle
Data association function, specified as a function handle. This function associates the measurements with the landmarks already available in the state vector. The function may take additional input parameters.

The function should have this signature:
[associations,newLandmarks] =
DataAssociationFcn(knownLandmarks,knownLandmarksCovariance,observedLandmarks, observedLandmarksCovariance, parameters)
- knownLandmarks are known landmarks in the map.
- knownLandmarksCovariance is the covariance of knownLandmarks.
- observedLandmarks are the observed landmarks in the environment.
- observedLandmarksCovariance is the covariance of observedLandmarks.
- parameters are any additional arguments required.
- associations is a list of associations from knownLandmarks to observedLandmarks.
- newLandmarks are the indices of observedLandmarks that qualify as new landmarks.

Data Types: function_handle

\section*{ProcessNoise - Process noise covariance}
eye(2) (default) \(\mid W\)-by- \(W\) matrix
Process noise covariance, specified as a \(W\)-by- \(W\) matrix. \(W\) is the number of process noise terms.
Data Types: single|double

\section*{MaxAssociationRange - Maximum range for landmarks to be checked for association inf (default) | positive integer}

Maximum range for the landmarks to be checked for association, specified as a positive integer.
Data Types: single | double

\section*{MaxNumLandmark - Maximum number of landmarks in state vector \\ inf (default) | positive integer}

Maximum number of landmarks in the state vector, specified as a positive integer.
Data Types: single | double
MaxNumPoseStored - Maximum size of pose history
inf (default) | positive integer
Maximum size of pose history, specified as a positive integer.
Data Types: single | double

\section*{Object Functions}
\begin{tabular}{ll} 
copy & Create deep copy of EKF SLAM object \\
correct & Correct state and state error covariance \\
landmarkInfo & Retrieve landmark information \\
poseHistory & Retrieve corrected and predicted pose history \\
predict & Predict state and state error covariance \\
removeLandmark & Remove landmark from state vector \\
reset & Reset state and state estimation error covariance
\end{tabular}

\section*{Examples}

\section*{Perform Landmark SLAM Using Extended Kalman Filter}

Load a race track data set that contains the initial vehicle state, initial vehicle state covariance, process noise covariance, control input, time step size, measurement, measurement covariance, and validation gate values.
```

load("racetrackDataset.mat","initialState","initialStateCovariance", ...
"processNoise","controllerInputs","timeStep", ...
"measurements","measCovar","validationGate");

```

Create an ekfSLAM object with initial state, initial state covariance, and process noise.
```

ekfSlamObj = ekfSLAM("State",initialState, ...
"StateCovariance",initialStateCovariance, ...
"ProcessNoise",processNoise);

```

Initialize a variable to store the pose.
```

storedPose = nan(size(controllerInputs,1)+1,3);
storedPose(1,:) = ekfSlamObj.State(1:3);

```

Predict the state using the control input and time step size for the state transition function. Then, correct the state using the data of the observed landmarks, measurement covariance, and validation gate for the data association function.
```

for count = 1:size(controllerInputs,1)
% Predict the state
predict(ekfSlamObj,controllerInputs(count,:),timeStep);
% Get the landmarks in the environment
observedLandmarks = measurements{count};
% Correct the state
if ~isempty(observedLandmarks)
correct(ekfSlam0bj,observedLandmarks, ...
measCovar,validationGate);
end
% Log the estimated pose
storedPose(count+1,:) = ekfSlamObj.State(1:3);
end

```

Visualize the created map.
```

fig = figure;
figAx = axes(fig);
axis equal
grid minor
hold on
plot(figAx,storedPose(:,1),storedPose(:,2),"g.-")
landmarks = reshape(ekfSlamObj.State(4:end),2,[])';
plot(figAx,landmarks(:,1),landmarks(:,2),"m+")
plot(figAx,storedPose(1,1),storedPose(1,2),"k*")
plot(figAx,storedPose(end,1),storedPose(end,2),"rd")
legend("Robot trajectory","Landmarks","Start","End")

```


\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder \(^{\text {TM }}\).

\section*{See Also}

\section*{Objects}
lidarSLAM

\section*{Functions}
copy | correct | landmarkInfo| poseHistory | predict | removeLandmark| reset
Topics
"EKF-Based Landmark SLAM"

Introduced in R2021b

\section*{copy}

Create deep copy of EKF SLAM object

\section*{Syntax}
newSlamObj = copy(slamObj)

\section*{Description}
newSlamObj = copy(slamObj) creates a deep copy of slamObj with the same properties. Any changes made to newSlamObj are not reflected in slamObj.

\section*{Examples}

\section*{Remove Landmark from ekfSLAM Object}

Specify the initial vehicle state.
initialState = [1; -2; 0.1];
Specify the initial landmark positions.
```

landmarkPosition = [15.8495; -12.9496;
25.2455; -15.4705;
37.5880; 3.1023;
16.5690; 2.7466];

```

Specify the initial vehicle state covariance.
```

initialStateCovar = diag([0.1*ones(1,3) 1.1*ones(1,8)]);

```

Create an ekfSLAM object with initial state and initial state covariance.
```

ekfSlamObj = ekfSLAM('State',[initialState; landmarkPosition], ...

```
    'StateCovariance',initialStateCovar);
landmarkInfo(ekfSlam0bj)
ans \(=4 \times 3\) table
    landmark number landmark state index landmark position
\begin{tabular}{lrrrrr} 
& & & & & \\
1 & 4 & 5 & & 15.85 & -12.95 \\
2 & 6 & 7 & & 25.245 & -15.47 \\
3 & 8 & 9 & & 37.588 & 3.1023 \\
4 & 10 & 11 & & 16.569 & 2.7466
\end{tabular}

Create a deep copy of the ekfSLAM object.
newEkfSlamObj = copy(ekfSlamObj);
Specify the landmark number to be removed.
removeLandmark(newEkfSlamObj,3);
landmarkInfo(newEkfSlam0bj)
ans \(=3 \times 3\) table
landmark number landmark state index landmark position
\begin{tabular}{rrrrr}
1 & 4 & 5 & 15.85 & -12.95 \\
2 & 6 & 7 & 25.245 & -15.47 \\
3 & 8 & 9 & 16.569 & 2.7466
\end{tabular}

\section*{Input Arguments}
slamObj - EKF SLAM object
ekfSLAM object
EKF SLAM object, specified as an ekfSLAM object.

\section*{Output Arguments}
newSlamObj - Copy of EKF SLAM object
ekfSLAM object
Copy of the EKF SLAM object, returned as an ekfSLAM object.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and C++ code using MATLAB® Coder \(^{\mathrm{Tm}}\).

\section*{See Also}

\section*{Objects}
ekfSLAM | lidarSLAM

\section*{Functions}
correct | landmarkInfo| poseHistory | predict | removeLandmark|reset
Introduced in R2021b

\section*{correct}

Correct state and state error covariance

\section*{Syntax}
```

[associations,newLandmark] = correct(slamObj,measurement,
measurementCovariance)
[associations,newLandmark] = correct(slamObj,measurement,
measurementCovariance,varargin)

```

\section*{Description}
[associations,newLandmark] = correct(slam0bj,measurement, measurementCovariance) corrects the state and its associated state covariance based on the measurement and measurementCovariance at the current time step. correct uses the data association function specified in the DataAssociationFcn property of the ekfSLAM object, slam0bj, to associate the measurement to landmarks and extract new landmarks from the measurement.

The correct function uses these associations to correct the state and associated state covariance, then augments the state with new landmarks.
[associations, newLandmark] = correct(slam0bj,measurement, measurementCovariance, varargin) passes all additional arguments specified in varargin to the underlying DataAssociationFcn property of slamObj.

The first four inputs to the DataAssociationFcn property are the landmark position, landmark position covariance, measurement, and measurement covariance, followed by all arguments in varargin.

\section*{Examples}

\section*{Perform Landmark SLAM Using Extended Kalman Filter}

Load a race track data set that contains the initial vehicle state, initial vehicle state covariance, process noise covariance, control input, time step size, measurement, measurement covariance, and validation gate values.
```

load("racetrackDataset.mat","initialState","initialStateCovariance", ...
"processNoise","controllerInputs","timeStep", ...
"measurements","measCovar", "validationGate");

```

Create an ekfSLAM object with initial state, initial state covariance, and process noise.
```

ekfSlamObj = ekfSLAM("State",initialState, ...
"StateCovariance",initialStateCovariance, ...
"ProcessNoise",processNoise);

```

Initialize a variable to store the pose.
```

storedPose = nan(size(controllerInputs,1)+1,3);
storedPose(1,:) = ekfSlamObj.State(1:3);

```

Predict the state using the control input and time step size for the state transition function. Then, correct the state using the data of the observed landmarks, measurement covariance, and validation gate for the data association function.
```

for count = 1:size(controllerInputs,1)
% Predict the state
predict(ekfSlamObj,controllerInputs(count,:),timeStep);
% Get the landmarks in the environment
observedLandmarks = measurements{count};
% Correct the state
if ~isempty(observedLandmarks)
correct(ekfSlam0bj,observedLandmarks, ...
measCovar,validationGate);
end
% Log the estimated pose
storedPose(count+1,:) = ekfSlamObj.State(1:3);
end

```

Visualize the created map.
```

fig = figure;
figAx = axes(fig);
axis equal
grid minor
hold on
plot(figAx,storedPose(:,1),storedPose(:,2),"g.-")
landmarks = reshape(ekfSlamObj.State(4:end),2,[])';
plot(figAx,landmarks(:,1),landmarks(:,2),"m+")
plot(figAx,storedPose(1,1),storedPose(1,2),"k*")
plot(figAx,storedPose(end,1),storedPose(end,2),"rd")
legend("Robot trajectory","Landmarks","Start","End")

```


\section*{Input Arguments}
slam0bj - EKF SLAM object
ekfSLAM object
EKF SLAM object, specified as an ekfSLAM object.

\section*{measurement - Measurements of landmarks in environment \\ \(N\)-by-K matrix}

Measurements of the landmarks in the environment, specified as an \(N\)-by- \(K\) matrix. \(K\) is the dimension of the measurement. \(N\) is the number of measurements.
Data Types: single \| double
measurementCovariance - Covariance of measurements
\(K\)-element vector | \(N^{*} \mathrm{~K}\)-by- \(N^{*} \mathrm{~K}\) matrix
Covariance of the measurements, specified as a \(K\)-element vector or \(N^{*} K\)-by- \(N^{*} K\) matrix. \(K\) is the dimension of the measurement. \(N\) is the number of measurements. When specified as a vector, the same covariance value is used for all measurements.

Data Types: single | double
varargin - Variable-length input argument list
comma-separated list

Variable-length input argument list, specified as a comma-separated list. This input is passed directly into the DataAssociationFcn property of slam0bj. When you call:
correct(slam0bj, measurement, measurementCovariance, arg1, arg2)
MATLAB essentially calls the dataAssociationFcn as:
dataAssociationFcn(knownLandmarks,knownLandmarksCovariance, ...
measurement, measurementCovariance, arg1, arg2)

\section*{Output Arguments}

\section*{associations - List of associations of landmarks to measurements \(P\)-by-2 matrix}

List of associations of landmarks to measurements, returned as a \(P\)-by-2 matrix. \(P\) is the number of associations. The first column of the matrix contains the indices of the associated landmarks, and the second column contains the associated measurement indices.

\section*{newLandmark - List of indices of measurements that qualify as new landmarks}
\(Q\)-element vector
List of indices of the measurements that qualify as new landmarks, returned as a \(Q\)-element vector. \(Q\) is the number of measurements that qualify as new landmarks.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and C++ code using MATLAB® Coder \(^{\text {TM }}\).

\section*{See Also}

\section*{Objects}
ekfSLAM

\section*{Functions}
landmarkInfo|poseHistory|predict|removeLandmark|reset
Introduced in R2021b

\section*{landmarkInfo}

Retrieve landmark information

\section*{Syntax}

Info = landmarkInfo(slamObj)
Info = landmarkInfo(slamObj,landmarkIndex)

\section*{Description}

Info = landmarkInfo(slamObj)retrieves landmark information from the ekfSLAM object as a table that contains each landmark number along with its position and state index.

Info = landmarkInfo(slamObj, landmarkIndex) retrieves landmark information for only those landmarks specified by landmarkIndex.

\section*{Examples}

\section*{Retrieve All Landmark Information from ekfSLAM Object}

Specify the initial vehicle state.
```

initialState = [1; -2; 0.1];

```

Specify the initial landmark positions.
landmarkPosition \(=\) [15.8495; -12.9496;
25.2455; -15.4705;
37.5880; 3.1023;
16.5690; 2.7466];

Specify the initial vehicle state covariance.
```

initialStateCovar = diag([0.1*ones(1,3) 1.1*ones(1,8)]);

```

Create an ekfSLAM object with initial state and initial state covariance.
```

ekfSlamObj = ekfSLAM('State',[initialState; landmarkPosition], ...

```
                                    'StateCovariance',initialStateCovar)
ekfSlamObj =
    ekfSLAM with properties:
                            State: [11x1 double]
            StateCovariance: [11x11 double]
                MaxNumLandmark: Inf
        StateTransitionFcn: @nav.algs.velocityMotionModel
            ProcessNoise: [2x2 double]

DataAssociationFcn: @nav.algs.associateMaxLikelihood MaxAssociationRange: Inf

Get the information for all the landmarks.
```

info = landmarkInfo(ekfSlamObj)

```
info \(=4 \times 3\) table
    landmark number landmark state index landmark position
\begin{tabular}{lrrrrr} 
& & & & \\
1 & 4 & 5 & & 15.85 & -12.95 \\
2 & 6 & 7 & & 25.245 & -15.47 \\
3 & 8 & 9 & & 37.588 & 3.1023 \\
4 & 10 & 11 & & 16.569 & 2.7466
\end{tabular}

\section*{Input Arguments}
slamObj - EKF SLAM object
ekfSLAM object
EKF SLAM object, specified as an ekfSLAM object.
landmarkIndex - Indices of landmarks for which to retrieve information
\(N\)-element column vector | \(N\)-by-2 matrix
Indices of landmarks for which to retrieve information, specified as an \(N\)-element column vector of landmark numbers in the state vector or an \(N\)-by-2 matrix of exact positions of landmarks in the state vector. \(N\) is the number of landmarks.

Data Types: single | double

\section*{Output Arguments}

\section*{Info - Landmark information}
table
Landmark information, returned as a table.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder \(^{\text {TM }}\).

\section*{See Also}

\section*{Objects}
ekfSLAM
Functions
correct | poseHistory | predict | removeLandmark | reset

Introduced in R2021b

\section*{poseHistory}

Retrieve corrected and predicted pose history

\section*{Syntax}
[correctedPose,predictedPose] = poseHistory(slamObj)

\section*{Description}
[correctedPose,predictedPose] = poseHistory(slam0bj) retrieves the corrected and predicted pose history up to the current pose.

Note To use this function during code generation, you must specify the MaxNumPoseStored property of the ekfSLAM object. Otherwise, this function returns an error.

\section*{Examples}

\section*{Retrieve Pose History from ekfSLAM Object}

Specify the initial vehicle state.
```

initialState = [1; -2; 0.1];

```

Specify the initial landmark positions.
```

landmarkPosition = [15.8495; -12.9496;
25.2455; -15.4705;
37.5880; 3.1023;
16.5690; 2.7466];

```

Specify the initial vehicle state covariance.
```

initialStateCovar = diag([0.1*ones(1,3) 1.1*ones(1,8)]);

```

Create an ekfSLAM object with initial state and initial state covariance.
```

ekfSlamObj = ekfSLAM('State',[initialState; landmarkPosition], ...
'StateCovariance',initialStateCovar);

```

Specify the control input and time step size for the state transition function.
```

velocity = [1 0];
timeStep = 0.25;

```

Call the predict function.
predict(ekfSlamObj, velocity,timeStep);
Specify the measurement and measurement covariance for the data association function.
```

measurement = [18.4500 -0.7354;
27.7362 -0.6071;
36.9421 0.0386;
16.2765 0.1959];
measureCovar = [0.1^2 (1.0*pi/180)^2];
Call the correct function.
validationGate = 5.991;
associations = correct(ekfSlamObj,measurement, ...
measureCovar,validationGate);

```

Get the pose history.
```

[corrPose,predPose] = poseHistory(ekfSlamObj)
corrPose = 1\times3
1.1609 -1.9736 0.0981
predPose = 1\times3
1.2488 -1.9750 0.1000

```

\section*{Input Arguments}
slamObj - EKF SLAM object
ekfSLAM object
EKF SLAM object, specified as an ekfSLAM object.

\section*{Output Arguments}
correctedPose - Corrected poses
\(M\)-by-3 matrix
Corrected poses, returned as an \(M\)-by-3 matrix with rows of the form [ \(X\) Y Yaw]. \(X\) and \(Y\) specify the position in meters. Yaw specifies the orientation in radians.

\section*{predictedPose - Predicted poses}

M-by-3 matrix
Predicted poses, returned as an \(M\)-by-3 matrix with rows of the form [ \(X\) Y Yaw]. \(X\) and \(Y\) specify the position in meters. Yaw specifies the orientation in radians.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}

\section*{Objects}
ekfSLAM
Functions
correct | landmarkInfo|predict | removeLandmark|reset
Introduced in R2021b

\section*{predict}

Predict state and state error covariance

\section*{Syntax}
predict(slam0bj, controlInput)
predict(slam0bj, controlInput, varargin)

\section*{Description}
predict(slamObj, controlInput) predicts the state and state error covariance. predict uses the StateTransitionFcn property of the ekfSLAM object, slamObj, and the controller input control Input to predict the state.
predict(slamObj, controlInput, varargin) passes all additional arguments specified in varargin to the underlying StateTransitionFen property of slamObj.

The first input to StateTransitionFcn is the pose from the previous time step, followed by all userdefined arguments in varargin.

\section*{Examples}

\section*{Perform Landmark SLAM Using Extended Kalman Filter}

Load a race track data set that contains the initial vehicle state, initial vehicle state covariance, process noise covariance, control input, time step size, measurement, measurement covariance, and validation gate values.
```

load("racetrackDataset.mat","initialState","initialStateCovariance", ...
"processNoise","controllerInputs","timeStep", ...
"measurements","measCovar","validationGate");

```

Create an ekfSLAM object with initial state, initial state covariance, and process noise.
```

ekfSlamObj = ekfSLAM("State",initialState, ...
"StateCovariance",initialStateCovariance, ...
"ProcessNoise",processNoise);

```

Initialize a variable to store the pose.
```

storedPose = nan(size(controllerInputs,1)+1,3);
storedPose(1,:) = ekfSlamObj.State(1:3);

```

Predict the state using the control input and time step size for the state transition function. Then, correct the state using the data of the observed landmarks, measurement covariance, and validation gate for the data association function.
```

for count = 1:size(controllerInputs,1)
% Predict the state
predict(ekfSlamObj,controllerInputs(count,:),timeStep);

```
```

    % Get the landmarks in the environment
    observedLandmarks = measurements{count};
    % Correct the state
    if ~isempty(observedLandmarks)
        correct(ekfSlam0bj,observedLandmarks, ...
            measCovar,validationGate);
    end
    % Log the estimated pose
    storedPose(count+1,:) = ekfSlamObj.State(1:3);
    end

```

Visualize the created map.
```

fig = figure;
figAx = axes(fig);
axis equal
grid minor
hold on
plot(figAx,storedPose(:,1),storedPose(:,2),"g.-")
landmarks = reshape(ekfSlamObj.State(4:end),2,[])';
plot(figAx,landmarks(:,1),landmarks(:,2),"m+")
plot(figAx,storedPose(1,1),storedPose(1,2),"k*")
plot(figAx,storedPose(end,1),storedPose(end,2),"rd")
legend("Robot trajectory","Landmarks","Start","End")

```


\section*{Input Arguments}

\section*{slamObj - EKF SLAM object \\ ekfSLAM object}

EKF SLAM object, specified as a ekfSLAM object.
controlInput - Controller input required to propagate state
\(N\)-element vector
Controller input required to propagate the state from initial value to final value, specified as an N element vector.

Note The dimension of the process noise must be equal to the number of elements in controlInput.

Data Types: single | double

\section*{varargin - Variable-length input argument list}
comma-separated list
Variable-length input argument list, specified as a comma-separated list. This input is passed directly into the StateTransitionFcn property of slamObj to evolve the state. When you call:
predict(slamObj, controlInput, arg1,arg2)
MATLAB essentially calls the stateTransitionFcn as:
stateTransitionFcn(pose(k-1), controlInput, arg1, arg2)

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}

\section*{Objects}
ekfSLAM

\section*{Functions}
correct | landmarkInfo| poseHistory| removeLandmark| reset
Introduced in R2021b

\section*{removeLandmark}

Remove landmark from state vector

\section*{Syntax}
removeLandmark(slam0bj,landmarkIndex)

\section*{Description}
removeLandmark(slamObj,landmarkIndex) removes the landmarks at the specified indices landmarkIndex from the state vector, along with associated covariances from the state covariance matrix.

\section*{Examples}

\section*{Remove Landmark from ekfSLAM Object}

Specify the initial vehicle state.
```

initialState = [1; -2; 0.1];

```

Specify the initial landmark positions.
```

landmarkPosition = [15.8495; -12.9496;
25.2455; -15.4705;
37.5880; 3.1023;
16.5690; 2.7466];

```

Specify the initial vehicle state covariance.
```

initialStateCovar = diag([0.1*ones(1,3) 1.1*ones(1,8)]);

```

Create an ekfSLAM object with initial state and initial state covariance.
```

ekfSlamObj = ekfSLAM('State',[initialState; landmarkPosition], ...
'StateCovariance',initialStateCovar);
landmarkInfo(ekfSlamObj)
ans=4\times3 table
landmark number landmark state index landmark position

```
\(\qquad\)
```

| 1 | 4 | 5 | 15.85 | -12.95 |
| ---: | ---: | ---: | ---: | ---: |
| 2 | 6 | 7 | 25.245 | -15.47 |
| 3 | 8 | 9 | 37.588 | 3.1023 |
| 4 | 10 | 11 | 16.569 | 2.7466 |

```

Create a deep copy of the ekfSLAM object.
newEkfSlamObj = copy(ekfSlamObj);

Specify the landmark number to be removed.
removeLandmark(newEkfSlam0bj,3);
landmarkInfo(newEkfSlam0bj)
ans \(=3 \times 3\) table
landmark number landmark state index landmark position
\begin{tabular}{lllrr}
1 & 4 & 5 & 15.85 & -12.95 \\
2 & 6 & 7 & 25.245 & -15.47 \\
3 & 8 & 9 & 16.569 & 2.7466
\end{tabular}

\section*{Input Arguments}
slamObj - EKF SLAM object
ekfSLAM object
EKF SLAM object, specified as an ekfSLAM object.

\section*{landmarkIndex - Indices of landmarks to remove}
\(N\)-element column vector | \(N\)-by-2 matrix
Indices of the landmarks to remove, specified as an \(N\)-element column vector of landmark numbers in the state vector or an \(N\)-by- 2 matrix of the exact positions of landmarks in the state vector. \(N\) is the number of landmarks to remove.
Data Types: single | double

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and C++ code using MATLAB® Coder \(^{\text {TM }}\).

\section*{See Also}

\section*{Objects}
ekfSLAM

\section*{Functions}
correct | landmarkInfo| poseHistory | predict | reset

\section*{Introduced in R2021b}

\section*{reset}

Reset state and state estimation error covariance

\section*{Syntax}
reset(slam0bj)

\section*{Description}
reset (slam0bj) resets the state and state estimation error covariance to their default values, and resets the internal states.

\section*{Examples}

\section*{Reset State and State Estimation Error Covariance in ekfSLAM Object}

Specify the initial vehicle state.
```

initialState = [1; -2; 0.1];

```

Specify the initial vehicle state covariance.
initialStateCovar = 0.1*eye(3);
Create an ekfSLAM object with initial state and initial state covariance.
```

ekfSlamObj = ekfSLAM('State',initialState, ...
'StateCovariance',initialStateCovar);

```

Get the state and the state covariance from the ekfSLAM object.
```

ekfSlamObj.State

```
ans \(=3 \times 1\)
    1.0000
    \(-2.0000\)
    0.1000
ekfSlam0bj.StateCovariance
ans \(=3 \times 3\)
\begin{tabular}{rrr}
0.1000 & 0 & 0 \\
0 & 0.1000 & 0 \\
0 & 0 & 0.1000
\end{tabular}

Reset the state and state estimation error covariance to the default value.
```

reset(ekfSlamObj)

```

Get the state and the state covariance from the ekfSLAM object.
ekfSlamObj.State
ans \(=3 \times 1\)
0
0
0
ekfSlamObj.StateCovariance
ans \(=3 \times 3\)
\begin{tabular}{lll}
1 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & 1
\end{tabular}

\section*{Input Arguments}
slamObj - EKF SLAM object
ekfSLAM object
EKF SLAM object, specified as an ekfSLAM object.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}

Objects
ekfSLAM
Functions
correct | landmarkInfo| poseHistory | predict | removeLandmark
Introduced in R2021b

\section*{factorlMU}

Convert IMU readings to factor

\section*{Description}

The factorIMU object converts raw IMU readings into constraints between poses, velocities, and IMU biases for a factorGraph object.

\section*{Creation}

\section*{Syntax}

F = factorIMU(nodeID,GyroscopeBiasNoise,AccelerometerBiasNoise, GyroscopeNoise, AccelerometerNoise, GyroscopeReadings, AccelerometerReadings) F = factorIMU( \(\qquad\) ,ReferenceFrame="NED")

Description
F = factorIMU(nodeID,GyroscopeBiasNoise,AccelerometerBiasNoise, GyroscopeNoise,AccelerometerNoise, GyroscopeReadings, AccelerometerReadings) creates a factorIMU object, F, with the specified node identification numbers property NodeID set to nodeID, and with a sample rate, gyroscope bias noise, accelerometer bias noise, gyroscope noise, accelerometer noise, gyroscope readings, and accelerometer readings set to their corresponding values.

F = factorIMU( \(\qquad\) ,ReferenceFrame="NED") specifies the reference frame for the local coordinate system as north-east-down (NED) instead of east-north-up (ENU), in addition to all input arguments from the previous syntax.

\section*{Properties}

\section*{NodeID - Node ID numbers}
six-element row vector of integers
This property is read-only.
Node ID numbers, specified as a six-element row vector. This indicates which nodes in the factor graph this factor connects to.

You must specify this property at object creation.

\section*{SampleRate - IMU sampling rate}
positive scalar greater than 100
This property is read-only.
IMU sampling rate, in Hz , specified as a positive scalar greater than 100.

You must specify this property at object creation.

\section*{GyroscopeBiasNoise - Gyroscope bias noise covariance}

\section*{3-by-3 matrix}

This property is read-only.
Gyroscope bias noise covariance, specified as a 3-by-3 matrix.
You must specify this property at object creation.

\section*{AccelerometerBiasNoise - Accelerometer bias noise covariance}

3-by-3 matrix
This property is read-only.
Accelerometer bias noise covariance, specified as a 3-by-3 matrix.
You must specify this property at object creation.
GyroscopeNoise - Gyroscope measurement noise covariance
3-by-3 matrix
This property is read-only.
Gyroscope measurement noise covariance, specified as a 3-by-3 matrix.
You must specify this property at object creation.

\section*{AccelerometerBiasNoise - Accelerometer measurement noise covariance}

3-by-3 matrix
This property is read-only.
Accelerometer measurement noise covariance, specified as a 3-by-3 matrix.
You must specify this property at object creation.

\section*{GyroscopeReadings - Gyroscope readings}
\(N\)-by-3 matrix
This property is read-only.
Gyroscope readings,, specified as an \(N\)-by- 3 matrix, where \(N\) is the number of readings. The specified gyroscope readings are preintegrated into the factor. GyroscopeReadings and AccelerometerReadings must have the same size.

You must specify this property at object creation.

\section*{AccelerometerReadings - Accelerometer readings}
\(N\)-by-3 matrix
This property is read-only.
Accelerometer readings, specified as an \(N\)-by- 3 matrix, where N is the number of readings. The specified accelerometer readings are preintegrated into the factor. GyroscopeReadings and AccelerometerReadings must have the same size.

You must specify this property at object creation.

\section*{ReferenceFrame - Reference frame for local coordinate system}
"ENU" (default) | "NED"
Reference frame for the local coordinate system as "ENU" (east-north-up) or "NED" (north-eastdown).

\section*{Object Functions}
nodeType Get node type of node in factor graph predict Predict pose and velocity of factor

\section*{Examples}

\section*{Add factorIMU Object to Factor Graph}

Set up parameters such as the connected node IDs, sample rate, noise, and readings. Then create an IMU factor with these parameters as arguments.
```

nodeID = [1,2,3,4,5,6];
sampleRate = 400; % Hz
gyroBiasNoise = 1.5e-9 * eye(3);
accelBiasNoise = diag([9.62e-9, 9.62e-9, 2.17e-8]);
gyroNoise = 6.93e-5 * eye(3);
accelNoise = 2.9e-6 * eye(3);
gyroReadings = [ -0.0151 0.0299 0.0027
-0.0079 0.0370 -0.0014
-0.0320 0.0306 0.0035
-0.0043 0.0340 -0.0066
-0.0033 0.0331 -0.0011];
accelReadings = [ [ 1.0666 0.0802 9.9586
1.1002 0.0199 9.6650
1.0287 0.3071 10.1864
0.9077 -0.2239 10.2989
1.2322 0.0174 9.8411];
f = factorIMU(nodeID, sampleRate, gyroBiasNoise, accelBiasNoise, ...
gyroNoise, accelNoise, gyroReadings, accelReadings, ReferenceFrame="NED");

```

Create a default factor graph and add the factor to the graph using the addFactor function.
```

g = factorGraph;
addFactor(g,f);

```

\section*{References}
[1] Forster, Christian, Luca Carlone, Frank Dellaert, and Davide Scaramuzza. "On-Manifold Preintegration for Real-Time Visual--Inertial Odometry." IEEE Transactions on Robotics 33, no. 1 (February 2017): 1-21. https://doi.org/10.1109/TRO.2016.2597321.

\section*{See Also}

\section*{Objects}
factorGraph|factorGPS| factorTwoPoseSE2|factorTwoPoseSE3|factorIMUBiasPrior | factorVelocity3Prior|factorPoseSE3Prior

\section*{Topics}
"Factor Graph-Based Pedestrian Localization with IMU and GPS Sensors"

Introduced in R2022a

\section*{predict}

Predict pose and velocity of factor

\section*{Syntax}
[predictedpose,predictedvel] = predict(factor,prevpose,prevvel, prevbias)

\section*{Description}
[predictedpose,predictedvel] = predict(factor,prevpose,prevvel, prevbias) predicts the pose predictpose and velocity predictedvel of the factor factor based on IMU readings and the initial pose, prevpose, velocity prevvel, and biasprevbias.

\section*{Examples}

\section*{Predict Pose and Velocity of IMU Factor}

Predict the next pose and velocity of an IMU factor based on the previous pose, velocity, and biases.
Set up parameters such as the connected node IDs, sample rate, noise, and readings. Then create an IMU factor with these parameters as arguments.
```

nodeID = [1,2,3, 4,5,6];
sampleRate = 400; % Hz
gyroBiasNoise = 1.5e-9 * eye(3);
accelBiasNoise = diag([9.62e-9, 9.62e-9, 2.17e-8]);
gyroNoise = 6.93e-5 * eye(3);
accelNoise = 2.9e-6 * eye(3);

| gyroReadings = [ | -0.0151 | 0.0299 | 0.0027 |
| :---: | :---: | :---: | :---: |
|  | -0.0079 | 0.0370 | -0.0014 |
|  | -0.0320 | 0.0306 | 0.0035 |
|  | -0.0043 | 0.0340 | -0.0066 |
|  | -0.0033 | 0.0331 | -0.0011]; |
| accelReadings $=$ [ | [ 1.0666 | 0.0802 | 9.9586 |
|  | 1.1002 | 0.0199 | 9.6650 |
|  | 1.0287 | 0.3071 | 10.1864 |
|  | 0.9077 | -0.2239 | 10.2989 |
|  | 1.2322 | 0.0174 | $9.8411]$ |

```
f = factorIMU(nodeID, sampleRate, gyroBiasNoise, accelBiasNoise, ...
    gyroNoise, accelNoise, gyroReadings, accelReadings, ReferenceFrame="NED");

\section*{Predict Pose and Velocity}

Set up previous pose, velocity and biases measurements to use to predict the next pose and velocity.
```

prevpose = rand(1,7);
prevvel = rand(1,3);
prevaccelbias = rand(1,3);

```
```

prevgyrobias = rand(1,3);
prevbiases = [prevgyrobias,prevaccelbias]
prevbiases = 1×6
0.4854 0.8003 0.1419 0.1576 0.9706 0.9572

```

Use the predict function and the previous measurements to predict the next pose and velocity.
```

[predictedpose,predictedvel] = predict(f,prevpose,prevvel,prevbiases)
predictedpose = 1×7
0.8218 0.9189 0.1383 0.6307 0.7048 0.1055 0.3071
predictedvel = 1×3
0.5686 1.0891 0.8818

```

\section*{Input Arguments}
factor - IMU factor
factorIMU object
IMU factor, specified as a factorIMU object.
prevpose - Previous pose of factor
seven-element vector
Previous pose of the factor, specified as a seven-element vector. The pose consists of the 3-D position and orientation quaternion of the factor of the form \([x y z w q x q y q z]\).

\section*{prevvel - Previous 3-D velocity}
three-element vector
Previous 3-D velocity, specified as a three-element vector of the form [ \(v x v y v z\) ].
prevbias - Previous 3-D biases of gyroscope and accelerometer
six-element vector
Previous 3-D biases of the gyroscope and accelerometer, specified as a six-element vector of the form [gx gy gz ax ay \(a z\) ].

\section*{Output Arguments}
predictedpose - Predicted pose
seven-element vector
Predicted 3-D position and orientation quaternion, returned as a seven-element vector of the form [ \(x\) \(y z w q x q y q z]\)..

\section*{predictedvel - Predicted velocity}
three-element vector
predicted 3-D velocity, returned as a three-element vector of the form [ \(v x v y v z]\).

\section*{See Also}
factorIMU | factorGraph

\section*{Topics}
"Factor Graph-Based Pedestrian Localization with IMU and GPS Sensors"
Introduced in R2022a

\section*{factorGPS}

Factor for GPS measurement

\section*{Description}

The factorGPS object adds a constraint to a node in a factorGraph by using a GPS position measurement.

\section*{Creation}

\section*{Syntax}

F = factorGPS(NodeID)
F = factorGPS(NodeID,Name=Value)

\section*{Description}

F = factorGPS(NodeID) returns a factorGPS object, F, with the node identification number set to NodeID. The GPS factor adds a constraint to the corresponding factor graph node by using a GPS position measurement.

F = factorGPS(NodeID,Name=Value) specifies properties using one or more name-value arguments. For example, factorGPS (1,VDOP=1) sets the VDOP property of the factorGPS object to 1 .

\section*{Properties}

\section*{NodeID - Node ID number}

\section*{nonnegative integer}

This property is read-only.
Node ID number, specified as a nonnegative integer. The GPS factor connects to this node in the factor graph.

You must specify this property at object creation.

\section*{Location - Geodetic position measurement}
[0 0 0] (default) | three-element row vector
Geodetic position measurement, specified as a three-element row vector of geodetic coordinates in the form (latitude longitude altitude). Latitude and longitude are in degrees and altitude is in meters.

\section*{HDOP - Horizontal dilution of precision}

1 (default) | positive scalar
Horizontal dilution of precision, specified as a positive scalar.

\section*{VDOP - Vertical dilution of precision}

2 (default) | positive scalar
Vertical dilution of precision, specified as a positive scalar.

\section*{ReferenceLocation - Origin of local coordinate system}
[0 0 0] (default) |3-element row vector
Origin of the local coordinate system, specified as a three-element row vector of geodetic coordinates in the form (latitude longitude altitude). Latitude and longitude are in degrees and altitude is in meters.

Altitude is the height above the reference ellipsoid mode, WGS84.

\section*{ReferenceFrame - Reference frame for local coordinate system}
"ENU" (default) | "NED"
Reference frame for the local coordinate system as "ENU" (east-north-up) or "NED" (north-east-down)

\section*{Object Functions}
nodeType Get node type of node in factor graph

\section*{Examples}

\section*{Add factorGPS Object to Factor Graph}

Set up parameters such as the connected node ID, and reference location. Then create a GPS factor with these parameters as arguments, and set the reference frame to "NED".
```

id = 1;
loc = [5 5 1000];
hdop = 1.5;
vdop = 2.4;
refloc = [0 0 100];
f = factorGPS(id,Location=loc,HDOP=hdop,VDOP=vdop,ReferenceLocation=refloc,ReferenceFrame="NED")

```

Create a default factor graph and add the factor to the graph using the addFactor function.
```

g = factorGraph;
addFactor(g,f);

```

\section*{See Also}

\section*{Objects}
factorGraph | factorGraphSolverOptions | factorIMU|factorTwoPoseSE2 |
factorTwoPoseSE3| factorIMUBiasPrior|factorVelocity3Prior|factorPoseSE3Prior

\section*{Functions}
importFactorGraph

\section*{Topics}
"Factor Graph-Based Pedestrian Localization with IMU and GPS Sensors"

Introduced in R2022a

\section*{factorTwoPoseSE2}

Factor relating two \(\mathrm{SE}(2)\) poses

\section*{Description}

The factorTwoPoseSE2 object relates two poses in the SE(2) state space for a factorGraph object.

\section*{Creation}

\section*{Syntax}

F = factorTwoPoseSE2(nodeID)
F = factorTwoPoseSE2(nodeID,Name=Value)

\section*{Description}

F = factorTwoPoseSE2(nodeID) creates a factorTwoPoseSE2 object, \(F\), with the node identification numbers property, NodeID, set to nodeID.

F = factorTwoPoseSE2 (nodeID, Name=Value) specifies properties using one or more namevalue arguments. For example, factorTwoPoseSE2 ([1, 2] , Measurement=[1,5,7]) sets the Measurement property of the factorTwoPoseSE2 object to [1,5,7].

\section*{Properties}

\section*{NodeID - Node ID numbers}
two-element row vector of integers
This property is read-only.
ID numbers of connected nodes in the factor graph, specified as a two-element row vector of integers.
You must specify this property at object creation.

\section*{Measurement - Measured relative pose}
[0, 0, 0] (default) | three-element row vector
Measured relative pose, specified as a three-element row vector of the form \([x y\) theta].
Information - Information matrix associated with measurement
eye(3) (default) | 3-by-3 matrix
Information matrix associated with the measurement, specified as a 3-by-3 matrix.

\section*{Object Functions}
nodeType Get node type of node in factor graph

\section*{Examples}

\section*{Add FactorTwoPoseSE2 Object to Factor Graph}

Create measurement vector, information matrix, and a node ID number vector. Create a factorTwoPoseSE2 object, specifying the node IDs, measurement, and information as arguments.
```

nodeID = [1 2];
measure = [5 5 pi/2];
info = rand(3,3);
f = factorTwoPoseSE2(nodeID,Measurement=measure,Information=info);

```

Create a default factor graph and add the factor to the graph using the addFactor function.
\(\mathrm{g}=\mathrm{factor} \mathrm{Graph}\);
addFactor(g,f);

\section*{See Also}

\section*{Objects}
factorGraph | factorGPS | factorIMU | factorTwoPoseSE3 | factorIMUBiasPrior| factorVelocity3Prior|factorPoseSE3Prior

Introduced in R2022a

\section*{factorTwoPoseSE3}

Factor relating two \(\mathrm{SE}(3)\) poses

\section*{Description}

The factorTwoPoseSE3 object relates two poses in the SE(3) state space for a factorGraph object.

\section*{Creation}

\section*{Syntax}

F = factorTwoPoseSE3(nodeID)
F = factorTwoPoseSE3(nodeID, Name=Value)

\section*{Description}

F = factorTwoPoseSE3(nodeID) creates a factorTwoPoseSE3 object, \(F\), with the node identification numbers property, NodeID, set to nodeID.
\(F=\) factorTwoPoseSE3(nodeID, Name=Value) specifies properties using one or more namevalue arguments. For example, factorTwoPoseSE3([1, 2] , Measurement \(=[1,2,3,4,5,6,7])\) sets the Measurement property of the factorTwoPoseSE3 object to \([1,2,3,4,5,6,7]\).

\section*{Properties}

\section*{NodeID - Node ID numbers}
two-element row vector of integers
This property is read-only.
Node ID numbers that this factor connects to in the factor graph, specified as a two-element row vector of integers.

You must specify this property at object creation.

\section*{Measurement - Measured relative pose}
[0, 0, 0, 1, 0, 0, 0] (default) | seven-element row vector
Measured relative pose, specified as a seven-element row vector of the form [ \(d x d y d z d q w d q x d q y\) \(d q z] . d x, d y\), and \(d z\) are the change in position in \(x, y\), and \(z\) respectively. \(d q w, d q x, d q y\), and \(d q z\) are the change in quaternion rotation in \(w, x, y\), and \(z\) respectively.

\section*{Information - Information matrix associated with the measurement \\ eye(6) (default) | 6-by-6 matrix}

Information matrix associated with the measurement, specified as a 6 -by- 6 matrix.

\section*{Object Functions}
nodeType Get node type of node in factor graph

\section*{Examples}

Add factorTwoPoseSE3 Object to Factor Graph
Create a two pose SE(3) state space factor with the connected node IDs set to 1 and 2.
f = factorTwoPoseSE3([1 2]);
Create a default factor graph and add the factor to the graph using the addFactor function.
\(\mathrm{g}=\) factorGraph;
addFactor(g,f);

\section*{See Also}
```

Objects
factorGraph | factorTwoPoseSE2 | factorIMU | factorGPS | factorIMUBiasPrior|
factorVelocity3Prior|factorPoseSE3Prior
Introduced in R2022a

```

\section*{factorlMUBiasPrior}

Prior factor for IMU bias

\section*{Description}

The factorIMUBiasPrior object is a factor that has prior information for an IMU bias for a factorGraph object.

\section*{Creation}

\section*{Syntax}

F = factorIMUBiasPrior(nodeID)
F = factorIMUBiasPrior(nodeID,Name=Value)
Description
F = factorIMUBiasPrior(nodeID) creates a factorIMUBiasPrior object, F, with the node identification numbers property, NodeID, set to nodeID

F = factorIMUBiasPrior(nodeID,Name=Value) specifies properties using one or more namevalue arguments. For example, factorIMUBiasPrior( 1, Measurement \(=[1,2,3,1,2,3]\) ) sets the Measurement property of the factorIMUBiasPrior object to \([1,2,3,1,2,3]\).

\section*{Properties}

\section*{NodeID - Node ID number}
nonnegative integer
This property is read-only.
Node ID number of the factor in the factor graph, specified as a nonnegative integer.
You must specify this property at object creation.

\section*{Measurement - Measured relative pose}
[0, 0, 0, 0, 0, 0] (default) | six-element row vector
Measured prior IMU bias, specified as a six-element row vector in the form [GyroBias, AccelBias], where GyroBias and AccelBias are three-element row vectors of the gyro bias and acceleration bias in radians per second and meters per second respectively.

Information - Information matrix associated with the measurement
eye(6) (default) | 6-by-6 matrix
Information matrix associated with the measurement, specified as a 6 -by- 6 matrix.

\section*{Object Functions}
nodeType Get node type of node in factor graph

\section*{Examples}

Add factorIMUBiasPrior Object to Factor Graph
Create an IMU bias prior factor with a node ID of 1.
f = factorIMUBiasPrior(1);
Create a default factor graph and add the factor to the graph using the addFactor function.
\(\mathrm{g}=\) factorGraph;
addFactor(g,f);

\section*{See Also}

\section*{Objects}
factorGraph | factorIMU| factorGPS | factorTwoPoseSE2 | factorTwoPoseSE3|
factorVelocity3Prior|factorPoseSE3Prior

\section*{Topics}
"Factor Graph-Based Pedestrian Localization with IMU and GPS Sensors"

Introduced in R2022a

\section*{factorVelocity3Prior}

Prior factor for 3-D velocity

\section*{Description}

The factorVelocity3Prior object is a factor that has information for a prior velocity in 3-D for a factorGraph object.

\section*{Creation}

\section*{Syntax}

F = factorVelocity3Prior(nodeID)
F = factorVelocity3Prior(nodeID,Name=Value)

\section*{Description}

F = factorVelocity3Prior(nodeID) creates a factorVelocity3Prior object, \(F\), with the node identification numbers property, NodeID, set to nodeID.

F = factorVelocity3Prior(nodeID,Name=Value) specifies properties using one or more name-value arguments. For example, factorVelocity3Prior( 1 , Measurement=[1,5,7]) sets the Measurement property of the factorVelocity3Prior object to [1, 5, 7].

\section*{Properties}

\section*{NodeID - Node ID number}
nonnegative integer
This property is read-only.
Node ID number of the factor in the factor graph, specified as a nonnegative integer.
You must specify this property at object creation.

\section*{Measurement - Measured prior velocity}
[0,0,0] (default) | three-element row vector
Measured relative velocity, specified as a three-element row vector of the form \([x z y z v z]\).
Information - Information matrix associated with the measurement eye(3) (default) | 3-by-3 matrix

Information matrix associated with the measurement, specified as a 3-by-3 matrix.

\section*{Object Functions}
nodeType Get node type of node in factor graph

\section*{Examples}

\section*{Add factorVelocity3Prior Object to Factor Graph}

Create a velocity prior factor with a node ID of 1.
f = factorVelocity3Prior(1);
Create a default factor graph and add the factor to the graph using the addFactor function.
\(\mathrm{g}=\) factorGraph;
addFactor(g,f);

\section*{See Also}

\author{
Objects \\ factorGraph | factorTwoPoseSE2| factorTwoPoseSE3|factorIMU|factorGPS | factorIMUBiasPrior| factorPoseSE3Prior \\ Topics \\ "Factor Graph-Based Pedestrian Localization with IMU and GPS Sensors" \\ Introduced in R2022a
}

\section*{factorPoseSE3Prior}

Full-state prior factor for \(\operatorname{SE}(3)\) pose

\section*{Description}

The factorPoseSE3Prior object is a full-state prior factor for an \(\mathrm{SE}(3)\) state space pose for a factorGraph object.

\section*{Creation}

\section*{Syntax}

F = factorPoseSE3Prior(nodeID)
F = factorPoseSE3Prior(nodeID,Name=Value)
Description
F = factorPoseSE3Prior(nodeID) creates a factorPoseSE3Prior object, F, with the node identification numbers property, NodeID, set to nodeID.
\(F=\) factorPoseSE3Prior(nodeID, Name=Value) specifies properties using one or more namevalue arguments. For example, factorPoseSE3Prior ( 1 , Measurement=[1, 2, 3, 4, 5, 6, 7]) sets the Measurement property of the factorPoseSE3Prior object to \([1,2,3,4,5,6,7]\).

\section*{Properties}

\section*{NodeID - Node ID number}
nonnegative integer
This property is read-only.
Node ID number of the factor in the factor graph, specified as a nonnegative integer.
You must specify this property at object creation.

\section*{Measurement - Measured relative pose}
[0, 0, 0, 1, 0, 0, 0] (default) | seven-element row vector
Measured absolute \(\operatorname{SE}(3)\) prior pose in local coordinates, specified as a seven-element row vector of the form [x \(y z q w q x q y q z\) ]. \(x, y\), and \(z\) are the change in position in \(x, y\), and \(z\) respectively. \(q w, q x\), \(q y\), and \(q z\) are the change in quaternion rotation in \(w, x, y\), and \(z\) respectively.

\section*{Information - Information matrix associated with the measurement \\ eye(6) (default) | 6-by-6 matrix}

Information matrix associated with the measurement, specified as a 6 -by- 6 matrix.

\section*{Object Functions}
nodeType Get node type of node in factor graph

\section*{Examples}

Add factorPoseSE3Prior Object to Factor Graph
Create a prior SE(3) pose factor with a node ID of 1.
f = factorPoseSE3Prior(1);
Create a default factor graph and add the factor to the graph using the addFactor function.
\(\mathrm{g}=\) factorGraph;
addFactor(g,f);

\section*{See Also}

\section*{Objects}
factorGraph| factorTwoPoseSE2|factorTwoPoseSE3|factorIMU|factorGPS |
factorIMUBiasPrior| factorVelocity3Prior

\section*{Topics}
"Factor Graph-Based Pedestrian Localization with IMU and GPS Sensors"

Introduced in R2022a

\section*{factorGraph}

Bipartite graph of factors and nodes

\section*{Description}

A factorGraph object stores a bipartite graph consisting of factors connected to variable nodes. The nodes represent the unknown random variables in an estimation problem, and the factors represent probabilistic constraints on those variables, derived from measurements or prior knowledge. Add factors and nodes to the factor graph by using the addFactor function.

\section*{Creation}

\section*{Syntax}

G = factorGraph

\section*{Description}

G = factorGraph creates an empty factorGraph object.

\section*{Properties}

\section*{NumNodes - Number of nodes in factor graph}
positive integer
This property is read-only.
Number of nodes in the factor graph, specified as a positive integer.

\section*{NumFactors - Number of factors in factor graph}
positive integer
This property is read-only.
Number of factors in the factor graph, specified as a positive integer.

\section*{Object Functions}
addFactor Add factor to factor graph
fixNode \(\quad\) Fix or free node in factor graph
hasNode Check if node ID exists in factor graph
isConnected Check if factor graph is connected
isNodeFixed Check if node is fixed
nodeIDs
nodeState
Get all node IDs in factor graph
nodeType Get node type of node in factor graph
optimize
Optimize factor graph

\section*{Examples}

\section*{Create and Optimize Factor Graph with Custom Options}

Create and optimize a factor graph with custom solver options.

\section*{Create Factor Graph and Solver Settings}

Create a factor graph and solver options with custom settings. Set the maximum number of iterations to 1000 and set the verbosity of the optimize output to 2 .
```

G = factorGraph;
optns = factorGraphSolverOptions(MaxIterations=1000,VerbosityLevel=2)
optns =
factorGraphSolverOptions with properties:
MaxIterations: 1000
FunctionTolerance: 1.0000e-06
GradientTolerance: 1.0000e-10
StepTolerance: 1.0000e-08
VerbosityLevel: 2
TrustRegionStrategyType: 1

```

\section*{Add GPS Factor}

Create a GPS factor with node identification number of 1 with NED ReferenceFrame and add it to the factor graph.
```

fgps = factorGPS(1,ReferenceFrame="NED");
addFactor(G,fgps);

```

\section*{Optimize Factor Graph}

Optimize the factor graph with the custom settings. The results of the optimization are displayed with the level of detail depending on the VerbosityLevel.
```

optimize(G,optns);

```

```

Given Used
Linear solver SPARSE_NORMAL_CHOLESKY
Linear solver ordering AUTOMATIC 1
Cost:
Initial 0.000000e+00
Final 0.000000e+00
Change 0.000000e+00
Minimizer iterations 1
Successful steps 1
Unsuccessful steps 0
Time (in seconds):
Preprocessor 0.024089
Residual only evaluation 0.000000 (0)
Jacobian \& residual evaluation 0.015954 (1)
Linear solver 0.000000 (0)
Minimizer 0.027680
Postprocessor 0.000021
Total 0.051791
Termination: CONVERGENCE (Gradient tolerance reached. Gradient max norm: 0.(

```

\section*{References}
[1] Dellaert, Frank. Factor graphs and GTSAM: A Hands-On Introduction. Georgia: Georgia Tech, September, 2012.

\section*{See Also}

\section*{Objects}
factorGraphSolverOptions | factorTwoPoseSE2| factorTwoPoseSE3|factorIMU |
factorGPS | factorPoseSE3Prior | factorIMUBiasPrior| factorVelocity3Prior

\section*{Functions}
importFactorGraph

\section*{Topics}
"Factor Graph-Based Pedestrian Localization with IMU and GPS Sensors"

Introduced in R2022a

\section*{addFactor}

Add factor to factor graph

\section*{Syntax}
addFactor(graph,factor)

\section*{Description}
addFactor(graph,factor) adds a factor object, factor, as a node in the specified factorGraph object graph.

\section*{Input Arguments}
graph - Factor graph to add node to
factorGraph object
Factor graph to add node to, specified as a factorGraph object.

\section*{factor - Factor node to add to factor graph}
valid factor object
Factor to add to the factor graph, specified as a valid factor object.
- factorTwoPoseSE2
- factorTwoPoseSE3
- factorPoseSE3Prior
- factorVelocity3Prior
- factorIMUBiasPrior
- factorGPS
- factorIMU

\section*{See Also}

\section*{Objects}
factorGraph|factorTwoPoseSE2|factorTwoPoseSE3|factorPoseSE3Prior|
factorVelocity3Prior|factorIMUBiasPrior|factorGPS|factorIMU
Topics
"Factor Graph-Based Pedestrian Localization with IMU and GPS Sensors"

Introduced in R2022a

\section*{fixNode}

Fix or free node in factor graph

\section*{Syntax}
```

fixNode(graph,nodeID)
fixNode(graph,nodeID,flag)

```

\section*{Description}
fixNode(graph, nodeID) fixes the node at the specified ID, nodeID during optimization.
fixNode(graph, nodeID, flag) specifies whether to fix or free the node at the specified ID, nodeID.

\section*{Input Arguments}

\section*{graph - Factor graph containing nodes to fix}
factorGraph object
Factor graph containing nodes to fix, specified as a factorGraph object.

\section*{nodeID - ID of node to fix or free}
nonnegative integer
ID of the node to fix or free within the factor graph, specified as a nonnegative integer.

\section*{flag - New fix status of node}
true or 1 (default) | false or 0
New fix status of the node, specified as a logical 1 (true) or 0 (false). If specified as true, the function fixes the node. If specified as true, the function frees the node during optimization.

\section*{See Also}

\section*{Objects}
factorGraph
Introduced in R2022a

\section*{hasNode}

Check if node ID exists in factor graph

\section*{Syntax}
nodeExist \(=\) hasNode(graph, nodeID)

\section*{Description}
nodeExist \(=\) hasNode(graph, nodeID) checks if a node with the specified ID nodeID exists in the factor graph graph.

\section*{Input Arguments}
graph - Factor graph
factorGraph object
Factor graph, specified as a factorGraph object.
nodeID - ID of node to check
nonnegative integer
ID of node to check, specified as a nonnegative integer.

\section*{Output Arguments}

\section*{nodeExist - Node exists in the factor graph}
false or \(0 \mid\) true or 1
Node exists in the factor graph, returned as a logical 0 (false) or 1 (true). The function returns 0 if the node does not exist, and 1 if it does exist.

\section*{See Also}

Objects
factorGraph
Introduced in R2022a

\section*{isConnected}

Check if factor graph is connected

\section*{Syntax}
connected \(=\) isConnected (graph)

\section*{Description}
connected \(=\) isConnected (graph) returns a logical flag indicating whether the specified factorGraph object graph, contains nodes that all have at least one connection.

\section*{Input Arguments}
graph - Factor graph
factorGraph object
Factor object, specified as a factorGraph object.

\section*{Output Arguments}

\section*{connected - Graph is connected in factor graph \\ false or \(0 \mid\) true or 1}

Graph is connected in factor graph, returned as 1 (true) if the factorGraph has a single connected component and 0 or false if it does not have a single connected component.

\section*{See Also}

\section*{Objects}
factorGraph
Introduced in R2022a

\section*{isNodeFixed}

Check if node is fixed

\section*{Syntax}
isFixed = isNodeFixed(graph,nodeID)

\section*{Description}
isFixed = isNodeFixed(graph, nodeID) returns a logical flag indicating whether the node with the specified nodeID in the factor graph, graph is fixed or not fixed during optimization.

\section*{Input Arguments}
graph - Factor graph
factorGraph object
Factor graph, specified as a factorGraph object.

\section*{nodeID - Node ID of existing node}
nonnegative integer
Node ID of an existing node, specified as a nonnegative integer.

\section*{Output Arguments}

\section*{isFixed - Fix status of node \\ true or \(1 \mid\) false or 0}

Fix status of the node, returned as a logical 1 (true) or 0 (false). The function returns true when the node is fixed, and returns false when the node is free.

\section*{See Also}

\section*{Objects}
factorGraph

\section*{Introduced in R2022a}

\section*{nodelDs}

Get all node IDs in factor graph

\section*{Syntax}
ids \(=\) nodeIDs(graph)

\section*{Description}
ids \(=\) nodeIDs(graph) returns all node IDs, ids, currently in the factor graph, graph.

\section*{Input Arguments}
graph - Factor graph
factorGraph object
Factor graph, specified as a factorGraph object.

\section*{Output Arguments}

\section*{ids - Node IDs \\ \(N\)-element row vector}

Node IDs of all nodes within the specified factorGraph object, returned as an \(N\)-element row vector. \(N\) is the total number of nodes in the graph. Note that the node IDs may not be contiguous within the vector.

\section*{See Also}

Introduced in R2022a

\section*{nodeState}

Get or set node state in factor graph

\section*{Syntax}
state = nodeState(graph, nodeID)
nodeState(graph, nodeID, newState)

\section*{Description}
state \(=\) nodeState \((g r a p h\), nodeID \()\) returns the state of the node with the specified ID nodeID in the specified factorGraph object graph.
nodeState(graph, nodeID, newState) sets the state of the node with the specified ID nodeID in the specified factorGraph object graph to the specified state newState.

\section*{Input Arguments}
graph - Factor graph
factorGraph object
Factor graph, specified as a factorGraph object.
nodeID - ID of node to get or set
nonnegative integer
ID of the node to get or set, specified as a nonnegative integer.

\section*{newState - New node state}
\(N\)-element row vector
New node state, specified as an \(N\)-element row vector, where \(N\) is the number of state elements in the specified node.

\section*{Output Arguments}
state - State of node
\(N\)-element row vector
State of the state, returned as an \(N\)-element row vector, where \(N\) is the number of state elements in the specified node.

\section*{See Also}

\section*{Objects}
factorGraph

Introduced in R2022a

\section*{nodeType}

Get node type of node in factor graph

\section*{Syntax}
type = nodeType(graph, nodeID)

\section*{Description}
type \(=\) nodeType(graph, nodeID) returns the type type of the specified node nodeID, in the factor graph graph.

\section*{Input Arguments}
graph - Factor graph
factorGraph object
Factor graph, specified as a factorGraph object.
nodeID - ID of node to check
nonnegative integer
ID of node to check, specified as a nonnegative integer.

\section*{Output Arguments}
```

type - Type of node

```
string scalar
Type of the node, returned as a string scalar. The supported node types are:
- "POSE_SE2"
- "POSE_SE3"
- "VEL3"
- "POINT_XY"
- "POINT_XYZ"
- "IMU_BIAS"

\section*{See Also}

Objects
factorGraph
Introduced in R2022a

\section*{optimize}

Optimize factor graph

\section*{Syntax}
```

solnInfo = optimize(graph,solverOptions)

```

\section*{Description}
solnInfo = optimize(graph, solverOptions) optimizes the factorGraph object graph using the specified factor graph solver options, solverOptions, and returns the resulting solution info solnInfo.

\section*{Examples}

\section*{Create and Optimize Factor Graph with Custom Options}

Create and optimize a factor graph with custom solver options.

\section*{Create Factor Graph and Solver Settings}

Create a factor graph and solver options with custom settings. Set the maximum number of iterations to 1000 and set the verbosity of the optimize output to 2 .

G = factorGraph;
optns = factorGraphSolverOptions(MaxIterations=1000,VerbosityLevel=2)
optns =
factorGraphSolverOptions with properties:
MaxIterations: 1000
FunctionTolerance: 1.0000e-06
GradientTolerance: 1.0000e-10
StepTolerance: 1.0000e-08
VerbosityLevel: 2
TrustRegionStrategyType: 1

\section*{Add GPS Factor}

Create a GPS factor with node identification number of 1 with NED ReferenceFrame and add it to the factor graph.
```

fgps = factorGPS(1,ReferenceFrame="NED");
addFactor(G,fgps);

```

\section*{Optimize Factor Graph}

Optimize the factor graph with the custom settings. The results of the optimization are displayed with the level of detail depending on the VerbosityLevel.
```

optimize(G,optns);

```
```

| iter | cost | cost_change | \|gradient| | \|step| | tr_ratio | s | ls_iter | e |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0.000000e+00 | $0.00 \mathrm{e}+00$ | 0.00e+00 | $0.00 \mathrm{e}+00$ | 0.00e+00 | 1.00e+04 | 0 | $1.99 \mathrm{e}-02$ |
| Termi | nating: Gradi | t tolerance | eached Grad | ient max | rm: 0 0000 | 00e+00 < | 00000 |  |

Solver Summary (v 2.0.0-eigen-(3.3.4)-no_lapack-eigensparse-no_openmp)
Original Reduced
Parameter blocks 1 1
Parameters 7 7
Effective parameters 6 6
Residual blocks 1 1
Residuals 3 3
Minimizer TRUST REGION
Sparse linear algebra library EIGEN SPARSE
Trust region strategy DOGLEG (TRADITIONAL)

|  | Given |  |
| :--- | ---: | ---: |
| Linear solver | SPARSE_NORMAL_CHOLESKY | Used |
| Threads | 1 | SPARSE_NORMAL_CHOLESKY |
| Linear solver ordering | AUTOMATIC | 1 |
|  |  |  |

Cost:
Initial 0.000000e+00
Final 0.000000e+00
Change 0.000000e+00
Minimizer iterations 1
Successful steps 1
Unsuccessful steps 0
Time (in seconds):
Preprocessor 0.024089
Residual only evaluation 0.000000 (0)
Jacobian \& residual evaluation 0.015954 (1)
Linear solver 0.000000 (0)
Minimizer 0.027680
Postprocessor 0.000021
Total
0.051791
Termination: CONVERGENCE (Gradient tolerance reached. Gradient max norm: 0

```

\section*{Input Arguments}
graph - Factor graph
factorGraph object
Factor graph, specified as a factorGraph object.

\section*{solverOptions - Solver options for factor graph}
factorGraphSolverOptions object
Solver options for the factor graph, specified as a factorGraphSolverOptions object.

\section*{Output Arguments}

\section*{solnInfo - Results of optimization}
structure
Results of the optimization, returned as a structure containing:
- InitialCost - Initial cost
- FinalCost - Final cost
- NumSuccessfulSteps - Number of successful optimization steps
- NumUnsuccessfulSteps - Number of unsuccessful optimization steps
- TotalTime - Total optimization time in seconds
- TerminationType - Termination type
- IsSolutionUsable - Solution is usable if 1 (true), not usable if 0 (false)

\section*{See Also}

\section*{Objects}
factorGraph | factorGraphSolverOptions
Introduced in R2022a

\section*{factorGraphSolverOptions}

Solver options for factor graph

\section*{Description}

The factorGraphSolverOptions object contains solver options for optimizing a factor graph.

\section*{Creation}

\section*{Syntax}

Options = factorGraphSolverOptions
Options = factorGraphSolverOptions(Name=Value)

\section*{Description}

Options = factorGraphSolverOptions returns a default factor graph solver options object, Options.

Options = factorGraphSolverOptions(Name=Value) specifies properties using one or more name-value arguments. For example, factorGraphSolverOptions (MaxIterations=150) sets the MaxIterations property of the factorGraphSolverOptions object to 150.

\section*{Properties}

\section*{MaxIterations - Maximum number of solver iterations}

200 (default) | positive integer
Maximum number of solver iterations, specified as a positive integer.
FunctionTolerance - Lower bound of change in cost function
1e-6 (default) | positive scalar
Lower bound of change in the cost function, specified as a positive scalar. The cost function is:
|newCost - oldCost \(\mid\) < FunctionTolerance *oldCost
All costs are greater than 0 .

\section*{GradientTolerance - Lower bound of norm of gradient}

1e-10 (default) | positive scalar
Lower bound of the norm of the gradient, specified as positive scalar. The norm function is:
max_norm \(\{x-[x *\) Oplus \(-g(x)]\}<=\) GradientTolerance
Oplus is the manifold version of the plus operation and \(g(x)\) is the gradient at \(x\).

\section*{StepTolerance - Lower bound of step size}
le-8 (default) | positive integer
Lower bound of step size of the linear solver, specified as a positive scalar. The relationship between the step size and the step tolerance is:
\(\mid\) deltaX \(\mid<=(|x|+\) StepTolerance \() *\) StepTolerance
deltaX is the step size of the linear solver.

\section*{VerbosityLevel - Command line verbosity flag}

0 (default) | 1 | 2
Command line verbosity flag, specified as 1,2 , or 3.
- 0 - Do not print to command line
- 1 - Print solver summary
- 2 - Print per-iteration updates and solver summary

\section*{TrustRegionStrategyType - Trust region step computation algorithm}

1 (default)|0
Trust region step computation algorithm, specified as 0 or 1 .
- 0 - Levenberg Marquardt
- 1 - Dogleg

\section*{Examples}

\section*{Create and Optimize Factor Graph with Custom Options}

Create and optimize a factor graph with custom solver options.

\section*{Create Factor Graph and Solver Settings}

Create a factor graph and solver options with custom settings. Set the maximum number of iterations to 1000 and set the verbosity of the optimize output to 2 .
```

G = factorGraph;
optns =
factorGraphSolverOptions with properties:
MaxIterations: 1000
FunctionTolerance: 1.0000e-06
GradientTolerance: 1.0000e-10
StepTolerance: 1.0000e-08
VerbosityLevel: 2
TrustRegionStrategyType: 1

```
optns = factorGraphSolverOptions(MaxIterations=1000, VerbosityLevel=2)

\section*{Add GPS Factor}

Create a GPS factor with node identification number of 1 with NED ReferenceFrame and add it to the factor graph.
```

fgps = factorGPS(1,ReferenceFrame="NED");
addFactor(G,fgps);

```

\section*{Optimize Factor Graph}

Optimize the factor graph with the custom settings. The results of the optimization are displayed with the level of detail depending on the VerbosityLevel.
```

optimize(G,optns);
iter cost cost_change |gradient| |step| tr_ratio tr_radius ls_iter iter_time
0 0.000000e+00 0.0.00e+00 0.00e+00 0.00e+00 0.000e+00 1.\overline{0}0\textrm{e}+04
Terminating: Gradient tolerance reached. Gradient max norm: 0.000000e+00 <= 1.000000e-10
Solver Summary (v 2.0.0-eigen-(3.3.4)-no_lapack-eigensparse-no_openmp)
Parameter blocks Origin
Effective parameters 6 6
Residual blocks 1 1
Residuals 3
Minimizer TRUST_REGION
Sparse linear algebra library EIGEN_SPARSE
Trust region strategy DOGLEG (TRADITIONAL)

| Linear solver | SPARSE_NORMAL_CHOLESKY | SPARSE_NORMAL_CHOLESKY |
| :--- | ---: | ---: |
| Threads | 1 | Used |
| Linear solver ordering | AUTOMATIC | 1 |

Cost:
Initial 0.000000e+00
Final 0.000000e+00
Change 0.000000e+00
Minimizer iterations 1
Successful steps 1
Unsuccessful steps 0
Time (in seconds):
Preprocessor 0.024089
Residual only evaluation 0.000000 (0)
Jacobian \& residual evaluation 0.015954 (1)
Linear solver 0.000000 (0)
Minimizer 0.027680
Postprocessor 0.000021
Total 0.051791

```

\section*{See Also}

\section*{Objects}
factorGraph

\section*{Functions}
importFactorGraph

\section*{Topics}
"Factor Graph-Based Pedestrian Localization with IMU and GPS Sensors"
Introduced in R2022a

\section*{insfilterErrorState}

Estimate pose from IMU, GPS, and monocular visual odometry (MVO) data

\section*{Description}

The insfilterErrorState object implements sensor fusion of IMU, GPS, and monocular visual odometry (MVO) data to estimate pose in the NED (or ENU) reference frame. The filter uses a 17element state vector to track the orientation quaternion, velocity, position, IMU sensor biases, and the MVO scaling factor. The insfilterErrorState object uses an error-state Kalman filter to estimate these quantities.

\section*{Creation}

\section*{Syntax}
filter \(=\) insfilterErrorState
filter \(=\) insfilterErrorState('ReferenceFrame',RF)
filter \(=\) insfilterErrorState( _ _ , Name, Value)

\section*{Description}
filter = insfilterErrorState creates an insfilterErrorState object with default property values.
filter = insfilterErrorState('ReferenceFrame',RF) allows you to specify the reference frame, RF, of the filter. Specify RF as 'NED' (North-East-Down) or 'ENU' (East-North-Up). The default value is 'NED'.
filter = insfilterErrorState( \(\qquad\) ,Name, Value) also allows you set properties of the created filter using one or more name-value pairs. Enclose each property name in single quotes.

\section*{Properties}

\section*{IMUSampleRate - Sample rate of IMU (Hz)}

100 (default) | positive scalar
Sample rate of the inertial measurement unit (IMU) in Hz, specified as a positive scalar.

\section*{Data Types: single | double}

ReferenceLocation - Reference location (deg, deg, meters)
[0 0 0] (default) | 3-element positive row vector
Reference location, specified as a 3-element row vector in geodetic coordinates (latitude, longitude, and altitude). Altitude is the height above the reference ellipsoid model, WGS84. The reference location units are [degrees degrees meters].
Data Types: single|double

\section*{GyroscopeNoise - Multiplicative process noise variance from gyroscope ((rad/s) \({ }^{\mathbf{2}}\) )}
[1e-6 1e-6 1e-6] (default)| scalar|3-element row vector
Multiplicative process noise variance from the gyroscope in (rad/s) \({ }^{2}\), specified as a scalar or 3element row vector of positive real finite numbers.
- If GyroscopeNoise is specified as a row vector, the elements correspond to the noise in the \(x, y\), and \(z\) axes of the gyroscope, respectively.
- If GyroscopeNoise is specified as a scalar, the single element is applied to each axis.

Data Types: single | double
GyroscopeBiasNoise - Additive process noise variance from gyroscope bias ((rad/s) \({ }^{\mathbf{2}}\) )
[1e-9 1e-9 1e-9] (default)| scalar | 3-element row vector
Additive process noise variance from the gyroscope bias in \((\mathrm{rad} / \mathrm{s})^{2}\), specified as a scalar or 3-element row vector of positive real finite numbers.
- If GyroscopeBiasNoise is specified as a row vector, the elements correspond to the noise in the \(x, y\), and \(z\) axes of the gyroscope, respectively.
- If GyroscopeBiasNoise is specified as a scalar, the single element is applied to each axis

Data Types: single |double
AccelerometerNoise - Multiplicative process noise variance from accelerometer ((m/s \(\left.\mathbf{s}^{\mathbf{2}}\right)^{\mathbf{2}}\) )
[1e-4 le-4 1e-4] (default)| scalar|3-element row vector
Multiplicative process noise variance from the accelerometer in \(\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}\), specified as a scalar or 3element row vector of positive real finite numbers.
- If AccelerometerNoise is specified as a row vector, the elements correspond to the noise in the \(x, y\), and \(z\) axes of the accelerometer, respectively.
- If AccelerometerNoise is specified as a scalar, the single element is applied to each axis.

Data Types: single | double
AccelerometerBiasNoise - Additive process noise variance from accelerometer bias \(\left(\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}\right)\)
[1e-4 le-4 le-4] (default)| scalar | 3-element row vector
Additive process noise variance from accelerometer bias in \(\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}\), specified as a scalar or 3-element row vector of positive real numbers.
- If AccelerometerBiasNoise is specified as a row vector, the elements correspond to the noise in the \(x, y\), and \(z\) axes of the accelerometer, respectively.
- If AccelerometerBiasNoise is specified as a scalar, the single element is applied to each axis.

\section*{State - State vector of Kalman filter}
[1;zeros(15,1);1] (default)| 17-element column vector
State vector of the extended Kalman filter, specified as a 17 -element column vector. The state values represent:
\begin{tabular}{lll} 
State & Units & Index \\
Orientation (quaternion parts) & \(\mathrm{N} / \mathrm{A}\) & \(1: 4\) \\
Position (NED or ENU) & m & \(5: 7\) \\
Velocity (NED or ENU) & \(\mathrm{m} / \mathrm{s}\) & \(8: 10\) \\
Gyroscope Bias (XYZ) & \(\mathrm{rad} / \mathrm{s}\) & \(11: 13\) \\
Accelerometer Bias (XYZ) & \(\mathrm{m} / \mathrm{s}^{2}\) & \(14: 16\) \\
Visual Odometry Scale (XYZ) & \(\mathrm{N} / \mathrm{A}\) & 17
\end{tabular}

The default initial state corresponds to an object at rest located at [000] in geodetic LLA coordinates.

Data Types: single | double

\section*{StateCovariance - State error covariance for Kalman filter}
ones(16) (default)| 16-by-16 matrix
State error covariance for the Kalman filter, specified as a 16-by-16-element matrix of real numbers. The state error covariance values represent:
\begin{tabular}{ll} 
State Covariance & Row/Column Index \\
\hline\(\delta\) Rotation Vector (XYZ) & \(1: 3\) \\
\(\delta\) Position (NED or ENU) & \(4: 6\) \\
\(\delta\) Velocity (NED or ENU) & \(7: 9\) \\
\(\delta\) Gyroscope Bias (XYZ) & \(10: 12\) \\
\(\delta\) Accelerometer Bias (XYZ) & \(13: 15\) \\
\(\delta\) Visual Odometry Scale (XYZ) & 16
\end{tabular}

Note that because this is an error-state Kalman filter, it tracks the errors in the states. \(\delta\) represents the error in the corresponding state.
Data Types: single | double

\section*{Object Functions}
predict
correct residual
fusegps residualgps
fusemvo residualmvo
pose Current orientation and position estimate for insfilterErrorState
reset Reset internal states for insfilterErrorState
stateinfo Display state vector information for insfilterErrorState tune Tune insfilterErrorState parameters to reduce estimation error
copy Create copy of insfilterErrorState

\section*{Examples}

\section*{Estimate Pose of Ground Vehicle}

Load logged data of a ground vehicle following a circular trajectory. The .mat file contains IMU and GPS sensor measurements and ground truth orientation and position.
```

load('loggedGroundVehicleCircle.mat', ...
'imuFs','localOrigin', ...
'initialStateCovariance', ...
'accelData','gyroData', ...
'gpsFs','gpsLLA','Rpos','gpsVel','Rvel', ...
'trueOrient','truePos');

```

Create an INS filter to fuse IMU and GPS data using an error-state Kalman filter.
```

initialState = [compact(trueOrient(1)),truePos(1,:),-6.8e-3,2.5002,0,zeros(1,6),1].';
filt = insfilterErrorState;
filt.IMUSampleRate = imuFs;
filt.ReferenceLocation = localOrigin;
filt.State = initialState;
filt.StateCovariance = initialStateCovariance;

```

Preallocate variables for position and orientation. Allocate a variable for indexing into the GPS data.
```

numIMUSamples = size(accelData,1);
estOrient = ones(numIMUSamples,1,'quaternion');
estPos = zeros(numIMUSamples,3);
gpsIdx = 1;

```

Fuse accelerometer, gyroscope, and GPS data. The outer loop predicts the filter forward at the fastest sample rate (the IMU sample rate).
```

for idx = 1:numIMUSamples
% Use predict to estimate the filter state based on the accelData and
% gyroData arrays.
predict(filt,accelData(idx,:),gyroData(idx,:));
% GPS data is collected at a lower sample rate than IMU data. Fuse GPS
% data at the lower rate.
if mod(idx, imuFs / gpsFs) == 0
% Correct the filter states based on the GPS data.
fusegps(filt,gpsLLA(gpsIdx,:),Rpos,gpsVel(gpsIdx,:),Rvel);
gpsIdx = gpsIdx + 1;
end
% Log the current pose estimate
[estPos(idx,:), estOrient(idx,:)] = pose(filt);
end

```

Calculate the RMS errors between the known true position and orientation and the output from the error-state filter.
```

pErr = truePos - estPos;
qErr = rad2deg(dist(estOrient,trueOrient));

```
```

pRMS = sqrt(mean(pErr.^2));
qRMS = sqrt(mean(qErr.^2));
fprintf('Position RMS Error\n');
Position RMS Error
fprintf('\tX: %.2f, Y: %.2f, Z: %.2f (meters)\n\n',pRMS(1),pRMS(2),pRMS(3));
X: 0.40, Y: 0.24, Z: 0.05 (meters)
fprintf('Quaternion Distance RMS Error\n');
Quaternion Distance RMS Error
fprintf('\t%.2f (degrees)\n\n',qRMS);
0.30 (degrees)

```

Visualize the true position and the estimated position.
```

plot(truePos(:,1),truePos(:,2),estPos(:,1),estPos(:,2),'r:','LineWidth',2)
grid on
axis square
xlabel('N (m)')
ylabel('E (m)')
legend('Ground Truth','Estimation')

```


\section*{Algorithms}

Note: The following algorithm only applies to an NED reference frame.
insfilterErrorState uses a 17-axis error state Kalman filter structure to estimate pose in the NED reference frame. The state is defined as:
\(\chi=\left[\begin{array}{c}q_{0} \\ q_{1} \\ q_{2} \\ q_{3} \\ \text { position }_{N} \\ \text { position }_{E} \\ \text { position }_{D} \\ v_{N} \\ v_{E} \\ v_{D} \\ \text { gyrobias }_{X} \\ \text { gyrobias }_{Y} \\ \text { gyrobias }_{Z} \\ \text { accelbias } \\ \text { accelbias } \\ \text { a } \\ \text { accelbias } \\ Z \\ \text { scaleFactor }\end{array}\right]\)
where
- \(q_{0}, q_{1}, q_{2}, q_{3}\)-- Parts of orientation quaternion. The orientation quaternion represents a frame rotation from the platform's current orientation to the local NED coordinate system.
- position \({ }_{\mathrm{N}}\), position \(_{\mathrm{E}}\), position \(_{\mathrm{D}}\)-- Position of the platform in the local NED coordinate system.
- gyrobias \(_{\mathrm{X}}\), gyrobias \(_{\mathrm{Y}}\), gyrobias \(_{\mathrm{z}}\)-- Bias in the gyroscope reading.
- accelbias \({ }_{\mathrm{X}}\), accelbias \(_{\mathrm{Y}}\), accelbias \(\mathrm{Z}_{\mathrm{Z}}\)-- Bias in the accelerometer reading.
- scaleFactor -- Scale factor of the pose estimate.

Given the conventional formulation of the state transition function,
\[
x_{k \mid k-1}=f\left(\widehat{x}_{k-1 \mid k-1}\right)
\]
the predicted state estimate is:
where
- \(\Delta t\)-- IMU sample time.
- \(g_{\mathrm{N}}, g_{\mathrm{E}}, g_{\mathrm{D}}--\) Constant gravity vector in the NED frame.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}
insfilterAsync|insfilterMARG|insfilterNonholonomic

Introduced in R2019a

\section*{correct}

Correct states using direct state measurements for insfilterErrorState

\section*{Syntax}
```

correct(FUSE,idx,measurement,measurementCovariance)

```

\section*{Description}
correct(FUSE,idx, measurement, measurementCovariance) corrects the state and state estimation error covariance of FUSE, an insfilterErrorState object, based on the measurement and measurement covariance. The measurement maps directly to the state specified by the indices idx.

\section*{Input Arguments}

FUSE - INS filter object
insfilterErrorState
insfilterErrorState, specified as an object.
idx - State vector index of measurements to correct
\(N\)-element vector of increasing integers in the range [1,17]
State vector index of measurements to correct, specified as an \(N\)-element vector of increasing integers in the range [1, 17].

The state values represent:
\begin{tabular}{lll} 
State & Units & Index \\
Orientation (quaternion parts) & \(\mathrm{N} / \mathrm{A}\) & \(1: 4\) \\
Position (NED) & m & \(5: 7\) \\
Velocity (NED) & \(\mathrm{m} / \mathrm{s}\) & \(8: 10\) \\
Gyroscope Bias (XYZ) & \(\mathrm{rad} / \mathrm{s}\) & \(11: 13\) \\
Accelerometer Bias (XYZ) & \(\mathrm{m} / \mathrm{s}^{2}\) & \(14: 16\) \\
Visual Odometry Scale (XYZ) & \(\mathrm{N} / \mathrm{A}\) & 17
\end{tabular}

Data Types: single | double

\section*{measurement - Direct measurement of state}
\(N\)-element vector
Direct measurement of state, specified as a \(N\)-element vector. \(N\) is the number of elements of the index argument, idx.
Data Types: single | double
measurementCovariance - Covariance of measurement
scalar | \(M\)-element vector | \(M\)-by- \(M\) matrix

Covariance of measurement, specified as a scalar, \(M\)-element vector, or \(M\)-by- \(M\) matrix. If you correct orientation (state indices 1-4), then \(M=\) numel(idx)-1. If you do not correct orientation, then \(M=\) numel(idx).
Data Types: single | double

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).

\section*{See Also}
insfilterErrorState|insfilter
Introduced in R2019a

\section*{copy}

Create copy of insfilterErrorState

\section*{Syntax}
newFilter \(=\) copy(filter)

\section*{Description}
newFilter = copy(filter) returns a copy of the insfilterErrorState, filter, with the exactly same property values.

\section*{Input Arguments}
filter - Filter to be copied
insfilterErrorState
Filter to be copied, specified as an insfilterErrorState object.

\section*{Output Arguments}
newFilter - New copied filter
insfilterErrorState
New copied filter, returned as an insfilterErrorState object.

\section*{See Also}
insfilterErrorState
Introduced in R2020b

\section*{fusegps}

Correct states using GPS data for insfilterErrorState

\section*{Syntax}
[res,resCov] = fusegps(FUSE,position,positionCovariance)
[res,resCov] = fusegps(FUSE,position, positionCovariance,velocity, velocityCovariance)

\section*{Description}
[res,resCov] = fusegps(FUSE,position, positionCovariance) fuses GPS position data to correct the state estimate.
[res,resCov] = fusegps(FUSE,position,positionCovariance,velocity, velocityCovariance) fuses GPS position and velocity data to correct the state estimate.

\section*{Input Arguments}

FUSE - INS filter object
insfilterErrorState
insfilterErrorState, specified as an object.
position - Position of GPS receiver (LLA)
3-element row vector
Position of GPS receiver in geodetic latitude, longitude, and altitude (LLA) specified as a real finite 3element row vector. Latitude and longitude are in degrees with north and east being positive. Altitude is in meters.
Data Types: single | double
positionCovariance - Position measurement covariance of GPS receiver ( \(\mathbf{m}^{\mathbf{2}}\) )
scalar | 3-element row vector | 3-by-3 matrix
Position measurement covariance of GPS receiver in \(\mathrm{m}^{2}\), specified as a 3-by-3 matrix.
Data Types: single | double
velocity - Velocity of GPS receiver in local NED coordinate system ( \(\mathrm{m} / \mathrm{s}\) )
3 -element row vector
Velocity of the GPS receiver in the local NED coordinate system in \(\mathrm{m} / \mathrm{s}\), specified as a 3-element row vector.

Data Types: single | double
velocityCovariance - Velocity measurement covariance of GPS receiver (m/s) \({ }^{\mathbf{2}}\) scalar | 3-element row vector | 3-by-3 matrix

Velocity measurement covariance of the GPS receiver in the local NED coordinate system in (m/s) \({ }^{2}\), specified as a 3-by-3 matrix.

Data Types: single | double

\section*{Output Arguments}

\section*{res - Position and velocity residual}

1-by-6 vector of real values
Position and velocity residual, returned as a 1-by-6 vector of real values in \(m\) and \(m / s\), respectively.

\section*{resCov - Innovation residual}

6 -by-6 matrix of real values
Innovation residual, returned as a 6-by-6 matrix of real values.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).

\section*{See Also}
insfilterErrorState|insfilter
Introduced in R2019a

\section*{fusemvo}

Correct states using monocular visual odometry for insfilterErrorState

\section*{Syntax}
[pResidual,oResidual,resCov] = fusemvo(FUSE,position,positionCovariance,ornt, orntCovariance)

\section*{Description}
[pResidual,oResidual, resCov] = fusemvo(FUSE,position, positionCovariance,ornt, orntCovariance) fuses position and orientation data from monocular visual odometry (MVO) measurements to correct the state and state estimation error covariance.

\section*{Input Arguments}

\section*{FUSE - INS filter object}
insfilterErrorState
insfilterErrorState, specified as an object.
position - Position of camera in local NED coordinate system (m)
3 -element row vector
Position of camera in the local NED coordinate system in meters, specified as a real finite 3-element row vector.
Data Types: single | double
positionCovariance - Position measurement covariance of MVO (m²)
scalar | 3-element vector | 3-by-3 matrix
Position measurement covariance of MVO in \(\mathrm{m}^{2}\), specified as a scalar, 3-element vector, or 3-by-3 matrix.

Data Types: single | double
ornt - Orientation of camera with respect to local NED coordinate system
scalar quaternion | rotation matrix
Orientation of the camera with respect to the local NED coordinate system, specified as a scalar quaternion or 3 -by- 3 rotation matrix. The quaternion or rotation matrix is a frame rotation from the NED coordinate system to the current camera coordinate system.
Data Types: quaternion | single | double
orntCovariance - Orientation measurement covariance of monocular visual odometry \(\left(\mathrm{rad}^{2}\right)\)
scalar | 3-element vector | 3-by-3 matrix
Orientation measurement covariance of monocular visual odometry in \(\operatorname{rad}^{2}\), specified as a scalar, 3element vector, or 3-by-3 matrix.

Data Types: single | double

\section*{Output Arguments}
pResidual - Position residual
1-by-3 vector of real values
Position residual, returned as a 1-by-3 vector of real values in m .
oResidual - Rotation vector residual
1-by-3 vector of real values
Rotation vector residual, returned as a 1-by-3 vector of real values in radians.
resCov - Residual covariance
6 -by-6 matrix of real values
Residual covariance, returned as a 6-by-6 matrix of real values.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).
See Also
insfilterErrorState|insfilter

Introduced in R2019a

\section*{predict}

Update states using accelerometer and gyroscope data for insfilterErrorState

\section*{Syntax}
predict(FUSE, accelReadings,gyroReadings)

\section*{Description}
predict(FUSE, accelReadings,gyroReadings) fuses accelerometer and gyroscope data to update the state estimate.

\section*{Input Arguments}

FUSE - INS filter object
insfilterErrorState
insfilterErrorState, specified as an object.
accelReadings - Accelerometer readings in local sensor body coordinate system (m/s \({ }^{\mathbf{2}}\) )
3-element row vector
Accelerometer readings in \(\mathrm{m} / \mathrm{s}^{2}\), specified as a 3 -element row vector.
Data Types: single|double
gyroReadings - Gyroscope readings in local sensor body coordinate system (rad/s)
3-element row vector
Gyroscope readings in rad/s, specified as a 3 -element row vector.
Data Types: single|double

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder \(^{\text {TM }}\).

\section*{See Also}
insfilterErrorState|insfilter
Introduced in R2019a

\section*{reset}

Reset internal states for insfilterErrorState

\section*{Syntax}
reset (FUSE)

\section*{Description}
reset (FUSE) resets the State, StateCovariance, and internal integrators of FUSE, an insfilterErrorState object, to their default values.

\section*{Input Arguments}

FUSE - INS filter object
insfilterErrorState
insfilterErrorState, specified as an object.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}
insfilterErrorState|insfilter

Introduced in R2019a

\section*{residual}

Residuals and residual covariances from direct state measurements for insfilterErrorState

\section*{Syntax}
[res, resCov]= residual(FUSE,idx,measurement,measurementCovariance)

\section*{Description}
[res, resCov]= residual(FUSE,idx,measurement,measurementCovariance) computes the residual, res, and the residual covariance, resCov, based on the direct state measurement and measurement covariance. The measurement maps directly to the states specified by indices, idx.

\section*{Input Arguments}

FUSE - INS filter object
insfilterErrorState
insfilterErrorState, specified as an object.
idx - State vector index of measurements to correct
\(N\)-element vector of increasing integers in the range [1,17]
State vector index of measurements to correct, specified as an \(N\)-element vector of increasing integers in the range [1, 17].

The state values represent:
\begin{tabular}{lll} 
State & Units & Index \\
\hline Orientation (quaternion parts) & \(\mathrm{N} / \mathrm{A}\) & \(1: 4\) \\
Position (NED) & m & \(5: 7\) \\
Velocity (NED) & \(\mathrm{m} / \mathrm{s}\) & \(8: 10\) \\
Gyroscope Bias (XYZ) & \(\mathrm{rad} / \mathrm{s}\) & \(11: 13\) \\
Accelerometer Bias (XYZ) & \(\mathrm{m} / \mathrm{s}^{2}\) & \(14: 16\) \\
Visual Odometry Scale (XYZ) & \(\mathrm{N} / \mathrm{A}\) & 17
\end{tabular}

Data Types: single | double
measurement - Direct measurement of state
\(N\)-element vector
Direct measurement of state, specified as a \(N\)-element vector. \(N\) is the number of elements of the index argument, idx.

Covariance of measurement, specified as an \(N\)-by- \(N\) matrix. \(N\) is the number of elements of the index argument, idx.

\section*{Output Arguments}

\section*{res - Measurement residual}

1 -by- \(N\) vector of real values
Measurement residual, returned as a 1 -by- \(N\) vector of real values.
resCov - Residual covariance
\(N\)-by- \(N\) matrix of real values
Residual covariance, returned as a \(N\)-by- \(N\) matrix of real values.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}
insfilterErrorState
Introduced in R2020a

\section*{residualgps}

Residuals and residual covariance from GPS measurements for insfilterErrorState

\section*{Syntax}
[res,resCov] = residualgps(FUSE,position,positionCovariance)
[res,resCov] = residualgps(FUSE,position, positionCovariance,velocity, velocityCovariance)

\section*{Description}
[res,resCov] = residualgps(FUSE, position, positionCovariance) computes the residual, res, and the residual covariance, resCov, based on the GPS position measurement and covariance.
[res,resCov] = residualgps(FUSE,position, positionCovariance, velocity, velocityCovariance) computes the residual, res, and the residual covariance, resCov, based on the GPS position measurement and covariance.

\section*{Input Arguments}

FUSE - INS filter object
insfilterErrorState
insfilterErrorState, specified as an object.
position - Position of GPS receiver (LLA)
3 -element row vector
Position of GPS receiver in geodetic latitude, longitude, and altitude (LLA) specified as a real finite 3element row vector. Latitude and longitude are in degrees with north and east being positive. Altitude is in meters.

\section*{Data Types: single | double}
positionCovariance - Position measurement covariance of GPS receiver ( \(\mathbf{m}^{\mathbf{2}}\) )
3-by-3 matrix
Position measurement covariance of GPS receiver in \(\mathrm{m}^{2}\), specified as a 3-by-3 matrix.
Data Types: single | double

\section*{velocity - Velocity of GPS receiver in local NED coordinate system (m/s)}

3-element row vector
Velocity of the GPS receiver in the local NED coordinate system in \(\mathrm{m} / \mathrm{s}\), specified as a 3 -element row vector.

Data Types: single | double
velocityCovariance - Velocity measurement covariance of GPS receiver ( \(\mathbf{m} / \mathbf{s}^{\mathbf{2}}\) )
3-by-3 matrix

Velocity measurement covariance of the GPS receiver in the local NED coordinate system in \(\mathrm{m} / \mathrm{s}^{2}\), specified as a 3-by-3 matrix.

Data Types: single | double

\section*{Output Arguments}

\section*{res - Position and velocity residual}

1 -by- 3 vector of real values | 1 -by-6 vector of real values
Position and velocity residual, returned as a 1-by-3 vector of real values if the inputs only contain position information, and returned as 1-by-6 vector of real values if the inputs also contain velocity information.

\section*{resCov - Residual covariance}

3-by-3 matrix of real values | 6-by-6 matrix of real values
Residual covariance, returned as a 3-by-3 matrix of real values if the inputs only contain position information, and a 6 -by- 6 matrix of real values if the inputs also contain velocity information.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).

\section*{See Also}
insfilterErrorState
Introduced in R2020a

\section*{residualmvo}

Residuals and residual covariance from monocular visual odometry measurements for insfilterErrorState

\section*{Syntax}
[pResidual,oResidual, resCov] = residualmvo(FUSE,position, positionCovariance, ornt,orntCovariance)

\section*{Description}
[pResidual,oResidual,resCov] = residualmvo(FUSE,position,positionCovariance, ornt, orntCovariance) computes the residual information based on the monocular visual odometry measurements and covariance.

\section*{Input Arguments}

FUSE - INS filter object
insfilterErrorState
insfilterErrorState, specified as an object.

\section*{position - Position of camera in local NED coordinate system (m)}

3-element row vector
Position of camera in the local NED coordinate system in meters, specified as a real finite 3-element row vector.

\section*{Data Types: single | double}
positionCovariance - Position measurement covariance of MVO (m²)
scalar | 3-element vector | 3-by-3 matrix
Position measurement covariance of MVO in \(\mathrm{m}^{2}\), specified as a scalar, 3-element vector, or 3-by-3 matrix.
Data Types: single | double
ornt - Orientation of camera with respect to local NED coordinate system
scalar quaternion | rotation matrix
Orientation of the camera with respect to the local NED coordinate system, specified as a scalar quaternion or 3-by-3 rotation matrix. The quaternion or rotation matrix is a frame rotation from the NED coordinate system to the current camera coordinate system.
Data Types: quaternion | single | double
orntCovariance - Orientation measurement covariance of monocular visual odometry \(\left(\mathrm{rad}^{2}\right)\)
scalar | 3-element vector | 3-by-3 matrix

Orientation measurement covariance of monocular visual odometry in \(\operatorname{rad}^{2}\), specified as a scalar, 3element vector, or 3-by-3 matrix.
Data Types: single | double

\section*{Output Arguments}

\section*{pResidual - Position residual}

1-by-3 vector of real values
Position residual, returned as a 1-by-3 vector of real values in meters.
oResidual - Rotation vector residual
1-by-3 vector of real values
Rotation vector residual, returned a 1-by-3 vector of real values in radians.
```

resCov - Residual covariance

```

6-by-6 matrix of real values
Residual covariance, returned as a 6-by-6 matrix of real values.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® \({ }^{\circledR}\) Coder \(^{\text {TM }}\).

\section*{See Also}
insfilterErrorState|insfilter
Introduced in R2020a

\section*{stateinfo}

Display state vector information for insfilterErrorState

\section*{Syntax}
```

stateinfo(FUSE)
info = stateinfo(FUSE)

```

\section*{Description}
stateinfo(FUSE) displays the meaning of each index of the State property of FUSE, an insfilterErrorState object, and the associated units.
info = stateinfo(FUSE) returns a structure with fields containing descriptions of the elements of the state vector of the filter, FUSE.

\section*{Examples}

\section*{State Information of insfilterErrorState}

Create an insfilterErrorState object.
filter \(=\) insfilterErrorState;
Display the state information of the created filter.
```

stateinfo(filter)

| States | Units | Index |
| :--- | :--- | :--- |
| Orientation (quaternion parts) |  | $1: 4$ |
| Position (NAV) | m | $5: 7$ |
| Velocity (NAV) | $\mathrm{m} / \mathrm{s}$ | $8: 10$ |
| Gyroscope Bias (XYZ) | $\mathrm{rad} / \mathrm{s}$ | $11: 13$ |
| Accelerometer Bias (XYZ) | $\mathrm{m} / \mathrm{s}^{2}$ | $14: 16$ |
| Visual Odometry Scale |  | 17 |

```

Output the state information of the filter as a structure.
```

info = stateinfo(filter)
info = struct with fields:
Orientation: [lllll
Position: [5 6 7]
Velocity: [8 9 10]
GyroscopeBias: [11 12 13]
AccelerometerBias: [14 15 16]
VisualOdometryScale: 17

```

\section*{Input Arguments}

FUSE - INS filter object
insfilterErrorState
insfilterErrorState, specified as an object.

\section*{Output Arguments}
info - State information
structure
State information, returned as a structure. The field names of the structure are names of the elements of the state vector in the filter. The values of each field are the corresponding indices of the state vector.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}
insfilterErrorState|insfilter
Introduced in R2019a

\section*{pose}

Current orientation and position estimate for insfilterErrorState

\section*{Syntax}
[position,orientation, velocity] = pose(FUSE)
[position,orientation,velocity] = pose(FUSE,format)

\section*{Description}
[position,orientation, velocity] = pose(FUSE) returns the current estimate of the pose of the object tracked by FUSE, an insfilterErrorState object.
[position,orientation, velocity] = pose(FUSE,format) returns the current estimate of the pose with orientation in the specified orientation format.

\section*{Input Arguments}

\section*{FUSE - INS filter object}
insfilterErrorState
insfilterErrorState, specified as an object.

\section*{format - Output orientation format}
'quaternion' (default) | 'rotmat'
Output orientation format, specified as either 'quaternion' for a quaternion or 'rotmat' for a rotation matrix.

Data Types: char|string

\section*{Output Arguments}

\section*{position - Position estimate expressed in the local coordinate system (m)}

3-element row vector
Position estimate expressed in the local coordinate system of the filter in meters, returned as a 3element row vector.

Data Types: single | double
orientation - Orientation estimate expressed in the local coordinate system
quaternion (default) | 3-by-3 rotation matrix
Orientation estimate expressed in the local coordinate system of the filter, returned as a scalar quaternion or 3-by-3 rotation matrix. The quaternion or rotation matrix represents a frame rotation from the local reference frame of the filter to the body reference frame.
Data Types: single | double | quaternion
velocity - Velocity estimate expressed in local coordinate system (m/s)
3-element row vector
Velocity estimate expressed in the local coordinate system of the filter in \(\mathrm{m} / \mathrm{s}\), returned as a 3 -element row vector.

Data Types: single | double

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder \(^{\text {TM }}\).

\section*{See Also}
insfilterErrorState|insfilter
Introduced in R2019a

\section*{tune}

Tune insfilterErrorState parameters to reduce estimation error

\section*{Syntax}
tunedMeasureNoise = tune(filter,measureNoise, sensorData,groundTruth) tunedMeasureNoise \(=\) tune( \(\qquad\) ,config)

\section*{Description}
tunedMeasureNoise = tune(filter,measureNoise, sensorData, groundTruth) adjusts the properties of the insfilterErrorState filter object, filter, and measurement noises to reduce the root-mean-squared (RMS) state estimation error between the fused sensor data and the ground truth. The function also returns the tuned measurement noise, tunedMeasureNoise. The function uses the property values in the filter and the measurement noise provided in the measureNoise structure as the initial estimate for the optimization algorithm.
tunedMeasureNoise = tune( \(\qquad\) , config) specifies the tuning configuration based on a tunerconfig object, config.

\section*{Examples}

\section*{Tune insfilterErrorState to Optimize Pose Estimate}

Load the recorded sensor data and ground truth data.
```

load('insfilterErrorStateTuneData.mat');

```

Create tables for the sensor data and the truth data.
```

sensorData = table(Accelerometer,Gyroscope, ...
GPSPosition,GPSVelocity,MV00rientation, ...
MVOPosition);
groundTruth = table(Orientation,Position);
Create an insfilterErrorState filter object.

```
```

filter = insfilterErrorState('State',initialState, ...

```
filter = insfilterErrorState('State',initialState, ...
    'StateCovariance',initialStateCovariance);
```

Create a tuner configuration object for the filter. Use the tuner noise function to obtain a set of initial sensor noises used in the filter.

```
cfg = tunerconfig('insfilterErrorState','MaxIterations',40);
measNoise = tunernoise('insfilterErrorState')
measNoise = struct with fields:
    MVOOrientationNoise: 1
            MVOPositionNoise: 1
            GPSPositionNoise: 1
```

```
GPSVelocityNoise: 1
```

Tune the filter and obtain the tuned parameters.

```
tunedmn = tune(filter,measNoise,sensorData, ...
    groundTruth,cfg);
```

| Iteration | Parameter | Metric |
| :---: | :---: | :---: |
| 1 | AccelerometerNoise | $\overline{4.1291}$ |
| 1 | GyroscopeNoise | 4.1291 |
| 1 | AccelerometerBiasNoise | 4.1290 |
| 1 | GyroscopeBiasNoise | 4.1290 |
| 1 | GPSPositionNoise | 4.0213 |
| 1 | GPSVelocityNoise | 4.0051 |
| 1 | MVOPositionNoise | 3.9949 |
| 1 | MV00rientationNoise | 3.9886 |
| 2 | AccelerometerNoise | 3.9886 |
| 2 | GyroscopeNoise | 3.9886 |
| 2 | AccelerometerBiasNoise | 3.9886 |
| 2 | GyroscopeBiasNoise | 3.9886 |
| 2 | GPSPositionNoise | 3.8381 |
| 2 | GPSVelocityNoise | 3.8268 |
| 2 | MVOPositionNoise | 3.8219 |
| 2 | MV00rientationNoise | 3.8035 |
| 3 | AccelerometerNoise | 3.8035 |
| 3 | GyroscopeNoise | 3.8035 |
| 3 | AccelerometerBiasNoise | 3.8035 |
| 3 | GyroscopeBiasNoise | 3.8035 |
| 3 | GPSPositionNoise | 3.6299 |
| 3 | GPSVelocityNoise | 3.6276 |
| 3 | MVOPositionNoise | 3.6241 |
| 3 | MV00rientationNoise | 3.5911 |
| 4 | AccelerometerNoise | 3.5911 |
| 4 | GyroscopeNoise | 3.5911 |
| 4 | AccelerometerBiasNoise | 3.5911 |
| 4 | GyroscopeBiasNoise | 3.5911 |
| 4 | GPSPositionNoise | 3.1728 |
| 4 | GPSVelocityNoise | 3.1401 |
| 4 | MVOPositionNoise | 2.7686 |
| 4 | MV00rientationNoise | 2.6632 |
| 5 | AccelerometerNoise | 2.6632 |
| 5 | GyroscopeNoise | 2.6632 |
| 5 | AccelerometerBiasNoise | 2.6632 |
| 5 | GyroscopeBiasNoise | 2.6632 |
| 5 | GPSPositionNoise | 2.3242 |
| 5 | GPSVelocityNoise | 2.2291 |
| 5 | MVOPositionNoise | 2.2291 |
| 5 | MV00rientationNoise | 2.0904 |
| 6 | AccelerometerNoise | 2.0903 |
| 6 | GyroscopeNoise | 2.0903 |
| 6 | AccelerometerBiasNoise | 2.0903 |
| 6 | GyroscopeBiasNoise | 2.0903 |
| 6 | GPSPositionNoise | 2.0903 |
| 6 | GPSVelocityNoise | 2.0141 |
| 6 | MVOPositionNoise | 1.9952 |
| 6 | MVOOrientationNoise | 1.849 |


| AccelerometerNoise | 1.8497 |
| :---: | :---: |
| GyroscopeNoise | 1.8496 |
| AccelerometerBiasNoise | 1.8496 |
| GyroscopeBiasNoise | 1.8496 |
| GPSPositionNoise | 1.8398 |
| GPSVelocityNoise | 1.7528 |
| MVOPositionNoise | 1.7362 |
| MVOOrientationNoise | 1.5762 |
| AccelerometerNoise | 1.5762 |
| GyroscopeNoise | 1.5762 |
| AccelerometerBiasNoise | 1.5762 |
| GyroscopeBiasNoise | 1.5762 |
| GPSPositionNoise | 1.5762 |
| GPSVelocityNoise | 1.5107 |
| MVOPositionNoise | 1.4786 |
| MVOOrientationNoise | 1.3308 |
| AccelerometerNoise | 1.3308 |
| GyroscopeNoise | 1.3308 |
| AccelerometerBiasNoise | 1.3308 |
| GyroscopeBiasNoise | 1.3308 |
| GPSPositionNoise | 1.3308 |
| GPSVelocityNoise | 1.2934 |
| MVOPositionNoise | 1.2525 |
| MVOOrientationNoise | 1.1462 |
| AccelerometerNoise | 1.1462 |
| GyroscopeNoise | 1.1462 |
| AccelerometerBiasNoise | 1.1462 |
| GyroscopeBiasNoise | 1.1462 |
| GPSPositionNoise | 1.1443 |
| GPSVelocityNoise | 1.1332 |
| MVOPositionNoise | 1.0964 |
| MVOOrientationNoise | 1.0382 |
| AccelerometerNoise | 1.0382 |
| GyroscopeNoise | 1.0382 |
| AccelerometerBiasNoise | 1.0382 |
| GyroscopeBiasNoise | 1.0382 |
| GPSPositionNoise | 1.0348 |
| GPSVelocityNoise | 1.0348 |
| MVOPositionNoise | 1.0081 |
| MVOOrientationNoise | 0.9734 |
| AccelerometerNoise | 0.9734 |
| GyroscopeNoise | 0.9734 |
| AccelerometerBiasNoise | 0.9734 |
| GyroscopeBiasNoise | 0.9734 |
| GPSPositionNoise | 0.9693 |
| GPSVelocityNoise | 0.9682 |
| MVOPositionNoise | 0.9488 |
| MVOOrientationNoise | 0.9244 |
| AccelerometerNoise | 0.9244 |
| GyroscopeNoise | 0.9244 |
| AccelerometerBiasNoise | 0.9244 |
| GyroscopeBiasNoise | 0.9244 |
| GPSPositionNoise | 0.9203 |
| GPSVelocityNoise | 0.9199 |
| MVOPositionNoise | 0.9045 |
| MVOOrientationNoise | 0.8846 |
| AccelerometerNoise | 0.8846 |
| GyroscopeNoise | 0.8846 |


| 14 | AccelerometerBiasNoise | 0.8845 |
| :---: | :---: | :---: |
| 14 | GyroscopeBiasNoise | 0.8845 |
| 14 | GPSPositionNoise | 0.8807 |
| 14 | GPSVelocityNoise | 0.8807 |
| 14 | MVOPositionNoise | 0.8659 |
| 14 | MV00rientationNoise | 0.8501 |
| 15 | AccelerometerNoise | 0.8501 |
| 15 | GyroscopeNoise | 0.8501 |
| 15 | AccelerometerBiasNoise | 0.8500 |
| 15 | GyroscopeBiasNoise | 0.8500 |
| 15 | GPSPositionNoise | 0.8457 |
| 15 | GPSVelocityNoise | 0.8453 |
| 15 | MVOPositionNoise | 0.8299 |
| 15 | MV00rientationNoise | 0.8173 |
| 16 | AccelerometerNoise | 0.8173 |
| 16 | GyroscopeNoise | 0.8173 |
| 16 | AccelerometerBiasNoise | 0.8172 |
| 16 | GyroscopeBiasNoise | 0.8172 |
| 16 | GPSPositionNoise | 0.8122 |
| 16 | GPSVelocityNoise | 0.8116 |
| 16 | MVOPositionNoise | 0.7961 |
| 16 | MVOOrientationNoise | 0.7858 |
| 17 | AccelerometerNoise | 0.7858 |
| 17 | GyroscopeNoise | 0.7858 |
| 17 | AccelerometerBiasNoise | 0.7857 |
| 17 | GyroscopeBiasNoise | 0.7857 |
| 17 | GPSPositionNoise | 0.7807 |
| 17 | GPSVelocityNoise | 0.7800 |
| 17 | MVOPositionNoise | 0.7655 |
| 17 | MV00rientationNoise | 0.7572 |
| 18 | AccelerometerNoise | 0.7572 |
| 18 | GyroscopeNoise | 0.7572 |
| 18 | AccelerometerBiasNoise | 0.7570 |
| 18 | GyroscopeBiasNoise | 0.7570 |
| 18 | GPSPositionNoise | 0.7525 |
| 18 | GPSVelocityNoise | 0.7520 |
| 18 | MVOPositionNoise | 0.7401 |
| 18 | MV00rientationNoise | 0.7338 |
| 19 | AccelerometerNoise | 0.7337 |
| 19 | GyroscopeNoise | 0.7337 |
| 19 | AccelerometerBiasNoise | 0.7335 |
| 19 | GyroscopeBiasNoise | 0.7335 |
| 19 | GPSPositionNoise | 0.7293 |
| 19 | GPSVelocityNoise | 0.7290 |
| 19 | MVOPositionNoise | 0.7185 |
| 19 | MV00rientationNoise | 0.7140 |
| 20 | AccelerometerNoise | 0.7138 |
| 20 | GyroscopeNoise | 0.7138 |
| 20 | AccelerometerBiasNoise | 0.7134 |
| 20 | GyroscopeBiasNoise | 0.7134 |
| 20 | GPSPositionNoise | 0.7086 |
| 20 | GPSVelocityNoise | 0.7068 |
| 20 | MVOPositionNoise | 0.6956 |
| 20 | MV00rientationNoise | 0.6926 |
| 21 | AccelerometerNoise | 0.6922 |
| 21 | GyroscopeNoise | 0.6922 |
| 21 | AccelerometerBiasNoise | 0.6916 |
| 21 | GyroscopeBiasNoise | 0.6916 |

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| GPSPositionNoise | 0.6862 |
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| GPSVelocityNoise | 0.6822 |
| MVOPositionNoise | 0.6682 |
| MVOOrientationNoise | 0.6667 |
| AccelerometerNoise | 0.6660 |
| GyroscopeNoise | 0.6660 |
| AccelerometerBiasNoise | 0.6650 |
| GyroscopeBiasNoise | 0.6650 |
| GPSPositionNoise | 0.6605 |
| GPSVelocityNoise | 0.6541 |
| MVOPositionNoise | 0.6372 |
| MV00rientationNoise | 0.6368 |
| AccelerometerNoise | 0.6356 |
| GyroscopeNoise | 0.6356 |
| AccelerometerBiasNoise | 0.6344 |
| GyroscopeBiasNoise | 0.6344 |
| GPSPositionNoise | 0.6324 |
| GPSVelocityNoise | 0.6252 |
| MVOPositionNoise | 0.6087 |
| MV00rientationNoise | 0.6087 |
| AccelerometerNoise | 0.6075 |
| GyroscopeNoise | 0.6075 |
| AccelerometerBiasNoise | 0.6068 |
| GyroscopeBiasNoise | 0.6068 |
| GPSPositionNoise | 0.6061 |
| GPSVelocityNoise | 0.6032 |
| MVOPositionNoise | 0.6032 |
| MV00rientationNoise | 0.6032 |
| AccelerometerNoise | 0.6017 |
| GyroscopeNoise | 0.6017 |
| AccelerometerBiasNoise | 0.6012 |
| GyroscopeBiasNoise | 0.6012 |
| GPSPositionNoise | 0.6010 |
| GPSVelocityNoise | 0.6005 |
| MVOPositionNoise | 0.6005 |
| MVOOrientationNoise | 0.6005 |
| AccelerometerNoise | 0.5992 |
| GyroscopeNoise | 0.5992 |
| AccelerometerBiasNoise | 0.5987 |
| GyroscopeBiasNoise | 0.5987 |
| GPSPositionNoise | 0.5983 |
| GPSVelocityNoise | 0.5983 |
| MVOPositionNoise | 0.5983 |
| MV00rientationNoise | 0.5983 |
| AccelerometerNoise | 0.5975 |
| GyroscopeNoise | 0.5975 |
| AccelerometerBiasNoise | 0.5974 |
| GyroscopeBiasNoise | 0.5974 |
| GPSPositionNoise | 0.5973 |
| GPSVelocityNoise | 0.5972 |
| MVOPositionNoise | 0.5971 |
| MV00rientationNoise | 0.5971 |
| AccelerometerNoise | 0.5971 |
| GyroscopeNoise | 0.5971 |
| AccelerometerBiasNoise | 0.5970 |
| GyroscopeBiasNoise | 0.5970 |
| GPSPositionNoise | 0.5970 |
| GPSVelocityNoise | 0.5970 |

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| MVOPositionNoise | 0.5970 |
| :---: | :---: |
| MVOOrientationNoise | 0.5970 |
| AccelerometerNoise | 0.5970 |
| GyroscopeNoise | 0.5970 |
| AccelerometerBiasNoise | 0.5970 |
| GyroscopeBiasNoise | 0.5970 |
| GPSPositionNoise | 0.5970 |
| GPSVelocityNoise | 0.5970 |
| MVOPositionNoise | 0.5970 |
| MV00rientationNoise | 0.5970 |
| AccelerometerNoise | 0.5969 |
| GyroscopeNoise | 0.5969 |
| AccelerometerBiasNoise | 0.5969 |
| GyroscopeBiasNoise | 0.5969 |
| GPSPositionNoise | 0.5969 |
| GPSVelocityNoise | 0.5969 |
| MVOPositionNoise | 0.5968 |
| MV00rientationNoise | 0.5968 |
| AccelerometerNoise | 0.5968 |
| GyroscopeNoise | 0.5968 |
| AccelerometerBiasNoise | 0.5968 |
| GyroscopeBiasNoise | 0.5968 |
| GPSPositionNoise | 0.5968 |
| GPSVelocityNoise | 0.5968 |
| MVOPositionNoise | 0.5967 |
| MVOOrientationNoise | 0.5967 |
| AccelerometerNoise | 0.5967 |
| GyroscopeNoise | 0.5967 |
| AccelerometerBiasNoise | 0.5967 |
| GyroscopeBiasNoise | 0.5967 |
| GPSPositionNoise | 0.5967 |
| GPSVelocityNoise | 0.5967 |
| MVOPositionNoise | 0.5966 |
| MV00rientationNoise | 0.5966 |
| AccelerometerNoise | 0.5966 |
| GyroscopeNoise | 0.5966 |
| AccelerometerBiasNoise | 0.5966 |
| GyroscopeBiasNoise | 0.5966 |
| GPSPositionNoise | 0.5966 |
| GPSVelocityNoise | 0.5966 |
| MVOPositionNoise | 0.5965 |
| MV00rientationNoise | 0.5965 |
| AccelerometerNoise | 0.5965 |
| GyroscopeNoise | 0.5965 |
| AccelerometerBiasNoise | 0.5965 |
| GyroscopeBiasNoise | 0.5965 |
| GPSPositionNoise | 0.5965 |
| GPSVelocityNoise | 0.5964 |
| MVOPositionNoise | 0.5964 |
| MVOOrientationNoise | 0.5964 |
| AccelerometerNoise | 0.5964 |
| GyroscopeNoise | 0.5964 |
| AccelerometerBiasNoise | 0.5963 |
| GyroscopeBiasNoise | 0.5963 |
| GPSPositionNoise | 0.5963 |
| GPSVelocityNoise | 0.5963 |
| MVOPositionNoise | 0.5963 |
| MVOOrientationNoise | 0.5963 |


| 36 | AccelerometerNoise | 0.5963 |
| :--- | :--- | :--- |
| 36 | GyroscopeNoise | 0.5963 |
| 36 | AccelerometerBiasNoise | 0.5963 |
| 36 | GyroscopeBiasNoise | 0.5963 |
| 36 | GPSPositionNoise | 0.5963 |
| 36 | GPSVelocityNoise | 0.5963 |
| 36 | MVOPositionNoise | 0.5963 |
| 36 | MV00rientationNoise | 0.5963 |
| 37 | AccelerometerNoise | 0.5963 |
| 37 | GyroscopeNoise | 0.5963 |
| 37 | AccelerometerBiasNoise | 0.5963 |
| 37 | GyroscopeBiasNoise | 0.5963 |
| 37 | GPSPositionNoise | 0.5962 |
| 37 | GPSVelocityNoise | 0.5962 |
| 37 | MVOPositionNoise | 0.5962 |
| 37 | MVOOrientationNoise | 0.5962 |
| 38 | AccelerometerNoise | 0.5962 |
| 38 | GyroscopeNoise | 0.5962 |
| 38 | AccelerometerBiasNoise | 0.5962 |
| 38 | GyroscopeBiasNoise | 0.5962 |
| 38 | GPSPositionNoise | 0.5962 |
| 38 | GPSVelocityNoise | 0.5961 |
| 38 | MVOPositionNoise | 0.5961 |
| 38 | MVOOrientationNoise | 0.5961 |
| 39 | AccelerometerNoise | 0.5961 |
| 39 | GyroscopeNoise | 0.5961 |
| 39 | AccelerometerBiasNoise | 0.5961 |
| 39 | GyroscopeBiasNoise | 0.5961 |
| 39 | GPSPositionNoise | 0.5961 |
| 39 | GPSVelocityNoise | 0.5960 |
| 39 | MVOPositionNoise | 0.5960 |
| 39 | MVOOrientationNoise | 0.5960 |
| 40 | AccelerometerNoise | 0.5960 |
| 40 | GyroscopeNoise | 0.5960 |
| 40 | AccelerometerBiasNoise | 0.5960 |
| 40 | GyroscopeBiasNoise | 0.5960 |
| 40 | GPSPositionNoise | 0.5960 |
| 40 | GPSVelocityNoise | 0.5959 |
| 40 | MVOPositionNoise | 0.5959 |
| 40 | MVoOrientationNoise | 0.5959 |
|  |  |  |

Fuse the sensor data using the tuned filter.

```
N = size(sensorData,1);
qEstTuned = quaternion.zeros(N,1);
posEstTuned = zeros(N,3);
for ii=1:N
    predict(filter, Accelerometer(ii,:),Gyroscope(ii,:));
    if all(~isnan(GPSPosition(ii,1)))
            fusegps(filter,GPSPosition(ii,:), ...
                tunedmn.GPSPositionNoise,GPSVelocity(ii,:), ...
                tunedmn.GPSVelocityNoise);
    end
    if all(~isnan(MVOPosition(ii,1)))
        fusemvo(filter,MVOPosition(ii,:),tunedmn.MVOPositionNoise, ...
                MVOOrientation{ii},tunedmn.MVOOrientationNoise);
    end
```

```
    [posEstTuned(ii,:),qEstTuned(ii,:)] = pose(filter);
```

end

Compute the RMS errors.

```
orientationErrorTuned = rad2deg(dist(qEstTuned,Orientation));
```

rmsOrientationErrorTuned $=$ sqrt(mean(orientationErrorTuned.^2))
rmsOrientationErrorTuned $=4.4999$
positionErrorTuned $=$ sqrt(sum((posEstTuned - Position).^2,2));
rmsPositionErrorTuned $=$ sqrt(mean( positionErrorTuned.^2))
rmsPositionErrorTuned $=0.1172$

Visualize the results.

```
figure;
t = (0:N-1)./filter.IMUSampleRate;
subplot(2,1,1)
plot(t, positionErrorTuned,'b');
title("Tuned insfilterErrorState" + newline + ...
    "Euclidean Distance Position Error")
xlabel('Time (s)');
ylabel('Position Error (meters)')
subplot(2,1,2)
plot(t, orientationErrorTuned,'b');
title("Orientation Error")
xlabel('Time (s)');
ylabel('Orientation Error (degrees)');
```



## Input Arguments

filter - Filter object
insfilterErrorState object
Filter object, specified as an insfilterErrorState object.

## measureNoise - Measurement noise

structure
Measurement noise, specified as a structure. The function uses the measurement noise input as the initial guess for tuning the measurement noise. The structure must contain these fields:

| Field name | Description |
| :--- | :--- |
| MVOOrientationNoise | Orientation measurement covariance of <br> monocular visual odometry, specified as a scalar, <br> 3-element vector, or 3-by-3 matrix in rad |
| MVOPositionNoise | Position measurement covariance of MVO, <br> specified as a scalar, 3-element vector, or 3-by-3 <br> matrix in $\mathrm{m}^{2}$ |
| GPSPositionNoise | Variance of GPS position noise, specified as a <br> scalar in $\mathrm{m}^{2}$ |


| Field name |
| :--- |
| GPSVelocityNoise |
| sensorData - Sensor data |

Sensor data, specified as a table. In each row, the sensor data is specified as:

- Accelerometer - Accelerometer data, specified as a 1-by-3 vector of scalars in $\mathrm{m}^{2} / \mathrm{s}$.
- Gyroscope- Gyroscope data, specified as a 1-by-3 vector of scalars in rad/s.
- MVOOrienation - Orientation of the camera with respect to the local navigation frame, specified as a scalar quaternion or 3-by-3 rotation matrix. The quaternion or rotation matrix is a frame rotation from the local navigation frame to the current camera coordinate system.
- MVOPosition - Position of camera in the local navigation frame, specified as a real 3-element row vector in meters.
- GPSPosition - GPS position data, specified as a 1-by-3 vector of scalars in meters.
- GPSVelocity - GPS velocity data, specified as a 1-by-3 vector of scalars in m/s.

If the GPS sensor does not produce complete measurements, specify the corresponding entry for GPSPosition and/or GPSVelocity as NaN. If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the sensorData input based on your choice.

## groundTruth - Ground truth data <br> table

Ground truth data, specified as a table. In each row, the table can optionally contain any of these variables:

- Orientation - Orientation from the navigation frame to the body frame, specified as a quaternion or a 3-by-3 rotation matrix.
- Position - Position in navigation frame, specified as a 1-by-3 vector of scalars in meters.
- Velocity - Velocity in navigation frame, specified as a 1-by-3 vector of scalars in $\mathrm{m} / \mathrm{s}$.
- AccelerometerBias - Accelerometer delta angle bias in body frame, specified as a 1-by-3 vector of scalars in $\mathrm{m}^{2} / \mathrm{s}$.
- VisualOdometryScale - Visual odometry scale factor, specified as a scalar.

The function processes each row of the sensorData and groundTruth tables sequentially to calculate the state estimate and RMS error from the ground truth. State variables not present in groundTruth input are ignored for the comparison. The sensorData and the groundTruth tables must have the same number of rows.

If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the groundTruth input based on your choice.

## config - Tuner configuration

tunerconfig object
Tuner configuration, specified as a tunerconfig object.

## Output Arguments

## tunedMeasureNoise - Tuned measurement noise

structure
Tuned measurement noise, returned as a structure. The structure contains these fields.

| Field name | Description |
| :--- | :--- |
| MVOOrientationNoise | Orientation measurement covariance of <br> monocular visual odometry, specified as a scalar, <br> 3-element vector, or 3-by-3 matrix in rad |
| MVOPositionNoise | Position measurement covariance of MVO, <br> specified as a scalar, 3-element vector, or 3-by-3 <br> matrix in $\mathrm{m}^{2}$ |
| GPSPositionNoise | Variance of GPS position noise, specified as a <br> scalar in $\mathrm{m}^{2}$ |
| GPSVelocityNoise | Variance of GPS velocity noise, specified as a <br> scalar in $(\mathrm{m} / \mathrm{s})^{2}$ |

## References

[1] Abbeel, P., Coates, A., Montemerlo, M., Ng, A.Y. and Thrun, S. Discriminative Training of Kalman Filters. In Robotics: Science and systems, Vol. 2, pp. 1, 2005.

## See Also

tunerconfig|tunernoise
Introduced in R2021a

## gpsSensor

GPS receiver simulation model

## Description

The gpsSensor System object models data output from a Global Positioning System (GPS) receiver.
To model a GPS receiver:
1 Create the gpsSensor object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

```
GPS = gpsSensor
GPS = gpsSensor('ReferenceFrame',RF)
GPS = gpsSensor(
```

$\qquad$

``` ,Name, Value)
```


## Description

GPS = gpsSensor returns a gpsSensor System object that computes a Global Positioning System receiver reading based on a local position and velocity input signal. The default reference position in geodetic coordinates is

- latitude: $0^{\circ} \mathrm{N}$
- longitude: $0^{\circ} \mathrm{E}$
- altitude: 0 m

GPS = gpsSensor('ReferenceFrame', RF) returns a gpsSensor System object that computes a global positioning system receiver reading relative to the reference frame RF. Specify RF as 'NED' (North-East-Down) or 'ENU' (East-North-Up). The default value is 'NED'.

GPS = gpsSensor( $\qquad$ ,Name, Value) sets each property Name to the specified Value. Unspecified properties have default values.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

## SampleRate - Update rate of receiver (Hz)

1 (default) | positive real scalar
Update rate of the receiver in Hz , specified as a positive real scalar.
Data Types: single | double
ReferenceLocation - Origin of local navigation reference frame
[0 0 0] (default)|[latitude longitude altitude]
Reference location, specified as a 3-element row vector in geodetic coordinates (latitude, longitude, and altitude). Altitude is the height above the reference ellipsoid model, WGS84. The reference location is in [degrees degrees meters]. The degree format is decimal degrees (DD).
Data Types: single | double

## PositionInputFormat - Position coordinate input format

'Local' (default)|'Geodetic'
Position coordinate input format, specified as 'Local' or 'Geodetic'.

- If you set the property as 'Local' , then you need to specify the truePosition input as Cartesian coordinates with respect to the local navigation frame whose origin is fixed and defined by the ReferenceLcation property. Additionally, when you specify the trueVelocity input, you need to specify it with respect to this local navigation frame.
- If you set the property as 'Geodetic', then you need to specify the truePosition input as geodetic coordinates in latitude, longitude, and altitude. Additionally, when you specify the trueVelocity input, you need to specify it with respect to the navigation frame (NED or ENU) whose origin corresponds to the truePosition input. When setting the property as 'Geodetic', the gpsSensor object neglects the ReferenceLocation property.

Data Types: character vector

## HorizontalPositionAccuracy - Horizontal position accuracy (m)

1.6 (default) | nonnegative real scalar

Horizontal position accuracy in meters, specified as a nonnegative real scalar. The horizontal position accuracy specifies the standard deviation of the noise in the horizontal position measurement.

Tunable: Yes
Data Types: single | double

## VerticalPositionAccuracy - Vertical position accuracy (m) <br> 3 (default) | nonnegative real scalar

Vertical position accuracy in meters, specified as a nonnegative real scalar. The vertical position accuracy specifies the standard deviation of the noise in the vertical position measurement.

Tunable: Yes
Data Types: single | double

## VelocityAccuracy - Velocity accuracy (m/s)

## 0.1 (default) | nonnegative real scalar

Velocity accuracy in meters per second, specified as a nonnegative real scalar. The velocity accuracy specifies the standard deviation of the noise in the velocity measurement.

Tunable: Yes
Data Types: single | double

## DecayFactor - Global position noise decay factor

0.999 (default) | scalar in the range [0,1]

Global position noise decay factor, specified as a scalar in the range $[0,1]$.
A decay factor of 0 models the global position noise as a white noise process. A decay factor of 1 models the global position noise as a random walk process.

Tunable: Yes
Data Types: single | double

## RandomStream - Random number source

'Global stream' (default)|'mt19937ar with seed'
Random number source, specified as a character vector or string:

- 'Global stream' -- Random numbers are generated using the current global random number stream.
- 'mt19937ar with seed ' -- Random numbers are generated using the mt19937ar algorithm with the seed specified by the Seed property.

Data Types: char | string

## Seed - Initial seed

67 (default) | nonnegative integer scalar
Initial seed of an mt19937ar random number generator algorithm, specified as a nonnegative integer scalar.

## Dependencies

To enable this property, set RandomStream to 'mt19937ar with seed'.

```
Data Types: single | double | int8 | int16 | int32 | int64 | uint8|uint16|uint32 | uint64
```


## Usage

## Syntax

[position, velocity,groundspeed,course] = GPS(truePosition,trueVelocity)

## Description

[position, velocity,groundspeed,course] = GPS(truePosition,trueVelocity) computes global navigation satellite system receiver readings from the position and velocity inputs.

## Input Arguments

## truePosition - Position of GPS receiver in navigation coordinate system <br> $N$-by-3 matrix

Position of the GPS receiver in the navigation coordinate system, specified as a real finite $N$-by- 3 matrix. $N$ is the number of samples in the current frame.

- When the PositionInputFormat property is specified as 'Local', specify truePosition as Cartesian coordinates with respect to the local navigation frame whose origin is fixed at ReferenceLocation.
- When the PositionInputFormat property is specified as 'Geodetic', specify truePosition as geodetic coordinates in [latitude longitude altitude]. Latitude and longitude are in meters. altitude is the height above the WGS84 ellipsoid model in meters.

Data Types: single | double

## trueVelocity - Velocity of GPS receiver in navigation coordinate system (m/s)

N -by-3 matrix
Velocity of GPS receiver in the navigation coordinate system in meters per second, specified as a real finite $N$-by- 3 matrix. $N$ is the number of samples in the current frame.

- When the PositionInputFormat property is specified as 'Local', specify trueVelocity with respect to the local navigation frame (NED or ENU) whose origin is fixed at ReferenceLocation.
- When the PositionInputFormat property is specified as 'Geodetic', specify trueVelocity with respect to the navigation frame (NED or ENU) whose origin corresponds to the truePosition input.

Data Types: single | double

## Output Arguments

## position - Position in LLA coordinate system

N -by-3 matrix
Position of the GPS receiver in the geodetic latitude, longitude, and altitude (LLA) coordinate system, returned as a real finite $N$-by-3 array. Latitude and longitude are in degrees with North and East being positive. Altitude is in meters.
$N$ is the number of samples in the current frame.
Data Types: single|double

## velocity - Velocity in local navigation coordinate system (m/s)

$N$-by-3 matrix
Velocity of the GPS receiver in the local navigation coordinate system in meters per second, returned as a real finite $N$-by- 3 array. $N$ is the number of samples in the current frame.

- When the PositionInputFormat property is specified as 'Local', the returned velocity is with respect to the local navigation frame whose origin is fixed at ReferenceLocation.
- When the PositionInputFormat property is specified as 'Geodetic', the returned velocity is with respect to the navigation frame (NED or ENU) whose origin corresponds to the position output.

Data Types: single | double
groundspeed - Magnitude of horizontal velocity in local navigation coordinate system (m/s)
$N$-by-1 column vector
Magnitude of the horizontal velocity of the GPS receiver in the local navigation coordinate system in meters per second, returned as a real finite $N$-by- 1 column vector.
$N$ is the number of samples in the current frame.
Data Types: single|double

## course - Direction of horizontal velocity in local navigation coordinate system ( ${ }^{\circ}$ ) $N$-by-1 column vector

Direction of the horizontal velocity of the GPS receiver in the local navigation coordinate system in degrees, returned as a real finite $N$-by- 1 column of values between 0 and 360 . North corresponds to 360 degrees and East corresponds to 90 degrees.
$N$ is the number of samples in the current frame.

## Data Types: single | double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:
release(obj)

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Generate GPS Position Measurements From Stationary Input

Create a gpsSensor System object ${ }^{\text {TM }}$ to model GPS receiver data. Assume a typical one Hz sample rate and a 1000 -second simulation time. Define the reference location in terms of latitude, longitude, and altitude (LLA) of Natick, MA (USA). Define the sensor as stationary by specifying the true position and velocity with zeros.

```
fs = 1;
duration = 1000;
numSamples = duration*fs;
```

```
refLoc = [42.2825 -71.343 53.0352];
truePosition = zeros(numSamples,3);
trueVelocity = zeros(numSamples,3);
gps = gpsSensor('SampleRate',fs,'ReferenceLocation',refLoc);
```

Call gps with the specified truePosition and trueVelocity to simulate receiving GPS data for a stationary platform.

```
position = gps(truePosition,trueVelocity);
```

Plot the true position and the GPS sensor readings for position.

```
t = (0:(numSamples-1))/fs;
subplot(3, 1, 1)
plot(t, position(:,1), ..
    t, ones(numSamples)*refLoc(1))
title('GPS Sensor Readings')
ylabel('Latitude (degrees)')
subplot(3, 1, 2)
plot(t, position(:,2), ...
    t, ones(numSamples)*refLoc(2))
ylabel('Longitude (degrees)')
subplot(3, 1, 3)
plot(t, position(:,3), ...
    t, ones(numSamples)*refLoc(3))
ylabel('Altitude (m)')
xlabel('Time (s)')
```



The position readings have noise controlled by HorizontalPositionAccuracy, VerticalPositionAccuracy, VelocityAccuracy, and DecayFactor. The DecayFactor property controls the drift in the noise model. By default, DecayFactor is set to 0.999, which approaches a random walk process. To observe the effect of the DecayFactor property:

1 Reset the gps object.
2 Set DecayFactor to 0.5.
3 Call gps with variables specifying a stationary position.
4 Plot the results.
The GPS position readings now oscillate around the true position.

```
reset(gps)
gps.DecayFactor = 0.5;
position = gps(truePosition,trueVelocity);
subplot(3, 1, 1)
plot(t, position(:,1), ...
    t, ones(numSamples)*refLoc(1))
title('GPS Sensor Readings - Decay Factor = 0.5')
ylabel('Latitude (degrees)')
subplot(3, 1, 2)
plot(t, position(:,2), ...
    t, ones(numSamples)*refLoc(2))
ylabel('Longitude (degrees)')
```

```
subplot(3, 1, 3)
plot(t, position(:,3), ...
        t, ones(numSamples)*refLoc(3))
ylabel('Altitude (m)')
xlabel('Time (s)')
```



## Relationship Between Groundspeed and Course Accuracy

GPS receivers achieve greater course accuracy as groundspeed increases. In this example, you create a GPS receiver simulation object and simulate the data received from a platform that is accelerating from a stationary position.

Create a default gpsSensor System object ${ }^{\text {TM }}$ to model data returned by a GPS receiver.

```
GPS = gpsSensor
GPS =
    gpsSensor with properties:
```

SampleRate: 1
PositionInputFormat: 'Local' ReferenceLocation: [0 0 0] HorizontalPositionAccuracy: 1.6 VerticalPositionAccuracy: 3

Hz
[deg deg m]
m
m

```
VelocityAccuracy: 0.1 m/s
    RandomStream: 'Global stream'
    DecayFactor: 0.999
```

Create matrices to describe the position and velocity of a platform in the NED coordinate system. The platform begins from a stationary position and accelerates to $60 \mathrm{~m} / \mathrm{s}$ North-East over 60 seconds, then has a vertical acceleration to $2 \mathrm{~m} / \mathrm{s}$ over 2 seconds, followed by a $2 \mathrm{~m} / \mathrm{s}$ rate of climb for another 8 seconds. Assume a constant velocity, such that the velocity is the simple derivative of the position.

```
duration = 70;
numSamples = duration*GPS.SampleRate;
course = 45*ones(duration,1);
groundspeed = [(1:60)';60*ones(10,1)];
Nvelocity = groundspeed.*sind(course);
Evelocity = groundspeed.*cosd(course);
Dvelocity = [zeros(60,1);-1;-2*ones(9,1)];
NEDvelocity = [Nvelocity,Evelocity,Dvelocity];
Ndistance = cumsum(Nvelocity);
Edistance = cumsum(Evelocity);
Ddistance = cumsum(Dvelocity);
NEDposition = [Ndistance,Edistance,Ddistance];
```

Model GPS measurement data by calling the GPS object with your velocity and position matrices.

```
[~,~,groundspeedMeasurement,courseMeasurement] = GPS(NEDposition,NEDvelocity);
```

Plot the groundspeed and the difference between the true course and the course returned by the GPS simulator.

As groundspeed increases, the accuracy of the course increases. Note that the velocity increase during the last ten seconds has no effect, because the additional velocity is not in the ground plane.

```
t = (0:numSamples-1)/GPS.SampleRate;
subplot(2,1,1)
plot(t,groundspeed);
ylabel('Speed (m/s)')
title('Relationship Between Groundspeed and Course Accuracy')
subplot(2,1,2)
courseAccuracy = courseMeasurement - course;
plot(t,courseAccuracy)
xlabel('Time (s)');
ylabel('Course Accuracy (degrees)')
```



## Model GPS Receiver Data

Simulate GPS data received during a trajectory from the city of Natick, MA, to Boston, MA.
Define the decimal degree latitude and longitude for the city of Natick, MA USA, and Boston, MA USA. For simplicity, set the altitude for both locations to zero.

```
NatickLLA = [42.27752809999999, -71.34680909999997, 0];
BostonLLA = [42.3600825, -71.05888010000001, 0];
```

Define a motion that can take a platform from Natick to Boston in 20 minutes. Set the origin of the local NED coordinate system as Natick. Create a waypointTrajectory object to output the trajectory 10 samples at a time.

```
fs = 1;
duration = 60*20;
bearing = 68; % degrees
distance = 25.39e3; % meters
distanceEast = distance*sind(bearing);
distanceNorth = distance*cosd(bearing);
NatickNED = [0,0,0];
BostonNED = [distanceNorth,distanceEast,0];
```

```
trajectory = waypointTrajectory( ...
    'Waypoints', [NatickNED;BostonNED], ...
    'TimeOfArrival',[0;duration], ...
    'SamplesPerFrame',10, ...
    'SampleRate',fs);
```

Create a gpsSensor object to model receiving GPS data for the platform. Set the HorizontalPositionalAccuracy to 25 and the DecayFactor to 0.25 to emphasize the noise. Set the ReferenceLocation to the Natick coordinates in LLA.

```
GPS = gpsSensor( ...
    'HorizontalPositionAccuracy',25, ...
    'DecayFactor',0.25, ...
    'SampleRate',fs, ...
    'ReferenceLocation',NatickLLA);
```

Open a figure and plot the position of Natick and Boston in LLA. Ignore altitude for simplicity.
In a loop, call the gpsSensor object with the ground-truth trajectory to simulate the received GPS data. Plot the ground-truth trajectory and the model of received GPS data.

```
figure(1)
plot(NatickLLA(1),NatickLLA(2),'ko', ...
    BostonLLA(1),BostonLLA(2),'kx')
xlabel('Latitude (degrees)')
ylabel('Longitude (degrees)')
title('GPS Sensor Data for Natick to Boston Trajectory')
hold on
while ~isDone(trajectory)
    [truePositionNED,~,trueVelocityNED] = trajectory();
    reportedPositionLLA = GPS(truePositionNED,trueVelocityNED);
    figure(1)
    plot(reportedPositionLLA(:,1),reportedPositionLLA(:,2),'r.')
end
```



As a best practice, release System objects when complete.

```
release(GPS)
```

release(trajectory)

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

## Objects

imuSensor|insSensor

## Topics

"Model IMU, GPS, and INS/GPS"
Introduced in R2019b

## gyroparams

Gyroscope sensor parameters

## Description

The gyroparams class creates a gyroscope sensor parameters object. You can use this object to model a gyroscope when simulating an IMU with imuSensor. See the "Algorithms" on page 2-477 section of imuSensor for details of gyroparams modeling.

## Creation

## Syntax

```
params = gyroparams
params = gyroparams(Name,Value)
```


## Description

params = gyroparams returns an ideal gyroscope sensor parameters object with default values.
params = gyroparams(Name,Value) configures gyroparams object properties using one or more Name, Value pair arguments. Name is a property name and Value is the corresponding value. Name must appear inside single quotes (' ' ). You can specify several name-value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN. Any unspecified properties take default values.

## Properties

## MeasurementRange - Maximum sensor reading (rad/s)

Inf (default) | real positive scalar
Maximum sensor reading in rad/s, specified as a real positive scalar.
Data Types: single | double

## Resolution - Resolution of sensor measurements ((rad/s)/LSB)

0 (default) | real nonnegative scalar
Resolution of sensor measurements in (rad/s)/LSB, specified as a real nonnegative scalar. Here, LSB is the acronym for least significant bit.

## Data Types: single | double

## ConstantBias - Constant sensor offset bias (rad/s)

[0000] (default) | real scalar | real 3-element row vector
Constant sensor offset bias in rad/s, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3 -element row vector where each element has the input scalar value.
Data Types: single | double

## AxesMisalignment - Sensor axes skew (\%)

diag ([100 100 100]) (default) | scalar in the range [0,100]|3-element row vector in the range $[0,100] \mid 3$-by-3 matrix in the range $[0,100]$

Sensor axes skew in percentage, specified as a scalar, a 3-element row vector, or a 3-by-3 matrix with values ranging from 0 to 100 . The diagonal elements of the matrix account for the misalignment effects for each axes. The off-diagonal elements account for the cross-axes misalignment effects. The measured state $v_{\text {measure }}$ is obtained from the true state $v_{\text {true }}$ via the misalignment matrix as:

$$
v_{\text {measure }}=\frac{1}{100} M v_{\text {true }}=\frac{1}{100}\left[\begin{array}{lll}
m_{11} & m_{12} & m_{13} \\
m_{21} & m_{22} & m_{23} \\
m_{31} & m_{32} & m_{33}
\end{array}\right] v_{\text {true }}
$$

- If you specify the property as a scalar, then all the off-diagonal elements of the matrix take the value of the specified scalar and all the diagonal elements are 100.
- If you specify the property as a vector [ $a b c$ ], then $m_{21}=m_{31}=a, m_{12}=m_{32}=b$, and $m_{13}=m_{23}=$ $c$. All the diagonal elements are 100.


## Data Types: single | double

## NoiseDensity - Power spectral density of sensor noise ((rad/s)/VHz)

[0 0 0 0 (default) | real scalar | real 3-element row vector
Power spectral density of sensor noise in $(\mathrm{rad} / \mathrm{s}) / \mathrm{VHz}$, specified as a real scalar or 3-element row vector. This property corresponds to the angle random walk (ARW). Any scalar input is converted into a real 3 -element row vector where each element has the input scalar value.
Data Types: single | double

## BiasInstability - Instability of the bias offset (rad/s)

[0 0000$]$ (default) | real scalar | real 3-element row vector
Instability of the bias offset in rad/s, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

## Data Types: single | double

## RandomWalk - Integrated white noise of sensor ((rad/s)(VHz))

[0 0 0] (default) | real scalar | real 3-element row vector
Integrated white noise of sensor in $(\mathrm{rad} / \mathrm{s})(\sqrt{\mathrm{Hz}})$, specified as a real scalar or 3 -element row vector. Any scalar input is converted into a real 3 -element row vector where each element has the input scalar value.
Data Types: single | double
TemperatureBias - Sensor bias from temperature ((rad/s)/ ${ }^{\circ} \mathbf{C}$ )
[0 0 0 0] (default) | real scalar | real 3-element row vector
Sensor bias from temperature in $\left((\mathrm{rad} / \mathrm{s}) /{ }^{\circ} \mathrm{C}\right)$, specified as a real scalar or 3 -element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.
Data Types: single | double

## TemperatureScaleFactor - Scale factor error from temperature (\%/ ${ }^{\circ} \mathbf{C}$ )

$\left[\begin{array}{lll}0 & 0 & 0\end{array}\right]$ (default) | real scalar in the range [0,100] | real 3-element row vector in the range $[0,100]$
Scale factor error from temperature in $\left(\% /{ }^{\circ} \mathrm{C}\right)$, specified as a real scalar or 3 -element row vector with values ranging from 0 to 100 . Any scalar input is converted into a real 3 -element row vector where each element has the input scalar value.

Data Types: single | double

## AccelerationBias - Sensor bias from linear acceleration (rad/s)/(m/s ${ }^{\mathbf{2}}$ )

[0 0 0 0 ] (default) | real scalar | real 3-element row vector
Sensor bias from linear acceleration in $(\mathrm{rad} / \mathrm{s}) /\left(\mathrm{m} / \mathrm{s}^{2}\right)$, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3 -element row vector where each element has the input scalar value.

## Data Types: single | double

## Examples

## Generate Gyroscope Data from Stationary Inputs

Generate gyroscope data for an imuSensor object from stationary inputs.
Generate a gyroscope parameter object with a maximum sensor reading of $4.363 \mathrm{rad} / \mathrm{s}$ and a resolution of $1.332 \mathrm{e}-4(\mathrm{rad} / \mathrm{s}) / \mathrm{LSB}$. The constant offset bias is $0.349 \mathrm{rad} / \mathrm{s}$. The sensor has a power spectral density of $8.727 \mathrm{e}-4 \mathrm{rad} / \mathrm{s} / \sqrt{\mathrm{Hz}}$. The bias from temperature is $0.349 \mathrm{rad} / \mathrm{s} / 0 \mathrm{C}$. The bias from temperature is $0.349\left(\mathrm{rad} / \mathrm{s}^{2}\right) /{ }^{\circ} \mathrm{C}$. The scale factor error from temperature is $0.2 \% / 0 \mathrm{C}$. The sensor axes are skewed by $2 \%$. The sensor bias from linear acceleration is $0.178 \mathrm{e}-3(\mathrm{rad} / \mathrm{s}) /\left(\mathrm{m} / \mathrm{s}^{2}\right)$
params = gyroparams('MeasurementRange',4.363,'Resolution',1.332e-04,'ConstantBias', 0.349, 'NoiseD
Use a sample rate of 100 Hz spaced out over 1000 samples. Create the imuSensor object using the gyroscope parameter object.

Fs = 100;
numSamples = 1000;
$\mathrm{t}=0: 1 / \mathrm{Fs}:($ numSamples-1)/Fs;
imu = imuSensor('accel-gyro','SampleRate', Fs, 'Gyroscope', params);
Generate gyroscope data from the imuSensor object.

```
orient = quaternion.ones(numSamples, 1);
acc = zeros(numSamples, 3);
angvel = zeros(numSamples, 3);
[~, gyroData] = imu(acc, angvel, orient);
```

Plot the resultant gyroscope data.

```
plot(t, gyroData)
title('Gyroscope')
xlabel('s')
ylabel('rad/s')
```



## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

accelparams | magparams |imuSensor

## Introduced in R2018b

## imufilter

Orientation from accelerometer and gyroscope readings

## Description

The imufilter System object fuses accelerometer and gyroscope sensor data to estimate device orientation.

To estimate device orientation:
1 Create the imufilter object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

```
FUSE = imufilter
FUSE = imufilter('ReferenceFrame',RF)
FUSE = imufilter(
```

$\qquad$

``` ,Name,Value)
```


## Description

FUSE = imufilter returns an indirect Kalman filter System object, FUSE, for fusion of accelerometer and gyroscope data to estimate device orientation. The filter uses a nine-element state vector to track error in the orientation estimate, the gyroscope bias estimate, and the linear acceleration estimate.

FUSE = imufilter('ReferenceFrame',RF) returns an imufilter filter System object that fuses accelerometer and gyroscope data to estimate device orientation relative to the reference frame RF. Specify RF as 'NED ' (North-East-Down) or 'ENU ' (East-North-Up). The default value is 'NED'.

FUSE = imufilter( $\qquad$ ,Name, Value) sets each property Name to the specified Value.
Unspecified properties have default values.
Example: FUSE = imufilter('SampleRate',200,'GyroscopeNoise',le-6) creates a System object, FUSE, with a 200 Hz sample rate and gyroscope noise set to $1 \mathrm{e}-6$ radians per second squared.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

## SampleRate - Sample rate of input sensor data (Hz)

100 (default) | positive finite scalar
Sample rate of the input sensor data in Hz , specified as a positive finite scalar.
Tunable: No
Data Types: single | double | uint8 | uint16 | uint32 | uint64 | int8 | int16|int32|int64

## DecimationFactor - Decimation factor

1 (default) | positive integer scalar
Decimation factor by which to reduce the sample rate of the input sensor data, specified as a positive integer scalar.

The number of rows of the inputs, accelReadings and gyroReadings, must be a multiple of the decimation factor.

Tunable: No
Data Types: single | double | uint8 | uint16|uint32 | uint64 | int8|int16|int32|int64
AccelerometerNoise - Variance of accelerometer signal noise ((m/s $\left.\left.\mathbf{s}^{\mathbf{2}}\right)^{\mathbf{2}}\right)$
0.00019247 (default) | positive real scalar

Variance of accelerometer signal noise in $\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}$, specified as a positive real scalar.
Tunable: Yes
Data Types: single | double | uint8 | uint16 | uint32 | uint64 | int8 | int16|int32 |int64

## GyroscopeNoise - Variance of gyroscope signal noise ((rad/s) ${ }^{\mathbf{2}}$ )

9.1385e-5 (default) | positive real scalar

Variance of gyroscope signal noise in (rad/s) ${ }^{2}$, specified as a positive real scalar.
Tunable: Yes
Data Types: single | double |uint8|uint16|uint32|uint64 | int8|int16|int32|int64
GyroscopeDriftNoise - Variance of gyroscope offset drift ((rad/s) ${ }^{\mathbf{2}}$ )
3.0462e-13 (default) | positive real scalar

Variance of gyroscope offset drift in (rad/s) $)^{2}$, specified as a positive real scalar.
Tunable: Yes
Data Types: single | double | uint8 | uint16|uint32|uint64 | int8|int16|int32|int64

## LinearAccelerationNoise - Variance of linear acceleration noise ((m/s $\left.\mathbf{s}^{\mathbf{2}}\right)^{\mathbf{2}}$

### 0.0096236 (default) | positive real scalar

Variance of linear acceleration noise in $\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}$, specified as a positive real scalar. Linear acceleration is modeled as a lowpass filtered white noise process.

## Tunable: Yes

Data Types: single | double | uint8 | uint16 | uint32 | uint64 | int8 | int16| int32 | int64

## LinearAcclerationDecayFactor - Decay factor for linear acceleration drift

0.5 (default) | scalar in the range [0,1]

Decay factor for linear acceleration drift, specified as a scalar in the range [0,1]. If linear acceleration is changing quickly, set LinearAccelerationDecayFactor to a lower value. If linear acceleration changes slowly, set LinearAccelerationDecayFactor to a higher value. Linear acceleration drift is modeled as a lowpass-filtered white noise process.

Tunable: Yes
Data Types: single | double | uint8 | uint16 | uint32 | uint64 | int8|int16|int32|int64

## InitialProcessNoise - Covariance matrix for process noise

9-by-9 matrix
Covariance matrix for process noise, specified as a 9 -by- 9 matrix. The default is:
Columns 1 through 6

| 0.000006092348396 | 0 | 0 | 0 | 0 | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0.000006092348396 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0.000006092348396 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0.000076154354947 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0.000076154354947 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0.000076154354947 |
| 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 |

Columns 7 through 9

| 0 | 0 | 0 |
| ---: | ---: | ---: |
| 0 | 0 | 0 |
| 0 | 0 | 0 |
| 0 | 0 | 0 |
| 0 | 0 | 0 |
| 0 | 0 | 0 |
| 0.009623610000000 | 0 | 0 |
| 0 | 0.009623610000000 | 0 |
| 0 | 0 | 0.009623610000000 |

The initial process covariance matrix accounts for the error in the process model.
Data Types: single | double | uint8 | uint16 | uint32 | uint64 | int8 | int16| int32 | int64

## OrientationFormat - Output orientation format

'quaternion' (default)|'Rotation matrix'
Output orientation format, specified as 'quaternion' or 'Rotation matrix'. The size of the output depends on the input size, $N$, and the output orientation format:

- 'quaternion' -- Output is an $N$-by-1 quaternion.
- 'Rotation matrix' -- Output is a 3 -by-3-by- $N$ rotation matrix.

Data Types: char | string

## Usage

## Syntax

[orientation,angularVelocity] = FUSE(accelReadings,gyroReadings)

## Description

[orientation, angularVelocity] = FUSE(accelReadings,gyroReadings) fuses accelerometer and gyroscope readings to compute orientation and angular velocity measurements. The algorithm assumes that the device is stationary before the first call.

## Input Arguments

## accelReadings - Accelerometer readings in sensor body coordinate system (m/s $\mathbf{s}^{\mathbf{2}}$ ) <br> $N$-by-3 matrix

Accelerometer readings in the sensor body coordinate system in $\mathrm{m} / \mathrm{s}^{2}$, specified as an $N$-by- 3 matrix. $N$ is the number of samples, and the three columns of accelReadings represent the [ $x y z$ ] measurements. Accelerometer readings are assumed to correspond to the sample rate specified by the SampleRate property.

Data Types: single | double
gyroReadings - Gyroscope readings in sensor body coordinate system (rad/s)
N -by-3 matrix
Gyroscope readings in the sensor body coordinate system in rad/s, specified as an $N$-by- 3 matrix. $N$ is the number of samples, and the three columns of gyroReadings represent the $[x y z$ ] measurements. Gyroscope readings are assumed to correspond to the sample rate specified by the SampleRate property.

## Data Types: single | double

## Output Arguments

## orientation - Orientation that rotates quantities from global coordinate system to sensor body coordinate system <br> $M$-by-1 vector of quaternions (default) | 3 -by-3-by- $M$ array

Orientation that can rotate quantities from a global coordinate system to a body coordinate system, returned as quaternions or an array. The size and type of orientation depends on whether the OrienationFormat property is set to 'quaternion' or 'Rotation matrix':

- 'quaternion ' -- The output is an $M$-by-1 vector of quaternions, with the same underlying data type as the inputs.
- 'Rotation matrix' -- The output is a 3-by-3-by-M array of rotation matrices the same data type as the inputs.

The number of input samples, $N$, and the DecimationFactor property determine $M$.
You can use orientation in a rotateframe function to rotate quantities from a global coordinate system to a sensor body coordinate system.
Data Types: quaternion | single | double

## angularVelocity - Angular velocity in sensor body coordinate system (rad/s) <br> M-by-3 array (default)

Angular velocity with gyroscope bias removed in the sensor body coordinate system in rad/s, returned as an $M$-by- 3 array. The number of input samples, $N$, and the DecimationFactor property determine $M$.

Data Types: single | double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to imufilter

tune Tune imufilter parameters to reduce estimation error

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Estimate Orientation from IMU data

Load the rpy_9axis file, which contains recorded accelerometer, gyroscope, and magnetometer sensor data from a device oscillating in pitch (around $y$-axis), then yaw (around $z$-axis), and then roll (around $x$-axis). The file also contains the sample rate of the recording.

```
load 'rpy_9axis.mat' sensorData Fs
accelerometerReadings = sensorData.Acceleration;
gyroscopeReadings = sensorData.AngularVelocity;
```

Create an imufilter System object ${ }^{\mathrm{TM}}$ with sample rate set to the sample rate of the sensor data. Specify a decimation factor of two to reduce the computational cost of the algorithm.

```
decim = 2;
fuse = imufilter('SampleRate',Fs,'DecimationFactor',decim);
```

Pass the accelerometer readings and gyroscope readings to the imufilter object, fuse, to output an estimate of the sensor body orientation over time. By default, the orientation is output as a vector of quaternions.
q = fuse(accelerometerReadings,gyroscopeReadings);
Orientation is defined by the angular displacement required to rotate a parent coordinate system to a child coordinate system. Plot the orientation in Euler angles in degrees over time.
imufilter fusion correctly estimates the change in orientation from an assumed north-facing initial orientation. However, the device's $x$-axis was pointing southward when recorded. To correctly estimate the orientation relative to the true initial orientation or relative to NED, use ahrsfilter.

```
time = (0:decim:size(accelerometerReadings,1)-1)/Fs;
plot(time,eulerd(q,'ZYX','frame'))
title('Orientation Estimate')
legend('Z-axis', 'Y-axis', 'X-axis')
xlabel('Time (s)')
ylabel('Rotation (degrees)')
```



## Model Tilt Using Gyroscope and Accelerometer Readings

Model a tilting IMU that contains an accelerometer and gyroscope using the imuSensor System object ${ }^{\text {TM }}$. Use ideal and realistic models to compare the results of orientation tracking using the imufilter System object.

Load a struct describing ground-truth motion and a sample rate. The motion struct describes sequential rotations:

1 yaw: 120 degrees over two seconds
2 pitch: 60 degrees over one second

3 roll: 30 degrees over one-half second
4 roll: -30 degrees over one-half second
5 pitch: -60 degrees over one second
6 yaw: -120 degrees over two seconds
In the last stage, the motion struct combines the 1st, 2nd, and 3rd rotations into a single-axis rotation. The acceleration, angular velocity, and orientation are defined in the local NED coordinate system.

```
load y120p60r30.mat motion fs
accNED = motion.Acceleration;
angVelNED = motion.AngularVelocity;
orientationNED = motion.Orientation;
numSamples = size(motion.Orientation,1);
t = (0:(numSamples-1)).'/fs;
```

Create an ideal IMU sensor object and a default IMU filter object.

```
IMU = imuSensor('accel-gyro','SampleRate',fs);
aFilter = imufilter('SampleRate',fs);
```

In a loop:
1 Simulate IMU output by feeding the ground-truth motion to the IMU sensor object.
2 Filter the IMU output using the default IMU filter object.
orientation = zeros(numSamples, 1, 'quaternion');
for $\mathrm{i}=1$ :numSamples
[accelBody,gyroBody] = IMU(accNED(i,:),angVelNED(i,:),orientationNED(i,:));
orientation(i) = aFilter(accelBody,gyroBody);
end
release(aFilter)
Plot the orientation over time.

```
figure(1)
plot(t,eulerd(orientation,'ZYX','frame'))
xlabel('Time (s)')
ylabel('Rotation (degrees)')
title('Orientation Estimation -- Ideal IMU Data, Default IMU Filter')
legend('Z-axis','Y-axis','X-axis')
```



Modify properties of your imuSensor to model real-world sensors. Run the loop again and plot the orientation estimate over time.

IMU.Accelerometer = accelparams( ...
'MeasurementRange',19.62, ...
'Resolution',0.00059875, ...
'ConstantBias',0.4905, ...
'AxesMisalignment',2, ...
'NoiseDensity',0.003924, ...
'BiasInstability',0, ...
'TemperatureBias', [0.34335 0.34335 0.5886], ...
'TemperatureScaleFactor',0.02);
IMU.Gyroscope = gyroparams( ...
'MeasurementRange',4.3633, ...
'Resolution',0.00013323, ...
'AxesMisalignment',2, ...
'NoiseDensity',8.7266e-05, ...
'TemperatureBias',0.34907, ...
'TemperatureScaleFactor',0.02, ...
'AccelerationBias',0.00017809, ...
'ConstantBias',[0.3491,0.5,0]);
orientationDefault = zeros(numSamples,1,'quaternion');
for i = 1:numSamples
[accelBody,gyroBody] = IMU(accNED(i,:), angVelNED(i,:),orientationNED(i,:));

```
    orientationDefault(i) = aFilter(accelBody,gyroBody);
end
release(aFilter)
figure(2)
plot(t,eulerd(orientationDefault,'ZYX','frame'))
xlabel('Time (s)')
ylabel('Rotation (degrees)')
title('Orientation Estimation -- Realistic IMU Data, Default IMU Filter')
legend('Z-axis','Y-axis','X-axis')
```



The ability of the imufilter to track the ground-truth data is significantly reduced when modeling a realistic IMU. To improve performance, modify properties of your imufilter object. These values were determined empirically. Run the loop again and plot the orientation estimate over time.

```
aFilter.GyroscopeNoise = 7.6154e-7;
aFilter.AccelerometerNoise = 0.0015398;
aFilter.GyroscopeDriftNoise = 3.0462e-12;
aFilter.LinearAccelerationNoise = 0.00096236;
aFilter.InitialProcessNoise = aFilter.InitialProcessNoise*10;
orientationNondefault = zeros(numSamples,1,'quaternion');
for i = 1:numSamples
    [accelBody,gyroBody] = IMU(accNED(i,:),angVelNED(i,:),orientationNED(i,:));
    orientationNondefault(i) = aFilter(accelBody,gyroBody);
```

```
end
release(aFilter)
figure(3)
plot(t,eulerd(orientationNondefault,'ZYX','frame'))
xlabel('Time (s)')
ylabel('Rotation (degrees)')
title('Orientation Estimation -- Realistic IMU Data, Nondefault IMU Filter')
legend('Z-axis','Y-axis','X-axis')
```



To quantify the improved performance of the modified imufilter, plot the quaternion distance between the ground-truth motion and the orientation as returned by the imufilter with default and nondefault properties.

```
qDistDefault = rad2deg(dist(orientationNED,orientationDefault));
qDistNondefault = rad2deg(dist(orientationNED,orientationNondefault));
figure(4)
plot(t,[qDistDefault,qDistNondefault])
title('Quaternion Distance from True Orientation')
legend('Realistic IMU Data, Default IMU Filter', ...
    'Realistic IMU Data, Nondefault IMU Filter')
xlabel('Time (s)')
ylabel('Quaternion Distance (degrees)')
```



## Remove Bias from Angular Velocity Measurement

This example shows how to remove gyroscope bias from an IMU using imufilter.
Use kinematicTrajectory to create a trajectory with two parts. The first part has a constant angular velocity about the $y$-and $z$-axes. The second part has a varying angular velocity in all three axes.

```
duration = 60*8;
fs = 20;
numSamples = duration * fs;
rng('default') % Seed the RNG to reproduce noisy sensor measurements.
initialAngVel = [0,0.5,0.25];
finalAngVel = [-0.2,0.6,0.5];
constantAngVel = repmat(initialAngVel,floor(numSamples/2),1);
varyingAngVel = [linspace(initialAngVel(1), finalAngVel(1), ceil(numSamples/2)).', ...
    linspace(initialAngVel(2), finalAngVel(2), ceil(numSamples/2)).', ...
    linspace(initialAngVel(3), finalAngVel(3), ceil(numSamples/2)).'];
angVelBody = [constantAngVel; varyingAngVel];
accBody = zeros(numSamples,3);
traj = kinematicTrajectory('SampleRate',fs);
[~,qNED,~,accNED,angVelNED] = traj(accBody,angVelBody);
```

Create an imuSensor System object ${ }^{\text {TM }}$, IMU, with a nonideal gyroscope. Call IMU with the groundtruth acceleration, angular velocity, and orientation.

```
IMU = imuSensor('accel-gyro', ...
    'Gyroscope',gyroparams('RandomWalk',0.003,'ConstantBias',0.3), ...
    'SampleRate',fs);
[accelReadings, gyroReadingsBody] = IMU(accNED,angVelNED,qNED);
```

Create an imufilter System object, fuse. Call fuse with the modeled accelerometer readings and gyroscope readings.

```
fuse = imufilter('SampleRate',fs, 'GyroscopeDriftNoise', le-6);
[~,angVelBodyRecovered] = fuse(accelReadings,gyroReadingsBody);
```

Plot the ground-truth angular velocity, the gyroscope readings, and the recovered angular velocity for each axis.

The angular velocity returned from the imufilter compensates for the effect of the gyroscope bias over time and converges to the true angular velocity.

```
time = (0:numSamples-1)'/fs;
figure(1)
plot(time,angVelBody(:,1), ...
    time,gyroReadingsBody(:,1), ...
    time,angVelBodyRecovered(:,1))
title('X-axis')
legend('True Angular Velocity', ...
        'Gyroscope Readings', ...
        'Recovered Angular Velocity')
ylabel('Angular Velocity (rad/s)')
```


## X-axis


figure(2)
plot(time, angVelBody(:,2), ...
time,gyroReadingsBody(:,2), ...
time, angVelBodyRecovered (:, 2 )
title('Y-axis')
ylabel('Angular Velocity (rad/s)')

figure(3)
plot (time, angVelBody(:,3), ...
time, gyroReadingsBody(:,3), ..
time, angVelBodyRecovered (: , 3) )
title('Z-axis')
ylabel('Angular Velocity (rad/s)')
xlabel('Time (s)')

## Z-axis



## Algorithms

Note: The following algorithm only applies to an NED reference frame.
The imufilter uses the six-axis Kalman filter structure described in [1]. The algorithm attempts to track the errors in orientation, gyroscope offset, and linear acceleration to output the final orientation and angular velocity. Instead of tracking the orientation directly, the indirect Kalman filter models the error process, $\chi$, with a recursive update:

$$
x_{k}=\left[\begin{array}{l}
\theta_{k} \\
b_{k} \\
a_{k}
\end{array}\right]=F_{k}\left[\begin{array}{l}
\theta_{k}-1 \\
b_{k-1} \\
a_{k-1}
\end{array}\right]+w_{k}
$$

where $x_{k}$ is a 9 -by- 1 vector consisting of:

- $\theta_{k}$-- 3-by-1 orientation error vector, in degrees, at time $k$
- $b_{k}$-- 3-by-1 gyroscope zero angular rate bias vector, in deg/s, at time $k$
- $a_{k}-$ - 3-by-1 acceleration error vector measured in the sensor frame, in g , at time $k$
- $w_{k}--9$-by- 1 additive noise vector
- $F_{k}$-- state transition model

Because $\chi_{\mathrm{k}}$ is defined as the error process, the a priori estimate is always zero, and therefore the state transition model, $F_{k}$, is zero. This insight results in the following reduction of the standard Kalman equations:

Standard Kalman equations:

$$
\begin{aligned}
& x_{k}^{-}=F_{k} x_{k}^{+}-1 \\
& P_{k}^{-}=F_{k} P_{k-1}^{+} F_{k}^{T}+Q_{k} \\
& y_{k}=z_{k}-H_{k} x_{k}^{-} \\
& S_{k}=R_{k}+H_{k} P_{k}^{-} H_{k} T \\
& K_{k}=P_{k}^{-} H_{k}^{T}\left(S_{k}\right)^{-1} \\
& x_{k}^{+}=x_{k}^{-}+K_{k} y_{k} \\
& P_{k}^{+}=P_{k}^{-}-K_{k} H_{k} P_{k}^{-}
\end{aligned}
$$

Kalman equations used in this algorithm:

$$
\begin{aligned}
& x_{k}^{-}=0 \\
& P_{k^{-}}=Q_{k} \\
& y_{k}=z_{k} \\
& S_{k}=R_{k}+H_{k} P_{k}^{-} H_{k} T \\
& K_{k}=P_{k}^{-} H_{k}^{T}\left(S_{k}\right)^{-1} \\
& x_{k}^{+}=K_{k} y_{k} \\
& P_{k}^{+}=P_{k}{ }^{-}-K_{k} H_{k} P_{k}^{-}
\end{aligned}
$$

where

- $x_{k}{ }^{-}$-- predicted (a priori) state estimate; the error process
- $P_{k}{ }^{-}$-- predicted (a priori) estimate covariance
- $y_{k}$-- innovation
- $S_{k}$-- innovation covariance
- $K_{k}--$ Kalman gain
- $x_{k}{ }^{+}$-- updated (a posteriori) state estimate
- $P_{k}{ }^{+}$-- updated (a posteriori) estimate covariance
$k$ represents the iteration, the superscript ${ }^{+}$represents an a posteriori estimate, and the superscript ${ }^{-}$ represents an a priori estimate.

The graphic and following steps describe a single frame-based iteration through the algorithm.


Before the first iteration, the accelReadings and gyroReadings inputs are chunked into 1-by-3 frames and DecimationFactor-by-3 frames, respectively. The algorithm uses the most current accelerometer readings corresponding to the chunk of gyroscope readings.

## Detailed Overview

Step through the algorithm for an explanation of each stage of the detailed overview.


## Model

The algorithm models acceleration and angular change as linear processes.


## Predict Orientation

The orientation for the current frame is predicted by first estimating the angular change from the previous frame:

$$
\Delta \varphi_{N \times 3}=\frac{\left(\text { gyroReadings }_{N \times 3}-\text { gyroOffset }_{1 \times 3}\right)}{f s}
$$

where $N$ is the decimation factor specified by the DecimationFactor property, and $f s$ is the sample rate specified by the SampleRate property.

The angular change is converted into quaternions using the rotvec quaternion construction syntax:

$$
\Delta Q_{N \times 1}=\text { quaternion }\left(\Delta \varphi_{N \times 3}, \text { rotvec }^{\prime}\right)
$$

The previous orientation estimate is updated by rotating it by $\Delta Q$ :

$$
q_{1 \times 1}^{-}=\left(q_{1}^{+} \times 1\right)\left(\prod_{n=1}^{N} \Delta Q_{n}\right)
$$

During the first iteration, the orientation estimate, $q^{-}$, is initialized by ecompass with an assumption that the $x$-axis points north.

## Estimate Gravity from Orientation

The gravity vector is interpreted as the third column of the quaternion, $q^{-}$, in rotation matrix form:

$$
g_{1 \times 3}=(r \operatorname{Prior}(:, 3))^{T}
$$

See ecompass for an explanation of why the third column of rPrior can be interpreted as the gravity vector.

## Estimate Gravity from Acceleration

A second gravity vector estimation is made by subtracting the decayed linear acceleration estimate of the previous iteration from the accelerometer readings:

```
gAccel }1\times3=\mp@subsup{accelReadings}{1\times3}{}-\mp@subsup{\mathrm{ linAccelprior }}{1\times3}{
```


## Error Model

The error model is the difference between the gravity estimate from the accelerometer readings and the gravity estimate from the gyroscope readings: $z=g-g A c c e l$.


## Kalman Equations

The Kalman equations use the gravity estimate derived from the gyroscope readings, $g$, and the observation of the error process, $z$, to update the Kalman gain and intermediary covariance matrices. The Kalman gain is applied to the error signal, $z$, to output an a posteriori error estimate, $\chi^{+}$.


## Observation Model

The observation model maps the 1-by-3 observed state, $g$, into the 3-by-9 true state, $H$.
The observation model is constructed as:

$$
H_{3 \times 9}=\left[\begin{array}{ccccccccc}
0 & g_{z} & -g_{y} & 0 & -\kappa g_{z} & \kappa g_{y} & 1 & 0 & 0 \\
-g_{z} & 0 & g_{x} & \kappa g_{z} & 0 & -\kappa g_{x} & 0 & 1 & 0 \\
g_{y} & -g_{x} & 0 & -\kappa g_{y} & \kappa g_{x} & 0 & 0 & 0 & 1
\end{array}\right]
$$

where $g_{x}, g_{y}$, and $g_{z}$ are the $x$-, $y$-, and $z$-elements of the gravity vector estimated from the orientation, respectively. $\kappa$ is a constant determined by the SampleRate and DecimationFactor properties: $\kappa=$ DecimationFactor/SampleRate.

See sections 7.3 and 7.4 of [1] for a derivation of the observation model.

## Innovation Covariance

The innovation covariance is a 3-by-3 matrix used to track the variability in the measurements. The innovation covariance matrix is calculated as:

$$
S_{3 \times 3}=R_{3 \times 3}+\left(H_{3 \times 9}\right)\left(P_{9 \times 9}^{-}\right)\left(H_{3 \times 9}\right)^{T}
$$

where

- $H$ is the observation model matrix
- $P^{-}$is the predicted (a priori) estimate of the covariance of the observation model calculated in the previous iteration
- $R$ is the covariance of the observation model noise, calculated as:

$$
R_{3 \times 3}=(\lambda+\xi+\kappa(\beta+\eta))\left[\begin{array}{lll}
1 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & 1
\end{array}\right] .
$$

The following properties define the observation model noise variance:

- $K_{--}$(DecimationFactor/SampleRate) ${ }^{2}$
- $\beta$-- GyroscopeDriftNoise
- $\eta$-- GyroscopeNoise
- $\lambda$-- AccelerometerNoise
- $\xi$-- LinearAccelerationNoise


## Update Error Estimate Covariance

The error estimate covariance is a 9-by-9 matrix used to track the variability in the state.
The error estimate covariance matrix is updated as:

$$
P_{9 \times 9}^{+}=P_{9 \times 9}^{-}-\left(K_{9 \times 3}\right)\left(H_{3 \times 9}\right)\left(P_{9 \times 9}^{-}\right)
$$

where $K$ is the Kalman gain, $H$ is the measurement matrix, and $P^{-}$is the error estimate covariance calculated during the previous iteration.

## Predict Error Estimate Covariance

The error estimate covariance is a 9 -by- 9 matrix used to track the variability in the state. The a priori error estimate covariance, $P^{-}$, is set to the process noise covariance, $Q$, determined during the previous iteration. $Q$ is calculated as a function of the a posteriori error estimate covariance, $P^{+}$. When calculating $Q$, the cross-correlation terms are assumed to be negligible compared to the autocorrelation terms, and are set to zero:

$$
Q=
$$

$\left[\begin{array}{ccccc}P^{+}(1)+\kappa^{2} P^{+}(31)+\beta+\eta & 0 & 0 & -K\left(P^{+}(31)+\beta\right) & 0 \\ 0 & P^{+}(11)+K^{2} P^{+}(41)+\beta+\eta & 0 & 0 & -K\left(P^{+}(41)+\right. \\ 0 & 0 & P^{+}(21)+K^{2} P^{+}(51)+\beta+\eta & 0 & 0 \\ -K\left(P^{+}(31)+\beta\right) & 0 & 0 & P^{+}(31)+\beta & 0 \\ 0 & -K\left(P^{+}(41)+\beta\right) & 0 & 0 & P^{+}(41)+\beta \\ 0 & 0 & -K\left(P^{+}(51)+\beta\right) & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0\end{array}\right.$
where

- $P^{+}$-- is the updated (a posteriori) error estimate covariance
- $\kappa$-- DecimationFactor/SampleRate
- $\beta$-- GyroscopeDriftNoise
- $\eta$-- GyroscopeNoise
- $\nu$-- LinearAcclerationDecayFactor
- $\xi$-- LinearAccelerationNoise

See section 10.1 of [1] for a derivation of the terms of the process error matrix.

## Kalman Gain

The Kalman gain matrix is a 9-by-3 matrix used to weight the innovation. In this algorithm, the innovation is interpreted as the error process, $z$.

The Kalman gain matrix is constructed as:

$$
K_{9 \times 3}=\left(P_{9 \times 9}^{-}\right)\left(H_{3 \times 9}\right)^{T}\left(\left(S_{3 \times 3}\right)^{T}\right)^{-1}
$$

where

- $P^{-}$-- predicted error covariance
- H -- observation model
- $S$-- innovation covariance


## Update a Posteriori Error

The a posterior error estimate is determined by combining the Kalman gain matrix with the error in the gravity vector estimations:

$$
x_{9 \times 1}=\left(K_{9 \times 3}\right)\left(z_{1 \times 3}\right)^{T}
$$

Correct


## Estimate Orientation

The orientation estimate is updated by multiplying the previous estimation by the error:

$$
q^{+}=\left(q^{-}\right)\left(\theta^{+}\right)
$$

## Estimate Linear Acceleration

The linear acceleration estimation is updated by decaying the linear acceleration estimation from the previous iteration and subtracting the error:

$$
\text { linAccelPrior }=\left(\text { linAccelPrior }_{k-1}\right) \nu-b^{+}
$$

where

- $\quad \nu$-- LinearAcclerationDecayFactor


## Estimate Gyroscope Offset

The gyroscope offset estimation is updated by subtracting the gyroscope offset error from the gyroscope offset from the previous iteration:

$$
\text { gyroOffset }=\text { gyroOffset }_{k-1}-a^{+}
$$

## Compute Angular Velocity

To estimate angular velocity, the frame of gyroReadings are averaged and the gyroscope offset computed in the previous iteration is subtracted:

$$
\text { angularVelocity }_{1 \times 3}=\frac{\sum \text { gyroReadings }_{N \times 3}}{N}-\text { gyroOffset }_{1 \times 3}
$$

where $N$ is the decimation factor specified by the DecimationFactor property.
The gyroscope offset estimation is initialized to zeros for the first iteration.

## References

[1] Open Source Sensor Fusion. https://github.com/memsindustrygroup/Open-Source-Sensor-Fusion/ tree/master/docs
[2] Roetenberg, D., H.J. Luinge, C.T.M. Baten, and P.H. Veltink. "Compensation of Magnetic Disturbances Improves Inertial and Magnetic Sensing of Human Body Segment Orientation." IEEE Transactions on Neural Systems and Rehabilitation Engineering. Vol. 13. Issue 3, 2005, pp. 395-405.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder ${ }^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

ecompass|ahrsfilter|imuSensor|gpsSensor

## Introduced in R2018b

## tune

Tune imufilter parameters to reduce estimation error

## Syntax

```
tune(filter,sensorData,groundTruth)
tune(
```

$\qquad$

``` , config)
```


## Description

tune(filter, sensorData, groundTruth) adjusts the properties of the imufilter filter object, filter, to reduce the root-mean-squared (RMS) quaternion distance error between the fused sensor data and the ground truth. The function fuses the sensor data to estimate the orientation, which is compared to the orientation in the ground truth. The function uses the property values in the filter as the initial estimate for the optimization algorithm.
tune( $\qquad$ , config) specifies the tuning configuration based on a tunerconfig object, config.

## Examples

## Tune imufilter to Optimize Orientation Estimate

Load recorded sensor data and ground truth data.

```
ld = load('imufilterTuneData.mat');
qTrue = ld.groundTruth.Orientation; % true orientation
```

Create an imufilter object and fuse the filter with the sensor data.

```
fuse = imufilter;
qEstUntuned = fuse(ld.sensorData.Accelerometer, ...
    ld.sensorData.Gyroscope);
```

Create a tunerconfig object and tune the imufilter to improve the orientation estimate.

```
cfg = tunerconfig('imufilter');
tune(fuse, ld.sensorData, ld.groundTruth, cfg);
\begin{tabular}{llll} 
Iteration & & Parameter & Metric \\
\cline { 1 - 1 } & & & AccelerometerNoise \\
1 & & GyroscopeNoise & 0.1149 \\
1 & & GyroscopeDriftNoise & 0.1146 \\
1 & & LinearAccelerationNoise & 0.1146 \\
1 & & LinearAccelerationDecayFactor & 0.1122 \\
2 & & AccelerometerNoise & 0.1103 \\
2 & & GyroscopeNoise & 0.1102 \\
2 & & GyroscopeDriftNoise & 0.1098 \\
2 & & LinearAccelerationNoise & 0.1098 \\
2 & & LinearAccelerationDecayFactor & 0.1070 \\
3 & & AccelerometerNoise & 0.1053 \\
& & & 0.1053
\end{tabular}
```

| GyroscopeNoise | 0.1048 |
| :---: | :---: |
| GyroscopeDriftNoise | 0.1048 |
| LinearAccelerationNoise | 0.1016 |
| LinearAccelerationDecayFactor | 0.1002 |
| AccelerometerNoise | 0.1001 |
| GyroscopeNoise | 0.0996 |
| GyroscopeDriftNoise | 0.0996 |
| LinearAccelerationNoise | 0.0962 |
| LinearAccelerationDecayFactor | 0.0950 |
| AccelerometerNoise | 0.0950 |
| GyroscopeNoise | 0.0943 |
| GyroscopeDriftNoise | 0.0943 |
| LinearAccelerationNoise | 0.0910 |
| LinearAccelerationDecayFactor | 0.0901 |
| AccelerometerNoise | 0.0900 |
| GyroscopeNoise | 0.0893 |
| GyroscopeDriftNoise | 0.0893 |
| LinearAccelerationNoise | 0.0862 |
| LinearAccelerationDecayFactor | 0.0855 |
| AccelerometerNoise | 0.0855 |
| GyroscopeNoise | 0.0848 |
| GyroscopeDriftNoise | 0.0848 |
| LinearAccelerationNoise | 0.0822 |
| LinearAccelerationDecayFactor | 0.0818 |
| AccelerometerNoise | 0.0817 |
| GyroscopeNoise | 0.0811 |
| GyroscopeDriftNoise | 0.0811 |
| LinearAccelerationNoise | 0.0791 |
| LinearAccelerationDecayFactor | 0.0789 |
| AccelerometerNoise | 0.0788 |
| GyroscopeNoise | 0.0782 |
| GyroscopeDriftNoise | 0.0782 |
| LinearAccelerationNoise | 0.0769 |
| LinearAccelerationDecayFactor | 0.0768 |
| AccelerometerNoise | 0.0768 |
| GyroscopeNoise | 0.0762 |
| GyroscopeDriftNoise | 0.0762 |
| LinearAccelerationNoise | 0.0754 |
| LinearAccelerationDecayFactor | 0.0753 |
| AccelerometerNoise | 0.0753 |
| GyroscopeNoise | 0.0747 |
| GyroscopeDriftNoise | 0.0747 |
| LinearAccelerationNoise | 0.0741 |
| LinearAccelerationDecayFactor | 0.0740 |
| AccelerometerNoise | 0.0740 |
| GyroscopeNoise | 0.0734 |
| GyroscopeDriftNoise | 0.0734 |
| LinearAccelerationNoise | 0.0728 |
| LinearAccelerationDecayFactor | 0.0728 |
| AccelerometerNoise | 0.0728 |
| GyroscopeNoise | 0.0721 |
| GyroscopeDriftNoise | 0.0721 |
| LinearAccelerationNoise | 0.0715 |
| LinearAccelerationDecayFactor | 0.0715 |
| AccelerometerNoise | 0.0715 |
| GyroscopeNoise | 0.0706 |
| GyroscopeDriftNoise | 0.0706 |
| LinearAccelerationNoise | 0.0700 |


| 14 | LinearAccelerationDecayFactor | 0.0700 |
| :--- | :--- | :--- |
| 15 | AccelerometerNoise | 0.0700 |
| 15 | GyroscopeNoise | 0.0690 |
| 15 | GyroscopeDriftNoise | 0.0690 |
| 15 | LinearAccelerationNoise | 0.0684 |
| 15 | LinearAccelerationDecayFactor | 0.0684 |
| 16 | AccelerometerNoise | 0.0684 |
| 16 | GyroscopeNoise | 0.0672 |
| 16 | GyroscopeDriftNoise | 0.0672 |
| 16 | LinearAccelerationNoise | 0.0668 |
| 16 | LinearAccelerationDecayFactor | 0.0667 |
| 17 | AccelerometerNoise | 0.0667 |
| 17 | GyroscopeNoise | 0.0655 |
| 17 | GyroscopeDriftNoise | 0.0655 |
| 17 | LinearAccelerationNoise | 0.0654 |
| 17 | LinearAccelerationDecayFactor | 0.0654 |
| 18 | AccelerometerNoise | 0.0654 |
| 18 | GyroscopeNoise | 0.0641 |
| 18 | GyroscopeDriftNoise | 0.0641 |
| 18 | LinearAccelerationNoise | 0.0640 |
| 18 | LinearAccelerationDecayFactor | 0.0639 |
| 19 | AccelerometerNoise | 0.0639 |
| 19 | GyroscopeNoise | 0.0627 |
| 19 | GyroscopeDriftNoise | 0.0627 |
| 19 | LinearAccelerationNoise | 0.0627 |
| 19 | LinearAccelerationDecayFactor | 0.0624 |
| 20 | AccelerometerNoise | 0.0624 |
| 20 | GyroscopeNoise | 0.0614 |
| 20 | GyroscopeDriftNoise | 0.0614 |
| 20 | LinearAccelerationNoise | 0.0613 |
| 20 | LinearAccelerationDecayFactor | 0.0613 |

Fuse the sensor data again using the tuned filter.

```
qEstTuned = fuse(ld.sensorData.Accelerometer, ...
    ld.sensorData.Gyroscope);
```

Compare the tuned and untuned filter RMS error performances.

```
dUntuned = rad2deg(dist(qEstUntuned, qTrue));
dTuned = rad2deg(dist(qEstTuned, qTrue));
rmsUntuned = sqrt(mean(dUntuned.^2))
rmsUntuned = 6.5864
rmsTuned = sqrt(mean(dTuned.^2))
rmsTuned = 3.5098
```

Visualize the results.

```
N = numel(dUntuned);
t = (0:N-1)./ fuse.SampleRate;
plot(t, dUntuned, 'r', t, dTuned, 'b');
legend('Untuned', 'Tuned');
title('imufilter - Tuned vs Untuned Error')
xlabel('Time (s)');
ylabel('Orientation Error (degrees)');
```

imufilter - Tuned vs Untuned Error


## Input Arguments

filter - Filter object
imufilter object
Filter object, specified as an imufilter object.

## sensorData - Sensor data <br> table

Sensor data, specified as a table. In each row, the sensor data is specified as:

- Accelerometer - Accelerometer data, specified as a 1 -by-3 vector of scalars in $\mathrm{m}^{2} / \mathrm{s}$.
- Gyroscope - Gyroscope data, specified as a 1-by-3 vector of scalars in rad/s.

If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the sensorData input based on your choice.

## groundTruth - Ground truth data

timetable
Ground truth data, specified as a table. The table has only one column of Orientation data. In each row, the orientation is specified as a quaternion object or a 3-by-3 rotation matrix.

The function processes each row of the sensorData and groundTruth tables sequentially to calculate the state estimate and RMS error from the ground truth. Each row of the sensorData and the groundTruth tables must correspond to each other.

If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the groundTruth input based on your choice.

## config - Tuner configuration

tunerconfig object
Tuner configuration, specified as a tunerconfig object.

## References

[1] Abbeel, P., Coates, A., Montemerlo, M., Ng, A.Y. and Thrun, S. Discriminative Training of Kalman Filters. In Robotics: Science and systems, Vol. 2, pp. 1, 2005.

## See Also

Introduced in R2020b

## imuSensor

IMU simulation model

## Description

The imuSensor System object models receiving data from an inertial measurement unit (IMU).
To model an IMU:
1 Create the imuSensor object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

```
IMU = imuSensor
IMU = imuSensor('accel-gyro')
IMU = imuSensor('accel-mag')
IMU = imuSensor('accel-gyro-mag')
IMU = imuSensor(___,'ReferenceFrame',RF)
IMU = imuSensor(___,Name,Value)
```


## Description

IMU = imuSensor returns a System object, IMU, that computes an inertial measurement unit reading based on an inertial input signal. IMU has an ideal accelerometer and gyroscope.

IMU = imuSensor('accel-gyro') returns an imuSensor System object with an ideal accelerometer and gyroscope. imuSensor and imuSensor('accel-gyro') are equivalent creation syntaxes.

IMU = imuSensor('accel-mag') returns an imuSensor System object with an ideal accelerometer and magnetometer.

IMU = imuSensor('accel-gyro-mag' ) returns an imuSensor System object with an ideal accelerometer, gyroscope, and magnetometer.

IMU = imuSensor( $\qquad$ ,'ReferenceFrame', RF) returns an imuSensor System object that computes an inertial measurement unit reading relative to the reference frame RF. Specify RF as 'NED ' (North-East-Down) or 'ENU ' (East-North-Up). The default value is 'NED'.

IMU = imuSensor( $\qquad$ ,Name, Value) sets each property Name to the specified Value.
Unspecified properties have default values. This syntax can be used in combination with any of the previous input arguments.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## IMUType - Type of inertial measurement unit

'accel-gyro' (default)|'accel-mag'|'accel-gyro-mag'
Type of inertial measurement unit, specified as a 'accel-gyro', 'accel-mag', or 'accel-gyromag'.

The type of inertial measurement unit specifies which sensor readings to model:

- 'accel-gyro' -- Accelerometer and gyroscope
- 'accel-mag' -- Accelerometer and magnetometer
- 'accel-gyro-mag' -- Accelerometer, gyroscope, and magnetometer

You can specify IMUType as a value-only argument during creation or as a Name, Value pair.

## Data Types: char | string

## SampleRate - Sample rate of sensor (Hz)

100 (default) | positive scalar
Sample rate of the sensor model in Hz , specified as a positive scalar.
Data Types: single | double
Temperature - Temperature of IMU ( ${ }^{\circ} \mathrm{C}$ )
25 (default) | real scalar
Operating temperature of the IMU in degrees Celsius, specified as a real scalar.
When the object calculates temperature scale factors and environmental drift noises, $25^{\circ} \mathrm{C}$ is used as the nominal temperature.

Tunable: Yes
Data Types: single | double

## MagneticField - Magnetic field vector in local navigation coordinate system ( $\mu \mathrm{T}$ )

[27.5550-2.4169-16.0849] (default) | real scalar
Magnetic field vector in microtesla, specified as a three-element row vector in the local navigation coordinate system.

The default magnetic field corresponds to the magnetic field at latitude zero, longitude zero, and altitude zero.

Tunable: Yes
Data Types: single | double

## Accelerometer - Accelerometer sensor parameters <br> accelparams object (default)

Accelerometer sensor parameters, specified by an accelparams object.
Tunable: Yes

## Gyroscope - Gyroscope sensor parameters

gyroparams object (default)
Gyroscope sensor parameters, specified by a gyroparams object.
Tunable: Yes
Magnetometer - Magnetometer sensor parameters
magparams object (default)
Magnetometer sensor parameters, specified by a magparams object.
Tunable: Yes

## RandomStream - Random number source

'Global stream' (default)|'mt19937ar with seed'
Random number source, specified as a character vector or string:

- 'Global stream' -- Random numbers are generated using the current global random number stream.
- 'mt19937ar with seed' -- Random numbers are generated using the mt19937ar algorithm with the seed specified by the Seed property.

Data Types: char | string

## Seed - Initial seed

67 (default) | nonnegative integer scalar
Initial seed of an mt19937ar random number generator algorithm, specified as a real, nonnegative integer scalar.

## Dependencies

To enable this property, set RandomStream to 'mt19937ar with seed'.
Data Types: single | double | int8 | int16 | int32 | int64 | uint8|uint16|uint32|uint64

## Usage

## Syntax

[accelReadings,gyroReadings] = IMU(acc,angVel)
[accelReadings,gyroReadings] = IMU(acc,angVel,orientation)
[accelReadings,magReadings] = IMU(acc,angVel)
[accelReadings,magReadings] = IMU(acc,angVel,orientation)

```
[accelReadings,gyroReadings,magReadings] = IMU(acc,angVel)
[accelReadings,gyroReadings,magReadings] = IMU(acc,angVel,orientation)
```


## Description

[accelReadings,gyroReadings] = IMU(acc,angVel) generates accelerometer and gyroscope readings from the acceleration and angular velocity inputs.

This syntax is only valid if IMUType is set to 'accel-gyro' or 'accel-gyro-mag'.
[accelReadings,gyroReadings] = IMU(acc,angVel,orientation) generates accelerometer and gyroscope readings from the acceleration, angular velocity, and orientation inputs.

This syntax is only valid if IMUType is set to 'accel-gyro' or 'accel-gyro-mag'.
[accelReadings,magReadings] = IMU(acc,angVel) generates accelerometer and magnetometer readings from the acceleration and angular velocity inputs.

This syntax is only valid if IMUType is set to 'accel-mag '.
[accelReadings,magReadings] = IMU(acc,angVel,orientation) generates accelerometer and magnetometer readings from the acceleration, angular velocity, and orientation inputs.

This syntax is only valid if IMUType is set to 'accel-mag'.
[accelReadings,gyroReadings,magReadings] = IMU(acc,angVel) generates accelerometer, gyroscope, and magnetometer readings from the acceleration and angular velocity inputs.

This syntax is only valid if IMUType is set to 'accel-gyro-mag'.
[accelReadings,gyroReadings,magReadings] = IMU(acc,angVel,orientation) generates accelerometer, gyroscope, and magnetometer readings from the acceleration, angular velocity, and orientation inputs.

This syntax is only valid if IMUType is set to 'accel-gyro-mag'.

## Input Arguments

## acc - Acceleration of IMU in local navigation coordinate system ( $\mathbf{m} / \mathbf{s}^{\mathbf{2}}$ )

$N$-by-3 matrix
Acceleration of the IMU in the local navigation coordinate system, specified as a real, finite $N$-by- 3 array in meters per second squared. $N$ is the number of samples in the current frame.

## Data Types: single | double

## angVel - Angular velocity of IMU in local navigation coordinate system (rad/s)

N -by-3 matrix
Angular velocity of the IMU in the local navigation coordinate system, specified as a real, finite $N$ -by-3 array in radians per second. $N$ is the number of samples in the current frame.

## Data Types: single | double

Orientation of the IMU with respect to the local navigation coordinate system, specified as a quaternion $N$-element column vector or a 3 -by-3-by- $N$ rotation matrix. Each quaternion or rotation matrix represents a frame rotation from the local navigation coordinate system to the current IMU sensor body coordinate system. $N$ is the number of samples in the current frame.
Data Types: single|double|quaternion

## Output Arguments

accelReadings - Accelerometer measurement of IMU in sensor body coordinate system (m/s ${ }^{2}$ )
$N$-by-3 matrix
Accelerometer measurement of the IMU in the sensor body coordinate system, specified as a real, finite $N$-by- 3 array in meters per second squared. $N$ is the number of samples in the current frame.

## Data Types: single|double

gyroReadings - Gyroscope measurement of IMU in sensor body coordinate system (rad/s)
$N$-by-3 matrix
Gyroscope measurement of the IMU in the sensor body coordinate system, specified as a real, finite $N$-by-3 array in radians per second. $N$ is the number of samples in the current frame.

## Data Types: single | double

magReadings - Magnetometer measurement of IMU in sensor body coordinate system ( $\mu \mathrm{T}$ )
$N$-by-3 matrix (default)
Magnetometer measurement of the IMU in the sensor body coordinate system, specified as a real, finite $N$-by-3 array in microtelsa. $N$ is the number of samples in the current frame.
Data Types: single | double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:
release(obj)

## Specific to imuSensor

loadparams Load sensor parameters from JSON file
perturbations Perturbation defined on object
perturb Apply perturbations to object

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Create Default imuSensor System object

The imuSensor System object ${ }^{\text {TM }}$ enables you to model the data received from an inertial measurement unit consisting of a combination of gyroscope, accelerometer, and magnetometer.

Create a default imuSensor object.

```
IMU = imuSensor
IMU =
    imuSensor with properties:
            IMUType: 'accel-gyro'
            SampleRate: 100
            Temperature: 25
        Accelerometer: [1x1 accelparams]
            Gyroscope: [1x1 gyroparams]
            RandomStream: 'Global stream'
```

The imuSensor object, IMU, contains an idealized gyroscope and accelerometer. Use dot notation to view properties of the gyroscope.

IMU. Gyroscope

```
ans =
    gyroparams with properties:
        MeasurementRange: Inf rad/s
            Resolution: 0 (rad/s)/LSB
            ConstantBias: [0 0 0] rad/s
        AxesMisalignment: [3x3 double] %
            NoiseDensity: [0 0 0] (rad/s)/\sqrt{}{Hz}
        BiasInstability: [0 0 0] rad/s
            RandomWalk: [0 0 0] (rad/s)*/ Hz
            TemperatureBias: [0 0 0] (rad/s)/ }\mp@subsup{}{}{\circ}\textrm{C
        TemperatureScaleFactor: [0 0 0] %/ }\mp@subsup{}{}{\circ}\textrm{C
            AccelerationBias: [0 0 0] (rad/s)/(m/s2)
```

Sensor properties are defined by corresponding parameter objects. For example, the gyroscope model used by the imuSensor is defined by an instance of the gyroparams class. You can modify properties of the gyroscope model using dot notation. Set the gyroscope measurement range to 4.3 rad/s.

IMU.Gyroscope.MeasurementRange = 4.3;
You can also set sensor properties to preset parameter objects. Create an accelparams object to mimic specific hardware, and then set the IMU Accelerometer property to the accelparams object. Display the Accelerometer property to verify the properties are correctly set.

```
SpecSheet1 = accelparams( ...
    'MeasurementRange',19.62, ...
    'Resolution',0.00059875, ...
    'ConstantBias',0.4905, ...
    'AxesMisalignment',2, ...
```

```
'NoiseDensity',0.003924, ...
'BiasInstability',0, ...
'TemperatureBias', [0.34335 0.34335 0.5886], ...
'TemperatureScaleFactor', 0.02);
```

```
IMU.Accelerometer = SpecSheet1;
IMU.Accelerometer
ans =
    accelparams with properties:
        MeasurementRange: 19.62 m/s
                Resolution: 0.00059875
            ConstantBias: [0.4905 0.4905 0.4905]
    AxesMisalignment: [3x3 double]
                                (m/s2)/LSB
    m/s}\mp@subsup{}{}{2
    %
        NoiseDensity: [0.003924 0.003924 0.003924] (m/s2)/\sqrt{}{Hz}
    BiasInstability: [0 0 0] m/s2
            RandomWalk: [0 0 0] [ (m/s}\mp@subsup{)}{}{2})*/\textrm{Hz
            TemperatureBias: [0.34335 0.34335 0.5886] (m/s2)/ }\mp@subsup{}{}{\circ}\textrm{C
    TemperatureScaleFactor: [0.02 0.02 0.02] %/}\textrm{C
```


## Generate IMU Data from Stationary Input

Use the imuSensor System object ${ }^{\text {TM }}$ to model receiving data from a stationary ideal IMU containing an accelerometer, gyroscope, and magnetometer.

Create an ideal IMU sensor model that contains an accelerometer, gyroscope, and magnetometer.

```
IMU = imuSensor('accel-gyro-mag')
IMU =
    imuSensor with properties:
            IMUType: 'accel-gyro-mag'
        SampleRate: 100
        Temperature: 25
        MagneticField: [27.5550 -2.4169 -16.0849]
        Accelerometer: [1x1 accelparams]
            Gyroscope: [1x1 gyroparams]
        Magnetometer: [1x1 magparams]
        RandomStream: 'Global stream'
```

Define the ground-truth, underlying motion of the IMU you are modeling. The acceleration and angular velocity are defined relative to the local NED coordinate system.

```
numSamples = 1000;
acceleration = zeros(numSamples,3);
angularVelocity = zeros(numSamples,3);
```

Call IMU with the ground-truth acceleration and angular velocity. The object outputs accelerometer readings, gyroscope readings, and magnetometer readings, as modeled by the properties of the
imuSensor System object. The accelerometer readings, gyroscope readings, and magnetometer readings are relative to the IMU sensor body coordinate system.
[accelReading,gyroReading,magReading] = IMU(acceleration, angularVelocity);
Plot the accelerometer readings, gyroscope readings, and magnetometer readings.

```
t = (0:(numSamples-1))/IMU.SampleRate;
subplot(3,1,1)
plot(t,accelReading)
legend('X-axis','Y-axis','Z-axis')
title('Accelerometer Readings')
ylabel('Acceleration (m/s^2)')
subplot(3,1,2)
plot(t,gyroReading)
legend('X-axis','Y-axis','Z-axis')
title('Gyroscope Readings')
ylabel('Angular Velocity (rad/s)')
subplot(3,1,3)
plot(t,magReading)
legend('X-axis','Y-axis','Z-axis')
title('Magnetometer Readings')
xlabel('Time (s)')
ylabel('Magnetic Field (uT)')
```



Orientation is not specified and the ground-truth motion is stationary, so the IMU sensor body coordinate system and the local NED coordinate system overlap for the entire simulation.

- Accelerometer readings: The $z$-axis of the sensor body corresponds to the Down-axis. The 9.8 $\mathrm{m} / \mathrm{s}^{\wedge} 2$ acceleration along the $z$-axis is due to gravity.
- Gyroscope readings: The gyroscope readings are zero along each axis, as expected.
- Magnetometer readings: Because the sensor body coordinate system is aligned with the local NED coordinate system, the magnetometer readings correspond to the MagneticField property of imuSensor. The MagneticField property is defined in the local NED coordinate system.


## Model Rotating Six-Axis IMU Data

Use imuSensor to model data obtained from a rotating IMU containing an ideal accelerometer and an ideal magnetometer. Use kinematicTrajectory to define the ground-truth motion. Fuse the imuSensor model output using the ecompass function to determine orientation over time.

Define the ground-truth motion for a platform that rotates 360 degrees in four seconds, and then another 360 degrees in two seconds. Use kinematicTrajectory to output the orientation, acceleration, and angular velocity in the NED coordinate system.

```
fs = 100;
firstLoopNumSamples = fs*4;
secondLoopNumSamples = fs*2;
totalNumSamples = firstLoopNumSamples + secondLoopNumSamples;
traj = kinematicTrajectory('SampleRate',fs);
accBody = zeros(totalNumSamples,3);
angVelBody = zeros(totalNumSamples,3);
angVelBody(1:firstLoopNumSamples,3) = (2*pi)/4;
angVelBody(firstLoopNumSamples+1:end,3) = (2*pi)/2;
[~,orientationNED,~,accNED,angVelNED] = traj(accBody,angVelBody);
```

Create an imuSensor object with an ideal accelerometer and an ideal magnetometer. Call IMU with the ground-truth acceleration, angular velocity, and orientation to output accelerometer readings and magnetometer readings. Plot the results.

```
IMU = imuSensor('accel-mag','SampleRate',fs);
[accelReadings,magReadings] = IMU(accNED,angVelNED,orientationNED);
figure(1)
t = (0:(totalNumSamples-1))/fs;
subplot(2,1,1)
plot(t,accelReadings)
legend('X-axis','Y-axis','Z-axis')
ylabel('Acceleration (m/s^2)')
title('Accelerometer Readings')
subplot(2,1,2)
plot(t,magReadings)
legend('X-axis','Y-axis','Z-axis')
```

```
ylabel('Magnetic Field (\muT)')
xlabel('Time (s)')
title('Magnetometer Readings')
```



The accelerometer readings indicate that the platform has no translation. The magnetometer readings indicate that the platform is rotating around the $z$-axis.

Feed the accelerometer and magnetometer readings into the ecompass function to estimate the orientation over time. The ecompass function returns orientation in quaternion format. Convert orientation to Euler angles and plot the results. The orientation plot indicates that the platform rotates about the $z$-axis only.

```
orientation = ecompass(accelReadings,magReadings);
orientationEuler = eulerd(orientation,'ZYX','frame');
figure(2)
plot(t,orientationEuler)
legend('Z-axis','Y-axis','X-axis')
xlabel('Time (s)')
ylabel('Rotation (degrees)')
title('Orientation')
```


## Orientation



## Model Rotating Six-Axis IMU Data with Noise

Use imuSensor to model data obtained from a rotating IMU containing a realistic accelerometer and a realistic magnetometer. Use kinematicTrajectory to define the ground-truth motion. Fuse the imuSensor model output using the ecompass function to determine orientation over time.

Define the ground-truth motion for a platform that rotates 360 degrees in four seconds, and then another 360 degrees in two seconds. Use kinematicTrajectory to output the orientation, acceleration, and angular velocity in the NED coordinate system.

```
fs = 100;
firstLoopNumSamples = fs*4;
secondLoopNumSamples = fs*2;
totalNumSamples = firstLoopNumSamples + secondLoopNumSamples;
traj = kinematicTrajectory('SampleRate',fs);
accBody = zeros(totalNumSamples,3);
angVelBody = zeros(totalNumSamples,3);
angVelBody(1:firstLoopNumSamples,3) = (2*pi)/4;
angVelBody(firstLoopNumSamples+1:end,3) = (2*pi)/2;
[~,orientationNED,~,accNED,angVelNED] = traj(accBody,angVelBody);
```

Create an imuSensor object with a realistic accelerometer and a realistic magnetometer. Call IMU with the ground-truth acceleration, angular velocity, and orientation to output accelerometer readings and magnetometer readings. Plot the results.

```
IMU = imuSensor('accel-mag','SampleRate',fs);
IMU.Accelerometer = accelparams( ...
    'MeasurementRange',19.62, ... %m/s^2
    'Resolution',0.0023936, ... % m/s^2 / LSB
    'TemperatureScaleFactor',0.008, ... %%/ degree C
    'ConstantBias',0.1962, ... %m/s^2
    'TemperatureBias',0.0014715, ... %m/s^2 / degree C
    'NoiseDensity',0.0012361); % m/s^2 / Hz^(1/2)
IMU.Magnetometer = magparams( ...
    'MeasurementRange',1200, ... % uT
    'Resolution',0.1, ... %uT / LSB
    'TemperatureScaleFactor',0.1, ... %%/ degree C
    'ConstantBias',1, ... %uT
    'TemperatureBias',[0.8 0.8 2.4], ... %uT / degree C
    'NoiseDensity',[0.6 0.6 0.9]/sqrt(100)); % uT / Hz^(1/2)
[accelReadings,magReadings] = IMU(accNED,angVelNED,orientationNED);
figure(1)
t = (0:(totalNumSamples-1))/fs;
subplot(2,1,1)
plot(t,accelReadings)
legend('X-axis','Y-axis','Z-axis')
ylabel('Acceleration (m/s^2)')
title('Accelerometer Readings')
subplot(2,1,2)
plot(t,magReadings)
legend('X-axis','Y-axis','Z-axis')
ylabel('Magnetic Field (\muT)')
xlabel('Time (s)')
title('Magnetometer Readings')
```



The accelerometer readings indicate that the platform has no translation. The magnetometer readings indicate that the platform is rotating around the $z$-axis.

Feed the accelerometer and magnetometer readings into the ecompass function to estimate the orientation over time. The ecompass function returns orientation in quaternion format. Convert orientation to Euler angles and plot the results. The orientation plot indicates that the platform rotates about the $z$-axis only.

```
orientation = ecompass(accelReadings,magReadings);
orientationEuler = eulerd(orientation,'ZYX','frame');
figure(2)
plot(t,orientationEuler)
legend('Z-axis','Y-axis','X-axis')
xlabel('Time (s)')
ylabel('Rotation (degrees)')
title('Orientation')
```


## Orientation


$\%$

## Model Tilt Using Gyroscope and Accelerometer Readings

Model a tilting IMU that contains an accelerometer and gyroscope using the imuSensor System object $^{\text {Tm }}$. Use ideal and realistic models to compare the results of orientation tracking using the imufilter System object.

Load a struct describing ground-truth motion and a sample rate. The motion struct describes sequential rotations:

1 yaw: 120 degrees over two seconds
2 pitch: 60 degrees over one second
3 roll: 30 degrees over one-half second
4 roll: -30 degrees over one-half second
5 pitch: -60 degrees over one second
6 yaw: -120 degrees over two seconds
In the last stage, the motion struct combines the 1st, 2nd, and 3rd rotations into a single-axis rotation. The acceleration, angular velocity, and orientation are defined in the local NED coordinate system.

```
load y120p60r30.mat motion fs
accNED = motion.Acceleration;
angVelNED = motion.AngularVelocity;
orientationNED = motion.Orientation;
numSamples = size(motion.Orientation,1);
t = (0:(numSamples-1)).'/fs;
```

Create an ideal IMU sensor object and a default IMU filter object.

```
IMU = imuSensor('accel-gyro','SampleRate',fs);
aFilter = imufilter('SampleRate',fs);
```

In a loop:
1 Simulate IMU output by feeding the ground-truth motion to the IMU sensor object.
2 Filter the IMU output using the default IMU filter object.

```
orientation = zeros(numSamples,1,'quaternion');
for i = 1:numSamples
    [accelBody,gyroBody] = IMU(accNED(i,:),angVelNED(i,:),orientationNED(i,:));
    orientation(i) = aFilter(accelBody,gyroBody);
end
release(aFilter)
```

Plot the orientation over time.

```
figure(1)
plot(t,eulerd(orientation,'ZYX','frame'))
xlabel('Time (s)')
ylabel('Rotation (degrees)')
title('Orientation Estimation -- Ideal IMU Data, Default IMU Filter')
legend('Z-axis','Y-axis','X-axis')
```



Modify properties of your imuSensor to model real-world sensors. Run the loop again and plot the orientation estimate over time.

IMU.Accelerometer = accelparams( ...
'MeasurementRange',19.62, ...
'Resolution',0.00059875, ...
'ConstantBias',0.4905, ...
'AxesMisalignment',2, ...
'NoiseDensity',0.003924, ...
'BiasInstability',0, ...
'TemperatureBias', [0.34335 0.34335 0.5886], ...
'TemperatureScaleFactor', 0.02);
IMU.Gyroscope $=$ gyroparams(.. .
'MeasurementRange',4.3633, ...
'Resolution',0.00013323, ...
'AxesMisalignment',2, ...
'NoiseDensity',8.7266e-05, ...
'TemperatureBias',0.34907, ...
'TemperatureScaleFactor',0.02, ...
'AccelerationBias',0.00017809, ...
'ConstantBias',[0.3491,0.5,0]);
orientationDefault = zeros(numSamples,1,'quaternion');
for $\mathrm{i}=1$ :numSamples
[accelBody,gyroBody] = IMU(accNED(i,:),angVelNED(i,:),orientationNED(i,:));

```
    orientationDefault(i) = aFilter(accelBody,gyroBody);
end
release(aFilter)
figure(2)
plot(t,eulerd(orientationDefault,'ZYX','frame'))
xlabel('Time (s)')
ylabel('Rotation (degrees)')
title('Orientation Estimation -- Realistic IMU Data, Default IMU Filter')
legend('Z-axis','Y-axis','X-axis')
```



The ability of the imufilter to track the ground-truth data is significantly reduced when modeling a realistic IMU. To improve performance, modify properties of your imufilter object. These values were determined empirically. Run the loop again and plot the orientation estimate over time.

```
aFilter.GyroscopeNoise = 7.6154e-7;
aFilter.AccelerometerNoise = 0.0015398;
aFilter.GyroscopeDriftNoise = 3.0462e-12;
aFilter.LinearAccelerationNoise = 0.00096236;
aFilter.InitialProcessNoise = aFilter.InitialProcessNoise*10;
orientationNondefault = zeros(numSamples,1,'quaternion');
for i = 1:numSamples
    [accelBody,gyroBody] = IMU(accNED(i,:),angVelNED(i,:),orientationNED(i,:));
    orientationNondefault(i) = aFilter(accelBody,gyroBody);
```

```
end
release(aFilter)
figure(3)
plot(t,eulerd(orientationNondefault,'ZYX','frame'))
xlabel('Time (s)')
ylabel('Rotation (degrees)')
title('Orientation Estimation -- Realistic IMU Data, Nondefault IMU Filter')
legend('Z-axis','Y-axis','X-axis')
```



To quantify the improved performance of the modified imufilter, plot the quaternion distance between the ground-truth motion and the orientation as returned by the imufilter with default and nondefault properties.

```
qDistDefault = rad2deg(dist(orientationNED,orientationDefault));
qDistNondefault = rad2deg(dist(orientationNED,orientationNondefault));
figure(4)
plot(t,[qDistDefault,qDistNondefault])
title('Quaternion Distance from True Orientation')
legend('Realistic IMU Data, Default IMU Filter', ...
    'Realistic IMU Data, Nondefault IMU Filter')
xlabel('Time (s)')
ylabel('Quaternion Distance (degrees)')
```



## Algorithms

## Accelerometer

The following algorithm description assumes an NED navigation frame. The accelerometer model uses the ground-truth orientation and acceleration inputs and the imuSensor and accelparams properties to model accelerometer readings.


## Obtain Total Acceleration

To obtain the total acceleration (totalAcc), the acceleration is preprocessed by negating and adding the gravity constant vector ( $g=[0 ; 0 ; 9.8] \mathrm{m} / \mathrm{s}^{2}$ assuming an NED frame) as:

$$
\text { totalAcc }=- \text { acceleration }+g
$$

The acceleration term is negated to obtain zero total acceleration readings when the accelerometer is in a free fall. The acceleration term is also known as the specific force.

## Convert to Sensor Frame

Then the total acceleration is converted from the local navigation frame to the sensor frame using:

$$
a=(\text { orientation })(\text { totalAcc })^{T}
$$

If the orientation is input in quaternion form, it is converted to a rotation matrix before processing.

## Bulk Model

The ground-truth acceleration in the sensor frame, $a$, passes through the bulk model, which adds axes misalignment and bias:

$$
b=\left(\left[\begin{array}{ccc}
1 & \frac{\alpha_{2}}{100} & \frac{\alpha_{3}}{100} \\
\frac{\alpha_{1}}{100} & 1 & \frac{\alpha_{3}}{100} \\
\frac{\alpha_{1}}{100} & \frac{\alpha_{2}}{100} & 1
\end{array}\right]\left(a^{T}\right)\right)^{T}+\text { ConstantBias }
$$

where ConstantBias is a property of accelparams, and $\alpha_{1}, \alpha_{2}$, and $\alpha_{3}$ are given by the first, second, and third elements of the AxesMisalignment property of accelparams.

## Bias Instability Drift

The bias instability drift is modeled as white noise biased and then filtered:

$$
\beta_{1}=h_{1} *(w)(\text { BiasInstability })
$$

where BiasInstability is a property of accelparams, and $h_{1}$ is a filter defined by the SampleRate property:

$$
H_{1}(z)=\frac{1}{1-\frac{1}{2} z^{-1}}
$$

## White Noise Drift

White noise drift is modeled by multiplying elements of the white noise random stream by the standard deviation:

$$
\beta_{2}=(w)\left(\sqrt{\frac{\text { SampleRate }}{2}}\right)(\text { NoiseDensity })
$$

where SampleRate is an imuSensor property, and NoiseDensity is an accelparams property. Elements of $w$ are random numbers given by settings of the imuSensor random stream.

## Random Walk Drift

The random walk drift is modeled by biasing elements of the white noise random stream and then filtering:

$$
\beta_{3}=h_{2} *(w)\left(\frac{\text { RandomWalk }}{\sqrt{\frac{\text { SampleRate }}{2}}}\right)
$$

where RandomWalk is a property of accelparams, SampleRate is a property of imuSensor, and $h_{2}$ is a filter defined as:

$$
H_{2}(z)=\frac{1}{1-z^{-1}}
$$

## Environmental Drift Noise

The environmental drift noise is modeled by multiplying the temperature difference from a standard with the temperature bias:

$$
\Delta_{e}=(\text { Temperature }-25)(\text { TemperatureBias })
$$

where Temperature is a property of imuSensor, and TemperatureBias is a property of accelparams. The constant 25 corresponds to a standard temperature.

## Scale Factor Error Model

The temperature scale factor error is modeled as:

$$
\text { scaleFactorError }=1+\left(\frac{\text { Temperature }-25}{100}\right) \text { (TemperatureScaleFactor) }
$$

where Temperature is a property of imuSensor, and TemperatureScaleFactor is a property of accelparams. The constant 25 corresponds to a standard temperature.

## Quantization Model

The quantization is modeled by first saturating the continuous signal model:

$$
e=\left\{\begin{array}{cc}
\text { MeasurementRange } & \text { if } \\
- \text { MeasurementRange } & \text { if }-d>\text { MeasurementRange } \\
d & \text { else }
\end{array}\right.
$$

and then setting the resolution:

$$
\text { accelReadings }=(\text { Resolution })\left(\operatorname{round}\left(\frac{e}{\text { Resolution }}\right)\right)
$$

where MeasurementRange is a property of accelparams.

## Gyroscope

The following algorithm description assumes an NED navigation frame. The gyroscope model uses the ground-truth orientation, acceleration, and angular velocity inputs, and the imuSensor and gyroparams properties to model accelerometer readings.


## Convert to Sensor Frame

The ground-truth angular velocity is converted from the local frame to the sensor frame using the ground-truth orientation:

$$
a=(\text { orientation })(\text { angularVelocity })^{T}
$$

If the orientation is input in quaternion form, it is converted to a rotation matrix before processing.

## Bulk Model

The ground-truth angular velocity in the sensor frame, $a$, passes through the bulk model, which adds axes misalignment and bias:

$$
b=\left(\left[\begin{array}{ccc}
1 & \frac{\alpha_{2}}{100} & \frac{\alpha_{3}}{100} \\
\frac{\alpha_{1}}{100} & 1 & \frac{\alpha_{3}}{100} \\
\frac{\alpha_{1}}{100} & \frac{\alpha_{2}}{100} & 1
\end{array}\right]\left(a^{T}\right)\right)^{T}+\text { ConstantBias }
$$

where ConstantBias is a property of gyroparams, and $\alpha_{1}, \alpha_{2}$, and $\alpha_{3}$ are given by the first, second, and third elements of the AxesMisalignment property of gyroparams.

## Bias Instability Drift

The bias instability drift is modeled as white noise biased and then filtered:

$$
\beta_{1}=h_{1} *(w)(\text { BiasInstability })
$$

where BiasInstability is a property of gyroparams and $h_{1}$ is a filter defined by the SampleRate property:

$$
H_{1}(z)=\frac{1}{1-\frac{1}{2} z^{-1}}
$$

## White Noise Drift

White noise drift is modeled by multiplying elements of the white noise random stream by the standard deviation:

$$
\beta_{2}=(w)\left(\sqrt{\frac{\text { SampleRate }}{2}}\right)(\text { NoiseDensity })
$$

where SampleRate is an imuSensor property, and NoiseDensity is an gyroparams property. The elements of $w$ are random numbers given by settings of the imuSensor random stream.

## Random Walk Drift

The random walk drift is modeled by biasing elements of the white noise random stream and then filtering:

$$
\beta_{3}=h_{2} *(w)\left(\frac{\text { RandomWalk }}{\sqrt{\frac{\text { SampleRate }}{2}}}\right)
$$

where RandomWalk is a property of gyroparams, SampleRate is a property of imuSensor, and $h_{2}$ is a filter defined as:

$$
H_{2}(z)=\frac{1}{1-z^{-1}}
$$

## Environmental Drift Noise

The environmental drift noise is modeled by multiplying the temperature difference from a standard with the temperature bias:

$$
\Delta_{e}=\text { (Temperature - 25)(TemperatureBias) }
$$

where Temperature is a property of imuSensor, and TemperatureBias is a property of gyroparams. The constant 25 corresponds to a standard temperature.

## Scale Factor Error Model

The temperature scale factor error is modeled as:

$$
\text { scaleFactorError }=1+\left(\frac{\text { Temperature-25 }}{100}\right) \text { (TemperatureScaleFactor) }
$$

where Temperature is a property of imuSensor, and TemperatureScaleFactor is a property of gyroparams. The constant 25 corresponds to a standard temperature.

## Quantization Model

The quantization is modeled by first saturating the continuous signal model:

$$
e=\left\{\begin{array}{cc}
\text { MeasurementRange if } \\
- \text { MeasurementRange if } \\
d>\text { MeasurementRange } \\
d & \text { else }
\end{array}\right.
$$

and then setting the resolution:

$$
\text { gyroReadings }=(\text { Resolution })\left(\text { round }\left(\frac{e}{\text { Resolution }}\right)\right)
$$

where MeasurementRange is a property of gyroparams.

## Magnetometer

The following algorithm description assumes an NED navigation frame. The magnetometer model uses the ground-truth orientation and acceleration inputs, and the imuSensor and magparams properties to model magnetometer readings.


## Convert to Sensor Frame

The ground-truth acceleration is converted from the local frame to the sensor frame using the ground-truth orientation:

$$
a=(\text { orientation })(\text { totalAcc })^{T}
$$

If the orientation is input in quaternion form, it is converted to a rotation matrix before processing.

## Bulk Model

The ground-truth acceleration in the sensor frame, $a$, passes through the bulk model, which adds axes misalignment and bias:

$$
b=\left(\left[\begin{array}{ccc}
1 & \frac{\alpha_{2}}{100} & \frac{\alpha_{3}}{100} \\
\frac{\alpha_{1}}{100} & 1 & \frac{\alpha_{3}}{100} \\
\frac{\alpha_{1}}{100} & \frac{\alpha_{2}}{100} & 1
\end{array}\right]\left(a^{T}\right)\right)^{T}+\text { ConstantBias }
$$

where ConstantBias is a property of magparams, and $\alpha_{1}, \alpha_{2}$, and $\alpha_{3}$ are given by the first, second, and third elements of the AxesMisalignment property of magparams.

## Bias Instability Drift

The bias instability drift is modeled as white noise biased and then filtered:

$$
\beta_{1}=h_{1} *(w)(\text { BiasInstability })
$$

where BiasInstability is a property of magparams and $h_{1}$ is a filter defined by the SampleRate property:

$$
H_{1}(z)=\frac{1}{1-\frac{1}{2} z^{-1}}
$$

## White Noise Drift

White noise drift is modeled by multiplying elements of the white noise random stream by the standard deviation:

$$
\beta_{2}=(w)\left(\sqrt{\frac{\text { SampleRate }}{2}}\right) \text { (NoiseDensity) }
$$

where SampleRate is an imuSensor property, and NoiseDensity is an magparams property. The elements of $w$ are random numbers given by settings of the imuSensor random stream.

## Random Walk Drift

The random walk drift is modeled by biasing elements of the white noise random stream and then filtering:

$$
\beta_{3}=h_{2} *(w)\left(\frac{\text { RandomWalk }}{\sqrt{\frac{\text { SampleRate }}{2}}}\right)
$$

where RandomWalk is a property of magparams, SampleRate is a property of imuSensor, and $h_{2}$ is a filter defined as:

$$
H_{2}(z)=\frac{1}{1-z^{-1}}
$$

## Environmental Drift Noise

The environmental drift noise is modeled by multiplying the temperature difference from a standard with the temperature bias:

$$
\Delta_{e}=\text { (Temperature - 25)(TemperatureBias) }
$$

where Temperature is a property of imuSensor, and TemperatureBias is a property of magparams. The constant 25 corresponds to a standard temperature.

## Scale Factor Error Model

The temperature scale factor error is modeled as:

$$
\text { scaleFactorError }=1+\left(\frac{\text { Temperature }-25}{100}\right) \text { (TemperatureScaleFactor) }
$$

where Temperature is a property of imuSensor, and TemperatureScaleFactor is a property of magparams. The constant 25 corresponds to a standard temperature.
Quantization Model
The quantization is modeled by first saturating the continuous signal model:

$$
e=\left\{\begin{array}{cc}
\text { MeasurementRange } & \text { if } d>\text { MeasurementRange } \\
- \text { MeasurementRange } & \text { if }-d>\text { MeasurementRange } \\
d & \text { else }
\end{array}\right.
$$

and then setting the resolution:

$$
\text { magReadings }=(\text { Resolution })\left(\text { round }\left(\frac{e}{\text { Resolution }}\right)\right)
$$

where MeasurementRange is a property of magparams.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
The object functions, perturbations and perturb, do not support code generation.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

```
Classes
accelparams|gyroparams|magparams
Objects
gpsSensor
```

Introduced in R2019b

## insSensor

Inertial navigation system and GNSS/GPS simulation model

## Description

The insSensor System object models a device that fuses measurements from an inertial navigation system (INS) and global navigation satellite system (GNSS) such as a GPS, and outputs the fused measurements.

To output fused INS and GNSS measurements:
1 Create the insSensor object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

INS = insSensor
INS $=$ insSensor(Name, Value)

## Description

INS = insSensor returns a System object, INS, that models a device that outputs measurements from an INS and GNSS.

INS = insSensor(Name, Value) sets properties on page 2-487 using one or more name-value pairs. Unspecified properties have default values. Enclose each property name in quotes.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## MountingLocation - Location of sensor on platform (m)

$\left[\begin{array}{lll}0 & 0 & 0\end{array}\right]$ (default)| three-element real-valued vector of form $[x y z]$
Location of the sensor on the platform, in meters, specified as a three-element real-valued vector of the form $[x y z]$. The vector defines the offset of the sensor origin from the origin of the platform.

Tunable: Yes

## Data Types: single |double

## RollAccuracy - Accuracy of roll measurement (deg)

0.2 (default) | nonnegative real scalar

Accuracy of the roll measurement of the sensor body, in degrees, specified as a nonnegative real scalar.

Roll is the rotation around the $x$-axis of the sensor body. Roll noise is modeled as a white noise process. RollAccuracy sets the standard deviation of the roll measurement noise.

Tunable: Yes
Data Types: single | double

## PitchAccuracy - Accuracy of pitch measurement (deg)

0.2 (default) | nonnegative real scalar

Accuracy of the pitch measurement of the sensor body, in degrees, specified as a nonnegative real scalar.

Pitch is the rotation around the $y$-axis of the sensor body. Pitch noise is modeled as a white noise process. PitchAccuracy defines the standard deviation of the pitch measurement noise.

Tunable: Yes
Data Types: single | double
YawAccuracy - Accuracy of yaw measurement (deg)
1 (default) | nonnegative real scalar
Accuracy of the yaw measurement of the sensor body, in degrees, specified as a nonnegative real scalar.

Yaw is the rotation around the $z$-axis of the sensor body. Yaw noise is modeled as a white noise process. YawAccuracy defines the standard deviation of the yaw measurement noise.

Tunable: Yes
Data Types: single | double

## PositionAccuracy - Accuracy of position measurement (m)

[1 $\left.\begin{array}{lll}1 & 1 & 1\end{array}\right]$ (default) | nonnegative real scalar | three-element real-valued vector
Accuracy of the position measurement of the sensor body, in meters, specified as a nonnegative real scalar or a three-element real-valued vector. The elements of the vector set the accuracy of the $x-, y$-, and $z$-position measurements, respectively. If you specify PositionAccuracy as a scalar value, then the object sets the accuracy of all three positions to this value.

Position noise is modeled as a white noise process. PositionAccuracy defines the standard deviation of the position measurement noise.

Tunable: Yes
Data Types: single | double
VelocityAccuracy - Accuracy of velocity measurement (m/s)
0.05 (default) | nonnegative real scalar

Accuracy of the velocity measurement of the sensor body, in meters per second, specified as a nonnegative real scalar.

Velocity noise is modeled as a white noise process. VelocityAccuracy defines the standard deviation of the velocity measurement noise.

Tunable: Yes
Data Types: single|double

## AccelerationAccuracy - Accuracy of acceleration measurement (m/s²)

0 (default) | nonnegative real scalar
Accuracy of the acceleration measurement of the sensor body, in meters per second, specified as a nonnegative real scalar.

Acceleration noise is modeled as a white noise process. AccelerationAccuracy defines the standard deviation of the acceleration measurement noise.

Tunable: Yes
Data Types: single | double

## AngularVelocityAccuracy - Accuracy of angular velocity measurement (deg/s)

0 (default) | nonnegative real scalar
Accuracy of the angular velocity measurement of the sensor body, in meters per second, specified as a nonnegative real scalar.

Angular velocity is modeled as a white noise process. AngularVelocityAccuracy defines the standard deviation of the acceleration measurement noise.

Tunable: Yes
Data Types: single | double
TimeInput - Enable input of simulation time
false or 0 (default) | true or 1
Enable input of simulation time, specified as a logical 0 (false) or 1 (true). Set this property to true to input the simulation time by using the simTime argument.

Tunable: No
Data Types: logical

## HasGNSSFix - Enable GNSS fix

true or 1 (default) | false or 0
Enable GNSS fix, specified as a logical 1 (true) or 0 (false). Set this property to false to simulate the loss of a GNSS receiver fix. When a GNSS receiver fix is lost, position measurements drift at a rate specified by the PositionErrorFactor property.

Tunable: Yes
Dependencies
To enable this property, set TimeInput to true.

Data Types: logical

## PositionErrorFactor - Position error factor without GNSS fix

[0 0 0 0 (default) | nonnegative scalar | 1-by-3 vector of scalars
Position error factor without GNSS fix, specified as a scalar or a 1-by-3 vector of scalars.
When the HasGNSSFix property is set to false, the position error grows at a quadratic rate due to constant bias in the accelerometer. The position error for a position component $E(t)$ can be expressed as $E(t)=1 / 2 \alpha t^{2}$, where $\alpha$ is the position error factor for the corresponding component and $t$ is the time since the GNSS fix is lost. While running, the object computes $t$ based on the simTime input. The computed $E(t)$ values for the $x, y$, and $z$ components are added to the corresponding position components of the gTruth input.

Tunable: Yes

## Dependencies

To enable this property, set TimeInput to true and HasGNSSFix to false.

## Data Types: single | double

## RandomStream - Random number source

'Global stream' (default)|'mt19937ar with seed'
Random number source, specified as one of these options:

- 'Global stream' -- Generate random numbers using the current global random number stream.
- 'mt19937ar with seed ' -- Generate random numbers using the mt19937ar algorithm, with the seed specified by the Seed property.

Data Types: char | string

## Seed - Initial seed

67 (default) | nonnegative integer
Initial seed of the mt19937ar random number generator algorithm, specified as a nonnegative integer.

## Dependencies

To enable this property, set RandomStream to 'mt19937ar with seed'.
Data Types: single | double | int8 | int16|int32 | int64 | uint8|uint16|uint32|uint64

## Usage

## Syntax

```
measurement = INS(gTruth)
measurement = INS(gTruth,simTime)
```


## Description

measurement $=$ INS(gTruth) models the data received from an INS sensor reading and GNSS sensor reading. The output measurement is based on the inertial ground-truth state of the sensor body, gTruth.
measurement $=$ INS( $g$ Truth, simTime) additionally specifies the time of simulation, simTime. To enable this syntax, set the TimeInput property to true.

## Input Arguments

## gTruth - Inertial ground-truth state of sensor body

structure
Inertial ground-truth state of sensor body, in local Cartesian coordinates, specified as a structure containing these fields:

| Field | Description |
| :--- | :--- |
| 'Position' | Position, in meters, specified as a real, finite $N$ - <br> by-3 matrix of $[x \quad y z]$ vectors. $N$ is the number of <br> samples in the current frame. |
| 'Velocity' | Velocity $(v)$, in meters per second, specified as a <br> real, finite $N$-by-3 matrix of $\left[v_{\mathrm{x}} v_{\mathrm{y}} v_{z}\right]$ vector. $N$ is <br> the number of samples in the current frame. |
| 'Orientation' | Orientation with respect to the local Cartesian <br> coordinate system, specified as one of these <br> options: |
| -$N$-element column vector of quaternion <br> objects |  |
| - 3 -by-3-by- $N$ array of rotation matrices |  |
| -$N$-by-3 matrix of $\left[x_{\text {roll }} y_{\text {pitch }} z_{\text {yaw }}\right]$ angles in <br> degrees |  |
| Each quaternion or rotation matrix is a frame |  |
| rotation from the local Cartesian coordinate |  |
| system to the current sensor body coordinate |  |
| system. $N$ is the number of samples in the current |  |
| frame. |  |

The field values must be of type double or single.
The Position, Velocity, and Orientation fields are required. The other fields are optional.

Example: struct('Position',[0 0 0],'Velocity',[0 0 0],'Orientation',quaternion([1 0 0 0]))

## simTime - Simulation time

nonnegative real scalar
Simulation time, in seconds, specified as a nonnegative real scalar.
Data Types: single | double

## Output Arguments

## measurement - Measurement of sensor body motion

structure
Measurement of the sensor body motion, in local Cartesian coordinates, returned as a structure containing these fields:

| Field | Description |
| :---: | :---: |
| 'Position' | Position, in meters, specified as a real, finite $N$ -by-3 matrix of $[x y z]$ vectors. $N$ is the number of samples in the current frame. |
| 'Velocity' | Velocity ( $v$ ), in meters per second, specified as a real, finite $N$-by-3 matrix of $\left[v_{\mathrm{x}} v_{\mathrm{y}} v_{z}\right]$ vector. $N$ is the number of samples in the current frame. |
| 'Orientation' | Orientation with respect to the local Cartesian coordinate system, specified as one of these options: <br> - $N$-element column vector of quaternion objects <br> - 3-by-3-by- $N$ array of rotation matrices <br> - $N$-by-3 matrix of [ $x_{\text {roll }} y_{\text {pitch }} z_{\text {yaw }}$ ] angles in degrees <br> Each quaternion or rotation matrix is a frame rotation from the local Cartesian coordinate system to the current sensor body coordinate system. $N$ is the number of samples in the current frame. |
| 'Acceleration' | Acceleration (a), in meters per second squared, specified as a real, finite $N$-by- 3 matrix of $\left[a_{\mathrm{x}} a_{\mathrm{y}}\right.$ $\left.a_{z}\right]$ vectors. $N$ is the number of samples in the current frame. |
| 'AngularVelocity' | Angular velocity ( $\omega$ ), in degrees per second squared, specified as a real, finite $N$-by- 3 matrix of $\left[\omega_{\mathrm{x}} \omega_{\mathrm{y}} \omega_{\mathrm{z}}\right.$ ] vectors. $N$ is the number of samples in the current frame. |

The returned field values are of type double or single and are of the same type as the corresponding field values in the gTruth input.

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to insSensor

perturbations Perturbation defined on object
perturb Apply perturbations to object

## Common to All System Objects

step Run System object algorithm
clone Create duplicate System object
isLocked Determine if System object is in use
reset Reset internal states of System object
release Release resources and allow changes to System object property values and input characteristics

## Examples

## Generate INS Measurements from Stationary Input

Create a motion structure that defines a stationary position at the local north-east-down (NED) origin. Because the platform is stationary, you need to define only a single sample. Assume the ground-truth motion is sampled for 10 seconds with a 100 Hz sample rate. Create a default insSensor System object $^{\text {TM }}$. Preallocate variables to hold output from the insSensor object.

```
Fs = 100;
duration = 10;
numSamples = Fs*duration;
motion = struct( ...
    'Position',zeros(1,3), ...
    'Velocity',zeros(1,3), ...
    'Orientation',ones(1,1,'quaternion'));
INS = insSensor;
positionMeasurements = zeros(numSamples,3);
velocityMeasurements = zeros(numSamples,3);
orientationMeasurements = zeros(numSamples,1,'quaternion');
```

In a loop, call INS with the stationary motion structure to return the position, velocity, and orientation measurements in the local NED coordinate system. Log the position, velocity, and orientation measurements.

```
for i = 1:numSamples
    measurements = INS(motion);
    positionMeasurements(i,:) = measurements.Position;
    velocityMeasurements(i,:) = measurements.Velocity;
```

```
    orientationMeasurements(i) = measurements.Orientation;
end
```

Convert the orientation from quaternions to Euler angles for visualization purposes. Plot the position, velocity, and orientation measurements over time.

```
orientationMeasurements = eulerd(orientationMeasurements,'ZYX','frame');
t = (0:(numSamples-1))/Fs;
subplot(3,1,1)
plot(t,positionMeasurements)
title('Position')
xlabel('Time (s)')
ylabel('Position (m)')
legend('North','East','Down')
subplot(3,1,2)
plot(t,velocityMeasurements)
title('Velocity')
xlabel('Time (s)')
ylabel('Velocity (m/s)')
legend('North','East','Down')
subplot(3,1,3)
plot(t,orientationMeasurements)
title('0rientation')
xlabel('Time (s)')
ylabel('Rotation (degrees)')
legend('Roll', 'Pitch', 'Yaw')
```



## Generate INS Measurements for a Turning Platform

Generate INS measurements using the insSensor System object ${ }^{\mathrm{TM}}$. Use waypointTrajectory to generate the ground-truth path.

Specify a ground-truth orientation that begins with the sensor body $x$-axis aligned with North and ends with the sensor body $x$-axis aligned with East. Specify waypoints for an arc trajectory and a time-of-arrival vector for the corresponding waypoints. Use a 100 Hz sample rate. Create a waypointTrajectory System object with the waypoint constraints, and set SamplesPerFrame so that the entire trajectory is output with one call.

```
eulerAngles = [0,0,0; ...
    0,0,0; ...
    90,0,0; ...
    90,0,0];
orientation = quaternion(eulerAngles,'eulerd','ZYX','frame');
r = 20;
waypoints = [0,0,0; ...
    100,0,0; ...
    100+r,r,0; ...
    100+r,100+r,0];
toa = [0,10,10+(2*pi*r/4),20+(2*pi*r/4)];
```

```
Fs = 100;
numSamples = floor(Fs*toa(end));
path = waypointTrajectory('Waypoints',waypoints, ...
    'TimeOfArrival',toa, ...
    'Orientation',orientation, ...
    'SampleRate',Fs, ...
    'SamplesPerFrame',numSamples);
```

Create an insSensor System object to model receiving INS data. Set the PositionAccuracy to 0.1.

```
ins = insSensor('PositionAccuracy',0.1);
```

Call the waypoint trajectory object, path, to generate the ground-truth motion. Call the INS simulator, ins, with the ground-truth motion to generate INS measurements.

```
[motion.Position,motion.Orientation,motion.Velocity] = path();
insMeas = ins(motion);
```

Convert the orientation returned by ins to Euler angles in degrees for visualization purposes. Plot the full path and orientation over time.

```
orientationMeasurementEuler = eulerd(insMeas.Orientation,'ZYX','frame');
subplot(2,1,1)
plot(insMeas.Position(:,1),insMeas.Position(:,2));
title('Path')
xlabel('North (m)')
ylabel('East (m)')
subplot(2,1,2)
t = (0:(numSamples-1)).'/Fs;
plot(t,orientationMeasurementEuler(:,1), ...
    t,orientationMeasurementEuler(:,2), ...
    t,orientationMeasurementEuler(:,3));
title('Orientation')
legend('Yaw','Pitch','Roll')
xlabel('Time (s)')
ylabel('Rotation (degrees)')
```



## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
The object functions, perturbations and perturb, do not support code generation.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

## Objects

imuSensor|gpsSensor

## Objects

## Topics

"Model IMU, GPS, and INS/GPS"
"Simulate Inertial Sensor Readings from a Driving Scenario"
Introduced in R2020b

## loadparams

Load sensor parameters from JSON file

## Syntax

loadparams(sensor,file, PN)

## Description

loadparams(sensor, file, PN) configures the imuSensor object, sensor, to match the parameters in the PN part of a JSON file, File.

## Examples

## Load Pre-defined Parameters in imuSensor

Create an imuSensor system object.
s = imuSensor;
Load a JSON file.

```
fn = fullfile(matlabroot,'toolbox','shared',...
    'positioning','positioningdata','generic.json');
```

Here is a screen shot of the JSON file with some parts collapsed.

```
{
    "GenericLowCost9Axis":
    {
        "Accelerometer":
    {
        "MeasurementRange": 19.6133,
        "Resolution": 0.0023928,
        "ConstantBias": [0.19,0.19,0.19],
        "AxesMisalignment": [0,0,0],
        "NoiseDensity": [0.0012356,0.0012356,0.0012356],
        "BiasInstability": [0,0,0],
        "RandomWalk": [0,0,0],
        "TemperatureBias": [0,0,0],
        "TemperatureScaleFactor": [0,0,0]
    },
    "Gyroscope":
    {#},
    "Magnetometer":
        {#}
    },
    "GenericLowCost6Axis":
    {\Xi}
}
```

Configure the object as a 6 -axis sensor.

```
loadparams(s,fn,'GenericLowCost6Axis')
```

s
s =
imuSensor with properties:
IMUType: 'accel-gyro'
SampleRate: 100
Temperature: 25
Accelerometer: [1x1 accelparams]
Gyroscope: [1×1 gyroparams]
RandomStream: 'Global stream'

Configure the object as a 9 -axis sensor.
loadparams(s,fn, 'GenericLowCost9Axis')
s
s =
imuSensor with properties:
IMUType: 'accel-gyro-mag'
SampleRate: 100
Temperature: 25
MagneticField: [27.5550-2.4169-16.0849]
Accelerometer: [1x1 accelparams]
Gyroscope: [1x1 gyroparams]
Magnetometer: [1x1 magparams]
RandomStream: 'Global stream'

## Input Arguments

## sensor - IMU sensor

imuSensor object
IMU sensor, specified as an imuSensor system object.

## file - JSON file

. json file
JavaScript Object Notation (JSON) format file, specified as a .json file.

```
PN - Part name
string
```

Part name in a JSON file, specified as a string.

## See Also

imuSensor

Introduced in R2020a

## kinematicTrajectory

Rate-driven trajectory generator

## Description

The kinematicTrajectory System object generates trajectories using specified acceleration and angular velocity.

To generate a trajectory from rates:
1 Create the kinematicTrajectory object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

trajectory = kinematicTrajectory
trajectory = kinematicTrajectory (Name, Value)

## Description

trajectory $=$ kinematicTrajectory returns a System object, trajectory, that generates a trajectory based on acceleration and angular velocity.
trajectory = kinematicTrajectory (Name, Value) sets each property Name to the specified Value. Unspecified properties have default values.
Example: trajectory = kinematicTrajectory('SampleRate' , 200, 'Position' , [0, 1, 10]) creates a kinematic trajectory System object, trajectory, with a sample rate of 200 Hz and the initial position set to [0,1,10].

## Properties

If a property is tunable, you can change its value at any time.

## SampleRate - Sample rate of trajectory (Hz)

100 (default) | positive scalar
Sample rate of trajectory in Hz , specified as a positive scalar.
Tunable: Yes
Data Types: single|double

## Position - Position state in local navigation coordinate system (m)

[0 0 0 ] (default)|3-element row vector

Position state in the local navigation coordinate system in meters, specified as a three-element row vector.

Tunable: Yes
Data Types: single | double

## Velocity - Velocity state in local navigation coordinate system (m/s)

[0 0 0] (default) | 3 -element row vector
Velocity state in the local navigation coordinate system in $\mathrm{m} / \mathrm{s}$, specified as a three-element row vector.

Tunable: Yes
Data Types: single | double
Orientation - Orientation state in local navigation coordinate system quaternion ( $1,0,0,0$ ) (default) | scalar quaternion | 3-by-3 real matrix

Orientation state in the local navigation coordinate system, specified as a scalar quaternion or 3-by-3 real matrix. The orientation is a frame rotation from the local navigation coordinate system to the current body frame.

Tunable: Yes
Data Types: quaternion | single | double
AccelerationSource - Source of acceleration state
'Input' (default)|'Property'
Source of acceleration state, specified as 'Input ' or 'Property'.

- 'Input ' -- specify acceleration state as an input argument to the kinematic trajectory object
- 'Property ' -- specify acceleration state by setting the Acceleration property

Tunable: No
Data Types: char|string

## Acceleration - Acceleration state (m/s $\mathbf{s}^{\mathbf{2}}$ )

[0 0 0 ] (default) | three-element row vector
Acceleration state in $\mathrm{m} / \mathrm{s}^{2}$, specified as a three-element row vector.
Tunable: Yes

## Dependencies

To enable this property, set AccelerationSource to 'Property'.

## Data Types: single | double

## AngularVelocitySource - Source of angular velocity state <br> 'Input' (default)|'Property'

Source of angular velocity state, specified as 'Input' or 'Property'.

- 'Input ' -- specify angular velocity state as an input argument to the kinematic trajectory object
- 'Property' -- specify angular velocity state by setting the AngularVelocity property

Tunable: No
Data Types: char|string

## AngularVelocity - Angular velocity state (rad/s)

[0 0 0 ] (default) |three-element row vector
Angular velocity state in rad/s, specified as a three-element row vector.
Tunable: Yes

## Dependencies

To enable this property, set AngularVelocitySource to 'Property'.
Data Types: single|double
SamplesPerFrame - Number of samples per output frame
1 (default) | positive integer
Number of samples per output frame, specified as a positive integer.
Tunable: No

## Dependencies

To enable this property, set AngularVelocitySource to 'Property' and AccelerationSource to
'Property'.
Data Types: single|double

## Usage

## Syntax

```
[position,orientation,velocity,acceleration,angularVelocity] = trajectory(
bodyAcceleration,bodyAngularVelocity)
[position,orientation,velocity,acceleration,angularVelocity] = trajectory(
bodyAngularVelocity)
[position,orientation,velocity,acceleration,angularVelocity] = trajectory(
bodyAcceleration)
[position,orientation,velocity,acceleration,angularVelocity] = trajectory()
```


## Description

[position,orientation, velocity, acceleration, angularVelocity] = trajectory( bodyAcceleration, bodyAngularVelocity) outputs the trajectory state and then updates the trajectory state based on bodyAcceleration and bodyAngularVelocity.

This syntax is only valid if AngularVelocitySource is set to 'Input' and AccelerationSource is set to 'Input'.
[position,orientation, velocity, acceleration,angularVelocity] = trajectory( bodyAngularVelocity) outputs the trajectory state and then updates the trajectory state based on bodyAngularAcceleration.

This syntax is only valid if AngularVelocitySource is set to 'Input ' and AccelerationSource is set to 'Property'.
[position,orientation,velocity,acceleration, angularVelocity] = trajectory( bodyAcceleration) outputs the trajectory state and then updates the trajectory state based on bodyAcceleration.

This syntax is only valid if AngularVelocitySource is set to 'Property' and AccelerationSource is set to 'Input'.
[position,orientation, velocity, acceleration, angularVelocity] = trajectory() outputs the trajectory state and then updates the trajectory state.

This syntax is only valid if AngularVelocitySource is set to 'Property' and AccelerationSource is set to 'Property'.

Input Arguments
bodyAcceleration - Acceleration in body coordinate system (m/s²)
N -by-3 matrix
Acceleration in the body coordinate system in meters per second squared, specified as an $N$-by- 3 matrix.
$N$ is the number of samples in the current frame.

## bodyAngularVelocity - Angular velocity in body coordinate system (rad/s)

N -by-3 matrix
Angular velocity in the body coordinate system in radians per second, specified as an N -by- 3 matrix.
$N$ is the number of samples in the current frame.

## Output Arguments

position - Position in local navigation coordinate system (m)
N -by-3 matrix
Position in the local navigation coordinate system in meters, returned as an $N$-by- 3 matrix.
$N$ is the number of samples in the current frame.
Data Types: single | double
orientation - Orientation in local navigation coordinate system
$N$-element quaternion column vector | 3 -by-3-by- $N$ real array
Orientation in the local navigation coordinate system, returned as an $N$-by-1 quaternion column vector or a 3-by-3-by-N real array. Each quaternion or 3-by-3 rotation matrix is a frame rotation from the local navigation coordinate system to the current body coordinate system.
$N$ is the number of samples in the current frame.

Data Types: single | double

## velocity - Velocity in local navigation coordinate system ( $\mathrm{m} / \mathrm{s}$ )

$N$-by-3 matrix
Velocity in the local navigation coordinate system in meters per second, returned as an $N$-by- 3 matrix.
$N$ is the number of samples in the current frame.
Data Types: single|double
acceleration - Acceleration in local navigation coordinate system (m/s²)
$N$-by-3 matrix
Acceleration in the local navigation coordinate system in meters per second squared, returned as an $N$-by-3 matrix.
$N$ is the number of samples in the current frame.
Data Types: single | double
angularVelocity - Angular velocity in local navigation coordinate system (rad/s)
$N$-by-3 matrix
Angular velocity in the local navigation coordinate system in radians per second, returned as an N -by-3 matrix.
$N$ is the number of samples in the current frame.
Data Types: single | double

## Object Functions

## Specific to kinematicTrajectory

perturbations Perturbation defined on object
perturb Apply perturbations to object

## Common to All System Objects

step Run System object algorithm

## Examples

## Create Default kinematicTrajectory

Create a default kinematicTrajectory System object ${ }^{\text {TM }}$ and explore the relationship between input, properties, and the generated trajectories.

```
trajectory = kinematicTrajectory
trajectory =
    kinematicTrajectory with properties:
                            SampleRate: 100
```

```
            Position: [0 0 0]
            Orientation: [1x1 quaternion]
            Velocity: [0 0 0]
        AccelerationSource: 'Input'
AngularVelocitySource: 'Input'
```

By default, the kinematicTrajectory object has an initial position of [000] and an initial velocity of [0 000 ]. Orientation is described by a quaternion one $(1+0 i+0 j+0 k)$.

The kinematicTrajectory object maintains a visible and writable state in the properties Position, Velocity, and Orientation. When you call the object, the state is output and then updated.

For example, call the object by specifying an acceleration and angular velocity relative to the body coordinate system.

```
bodyAcceleration = [5,5,0];
bodyAngularVelocity = [0,0,1];
[position,orientation,velocity,acceleration,angularVelocity] = trajectory(bodyAcceleration,bodyA
position = 1\times3
    0 0 0
orientation = quaternion
    1 + 0i + 0j + 0k
velocity = 1\times3
    0 0 0
acceleration = 1\times3
    5 5 0
angularVelocity = 1\times3
    0 0 1
```

The position, orientation, and velocity output from the trajectory object correspond to the state reported by the properties before calling the object. The trajectory state is updated after being called and is observable from the properties:

```
trajectory
trajectory =
    kinematicTrajectory with properties:
            SampleRate: 100
                            Position: [2.5000e-04 2.5000e-04 0]
            Orientation: [1x1 quaternion]
            Velocity: [0.0500 0.0500 0]
            AccelerationSource: 'Input'
```

```
AngularVelocitySource: 'Input'
```

The acceleration and angularVelocity output from the trajectory object correspond to the bodyAcceleration and bodyAngularVelocity, except that they are returned in the navigation coordinate system. Use the orientation output to rotate acceleration and angularVelocity to the body coordinate system and verify they are approximately equivalent to bodyAcceleration and bodyAngularVelocity.

```
rotatedAcceleration = rotatepoint(orientation,acceleration)
rotatedAcceleration = 1\times3
    5 5 0
rotatedAngularVelocity = rotatepoint(orientation,angularVelocity)
rotatedAngularVelocity = 1\times3
```

    \(0 \quad 0 \quad 1\)
    The kinematicTrajectory System object ${ }^{\text {TM }}$ enables you to modify the trajectory state through the properties. Set the position to $[0,0,0]$ and then call the object with a specified acceleration and angular velocity in the body coordinate system. For illustrative purposes, clone the trajectory object before modifying the Position property. Call both objects and observe that the positions diverge.

```
trajectoryClone = clone(trajectory);
```

trajectory. Position $=[0,0,0]$;
position = trajectory(bodyAcceleration, bodyAngularVelocity)
position $=1 \times 3$
$0 \quad 0 \quad 0$
clonePosition = trajectoryClone(bodyAcceleration,bodyAngularVelocity)
clonePosition = $1 \times 3$
$10^{-3} \times$
$0.2500 \quad 0.2500 \quad 0$

## Create Oscillating Trajectory

This example shows how to create a trajectory oscillating along the North axis of a local NED coordinate system using the kinematicTrajectory System object ${ }^{\mathrm{TM}}$.

Create a default kinematicTrajectory object. The default initial orientation is aligned with the local NED coordinate system.

```
traj = kinematicTrajectory
```

```
traj =
    kinematicTrajectory with properties:
            SampleRate: 100
                            Position: [0 0 0]
                    Orientation: [1x1 quaternion]
                        Velocity: [0 0 0]
        AccelerationSource: 'Input'
    AngularVelocitySource: 'Input'
```

Define a trajectory for a duration of 10 seconds consisting of rotation around the East axis (pitch) and an oscillation along North axis of the local NED coordinate system. Use the default kinematicTrajectory sample rate.

```
fs = traj.SampleRate;
duration = 10;
numSamples = duration*fs;
cyclesPerSecond = 1;
samplesPerCycle = fs/cyclesPerSecond;
numCycles = ceil(numSamples/samplesPerCycle);
maxAccel = 20;
triangle = [linspace(maxAccel,1/fs-maxAccel,samplesPerCycle/2), ...
    linspace(-maxAccel,maxAccel-(1/fs),samplesPerCycle/2)]';
oscillation = repmat(triangle,numCycles,1);
oscillation = oscillation(1:numSamples);
accNED = [zeros(numSamples,2),oscillation];
angVelNED = zeros(numSamples,3);
angVelNED(:,2) = 2*pi;
```

Plot the acceleration control signal.

```
timeVector = 0:1/fs:(duration-1/fs);
figure(1)
plot(timeVector,oscillation)
xlabel('Time (s)')
ylabel('Acceleration (m/s)^2')
title('Acceleration in Local NED Coordinate System')
```



Generate the trajectory sample-by-sample in a loop. The kinematicTrajectory System object assumes the acceleration and angular velocity inputs are in the local sensor body coordinate system. Rotate the acceleration and angular velocity control signals from the NED coordinate system to the sensor body coordinate system using rotateframe and the Orientation state. Update a 3-D plot of the position at each time. Add pause to mimic real-time processing. Once the loop is complete, plot the position over time. Rotating the accNED and angVelNED control signals to the local body coordinate system assures the motion stays along the Down axis.

```
figure(2)
plotHandle = plot3(traj.Position(1),traj.Position(2),traj.Position(3),'bo');
grid on
xlabel('North')
ylabel('East')
zlabel('Down')
axis([-1 1 -1 1 0 1.5])
hold on
q = ones(numSamples,1,'quaternion');
for ii = 1:numSamples
    accBody = rotateframe(traj.Orientation,accNED(ii,:));
    angVelBody = rotateframe(traj.Orientation,angVelNED(ii,:));
    [pos(ii,:),q(ii),vel,ac] = traj(accBody,angVelBody);
    set(plotHandle,'XData',pos(ii,1),'YData',pos(ii,2),'ZData',pos(ii,3))
    pause(1/fs)
```

end
figure(3)
plot(timeVector,pos(:,1),'bo',...
timeVector, pos(:,2),'r.',...
timeVector, pos(:,3),'g.')
xlabel('Time (s)')
ylabel('Position (m)')
title('NED Position Over Time')
legend('North','East','Down')



Convert the recorded orientation to Euler angles and plot. Although the orientation of the platform changed over time, the acceleration always acted along the North axis.

```
figure(4)
eulerAngles = eulerd(q,'ZYX','frame');
plot(timeVector,eulerAngles(:,1),'bo',...
    timeVector,eulerAngles(:,2),'r.',...
    timeVector,eulerAngles(:,3),'g.')
axis([0,duration,-180,180])
legend('Yaw','Pitch','Roll')
xlabel('Time (s)')
ylabel('Rotation (degrees)')
title('Orientation')
```



## Generate a Coil Trajectory

This example shows how to generate a coil trajectory using the kinematicTrajectory System object ${ }^{\mathrm{TM}}$.

Create a circular trajectory for a 1000 second duration and a sample rate of 10 Hz . Set the radius of the circle to 5000 meters and the speed to 80 meters per second. Set the climb rate to 100 meters per second and the pitch to 15 degrees. Specify the initial orientation as pointed in the direction of motion.

```
duration = 1000; % seconds
fs = 10; % Hz
N = duration*fs; % number of samples
radius = 5000; % meters
speed = 80; % meters per second
climbRate = 50; % meters per second
initialYaw = 90; % degrees
pitch = 15; % degrees
initPos = [radius, 0, 0];
initVel = [0, speed, climbRate];
initOrientation = quaternion([initialYaw,pitch,0],'eulerd','zyx','frame');
trajectory = kinematicTrajectory('SampleRate',fs, ...
```

```
'Velocity',initVel, ...
'Position',initPos, ...
'Orientation',initOrientation);
```

Specify a constant acceleration and angular velocity in the body coordinate system. Rotate the body frame to account for the pitch.

```
accBody = zeros(N,3);
accBody(:,2) = speed^2/radius;
accBody(:,3) = 0.2;
angVelBody = zeros(N,3);
angVelBody(:,3) = speed/radius;
pitchRotation = quaternion([0,pitch,0],'eulerd','zyx','frame');
angVelBody = rotateframe(pitchRotation,angVelBody);
accBody = rotateframe(pitchRotation,accBody);
```

Call trajectory with the specified acceleration and angular velocity in the body coordinate system. Plot the position, orientation, and speed over time.

```
[position, orientation, velocity] = trajectory(accBody,angVelBody);
eulerAngles = eulerd(orientation,'ZYX','frame');
speed = sqrt(sum(velocity.^2,2));
timeVector = (0:(N-1))/fs;
figure(1)
plot3(position(:,1),position(:,2),position(:,3))
xlabel('North (m)')
ylabel('East (m)')
zlabel('Down (m)')
title('Position')
grid on
```


figure(2)
plot(timeVector,eulerAngles(:,1),...
timeVector, eulerAngles(:,2),...
timeVector, eulerAngles(:,3))
axis([0,duration,-180,180])
legend('Yaw (Rotation Around Down)','Pitch (Rotation Around East)','Roll (Rotation Around North) xlabel('Time (s)')
ylabel('Rotation (degrees)')
title('Orientation')

figure(3)
plot(timeVector,speed)
xlabel('Time (s)')
ylabel('Speed (m/s)')
title('Speed')

Speed


## Generate Spiraling Circular Trajectory with No Inputs

Define a constant angular velocity and constant acceleration that describe a spiraling circular trajectory.

```
Fs = 100;
r = 10;
speed = 2.5;
initialYaw = 90;
initPos = [r 0 0];
initVel = [0 speed 0];
initOrient = quaternion([initialYaw 0 0], 'eulerd', 'ZYX', 'frame');
accBody = [0 speed^2/r 0.01];
angVelBody = [0 0 speed/r];
```

Create a kinematic trajectory object.

```
traj = kinematicTrajectory('SampleRate',Fs, ...
    'Position',initPos, ...
    'Velocity',initVel, ...
    'Orientation',initOrient, ...
    'AccelerationSource','Property', ...
    'Acceleration',accBody, ...
```

```
'AngularVelocitySource','Property', ...
```

'AngularVelocity', angVelBody);

Call the kinematic trajectory object in a loop and log the position output. Plot the position over time.

```
N = 10000;
pos = zeros(N, 3);
for i = 1:N
    pos(i,:) = traj();
end
plot3(pos(:,1), pos(:,2), pos(:,3))
title('Position')
xlabel('X (m)')
ylabel('Y (m)')
zlabel('Z (m)')
```


## Position



## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\mathrm{TM}}$.
The object functions, perturbations and perturb, do not support code generation.
Usage notes and limitations:
"System Objects in MATLAB Code Generation" (MATLAB Coder)

## See Also

waypointTrajectory
Introduced in R2019b

## lidarScan

Create object for storing 2-D lidar scan

## Description

A lidarScan object contains data for a single 2-D lidar (light detection and ranging) scan. The lidar scan is a laser scan for a 2-D plane with distances (Ranges) measured from the sensor to obstacles in the environment at specific angles (Angles). Use this laser scan object as an input to other robotics algorithms such as matchScans, controllerVFH, or monteCarloLocalization.

## Creation

## Syntax

scan = lidarScan(ranges,angles)
scan = lidarScan(cart)

## Description

scan = lidarScan(ranges,angles) creates a lidarScan object from the ranges and angles, that represent the data collected from a lidar sensor. The ranges and angles inputs are vectors of the same length and are set directly to the Ranges and Angles properties.
scan = lidarScan(cart) creates a lidarScan object using the input Cartesian coordinates as an $n$-by- 2 matrix. The Cartesian property is set directly from this input.
scan = lidarScan(scanMsg) creates a lidarScan object from a LaserScan ROS message object.

## Properties

## Ranges - Range readings from lidar in meters

vector
Range readings from lidar, specified as a vector in meters. This vector is the same length as Angles, and the vector elements are measured in meters.
Data Types: single | double

## Angles - Angle of readings from lidar in radians

vector
Angle of range readings from lidar, specified as a vector. This vector is the same length as Ranges, and the vector elements are measured in radians. Angles are measured counter-clockwise around the positive $z$-axis.
Data Types: single | double

## Cartesian - Cartesian coordinates of lidar readings in meters <br> [ $x$ y] matrix

Cartesian coordinates of lidar readings, returned as an [ $x$ y] matrix. In the lidar coordinate frame, positive $x$ is forward and positive $y$ is to the left.
Data Types: single | double

## Count - Number of lidar readings scalar

Number of lidar readings, returned as a scalar. This scalar is also equal to the length of the Ranges and Angles vectors or the number of rows in Cartesian.

Data Types: double

## Object Functions

```
plot Display laser or lidar scan readings
removeInvalidData Remove invalid range and angle data
transformScan Transform laser scan based on relative pose
```


## Examples

## Plot Lidar Scan and Remove Invalid Points

Specify lidar data as vectors of ranges and angles. These values include readings outside of the sensors range.

```
x = linspace(-2,2);
ranges = abs((1.5).*x.^2 + 5);
ranges(45:55) = 3.5;
angles = linspace(-pi/2,pi/2,numel(ranges));
```

Create a lidar scan by specifying the ranges and angles. Plot all points of the lidar scan.

```
scan = lidarScan(ranges,angles);
plot(scan)
```

LiDAR Scan


Remove invalid points based on a specified minimum and maximum range.

```
minRange = 0.1;
maxRange = 7;
scan2 = removeInvalidData(scan,'RangeLimits',[minRange maxRange]);
hold on
plot(scan2)
legend('All Points','Valid Points')
```

* $\quad$ All Points
- $\quad$ Valid Points

LiDAR Scan


## Transform Laser Scans

Create a lidarScan object. Specify the ranges and angles as vectors.
refRanges $=5 *$ ones ( 1,300 );
refAngles $=$ linspace(-pi/2,pi/2,300);
refScan = lidarScan(refRanges,refAngles);
Translate the laser scan by an $[x y]$ offset of ( $0.5,0.2$ ).
transformedScan = transformScan(refScan,[0.5 0.2 0]);
Rotate the laser scan by 20 degrees.

```
rotateScan = transformScan(refScan,[0,0,deg2rad(20)]);
```


## Match Lidar Scans

Create a reference lidar scan using lidarScan (Robotics System Toolbox). Specify ranges and angles as vectors.

```
refRanges = 5*ones(1,300);
refAngles = linspace(-pi/2,pi/2,300);
refScan = lidarScan(refRanges,refAngles);
```

Using the transformScan (Robotics System Toolbox) function, generate a second lidar scan at an $x, y$ offset of (0.5, 0.2).

```
currScan = transformScan(refScan,[0.5 0.2 0]);
```

Match the reference scan and the second scan to estimate the pose difference between them.

```
pose = matchScans(currScan,refScan);
```

Use the transformScan function to align the scans by transforming the second scan into the frame of the first scan using the relative pose difference. Plot both the original scans and the aligned scans.

```
currScan2 = transformScan(currScan,pose);
subplot(2,1,1);
hold on
plot(currScan)
plot(refScan)
title('Original Scans')
hold off
subplot(2,1,2);
hold on
plot(currScan2)
plot(refScan)
title('Aligned Scans')
xlim([0 5])
hold off
```



## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Lidar scans require a limited size in code generation. The lidar scans are limited to 4000 points (range and angles) as a maximum.

## See Also

matchScans | transformScan | controllerVFH|monteCarloLocalization
Introduced in R2019b

## plot

Display laser or lidar scan readings

## Syntax

plot(scanObj)
plot(__, Name,Value)
linehandle $=p l o t(\ldots \quad)$

## Description

plot(scanObj) plots the lidar scan readings specified in scanObj.
plot( $\qquad$ ,Name, Value) provides additional options specified by one or more Name, Value pair arguments.
linehandle = plot( $\qquad$ ) returns a column vector of line series handles, using any of the arguments from previous syntaxes. Use linehandle to modify properties of the line series after it is created.

## Examples

## Plot Lidar Scan and Remove Invalid Points

Specify lidar data as vectors of ranges and angles. These values include readings outside of the sensors range.

```
x = linspace(-2,2);
ranges = abs((1.5).*x.^2 + 5);
ranges(45:55) = 3.5;
angles = linspace(-pi/2,pi/2,numel(ranges));
```

Create a lidar scan by specifying the ranges and angles. Plot all points of the lidar scan.

```
scan = lidarScan(ranges,angles);
```

plot(scan)


Remove invalid points based on a specified minimum and maximum range.

```
minRange = 0.1;
maxRange = 7;
scan2 = removeInvalidData(scan,'RangeLimits',[minRange maxRange]);
hold on
plot(scan2)
legend('All Points','Valid Points')
```



## Input Arguments

## scan0bj - Lidar scan readings

## lidarScan object

Lidar scan readings, specified as a lidarScan object.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, ... , NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Example: "MaximumRange",5

## Parent - Parent of axes

axes object
Parent of axes, specified as the comma-separated pair consisting of "Parent" and an axes object in which the laser scan is drawn. By default, the laser scan is plotted in the currently active axes.

## MaximumRange - Range of laser scan

scan. RangeMax (default) | scalar

Range of laser scan, specified as the comma-separated pair consisting of "MaximumRange" and a scalar. When you specify this name-value pair argument, the minimum and maximum $x$-axis and the maximum $y$-axis limits are set based on specified value. The minimum $y$-axis limit is automatically determined by the opening angle of the laser scanner.

This name-value pair only works when you input scanMsg as the laser scan.

## Outputs

## linehandle - One or more chart line objects <br> scalar | vector

One or more chart line objects, returned as a scalar or a vector. These are unique identifiers, which you can use to query and modify properties of a specific chart line.

See Also<br>matchScans|transformScan | controllerVFH|monteCarloLocalization<br>Topics<br>"Estimate Robot Pose with Scan Matching"<br>Introduced in R2015a

## lidarSLAM

Perform localization and mapping using lidar scans

## Description

The lidarSLAM class performs simultaneous localization and mapping (SLAM) for lidar scan sensor inputs. The SLAM algorithm takes in lidar scans and attaches them to a node in an underlying pose graph. The algorithm then correlates the scans using scan matching. It also searches for loop closures, where scans overlap previously mapped regions, and optimizes the node poses in the pose graph.

## Creation

## Syntax

```
slamObj = lidarSLAM
slamObj = lidarSLAM(mapResolution,maxLidarRange)
slamObj = lidarSLAM(mapResolution,maxLidarRange,maxNumScans)
```


## Description

slamObj = lidarSLAM creates a lidar SLAM object. The default occupancy map size is 20 cells per meter. The maximum range for each lidar scan is 8 meters.
slam0bj = lidarSLAM(mapResolution,maxLidarRange) creates a lidar SLAM object and sets the MapResolution and MaxLidarRange properties based on the inputs.
slam0bj = lidarSLAM(mapResolution,maxLidarRange,maxNumScans) specifies the upper bound on the number of accepted scans allowed when generating code. maxNumScans is a positive integer. This scan limit is only required when generating code.

## Properties

## PoseGraph - Underlying pose graph that connects scans

poseGraph object
Underlying pose graph that connects scans, specified as a poseGraph object. Adding scans to lidarSLAM updates this pose graph. When loop closures are found, the pose graph is optimized using OptimizationFen.

## MapResolution - Resolution of occupancy grid map

20 cells per meter (default) | positive integer
Resolution of the occupancy grid map, specified as a positive integer in cells per meter. Specify the map resolution on construction.

MaxLidarRange - Maximum range of lidar sensor
8 meters (default) | positive scalar

Maximum range of the lidar sensor, specified as a positive scalar in meters. Specify the maximum range on construction.

## OptimizationFcn - Pose graph optimization function <br> optimizePoseGraph (default)| function handle

Pose graph optimization function, specified as a function handle. By default, the algorithm calls the optimizePoseGraph function. To specify your own optimization method, the class requires the function signature to be:
[updatedPose,stat] = myOptimizationFcn(poseGraph)
poseGraph is a poseGraph object. updatedPose is an $n$-by-3 vector of [ $x$ y theta] poses listed in sequential node ID order. stat is a structure containing a ResidualError field as a positive scalar. Use the stat structure to include other information relevant to your optimization.

## LoopClosureThreshold - Threshold for accepting loop closures

100 (default) | positive scalar
Threshold on the score from the scan matching algorithm for accepting loop closures, specified as a positive scalar. Higher thresholds correspond to a better match, but scores vary based on sensor data.

## LoopClosureSearchRadius - Search radius for loop closure detection <br> 8 meters (default) | positive scalar

Search radius for loop closure detection, specified as a positive scalar. Increasing this radius affects performance by increasing search time. Tune this distance based on your environment and the expected vehicle trajectory.

## LoopClosureMaxAttempts - Number of attempts at finding loop closures <br> 1 (default) | positive integer

Number of attempts at finding looping closures, specified as a positive integer. Increasing the number of attempts affects performance by increasing search time.

## LoopClosureAutoRollback - Allow automatic rollback of added loop closures true (default) | false

Allow automatic rollback of added loop closures, specified as true or false. The SLAM object tracks the residual error returned by the OptimizationFcn. If it detects a sudden change in the residual error and this property is true, it rejects (rolls back) the loop closure.

## OptimizationInterval - Number of loop closures accepted to trigger optimization 1 (default) | positive integer

Number of loop closures accepted to trigger optimization, specified as a positive integer. By default, the PoseGraph is optimized every time lidarSLAM adds a loop closure.

## MovementThreshold - Minimum change in pose required to process scans <br> [0 0] (default)|[translation rotation]

Minimum change in pose required to process scans, specified as a [translation rotation] vector. A relative pose change for a newly added scan is calculated as [x y theta]. If the translation in xy-position or rotation of theta exceeds these thresholds, the lidarSLAM object accepts the scan and adds a pose is added to the PoseGraph.

## ScanRegistrationMethod - Scan registration method

'BranchAndBound' (default)|'PhaseCorrelation'
Scan registration method, specified as a character vector.

Note Image Processing Toolbox ${ }^{\text {tM }}$ is required for using Phase Correlation method.

## TranslationSearchRange - Incremental match translational search range <br> [maxLidarRange/2 maxLidarRange/2] (default)|two-element vector of the form [ $x \quad y$ ]

Incremental match translational search range, specified as a two-element vector of the form $[x y]$ in meters. This property is only applicable when the ScanRegistrationMethod property is set to 'BranchAndBound'.

These values define the search window around the initial translation estimate specified in the relPoseEst argument of the addScan function. Set the value of this property to the maximum expected translation between consecutive accepted scans.

This property is similar to the 'TranslationSearchRange ' name-value pair argument in matchScansGrid function.

## RotationSearchRange - Incremental match rotational search range

pi/2 (default) | positive scalar
Incremental match rotational search range, specified as positive scalar in radians. This property is only applicable when the ScanRegistrationMethod property is set to 'BranchAndBound'.

This values define the search window around the initial rotation estimate specified in the relPoseEst argument of the addScan function. Set the value of this property to the maximum expected rotation between consecutive accepted scans.

This property is similar to the 'RotationSearchRange' name-value pair argument in matchScansGrid function.

## Object Functions

| addScan | Add scan to lidar SLAM map |
| :--- | :--- |
| copy | Copy lidar SLAM object |
| removeLoopClosures | Remove loop closures from pose graph |
| scansAndPoses | Extract scans and corresponding poses |
| show | Plot scans and robot poses |

## Examples

## Perform SLAM Using Lidar Scans

Use a lidarSLAM object to iteratively add and compare lidar scans and build an optimized pose graph of the robot trajectory. To get an occupancy map from the associated poses and scans, use the buildMap function.

## Load Data and Set Up SLAM Algorithm

Load a cell array of lidarScan objects. The lidar scans were collected in a parking garage on a Husky $\circledR_{\text {r robot from ClearPath Robotics } ® \text {. Typically, lidar scans are taken at a high frequency and }}$ each scan is not needed for SLAM. Therefore, down sample the scans by selecting only every 40th scan.

```
load garage_fl1_southend.mat scans
scans = scans(1:40:end);
```

To set up the SLAM algorithm, specify the lidar range, map resolution, loop closure threshold, and search radius. Tune these parameters for your specific robot and environment. Create the lidarSLAM object with these parameters.

```
maxRange = 19.2; % meters
resolution = 10; % cells per meter
slamObj = lidarSLAM(resolution,maxRange);
slamObj.LoopClosureThreshold = 360;
slamObj.LoopClosureSearchRadius = 8;
```


## Add Scans Iteratively

Using a for loop, add scans to the SLAM object. The object uses scan matching to compare each added scan to previously added ones. To improve the map, the object optimizes the pose graph whenever it detects a loop closure. Every 10 scans, display the stored poses and scans.

```
for i = 1:numel(scans)
    addScan(slamObj,scans{i});
    if rem(i,10) == 0
        show(slamObj);
    end
end
```



## View Occupancy Map

After adding all the scans to the SLAM object, build an occupancyMap map by calling buildMap with the scans and poses. Use the same map resolution and max range you used with the SLAM object.

```
[scansSLAM,poses] = scansAndPoses(slamObj);
occMap = buildMap(scansSLAM, poses,resolution,maxRange);
figure
show(occMap)
title('Occupancy Map of Garage')
```



## More About

## SLAM

Simultaneous localization and mapping (SLAM) is a general concept for algorithms correlating different sensor readings to build a map of a vehicle environment and track pose estimates. Different algorithms use different types of sensors and methods for correlating data.

The lidarSLAM algorithm uses lidar scans and odometry information as sensor inputs. The lidar scans map the environment and are correlated between each other to build an underlying pose graph of the vehicle trajectory. Odometry information is an optional input that gives an initial pose estimate for the scans to aid in the correlation. Scan matching algorithms correlate scans to previously added scans to estimate the relative pose between them and add them to an underlying pose graph.

The pose graph contains nodes connected by edges that represent the relative poses of the vehicle. Edges specify constraints on the node as an information matrix. To correct for drifting pose estimates, the algorithm optimizes over the whole pose graph whenever it detects loop closures.

The algorithm assumes that data comes from a vehicle navigating an environment and incrementally getting laser scans along its path. Therefore, scans are first compared to the most recent scan to identify relative poses and are added to the pose graph incrementally. However, the algorithm also searches for loop closures, which identify when the vehicle scans an area that was previously visited.

When working with SLAM algorithms, the environment and vehicle sensors affect the performance and data correlation quality. Tune your parameters properly for your expected environment or dataset.

## References

[1] Hess, Wolfgang, Damon Kohler, Holger Rapp, and Daniel Andor. "Real-Time Loop Closure in 2D LIDAR SLAM." 2016 IEEE International Conference on Robotics and Automation (ICRA). 2016.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Use this syntax when constructing lidarSLAM objects for code generation:
slamObj= lidarSLAM(mapResolution,maxLidarRange,maxNumScans) specifies the upper bound on the number of accepted scans allowed when generating code. maxNumScans is a positive integer. This scan limit is only required when generating code.

## See Also

poseGraph | optimizePoseGraph

## Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
"Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
Introduced in R2019b

## addScan

Add scan to lidar SLAM map

## Syntax

```
addScan(slamObj,currScan)
addScan(slamObj,currScan,relPoseEst)
[isAccepted,loopClosureInfo,optimInfo] = addScan(___)
```


## Description

addScan(slamObj, currScan) adds a lidar scan, currScan, to the lidar SLAM object, slamObj. The function uses scan matching to correlate this scan to the most recent one, then adds it to the pose graph defined in slam0bj. If the scan is accepted, addScan detects loop closures and optimizes based on settings in slam0bj.
addScan(slamObj, currScan, relPoseEst) also specifies a relative pose to the latest lidar scan pose in slamObj. This relative pose improves the scan matching.

Note The relPoseEst input is ignored when the ScanRegistrationMethod property of lidarSLAM object is set to 'PhaseCorrelation'.
[isAccepted,loopClosureInfo,optimInfo] = addScan( $\qquad$ ) outputs detailed information about adding the scan to the SLAM object. isAccepted indicates if the scan is added or rejected. loopClosureInfo and optimInfo indicate if a loop closure is detected or the pose graph is optimized.

## Examples

## Perform SLAM Using Lidar Scans

Use a lidarSLAM object to iteratively add and compare lidar scans and build an optimized pose graph of the robot trajectory. To get an occupancy map from the associated poses and scans, use the buildMap function.

## Load Data and Set Up SLAM Algorithm

Load a cell array of lidarScan objects. The lidar scans were collected in a parking garage on a Husky ${ }^{\circledR}$ robot from ClearPath Robotics®. Typically, lidar scans are taken at a high frequency and each scan is not needed for SLAM. Therefore, down sample the scans by selecting only every 40th scan.

```
load garage_fl1_southend.mat scans
scans = scans(1:40:end);
```

To set up the SLAM algorithm, specify the lidar range, map resolution, loop closure threshold, and search radius. Tune these parameters for your specific robot and environment. Create the lidarSLAM object with these parameters.

```
maxRange = 19.2; % meters
resolution = 10; % cells per meter
slamObj = lidarSLAM(resolution,maxRange);
slamObj.LoopClosureThreshold = 360;
slamObj.LoopClosureSearchRadius = 8;
```


## Add Scans Iteratively

Using a for loop, add scans to the SLAM object. The object uses scan matching to compare each added scan to previously added ones. To improve the map, the object optimizes the pose graph whenever it detects a loop closure. Every 10 scans, display the stored poses and scans.

```
for i = 1:numel(scans)
    addScan(slamObj,scans{i});
    if rem(i,10) == 0
        show(slamObj);
    end
end
```



## View Occupancy Map

After adding all the scans to the SLAM object, build an occupancyMap map by calling buildMap with the scans and poses. Use the same map resolution and max range you used with the SLAM object.

```
[scansSLAM,poses] = scansAndPoses(slamObj);
occMap = buildMap(scansSLAM,poses,resolution,maxRange);
figure
show(occMap)
title('Occupancy Map of Garage')
```



## Input Arguments

## slamObj - Lidar SLAM object

lidarSLAM object
Lidar SLAM object, specified as a lidarSLAM object. The object contains the SLAM algorithm parameters, sensor data, and underlying pose graph used to build the map.

## currScan - Lidar scan reading

lidarScan object
Lidar scan reading, specified as a lidarScan object. This scan is correlated to the most recent scan in slamObj using scan matching.

## relPoseEst - Relative pose estimate of scan

[x y theta] vector
Relative pose estimate of scan, specified as an [x y theta] vector. This relative pose improves scan matching.

## Output Arguments

## isAccepted - Indicates if scan is accepted <br> true |false

Indicates if scan is accepted, returned as true or false. If the relative pose between scans is below the MovementThreshold property of slamObj, the scan is rejected. By default, all scans are accepted.

## loopClosureInfo - Loop closure details

structure
Loop closure details, returned as a structure with these fields:

- EdgeIDs -- IDs of newly connected edges in the pose graph, returned as a vector.
- Edges -- Newly added loop closure edges, returned as an $n$-by-2 matrix of node IDs that each edge connects.
- Scores -- Scores of newly connected edges in the pose graph returned from scan matching, returned as a vector.

Note If the LoopClosureAutoRollback property is set to true in slam0bj, loop closure edges can be removed from the pose graph. This property rejects loops closures if the residual error changes drastically after optimization. Therefore, some of the edge IDs listed in this structure may not exist in the actual pose graph.

## optimInfo - Pose graph optimization details

structure
Pose graph optimization details, returned as a structure with these fields:

- IsPerformed -- Boolean indicating if optimization is performed when adding this scan. Optimization performance depends on the OptimizationInterval property in slam0bj.
- IsAccepted -- Boolean indicating if optimization was accepted based on ResidualError.
- ResidualError -- Error associated with optimization, returned as a scalar.
- LoopClosureRemoved -- List of IDs of loop closure edges removed during optimization, returned as a vector.


## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Use this syntax when constructing lidarSLAM objects for code generation:
slamObj= lidarSLAM(mapResolution,maxLidarRange,maxNumScans) specifies the upper bound on the number of accepted scans allowed when generating code. maxNumScans is a positive integer. This scan limit is only required when generating code.

## See Also

poseGraph | optimizePoseGraph

# Topics <br> "Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans" <br> "Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans" <br> Introduced in R2019b 

## copy

Copy lidar SLAM object

## Syntax

newSlamObj = copy(slamObj)

## Description

newSlamObj $=$ copy (slamObj) creates a deep copy of slamObj with the same properties. Any changes made to newSlamObj are not reflected in slamObj.

## Examples

## Create Copy of Lidar SLAM

Create a lidarSLAM object.

```
slamObj = lidarSLAM
slam0bj =
    lidarSLAM with properties:
                    PoseGraph: [1x1 poseGraph]
                MapResolution: 20
                    MaxLidarRange: 8
                    OptimizationFcn: @optimizePoseGraph
            LoopClosureThreshold: 100
        LoopClosureSearchRadius: 8
            LoopClosureMaxAttempts: 1
        LoopClosureAutoRollback: 1
            OptimizationInterval: 1
                MovementThreshold: [0 0]
            ScanRegistrationMethod: 'BranchAndBound'
            TranslationSearchRange: [4 4]
                RotationSearchRange: 1.5708
```

Create a copy of the lidar SLAM object.

```
slamObjNew = copy(slamObj)
slamObjNew =
    lidarSLAM with properties:
                PoseGraph: [1x1 poseGraph]
            MapResolution: 20
            MaxLidarRange: 8
            OptimizationFcn: @optimizePoseGraph
        LoopClosureThreshold: 100
        LoopClosureSearchRadius: 8
```

```
    LoopClosureMaxAttempts: 1
LoopClosureAutoRollback: 1
    OptimizationInterval: 1
        MovementThreshold: [0 0]
    ScanRegistrationMethod: 'BranchAndBound'
TranslationSearchRange: [4 4]
    RotationSearchRange: 1.5708
```


## Input Arguments

## slam0bj - Lidar SLAM object

lidarSLAM object
Lidar SLAM object, specified as a lidarSLAM object. The object contains the SLAM algorithm parameters, sensor data, and underlying pose graph used to build the map.

## Output Arguments

newSlam0bj - Lidar SLAM object
lidarSLAM object
Lidar SLAM object, returned as a lidarSLAM object.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.
Use this syntax when constructing lidarSLAM objects for code generation:
slamObj= lidarSLAM(mapResolution,maxLidarRange,maxNumScans) specifies the upper bound on the number of accepted scans allowed when generating code. maxNumScans is a positive integer. This scan limit is only required when generating code.

## See Also

poseGraph | optimizePoseGraph

## Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
"Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
Introduced in R2019b

## removeLoopClosures

Remove loop closures from pose graph

## Syntax

removeLoopClosures(slamObj)
removeLoopClosures(slam0bj,lcEdgeIDs)

## Description

removeLoopClosures(slamObj) removes all loop closures from the underlying pose graph in slam0bj.
removeLoopClosures(slam0bj,lcEdgeIDs) removes the loop closure edges with the specified IDs from the underlying pose graph in slam0bj.

## Input Arguments

## slamObj - Lidar SLAM object <br> lidarSLAM object

Lidar SLAM object, specified as a lidarSLAM object. The object contains the SLAM algorithm parameters, sensor data, and underlying pose graph used to build the map

## lcEdgeIDs - Loop closure edge IDs

vector of positive integers
Loop closure edge IDs, specified as a vector of positive integers. To find specific edge IDs, use findEdgeID on the underlying poseGraph object defined in slamObj.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\mathrm{TM}}$.
Use this syntax when constructing lidarSLAM objects for code generation:
slamObj= lidarSLAM(mapResolution,maxLidarRange,maxNumScans) specifies the upper bound on the number of accepted scans allowed when generating code. maxNumScans is a positive integer. This scan limit is only required when generating code.

## See Also

poseGraph | optimizePoseGraph

## Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
"Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

Introduced in R2019b

## scansAndPoses

Extract scans and corresponding poses

## Syntax

[scans,poses] = scansAndPoses(slam0bj)
[scans,poses] = scansAndPoses(slamObj,nodeIDs)

## Description

[scans, poses] = scansAndPoses(slam0bj) returns the scans used by the lidarSLAM object as lidarScan objects, along with their associated [x y theta] poses from the underlying pose graph of slam0bj.
[scans,poses] = scansAndPoses(slam0bj, nodeIDs) returns the scans and poses for the specific node IDs. To get the node IDs, see the underlying poseGraph object in slamObj for the node IDs.

## Examples

## Perform SLAM Using Lidar Scans

Use a lidarSLAM object to iteratively add and compare lidar scans and build an optimized pose graph of the robot trajectory. To get an occupancy map from the associated poses and scans, use the buildMap function.

## Load Data and Set Up SLAM Algorithm

Load a cell array of lidarScan objects. The lidar scans were collected in a parking garage on a Husky® robot from ClearPath Robotics®. Typically, lidar scans are taken at a high frequency and each scan is not needed for SLAM. Therefore, down sample the scans by selecting only every 40th scan.

```
load garage_fl1_southend.mat scans
scans = scañ(1; 40:end);
```

To set up the SLAM algorithm, specify the lidar range, map resolution, loop closure threshold, and search radius. Tune these parameters for your specific robot and environment. Create the lidarSLAM object with these parameters.

```
maxRange = 19.2; % meters
resolution = 10; % cells per meter
slamObj = lidarSLAM(resolution,maxRange);
slamObj.LoopClosureThreshold = 360;
slam0bj.LoopClosureSearchRadius = 8;
```


## Add Scans Iteratively

Using a for loop, add scans to the SLAM object. The object uses scan matching to compare each added scan to previously added ones. To improve the map, the object optimizes the pose graph whenever it detects a loop closure. Every 10 scans, display the stored poses and scans.

```
for i = 1:numel(scans)
    addScan(slamObj,scans{i});
    if rem(i,10) == 0
        show(slamObj);
    end
end
```



## View Occupancy Map

After adding all the scans to the SLAM object, build an occupancyMap map by calling buildMap with the scans and poses. Use the same map resolution and max range you used with the SLAM object.

```
[scansSLAM,poses] = scansAndPoses(slamObj);
occMap = buildMap(scansSLAM,poses,resolution,maxRange);
figure
show(occMap)
title('Occupancy Map of Garage')
```



## Input Arguments

## slamObj - Lidar SLAM object

## lidarSLAM object

Lidar SLAM object, specified as a lidarSLAM object. The object contains the SLAM algorithm parameters, sensor data, and underlying pose graph used to build the map.

## nodeIDs - Node IDs from pose graph

positive integer
Node IDs from pose graph, specified as a positive integer. Nodes are added to the pose graph with sequential ID numbers. To get the node IDs, see the underlying poseGraph object in slam0bj for the node IDs.

## Output Arguments

## scans - Lidar scan readings

lidarScan object
Lidar scan readings, returned as a lidarScan object.

## poses - Pose for each scan

$n$-by-3 matrix | [x y theta] vectors

Pose for each scan, returned as an n-by-3 matrix of [x y theta] vectors. Each row is a pose that corresponds to a scan in scans.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{Tm}}$.
Use this syntax when constructing lidarSLAM objects for code generation:
slamObj= lidarSLAM(mapResolution,maxLidarRange,maxNumScans) specifies the upper bound on the number of accepted scans allowed when generating code. maxNumScans is a positive integer. This scan limit is only required when generating code.

## See Also

poseGraph |optimizePoseGraph

## Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
"Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

Introduced in R2019b

## show

Plot scans and robot poses

## Syntax

```
show(slamObj)
show(slamObj,Name,Value)
axes = show(
```

$\qquad$

``` )
```


## Description

show(slamObj) plots all the scans added to the input lidarSLAM object overlaid with the lidar poses in its underlying pose graph.
show(slamObj, Name, Value) specifies options using Name, Value pair arguments. For example, "Poses", "off" turns off display of the underlying pose graph in slamObj.
axes $=$ show ( $\qquad$ ) returns the axes handle that the lidar SLAM data is plotted to using any of the previous syntaxes.

## Examples

## Perform SLAM Using Lidar Scans

Use a lidarSLAM object to iteratively add and compare lidar scans and build an optimized pose graph of the robot trajectory. To get an occupancy map from the associated poses and scans, use the buildMap function.

## Load Data and Set Up SLAM Algorithm

Load a cell array of lidarScan objects. The lidar scans were collected in a parking garage on a Husky ${ }^{\circledR}$ robot from ClearPath Robotics ${ }^{\circledR}$. Typically, lidar scans are taken at a high frequency and each scan is not needed for SLAM. Therefore, down sample the scans by selecting only every 40th scan.

```
load garage_fl1_southend.mat scans
scans = scans(1:40:end);
```

To set up the SLAM algorithm, specify the lidar range, map resolution, loop closure threshold, and search radius. Tune these parameters for your specific robot and environment. Create the lidarSLAM object with these parameters.

```
maxRange = 19.2; % meters
resolution = 10; % cells per meter
slamObj = lidarSLAM(resolution,maxRange);
slamObj.LoopClosureThreshold = 360;
slam0bj.LoopClosureSearchRadius = 8;
```


## Add Scans Iteratively

Using a for loop, add scans to the SLAM object. The object uses scan matching to compare each added scan to previously added ones. To improve the map, the object optimizes the pose graph whenever it detects a loop closure. Every 10 scans, display the stored poses and scans.

```
for i = 1:numel(scans)
    addScan(slamObj,scans{i});
    if rem(i,10) == 0
        show(slamObj);
    end
end
```



## View Occupancy Map

After adding all the scans to the SLAM object, build an occupancyMap map by calling buildMap with the scans and poses. Use the same map resolution and max range you used with the SLAM object.

```
[scansSLAM,poses] = scansAndPoses(slamObj);
occMap = buildMap(scansSLAM,poses,resolution,maxRange);
figure
show(occMap)
title('Occupancy Map of Garage')
```



## Input Arguments

## slamObj - Lidar SLAM object

lidarSLAM object
Lidar SLAM object, specified as a lidarSLAM object. The object contains the SLAM algorithm parameters, sensor data, and underlying pose graph used to build the map.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, . . , NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: "Poses", "off"

## Parent - Axes used to plot pose graph

Axes object | UIAxes object
Axes used to plot the pose graph, specified as the comma-separated pair consisting of "Parent" and either an Axes or UIAxes object. See axes or uiaxes.

## Poses - Display lidar poses

"on" (default)|"off"

Display lidar poses, specified as the comma-separated pair consisting of "Poses" and "on" or "off".

## Output Arguments

## axes - Axes used to plot the map

Axes object | UIAxes object
Axes used to plot the map, returned as either an Axes or UIAxes object. See axes or uiaxes.

## See Also

poseGraph | optimizePoseGraph

## Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
"Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

## Introduced in R2019b

## likelihoodFieldSensorModel

Create a likelihood field range sensor model

## Description

The likelihoodFieldSensor object creates a likelihood field sensor model object for range sensors. This object contains specific sensor model parameters. You can use this object to specify the model parameters in a monteCarloLocalization object.

## Creation

## Syntax

lf = likelihoodFieldSensorModel

## Description

lf = likelihoodFieldSensorModel creates a likelihood field sensor model object for range sensors.

## Properties

## Map - Occupancy grid representing the map

binary0ccupancyMap object (default)
Occupancy grid representing the map, specified as a binaryOccupancyMap object. This object represents the environment of the vehicle as a grid with binary values indicating obstacles as true (1) and free locations as false (0).

## SensorPose - Pose of the range sensor relative to the vehicle

[000] (default) | three-element vector
Pose of the range sensor relative to the coordinate frame of the vehicle, specified as a three-element vector, [x y theta].

## SensorLimits - Minimum and maximum range of sensor

[0 12] (default) | two-element vector
Minimum and maximum range of sensor, specified as a two-element vector in meters.

## NumBeams - Number of beams used for likelihood computation <br> 60 (default) | scalar

Number of beams used for likelihood computation, specified as a scalar. The computation efficiency can be improved by specifying a smaller number of beams than the actual number available from the sensor.

## MeasurementNoise - Standard deviation for measurement noise 0.2 (default) | scalar

Standard deviation for measurement noise, specified as a scalar.

## RandomMeasurementWeight - Weight for probability of random measurement 0.05 (default) | scalar

Weight for probability of random measurement, specified as a scalar. This scalar is the probability that the measurement is not accurate due to random interference.

## ExpectedMeasurementWeight - Weight for probability of expected measurement <br> 0.95 (default) | scalar

Weight for probability of expected measurement, specified as a scalar. The weight is the probability of getting a correct range measurement within the noise limits specified in MeasurementNoise property.

MaxLikelihoodDistance - Maximum distance to find nearest obstacles
2.0 (default) | scalar

Maximum distance to find nearest obstacles, specified as a scalar in meters.

## Limitations

If you change your sensor model after using it with the monteCarloLocalization object, call release on that object beforehand. For example:

```
mcl = monteCarloLocalization;
```

[isUpdated, pose,covariance] = mcl(ranges,angles);
release(mcl)
mcl.SensorModel.NumBeams = 120;

## See Also

monteCarloLocalization | odometryMotionModel

## Topics

"Localize TurtleBot Using Monte Carlo Localization"
"Monte Carlo Localization Algorithm"

## Introduced in R2019b

## magparams

Magnetometer sensor parameters

## Description

The magparams class creates a magnetometer sensor parameters object. You can use this object to model a magnetometer when simulating an IMU with imuSensor. See the "Algorithms" on page 2477 section of imuSensor for details of magparams modeling.

## Creation

## Syntax

```
params = magarams
```

params = magparams(Name,Value)

## Description

params = magarams returns an ideal magnetometer sensor parameters object with default values.
params = magparams (Name, Value) configures magparams object properties using one or more Name, Value pair arguments. Name is a property name and Value is the corresponding value. Name must appear inside single quotes (' ' ). You can specify several name-value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN. Any unspecified properties take default values.

## Properties

MeasurementRange - Maximum sensor reading ( $\mu \mathrm{T}$ )
Inf (default) | real positive scalar
Maximum sensor reading in $\mu \mathrm{T}$, specified as a real positive scalar.

## Data Types: single | double

## Resolution - Resolution of sensor measurements ( $\mu \mathrm{T} / \mathrm{LSB}$ )

0 (default) | real nonnegative scalar
Resolution of sensor measurements in $\mu \mathrm{T} / \mathrm{LSB}$, specified as a real nonnegative scalar. Here, LSB is the acronym for least significant bit.
Data Types: single | double

## ConstantBias - Constant sensor offset bias ( $\mu \mathrm{T}$ )

[0 0 0 ] (default) | real scalar | real 3-element row vector
Constant sensor offset bias in $\mu \mathrm{T}$, specified as a real scalar or 3 -element row vector. Any scalar input is converted into a real 3 -element row vector where each element has the input scalar value.
Data Types: single | double

## AxesMisalignment - Sensor axes skew (\%)

diag ([100 100 100]) (default) | scalar in the range [0,100]| 3 -element row vector in the range [ 0,100 ] | 3 -by-3 matrix in the range $[0,100$ ]

Sensor axes skew in percentage, specified as a scalar, a 3-element row vector, or a 3-by-3 matrix with values ranging from 0 to 100 . The diagonal elements of the matrix account for the misalignment effects for each axes. The off-diagonal elements account for the cross-axes misalignment effects. The measured state $v_{\text {measure }}$ is obtained from the true state $v_{\text {true }}$ via the misalignment matrix as:

$$
v_{\text {measure }}=\frac{1}{100} M v_{\text {true }}=\frac{1}{100}\left[\begin{array}{lll}
m_{11} & m_{12} & m_{13} \\
m_{21} & m_{22} & m_{23} \\
m_{31} & m_{32} & m_{33}
\end{array}\right] v_{\text {true }}
$$

- If you specify the property as a scalar, then all the off-diagonal elements of the matrix take the value of the specified scalar and all the diagonal elements are 100.
- If you specify the property as a vector [abc], then $m_{21}=m_{31}=a, m_{12}=m_{32}=b$, and $m_{13}=m_{23}=$ c. All the diagonal elements are 100.


## Data Types: single | double

## NoiseDensity - Power spectral density of sensor noise ( $\mu \mathrm{T} / \sqrt{ } \mathrm{Hz}$ )

[0000] (default) | real scalar | real 3-element row vector
Power spectral density of sensor noise in $\mu \mathrm{T} / \sqrt{ } \mathrm{Hz}$, specified as a real scalar or 3 -element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.
Data Types: single | double

## BiasInstability - Instability of the bias offset ( $\mu \mathrm{T}$ )

[0 0 0] (default) | real scalar | real 3-element row vector
Instability of the bias offset in $\mu \mathrm{T}$, specified as a real scalar or 3 -element row vector. Any scalar input is converted into a real 3 -element row vector where each element has the input scalar value.

Data Types: single | double

## RandomWalk - Integrated white noise of sensor ( $\mu \mathrm{T} / \sqrt{ } \mathrm{Hz}$ )

[0 0 0] (default) | real scalar | real 3-element row vector
Integrated white noise of sensor in ( $\mu \mathrm{T} / \sqrt{ } \mathrm{Hz}$ ), specified as a real scalar or 3 -element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.
Data Types: single | double

## TemperatureBias - Sensor bias from temperature ( $\mu \mathrm{T} /{ }^{\circ} \mathrm{C}$ )

[0 0000$]$ (default) | real scalar | real 3-element row vector
Sensor bias from temperature in $\left(\mu \mathrm{T} /{ }^{\circ} \mathrm{C}\right)$, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

## Data Types: single | double

TemperatureScaleFactor - Scale factor error from temperature (\%/ $\left.{ }^{\circ} \mathbf{C}\right)$
$\left[\begin{array}{lll}0 & 0 & 0\end{array}\right]$ (default) | real scalar in the range $[0,100] \mid$ real 3 -element row vector in the range $[0,100]$

Scale factor error from temperature in $\left(\% /{ }^{\circ} \mathrm{C}\right)$, specified as a real scalar or 3 -element row vector with values ranging from 0 to 100 . Any scalar input is converted into a real 3 -element row vector where each element has the input scalar value.
Data Types: single | double

## Examples

## Generate Magnetometer Data from Stationary Inputs

Generate magnetometer data for an imuSensor object from stationary inputs.
Generate a magnetometer parameter object with a maximum sensor reading of $1200 \mu \mathrm{~T}$ and a resolution of $0.1 \mu \mathrm{~T} / \mathrm{LSB}$. The constant offset bias is $1 \mu \mathrm{~T}$. The sensor has a power spectral density of $\left(\frac{[0.60 .60 .9]}{\sqrt{100}}\right) \mu \mathrm{T} / \sqrt{\mathrm{Hz}}$. The bias from temperature is $[0.80 .82 .4] \mu \mathrm{T} / 0 \mathrm{C}$. The scale factor error from temperature is $0.1 \% / 0 \mathrm{C}$.
params = magparams('MeasurementRange',1200,'Resolution', 0.1,'ConstantBias',1,'NoiseDensity', [0.6
Use a sample rate of 100 Hz spaced out over 1000 samples. Create the imuSensor object using the magnetometer parameter object.

```
Fs = 100;
numSamples = 1000;
t = 0:1/Fs:(numSamples-1)/Fs;
imu = imuSensor('accel-mag','SampleRate', Fs, 'Magnetometer', params);
```

Generate magnetometer data from the imuSensor object.

```
orient = quaternion.ones(numSamples, 1);
acc = zeros(numSamples, 3);
angvel = zeros(numSamples, 3);
```

[~, magData] = imu(acc, angvel, orient);

Plot the resultant magnetometer data.

```
plot(t, magData)
title('Magnetometer')
xlabel('s')
ylabel('\mu T')
```



## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

accelparams | gyroparams | imuSensor
Introduced in R2018b

## mapLayer

Create map layer for $N$-dimensional data

## Description

The mapLayer object creates an $N$-dimensional grid map, where the first two dimensions determine the footprint of the map, and all subsequent dimensions dictate the size and layout of the data stored in each cell. For storing scalar binary or probability values for a grid map, use the binary0ccupancyMap or occupancyMap objects instead.

A map layer stores data for grid cells that represent a discretized region of space. To query and update data using world, local, or grid coordinates, use the getMapData and setMapData object functions. Each grid cell in the map can store data of any size from a single a value to a multidimensional array. For more information, see the DataSize property.

Layer behavior can also be customized by providing function handles during creation using the GetTransformFcn and SetTransformFcn properties.

## Creation

## Syntax

```
map = mapLayer
map = mapLayer(p)
map = mapLayer(width,height)
map = mapLayer(rows,cols,'grid')
map = mapLayer(width,height,cellDims)
map = mapLayer(rows,cols,cellDims,'grid')
map = mapLayer(sourceMap)
map = mapLayer(
```

$\qquad$

``` ,Name, Value)
```


## Description

map = mapLayer creates an empty map object occupying 10-by-10 meters of space with a resolution of 1 cell per meter.
map $=$ mapLayer $(p)$ creates a map from the values in the matrix or matrix array $p$. For 3-D matrix arrays, each cell in the map is filled with the vector of values at each grid location along the third dimension of the array. For an $N$-by- $D$ matrix array, each cell contains a matrix ( $N=4$ ) or a matrix array $(N>4)$ of data for that grid location.
map = mapLayer(width, height) creates a map covering the specified width and height with a resolution of 1 cell per meter.
map = mapLayer(rows, cols,'grid') creates a map with a grid size of rows,cols with a resolution of 1 cell per meter.
map $=$ mapLayer(width, height, cellDims) creates the map where the size of the data stored in each cell is defined by the array of integers cellDims.
map $=$ mapLayer(rows, cols, cellDims,'grid') creates a map with a grid size of rowscols where the size of the data stored in each cell is defined by the array of integers cellDims.
map = mapLayer(sourceMap) creates a new object using the layers copied from another mapLayer object.
map $=$ mapLayer (__ , Name, Value) specifies property values using name-value pairs.
For example, mapLayer(__,'LocalOriginInWorld',[15 20]) sets the local origin to a specific world location.

## Properties

## DataSize - Size of the $\boldsymbol{N}$-dimensional data matrix

## [10 10] (default) | vector of integers

Size of the $N$-dimensional data matrix, specified as vector of integers. The first two dimensions define the footprint of the map, and all subsequent dimensions dictate the size and layout of the data stored in each cell. The default value assumes a single value is stored for each cell in a 10-by-10 grid.

If the map stores an $n$-element vector of values in each cell, this property would be [width height $\mathrm{n}]$.

If the map stores a 10-by-10 grid with each cell containing a 3-by-3-by-3 matrix array, the data size would be $\left[\begin{array}{lllll}10 & 10 & 3 & 3 & 3\end{array}\right]$.

This property is set when you create the object based on the dimensions of the input matrix $p$ or the inputs width, height, and cellDims.

After you create the object, this property is read-only.
Data Types: double

## DataType - Data type of the values stored

'double' (default)| character vector
Data type of the values stored in the map, specified as a character vector.
This property is set based on the data type of the input $p$ or the data type of DefaultValue. After you create the object, this property is read-only.

Data Types: char

## DefaultValue - Default value for unspecified map locations

0 (default) | numeric scalar
Default value for unspecified map locations including areas outside the map, specified as a numeric scalar.

If you specify the GetTransformFcn or SetTransformFcn property when creating the object, the default value is updated based on that transformation function. If you create the map with a matrix of values $p$, the transform function modifies the values before storing.

## Data Types: double

## GetTransformFcn - Applies transformations to retrieved values

## function handle

Applies transformations to values retrieved by the getMapData function, specified as a function handle.

This function handle is called inside the getMapData object function. It can be used to apply a transformation to values retrieved from the map layer. The function definition must have the following format:
modifiedValues = getTransformFcnHandle(map,values,varargin)
The size of the output modifiedValues must match the size of the input values. The function provides all map data accessed from the getMapData object function to this transform function through the varargin inputs.

You can set this property when you create the object. After you create the object, this property is read-only.
Data Types: function_handle

## GridLocationInWorld - Location of the grid in local coordinates

[0 0] (default)|two-element vector|[xWorld yWorld]
Location of the bottom-left corner of the grid in world coordinates, specified as a two-element vector, [xWorld yWorld].

You can set this property when you create the object.
Data Types: double

## GridOriginInLocal - Location of the grid in local coordinates

[0 0] (default)|two-element vector|[xLocal yLocal]
Location of the bottom-left corner of the grid in local coordinates, specified as a two-element vector, [xLocal yLocal].

You can set this property when you create the object.
Data Types: double
GridSize - Number of rows and columns in grid
two-element integer-valued vector
Number of rows and columns in grid, stored as a 1-by-2 real-valued vector representing the number of rows and columns, in that order.

This property is set when you create the object based on the first two dimensions of the input matrix $p$, the inputs width and height, or the inputs row and col.
Data Types: double

## LayerName - Name of layer

'mapLayer' (default) | character vector | string scalar
Name of map layer, specified as a character vector or string scalar.

You can set this property when you create the object. After you create the object, this property is read-only.

## Data Types: double

## LocalOriginInWorld - Location of the local frame in world coordinates

[0 0] (default)|two-element vector|[xWorld yWorld]
Location of the origin of the local frame in world coordinates, specified as a two-element vector, [xLocal yLocal]. Use the move function to shift the local frame as your vehicle moves.

You can set this property when you create the object.

## Data Types: double

Resolution - Grid resolution
1 (default) | scalar
This property is read-only.
Grid resolution, stored as a scalar in cells per meter representing the number and size of grid locations.

You can set this property when you create the object. After you create the object, this property is read-only.
Data Types: double

## SetTransformFcn - Applies transformations to set values

function handle
Applies transformations to values set by the setMapData function, specified as a function handle.
This function handle is called inside the setMapData object function. It can be used to apply a transformation to values set in the map layer. The function must have the following syntax:

```
modifiedValues = setTransformFcnHandle(map,values,varargin)
    if numel(varargin) == 0
            return; %
    else
        % Custom Code
    end
end
```

The size of the output, modifiedValues, must match the size of the input, values. The function provides all map data specified in the setMapData object function to this transform function. When creating this object without starting values, the function is called without additional input arguments, so specify an if-statement to return when the number of elements in varagin is zero.

You can set this property when you create the object. After you create the object, this property is read-only.
Data Types: function_handle

## XLocalLimits - Minimum and maximum values of $x$-coordinates in local frame two-element vector

This property is read-only.

Minimum and maximum values of $x$-coordinates in local frame, stored as a two-element horizontal vector of the form [min max]. Local frame is defined by LocalOriginInWorld property.

Data Types: double
YLocalLimits - Minimum and maximum values of $\boldsymbol{y}$-coordinates in local frame two-element vector

This property is read-only.
Minimum and maximum values of $y$-coordinates in local frame, stored as a two-element horizontal vector of the form [min max]. Local frame is defined by LocalOriginInWorld property.
Data Types: double
XWorldLimits - Minimum and maximum world range values of x-coordinates
two-element vector
This property is read-only.
Minimum and maximum world range values of $x$-coordinates, stored as a 1-by-2 vector representing the minimum and maximum values, in that order.
Data Types: double
YWorldLimits - Minimum and maximum world range values of $\boldsymbol{y}$-coordinates
two-element vector
This property is read-only.
Minimum and maximum world range values of $y$-coordinates, stored as a 1-by- 2 vector representing the minimum and maximum values, in that order.
Data Types: double

## Object Functions

getMapData Retrieve data from map layer
grid2local Convert grid indices to local coordinates
grid2world Convert grid indices to world coordinates
local2grid Convert local coordinates to grid indices
local2world Convert local coordinates to world coordinates
move Move map in world frame
setMapData Assign data to map layer
syncWith Sync map with overlapping map
world2grid Convert world coordinates to grid indices
world2local Convert world coordinates to local coordinates

## Examples

## Store and Modify XY Velocities Using A Single Map Layer

Create a map layer that stores two values per grid location as $x y$-velocities.
Create an $m$-by- $n$-by-2 matrix of values. The first element in the third dimension is $\mathrm{d} x$ and the second is $d y$ as velocities.

```
dXY = reshape(1:200,10,20);
```

$d X Y(:,:, 2)=d X Y$;

Create a map layer from the matrix. Specify the resolution and layer name.

```
vLayer = mapLayer(dXY,'Resolution',1,'LayerName','dXY');
```

Get all the map data out as a matrix. Get the xy-locations of the velocity values by creating arrays that cover the minimum and maximum $x y$-world limits and is shifted to the grid-center locations. The $y$ locations are flipped when converting between matrix to world coordinates. Visualize the velocities corresponding to those grid-center locations using the quiver function.

```
v = getMapData(vLayer);
R = 1/(2*vLayer.Resolution);
xLim = vLayer.XWorldLimits;
yLim = vLayer.YWorldLimits;
xLoc = (xLim(1)+R):R*2:(xLim(2)-R);
yLoc = (yLim(2)-R):-R*2:(yLim(1)+R);
quiver(xLoc,yLoc,v(:,:,1),v(:,:,2))
```



Set the bottom-left quadrant to new updated values. Create the values as a matrix and specify the bottom-left corner $(0,0)$ in map coordinates to the setData function.

```
updateValues = repmat(reshape([-50,100],[1 1 2]),5,10);
```

setMapData(vLayer,[0 0],updateValues)
v = getMapData(vLayer);
quiver(xLoc,yLoc,v(:,:,1),v(:,: 2) )


Set new values for the top-left quadrant using grid coordinates. For maps, the top-left grid location is $(1,1)$.
setMapData(vLayer,[11],updateValues,'grid')
v = getMapData(vLayer);
quiver(xLoc, yLoc, v(:,: , 1), v(: ,: , 2) )


## Write Custom Transform Functions for Map Layers

The mapLayer object enables you to apply custom element-wise transformations when setting and getting data in the map. To transform data you set or get from the map, specify function handles for the GetTransfomFcn and SetTransformFcn properties. This example shows how to implement a log-odds probabilitistic map layer by creating a lookup table for probability and log-odds values. The transform functions use these lookup tables to convert between these values when setting or getting data.

## Create Lookup Tables

Generate a full lookup table of values that map the probability values to the minimum and maximum limits of int16 values.

Create an array of int16 values from intmin to intmax. Define the probablilty limits.

```
intType = 'int16';
intLinSpace = intmin(intType):intmax(intType);
numOfPoints = length(intLinSpace);
probLimits = [0.001 .999];
```

The exampleHelperProbToLogodds and examplerHelperLogoddsToProb functions covert between the log-odds and probability values. Use the helper functions to get the log-odds limits and
generate the array for looking up log-odds values. Create an interpolated grid for the entire lookup table.

```
logOddsLimits = exampleHelperProbToLogodds([0.001 .999]);
```

logOddsLookup = single(exampleHelperLogoddsToProb(linspace(logOddsLimits(1), log0ddsLimits(2), num
interpTable = griddedInterpolant(logOddsLookup,single(intLinSpace),'nearest');

## Specify Transform Function Handles

The transform function handles utilize example helpers that define how to convert between log-odds integer values and the probability values with an applied saturation limit. The probability saturation limits are [0.001 .999] as previously specified. This behavior is similar to the occupancyMap object.

```
getXformFcn = @(obj,logodds,varargin)...
    exampleHelperIntLogoddsToProb(logodds,log0ddsLookup(:),intLinSpace);
setXformFcn = @(obj,prob,varargin)...
    exampleHelperProbToIntLogodds(prob,interpTable,log0ddsLookup(:),intLinSpace,probLimits);
```


## Create Map Layer

Generate an occupancy map layer object from a matrix of probability values. Specify the get and set transform functions.

```
occupancyLayer = mapLayer(repmat(0.5,10,10),...
    'LayerName','Occupancy',...
    'GetTransformFcn',getXformFcn,...
    'SetTransformFcn',setXformFcn);
```

Notice that when you create the map, the default value is 0.001 instead of 0 . This difference is because the SetTransformFcn function has been applied to the default value of 0 when you create the object, which saturates the value to 0.001 .

```
disp(occupancyLayer.DefaultValue)
    0.0010
```


## Get and Set Map Data

The map data matches the matrix you set on creation.

```
extData = getMapData(occupancyLayer)
extData = 10\times10
\begin{tabular}{lllllllll}
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000
\end{tabular}
```

Set specific map locations to values that are:

- Outside of the probability saturation limits.
- Higher precision than the resolution of the lookup tables.

```
setMapData(occupancyLayer,[0 0],0.00001)
```

setMapData(occupancyLayer,[5 5],0.25999)

For the first location, the probability is bound to the saturation limits.

```
extData = getMapData(occupancyLayer,[0 0])
extData = 0.0010
```

The second location returns the value closest to the probability value in the lookup table.

```
extData2 = getMapData(occupancyLayer,[5 5])
extData2 = 0.2600
```

The generated map layer can now be used for updating a probability occupany map that are stored as int16 values. To combine this map with other layers or map types, see the multiLayerMap object.

## Limitations

- mapLayer objects can only belong to one multiLayerMap object at a time.


## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

- The LayerName property must be fixed at compile-time
- The DataType property must be known at compile-time.

As of MATLAB R2022a, default map behavior during code generation has changed, which may result in backwards compatibility issues. Maps such as mapLayer now support fixed-size code generation (DynamicMemoryAllocation="off").

1 Maps that are either default-constructed or constructed with compile-time constant size information (or matrices that are of compile-time constant size) produce fixed-size maps.
2 To restore the previous behavior, use the coder.ignoreConst function when specifying size inputs, or coder.varsize matrix variable name specified as a string scalar or character vector, prior to constructing the map.

## See Also

## Objects

multiLayerMap | occupancyMap3D | occupancyMap | binary0ccupancyMap

## Functions

getMapData| setMapData|move| syncWith

## Topics

"Motion Planning in Urban Environments Using Dynamic Occupancy Grid Map"
"Fuse Multiple Lidar Sensors Using Map Layers" Introduced in R2021a

## getMapData

Retrieve data from map layer

## Syntax

```
mapData = getMapData(map)
mapData = getMapData(map,xy)
mapData = getMapData(map,xy,'local')
mapData = getMapData(map,ij,'grid')
[mapData,inBounds] = getMapData(___)
mapData = getMapData(map,bottomLeft,mapSize)
mapData = getMapData(map,bottomLeft,mapSize,'local')
mapData = getMapData(map,topLeft,gridSize,'grid')
```


## Description

mapData $=$ getMapData(map) returns a matrix of values that contains all the data for the given map layer map.
mapData $=$ getMapData(map,xy) returns an array of values for the given $x y$-locations in world coordinates.
mapData $=$ getMapData(map, $x y$, 'local') returns an array of values for the given $x y$-locations in local coordinates.
mapData $=$ getMapData(map,ij,'grid') returns an array of values for the given $i j$-locations in grid coordinates. Each row of ij refers to a grid cell index [i j]
[mapData,inBounds] = getMapData( ___ ) also returns a vector of logical values indicating whether the corresponding input location $\overline{\mathrm{xy}}$ or ij is valid using the previous syntaxes.
mapData $=$ getMapData(map, bottomLeft, mapSize) returns a matrix of values in a subregion of the map layer, map. The subregion starts in the bottom-left xy-position bottomLeft in world coordinates with a given map size mapSize specified as [width height] in meters.
mapData $=$ getMapData(map, bottomLeft, mapSize, 'local') specifies the bottom-left corner of the subregion in local coordinates.
mapData $=$ getMapData(map,topLeft,gridSize,'grid') specifies the top-left corner of the sub region in grid coordinates. The subregion size, gridSize is also given in grid coordinates as [rows cols].

## Examples

## Store and Modify XY Velocities Using A Single Map Layer

Create a map layer that stores two values per grid location as $x y$-velocities.

Create an $m$-by- $n$-by-2 matrix of values. The first element in the third dimension is $\mathrm{d} x$ and the second is dy as velocities.

```
dXY = reshape(1:200,10,20);
dXY(:,:,2) = dXY;
```

Create a map layer from the matrix. Specify the resolution and layer name.

```
vLayer = mapLayer(dXY,'Resolution',1,'LayerName','dXY');
```

Get all the map data out as a matrix. Get the xy-locations of the velocity values by creating arrays that cover the minimum and maximum $x y$-world limits and is shifted to the grid-center locations. The $y$ locations are flipped when converting between matrix to world coordinates. Visualize the velocities corresponding to those grid-center locations using the quiver function.

```
v = getMapData(vLayer);
R = 1/(2*vLayer.Resolution);
xLim = vLayer.XWorldLimits;
yLim = vLayer.YWorldLimits;
xLoc = (xLim(1)+R):R*2:(xLim(2)-R);
yLoc = (yLim(2)-R):-R*2:(yLim(1)+R);
quiver(xLoc,yLoc,v(:,:,1),v(:,:,2))
```



Set the bottom-left quadrant to new updated values. Create the values as a matrix and specify the bottom-left corner $(0,0)$ in map coordinates to the setData function.

```
updateValues = repmat(reshape([-50,100],[[1 1 2]),5,10);
setMapData(vLayer,[0 0],updateValues)
v = getMapData(vLayer);
quiver(xLoc,yLoc,v(:,:,1),v(:,:,2))
```



Set new values for the top-left quadrant using grid coordinates. For maps, the top-left grid location is $(1,1)$.

```
setMapData(vLayer,[1 1],updateValues,'grid')
```

v = getMapData(vLayer);
quiver(xLoc,yLoc,v(:,:,1),v(:,: 2))


## Write Custom Transform Functions for Map Layers

The mapLayer object enables you to apply custom element-wise transformations when setting and getting data in the map. To transform data you set or get from the map, specify function handles for the GetTransfomFcn and SetTransformFcn properties. This example shows how to implement a log-odds probabilitistic map layer by creating a lookup table for probability and log-odds values. The transform functions use these lookup tables to convert between these values when setting or getting data.

## Create Lookup Tables

Generate a full lookup table of values that map the probability values to the minimum and maximum limits of int16 values.

Create an array of int16 values from intmin to intmax. Define the probablilty limits.

```
intType = 'int16';
intLinSpace = intmin(intType):intmax(intType);
numOfPoints = length(intLinSpace);
probLimits = [0.001 .999];
```

The exampleHelperProbToLogodds and examplerHelperLogoddsToProb functions covert between the log-odds and probability values. Use the helper functions to get the log-odds limits and
generate the array for looking up log-odds values. Create an interpolated grid for the entire lookup table.
logOddsLimits = exampleHelperProbToLogodds([0.001 .999]);
logOddsLookup = single(exampleHelperLogoddsToProb(linspace(logOddsLimits(1), logOddsLimits(2), num
interpTable = griddedInterpolant(logOddsLookup,single(intLinSpace), 'nearest');

## Specify Transform Function Handles

The transform function handles utilize example helpers that define how to convert between log-odds integer values and the probability values with an applied saturation limit. The probability saturation limits are [0.001 .999] as previously specified. This behavior is similar to the occupancyMap object.

```
getXformFcn = @(obj,logodds,varargin)...
    exampleHelperIntLogoddsToProb(logodds,log0ddsLookup(:),intLinSpace);
setXformFcn = @(obj,prob,varargin)...
    exampleHelperProbToIntLogodds(prob,interpTable,logOddsLookup(:),intLinSpace,probLimits);
```


## Create Map Layer

Generate an occupancy map layer object from a matrix of probability values. Specify the get and set transform functions.

```
occupancyLayer = mapLayer(repmat(0.5,10,10),...
    'LayerName','Occupancy',...
    'GetTransformFcn', getXformFcn,...
    'SetTransformFcn',setXformFcn);
```

Notice that when you create the map, the default value is 0.001 instead of 0 . This difference is because the SetTransformFcn function has been applied to the default value of 0 when you create the object, which saturates the value to 0.001 .

```
disp(occupancyLayer.DefaultValue)
    0.0010
```


## Get and Set Map Data

The map data matches the matrix you set on creation.

```
extData = getMapData(occupancyLayer)
extData = 10\times10
\begin{tabular}{lllllllll}
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000
\end{tabular}
```

Set specific map locations to values that are:

- Outside of the probability saturation limits.
- Higher precision than the resolution of the lookup tables.
setMapData(occupancyLayer,[0 0],0.00001)
setMapData(occupancyLayer,[5 5],0.25999)
For the first location, the probability is bound to the saturation limits.

```
extData = getMapData(occupancyLayer,[0 0])
extData = 0.0010
```

The second location returns the value closest to the probability value in the lookup table.

```
extData2 = getMapData(occupancyLayer,[5 5])
extData2 = 0.2600
```

The generated map layer can now be used for updating a probability occupany map that are stored as int16 values. To combine this map with other layers or map types, see the multiLayerMap object.

## Input Arguments

## map - Map layer

mapLayer object
Map layer, specified as a mapLayer object.

## xy - World or local coordinates

n-by-2 matrix
World or local coordinates, specified as an n-by-2 matrix of $[x y$ ] pairs, where $n$ is the number of coordinates.
Data Types: double

## ij - Grid positions

n-by-2 matrix
Grid positions, specified as an n-by-2 matrix of [ik] pairs in [rows cols] format, where $n$ is the number of grid positions.
Data Types: double

## bottomLeft - Location of output matrix in world or local coordinates

two-element vector | [xCoord yCoord]
Location of bottom left corner of output matrix in world or local coordinates, specified as a twoelement vector, [xCoord yCoord]. Location is in world or local coordinates based on syntax.
Data Types: double
mapSize - Subregion map size
two-element vector | [x y ]
Subregion map size, specified as a two-element vector $[x y$ ] in world or local coordinates.
Data Types: double

## gridSize - Output grid size

two-element vector | [ row col]
Output grid size, specified as a two-element vector [row col].
Data Types: double

## topLeft - Location of grid

two-element vector|[iCoord jCoord]
Location of top left corner of grid, specified as a two-element vector, [iCoord jCoord].
Data Types: double

## Output Arguments

mapData - Data values from map layer
matrix
Data values from map layer, returned as a matrix. By default, the function returns all data on the layer as an $M$-by- $N$-by-DataDims matrix. $M$ and $N$ are the grid rows and columns respectively. DataDims are the dimensions of the map data, map.DataSize(3:end).

For other syntaxes, the map data may be returned as an array of values with size $N$-by-DataDims or as a subregion of the full matrix.

## inBounds - Valid map locations

$n$-by-1 column vector
Valid map locations, returned as an $n$-by- 1 column vector equal in length to xy or ij . Locations inside the map limits return a value of 1 . Locations outside the map limits return a value of 0 .

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.

## See Also

## Objects

multiLayerMap |occupancyMap3D | occupancyMap | binary0ccupancyMap
Functions
setMapData|move | syncWith
Introduced in R2021a

## setMapData

Assign data to map layer

## Syntax

```
setMapData(map,mapData)
setMapData(map,xy,mapData)
setMapData(map,xy,mapData,'local')
setMapData(map,ij,mapData,'grid')
inBounds = setMapData(
```

$\qquad$

``` )
setMapData(map,bottomLeft,mapData)
setMapData(map,bottomLeft,mapData,'local')
setMapData(map,topLeft,mapData,'grid')
```


## Description

setMapData(map, mapData) overwrites all values in the map layer using a matrix with dimensions that match the map layer data dimensions, map. DataSize.
setMapData(map, xy, mapData) specifies an array of values for the given $x y$-locations in world coordinates. The mapData input must be an $X$-by-1-by-DataDims array. DataDims are the dimensions of the map data, map. DataSize (3: end). Locations outside the map boundaries are ignored.
setMapData(map, xy, mapData, 'local') specifies locations in local coordinates.
setMapData(map,ij, mapData, 'grid') specifies an array of values for the given $i j$-locations in grid coordinates. Each row of ij refers to a grid cell index [i j]
inBounds = setMapData( __ ) also returns a vector of logical values indicating whether the corresponding input location xy or ij is valid using the previous syntaxes.
setMapData(map, bottomLeft, mapData) specifies a matrix of values mapData for a subregion of the map layer, map. The subregion starts in the bottom-left $x y$-position bottomLeft and updates a subregion based on the size of mapData.
setMapData(map, bottomLeft, mapData, 'local') specifies the bottom-left corner of the subregion in local coordinates.
setMapData(map,topLeft, mapData, 'grid') specifies the top-left corner of a sub region in grid coordinates. The subregion is updated with values in mapData.

## Examples

## Store and Modify XY Velocities Using A Single Map Layer

Create a map layer that stores two values per grid location as $x y$-velocities.

Create an $m$-by- $n$-by-2 matrix of values. The first element in the third dimension is $\mathrm{d} x$ and the second is dy as velocities.

```
dXY = reshape(1:200,10,20);
dXY(:,:,2) = dXY;
```

Create a map layer from the matrix. Specify the resolution and layer name.
vLayer = mapLayer(dXY,'Resolution',1,'LayerName','dXY');
Get all the map data out as a matrix. Get the xy-locations of the velocity values by creating arrays that cover the minimum and maximum $x y$-world limits and is shifted to the grid-center locations. The $y$ locations are flipped when converting between matrix to world coordinates. Visualize the velocities corresponding to those grid-center locations using the quiver function.

```
v = getMapData(vLayer);
R = 1/(2*vLayer.Resolution);
xLim = vLayer.XWorldLimits;
yLim = vLayer.YWorldLimits;
xLoc = (xLim(1)+R):R*2:(xLim(2)-R);
yLoc = (yLim(2)-R):-R*2:(yLim(1)+R);
quiver(xLoc,yLoc,v(:,:,1),v(:,:,2))
```



Set the bottom-left quadrant to new updated values. Create the values as a matrix and specify the bottom-left corner $(0,0)$ in map coordinates to the setData function.

```
updateValues = repmat(reshape([-50,100],[[1 1 2]),5,10);
setMapData(vLayer,[0 0],updateValues)
v = getMapData(vLayer);
quiver(xLoc,yLoc,v(:,:,1),v(:,:,2))
```



Set new values for the top-left quadrant using grid coordinates. For maps, the top-left grid location is $(1,1)$.

```
setMapData(vLayer,[1 1],updateValues,'grid')
```

v = getMapData(vLayer);
quiver(xLoc,yLoc,v(:,:,1),v(:,: 2) )


## Write Custom Transform Functions for Map Layers

The mapLayer object enables you to apply custom element-wise transformations when setting and getting data in the map. To transform data you set or get from the map, specify function handles for the GetTransfomFcn and SetTransformFcn properties. This example shows how to implement a log-odds probabilitistic map layer by creating a lookup table for probability and log-odds values. The transform functions use these lookup tables to convert between these values when setting or getting data.

## Create Lookup Tables

Generate a full lookup table of values that map the probability values to the minimum and maximum limits of int16 values.

Create an array of int16 values from intmin to intmax. Define the probablilty limits.

```
intType = 'int16';
intLinSpace = intmin(intType):intmax(intType);
numOfPoints = length(intLinSpace);
probLimits = [0.001 .999];
```

The exampleHelperProbToLogodds and examplerHelperLogoddsToProb functions covert between the log-odds and probability values. Use the helper functions to get the log-odds limits and
generate the array for looking up log-odds values. Create an interpolated grid for the entire lookup table.

```
logOddsLimits = exampleHelperProbToLogodds([0.001 .999]);
```

logOddsLookup = single(exampleHelperLogoddsToProb(linspace(logOddsLimits(1), log0ddsLimits(2), num
interpTable = griddedInterpolant(logOddsLookup,single(intLinSpace), 'nearest');

## Specify Transform Function Handles

The transform function handles utilize example helpers that define how to convert between log-odds integer values and the probability values with an applied saturation limit. The probability saturation limits are [0.001 .999] as previously specified. This behavior is similar to the occupancyMap object.

```
getXformFcn = @(obj,logodds,varargin)...
    exampleHelperIntLogoddsToProb(logodds,log0ddsLookup(:),intLinSpace);
setXformFcn = @(obj,prob,varargin)...
    exampleHelperProbToIntLogodds(prob,interpTable,log0ddsLookup(:),intLinSpace,probLimits);
```


## Create Map Layer

Generate an occupancy map layer object from a matrix of probability values. Specify the get and set transform functions.

```
occupancyLayer = mapLayer(repmat(0.5,10,10),...
    'LayerName','Occupancy ', ...
    'GetTransformFcn', getXformFcn,...
    'SetTransformFcn',setXformFcn);
```

Notice that when you create the map, the default value is 0.001 instead of 0 . This difference is because the SetTransformFcn function has been applied to the default value of 0 when you create the object, which saturates the value to 0.001 .

```
disp(occupancyLayer.DefaultValue)
    0.0010
```


## Get and Set Map Data

The map data matches the matrix you set on creation.

```
extData = getMapData(occupancyLayer)
extData = 10\times10
\begin{tabular}{lllllllll}
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 \\
0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000 & 0.5000
\end{tabular}
```

Set specific map locations to values that are:

- Outside of the probability saturation limits.
- Higher precision than the resolution of the lookup tables.

```
setMapData(occupancyLayer,[0 0],0.00001)
setMapData(occupancyLayer,[5 5],0.25999)
```

For the first location, the probability is bound to the saturation limits.

```
extData = getMapData(occupancyLayer,[0 0])
extData = 0.0010
```

The second location returns the value closest to the probability value in the lookup table.

```
extData2 = getMapData(occupancyLayer,[5 5])
extData2 = 0.2600
```

The generated map layer can now be used for updating a probability occupany map that are stored as int16 values. To combine this map with other layers or map types, see the multiLayerMap object.

## Input Arguments

## map - Map layer

maLayer object
Map layer, specified as a maLayer object.

## mapData - Data values for setting map layer

matrix
Data values for setting map layer, specified as a matrix. By default, the function sets all data on the layer as an $M$-by- $N$-by-DataDims matrix. $M$ and $N$ are the grid height and width respectively. DataDims are the dimensions of the map data, map. DataSize(3,:).

For other syntaxes, the map data may be specified as a matrix with size $N$-by-DataDims, where $N$ is the number of elements in $x y$ or $i j$, or as a subregion of the full matrix.

## topLeft - Location of grid

two-element vector | [iCoord jCoord]
Location of top left corner of grid, specified as a two-element vector, [iCoord jCoord].
Data Types: double

## bottomLeft - Location of output matrix in world or local coordinates

two-element vector | [xCoord yCoord]
Location of bottom left corner of output matrix in world or local coordinates, specified as a twoelement vector, [xCoord yCoord]. Location is in world or local coordinates based on syntax.

Data Types: double

## ij - Grid positions

$n$-by-2 matrix

Grid positions, specified as an $n$-by-2 matrix of [ $i j$ ] pairs in [rows cols] format, where $n$ is the number of grid positions.
Data Types: double

## xy - World or local coordinates

$n$-by-2 matrix
World or local coordinates, specified as an $n$-by- 2 matrix of $[x y]$ pairs, where $n$ is the number of coordinates.
Data Types: double

## Output Arguments

## inBounds - Valid map locations

n-by-1 column vector
Valid map locations, returned as an $n$-by- 1 column vector equal in length to xy or ij . Locations inside the map limits return a value of 1 . Locations outside the map limits return a value of 0 .

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\mathrm{Tm}}$.

## See Also

## Objects

multiLayerMap | occupancyMap3D | occupancyMap | binary0ccupancyMap
Functions
getMapData| setMapData|move| syncWith
Introduced in R2021a

## insfilterMARG

Estimate pose from MARG and GPS data

## Description

The insfilterMARG object implements sensor fusion of MARG and GPS data to estimate pose in the NED (or ENU) reference frame. MARG (magnetic, angular rate, gravity) data is typically derived from magnetometer, gyroscope, and accelerometer sensors. The filter uses a 22 -element state vector to track the orientation quaternion, velocity, position, MARG sensor biases, and geomagnetic vector. The insfilterMARG object uses an extended Kalman filter to estimate these quantities.

## Creation

## Syntax

filter = insfilterMARG
filter = insfilterMARG('ReferenceFrame',RF)
filter = insfilterMARG( $\qquad$ ,Name, Value)

## Description

filter = insfilterMARG creates an insfilterMARG object with default property values.
filter = insfilterMARG('ReferenceFrame',RF) allows you to specify the reference frame, RF, of the filter. Specify RF as 'NED' (North-East-Down) or 'ENU' (East-North-Up). The default value is 'NED'.
filter = insfilterMARG( $\qquad$ , Name, Value) also allows you set properties of the created filter using one or more name-value pairs. Enclose each property name in single quotes.

## Properties

## IMUSampleRate - Sample rate of the IMU (Hz)

100 (default) | positive scalar
Sample rate of the inertial measurement unit (IMU) in Hz , specified as a positive scalar.
Data Types: single | double
ReferenceLocation - Reference location (deg, deg, meters)
[0 0 0] (default) | 3-element positive row vector
Reference location, specified as a 3-element row vector in geodetic coordinates (latitude, longitude, and altitude). Altitude is the height above the reference ellipsoid model, WGS84. The reference location units are [degrees degrees meters].
Data Types: single|double

GyroscopeNoise - Multiplicative process noise variance from gyroscope (rad/s) ${ }^{\mathbf{2}}$
1e-9 (default) | scalar | 3-element row vector
Multiplicative process noise variance from the gyroscope in (rad/s) ${ }^{2}$, specified as a scalar or 3element row vector of positive real finite numbers.

- If GyroscopeNoise is specified as a row vector, the elements correspond to the noise in the $x, y$, and $z$ axes of the gyroscope, respectively.
- If GyroscopeNoise is specified as a scalar, the single element is applied to the $x, y$, and $z$ axes of the gyroscope.

Data Types: single | double
GyroscopeBiasNoise - Multiplicative process noise variance from gyroscope bias (rad/s) ${ }^{\mathbf{2}}$ 1e-10 (default) | positive scalar | 3-element row vector

Multiplicative process noise variance from the gyroscope bias in (rad/s) ${ }^{2}$, specified as a scalar or 3element row vector of positive real numbers.

- If GyroscopeBiasNoise is specified as a row vector, the elements correspond to the noise in the $x, y$, and $z$ axes of the gyroscope bias, respectively.
- If GyroscopeBiasNoise is specified as a scalar, the single element is applied to each axis.

Data Types: single | double

## AccelerometerNoise - Multiplicative process noise variance from accelerometer (m/s $\mathbf{s}^{\mathbf{2}} \mathbf{2}^{\mathbf{2}}$ 1e-4 (default) | scalar | 3 -element row vector

Multiplicative process noise variance from the accelerometer in $\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}$, specified as a scalar or 3element row vector of positive real finite numbers.

- If AccelerometerNoise is specified as a row vector, the elements correspond to the noise in the $x, y$, and $z$ axes of the accelerometer, respectively.
- If AccelerometerNoise is specified as a scalar, the single element is applied to each axis.

Data Types: single | double

## AccelerometerBiasNoise - Multiplicative process noise variance from accelerometer bias $\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}$ <br> 1e-4 (default) | positive scalar | 3-element row vector

Multiplicative process noise variance from the accelerometer bias in $\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}$, specified as a scalar or 3 -element row vector of positive real numbers.

- If AccelerometerBiasNoise is specified as a row vector, the elements correspond to the noise in the $x, y$, and $z$ axes of the accelerometer bias, respectively.
- If AccelerometerBiasNoise is specified as a scalar, the single element is applied to each axis.

Data Types: single | double
GeomagneticVectorNoise - Additive process noise for geomagnetic vector ( $\boldsymbol{\mu} \mathbf{T}^{\mathbf{2}}$ )
le-6 (default) | positive scalar | 3-element row vector
Additive process noise for geomagnetic vector in $\mu \mathrm{T}^{2}$, specified as a scalar or 3-element row vector of positive real numbers.

- If GeomagneticVectorNoise is specified as a row vector, the elements correspond to the noise in the $x, y$, and $z$ axes of the geomagnetic vector, respectively.
- If GeomagneticVectorNoise is specified as a scalar, the single element is applied to each axis.


## Data Types: single | double

## MagnetometerBiasNoise - Additive process noise for magnetometer bias ( $\boldsymbol{\mu} \mathbf{T}^{\mathbf{2}}$ ) <br> 0.1 (default) | positive scalar | 3-element row vector

Additive process noise for magnetometer bias in $\mu \mathrm{T}^{2}$, specified as a scalar or 3-element row vector.

- If MagnetometerBiasNoise is specified as a row vector, the elements correspond to the noise in the $x, y$, and $z$ axes of the magnetometer bias, respectively.
- If MagnetometerBiasNoise is specified as a scalar, the single element is applied to each axis.


## Data Types: single | double

## State - State vector of extended Kalman filter

22-element column vector
State vector of the extended Kalman filter. The state values represent:

| State | Units | Index |
| :--- | :--- | :--- |
| Orientation (quaternion parts) | $\mathrm{N} / \mathrm{A}$ | $1: 4$ |
| Position (NED or ENU) | m | $5: 7$ |
| Velocity (NED or ENU) | $\mathrm{m} / \mathrm{s}$ | $8: 10$ |
| Delta Angle Bias (XYZ) | rad | $11: 13$ |
| Delta Velocity Bias (XYZ) | $\mathrm{m} / \mathrm{s}$ | $14: 16$ |
| Geomagnetic Field Vector (NED <br> or ENU) | T | $17: 19$ |
| Magnetometer Bias (XYZ) | $\mu \mathrm{T}$ | $20: 22$ |

Data Types: single | double
StateCovariance - State error covariance for extended Kalman filter
eye (22)*1e-6 (default) | 22-by-22 matrix
State error covariance for the extended Kalman filter, specified as a 22 -by-22-element matrix, or real numbers.

```
Data Types: single | double
```


## Object Functions

correct residual fusegps residualgps fusemag residualmag
pose

Correct states using direct state measurements for insfilterMARG
Residuals and residual covariances from direct state measurements for insfilterMARG Correct states using GPS data for insfilterMARG
Residuals and residual covariance from GPS measurements for insfilterMARG
Correct states using magnetometer data for insfilterMARG
Residuals and residual covariance from magnetometer measurements for insfilterMARG
Current orientation and position estimate for insfilterMARG
predict Update states using accelerometer and gyroscope data for insfilterMARG
reset stateinfo tune copy

Reset internal states for insfilterMARG
Display state vector information for insfilterMARG Tune insfilterMARG parameters to reduce estimation error Create copy of insfitlerMARG

## Examples

## Estimate Pose of UAV

This example shows how to estimate the pose of an unmanned aerial vehicle (UAV) from logged sensor data and ground truth pose.

Load the logged sensor data and ground truth pose of an UAV.
load uavshort.mat
Initialize the insfilterMARG filter object.

```
f = insfilterMARG;
f.IMUSampleRate = imuFs;
f.ReferenceLocation = refloc;
f.AccelerometerBiasNoise = 2e-4;
f.AccelerometerNoise = 2;
f.GyroscopeBiasNoise = 1e-16;
f.GyroscopeNoise = 1e-5;
f.MagnetometerBiasNoise = 1e-10;
f.GeomagneticVectorNoise = 1e-12;
f.StateCovariance = 1e-9*ones(22);
f.State = initstate;
gpsidx = 1;
N = size(accel,1);
p = zeros(N,3);
q = zeros(N,1,'quaternion');
```

Fuse accelerometer, gyroscope, magnetometer, and GPS data.

```
for ii = 1:size(accel,1) % Fuse IMU
    f.predict(accel(ii,:), gyro(ii,:));
    if ~mod(ii,fix(imuFs/2)) % Fuse magnetometer at 1/2 the IMU rate
        f.fusemag(mag(ii,:),Rmag);
    end
    if ~mod(ii,imuFs) % Fuse GPS once per second
        f.fusegps(lla(gpsidx,:),Rpos,gpsvel(gpsidx,:),Rvel);
        gpsidx = gpsidx + 1;
    end
    [p(ii,:),q(ii)] = pose(f); %Log estimated pose
end
```

Calculate and display RMS errors.

```
posErr = truePos - p;
qErr = rad2deg(dist(true0rient,q));
```

```
pRMS = sqrt(mean(posErr.^2));
qRMS = sqrt(mean(qErr.^2));
fprintf('Position RMS Error\n\tX: %.2f, Y: %.2f, Z: %.2f (meters)\n\n',pRMS(1),pRMS(2),pRMS(3));
Position RMS Error
    X: 0.57, Y: 0.53, Z: 0.68 (meters)
fprintf('Quaternion Distance RMS Error\n\t%.2f (degrees)\n\n',qRMS);
Quaternion Distance RMS Error
    0.28 (degrees)
```


## Algorithms

Note: The following algorithm only applies to an NED reference frame.
insfilterMARG uses a 22-axis extended Kalman filter structure to estimate pose in the NED reference frame. The state is defined as:

where

- $q_{0}, q_{1}, q_{2}, q_{3}-$ Parts of orientation quaternion. The orientation quaternion represents a frame rotation from the platform's current orientation to the local NED coordinate system.
- position ${ }_{\mathrm{N}}$, position $_{\mathrm{E}}$, position $_{\mathrm{D}}$-- Position of the platform in the local NED coordinate system.
- $\nu_{\mathrm{N}}, \nu_{\mathrm{E}}, \nu_{\mathrm{D}}--$ Velocity of the platform in the local NED coordinate system.
- $\Delta \theta$ bias $_{\mathrm{X}}, \Delta$ bbias $_{\mathrm{Y}}, \Delta \theta$ bias $_{\mathrm{Z}}$-- Bias in the integrated gyroscope reading.
- $\Delta \nu b i a s_{\mathrm{X}}, \Delta \nu b i a s_{\mathrm{Y}}, \Delta \nu b i a s_{\mathrm{Z}}-$ Bias in the integrated accelerometer reading.
- geomagneticFieldVector ${ }_{\mathrm{N}}$, geomagneticFieldVector ${ }_{\mathrm{E}}$, geomagneticFieldVector $\mathrm{D}_{\mathrm{D}}$-- Estimate of the geomagnetic field vector at the reference location.
- magbias $_{\mathrm{X}}$, magbias $_{\mathrm{Y}}$, magbias $_{\mathrm{Z}}$-- Bias in the magnetometer readings.

Given the conventional formation of the predicted state estimate,

$$
x_{k \mid k-1}=f\left(\widehat{x}_{k-1 \mid k-1}, u_{k}\right)
$$

$u_{\mathrm{k}}$ is controlled by accelerometer and gyroscope data that has been converted to delta velocity and delta angle through trapezoidal integration. The predicted state estimation is:

$$
\left[\begin{array}{c}
q_{0} q_{0}^{\prime}-q_{1} q_{1}^{\prime}-q_{2} q_{2}^{\prime}-q_{3} q_{3}^{\prime} \\
q_{1} q_{0}^{\prime}+q_{0} q_{1}^{\prime}-q_{3} q_{2}^{\prime}+q_{2} q_{3}^{\prime} \\
q_{2} q_{0}^{\prime}+q_{3} q_{1}^{\prime}+q_{0} q_{2}^{\prime}-q_{1} q_{3}^{\prime} \\
q_{3} q_{0}^{\prime}-q_{2} q_{1}^{\prime}+q_{1} q_{2}^{\prime}+q_{0} q_{3}^{\prime} \\
\text { position }_{\mathrm{N}}+(\Delta t)\left(\nu_{\mathrm{N}}\right) \\
\text { position }_{\mathrm{E}}+(\Delta t)\left(\nu_{\mathrm{E}}\right) \\
\text { position }_{\mathrm{D}}+(\Delta t)\left(\nu_{\mathrm{D}}\right) \\
\nu_{\mathrm{N}}+(\Delta t)\left(g_{\mathrm{N}}\right)+\left(\Delta \nu_{\mathrm{X}}-\Delta \nu \text { bias }_{\mathrm{X}}\right)\left(q_{0}^{2}+q_{1}^{2}-q_{2}^{2}-q_{3}^{2}\right)-2\left(\Delta \nu_{\mathrm{Y}}-\Delta \nu \text { bias }_{\mathrm{Y}}\right)\left(q_{0} q_{3}-q_{1} q_{2}\right)+2\left(\Delta \nu_{\mathrm{Z}}-\Delta \nu \text { bias }_{\mathrm{Z}}\right)\left(q_{0} q_{2}+\right. \\
\nu_{\mathrm{E}}+(\Delta t)\left(g_{\mathrm{E}}\right)+\left(\Delta \nu_{\mathrm{Y}}-\Delta \nu \text { bias }_{\mathrm{Y}}\right)\left(q_{0}^{2}-q_{1}^{2}+q_{2}^{2}-q_{3}^{2}\right)+2\left(\Delta \nu_{\mathrm{X}}-\Delta \nu b i a s_{\mathrm{X}}\right)\left(q_{0} q_{3}+q_{1} q_{2}\right)-2\left(\Delta \nu_{\mathrm{Z}}-\Delta \nu \text { bias }_{\mathrm{Z}}\right)\left(q_{0} q_{1}-\right. \\
\nu_{\mathrm{D}}+(\Delta t)\left(g_{\mathrm{D}}\right)+\left(\Delta \nu_{\mathrm{Z}}-\Delta \nu \text { bias }_{\mathrm{Z}}\right)\left(q_{0}^{2}-q_{1}^{2}-q_{2}^{2}+q_{3}^{2}\right)-2\left(\Delta \nu_{\mathrm{X}}-\Delta \nu b i a_{\mathrm{X}}\right)\left(q_{0} q_{2}-q_{1} q_{3}\right)+2\left(\Delta \nu_{\mathrm{Y}}-\Delta \nu b i a_{\mathrm{Y}}\right)\left(q_{0} q_{1}+\right. \\
\Delta \theta \text { bias }_{\mathrm{X}} \\
\Delta \text { bias } \\
\Delta \text { bias }_{\mathrm{Z}} \\
\Delta \nu \text { bias }_{\mathrm{X}} \\
\Delta \nu \text { bias }_{\mathrm{Y}} \\
\Delta \nu \text { bias }_{\mathrm{Z}} \\
\text { geomagneticFieldVector }
\end{array}\right.
$$

In the equation, $\left(q_{0}{ }^{\prime}, q_{1}{ }^{\prime}, q_{2}{ }^{\prime}, q_{3}^{\prime}\right)$ is the quaternion that accounts for the orientation change from one step to the next step. Assuming the orientation change is small, then the rotation vector can be approximated as ( $\Delta \theta_{\mathrm{X}}-\Delta \theta$ bias $_{\mathrm{X}}, \Delta \theta_{\mathrm{Y}}-\Delta \theta$ bias $_{\mathrm{Y}}, \Delta \theta_{\mathrm{Z}}-\Delta \theta$ bias $_{\mathrm{Z}}$ ), where $\Delta \theta_{\mathrm{X}}, \Delta \theta_{\mathrm{Y}}, \Delta \theta_{\mathrm{Z}}$ are the integrated gyroscope readings. $\left(q_{0}^{\prime}, q_{1}^{\prime}, q_{2}^{\prime}, q_{3}^{\prime}\right)$ is then obtained by converting the approximated rotation vector to a quaternion. In each calculation, the quaternion is normalized such that the length of the quaternion is 1 and its real part $q_{0}$ is nonnegative.

Additionally,

- $\Delta \nu_{\mathrm{X}}, \Delta \nu_{\mathrm{Y}}, \Delta \nu_{\mathrm{Z}}--$ Integrated accelerometer readings.
- $\Delta t$-- IMU sample time.
- $g_{\mathrm{N}}, g_{\mathrm{E}}, g_{\mathrm{D}}$-- Constant gravity vector in the NED frame.


## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

insfilterNonholonomic|insfilterErrorState|insfilterAsync
Introduced in R2018b

## correct

Correct states using direct state measurements for insfilterMARG

## Syntax

```
correct(FUSE,idx,measurement,measurementCovariance)
```


## Description

correct(FUSE,idx, measurement, measurementCovariance) corrects the state and state estimation error covariance based on the measurement and measurement covariance. The measurement maps directly to the state specified by the indices idx.

## Input Arguments

FUSE - insfilterMARG object
object
insfilterMARG, specified as an object.

## idx - State vector Index of measurement to correct

$N$-element vector of increasing integers in the range $[1,22]$
State vector index of measurement to correct, specified as an $N$-element vector of increasing integers in the range [1,22].

The state values represent:

| State | Units | Index |
| :--- | :--- | :--- |
| Orientation (quaternion parts) |  | $1: 4$ |
| Position (NED) | m | $5: 7$ |
| Velocity (NED) | $\mathrm{m} / \mathrm{s}$ | $8: 10$ |
| Delta Angle Bias (XYZ) | rad | $11: 13$ |
| Delta Velocity Bias (XYZ) | $\mathrm{m} / \mathrm{s}$ | $14: 16$ |
| Geomagnetic Field Vector (NED) | $\mu \mathrm{T}$ | $17: 19$ |
| Magnetometer Bias (XYZ) | $\mu \mathrm{T}$ | $20: 22$ |

Data Types: single | double
measurement - Direct measurement of state
$N$-element vector
Direct measurement of state, specified as a $N$-element vector. $N$ is the number of elements of the index argument, idx.
Data Types: single | double

## measurementCovariance - Covariance of measurement

scalar | $N$-element vector | $N$-by- $N$ matrix
Covariance of measurement, specified as a scalar, $N$-element vector, or $N$-by- $N$ matrix. $N$ is the number of elements of the index argument, idx.

Data Types: single | double

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® $\mathrm{Coder}^{\mathrm{TM}}$.

## See Also

insfilterMARG|insfilter

Introduced in R2018b

## copy

Create copy of insfitlerMARG

## Syntax

newFilter $=$ copy(filter)

## Description

newFilter = copy(filter) returns a copy of the insfilterMARG, filter, with the exactly same property values.

## Input Arguments

filter - Filter to be copied insfitlerMARG

Filter to be copied, specified as an insfilterMARG object.

## Output Arguments

newFilter - New copied filter
insfitlerMARG
New copied filter, returned as an insfilterMARG object.

## See Also

insfilterMARG
Introduced in R2020b

## fusegps

Correct states using GPS data for insfilterMARG

## Syntax

[res,resCov] = fusegps(FUSE,position,positionCovariance)
[res,resCov] = fusegps(FUSE,position,positionCovariance,velocity, velocityCovariance)

## Description

[res,resCov] = fusegps(FUSE,position, positionCovariance) fuses GPS position data to correct the state estimate.
[res,resCov] = fusegps(FUSE,position,positionCovariance,velocity, velocityCovariance) fuses GPS position and velocity data to correct the state estimate.

## Input Arguments

FUSE - insfilterMARG object
object
insfilterMARG, specified as an object.
position - Position of GPS receiver (LLA)
3-element row vector
Position of GPS receiver in geodetic latitude, longitude, and altitude (LLA) specified as a real finite 3element row vector. Latitude and longitude are in degrees with north and east being positive. Altitude is in meters.

## Data Types: single | double

positionCovariance - Position measurement covariance of GPS receiver ( $\mathbf{m}^{\mathbf{2}}$ )
3-by-3 matrix
Position measurement covariance of GPS receiver in $\mathrm{m}^{2}$, specified as a 3-by-3 matrix.
Data Types: single | double

## velocity - Velocity of GPS receiver in local NED coordinate system ( $\mathrm{m} / \mathrm{s}$ )

3-element row vector
Velocity of the GPS receiver in the local NED coordinate system in $\mathrm{m} / \mathrm{s}$, specified as a 3-element row vector.
Data Types: single | double
velocityCovariance - Velocity measurement covariance of GPS receiver ( $\mathrm{m} / \mathrm{s}^{\mathbf{2}}$ )
3-by-3 matrix

Velocity measurement covariance of the GPS receiver in the local NED coordinate system in $\mathrm{m} / \mathrm{s}^{2}$, specified as a 3-by-3 matrix.

Data Types: single|double

## Output Arguments

## res - Position and velocity residual

1-by-6 vector of real values
Position and velocity residual, returned as a 1-by-6 vector of real values in $m$ and $m / s$, respectively.
resCov - Residual covariance
6 -by-6 matrix of real values
Residual covariance, returned as a 6-by-6 matrix of real values.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

insfilter|insfilterMARG
Introduced in R2018b

## fusemag

Correct states using magnetometer data for insfilterMARG

## Syntax

[res,resCov] = fusemag(FUSE,magReadings,magReadingsCovariance)

## Description

[res,resCov] = fusemag(FUSE, magReadings, magReadingsCovariance) fuses magnetometer data to correct the state estimate.

## Input Arguments

FUSE - insfilterMARG object
object
insfilterMARG, specified as an object.

## magReadings - Magnetometer readings ( $\mu \mathrm{T}$ )

3-element row vector
Magnetometer readings in $\mu \mathrm{T}$, specified as a 3-element row vector of finite real numbers.
Data Types: single | double
magReadingsCovariance - Magnetometer readings error covariance ( $\boldsymbol{\mu} \mathbf{T}^{\mathbf{2}}$ )
scalar | 3-element row vector | 3-by-3 matrix
Magnetometer readings error covariance in $\mu \mathrm{T}^{2}$, specified as a scalar, 3-element row vector, or 3-by-3 matrix.
Data Types: single | double

## Output Arguments

res - Residual
1-by-3 vector of real values
Residual, returned a 1 -by- 3 vector of real values in $\mu \mathrm{T}$.
Data Types: single | double

## resCov - Residual covariance

3-by-3 matrix of real values
Residual covariance, returned a 3-by-3 matrix of real values in $(\mu \mathrm{T})^{2}$.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

insfilterMARG|insfilter
Introduced in R2018b

## pose

Current orientation and position estimate for insfilterMARG

## Syntax

[position,orientation, velocity] = pose(FUSE)
[position,orientation,velocity] = pose(FUSE,format)

## Description

[position,orientation, velocity] = pose(FUSE) returns the current estimate of the pose and velocity.
[position,orientation, velocity] = pose(FUSE, format) returns the current estimate of the pose with orientation in the specified orientation format.

## Input Arguments

## FUSE - insfilterMARG object

object
insfilterMARG, specified as an object.
format - Output orientation format
'quaternion' (default) | 'rotmat'
Output orientation format, specified as either 'quaternion' for a quaternion or 'rotmat' for a rotation matrix.

Data Types: char|string

## Output Arguments

## position - Position estimate expressed in the local coordinate system (m)

3-element row vector
Position estimate expressed in the local coordinate system of the filter in meters, returned as a 3element row vector.
Data Types: single | double
orientation - Orientation estimate expressed in the local coordinate system
quaternion (default) | 3-by-3 rotation matrix
Orientation estimate expressed in the local coordinate system of the filter, returned as a scalar quaternion or 3-by-3 rotation matrix. The quaternion or rotation matrix represents a frame rotation from the local reference frame of the filter to the body reference frame.
Data Types: single | double | quaternion
velocity - Velocity estimate expressed in local coordinate system (m/s)
3-element row vector
Velocity estimate expressed in the local coordinate system of the filter in $\mathrm{m} / \mathrm{s}$, returned as a 3 -element row vector.

Data Types: single | double

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

insfilterMARG|insfilter
Introduced in R2018b

## predict

Update states using accelerometer and gyroscope data for insfilterMARG

## Syntax

predict(FUSE, accelReadings,gyroReadings)

## Description

predict(FUSE, accelReadings,gyroReadings) fuses accelerometer and gyroscope data to update the state estimate.

## Input Arguments

FUSE - insfilterMARG object
object
insfilterMARG, specified as an object.
accelReadings - Accelerometer readings in local sensor body coordinate system (m/s ${ }^{\mathbf{2}}$ )
3-element row vector
Accelerometer readings in $\mathrm{m} / \mathrm{s}^{2}$, specified as a 3 -element row vector.
Data Types: single|double
gyroReadings - Gyroscope readings in local sensor body coordinate system (rad/s)
3-element row vector
Gyroscope readings in rad/s, specified as a 3 -element row vector.
Data Types: single|double

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

insfilterMARG|insfilter
Introduced in R2018b

## reset

Reset internal states for insfilterMARG

## Syntax

reset (FUSE)

## Description

reset (FUSE) resets the State, StateCovariance, and internal integrators to their default values.

## Input Arguments

FUSE - insfilterMARG object
object
insfilterMARG, specified as an object.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

insfilterMARG|insfilter

Introduced in R2018b

## residual

Residuals and residual covariances from direct state measurements for insfilterMARG

## Syntax

[res, resCov]= residual(FUSE,idx,measurement,measurementCovariance)

## Description

[res, resCov]= residual(FUSE,idx,measurement,measurementCovariance) computes the residual, res, and the residual covariance, resCov, based on the direct state measurement and measurement covariance. The measurement maps directly to the states specified by indices, idx.

## Input Arguments

FUSE - insfilterMARG object
object
insfilterMARG, specified as an object.

## idx - State vector index of measurement

$N$-element vector of increasing integers in the range [1,22]
State vector index of measurement, specified as an $N$-element vector of increasing integers in the range [1, 22].

The state values represent:

| State | Units | Index |
| :--- | :--- | :--- |
| Orientation (quaternion parts) |  | $1: 4$ |
| Position (NED) | m | $5: 7$ |
| Velocity (NED) | $\mathrm{m} / \mathrm{s}$ | $8: 10$ |
| Delta Angle Bias (XYZ) | rad | $11: 13$ |
| Delta Velocity Bias (XYZ) | $\mathrm{m} / \mathrm{s}$ | $14: 16$ |
| Geomagnetic Field Vector (NED) | mT | $17: 19$ |
| Magnetometer Bias (XYZ) | $\mu \mathrm{T}$ | $20: 22$ |

## measurement - Direct measurement of state

$N$-element vector
Direct measurement of state, specified as a $N$-element vector. $N$ is the number of elements of the index argument, idx.

## measurementCovariance - Covariance of measurement

$N$-by- $N$ matrix
Covariance of measurement, specified as an $N$-by- $N$ matrix. $N$ is the number of elements of the index argument, idx.

## Output Arguments

res - Measurement residual
1 -by- $N$ vector of real values
Measurement residual, returned as a 1 -by- $N$ vector of real values.
resCov - Residual covariance
$N$-by- $N$ matrix of real values
Residual covariance, returned as a $N$-by- $N$ matrix of real values.

## See Also

insfilterMARG

Introduced in R2020a

## residualgps

Residuals and residual covariance from GPS measurements for insfilterMARG

## Syntax

[res,resCov] = residualgps(FUSE,position,positionCovariance)
[res,resCov] = residualgps(FUSE,position, positionCovariance,velocity, velocityCovariance)

## Description

[res,resCov] = residualgps(FUSE, position, positionCovariance) computes the residual, res, and the residual covariance, resCov, based on the GPS position measurement and covariance.
[res,resCov] = residualgps(FUSE,position, positionCovariance, velocity, velocityCovariance) computes the residual, res, and the residual covariance, resCov, based on the GPS position measurement and covariance.

## Input Arguments

FUSE - insfilterMARG object
object
insfilterMARG, specified as an object.
position - Position of GPS receiver (LLA)
3 -element row vector
Position of GPS receiver in geodetic latitude, longitude, and altitude (LLA) specified as a real finite 3element row vector. Latitude and longitude are in degrees with north and east being positive. Altitude is in meters.

## Data Types: single | double

positionCovariance - Position measurement covariance of GPS receiver ( $\mathbf{m}^{\mathbf{2}}$ )
3-by-3 matrix
Position measurement covariance of GPS receiver in $\mathrm{m}^{2}$, specified as a 3 -by- 3 matrix.
Data Types: single | double

## velocity - Velocity of GPS receiver in local NED coordinate system (m/s)

3-element row vector
Velocity of the GPS receiver in the local NED coordinate system in $\mathrm{m} / \mathrm{s}$, specified as a 3 -element row vector.

Data Types: single | double
velocityCovariance - Velocity measurement covariance of GPS receiver ( $\mathbf{m} / \mathbf{s}^{\mathbf{2}}$ )
3-by-3 matrix

Velocity measurement covariance of the GPS receiver in the local NED coordinate system in $\mathrm{m} / \mathrm{s}^{2}$, specified as a 3-by-3 matrix.

Data Types: single | double

## Output Arguments

## res - Position and velocity residual

1 -by- 3 vector of real values | 1 -by-6 vector of real values
Position and velocity residual, returned as a 1 -by- 3 vector of real values if the inputs only contain position information, and returned as 1-by-6 vector of real values if the inputs also contain velocity information.

## resCov - Residual covariance

3-by-3 matrix of real values | 6-by-6 matrix of real values
Residual covariance, returned as a 3-by-3 matrix of real values if the inputs only contain position information, and a 6 -by- 6 matrix of real values if the inputs also contain velocity information.

## See Also

insfilter|insfilterMARG
Introduced in R2020a

## residualmag

Residuals and residual covariance from magnetometer measurements for insfilterMARG

## Syntax

[res,resCov] = residualmag(FUSE,magReadings,magReadingsCovariance)

## Description

[res,resCov] = residualmag(FUSE,magReadings,magReadingsCovariance) computes the residual, residual, and the residual covariance, resCov, based on the magnetometer readings and the corresponding covariance.

## Input Arguments

FUSE - insfilterMARG object
object
insfilterMARG, specified as an object.

## magReadings - Magnetometer readings ( $\mu \mathrm{T}$ )

3-element row vector
Magnetometer readings in $\mu \mathrm{T}$, specified as a 3 -element row vector of finite real numbers.
Data Types: single | double
magReadingsCovariance - Magnetometer readings error covariance ( $\boldsymbol{\mu} \mathbf{T}^{\mathbf{2}}$ )
scalar | 3-element row vector | 3-by-3 matrix
Magnetometer readings error covariance in $\mu \mathrm{T}^{2}$, specified as a scalar, 3-element row vector, or 3-by-3 matrix.
Data Types: single | double

## Output Arguments

## res - Residual

1-by-3 vector of real values
Residual, returned as a 1-by-3 vector of real values in $\mu \mathrm{T}$.
Data Types: single | double
resCov - Residual covariance
3-by-3 matrix of real values
Residual covariance, returned a 3-by-3 matrix of real values in $(\mu \mathrm{T})^{2}$.

## See Also

insfilterMARG|insfilter

Introduced in R2020a

## stateinfo

Display state vector information for insfilterMARG

## Syntax

stateinfo(FUSE)
info = stateinfo(FUSE)

## Description

stateinfo(FUSE) displays the meaning of each index of the State property and the associated units.
info = stateinfo(FUSE) returns a structure with fields containing descriptions of the elements of the state vector of the filter, FUSE.

## Examples

## State Information of insfilterMARG

Create an insfilterMARG object.

```
filter = insfilterMARG;
```

Display the state information of the created filter.

```
stateinfo(filter)
```

| States | Units | Index |
| :--- | :--- | :--- |
| Orientation (quaternion parts) |  | $1: 4$ |
| Position (NAV) | m | $5: 7$ |
| Velocity (NAV) | $\mathrm{m} / \mathrm{s}$ | $8: 10$ |
| Delta Angle Bias (XYZ) | rad | $11: 13$ |
| Delta Velocity Bias (XYZ) | $\mathrm{m} / \mathrm{s}$ | $14: 16$ |
| Geomagnetic Field Vector (NAV) | $\mu \mathrm{T}$ | $17: 19$ |
| Magnetometer Bias (XYZ) | $\mu \mathrm{T}$ | $20: 22$ |

Output the state information of the filter as a structure.

```
info = stateinfo(filter)
info = struct with fields:
    Orientation: [ll 2 3 4]
                        Position: [5 6 7]
                        Velocity: [8 9 10]
        DeltaAngleBias: [11 12 13]
        DeltaVelocityBias: [14 15 16]
    GeomagneticFieldVector: [lllll
        MagnetometerBias: [l20 21 22]
```


## Input Arguments

## FUSE - insfilterMARG object

object
insfilterMARG, specified as an object.
info - State information
structure
State information, returned as a structure. The field names of the structure are names of the elements of the state vector in the filter. The values of each field are the corresponding indices of the state vector.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

insfilterMARG|insfilter
Introduced in R2018b

## tune

Tune insfilterMARG parameters to reduce estimation error

## Syntax

tunedMeasureNoise = tune(filter,measureNoise,sensorData,groundTruth) tunedMeasureNoise = tune( $\qquad$ , config)

## Description

tunedMeasureNoise = tune(filter,measureNoise, sensorData, groundTruth) adjusts the properties of the insfilterMARG filter object, filter, and measurement noises to reduce the root-mean-squared (RMS) state estimation error between the fused sensor data and the ground truth. The function also returns the tuned measurement noise, tunedMeasureNoise. The function uses the property values in the filter and the measurement noise provided in the measureNoise structure as the initial estimate for the optimization algorithm.
tunedMeasureNoise = tune( $\qquad$ , config) specifies the tuning configuration based on a tunerconfig object, config.

## Examples

## Tune insfilterMARG to Optimize Pose Estimate

Load the recorded sensor data and ground truth data.
load('insfilterMARGTuneData.mat');
Create tables for the sensor data and the truth data.

```
sensorData = table(Accelerometer, Gyroscope, ...
    Magnetometer, GPSPosition, GPSVelocity);
groundTruth = table(Orientation, Position);
```

Create an insfilterMARG filter object that has a few noise properties.

```
filter = insfilterMARG('State',initialState,...
    'StateCovariance',initialStateCovariance,...
    'AccelerometerBiasNoise',1e-7,...
    'GyroscopeBiasNoise',1e-7,...
    'MagnetometerBiasNoise',1e-7,...
    'GeomagneticVectorNoise',1e-7);
```

Create a tuner configuration object for the filter. Set the maximum iterations to eight. Also, set the tunable parameters.

```
cfg = tunerconfig('insfilterMARG', 'MaxIterations', 8);
cfg.TunableParameters = setdiff(cfg.TunableParameters, ...
    {'GeomagneticFieldVector', 'AccelerometerBiasNoise', ...
    'GyroscopeBiasNoise', 'MagnetometerBiasNoise'});
```

Use the tuner noise function to obtain a set of initial sensor noises used in the filter.

```
measNoise = tunernoise('insfilterMARG')
measNoise = struct with fields:
    MagnetometerNoise: 1
        GPSPositionNoise: 1
        GPSVelocityNoise: 1
```

Tune the filter and obtain the tuned parameters.

```
tunedParams = tune(filter, measNoise, sensorData, ..
    groundTruth, cfg);
```

| Iteration | Parameter | Metric |
| :---: | :---: | :---: |
| 1 | AccelerometerNoise | 2.5701 |
| 1 | GPSPositionNoise | 2.5446 |
| 1 | GPSVelocityNoise | 2.5279 |
| 1 | GeomagneticVectorNoise | 2.5268 |
| 1 | GyroscopeNoise | 2.5268 |
| 1 | MagnetometerNoise | 2.5204 |
| 2 | AccelerometerNoise | 2.5203 |
| 2 | GPSPositionNoise | 2.4908 |
| 2 | GPSVelocityNoise | 2.4695 |
| 2 | GeomagneticVectorNoise | 2.4684 |
| 2 | GyroscopeNoise | 2.4684 |
| 2 | MagnetometerNoise | 2.4615 |
| 3 | AccelerometerNoise | 2.4615 |
| 3 | GPSPositionNoise | 2.4265 |
| 3 | GPSVelocityNoise | 2.4000 |
| 3 | GeomagneticVectorNoise | 2.3988 |
| 3 | GyroscopeNoise | 2.3988 |
| 3 | MagnetometerNoise | 2.3911 |
| 4 | AccelerometerNoise | 2.3911 |
| 4 | GPSPositionNoise | 2.3500 |
| 4 | GPSVelocityNoise | 2.3164 |
| 4 | GeomagneticVectorNoise | 2.3153 |
| 4 | GyroscopeNoise | 2.3153 |
| 4 | MagnetometerNoise | 2.3068 |
| 5 | AccelerometerNoise | 2.3068 |
| 5 | GPSPositionNoise | 2.2587 |
| 5 | GPSVelocityNoise | 2.2166 |
| 5 | GeomagneticVectorNoise | 2.2154 |
| 5 | GyroscopeNoise | 2.2154 |
| 5 | MagnetometerNoise | 2.2063 |
| 6 | AccelerometerNoise | 2.2063 |
| 6 | GPSPositionNoise | 2.1505 |
| 6 | GPSVelocityNoise | 2.0981 |
| 6 | GeomagneticVectorNoise | 2.0971 |
| 6 | GyroscopeNoise | 2.0971 |
| 6 | MagnetometerNoise | 2.0875 |
| 7 | AccelerometerNoise | 2.0874 |
| 7 | GPSPositionNoise | 2.0240 |
| 7 | GPSVelocityNoise | 1.9601 |
| 7 | GeomagneticVectorNoise | 1.9594 |
| 7 | GyroscopeNoise | 1.9594 |
| 7 | MagnetometerNoise | 1.9499 |


| 8 | AccelerometerNoise | 1.9499 |
| :--- | :--- | :--- |
| 8 | GPSPositionNoise | 1.8802 |
| 8 | GPSVelocityNoise | 1.8035 |
| 8 | GeomagneticVectorNoise | 1.8032 |
| 8 | GyroscopeNoise | 1.8032 |
| 8 | MagnetometerNoise | 1.7959 |

Fuse the sensor data using the tuned filter.

```
N = size(sensorData,1);
qEstTuned = quaternion.zeros(N,1);
posEstTuned = zeros(N,3);
for ii=1:N
    predict(filter,Accelerometer(ii,:),Gyroscope(ii,:));
    if all(~isnan(Magnetometer(ii,1)))
        fusemag(filter,Magnetometer(ii,:),...
                tunedParams.MagnetometerNoise);
    end
    if all(~isnan(GPSPosition(ii,1)))
            fusegps(filter,GPSPosition(ii,:),...
                tunedParams.GPSPositionNoise,GPSVelocity(ii,:),...
                tunedParams.GPSVelocityNoise);
    end
    [posEstTuned(ii,:),qEstTuned(ii,:)] = pose(filter);
end
```

Compute the RMS errors.

```
orientationErrorTuned = rad2deg(dist(qEstTuned,Orientation));
rmsOrientationErrorTuned = sqrt(mean(orientationErrorTuned.^2))
rmsOrientationErrorTuned = 0.8580
positionErrorTuned = sqrt(sum((posEstTuned - Position).^2,2));
rmsPositionErrorTuned = sqrt(mean(positionErrorTuned.^2))
rmsPositionErrorTuned = 1.7946
```

Visualize the results.

```
figure();
t = (0:N-1)./filter.IMUSampleRate;
subplot(2,1,1)
plot(t,positionErrorTuned,'b');
title("Tuned insfilterMARG" + newline + ...
    "Euclidean Distance Position Error")
xlabel('Time (s)');
ylabel('Position Error (meters)')
subplot(2,1,2)
plot(t, orientationErrorTuned,'b');
title("Orientation Error")
xlabel('Time (s)');
ylabel('Orientation Error (degrees)');
```

Tuned insfilterMARG



## Input Arguments

## filter - Filter object

infilterMARG object
Filter object, specified as an insfilterMARG object.

## measureNoise - Measurement noise

structure
Measurement noise, specified as a structure. The function uses the measurement noise input as the initial guess for tuning the measurement noise. The structure must contain these fields:

| Field name | Description |
| :--- | :--- |
| MagnetometerNoise | Variance of magnetometer noise, specified as a <br> scalar in $(\mu \mathrm{T})^{2}$ |
| GPSPositionNoise | Variance of GPS position noise, specified as a <br> scalar in $\mathrm{m}^{2}$ |
| GPSVelocityNoise | Variance of GPS velocity noise, specified as a <br> scalar in $(\mathrm{m} / \mathrm{s})^{2}$ |

[^2]Sensor data, specified as a table. In each row, the sensor data is specified as:

- Accelerometer - Accelerometer data, specified as a 1-by-3 vector of scalars in $\mathrm{m}^{2} / \mathrm{s}$.
- Gyroscope - Gyroscope data, specified as a 1-by-3 vector of scalars in rad/s.
- Magnetometer - Magnetometer data, specified as a 1-by-3 vector of scalars in $\mu \mathrm{T}$.
- GPSPosition - GPS position data, specified as a 1-by-3 vector of scalars in [degrees, degrees, meters].
- GPSVelocity - GPS velocity data, specified as a 1-by-3 vector of scalars in m/s.

If the GPS sensor does not produce complete measurements, specify the corresponding entry for GPSPosition and/or GPSVelocity as NaN. If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the sensorData input based on your choice.

## groundTruth - Ground truth data <br> table

Ground truth data, specified as a table. In each row, the table can optionally contain any of these variables:

- Orientation - Orientation from the navigation frame to the body frame, specified as a quaternion or a 3-by-3 rotation matrix.
- Position - Position in navigation frame, specified as a 1 -by- 3 vector of scalars in meters.
- Velocity - Velocity in navigation frame, specified as a 1-by-3 vector of scalars in $\mathrm{m} / \mathrm{s}$.
- DeltaAngleBias - Delta angle bias, specified as a 1-by-3 vector of scalars in radians.
- DeltaVelocityBias - Delta velocity bias, specified as a 1-by-3 vector of scalars in m/s.
- GeomagneticFieldVector - Geomagnetic field vector in navigation frame, specified as a 1-by-3 vector of scalars.
- MagnetometerBias - Magnetometer bias in body frame, specified as a 1-by-3 vector of scalars in $\mu \mathrm{T}$.

The function processes each row of the sensorData and groundTruth tables sequentially to calculate the state estimate and RMS error from the ground truth. State variables not present in groundTruth input are ignored for the comparison. The sensorData and the groundTruth tables must have the same number of rows.

If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the groundTruth input based on your choice.

## config - Tuner configuration

tunerconfig object
Tuner configuration, specified as a tunerconfig object.

## Output Arguments

tunedMeasureNoise - Tuned measurement noise
structure
Tuned measurement noise, returned as a structure. The structure contains these fields.

| Field name | Description |
| :--- | :--- |
| MagnetometerNoise | Variance of magnetometer noise, specified as a <br> scalar in $(\mu \mathrm{T})^{2}$ |
| GPSPositionNoise | Variance of GPS position noise, specified as a <br> scalar in $\mathrm{m}^{2}$ |
| GPSVelocityNoise | Variance of GPS velocity noise, specified as a <br> scalar in $(\mathrm{m} / \mathrm{s})^{2}$ |

## References

[1] Abbeel, P., Coates, A., Montemerlo, M., Ng, A.Y. and Thrun, S. Discriminative Training of Kalman Filters. In Robotics: Science and systems, Vol. 2, pp. 1, 2005.

## See Also

tunerconfig|tunernoise
Introduced in R2021a

## gnssSensor

Simulate GNSS to generate position and velocity readings

## Description

The gnssSensor System object simulates a global navigation satellite system (GNSS) to generate position and velocity readings based on local position and velocity data. The object calculates satellite positions and velocities based on the sensor time and data that specifies the satellite orbital parameters on page 2-622. The object uses only the Global Positioning System (GPS) constellations for calculations. To set the starting positions of the satellites, set the InitialTime property.

To generate GNSS position and velocity readings:
1 Create the gnssSensor object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?
Calling the object increments the time of the sensor and propagates the satellite position and velocities based on the orbital parameters.

## Creation

## Syntax

```
GNSS = gnssSensor
GNSS = gnssSensor('ReferenceFrame',frame)
GNSS = gnssSensor(___,Name,Value)
```


## Description

GNSS = gnssSensor returns a gnssSensor System object GNSS that computes global navigation satellite system receiver readings based on local position and velocity input.

GNSS = gnssSensor('ReferenceFrame', frame) specifies the reference frame in which the GNSS readings are reported. Specify frame as 'NED' (north-east-down) or 'ENU ' (east-north-up). The default value is 'NED '.

GNSS = gnssSensor (__ , Name, Value) sets properties using one or more name-value pairs. For example, gnssSensor('SampleRate', 2) creates a simulated GNSS with a sample rate of 2 Hz . Enclose each property name in quotes.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

## SampleRate - Sample rate of GNSS receiver (Hz)

1 (default) | positive scalar
Sample rate of the GNSS receiver, specified as a positive scalar in Hz .

## Data Types: single | double

## InitialTime - Initial time of GNSS receiver

datetime('now','TimeZone','UTC') (default)|datetime object
Initial time of the GNSS receiver, specified as a datetime object. The object accounts for leap seconds in the conversion between the UTC and the GNSS time.

## ReferenceLocation - Origin of local navigation reference frame

[0 0 0] (default) | three-element row vector of scalars
Origin of the local navigation reference frame, specified as a three-element row vector of scalars in geodetic coordinates (latitude in degrees, longitude in degrees, and altitude in meters). Altitude is the height above the reference ellipsoid model WGS84.

## Data Types: single | double

## MaskAngle - Elevation mask angle (deg)

10 (default) | scalar in [0, 90]
Elevation mask angle, specified as a scalar in the range of [0, 90] in degrees. Satellites in view but below the mask angle are not used in estimating the position of the receiver.

Tunable: Yes
Data Types: single | double

## RangeAccuracy - Standard deviation of measurement noise of pseudorange (m)

1 (default) | nonnegative scalar
Standard deviation of the measurement noise of pseudorange, specified as a nonnegative scalar in meters.

Tunable: Yes
Data Types: single | double
RangeRateAccuracy - Standard deviation of measurement noise of pseudorange rate ( $\mathrm{m} / \mathrm{s}$ ) 0.02 (default) | nonnegative scalar

Standard deviation of the measurement noise of pseudorange rate, specified as a nonnegative scalar in meters per second.

Tunable: Yes
Data Types: single | double

## RandomStream - Random number source

'Global stream' (default)|'mt19937ar with seed'

Random number source, specified as one of these options::

- 'Global stream' -- Random numbers are generated using the current global random number stream.
- 'mt19937ar with seed' -- Random numbers are generated using the mt19937ar algorithm with the seed specified by the Seed property.

Data Types: char|string

## Seed - Initial seed of mt19937ar random number generator algorithm

67 (default) | nonnegative integer
Initial seed of an mt19937ar random number generator algorithm, specified as a nonnegative integer.

## Dependencies

To enable this property, set RandomStream to 'mt19937ar with seed'.
Data Types: integer

## Usage

## Syntax

[positionReadings,velocityReadings,status] = GNSS(position,velocity)

## Description

[positionReadings, velocityReadings,status] = GNSS(position, velocity) computes global navigation satellite system receiver readings from the position and velocity inputs.

## Input Arguments

## position - Cartesian position of GNSS receiver in local navigation coordinate system (m)

$N$-by-3 matrix of scalar
Cartesian position of the GNSS receiver in the local navigation coordinate system, specified as an $N$ -by-3 matrix of scalars in meters. $N$ is the number of samples.

The default reference frame is NED (north-east-down). For ENU (east-north-up), set the ReferenceFrame name-value argument to 'ENU' on creation.

## Data Types: single | double

## velocity - Velocity of GNSS receiver in local navigation coordinate system (m/s)

N -by-3 matrix of scalars
Velocity of the GNSS receiver in the local navigation coordinate system, specified as an $N$-by- 3 matrix in meters per second. $N$ is the number of samples.

## Data Types: single | double

The default reference frame is NED (north-east-down). For ENU (east-north-up), set the ReferenceFrame name-value argument to 'ENU' on creation.

## Output Arguments

## positionReadings - Position readings in LLA coordinate system

$N$-by-3 matrix of scalar
Position readings of the GNSS receiver in the geodetic latitude, longitude, and altitude (LLA) coordinate system, returned as an $N$-by- 3 matrix of scalars. Altitude is the height above the reference ellipsoid model, WGS84. $N$ is the number of samples in the input argument. Latitude and longitude are in degrees. Altitude is in meters.
Data Types: single|double
velocityReadings - Velocity readings in local navigation coordinate system (m/s)
$N$-by-3 matrix of scalar
Velocity reading of the GNSS receiver in the local navigation coordinate system in meters per second, returned as an $N$-by- 3 matrix of scalars. $N$ is the number of samples in the input arguments.
Data Types: single|double
status - Status information of visible satellites
$N$-element array of structure
Status information of visible satellites, returned as an $N$-element array of structures. $N$ is the number of samples in the input arguments. Each structure contains these four fields:

| Field Name | Description |
| :--- | :--- |
| SatelliteAzimuth | Azimuth angles of visible satellites, returned as <br> an $M$-element vector of scalars in degrees. $M$ is <br> the number of visible satellites. |
| SatelliteElevation | Elevation angles of visible satellites, returned as <br> an $M$-element vector of scalars in degrees. $M$ is <br> the number of visible satellites. |
| HDOP | Horizontal dilution of precision, returned as a <br> scalar. |
| VDOP | Vertical dilution of precision, returned as a scalar. |

To plot the satellite positions, see the skyplot function.

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Common to All System Objects

clone Create duplicate System object
step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object
isDone End-of-data status

## Examples

## Generate GNSS Position and Velocity Readings

Generate target positions and velocities based on a waypoint trajectory.

```
rng(2020) % For repeatable results
fs = 0.1;
tArrival = 50;
tspan = 0:1/fs:tArrival;
% Create a waypoint trajectory.
trajectory = waypointTrajectory([0,0,0;1,1,1]*500,[0,tArrival]);
[positions,~,velocities] = lookupPose(trajectory,tspan)
positions = 6\times3
\begin{tabular}{rrr}
0 & 0 & 0 \\
100.0000 & 100.0000 & 100.0000 \\
200.0000 & 200.0000 & 200.0000 \\
300.0000 & 300.0000 & 300.0000 \\
400.0000 & 400.0000 & 400.0000 \\
500.0000 & 500.0000 & 500.0000
\end{tabular}
velocities = 6×3
\begin{tabular}{lll}
10.0000 & 10.0000 & 10.0000 \\
10.0000 & 10.0000 & 10.0000 \\
10.0000 & 10.0000 & 10.0000 \\
10.0000 & 10.0000 & 10.0000 \\
10.0000 & 10.0000 & 10.0000 \\
10.0000 & 10.0000 & 10.0000
\end{tabular}
```

Create a GNSS System object. Use the LLA position for Natick, MA as the local reference frame origin of the trajectory.

```
refLocNatick = [42.2825 -71.343 53.0352];
gnss = gnssSensor('SampleRate',fs, ...
    'ReferenceLocation',refLocNatick);
```

Generate position and velocity readings based on the GNSS object.
[llaReadings,velocityReadings,status] = gnss(positions,velocities)
llaReadings $=6 \times 3$

| 42.2825 | -71.3430 | 52.1304 |
| :--- | ---: | ---: |
| 42.2834 | -71.3418 | -42.9722 |
| 42.2843 | -71.3406 | -146.0978 |
| 42.2852 | -71.3394 | -246.4849 |
| 42.2861 | -71.3381 | -346.8723 |
| 42.2870 | -71.3369 | -446.1944 |

```
velocityReadings = 6×3
    10.0156 9.9953 9.9376
    9.9948 9.9788 9.9871
    9.9936 9.9871 10.0038
    9.9963 9.9968 9.9963
    10.0173 9.9931 9.9755
    9.9923 9.9892 10.0077
status=6\times1 struct array with fields:
    SatelliteAzimuth
    SatelliteElevation
    HDOP
    VDOP
```


## More About

## Orbital Parameters

The satellite positions and velocities are defined by orbital parameters from IS-GPS-200K Interface Specification, and are given in the Earth-Centered Earth-Fixed (ECEF) coordinates.

Position calculations use equations from Table 30-II in the same IS-GPS-200K Interface Specification.
Velocity calculations use equations 8.21-8.27 in Principles of GNSS, Inertial, and Multisensor Integrated Navigation Systems[1].

## References

[1] Groves, Paul D. Principles of GNSS, Inertial, and Multisensor Integrated Navigation Systems. 2nd ed, Artech House, 2013.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

## Objects

gpsSensor|imuSensor

## Functions

skyplot | gnssconstellation|lookangles|pseudoranges|receiverposition

## Introduced in R2020b

## mobileRobotPropagator

State propagator for wheeled robotic systems

## Description

The mobileRobotPropagator object is a state propagator that propagates and validates the state of a mobile robot based on control commands, durations, and target states. The object supports different kinematic models, integrator types, and control policies.

## Creation

## Syntax

```
mobileProp = mobileRobotPropagator
mobileProp = mobileRobotPropagator(Name,Value)
```


## Description

mobileProp $=$ mobileRobotPropagator creates a mobile robot propagator for a bicycle kinematic model using a linear-pursuit control policy.
mobileProp = mobileRobotPropagator(Name,Value) specifies properties using name-value arguments. For example, mobileRobotPropagator("ControlStepSize"=0.01) creates a mobile robot propagator with a control step size of 0.01 .

## Properties

## StateSpace - State space for sampling during planning <br> stateSpaceSE2 object (default) | object of subclass of nav. StateSpace object

State space for sampling during planning, specified as an object of a subclass of nav.StateSpace object.

The state space is responsible for representing the configuration space of a system. The object should include all state information related to the propagated system. Systems employing multi-layer cascade controllers can append persistent low-level control information directly to the state vector, whereas the state propagator directly manages top-level control commands.

## Environment - Environment for validating states

[] (default) | binary0ccupancyMap object | occupancyMap object | vehicleCostmap object
Environment for validating states, specified as a binary0ccupancyMap, occupancyMap, or vehicleCostmap object.

The mobileRobotPropagator object validates discrete states along the propagated motion. By default, the environment is empty, so the object only rejects states outside the state space bounds.

This property can only be set during construction.

## DistanceEstimator - Distance metric for estimating propagation cost <br> 'euclidean' (default)|'dubins'|'reedsshepp'

Distance metric for estimating propagation cost, specified as one of these options:

- 'euclidean' - Standard Euclidean distance.
- 'dubins ' - Distance along a Dubins path that connects the two states. For more information, see dubinsPathSegment.
- 'reedsshepp ' - Distance along a Reeds Shepp path that connects the two states. For more information, see reedsSheppPathSegment.

This property can only be set during construction.

## GoalDistance - Threshold of distance for reaching goal states

1 (default) | positive scalar
Threshold of distance for reaching goal states, specified as a positive scalar. When propagating states, a state is considered equal to the goal state when it is closer than this distance threshold.

This property can only be set during construction.

## KinematicModel - Kinematic model for propagating state

'bicycle' (default)|'ackermann'
Kinematic model for propagating the state, which determines the state variables, size of the control inputs, and other system parameters that you can specify in the SystemParameters property.

Kinematic Model States and Controls

| Type | State Vector | Control input |
| :--- | :--- | :--- |
| 'bicycle' | $[x$ y theta $]$ | $[v$ psi] |
| 'ackermann' | $[x$ y theta psi] | $[v$ psiDot $]$ |

This property can only be set during construction and selecting the Ackermann kinematic model requires the Robotics System Toolbox ${ }^{\mathrm{TM}}$.

## Integrator - Integration method when propagating state <br> 'rungekutta4' (default) | 'euler'

Integration method when propagating state. Integration step size can be updated through the SystemParameters property.
'rungekutta4' provides a more accurate integration result than 'euler' at the cost of speed.
This property can only be set during construction.

## SystemParameters - Parameters for kinematic model, integrator, and control policy structure

Parameters for the kinematic model, integrator, and control policy, specified as a structure with these fields:

- KinematicModel - Parameters for the kinematic model type specified in the KinematicModel property.
- WheelBase - Size of wheel base in meters
- SpeedLimit - Velocity in the forward and backward directions in meters per second.
- SteerRatelimit - Limits on steering rate in radians per second
- Integrator - Parameters for the integrator type specified in the Integrator property.
- ControlPolicy - Parameters for the control policy specified in the ControlPolicy property.


## Control Parameters

## ControlPolicy - Control command generation policy

'linearpursuit' (default)|'arcpursuit' | 'randomsamples'
Control command generation policy, specified as one of these options:

- 'linearpursuit' - Samples a random velocity and calculates a lookahead point along the vector that connects the initial state to the target state.
- 'arcpursuit' - Samples a random velocity and calculates a lookahead point along an arc that is tangential to the target state and intersects the initial $x y$-position.
- 'randomsamples ' - Draws a finite set of random control samples from the control space and propagates to each. The propagator selects the sample that gets the closest to the goal and then performs a validation.


## ControlLimits - Limits on control commands for each state

[-1 1; -pi/4 pi/4] (default)|n-by-2 matrix
Limits on control commands for each state, specified as an $n$-by- 2 matrix. $n$ is the number of control inputs for your system model.

## NumControlOutput - Number of control outputs

2 (default) | positive scalar
This property is read-only.
Number of control outputs, specified as a nonnegative scalar.

## ControlStepSize - Duration of each control command

0.1 (default) | positive scalar

Duration of each control command, specified as a positive scalar.

## MaxControlSteps - Maximum number of control steps

10 (default) | positive integer
Maximum number of times to propagate the system specified as positive integer.

## Object Functions

| distance | Estimate cost of propagating to target state |
| :--- | :--- |
| propagate | Propagate system without validation |
| propagateWhileValid | Propagate system and return valid motion |
| sampleControl | Generate control command and duration |
| setup | Set up the mobile robot state propagator |

## Examples

## Plan Kinodynamic Path with Controls for Mobile Robot

Plan control paths for a bicycle kinematic model with the mobileRobotPropagator object. Specify a map for the environment, set state bounds, and define a start and goal location. Plan a path using the control-based RRT algorithm, which uses a state propagator for planning motion and the required control commands.

## Set State and State Propagator Parameters

Load a ternary map matrix and create an occupancyMap object. Create the state propagator using the map. By default, the state propagator uses a bicycle kinematic model.

```
load('exampleMaps','ternaryMap')
map = occupancyMap(ternaryMap,10);
propagator = mobileRobotPropagator(Environment=map); % Bicycle model
```

Set the state bounds on the state space based on the map world limits.

```
propagator.StateSpace.StateBounds(1:2,:) = ...
    [map.XWorldLimits; map.YWorldLimits];
```


## Plan Path

Create the path planner from the state propagator.

```
planner = plannerControlRRT(propagator);
```

Specify the start and goal states.

```
start = [10 15 0];
goal = [40 30 0];
```

Plan a path between the states. For repeatable results, reset the random number generator before planning. The plan function outputs a navPathControl object, which contains the states, control commands, and durations.

```
rng("default")
path = plan(planner,start,goal)
path =
    navPathControl with properties:
        StatePropagator: [1\times1 mobileRobotPropagator]
                States: [192x3 double]
            Controls: [191x2 double]
            Durations: [191x1 double]
            TargetStates: [191x3 double]
                NumStates: 192
            NumSegments: }19
```


## Visualize Results

Visualize the map and plot the path states.

```
show(map)
hold on
plot(start(1),start(2),"rx")
plot(goal(1),goal(2),"go")
plot(path.States(:,1),path.States(:,2),"b")
hold off
```



Display the [v psi] control inputs of forward velocity and steering angle.
plot(path.Controls)
ylim([-1 1])
legend(["Velocity (m/s)","Steering Angle (rad)"])


## See Also

## Classes

nav.StateSpace
Objects
stateSpaceSE2|stateSpaceDubins|stateSpaceReedsShepp

## Functions

distance | propagate | propagateWhileValid| sampleControl| setup

Introduced in R2021b

## distance

Estimate cost of propagating to target state

## Syntax

h = distance(mobileProp,q1,q2)

## Description

h = distance(mobileProp, q1, q2) estimates the cost of propagating from one state to another. The DistanceEstimator property of the state propagator defines the distance metric for approximating cost.

## Input Arguments

mobileProp - Mobile robot state propagator
mobileRobotPropagator object
Mobile robot state propagator, specified as a mobileRobotPropagator object.

## q1 - Initial states

$n$-by-s matrix
Initial states, specified as an $n$-by-s matrix. $n$ is the number of states and $s$ is the size of the state vector.
q2 - Final states
$n$-by-s matrix
Final states, specified as an $n$-by-s matrix. $n$ is the number of states and $s$ is the size of the state vector.

## Output Arguments

$h$ - Cost values
n-element vector
Cost values, returned as an $n$-element vector. $n$ is the number of $q 1$ and $q 2$ pairs.
You can use the cost values returned by this function to find the nearest neighbor for sampled target states when planning a path.

## See Also

## Objects

mobileRobotPropagator
Functions
propagate|propagateWhileValid| sampleControl|setup

Introduced in R2021b

## propagate

Propagate system without validation

## Syntax

[q,u,steps] = propagate(mobileProp,q0,u0,qTgt,maxSteps)

## Description

[q,u,steps] = propagate(mobileProp,q0,u0,qTgt,maxSteps) iteratively propagates the system from the current state $q 0$ towards a target state $q$ Tgt with an initial control input $u 0$ for a maximum number of steps maxSteps.

At the end of each propagation step i, the system returns these values:

- $q(i,:)$ - Current state of the system
- $u(i,:)-$ Control input for step $i+1$
- steps(i) - Number of steps between i - 1 and i


## Input Arguments

mobileProp - Mobile robot state propagator
mobileRobotPropagator object
Mobile robot state propagator, specified as a mobileRobotPropagator object.

## q0 - Initial state

$s$-element vector
Initial state of the system, specified as an $s$-element vector. $s$ is the number of state variables in the state space.

## u0 - Initial control on initial state

c-element vector
Initial control on the initial state, specified as an $c$-element vector. $c$ is the number of control inputs.

## qTgt - Target state

$s$-element vector
Target state of the system, specified as an $s$-element vector. $s$ is the number of state variables in the state space.
maxSteps - Maximum number of steps
positive scalar
Maximum number of steps, specified as a positive scalar.

## Output Arguments

q - Propagated states
$n$-by-s matrix
Propagated states of the system, returned as an $s$-element vector. $s$ is the number of state variables in the state space.
u - Control inputs for propagating states
$n$-by-c matrix
Control inputs for propagating states, returned as an $n$-by- $c$ matrix. $c$ is the number of control inputs
steps - Number of steps between each state and control input to next
$n$-element vector of positive integers
Number of steps from each state and control input to next, returned as an $n$-element vector of positive integers.

## See Also

Objects
mobileRobotPropagator
Functions
distance | propagateWhileValid| sampleControl|setup

Introduced in R2021b

## propagateWhileValid

Propagate system and return valid motion

## Syntax

[q,u,steps] = propagate(mobileProp,q0,u0,qTgt,maxSteps)

## Description

[q,u,steps] = propagate(mobileProp,q0,u0,qTgt,maxSteps) iteratively propagates the system from the current state $q 0$ towards a target state $q T g t$ with an initial control input $u 0$ for a maximum number of steps maxSteps.

At the end of each propagation step $i$, the system returns these values:

- $q(i,:)$ - Current state of the system
- u(i,:) - Control input for step i + 1
- steps(i) - Number of steps between i - 1 and i

The function validates all propagations and returns system information between q 0 and the last valid state.

## Input Arguments

mobileProp - Mobile robot state propagator
mobileRobotPropagator object
Mobile robot state propagator, specified as a mobileRobotPropagator object.
q0 - Initial state
$s$-element vector
Initial state of the system, specified as an $s$-element vector. $s$ is the number of state variables in the state space.

## u0 - Initial control on initial state

$c$-element vector
Initial control on the initial state, specified as an $c$-element vector. $c$ is the number of control inputs.

## qTgt - Target state

$s$-element vector
Target state of the system, specified as an $s$-element vector. $s$ is the number of state variables in the state space.
maxSteps - Maximum number of steps
positive scalar
Maximum number of steps, specified as a positive scalar.

## Output Arguments

q - Propagated states
$n$-by-s matrix
Propagated states of the system, returned as an $s$-element vector. $s$ is the number of state variables in the state space.
u - Control inputs for propagating states
$n$-by-c matrix
Control inputs for propagating states, returned as an $n$-by- $c$ matrix. $c$ is the number of control inputs
steps - Number of steps from each state and control input to next
$n$-element vector of positive integers
Number of steps from each state and control input to next, returned as an $n$-element vector of positive integers.

## See Also

Objects
mobileRobotPropagator
Functions
distance | propagate | sampleControl| setup
Introduced in R2021b

## sampleControl

Generate control command and duration

## Syntax

[u,steps] = sampleControl(mobileProp,q0,u0,qTgt)

## Description

[u,steps] = sampleControl(mobileProp,q0,u0,qTgt) generates a series of control commands and number of steps to move from the current state $q 0$ with control command $u 0$ toward the target state qTgt.

## Input Arguments

mobileProp - Mobile robot state propagator
mobileRobotPropagator object
Mobile robot state propagator, specified as a mobileRobotPropagator object.
q0 - Initial state
$s$-element vector
Initial state of the system, specified as an $s$-element vector. $s$ is the number of state variables in the state space.
u0 - Initial control on the initial state
$c$-element vector
Initial control input, specified as an $c$-element vector. $c$ is the number of control inputs.

## qTgt - Target state

$s$-element vector
Target state of the system, specified as an $s$-element vector. $s$ is the number of state variables in the state space.

## Output Arguments

## u - Control inputs for propagating states

$n$-by-c matrix
Control inputs for propagating states, returned as an $c$-element vector. $c$ is the number of control inputs.

## steps - Number of steps from each state and control input to next <br> $n$-element vector of positive integers

Number of steps from each state and control input to next, returned as an $n$-element vector of positive integers.

## See Also

## Objects

mobileRobotPropagator
Functions
distance | propagate | propagateWhileValid| setup

Introduced in R2021b

## setup

Set up the mobile robot state propagator

## Syntax

```
setup(mobileProp)
```


## Description

setup(mobileProp) sets up the mobileRobotPropagator object based on the properties of the object. If you change the properties of the object, use this object function before you use the object to sample controls, propagate the system, or calculate distances.

Note Override this function to implement custom functionality to run in the setup.

## Input Arguments

mobileProp - Mobile robot state propagator
mobileRobotPropagator object
Mobile robot state propagator, specified as a mobileRobotPropagator object.

## See Also

## Objects

mobileRobotPropagator

## Functions

distance | propagate | propagateWhileValid | sampleControl
Introduced in R2021b

## monteCarloLocalization

Localize robot using range sensor data and map

## Description

The monteCarloLocalization System object creates a Monte Carlo localization (MCL) object. The MCL algorithm is used to estimate the position and orientation of a vehicle in its environment using a known map of the environment, lidar scan data, and odometry sensor data.

To localize the vehicle, the MCL algorithm uses a particle filter to estimate the vehicle's position. The particles represent the distribution of likely states for the vehicle, where each particle represents a possible vehicle state. The particles converge around a single location as the vehicle moves in the environment and senses different parts of the environment using a range sensor. An odometry sensor measures the vehicle's motion.

A monteCarloLocalization object takes the pose and lidar scan data as inputs. The input lidar scan sensor data is given in its own coordinate frame, and the algorithm transforms the data according to the SensorModel. SensorPose property that you must specify. The input pose is computed by integrating the odometry sensor data over time. If the change in pose is greater than any of the specified update thresholds, UpdateThresholds, then the particles are updated and the algorithm computes a new state estimate from the particle filter. The particles are updated using this process:

1 The particles are propagated based on the change in the pose and the specified motion model, MotionModel.
2 The particles are assigned weights based on the likelihood of receiving the range sensor reading for each particle. These likelihood weights are based on the sensor model you specify in SensorModel.
3 Based on the ResamplingInterval property, the particles are resampled from the posterior distribution, and the particles of low weight are eliminated. For example, a resampling interval of 2 means that the particles are resampled after every other update.

The outputs of the object are the estimated pose and covariance, and the value of isUpdated. This estimated state is the mean and covariance of the highest weighted cluster of particles. The output pose is given in the map's coordinate frame that is specified in the SensorModel. Map property. If the change in pose is greater than any of the update thresholds, then the state estimate has been updated and isUpdated is true. Otherwise, isUpdated is false and the estimate remains the same. For continuous tracking the best estimate of a robot's state, repeat this process of propagating particles, evaluating their likelihood, and resampling.

To estimate robot pose and covariance using lidar scan data:
1 Create the monteCarloLocalization object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

```
mcl = monteCarloLocalization
mcl = monteCarloLocalization(Name,Value)
Description
```

$\mathrm{mcl}=$ monteCarloLocalization returns an MCL object that estimates the pose of a vehicle using a map, a range sensor, and odometry data. By default, an empty map is assigned, so a valid map assignment is required before using the object.
$\mathrm{mcl}=$ monteCarloLocalization(Name, Value) creates an MCL object with additional options specified by one or more Name, Value pair arguments.

Name is a property name and Value is the corresponding value. Name must appear inside single quotes (' ' ). You can specify several name-value pair arguments in any order as
Name1, Value1, . . . , NameN, ValueN.

## Properties

## InitialPose - Initial pose of vehicle

[0 0000 (default) | three-element vector
Initial pose of the vehicle used to start localization, specified as a three-element vector, $[x y$ theta], that indicates the position and heading of the vehicle. Initializing the MCL object with an initial pose estimate enables you to use a smaller value for the maximum number of particles and still converge on a location.

## InitialCovariance - Covariance of initial pose

diag([1 1 1 1]) (default)| diagonal matrix | three-element vector | scalar
Covariance of the Gaussian distribution for the initial pose, specified as a diagonal matrix. Threeelement vector and scalar inputs are converted to a diagonal matrix. This matrix gives an estimate of the uncertainty of the InitialPose.

## GlobalLocalization - Flag to start global localization <br> false (default)| true

Flag indicating whether to perform global localization, specified as false or true. The default value, false, initializes particles using the InitialPose and InitialCovariance properties. A true value initializes uniformly distributed particles in the entire map and ignores the InitialPose and InitialCovariance properties. Global localization requires a large number of particles to cover the entire workspace. Use global localization only when the initial estimate of vehicle location and orientation is not available.

## ParticleLimits - Minimum and maximum number of particles

[500 5000] (default) | two-element vector
Minimum and maximum number of particles, specified as a two-element vector, [min max].

## SensorModel - Likelihood field sensor model

## likelihoodFieldSensor object

Likelihood field sensor model, specified as a likelihoodFieldSensor object. The default value uses the default likelihoodFieldSensorModel object. After using the object to get output, call release on the object to make changes to SensorModel. For example:

```
mcl = monteCarloLocalization;
[isUpdated,pose,covariance] = mcl(ranges,angles);
release(mcl)
mcl.SensorModel.NumBeams = 120;
```


## MotionModel - Odometry motion model for differential drive

odometryMotionModel object
Odometry motion model for differential drive, specified as an odomet ryMotionModel object. The default value uses the default odometryMotionModel object. After using the object to get output, call release on the object to make changes to MotionModel. For example:
$\mathrm{mcl}=$ monteCarloLocalization;
[isUpdated,pose,covariance] = mcl(ranges,angles);
release(mcl)
mcl. MotionModel. Noise $=[0.25$ 0.25 0.4 0.4];

## UpdateThresholds - Minimum change in states required to trigger update

[0.2 0.2 0.2] (default) | three-element vector
Minimum change in states required to trigger update, specified as a three-element vector. The localization updates the particles if the minimum change in any of the [ $x y$ theta] states is met. The pose estimate updates only if the particle filter is updated.

## ResamplingInterval - Number of filter updates between resampling of particles

1 (default) | positive integer
Number of filter updates between resampling of particles, specified as a positive integer.

## UseLidarScan - Use lidarScan object as scan input <br> false (default) | true

Use a lidarScan object as scan input, specified as either false or true.

## Usage

## Syntax

[isUpdated, pose,covariance] = mcl(odomPose,scan)
[isUpdated, pose,covariance] = mcl(odomPose, ranges,angles)

## Description

[isUpdated, pose,covariance] $=\mathrm{mcl}(o d o m P o s e, s c a n)$ estimates the pose and covariance of a vehicle using the MCL algorithm. The estimates are based on the pose calculated from the specified vehicle odometry, odomPose, and the specified lidar scan sensor data, scan. mcl is the
monteCarloLocalization object. isUpdated indicates whether the estimate is updated based on the UpdateThreshold property.

To enable this syntax, you must set the UseLidarScan property to true. For example:

```
mcl = monteCarloLocalization('UseLidarScan',true);
```

[isUpdated,pose,covariance] = mcl(odomPose,scan);
[isUpdated, pose,covariance] = mcl(odomPose, ranges,angles) specifies the lidar scan data as ranges and angles.

## Input Arguments

## odomPose - Pose based on odometry

three-element vector
Pose based on odometry, specified as a three-element vector, [x y theta]. This pose is calculated by integrating the odometry over time.

## scan - Lidar scan readings

lidarScan object
Lidar scan readings, specified as a lidarScan object.

## Dependencies

To use this argument, you must set the UseLidarScan property to true.
mcl.UseLidarScan = true;

## ranges - Range values from scan data

vector
Range values from scan data, specified as a vector with elements measured in meters. These range values are distances from a laser scan sensor at the specified angles. The ranges vector must have the same number of elements as the corresponding angles vector.

## angles - Angle values from scan data

vector
Angle values from scan data, specified as a vector with elements measured in radians. These angle values are the angles at which the specified ranges were measured. The angles vector must be the same length as the corresponding ranges vector.

## Output Arguments

## isUpdated - Flag for pose update

logical
Flag for pose update, returned as a logical. If the change in pose is more than any of the update thresholds, then the output is true. Otherwise, it is false. A true output means that updated pose and covariance are returned. A false output means that pose and covariance are not updated and are the same as at the last update.

## pose - Current pose estimate

three-element vector

Current pose estimate, returned as a three-element vector, [x y theta]. The pose is computed as the mean of the highest-weighted cluster of particles.

## covariance - Covariance estimate for current pose <br> matrix

Covariance estimate for current pose, returned as a matrix. This matrix gives an estimate of the uncertainty of the current pose. The covariance is computed as the covariance of the highestweighted cluster of particles.

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to monteCarloLocalization

getParticles Get particles from localization algorithm

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Estimate Vehicle Pose from Range Sensor Data

Create a monteCarloLocalization object, assign a sensor model, and calculate a pose estimate using the step method.

Note: Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step (obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

Create a monteCarloLocalization object. Set the UseLidarScan property to true.

```
mcl = monteCarloLocalization;
```

mcl .UseLidarScan = true;

Assign a sensor model with an occupancy grid map to the object.

```
sm = likelihoodFieldSensorModel;
p = zeros(200,200);
sm.Map = occupancyMap(p,20);
mcl.SensorModel = sm;
Create sample laser scan data input.
ranges = 10*ones(1,300);
ranges(1,130:170) = 1.0;
```

```
angles = linspace(-pi/2,pi/2,300);
odometryPose = [0 0 0];
Create a lidarScan object by specifying the ranges and angles.
```

```
scan = lidarScan(ranges,angles);
```

scan = lidarScan(ranges,angles);
Estimate vehicle pose and covariance.

```
```

[isUpdated,estimatedPose,covariance] = mcl(odometryPose,scan)

```
[isUpdated,estimatedPose,covariance] = mcl(odometryPose,scan)
isUpdated = logical
isUpdated = logical
    1
    1
estimatedPose = 1×3
estimatedPose = 1×3
    -0.0034 -0.0423 -0.0275
    -0.0034 -0.0423 -0.0275
covariance = 3×3
covariance = 3×3
    0.9379 -0.0365 0
    0.9379 -0.0365 0
    -0.0365 0.9656 0
    -0.0365 0.9656 0
        0 0 0.9870
```

        0 0 0.9870
    ```

\section*{References}
[1] Thrun, Sebatian, Wolfram Burgard, and Dieter Fox. Probabilistic Robotics. MIT Press, 2005.
[2] Dellaert, F., D. Fox, W. Burgard, and S. Thrun. "Monte Carlo Localization for Mobile Robots." Proceedings 1999 IEEE International Conference on Robotics and Automation.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{Tm}}\).

\section*{See Also}
lidarScan | likelihoodFieldSensorModel|odometryMotionModel
Topics
"Localize TurtleBot Using Monte Carlo Localization"
"Monte Carlo Localization Algorithm"
Class Attributes
Property Attributes

Introduced in R2019b

\section*{getParticles}

Get particles from localization algorithm

\section*{Syntax}
[particles,weights] = getParticles(mcl)

\section*{Description}
[particles,weights] = getParticles(mcl) returns the current particles used by the monteCarloLocalization object. particles is an \(n\)-by- 3 matrix that contains the location and orientation of each particle. Each row has a corresponding weight value specified in weights. The number of rows can change with each iteration of the MCL algorithm. Use this method to extract the particles and analyze them separately from the algorithm.

\section*{Examples}

\section*{Get Particles from Monte Carlo Localization Algorithm}

Get particles from the particle filter used in the Monte Carlo Localization object.
Create a map and a Monte Carlo localization object.
```

map = binary0ccupancyMap(10,10,20);
mcl = monteCarloLocalization(map);

```

Create robot data for the range sensor and pose.
```

ranges = 10*ones(1,300);
ranges(1,130:170) = 1.0;
angles = linspace(-pi/2,pi/2,300);
odometryPose = [0 0 0];
Initialize particles using step.

```
```

[isUpdated,estimatedPose,covariance] = step(mcl,odometryPose,ranges,angles);

```

Get particles from the updated object.
```

[particles,weights] = getParticles(mcl);

```

\section*{Input Arguments}

\section*{mcl - monteCarloLocalization object}
handle
monteCarloLocalization object, specified as an object handle.

\section*{Output Arguments}

\section*{particles - Estimation particles}
\(n\)-by-3 vector
Estimation particles, returned as an \(n\)-by- 3 vector, [ \(x\) y theta]. Each row corresponds to the position and orientation of a single particle. The length can change with each iteration of the algorithm.

\section*{weights - Weights of particles}
\(n\)-by-1 vector
Weights of particles, returned as a \(n\)-by- 1 vector. Each row corresponds to the weight of the particle in the matching row of particles. These weights are used in the final estimate of the pose of the vehicle. The length can change with each iteration of the algorithm.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and C++ code using MATLAB® \({ }^{\circledR}\) Coder \(^{\text {TM }}\).

\section*{See Also}
monteCarloLocalization

\section*{Topics}
"Monte Carlo Localization Algorithm"
Introduced in R2019b

\section*{multiLayerMap}

Manage multiple map layers

\section*{Description}

The multiLayerMap object groups and stores multiple map layers as mapLayer, occupancyMap, or binary0ccupancyMap objects.

Once added to this object, map layers can be modified by either using the multiLayerMap object functions or by performing actions on individual map layers using their object functions or the layer name as input. Any modification to common properties on the multiLayerMap object are reflected across all associated layers.

\section*{Creation}

\section*{Syntax}
```

map = multiLayerMap
map = multiLayerMap(maps)
map = multiLayerMap(names,mapData)
map = multiLayerMap(names,width,height)
map = multiLayerMap(names,width,height,cellDims)
map = multiLayerMap(names,rows,cols,'grid')
map = multiLayerMap(names,rows,cols,cellDims,'grid')
map = multiLayerMap(sourceMap)
map = multiLayerMap( , Name, Value)

```

\section*{Description}
map \(=\) multiLayerMap creates an empty map object occupying 10-by-10 meters of space with a resolution of 1 cell per meter.
map = multiLayerMap(maps) creates a multilayer map from a cell array of mapLayer, occupancyMap, or binary0ccupancyMap objects. Objects combined into a multilayer map must be defined with the same resolution and cover the same region in space, but can represent different categories of information over the shared region.
map \(=\) multiLayerMap(names, mapData) creates a multilayer map from the cell array of layer names and associated cell array of map matrices. Matrices must have the same first two dimensions to cover the same shared region. Default resolution is 1 cell per meter.
map = multiLayerMap(names,width,height) creates a multilayer map with the cell array of layer names covering the specified width and height as scalars in meters.
map = multiLayerMap(names, width, height, cellDims) creates a multilayer map where the size of the data stored in each cell of the map is defined by the array of integers, cellDims. For multiple layers, cellDims is a cell array of integer arrays.
map \(=\) multiLayerMap(names, rows,cols,'grid') specifies the map width and height as a grid size specified in the rows and cols inputs.
map \(=\) multiLayerMap (names, rows, cols, cellDims,'grid') creates a map with a specified grid size and the size of the data stored in each cell is defined by the array of integers or cell array of integer arrays cellDims.
map \(=\) multiLayerMap(sourceMap) creates a new object using the layers copied from another multiLayerMap object.
map = multiLayerMap( \(\qquad\) , Name, Value) specifies property values using name-value pairs.

For example, multiLayerMap(__, 'LocalOriginInWorld', [15 20]) sets the local origin to a specific world location.

\section*{Properties}

\section*{DataSize - Size of the data in each map layer data array \\ cell array of integer vectors}

Size of the data in each map layer data array, specified as a cell array of integer vectors. In each vector, the first two dimensions define the footprint of the map layer, and all subsequent dimensions dictate the size and layout of the data stored in each cell.

If the map stores an \(n\)-element vector of values in each cell, this property would be [width height \(\mathrm{n}]\).

If the map stores a 10-by-10 grid with each cell containing a 3-by-3-by-3 matrix array, the data size would be \(\left[\begin{array}{lllll}10 & 10 & 3 & 3 & 3\end{array}\right]\).

After you create the object, this property is read-only.
Data Types: cell|double

\section*{DataType - Data type of the values stored}
cell array of string scalars
Data type of the values stored in each layer, specified as a cell array of character vectors.
When you create this object, the specified map layers determine each data type. After you create the object, this property is read-only.

\section*{Data Types: cell | char}

\section*{DefaultValue - Default value for unspecified map locations}
\(\{0\}\) (default) | cell array of numeric scalars
Default value for unspecified map locations for each layer, specified as a cell array of numeric scalars. This default value is returned for areas outside the map as well.
Data Types: cell|double

Location of the bottom-left corner of the grid in world coordinates, specified as a two-element vector, [xWorld yWorld].

You can set this property when you create the object.
Data Types: double
GridOriginInLocal - Location of the grid in local coordinates
[0 0] (default)|two-element vector | [xLocal yLocal]
Location of the bottom-left corner of the grid in local coordinates, specified as a two-element vector, [xLocal yLocal].

You can set this property when you create the object.

\section*{Data Types: double}

\section*{GridSize - Number of rows and columns in grid}
two-element integer-valued vector
This property is read-only.
Number of rows and columns in grid, stored as a 1-by-2 real-valued vector representing the number of rows and columns, in that order.

Data Types: double

\section*{LayerNames - Name of each layer}
cell array of string scalars
Name of each layer, specified as a cell array of string scalars. The order of these names are associated with the order of other properties that are cell arrays.

You can set this property when you create the object. After you create the object, this property is read-only.

Data Types: cell | string

\section*{LocalOriginInWorld - Location of the local frame in world coordinates}
[0 0] (default)|two-element vector|[xWorld yWorld]
Location of the origin of the local frame in world coordinates, specified as a two-element vector, [xLocal yLocal]. Use the move function to shift the local frame as your vehicle moves.

You can set this property when you create the object.

\section*{Data Types: double}

\section*{NumLayers - Number of map layers}

1 (default) | positive integer
This property is read-only.
Number of map layers, stored as a positive integer.
Data Types: double
Resolution - Grid resolution
1 (default) | scalar

This property is read-only.
Grid resolution, stored as a scalar in cells per meter representing the number and size of grid locations.

You can set this property when you create the object. After you create the object, this property is read-only.
Data Types: double
XLocalLimits - Minimum and maximum values of x-coordinates in local frame two-element vector

This property is read-only.
Minimum and maximum values of \(x\)-coordinates in local frame, stored as a two-element horizontal vector of the form [min max]. Local frame is defined by LocalOriginInWorld property.
Data Types: double
YLocalLimits - Minimum and maximum values of \(\boldsymbol{y}\)-coordinates in local frame two-element vector

This property is read-only.
Minimum and maximum values of \(y\)-coordinates in local frame, stored as a two-element horizontal vector of the form [min max]. Local frame is defined by LocalOriginInWorld property.

Data Types: double
XWorldLimits - Minimum and maximum world range values of \(x\)-coordinates
two-element vector
This property is read-only.
Minimum and maximum world range values of \(x\)-coordinates, stored as a 1-by-2 vector representing the minimum and maximum values, in that order.

Data Types: double
YWorldLimits - Minimum and maximum world range values of \(\boldsymbol{y}\)-coordinates
two-element vector
This property is read-only.
Minimum and maximum world range values of \(y\)-coordinates, stored as a 1-by-2 vector representing the minimum and maximum values, in that order.
Data Types: double

\section*{Object Functions}
getLayer
Return individual layers from multilayer map
getMapData Retrieve data from map layers
grid2local Convert grid indices to local coordinates
grid2world Convert grid indices to world coordinates
local2grid Convert local coordinates to grid indices
\begin{tabular}{ll} 
local2world & Convert local coordinates to world coordinates \\
move & Move map in world frame \\
setMapData & Assign data to map layers \\
syncWith & Sync map with overlapping map \\
world2grid & Convert world coordinates to grid indices \\
world2local & Convert world coordinates to local coordinates
\end{tabular}

\section*{Examples}

\section*{Create Listeners Using Dependent Map Layers}

The multiLayerMap object enables you to group multiple map layers and define behavior for those layers when setting and getting data. Using separate map layers, you can store various map data and specify different behaviors for each. You can also define the SetTransformFcn and GetTransformFcn function handles for a map layer so that dependencies are created between layers. This example shows how to store data in a map layer and implement event listeners which update other maps. These maps store how many times the data is updated or accessed.

\section*{Dependent Layers}

Create two independent map layers.
```

mapAccessed = mapLayer(zeros(10,10),'LayerName','GetListener');
mapModified = mapLayer(zeros(10,10),'LayerName','SetListener');

```

Specify function handles for the get and set transform functions used in the main map layer. These functions increment the value of a grid location when you get or set map data in the input map mainMap. See Listener Function Handles on page 2-0 for the function implementation.
```

setHookFcn = @(mainMap,values,varargin)exampleHelperSetHookFcn(mapModified,mainMap,values,vararg

```
getHookFcn = @(mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,vararg:

Create the main map layer with default values of 0.5 . Specify the function handles to create the layer depencies.
```

map = mapLayer(repmat(0.5,10,10),...
'GetTransformFcn',getHookFcn,...
'SetTransformFcn',setHookFcn);

```

Add all maps to the same multiLayerMap object.
```

mapLayers = multiLayerMap({map,mapAccessed,mapModified});

```

Set the \((0,0)\) map location with a value of zero using the setMapData object function of map.
```

setMapData(map,[0 0],0)

```

Check that mapModified incremented their value.
```

getMapData(mapModified,[0 0])

```
ans \(=1\)

Get the data you just set to the main map layer. The expected value of zero is returned.
```

getMapData(map,[0 0])

```
```

ans = 0

```

Check that mapAccessed incremented their value.
```

getMapData(mapAccessed,[0 0])

```
ans \(=1\)

Update the entire map with a matrix of values. Access the data as well.
setMapData(map, rand \((10,10)\) )
getMapData(map)
```

ans = 10\times10

```
\begin{tabular}{llllll}
0.8147 & 0.1576 & 0.6557 & 0.7060 & 0.4387 & 0.2760 \\
0.9058 & 0.9706 & 0.0357 & 0.0318 & 0.3816 & 0.6797 \\
0.1270 & 0.9572 & 0.8491 & 0.2769 & 0.7655 & 0.6551 \\
0.9134 & 0.4854 & 0.9340 & 0.0462 & 0.7952 & 0.1626 \\
0.6324 & 0.8003 & 0.6787 & 0.0971 & 0.1869 & 0.1190 \\
0.0975 & 0.1419 & 0.7577 & 0.8235 & 0.4898 & 0.4984 \\
0.2785 & 0.4218 & 0.7431 & 0.6948 & 0.4456 & 0.9597 \\
0.5469 & 0.9157 & 0.3922 & 0.3171 & 0.6463 & 0.3404 \\
0.9575 & 0.7922 & 0.6555 & 0.9502 & 0.7094 & 0.5853 \\
0.9649 & 0.9595 & 0.1712 & 0.0344 & 0.7547 & 0.2238
\end{tabular}

Check that mapModified and mapAccessed incremented their values. getMapData(mapModified)
```

ans = 10×10

```
\begin{tabular}{llllllllll}
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
2 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1
\end{tabular}
getMapData(mapAccessed)
```

ans = 10×10

```
\begin{tabular}{llllllllll}
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
2 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1
\end{tabular}

The bottom-left location returns two and all other values are one. This confirms the listener functions are working as intended.

\section*{Listener Function Handles}

These functions implement the get and set example helper functions that update the other map layers.
```

function valuesOut = exampleHelperSetHookFcn(modifiedMap,sourceLayer,valueIn,varargin)
% Pass output through
valuesOut = valueIn;
% If no additional inputs are passed, return immediately.
if numel(varargin) == 0
return;
else
% Otherwise, increment the value in the modifiedMap.
if numel(varargin) == 1
currentValue = getMapData(modifiedMap);
setMapData(modifiedMap,currentValue+1);
else
currentValue = getMapData(modifiedMap,varargin{1},varargin{3:end});
% setMapData syntax <<<<>>>>
setMapData(modifiedMap,varargin{1},currentValue+1,varargin{3:end});
end
end
end
function data = exampleHelperGetHookFcn(accessedMap,sourceLayer,valuesIn,varargin)
data = valuesIn;
% If no additional inputs are passed, check if the values in
if numel(varargin) == 0
if isequal(size(valuesIn),sourceLayer.DataSize)
% Increment the depedent map.
currentValue = getMapData(accessedMap);
setMapData(accessedMap,currentValue+1);
end
else
currentValue = getMapData(accessedMap,varargin{:});
setMapData(accessedMap,varargin{1},currentValue+1,varargin{3:end});
end
end

```

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and \(\mathrm{C}++\) code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).
As of MATLAB R2022a, default map behavior during code generation has changed, which may result in backwards compatibility issues. Maps such as multiLayerMap now support fixed-size code generation (DynamicMemoryAllocation="off").

1 Maps that are either default-constructed or constructed with compile-time constant size information (or matrices that are of compile-time constant size) produce fixed-size maps.

2 To restore the previous behavior, use the coder.ignoreConst function when specifying size inputs, or coder.varsize matrix variable name specified as a string scalar or character vector, prior to constructing the map.

\section*{See Also}

\section*{Objects}
mapLayer | occupancyMap3D | occupancyMap | binaryOccupancyMap

\section*{Functions}
getMapData| setMapData|move| syncWith

\section*{Topics}
"Fuse Multiple Lidar Sensors Using Map Layers"

\section*{Introduced in R2021a}

\section*{getLayer}

Return individual layers from multilayer map

\section*{Syntax}
mapLayer = getLayer(map,layerName)

\section*{Description}
mapLayer = getLayer(map, layerName) returns the individual map layer, specified by the layer name layerName. For a list of all layer names, see the LayerNames property of the multiLayerMap object map.

\section*{Input Arguments}
map - Multilayer map
multiLayerMap object
Multilayer map, specified as a multiLayerMap object.

\section*{layerName - Name of individual map layer}
string scalar | character vector
Name of individual map layer, specified as a string scalar or character vector.
Data Types: char | string

\section*{Output Arguments}
mapLayer - Individual map layer
binary0ccupancyMap object | occupancyMap object | mapLayer object
Individual map layer, returned as a binary0ccupancyMap, occupancyMap, or mapLayer object as a handle. For more information, see "Handle Object Behavior".

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and C++ code using MATLAB® \({ }^{\circledR}\) Coder \(^{\text {TM }}\).

\section*{See Also}
```

Objects
mapLayer|occupancyMap3D | occupancyMap | binaryOccupancyMap
Functions
getMapData|setMapData|move| syncWith

```

\section*{Topics}
"Fuse Multiple Lidar Sensors Using Map Layers"
Introduced in R2021a

\section*{getMapData}

Retrieve data from map layers

\section*{Syntax}
```

mapData = getMapData(map)
mapData = getMapData(map,layername)
mapData = getMapData(map,layername,layerinputs)

```

\section*{Description}
mapData \(=\) getMapData(map) returns a cell array of matrices for the data in each layer of the specified multiLayerMap object. For binary or occupancy map layers, the values of this function are passed to the getOccupancy function. mapData is returned as an cell-array of matrices for each layer.
mapData \(=\) getMapData(map,layername) returns all the map data for the specified layer name. mapData is returned as a matrix equal to the DataSize of the specified layer.
mapData \(=\) getMapData(map,layername,layerinputs) takes the layerinputs arguments and passes them to the getMapData object function for the specified map layer name. To access individual cells or blocks of data in the world, local, or grid coordinates, see the syntaxes of getMapData.

\section*{Examples}

\section*{Create Listeners Using Dependent Map Layers}

The multiLayerMap object enables you to group multiple map layers and define behavior for those layers when setting and getting data. Using separate map layers, you can store various map data and specify different behaviors for each. You can also define the SetTransformFcn and GetTransformFcn function handles for a map layer so that dependencies are created between layers. This example shows how to store data in a map layer and implement event listeners which update other maps. These maps store how many times the data is updated or accessed.

\section*{Dependent Layers}

Create two independent map layers.
```

mapAccessed = mapLayer(zeros(10,10),'LayerName','GetListener');
mapModified = mapLayer(zeros(10,10),'LayerName','SetListener');

```

Specify function handles for the get and set transform functions used in the main map layer. These functions increment the value of a grid location when you get or set map data in the input map mainMap. See Listener Function Handles on page 2-0 for the function implementation.
```

setHookFcn = @(mainMap,values,varargin)exampleHelperSetHookFcn(mapModified,mainMap,values,vararg
getHookFcn = @(mainMap,values,varargin)exampleHelperGetHookFcn(mapAccessed,mainMap,values,vararg

```

Create the main map layer with default values of 0.5 . Specify the function handles to create the layer depencies.
```

map = mapLayer(repmat(0.5,10,10),...
'GetTransformFcn',getHookFcn,...
'SetTransformFcn',setHookFcn);

```

Add all maps to the same multiLayerMap object.
```

mapLayers = multiLayerMap({map,mapAccessed,mapModified});

```

Set the \((0,0)\) map location with a value of zero using the setMapData object function of map.
```

setMapData(map,[0 0],0)

```

Check that mapModified incremented their value.
getMapData(mapModified,[0 0])
ans \(=1\)
Get the data you just set to the main map layer. The expected value of zero is returned.
getMapData(map,[0 0])
ans \(=0\)
Check that mapAccessed incremented their value.
getMapData(mapAccessed,[0 0])
ans \(=1\)
Update the entire map with a matrix of values. Access the data as well.
```

setMapData(map,rand(10,10))
getMapData(map)
ans = 10\times10

| 0.8147 | 0.1576 | 0.6557 | 0.7060 | 0.4387 | 0.2760 | 0.7513 | 0.8407 | 0.3517 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0.9058 | 0.9706 | 0.0357 | 0.0318 | 0.3816 | 0.6797 | 0.2551 | 0.2543 | 0.8308 |
| 0.1270 | 0.9572 | 0.8491 | 0.2769 | 0.7655 | 0.6551 | 0.5060 | 0.8143 | 0.5853 |
| 0.9134 | 0.4854 | 0.9340 | 0.0462 | 0.7952 | 0.1626 | 0.6991 | 0.2435 | 0.5497 |
| 0.6324 | 0.8003 | 0.6787 | 0.0971 | 0.1869 | 0.1190 | 0.8909 | 0.9293 | 0.9172 |
| 0.0975 | 0.1419 | 0.7577 | 0.8235 | 0.4898 | 0.4984 | 0.9593 | 0.3500 | 0.2858 |
| 0.2785 | 0.4218 | 0.7431 | 0.6948 | 0.4456 | 0.9597 | 0.5472 | 0.1966 | 0.7572 |
| 0.5469 | 0.9157 | 0.3922 | 0.3171 | 0.6463 | 0.3404 | 0.1386 | 0.2511 | 0.7537 |
| 0.9575 | 0.7922 | 0.6555 | 0.9502 | 0.7094 | 0.5853 | 0.1493 | 0.6160 | 0.3804 |
| 0.9649 | 0.9595 | 0.1712 | 0.0344 | 0.7547 | 0.2238 | 0.2575 | 0.4733 | 0.5678 |

```

Check that mapModified and mapAccessed incremented their values.
```

getMapData(mapModified)
ans = 10\times10
1 1rlllllllll
1

```
\begin{tabular}{llllllllll}
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
2 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1
\end{tabular}
getMapData(mapAccessed)
ans \(=10 \times 10\)
\begin{tabular}{llllllllll}
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
2 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1
\end{tabular}

The bottom-left location returns two and all other values are one. This confirms the listener functions are working as intended.

\section*{Listener Function Handles}

These functions implement the get and set example helper functions that update the other map layers.
```

function valuesOut = exampleHelperSetHookFcn(modifiedMap,sourceLayer,valueIn,varargin)
% Pass output through
valuesOut = valueIn;
% If no additional inputs are passed, return immediately.
if numel(varargin) == 0
return;
else
% Otherwise, increment the value in the modifiedMap.
if numel(varargin) == 1
currentValue = getMapData(modifiedMap);
setMapData(modifiedMap,currentValue+1);
else
currentValue = getMapData(modifiedMap,varargin{1},varargin{3:end});
% setMapData syntax <<<<>>>>
setMapData(modifiedMap,varargin{1},currentValue+1,varargin{3:end});
end
end
end
function data = exampleHelperGetHookFcn(accessedMap,sourceLayer,valuesIn,varargin)
data = valuesIn;

```
```

    % If no additional inputs are passed, check if the values in
    if numel(varargin) == 0
    if isequal(size(valuesIn),sourceLayer.DataSize)
        % Increment the depedent map.
        currentValue = getMapData(accessedMap);
        setMapData(accessedMap,currentValue+1);
    end
    else
        currentValue = getMapData(accessedMap,varargin{:});
        setMapData(accessedMap,varargin{1},currentValue+1,varargin{3:end});
    end
    end

```

\section*{Input Arguments}
map - Multilayer map
multiLayerMap object
Multilayer map, specified as a multiLayerMap object.

\section*{layername - Map layer name}
string scalar | character array
Map layer name, specified as a string scalar or character array. Map layers have their name specified when creating the multiLayerMap object.

\section*{layerinputs - Variable-length inputs to map layer \\ varargin}

Variable-length inputs to getMapData function of map layer, specified as varargin. To specify individual cells or blocks of data in the world, local, or grid coordinates, see the syntaxes of getMapData.

\section*{Output Arguments}

\section*{mapData - Data values from map layer}
matrix
Data values from map layer, returned as a matrix. By default, the function returns all data on the layer as an \(M\)-by- \(N\)-by-DataDims matrix. \(M\) and \(N\) are the grid height and width respectively. DataDims are the dimensions of the map data, map. \(\operatorname{DataSize(3,:).~}\)

For other syntaxes, the map data may be given as an array of values with size \(N\)-by-DataDims or as a subregion of the full matrix.

\section*{See Also}

\section*{Objects}
multiLayerMap|mapLayer| occupancyMap3D | occupancyMap | binary0ccupancyMap

\section*{Functions}
getMapData|setMapData|move| syncWith

Introduced in R2021a

\section*{setMapData}

Assign data to map layers

\section*{Syntax}
setMapData(map,layername, layerinputs)
inBounds = setMapData(map,layername,layerinputs)

\section*{Description}
setMapData(map,layername,layerinputs) takes the layerinputs arguments and passes them to the setMapData object function for the specified map layer name. To specify individual cells or blocks of data in the world, local, or grid coordinates, see the syntaxes of setMapData.
inBounds = setMapData(map,layername,layerinputs) returns an array of values for the given locations in the layerinputs input argument.

\section*{Examples}

\section*{Create Listeners Using Dependent Map Layers}

The multiLayerMap object enables you to group multiple map layers and define behavior for those layers when setting and getting data. Using separate map layers, you can store various map data and specify different behaviors for each. You can also define the SetTransformFcn and GetTransformFcn function handles for a map layer so that dependencies are created between layers. This example shows how to store data in a map layer and implement event listeners which update other maps. These maps store how many times the data is updated or accessed.

\section*{Dependent Layers}

Create two independent map layers.
```

mapAccessed = mapLayer(zeros(10,10),'LayerName','GetListener');
mapModified = mapLayer(zeros(10,10),'LayerName','SetListener');

```

Specify function handles for the get and set transform functions used in the main map layer. These functions increment the value of a grid location when you get or set map data in the input map mainMap. See Listener Function Handles on page 2-0 for the function implementation.
setHookFcn = @(mainMap,values,varargin)exampleHelperSetHookFcn(mapModified,mainMap,values,vararg: getHookFcn = @(mainMap, values, varargin)exampleHelperGetHookFcn(mapAccessed, mainMap,values,vararg

Create the main map layer with default values of 0.5 . Specify the function handles to create the layer depencies.
```

map = mapLayer(repmat(0.5,10,10),...
'GetTransformFcn',getHookFcn,...
'SetTransformFcn',setHookFcn);

```

Add all maps to the same multiLayerMap object.
mapLayers = multiLayerMap(\{map,mapAccessed,mapModified\});
Set the \((0,0)\) map location with a value of zero using the setMapData object function of map.
```

setMapData(map,[0 0],0)

```

Check that mapModified incremented their value.
```

getMapData(mapModified,[0 0])

```
ans \(=1\)

Get the data you just set to the main map layer. The expected value of zero is returned.
```

getMapData(map,[0 0])

```
ans \(=0\)

Check that mapAccessed incremented their value.
getMapData(mapAccessed,[00])
ans \(=1\)
Update the entire map with a matrix of values. Access the data as well.
```

setMapData(map,rand(10,10))
getMapData(map)
ans = 10\times10

| 0.8147 | 0.1576 | 0.6557 | 0.7060 | 0.4387 | 0.2760 | 0.7513 | 0.8407 | 0.3517 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0.9058 | 0.9706 | 0.0357 | 0.0318 | 0.3816 | 0.6797 | 0.2551 | 0.2543 | 0.8308 |
| 0.1270 | 0.9572 | 0.8491 | 0.2769 | 0.7655 | 0.6551 | 0.5060 | 0.8143 | 0.5853 |
| 0.9134 | 0.4854 | 0.9340 | 0.0462 | 0.7952 | 0.1626 | 0.6991 | 0.2435 | 0.5497 |
| 0.6324 | 0.8003 | 0.6787 | 0.0971 | 0.1869 | 0.1190 | 0.8909 | 0.9293 | 0.9172 |
| 0.0975 | 0.1419 | 0.7577 | 0.8235 | 0.4898 | 0.4984 | 0.9593 | 0.3500 | 0.2858 |
| 0.2785 | 0.4218 | 0.7431 | 0.6948 | 0.4456 | 0.9597 | 0.5472 | 0.1966 | 0.7572 |
| 0.5469 | 0.9157 | 0.3922 | 0.3171 | 0.6463 | 0.3404 | 0.1386 | 0.2511 | 0.7537 |
| 0.9575 | 0.7922 | 0.6555 | 0.9502 | 0.7094 | 0.5853 | 0.1493 | 0.6160 | 0.3804 |
| 0.9649 | 0.9595 | 0.1712 | 0.0344 | 0.7547 | 0.2238 | 0.2575 | 0.4733 | 0.5678 |

```

Check that mapModified and mapAccessed incremented their values. getMapData(mapModified)
ans \(=10 \times 10\)
\begin{tabular}{llllllllll}
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
2 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1
\end{tabular}
```

getMapData(mapAccessed)
ans = 10\times10

| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 2 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |

```

The bottom-left location returns two and all other values are one. This confirms the listener functions are working as intended.

\section*{Listener Function Handles}

These functions implement the get and set example helper functions that update the other map layers.
```

function valuesOut = exampleHelperSetHookFcn(modifiedMap,sourceLayer,valueIn,varargin)
% Pass output through
valuesOut = valueIn;
% If no additional inputs are passed, return immediately.
if numel(varargin) == 0
return;
else
% Otherwise, increment the value in the modifiedMap.
if numel(varargin) == 1
currentValue = getMapData(modifiedMap);
setMapData(modifiedMap,currentValue+1);
else
currentValue = getMapData(modifiedMap,varargin{1},varargin{3:end});
% setMapData syntax <<<<>>>>
setMapData(modifiedMap,varargin{1},currentValue+1,varargin{3:end});
end
end
end
function data = exampleHelperGetHookFcn(accessedMap,sourceLayer,valuesIn,varargin)
data = valuesIn;
% If no additional inputs are passed, check if the values in
if numel(varargin) == 0
if isequal(size(valuesIn),sourceLayer.DataSize)
% Increment the depedent map.
currentValue = getMapData(accessedMap);
setMapData(accessedMap,currentValue+1);
end
else
currentValue = getMapData(accessedMap,varargin{:});
setMapData(accessedMap,varargin{1},currentValue+1,varargin{3:end});

```
end
end

\section*{Input Arguments}

\section*{map - Multilayer map}
multiLayerMap object
Multilayer map, specified as a multiLayerMap object.

\section*{layername - Map layer name}
string scalar | character array
Map layer name, specified as a string scalar or character array. Map layers have their name specified when creating the multiLayerMap object.

\section*{layerinputs - Variable-length inputs to map layer}
varargin
Variable-length inputs to setMapData function of the map layer, specified as varargin. To specify individual cells or blocks of data in the world, local, or grid coordinates, see the syntaxes of setMapData.

\section*{Output Arguments}

\section*{inBounds - Valid map locations}
\(n\)-by-1 column vector
Valid map locations, returned as an \(n\)-by- 1 column vector equal in length to xy or ij . Locations inside the map limits return a value of 1 . Locations outside the map limits return a value of 0 .

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and C++ code using MATLAB® Coder \({ }^{\mathrm{TM}}\).

\section*{See Also}

\section*{Objects}
multiLayerMap | mapLayer | occupancyMap3D | occupancyMap | binary0ccupancyMap
Functions
getMapData|setMapData|move| syncWith
Introduced in R2021a

\section*{gpsdev}

Connect to a GPS receiver connected to host computer

\section*{Description}

The gpsdev System object connects to a GPS receiver connected to the host computer.
To connect to a GPS receiver:
1 Create the gpsdev object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

\section*{Creation}

\section*{Syntax}
gps = gpsdev(port)
gps = gpsdev(serialobj)
gps = gpsdev( \(\qquad\) ,Name, Value)

\section*{Description}
gps = gpsdev(port) connects to a GPS Receiver at the specified serial port of host computer.
gps = gpsdev(serialobj) connects to a GPS Receiver specified by a serial object.
gps = gpsdev( __ , Name, Value) connects to a GPS Receiver on the specified port or specified through a serial object, using one or more name-value pairs.

\section*{Properties}

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

\section*{BaudRate - Baud rate 9600}

This property is read-only.

The baud rate for serial communication. The baud rate is set at 9600 bits/sec. The GPS receiver must be configured to work at \(9600 \mathrm{bits} / \mathrm{sec}\). If your GPS receiver is configured to some other baud rate, reconfigure it to 9600 bits/sec to use gpsdev function.

\section*{ReadMode - Specify which data samples to be returned}
'latest' (default)|'oldest'
Specify whether to return the latest or the oldest data samples. The number of samples depends on the SamplesPerRead value. The data read from the GPS receiver is stored in the MATLAB buffer.
- latest - Provides the latest data samples available in the buffer. All previous data samples in the buffer are discarded. For example, if SamplesPerRead \(=3\), the latest three data samples read by the GPS receiver are returned.
- oldest - Provides the oldest data samples available in the buffer. In this case, no data samples are discarded. For example, if SamplesPerRead =3, the first three data samples read are returned for the first read, the next three data samples are returned for the second read, and so on.

Tunable: No
Data Types: character vector|string

\section*{SamplesRead - Samples read}
double
This property is read-only.
Number of samples read from the GPS receiver using the read function, after the object is locked. The gpsdev object gets locked either at the first call of the read function after the object creation or at the first call of the read function after the execution of the release function.
Data Types: double

\section*{SamplesAvailable - Samples in the host buffer \\ double}

This property is read-only.
Samples available in the host buffer. When you release the object, SamplesAvailable is set to 0 .
Data Types: double

\section*{SamplesPerRead - Samples per read \\ 1 (default)}

Samples read from the first read, specified as a positive integer in the range [1 10].
Tunable: No

\section*{Data Types: double}

\section*{OutputFormat - Set output format}
'timetable' (default)|'matrix'
Set the output format of the data returned by executing the read function.
When the OutputFormat is set to timetable, the timetable returned has the following fields:
- LLA (Latitude, Longitude, Altitude)
- Ground Speed
- Course over ground
- Dilution of Precisions(DOPs), VDOP,HDOP,PDOP
- GPS Receiver Time
- Time - System time when the data is read, in datetime or duration format

When the OutputFormat is set to matrix, the data is returned as matrices of Time, LLA, Ground Speed, Course over ground, DOPs, and GPS receiver time. The units for the GPS receiver readings are the same as the timetable format.

Tunable: Yes
Data Types: character vector|string

\section*{TimeFormat - Set the format of the time displayed when the GPS data is read \\ 'datetime' (default)|'duration'}

Set the format of the time displayed when the GPS data is read.
- datetime - Displays the date and time at which the data is read.
- duration - Displays the time elapsed in seconds after the GPS object is locked. The gpsdev object gets locked either at the first call of the read function after the object creation or at the first call of the read function after the execution of the release function.

Tunable: Yes
Data Types: character vector|string

\section*{Object Functions}

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:
```

release(obj)

```
flush Flush all GPS data accumulated in the buffers and reset properties
info Read update rate, GPS lock information and number of satellites in view for the GPS receiver
read Read data from GPS receiver
release Release the GPS object
writeBytes Write raw commands to the GPS receiver

\section*{Examples}

\section*{Plot Geographic Position Using GPS Connected to Host Computer}

Get the geographic location using the GPS receiver connected to the host computer on a specific serial port and plot the location in a map.

\section*{Required Hardware}

To run this example, you need:
- UBlox Neo-6M GPS module
- GPS antenna
- USB to UART module
- USB cable
- Connecting wires

\section*{Hardware Connection}


Connect the pins on the UBlox Neo-6M GPS module to the pins on your USB to UART module. The connections are:
- VCC -+5 V
- RX - TXO
- TX - RXI
- GND - GND

Connect the GPS antenna to the GPS module. Connect the USB to UART module to the host computer with a USB cable. GPS Fix can be easily acquired in locations that have a clear view of the sky. Wait for the GPS module to acquire satelite signals (Fix).This can be verified by checking the Fix LED (D1) of your GPS module.

\section*{Create GPS Object}

Create a gpsdev object for the GPS module connected to a specific port.
```

gps = gpsdev('COM4')

```
gps =
gpsdev with properties:
SerialPort: COM4
BaudRate: 9600 (bits/s)
```

SamplesPerRead: 1
ReadMode: "latest"
SamplesRead: 0

```
Show all properties all functions

\section*{Read the GPS data}

Read the GPS data and extract latitude, longitude, and time from it. GPS returns UTC datetime. Convert it to system time zone.
```

[gpsData,~] = read(gps);
latitude = gpsData.LLA(1);
longitude = gpsData.LLA(2);
gpsTime = gpsData.GPSReceiverTime;
gpsTime.TimeZone = 'local';

```

\section*{Plot the position in a map along with the timestamp}

Plot the position in geographic axes with the data obtained from the GPS module. GPS should have fix to get valid values for latitude, longitude and gpsTime.

If the GPS module does not have fix, the above commands give NaNs for latitude and longitude and NaT for gpsTime. In this case, make sure the antenna is exposed to clear sky and wait for some time and try the above steps again.
```

if(~isnan(latitude) \&\& ~isnan(longitude))
% plot the position in geographic coordinates
fig = geoplot(latitude,longitude,'Marker',"o",'MarkerSize',6,'Color','red','MarkerFaceColor','r
% Sets the latitude and longitude limits of the base Map
geolimits([latitude-0.05 latitude+0.05],[longitude-0.05 longitude+0.05]) ;
% Selects the basemap
geobasemap streets;
timeString = strcat("Timestamp: ",string(gpsTime));
% Create annotation and display time received from GPS
annotation('textbox',[0.005 0.98 0.6 0.01],'FitBoxToText','on','string',timeString,'Color','blue
end

```

\section*{Clean Up}

When the connection is no longer needed, clear the associated object.
```

delete(gps);

```
clear gps;

\section*{Write Configuration Commands to GPS Receiver}

Write configuration commands to the GPS receiver connected to the host computer using serialport object.

\section*{Required Hardware}

To run this example, you need:
- UBlox Neo-6M GPS module
- GPS antenna
- USB to UART module
- USB cable
- Connecting wires

\section*{Hardware Connection}


Connect the pins on the UBlox Neo-6M GPS module to the pins on your USB to UART module. The connections are:
- VCC -+5 V
- RX - TXO
- TX - RXI
- GND - GND

Connect the GPS antenna to the GPS module. Connect the USB to UART module to the host computer with a USB cable. GPS Fix can be easily acquired in locations that have a clear view of the sky. Wait for the GPS module to acquire satelite signals (Fix).This can be verified by checking the Fix LED (D1) of your GPS module.

\section*{Create GPS Object}

Connect to the GPS receiver using serialport object. Specify the port name and the baud rate.
```

s = serialport('COM4',9600)
S =
Serialport with properties:
Port: "COM4"
BaudRate: 9600
NumBytesAvailable: 0
Show all properties, functions

```
```

gps = gpsdev(s)
gps =
gpsdev with properties:

```
        SerialPort: COM4
                        BaudRate: 9600 (bits/s)
SamplesPerRead: 1
            ReadMode: "latest"
                SamplesRead: 0
Show all properties all functions

\section*{Write Configuration Commands}

In the default configuration the GPS receiver returns the following NMEA messages: GPRMC, GPVTG, GPGGA, GPGSA, GPGSV, and GPGLL. The receiver can be configured to have a user defined set of output messages.

Read few lines of default messages from the serial port the GPS receiver is connected.
```

for i = 1:10
data = readline(s);
disp(data);
end
\$GPRMC, ,V, , , , , , , , , N*53
\$GPVTG, , , , , , , , ,N*30
\$GPGGA, , , , , ,0,00,99.99, , , , , ,48
\$GPGSA,A ,1, , , , , , , , , , , ,99.99, 99.99,99.99*30
\$GPGSV,2,1,08,01, , ,18,08, , ,12,09, , ,12,15, , ,19*77
\$GPGSV,2,2,08,23,, ,13,24,, ,09,25, ,,10,27, , ,25*79
\$GPGLL, , , , , , V,N*64
\$GPRMC, ,V, , , , , , , , ,N*53
\$GPVTG, , , , , , , , ,N*30
\$GPGGA, , , , , 0,00,99.99, , , , , ,*48

```

Write the version monitor command to the GPS receiver to return the software and hardware version of the GPS receiver.
```

configCMD = [0xB5 0x62 0x0A 0x04 0x00 0x00 0x0E 0x34];
% writeBytes(gps,cfg)
write(s,configCMD,'uint8')

```

Read few lines of messages again to verify the version message.
```

for i = 1:10
data = readline(s);
disp(data);
end
\$GPGSA, A ,1, , , , , , , , , , , , 99.99,99.99,99.99*30
\$GPGSV,2,1,05,01, , ,13,09, , ,11,15, , ,16,23, , ,12*74
\$GPGSV , 2, 2,05,25, , ,10*7A
\$GPGLL, , , , , ,V,N*64
\mub
( 7.03 (45969) 00040007 ` \$GPRMC,,V,,,,,,,,,,,N*53
\$GPVTG , , , , , , , , N*30

```
```

\$GPGGA, , , , , 0,00,99.99, , , , , ,*48
\$GPGSA,A ,1, , , , , , , , , , , , 99.99,99.99,99.99*30
\$GPGSV,2,1,06,01,,,11,09, , ,11,23, ,, 14,24, , ,21*75

```

It can be observed from the output, 7.03 (45969) is the software version and 00040007 is the hardware version.

\section*{Clean Up}

When the connection is no longer needed, clear the associated object.
```

delete(gps);
clear gps;
clear s;

```

\section*{Read Data from GPS Receiver as Timetable}

Read data from the GPS receiver connected to the host computer on a specific serial port.

\section*{Required Hardware}

To run this example, you need:
- UBlox Neo-6M GPS module
- GPS antenna
- USB to UART module
- USB cable
- Connecting wires

\section*{Hardware Connection}


Connect the pins on the UBlox Neo-6M GPS module to the pins on your USB to UART module. The connections are:
- VCC -+5 V
- RX - TXO
- TX - RXI
- GND - GND

Connect the GPS antenna to the GPS module. Connect the USB to UART module to the host computer with a USB cable. GPS Fix can be easily acquired in locations that have a clear view of the sky. Wait for the GPS module to acquire satelite signals (Fix).This can be verified by checking the Fix LED (D1) of your GPS module.

\section*{Create GPS Object}

Create a gpsdev object for the GPS receiver connected to a specific port. Specify the output format of the data as a timetable.
```

gps = gpsdev('COM4','OutputFormat',"timetable")
gps =
gpsdev with properties:
SerialPort: COM4
BaudRate: 9600 (bits/s)
SamplesPerRead: 1
ReadMode: "latest"
SamplesRead: 0
Show all properties all functions

```

\section*{Read the GPS data}

Read the GPS data and return them as a timetable.
```

[tt,overruns] = read(gps)

```


Display number of samples read and the samples available in the host buffer.
```

gps.SamplesRead
ans = 1
gps.SamplesAvailable
ans = 0

```

Release the GPS object to configure the non tunable properties. The release function also clears the buffer and resets the SamplesRead and SamplesAvailable properties.
```

release(gps)

```

Specify the number of samples per read to 2 . Read the GPS data.
```

gps.SamplesPerRead = 2;
read(gps)
ans=2\times5 timetable
Time LLA
22-Mar-2021 15:31:17.178 17.47 78.343 450
22-Mar-2021 15:31:17.178 17.47 78.343 450
GroundSpeed
Course
__
NaN
9.32
9.32

```

Display number of samples read and the samples available in the host buffer.
```

gps.SamplesRead
ans = 1
gps.SamplesAvailable
ans = 0

```

\section*{Clean Up}

When the connection is no longer needed, clear the associated object.
```

delete(gps);

```
clear gps;

\section*{More About}

GPS Modules
To verify the functionality, the following GPS modules were used:
- Adafruit Ultimate GPS
- Ublox NEO 6M
- Ublox NEO 7M

\section*{See Also}
nmeaParser
Introduced in R2020b

\section*{nmeaParser}

Parse data from standard and manufacturer-specific NMEA sentences sent from marine electronic devices

\section*{Description}

The nmeaParser System object parses data from any NMEA (National Marine Electronics Association) sentences. The sentences that need parsing of data can be any standard sentences compliant with the NMEA \(0183^{\circledR}\) specifications (which are sent from a GNSS (Global Navigation Satellite System) receiver), or other manufacturer-specific sentences approved by the NMEA (which are sent from other marine electronic devices).

The nmeaParser System object provides:
- Built-in support to parse data sent from GNSS receivers and identified by these nine NMEA message types: RMC, GGA, GSA, VTG, GLL, GST, ZDA, GSV, and HDT
- Additional configuration using the CustomSentence name-value pair to parse NMEA data from multiple device categories, including manufacturer-specific sentences from different hardware manufacturers

To parse data from NMEA sentences:
1 Create the nmeaParser object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?
The nmeaParser System object outputs an array of structures corresponding to the values extracted from the specified NMEA sentences.

\section*{Creation}

\section*{Syntax}
```

pnmea = nmeaParser
pnmea = nmeaParser("MessageIDs", 'msgID')
pnmea = nmeaParser("CustomSentence",
{['CustomMessageId1','parserFunctionName1'],
['CustomMessageId2','parserFunctionName2']})
pnmea = nmeaParser("MessageIDs", {'msgID1','msgID2'},"CustomSentence",
{['CustomMessageId1','parserFunctionNamel'],
['CustomMessageId2','parserFunctionName2']})

```

\section*{Description}
pnmea \(=\) nmeaParser returns a nmeaParser System object, pnmea, with default properties, that extracts data from these standard NMEA messages: RMC, GGA, and GSA. The order of structure arrays in the extracted output data is also: RMC, GGA, and GSA.
pnmea = nmeaParser("MessageIDs", 'msgID') returns a nmeaParser System object, pnmea, that extracts data from one of the nine standard NMEA messages with built-in support, specified using the Message IDs. Specify msgID as "RMC", "GGA", "GSA", "GSV", "VTG", "GLL", "GST", "ZDA", and "HDT", or a combination of these IDs (for example: [ "VTG" , "GLL" , "HDT"]). The order in which you specify the Message IDs determines the order of the structure arrays in the extracted output data. The default value is ["RMC", "GGA", "GSA"].
pnmea \(=\) nmeaParser("CustomSentence", \{['CustomMessageId1','parserFunctionName1'], ['CustomMessageId2','parserFunctionName2']\}) sets properties using the CustomSentence name-value pair and returns a nmeaParser System object, pnmea, that extracts data from any custom NMEA message (either standard NMEA message or manufacturer-specific NMEA message), specified using the message IDs.

The CustomSentence name-value pair accepts a nested cell array where each element is a pair of message ID name (either standard NMEA message ID name or manufacturer-specific message ID) and the corresponding user-defined parser function, which is created by including the extractNMEASentence function in a function file. The order in which you specify the message IDs determines the order of the structure arrays in the extracted output data.
pnmea \(=\) nmeaParser("MessageIDs", \{'msgID1','msgID2'\},"CustomSentence", \{['CustomMessageId1','parserFunctionName1'],
['CustomMessageId2', 'parserFunctionName2']\}) returns a nmeaParser System object, pnmea, that extracts data from two of the nine standard NMEA messages with built-in support and also from custom NMEA messages that you specified using the CustomSentence name-value pair.

\section*{Input Arguments}

\section*{Name-Value Pair Arguments}

Specify optional pairs of arguments as Namel=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
```

Example: pnmea = nmeaParser("CustomSentence",
{['CustomMessageId1','parserFunctionName1'],
['CustomMessageId2','parserFunctionName2']});

```

CustomSentence - Specify message ID of any sentence and the name of its parser function cell array of character vectors

Specify the message ID of any NMEA sentence from which you want to extract data and the name of the parser function. You can specify multiple message IDs and parser functions as a cell array of character vectors. The parser function is defined in a function file, which can optionally include the extractNMEASentence function.

Note The function file for the parser function must be present in the current directory or on MATLAB path.

CustomSentence accepts function name or function handle. For example, both these formats are valid:
- pnmea = nmeaParser('CustomSentence', \{['standardnmeaMessageId1','parserFunctionName1']\}
- parserFunctionHandle=@parserFunctionName1
```

pnmea = nmeaParser('CustomSentence', {['standardnmeaMessageId1',parserFunctionHandle]}

```

Note Using CustomSentence name-value pair to parse data instead of the built-in parser function results in override of the default fields when data is parsed. For example, nmeaParser('CustomSentence', \{["RMC", "parserRMC"]\}) overrides the default format of parsed data as RMC is one of the nine sentences with built-in support for parsing data.

Data Types: char | string

\section*{Properties}

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.
```

MessageIDs - Message IDs of nine standard NMEA sentences with built-in support to
extract data
["RMC","GGA","GSA"] (default)| RMC | GGA | GSA | GSV | VTG | GLL | GST | ZDA | HDT

```

Message IDs of nine NMEA sentences with built-in support, which are compliant with the NMEA 0183 Standard, from which you want to extract data. You can specify multiple message IDs as an array of strings to extract data from NMEA sentences.

Data Types: char | string

\section*{Usage}

\section*{Syntax}
[rmcData,ggaData,gsaData,vtgData,gllData,gstData,gsvData,zdaData,hdtData] = pnmea(rawData)
[customNmeaData1,customNmeaData2] = pnmea(rawData)

\section*{Description}
[rmcData,ggaData,gsaData,vtgData,gllData,gstData,gsvData,zdaData,hdtData] = pnmea (rawData) parses data from nine standard NMEA sentences with built-in support, and returns an array of structures, where each structure corresponds to a single Message ID. The sequence that you specify for the output arguments must be the same sequence that you specified for the Message IDs when creating the nmeaParser System object.
[customNmeaData1,customNmeaData2] = pnmea(rawData) parses data from two custom NMEA sentences (either standard NMEA sentence or manufacturer-specific NMEA sentence), and returns an array of structures, where each structure corresponds to a single Message ID. The
sequence that you specify for the output arguments must be the same sequence that you specified in the CustomSentence name-value pair when creating the nmeaParser System object.

\section*{Input Arguments}
rawData - NMEA data as obtained from a marine electronic device
string array
NMEA data, which is compliant with NMEA standard, as obtained from a marine electronic device.
Data Types: string | char
Output Arguments
rmcData - Data extracted from RMC sentence
structure
Data extracted from an RMC sentence. The output structure contains the information parsed from an RMC sentence along with the parsing status. If multiple RMC sentences are found in the input data, then an array of structures is returned. For more details, see "RMC Sentences" on page 2-689.

\section*{ggaData - Data extracted from GGA sentence \\ structure}

Data extracted from a GGA sentence. The output structure contains the information parsed from a GGA sentence along with the parsing status. If multiple GGA sentences are found in the input data, then an array of structures is returned. For more details, see "GGA Sentences" on page 2-690.

\section*{gsaData - Data extracted from GSA sentence}
structure
Data extracted from a GSA sentence. The output structure contains the information parsed from a GSA sentence along with the parsing status. If multiple GSA sentences are found in the input data, then an array of structures is returned. For more details, see "GSA Sentences" on page 2-692.

\section*{vtgData - Data extracted from VTG sentence}
structure
Data extracted from a VTG sentence. The output structure contains the information parsed from a VTG sentence along with the parsing status. If multiple VTG sentences are found in the input data, then an array of structures is returned. For more details, see "VTG Sentences" on page 2-696.

\section*{gllData - Data extracted from GLL sentence structure}

Data extracted from a GLL sentence. The output structure contains the information parsed from a GLL sentence along with the parsing status. If multiple GLL sentences are found in the input data, then an array of structures is returned. For more details, see "GLL Sentences" on page 2-695.

\section*{gstData - Data extracted from GST sentence}
structure
Data extracted from a GST sentence. The output structure contains the information parsed from a GST sentence along with the parsing status. If multiple GST sentences are found in the input data, then an array of structures is returned. For more details, see "GST Sentences" on page 2-697.

\section*{gsvData - Data extracted from GSV sentence}
structure
Data extracted from a GSV sentence. The output structure contains the information parsed from a GSV sentence along with the parsing status. The complete satellite information is available in multiple gsvData structures. Each gsvData structure can have a maximum of four satellite information. For more details, see "GSV Sentences" on page 2-693.
zdaData - Data extracted from ZDA sentence
structure
Data extracted from a ZDA sentence. The output structure contains the information parsed from a ZDA sentence along with the parsing status. If multiple ZDA sentences are found in the input data, then an array of structures is returned. For more details, see "ZDA Sentences" on page 2-695.

\section*{hdtData - Data extracted from HDT sentence}
structure
Data extracted from an HDT sentence. The output structure contains the information parsed from an HDT sentence along with the parsing status. If multiple HDT sentences are found in the input data, then an array of structures is returned. For more details, see "HDT Sentences" on page 2-698.

\section*{customNmeaDatal - Data extracted from any standard or manufacturer-specific NMEA sentence \\ structure}

Data extracted from any standard or manufacturer-specific NMEA sentence. The output structure contains the information parsed from the custom sentence along with the parsing status. If multiple sentences of the same NMEA message type are found in the input data, then an array of structures is returned.

\section*{Object Functions}

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:
```

release(obj)

```

\section*{Examples}

\section*{Extract Data from NMEA Sentences Using MessageID Property}

Extract data from any of the nine standard NMEA sentences as part of the built-in support using the MessageID property. The NMEA data is obtained from a GNSS receiver.

\section*{Extract Data from RMC Sentence}

Create an nmeaParser System Object by specifying the Message ID as "RMC".
```

pnmea = nmeaParser("MessageID","RMC");

```

Provide the RMC sentence obtained from the GNSS receiver as the input and extract data.
```

unparsedRMCLine=' \$GNRMC,143909.00,A,5107.0020216,N,11402.3294835,W,0.036,348.3,210307,0.0,E,A*31
rmcData = pnmea(unparsedRMCLine)
rmcData = struct with fields:
TalkerID: "GN"
MessageID: "RMC"
FixStatus: 'A'
Latitude: 51.1167
Longitude: -114.0388
GroundSpeed: 0.0185
TrueCourseAngle: 348.3000
UTCDateTime: 21-Mar-2007 14:39:09.000
MagneticVariation: 0
ModeIndicator: 'A'
NavigationStatus: "NA"
Status: 0

```

\section*{Extract Data from Multiple NMEA Message Types}

Provide GGA, GSA, and RMC sentences as the input.
```

unparsedGGALine = ['$GPGGA,111357.771,5231.364,N,01324.240,E,1,12,1.0,0.0,M,0.0,M, ,*69'];
unparsedGSALine = ['$GPGSA,A,3,01,02,03,04,05,06,07,08,09,10,11,12,1.0,1.0,1.0*30'];
unparsedRMCLine = ['\$GPRMC,111357.771,A,5231.364,N,01324.240,E,10903,221.5,020620,000.0,W*44'];

```

Create a string array to include the three sentences
```

rawNMEAData = [unparsedGGALine ,newline, unparsedGSALine ,newline, unparsedRMCLine]
rawNMEAData =
'\$GPGGA,111357.771,5231.364,N,01324.240,E,1,12,1.0,0.0,M,0.0,M, , *69
\$GPGSA, A , 3,01,02,03,04,05,06,07,08,09,10,11,12,1.0,1.0,1.0*30
\$GPRMC,111357.771,A,5231.364,N,01324.240,E,10903,221.5,020620,000.0,W*44'

```

However, consider that you need to extract data only from GGA and GSA sentences. So create the nmeaParser System Object 'pnmea', and specify the 'GGA' and 'GSA' Message IDs as a string array.
```

pnmea=nmeaParser("MessageIDs",["GGA","GSA"]);

```

Specify the output arguments for all the three sentences to extract the data as structures.
```

[ggaData,gsaData] = pnmea(rawNMEAData)
ggaData = struct with fields:
TalkerID: "GP"
MessageID: "GGA"
UTCTime: 11:13:57.771
Latitude: 52.5227
Longitude: 13.4040
QualityIndicator: 1
NumSatellitesInUse: 12
HDOP: 1
Altitude: 0
GeoidSeparation: 0
AgeOfDifferentialData: NaN
DifferentialReferenceStationID: NaN

```

\section*{Status: 0}
```

gsaData = struct with fields:
TalkerID: "GP"
MessageID: "GSA"
Mode: "A"
FixType: 3
SatellitesIDNumber: [1 2 3 4 5 6 7 8 9 10 11 12]
PDOP: 1
VDOP: 1
HDOP: 1
SystemID: NaN
Status: 0

```

The above output shows that only GGA and GSA sentences are extracted based on the Message IDs specified as input.

Provide another GGA sentence as an additional input, and extract data. In this case, you need not modify the System object as the Message ID has not changed.
```

unparsedGGALine1='$GNGGA,001043.00,4404.14036,N,12118.85961,W,1,12,0.98,1113.0,M,-21.3,M, ,*47'
unparsedGGALine1 =
'$GNGGA,001043.00,4404.14036,N,12118.85961,W,1,12,0.98,1113.0,M,-21.3,M, ,*47'
rawNMEAData = [unparsedGGALine ,newline, unparsedGSALine ,newline, unparsedGGALinel]
rawNMEAData =
'\$GPGGA,111357.771,5231.364,N,01324.240,E,1,12,1.0,0.0,M,0.0,M, ,*69
\$GPGSA,A,3,01,02,03,04,05,06,07,08,09,10,11,12,1.0,1.0,1.0*30
\$GNGGA,001043.00,4404.14036,N,12118.85961,W,1,12,0.98,1113.0,M,-21.3,M, ,*47'
[ggaData,gsaData] = pnmea(rawNMEAData)
ggaData=2\times1 struct array with fields:
TalkerID
MessageID
UTCTime
Latitude
Longitude
QualityIndicator
NumSatellitesInUse
HDOP
Altitude
GeoidSeparation
AgeOfDifferentialData
DifferentialReferenceStationID
Status
gsaData = struct with fields:
TalkerID: "GP"
MessageID: "GSA"
Mode: "A"
FixType: 3
SatellitesIDNumber: [11 2 3 4 5 6 7 8 9 10 11 12]

```
```

    PDOP: 1
    VDOP: 1
    HDOP: 1
    SystemID: NaN
Status: 0

```

A status of \(\mathbf{0}\) indicates that the data was parsed successfully.

\section*{Extract Data from GSV Sentence}

Create an nmeaParser System Object by specifying the Message ID as "GSV".
```

pnmea = nmeaParser("MessageID","GSV");

```

Provide the GSV sentence obtained from the GNSS receiver as the input and extract data.
```

unparsedGSVLine='\$GPGSV ,3,3,10,32,69,205,41,46,47,215,39*79';
gsvData = pnmea(unparsedGSVLine)
gsvData = struct with fields:
TalkerID: "GP"
MessageID: "GSV"
NumSentences: 3
SentenceNumber: 3
SatellitesInView: 10
SatelliteID: [32 46]
Elevation: [69 47]
Azimuth: [205 215]
SNR: [41 39]
SignalID: NaN
Status: 0

```

\section*{Extract Data from Multiple GSV Sentences}

Provide multiple GSV sentences as the input.
```

unparsedGSVLine1 = '$GPGSV,3,1,10,01, , 31,03,28,325,40,10, , ,33,12,20,047,30*70';
unparsedGSVLine2 = '$GPGSV,3,2,10,14,88,028,42,22,39,299,48,25, , ,25,31,79,289,46*49';
unparsedGSVLine3 = '\$GPGSV,3,3,10,32,69,205,41,46,47,215,39*79';

```

Create a string array to include the three sentences.
CRLF = [char(13), newline];
unparsedGSVLines = [unparsedGSVLine1,CRLF, unparsedGSVLine2, CRLF, unparsedGSVLine3];
Create the nmeaParser System Object 'pnmea', specify the 'GSV' Message ID, and extract data.
```

pnmea = nmeaParser("MessageIDs","GSV");

```
gsvData = pnmea(unparsedGSVLines)
gsvData=3×1 struct array with fields:

TalkerID
MessageID
NumSentences
SentenceNumber
SatellitesInView
SatelliteID
```

Elevation
Azimuth
SNR
SignalID
Status

```

\section*{Read Data from NMEA Log}

Read data from a sample NMEA log, so that the data can be parsed using the nmeaParser System Object.

The sample log file is nmeaLog. nmea, which is included in this example.
```

f = fopen('nmeaLog.nmea');
unParsedNMEAdata = fread(f);
pnmea = nmeaParser("MessageIDs",["RMC","GGA"]);
[rmcStruct, ggaStruct] = pnmea(unParsedNMEAdata)
rmcStruct=9\times1 struct array with fields:
TalkerID
MessageID
FixStatus
Latitude
Longitude
GroundSpeed
TrueCourseAngle
UTCDateTime
MagneticVariation
ModeIndicator
NavigationStatus
Status
ggaStruct=9\times1 struct array with fields:
TalkerID
MessageID
UTCTime
Latitude
Longitude
QualityIndicator
NumSatellitesInUse
HDOP
Altitude
GeoidSeparation
AgeOfDifferentialData
DifferentialReferenceStationID
Status

```

\section*{Extract Data Using CustomSentence Name-Value Pair}

You can extract data from any NMEA sentence using the CustomSentence name-value pair. The NMEA data to be parsed is obtained from marine electronic devices.

\section*{Identify the Structure of NMEA Sentence and Create the Parser Function}

You need to identify the structure of the NMEA sentence, as defined in the specification, and use that information to define the structure of output data to be used in the nmeaParser System object.

For example, let us consider an example sentence with Message ID, SSS.


After identifying the structure, you create a function file that defines the parser function, fsssParser. In the function file, you define the output data as a structure array with its fields matching the sequence as it appears in the specification.

The Navigation Toolbox \({ }^{\text {TM }}\) provides an optional pre-configured function, extractNMEASentence, that checks if the sentence is valid and convert the fields in the sentence into string array. You can call extractNMEASentence inside the function file. You can also use any other function instead (which outputs a string array from unparsed data), and then call it inside the function file.

The below image shows the function file with the code, with the assumption that the fields available in SSS sentence are TalkerID, MessageID, UTC, and LatitudeError. Refer the additional comments for details.
```

fsssParser.m < +
function OutputData = fsssParser(unparsedData, MessageId)
% fsssParser custom function to parse SSS sentence
% Define OutputData as a structure array with fields in the same sequence as they appear in
% SSS sentence structure
OutputData = struct('TalkerID',"",'MessageID',"",'UTC',nan,'LatitudeError',nan);
% Call another function to convert the unparsed data into string arrayl.
% To do this, use either extractNMEASentence function
% or any other function that outputs a string array.
[valid, splitString] = extractNMEASentence(unparsedData,MessageId);
% Map each field of the structure to the corresponding string element
if(valid)
OutputData.TalkerID = splitString(1);
OutputData.MessageID = splitString(2);
temp = char(splitString(3));
utcOutput = [temp(1:2), ':', temp(3:4), ':', temp(5:9)];
OutputData.UTC = utcOutput;
OutputData.LatitudeError = str2double(splitString(4));
end
end

```

In the above sample file, you define the mapping between the fields in the structure array and the elements of string array. For certain fields (for example, UTC time), you may need to define a character array to map the fields.

After you include the MATLAB code as mentioned above, save the function file (fsssParser.m) in the MATLAB path, so that you can call it to obtain parsed data using the CustomSentence name-value pair of nmeaParser System object.

To download another sample function file parserRMB.m that is used this example, click Open Live Script. This is a function file specific to the fields of an RMB sentence (mentioned in NMEA Standard, Version 4.1).

\section*{Extract Data from RMB Sentence}

Create an nmeaParser System Object by using the CustomSentence name-value pair and specifying the message ID as "RMB" and the function as "parserRMB" (downloaded in the previous step).
```

pnmea = nmeaParser("CustomSentence",{["RMB","parserRMB"]});

```

Provide the RMB sentence obtained from the GNSS receiver as the input and extract data.
```

unparsedRMBLine='\$GPRMB,A,4.08,L,EGLL,EGLM,5130.02,N,00046.34,W,004.6,213.9,122.9,A*3D';

```
rmbData \(=\) pnmea(unparsedRMBLine)
rmbData = struct with fields:
    TalkerID: "GP"
```

    MessageID: "RMB"
                    DataStatus: 'A'
            CrossTrackError: 4.0800
            DirectionToSteer: NaN
            OriginWaypointID: NaN
        DestinationWaypointID: NaN
    DestinationWaypointLatitude: '5130.02 N'
    DestinationWaypointLongitude: '00046.34 W'
RangeToDestination: 4.6000
BearingToDestination: 213.9000
DestinationClosingVelocity: 122.9000
ArrivalStatus: 'A'
ModeIndicator: "NA"
Status: 0

```

\section*{Extract Data from Multiple RMB Sentences}

Provide multiple RMB sentences as the input.
```

unparsedRMBLine1 = ['\$GPRMB,A,0.66,L,003,004,4917.24,N,12309.57,W,001.3,052.5,000.5,V*20'];

```
unparsedRMBLine2 = ['\$GPRMB,A,4.08,L,EGLL,EGLM,5130.02,N,00046.34,W,004.6,213.9,122.9,A*3D'];

Create a character array to include the two sentences
```

rawNMEAData = [unparsedRMBLine1 ,newline, unparsedRMBLine2]
rawNMEAData =
' \$GPRMB , A , 0.66,L,003,004,4917.24,N ,12309.57,W,001.3,052.5,000.5,V*20
\$GPRMB,A,4.08,L,EGLL,EGLM,5130.02,N,00046.34,W,004.6,213.9,122.9,A*3D'

```

Specify the output argument for the RMB sentence to extract the data.
```

[rmbData] = pnmea(rawNMEAData)
rmbData=2\times1 struct array with fields:
TalkerID
MessageID
DataStatus
CrossTrackError
DirectionToSteer
OriginWaypointID
DestinationWaypointID
DestinationWaypointLatitude
DestinationWaypointLongitude
RangeToDestination
BearingToDestination
DestinationClosingVelocity
ArrivalStatus
ModeIndicator
Status

```

\section*{Extract Data from a Sentence with Built-in Support (RMC) and RMB Sentence}

Create an nmeaParser System Object by using the MessageID property (to parse a sentence with built-in support - RMC) and also using the CustomSentence name-value pair (specifying the message ID as "RMB" and the function as "parserRMB" (created in a previous step)).
```

pnmea = nmeaParser("MessageID","RMC","CustomSentence",{["RMB","parserRMB"]});

```

Provide RMC and RMB sentences as the input.
```

unparsedRMCLine1 = ['\$GNRMC,143909.00,A,5107.0020216,N,11402.3294835,W,0.036,348.3,210307,0.0,E,

```
unparsedRMBLine2 \(=\left[\right.\) '\$GPRMB, \(\left.A, 4.08, L, E G L L, E G L M, 5130.02, N, 00046.34, W, 004.6,213.9,122.9, A^{*} 3 D^{\prime}\right]\);

Create a string array to include the two sentences
```

rawNMEAData = [unparsedRMCLine1 ,newline, unparsedRMBLine2]
rawNMEAData =
'\$GNRMC , 143909.00,A ,5107.0020216,N,11402.3294835,W,0.036,348.3,210307,0.0, E, A*31
\$GPRMB , A , 4.08,L,EGLL,EGLM, 5130.02,N,00046.34,W,004.6,213.9,122.9,A*3D'

```

Specify the output argument for the RMB sentence to extract the data.
```

[rmcdata,rmbData] = pnmea(rawNMEAData)
rmcdata = struct with fields:
TalkerID: "GN"
MessageID: "RMC"
FixStatus: 'A'
Latitude: 51.1167
Longitude: -114.0388
GroundSpeed: 0.0185
TrueCourseAngle: 348.3000
UTCDateTime: 21-Mar-2007 14:39:09.000
MagneticVariation: 0
ModeIndicator: 'A'
NavigationStatus: "NA"
Status: 0
rmbData = struct with fields:
TalkerID: "GP"
MessageID: "RMB"
DataStatus: 'A'
CrossTrackError: 4.0800
DirectionToSteer: NaN
OriginWaypointID: NaN
DestinationWaypointID: NaN
DestinationWaypointLatitude: '5130.02 N'
DestinationWaypointLongitude: '00046.34 W'
RangeToDestination: 4.6000
BearingToDestination: 213.9000
DestinationClosingVelocity: 122.9000
ArrivalStatus: 'A'
ModeIndicator: "NA"
Status: 0

```

\section*{Extract Data from a Manufacturer-specific Sentence Using CustomSentence Name-Value Pair}

\section*{1 Identify Structure of Manufacturer-specific Sentence and Create Function File with Parser Function}

The structure of NMEA sentence to be parsed is available in the specification of the device from the manufacturer. You need to identify the structure and use the information to define the structure of output data to be used in the nmeaParser System object.

For example, the structure of the NMEA sentence from a hardware manufacturer may look like this:
\$PMMCZ, hhmmss.ss,Latitude, N, Longitude, E,NavSatellite, DR*hh<CR><LF>
Here, P denotes that the sentence is manufacturer-specific, MMC is the manufacturer mnemonic code, and Z is the sentence type. Each field thereafter indicates a specific data (position, velocity, time, and so on). Some manufacturers use two characters for the sentence type, followed by the data fields.

After identifying the structure, create the parser function, parserMMCZ, using the optional extractNMEASentence function, as shown below (you can also use other functions to extract the unparsed data to strings, instead of extractNMEASentence).
```

function OutputData = parserMMCZ(unparsedData, MessageID)
OutputData = struct("MessageID",MessageID,...
"UTC","NA",...
"Latitude",NaN,...
"Longitude",NaN,...
"NavigationSatellites",NaN,...
"Status",uint8(1));
[isValid, splitString] = extractNMEASentence(unparsedData, MessageID);
if(isValid)
OutputData.MessageID = splitString(1);
temp = char(splitString(2));
utcOutput = [temp(1:2), ':', temp(3:4), ':', temp(5:6)];
OutputData.UTC = utcOutput;
OutputData.Latitude = str2double(splitString{3});
OutputData.Longitude = str2double(splitString{5});
OutputData.NavigationSatellites = str2double(splitString{7});
OutputData.Status = uint8(0);
end
end
Save parserMMCZ.m in the MATLAB path.

```

\section*{2 Extract Data from Manufacturer-specific Sentence}

Create an nmeaParser System Object by using the CustomSentence name-value pair and specifying the message ID as "MMCZ" and the function as "parserMMCZ" (created in the previous step).
```

pnmea = nmeaParser("CustomSentence",{["MMCZ","parserMMCZ"]});

```

Provide an MMC sentence obtained from the device as the input and extract data:
```

unparsedMMCLine='\$PMMCZ,225444,4917.24,N,00046.34,E,3,DR*7C';
mmcData = pnmea(unparsedMMCLine)
mmcData =
struct with fields:
MessageID: "MMCZ"
UTC: '22:54:44'
Latitude: 4.9172e+03
Longitude: 46.3400
NavigationSatellites: 3
Status: 0

```

\section*{More About}

\section*{Status Field}

The status field displayed along with the extracted values in each output structure can be used to determine the parsing status:
- Status: 0 - Sentence is valid (checksum validation is successful and the extracted data is as per the requested Message ID)
- Status: 1-Checksum of the sentence to be parsed is invalid
- Status: 2 - The requested sentence is not found in the input data

Note If a value is not available in the input sentence, the corresponding output value is displayed as "NA" for string values and "NaN" for numeric values.

\section*{RMC Sentences}
\begin{tabular}{|l|l|}
\hline \begin{tabular}{l} 
Name of field displayed in the output \\
structure after parsing is complete
\end{tabular} & Description \\
\hline TalkerID & \begin{tabular}{l} 
Identify the type of device that transmits data. \\
For example, for a GPS receiver, the TalkerID is \\
GP \\
Data type: string
\end{tabular} \\
\hline MessageID & \begin{tabular}{l} 
Type of NMEA message - RMC \\
Data type: string
\end{tabular} \\
\hline FixStatus & \begin{tabular}{l} 
Possible values: \\
- A - Data is valid \\
• V - Navigation receiver warning \\
Data type: string
\end{tabular} \\
\hline Latitude & \begin{tabular}{l} 
Latitude in degrees. North is considered positive. \\
Data type: double
\end{tabular} \\
\hline
\end{tabular}
\begin{tabular}{|c|c|}
\hline Name of field displayed in the output structure after parsing is complete & Description \\
\hline Longitude & \begin{tabular}{l}
Longitude in degrees. East is considered positive. \\
Data type: double
\end{tabular} \\
\hline GroundSpeed & \begin{tabular}{l}
Speed over ground in meters per second ( \(\mathrm{m} / \mathrm{s}\) ) \\
Data type: double
\end{tabular} \\
\hline TrueCourseAngle & \begin{tabular}{l}
Course over ground in degrees. \\
Data type: double
\end{tabular} \\
\hline UTCDateTime & UTC date and time Data type: datetime \\
\hline MagneticVariation & \begin{tabular}{l}
Magnetic variation value. Direction W is considered as negative \\
Data type: double
\end{tabular} \\
\hline ModeIndicator & \begin{tabular}{l}
Possible values: \\
- N - No fix \\
- E - Estimated/Dead reckoning fix \\
- A - Autonomous GNSS fix \\
- D - Differential GNSS fix \\
- F - RTK float \\
- M-Manual input mode \\
- P - Precision mode \\
Data type: string
\end{tabular} \\
\hline NavigationStatus & \begin{tabular}{l}
Possible values: \\
- S - Safe \\
- C - Caution \\
- \(\mathrm{U}=\) Unsafe \\
- \(\mathrm{V}=\) Navigational Status not valid \\
Data type: string
\end{tabular} \\
\hline
\end{tabular}

\section*{GGA Sentences}
\begin{tabular}{|l|l|}
\hline \begin{tabular}{l} 
Name of field displayed in the output \\
structure after parsing is complete
\end{tabular} & Description \\
\hline TalkerID & \begin{tabular}{l} 
Identify the type of device that transmits data. \\
For example, for a GPS receiver, the TalkerID is \\
GP \\
\\
\end{tabular} \\
\hline
\end{tabular}
\begin{tabular}{|c|c|}
\hline Name of field displayed in the output structure after parsing is complete & Description \\
\hline MessageID & Type of NMEA message - GGA Data type: string \\
\hline UTCTime & \begin{tabular}{l}
UTC Time (hhmmss.ss) \\
Data type: datetime
\end{tabular} \\
\hline Latitude & \begin{tabular}{l}
Latitude in degrees. North is considered positive. \\
Data type: double
\end{tabular} \\
\hline Longitude & \begin{tabular}{l}
Longitude in degrees. East is considered positive. \\
Data type: double
\end{tabular} \\
\hline QualityIndicator & \begin{tabular}{l}
Possible values: \\
- 0 - No fix \\
- 1 - Fix Valid \\
- 2 - Differential GPS, SPS mode fix \\
- 4 - RTK fix \\
- 5 - RTK float \\
- 6 - Estimated/Dead reckoning fix \\
- 7 - Manual input mode \\
- 8 -Simulator mode \\
Data type: uint8
\end{tabular} \\
\hline NumSatellitesInUse & \begin{tabular}{l}
Number of satellites used. This could be different from number of satellites in view. \\
Data type: uint8
\end{tabular} \\
\hline HDOP & Horizontal dilution of precision Data type: double \\
\hline Altitude & \begin{tabular}{l}
Altitude above mean sea level in meters \\
Data type: double
\end{tabular} \\
\hline GeoidSeparation & \begin{tabular}{l}
Difference between ellipsoid and mean sea level in meters \\
Data type: double
\end{tabular} \\
\hline AgeOfDifferentialData & \begin{tabular}{l}
Age of differential corrections \\
Data type: double
\end{tabular} \\
\hline DifferentialReferenceStationID & ID of station providing differential corrections Data type: uint16 \\
\hline
\end{tabular}

\section*{GSA Sentences}
\begin{tabular}{|c|c|}
\hline Name of field displayed in the output structure after parsing is complete & Description \\
\hline TalkerID & \begin{tabular}{l}
Identify the type of device that transmits data. For example, for a GPS receiver, the TalkerID is GP \\
Data type: string
\end{tabular} \\
\hline MessageID & \begin{tabular}{l}
Type of NMEA message - GSA \\
Data type: string
\end{tabular} \\
\hline Mode & \begin{tabular}{l}
Possible values: \\
- M - Manually set to operate in 2-D or 3-D mode \\
- A - Automatic switching between 2-D or 3-D mode \\
Data type: string
\end{tabular} \\
\hline FixType & Possible values:
- \(\quad 1\) - No fix
- \(2-2\)-D fix
- 3 - 3-D fix
Data type: uint8 \\
\hline SatellitesIDNumber & \begin{tabular}{l}
Satellite numbers (array of 12 bytes). Empty fields will be displayed as Nan. \\
Data type: uint8
\end{tabular} \\
\hline PDOP & \begin{tabular}{l}
Position dilution of precision \\
Data type: double
\end{tabular} \\
\hline VDOP & Vertical dilution of precision Data type: double \\
\hline HDOP & Horizontal Dilution of Precision Data type: double \\
\hline SystemID & NMEA defined GNSS System ID Data type: uint8 \\
\hline
\end{tabular}

GSV Sentences
\begin{tabular}{|l|l|}
\hline \begin{tabular}{l} 
Name of field displayed in the output \\
structure after parsing is complete
\end{tabular} & Description \\
\hline TalkerID & \begin{tabular}{l} 
Identify the type of device that transmits data. \\
For example, for a GPS receiver, the TalkerID is \\
GP
\end{tabular} \\
\hline DessageID & \begin{tabular}{l} 
Type of NMEA message - GSV \\
Data type: string
\end{tabular} \\
\hline NumSentences & \begin{tabular}{l} 
Total number of sentences. The complete satellite \\
information is available in multiple GSV \\
sentences. This field indicates the total number of \\
gsvData structures containing the complete \\
information per update.
\end{tabular} \\
\hline SentenceNumber & \begin{tabular}{l} 
Data type: double
\end{tabular} \\
\hline Sentence number of the currently parsed GSV \\
line
\end{tabular}\(|\)\begin{tabular}{l} 
Data type: double \\
\hline SatelliteID \\
\hline Total number of satellites in view \\
Data type: double \\
\hline Azimuth \\
\hline \begin{tabular}{l} 
Satellite ID numbers specified as a row vector of \\
size 1-by-N, where N is the number of satellite \\
information available in one sentence. The \\
maximum allowed valued of N is 4.
\end{tabular} \\
\hline Elevation \\
Data type: double \\
\hline
\end{tabular}
\begin{tabular}{|l|l|}
\hline \begin{tabular}{l} 
Name of field displayed in the output \\
structure after parsing is complete
\end{tabular} & Description \\
\hline SNR & \begin{tabular}{l} 
Signal-to-noise ratio in dB-Hz, specified as a row \\
vector of size 1-by-N, where N is the number of \\
satellite information available in one sentence. \\
The maximum allowed valued of N is 4. \\
The range of SNR value is [0,99] dB. \\
Data type: double
\end{tabular} \\
\hline SignalID & \begin{tabular}{l} 
Signal ID corresponding to the SatelliteID. \\
This value is displayed only if the sentences \\
conform to NMEA 0183 Standard, Version 4.1. \\
Otherwise, the value displayed is NaN.
\end{tabular} \\
\hline
\end{tabular}

The possible values of SignalID and the corresponding Signal Channel are listed in this table.
\begin{tabular}{|c|c|c|c|c|}
\hline System & TalkerID displayed in the parsed data & SatelliteID & Signalld & Signal Channel \\
\hline \multirow[t]{9}{*}{GPS} & \multirow[t]{9}{*}{GP} & \multirow[t]{9}{*}{\begin{tabular}{l}
- 1-32 (for GPS) \\
- 33-64 (for SBAS)
\end{tabular}} & 0 & All signals \\
\hline & & & 1 & L1 C/A \\
\hline & & & 2 & L1 P (Y) \\
\hline & & & 3 & L1 M \\
\hline & & & 4 & L2 P (Y) \\
\hline & & & 5 & L2C-M \\
\hline & & & 6 & L2C-L \\
\hline & & & 7 & L5-I \\
\hline & & & 8 & L5-Q \\
\hline \multirow[t]{5}{*}{GLONASS} & \multirow[t]{5}{*}{GL} & \multirow[t]{5}{*}{\begin{tabular}{l}
- 33-64 (for SBAS) \\
- 65-99 (for GLONASS)
\end{tabular}} & 0 & All signals \\
\hline & & & 1 & G1 C/A \\
\hline & & & 2 & G1 P \\
\hline & & & 3 & G2 C/A \\
\hline & & & 4 & \[
\begin{aligned}
& \text { GLONASS (M) G2 } \\
& \mathrm{P}
\end{aligned}
\] \\
\hline \multirow[t]{6}{*}{GALILEO} & \multirow[t]{6}{*}{GA} & \multirow[t]{6}{*}{\begin{tabular}{l}
- 1-36 (for Galileo satellites) \\
- 37-64 (for Galileo SBAS)
\end{tabular}} & 0 & All signals \\
\hline & & & 1 & E5a \\
\hline & & & 2 & E5b \\
\hline & & & 3 & E5a and E5b \\
\hline & & & 4 & E6-A \\
\hline & & & 5 & E6-BC \\
\hline
\end{tabular}
\begin{tabular}{|l|l|l|l|l|}
\hline System & \begin{tabular}{l} 
TalkerID \\
displayed in the \\
parsed data
\end{tabular} & SatelliteID & SignalID & Signal Channel \\
\hline & & & 6 & L1-A \\
\hline & & 7 & L1-BC \\
\hline
\end{tabular}

\section*{ZDA Sentences}
\begin{tabular}{|l|l|}
\hline \begin{tabular}{l} 
Name of field displayed in the output \\
structure after parsing is complete
\end{tabular} & Description \\
\hline TalkerID & \begin{tabular}{l} 
Identify the type of device that transmits data. \\
For example, for a GPS receiver, the TalkerID is \\
GP \\
Data type: string
\end{tabular} \\
\hline MessageID & \begin{tabular}{l} 
Type of NMEA message - ZDA \\
Data type: string
\end{tabular} \\
\hline UTCTime & \begin{tabular}{l} 
UTC Time \\
Data type: datetime
\end{tabular} \\
\hline UTCDay & \begin{tabular}{l} 
UTC Day \\
Data type: uint8
\end{tabular} \\
\hline UTCMonth & \begin{tabular}{l} 
UTC Month \\
Data type: uint8
\end{tabular} \\
\hline UTCYear & \begin{tabular}{l} 
UTC Year \\
Data type: uint8
\end{tabular} \\
\hline LocalZoneHours & Local zone hours ranging from 00 to +/-13 \\
\hline LocalZoneMinutes & Local zone minutes ranging from 00 to 59 \\
\hline
\end{tabular}

\section*{GLL Sentences}
\begin{tabular}{|l|l|}
\hline \begin{tabular}{l} 
Name of field displayed in the output \\
structure after parsing is complete
\end{tabular} & Description \\
\hline TalkerID & \begin{tabular}{l} 
Identify the type of device that transmits data. \\
For example, for a GPS receiver, the TalkerID is \\
GP
\end{tabular} \\
\hline
\end{tabular}
\begin{tabular}{|c|c|}
\hline Name of field displayed in the output structure after parsing is complete & Description \\
\hline MessageID & \begin{tabular}{l}
Type of NMEA message - GLL \\
Data type: string
\end{tabular} \\
\hline Latitude & \begin{tabular}{l}
Latitude in degrees. North is considered positive. \\
Data type: double
\end{tabular} \\
\hline Longitude & \begin{tabular}{l}
Longitude in degrees. East is considered positive. \\
Data type: double
\end{tabular} \\
\hline UTCTime & \begin{tabular}{l}
UTC Time \\
Data type: datetime
\end{tabular} \\
\hline DataValidity & \begin{tabular}{l}
Data validity status: \\
- A - Data valid \\
- V - Data invalid \\
Data type: string
\end{tabular} \\
\hline PositioningMode & \begin{tabular}{l}
Possible values: \\
- N - Data not Valid \\
- E - Estimated/Dead reckoning mode \\
- A - Autonomous mode \\
- D - Differential mode \\
- S - Simulator Mode \\
- M-Manual input mode \\
Data type: string
\end{tabular} \\
\hline
\end{tabular}

\section*{VTG Sentences}
\begin{tabular}{|l|l|}
\hline \begin{tabular}{l} 
Name of field displayed in the output \\
structure after parsing is complete
\end{tabular} & Description \\
\hline TalkerID & \begin{tabular}{l} 
Identify the type of device that transmits data. \\
For example, for a GPS receiver, the TalkerID is \\
GP \\
Data type: string
\end{tabular} \\
\hline MessageID & \begin{tabular}{l} 
Type of NMEA message - VTG \\
Data type: string
\end{tabular} \\
\hline TrueCourseAngle & \begin{tabular}{l} 
Course over ground (true) in degrees \\
Data type: double
\end{tabular} \\
\hline
\end{tabular}
\begin{tabular}{|c|c|}
\hline Name of field displayed in the output structure after parsing is complete & Description \\
\hline MagneticCourseAngle & \begin{tabular}{l}
Course over ground (magnetic) in degrees \\
Data type: double
\end{tabular} \\
\hline GroundSpeed & \begin{tabular}{l}
Speed over ground in meters per second (m/s) \\
Data type: double
\end{tabular} \\
\hline ModeIndicator & \begin{tabular}{l}
Possible values: \\
- N - No fix \\
- E - Estimated/Dead reckoning mode \\
- A - Autonomous mode \\
- D - Differential mode \\
- M-Manual input mode \\
- N - Data not valid \\
- P - Precise \\
- S - Simulator mode \\
Data type: string
\end{tabular} \\
\hline
\end{tabular}

GST Sentences
\begin{tabular}{|l|l|}
\hline \begin{tabular}{l} 
Name of field displayed in the output \\
structure after parsing is complete
\end{tabular} & Description \\
\hline TalkerID & \begin{tabular}{l} 
Identify the type of device that transmits data. \\
For example, for a GPS receiver, the TalkerID is \\
GP \\
Data type: string
\end{tabular} \\
\hline MessageID & \begin{tabular}{l} 
Type of NMEA message - GST \\
Data type: string
\end{tabular} \\
\hline UTCTime & \begin{tabular}{l} 
UTC Time \\
Data type: datetime
\end{tabular} \\
\hline RMSStdDeviationOfRanges & \begin{tabular}{l} 
RMS value of the standard deviation of the \\
ranges in meters. \\
Data type: double
\end{tabular} \\
\hline StdDeviationSemiMajorAxis & Standard deviation of semi-major axis in meters \\
Data type: double \\
\hline StdDeviationSemiMinorAxis & Standard deviation of semi-minor axis in meters \\
Data type: double \\
\hline
\end{tabular}
\begin{tabular}{|l|l|}
\hline \begin{tabular}{l} 
Name of field displayed in the output \\
structure after parsing is complete
\end{tabular} & Description \\
\hline OrientationSemiMajorAxis & \begin{tabular}{l} 
Orientation of semi-major axis, in degrees \\
Data type: double
\end{tabular} \\
\hline StdDeviationLatitudeError & \begin{tabular}{l} 
Standard deviation of latitude error, in meters \\
Data type: double
\end{tabular} \\
\hline StdDeviationLongitudeError & \begin{tabular}{l} 
Standard deviation of longitude error in meters \\
Data type: double
\end{tabular} \\
\hline StdDeviationAltitudeError & \begin{tabular}{l} 
Standard deviation of altitude error in meters \\
Data type: double
\end{tabular} \\
\hline
\end{tabular}

\section*{HDT Sentences}
\begin{tabular}{|l|l|}
\hline \begin{tabular}{l} 
Name of field displayed in the output \\
structure after parsing is complete
\end{tabular} & Description \\
\hline TalkerID & \begin{tabular}{l} 
Identify the type of device that transmits data. \\
For example, for a GPS receiver, the TalkerID is \\
GP \\
Data type: string
\end{tabular} \\
\hline MessageID & \begin{tabular}{l} 
Type of NMEA message - HDT \\
Data type: string
\end{tabular} \\
\hline TrueHeadingAngle & \begin{tabular}{l} 
Heading in degrees with respect to true north \\
Data type: double
\end{tabular} \\
\hline
\end{tabular}

\section*{See Also}
skyplot | extractNMEASentence

\section*{Topics}
"Plot Position of GNSS Receiver Using Live NMEA Data or NMEA Log File"

\section*{Introduced in R2020b}

\section*{navPath}

Planned path

\section*{Description}

The navPath object stores paths that are typically created by geometric path planners. Path points are stored as states in an associated state space.

\section*{Creation}

\section*{Syntax}
```

path = navPath
path = navPath(space)
path = navPath(space,states)

```

\section*{Description}
path = navPath creates a path object, path, using the SE2 state space with default settings.
path = navPath(space) creates a path object with state space specified by space. The space input also sets the value of the StateSpace property.
path = navPath(space,states) allows you to initialize the path with state samples given by states. Specify states as a matrix of state samples. States that are outside of the StateBounds of the state space object are reduced to the bounds. The states input also sets the value of the States property.

\section*{Properties}

\section*{StateSpace - State space for path}
stateSpaceSE2 (default) | state space object
State space for the path, specified as a state space object. Each state in the path is a sample from the specified state space. You can use objects such as stateSpaceSE2, stateSpaceDubins, or stateSpaceReedsShepp as a state space object. You can also customize a state space object using the nav.StateSpace object.
Data Types: object

\section*{States - States of path}
zeros (0,StateSpace.NumStateVariables) (default) | real-valued \(M\)-by-N matrix
States of the path, specified as a real-valued \(M\)-by- \(N\) matrix. \(M\) is the number of states in the path, and \(N\) is the dimension of each state. You can only set this property during object creation or using the append function.
Data Types: double

\section*{NumStates - Number of state samples in path}

0 (default) | nonnegative integer
Number of state samples in the path, specified as a nonnegative integer. The number is the same as the number of rows of the state matrix specified in the States property.

Data Types: double

\section*{Object Functions}
\begin{tabular}{ll} 
append & Add states to end of path \\
copy & Create copy of path object \\
interpolate & Interpolate points along path \\
pathLength & Length of path
\end{tabular}

\section*{Examples}

\section*{Create navPath Based on Multiple Waypoints}

Create a navPath object based on multiple waypoints in a Dubins space.
```

dubinsSpace = stateSpaceDubins([0 25; 0 25; -pi pi])
dubinsSpace =
stateSpaceDubins with properties:
SE2 Properties
Name: 'SE2 Dubins'
StateBounds: [3\times2 double]
NumStateVariables: 3
Dubins Vehicle Properties
MinTurningRadius: 1
pathobj = navPath(dubinsSpace)
pathobj =
navPath with properties:
StateSpace: [1x1 stateSpaceDubins]
States: [0x3 double]
NumStates: 0
waypoints = [...
8 10 pi/2;
10 12 pi/4;
12 17 pi/2;
11 10 -pi];
append(pathobj, waypoints);

```

Interpolate that path so that it contains exactly 250 points.
```

interpolate(pathobj, 250)

```

Visualize the interpolated path and the original waypoints.
figure;
grid on;
axis equal;
hold on;
plot(pathobj.States(:,1), pathobj.States(:,2), ".b");
plot(waypoints(:,1), waypoints(:,2), "*r", "MarkerSize", 10)


Calculate length of path.
len = pathLength(pathobj);
disp("Path length \(="+\) num2str(len))
Path length \(=19.37\)

\section*{See Also}
stateSpaceSE2|stateSpaceReedsShepp| stateSpaceDubins|nav.StateSpace| pathmetrics

\section*{Introduced in R2019b}

\section*{append}

Add states to end of path

\section*{Syntax}
append(path,states)

\section*{Description}
append(path, states) appends the state samples, states, to the end of the path.

\section*{Examples}

\section*{Create navPath Based on Multiple Waypoints}

Create a navPath object based on multiple waypoints in a Dubins space.
```

dubinsSpace = stateSpaceDubins([0 25; 0 25; -pi pi])

```
dubinsSpace =
    stateSpaceDubins with properties:
        SE2 Properties
                    Name: 'SE2 Dubins'
                StateBounds: [3×2 double]
        NumStateVariables: 3
        Dubins Vehicle Properties
            MinTurningRadius: 1
pathobj = navPath(dubinsSpace)
pathobj \(=\)
    navPath with properties:
        StateSpace: [1×1 stateSpaceDubins]
                States: [0x3 double]
            NumStates: 0
waypoints = [...
        810 pi/2;
        1012 pi/4;
        \(1217 \mathrm{pi} / 2\);
        1110 -pi];
append(pathobj, waypoints);

Interpolate that path so that it contains exactly 250 points.
```

interpolate(pathobj, 250)

```

Visualize the interpolated path and the original waypoints.
figure;
grid on;
axis equal;
hold on;
plot(pathobj.States(:,1), pathobj.States(:,2), ".b");
plot(waypoints(:,1), waypoints(:,2), "*r", "MarkerSize", 10)


Calculate length of path.
len = pathLength(pathobj);
disp("Path length = " + num2str(len))
Path length \(=19.37\)

\section*{Input Arguments}
path - path object
navPath object
Path object, specified as a navPath object.
Data Types: object
states - states of path
real-valued \(M\)-by- \(N\) matrix

States of the path, specified as a real-valued \(M\)-by- \(N\) matrix. \(M\) is the number of states appended to the path, and \(N\) is the dimension of each state. The dimension of each state is governed by the state space defined in the StateSpace property of navPath. States outside of the StateBounds of the state space of path are pruned to the bounds.
Example: [ 000 0; 1 1]
Data Types: double

\section*{See Also}
navPath

Introduced in R2019b

\section*{interpolate}

Interpolate points along path

\section*{Syntax}
interpolate(path, numStates)

\section*{Description}
interpolate(path, numStates) inserts a number of states in the path and ensures the distribution of all the points in the path to be uniform. The function preserves all the existing states in the path. The value of numStates must be greater than or equal to the number of existing states in the path.

\section*{Examples}

\section*{Create navPath Based on Multiple Waypoints}

Create a navPath object based on multiple waypoints in a Dubins space.
```

dubinsSpace = stateSpaceDubins([0 25; 0 25; -pi pi])
dubinsSpace =
stateSpaceDubins with properties:
SE2 Properties
Name: 'SE2 Dubins'
StateBounds: [3x2 double]
NumStateVariables: 3
Dubins Vehicle Properties
MinTurningRadius: 1
pathobj = navPath(dubinsSpace)
pathobj =
navPath with properties:
StateSpace: [1x1 stateSpaceDubins]
States: [0x3 double]
NumStates: 0
waypoints = [...
8 10 pi/2;
10 12 pi/4;
12 17 pi/2;
11 10 -pi];
append(pathobj, waypoints);

```

Interpolate that path so that it contains exactly 250 points.
interpolate(pathobj, 250)
Visualize the interpolated path and the original waypoints.
figure;
grid on;
axis equal;
hold on;
plot(pathobj.States(:,1), pathobj.States(:,2), ".b");
plot(waypoints(:,1), waypoints(:,2), "*r", "MarkerSize", 10)


Calculate length of path.
len = pathLength(pathobj);
disp("Path length = " + num2str(len))
Path length = 19.37

\section*{Input Arguments}
path - Path object
navpath object
Path object, specified as a navPath object.
Data Types: object
numStates - Number of states
nonnegative integer
Number of states inserted in the path, specified as a nonnegative integer. Its value must be greater than or equal to the number of existing states in the path.

Data Types: double

\section*{See Also}
navPath
```

Introduced in R2019b

```

\section*{pathLength}

Length of path

\section*{Syntax}
len = pathLength(path)

\section*{Description}
len \(=\) pathLength (path) returns the total length of path by summing the distances between every sequential pair of states in the path. The function uses the state space object associated with path to calculate the distance between each state pair.

\section*{Examples}

\section*{Create navPath Based on Multiple Waypoints}

Create a navPath object based on multiple waypoints in a Dubins space.
```

dubinsSpace = stateSpaceDubins([0 25; 0 25; -pi pi])
dubinsSpace =
stateSpaceDubins with properties:
SE2 Properties
Name: 'SE2 Dubins'
StateBounds: [3\times2 double]
NumStateVariables: 3
Dubins Vehicle Properties
MinTurningRadius: 1
pathobj = navPath(dubinsSpace)
pathobj =
navPath with properties:
StateSpace: [1x1 stateSpaceDubins]
States: [0x3 double]
NumStates: 0
waypoints = [...
8 10 pi/2;
10 12 pi/4;
12 17 pi/2;
11 10 -pi];
append(pathobj, waypoints);

```

Interpolate that path so that it contains exactly 250 points.
interpolate(pathobj, 250)
Visualize the interpolated path and the original waypoints.
figure;
grid on;
axis equal;
hold on;
plot(pathobj.States(:,1), pathobj.States(:,2), ".b");
plot(waypoints(:,1), waypoints(:,2), "*r", "MarkerSize", 10)


Calculate length of path.
len = pathLength(pathobj);
disp("Path length = " + num2str(len))
Path length = 19.37

\section*{Input Arguments}
path - Path object
navpath object
Path object, specified as a navPath object.
Data Types: object

\section*{Output Arguments}
len - Length of path
nonnegative scalar
Length of the path, returned as a nonnegative scalar.
See Also
navPath

Introduced in R2019b

\section*{navPathControl}

Path representing control-based kinematic trajectory

\section*{Description}

The navPathControl object stores paths that are typically created by control-based path planners like the plannerControlRRT object. The navPathControl object represents paths as a sequence of states, controls, durations, and targets. This object associates each path with a specific state propagator, which propagates the control commands to determine the resulting states.

This object specifies states and targets in the path in the state space of propagator. Controls are outputs from a controller that are used to update your systems state during propagation. This object applies each control for an associated duration. Controls can be reference signals or direct inputs to an integrator depending on your system design.

\section*{Creation}

\section*{Syntax}
```

pathObj = navPathControl(propagator)
pathObj = navPathControl(propagator,states,controls,targets,durations)

```

\section*{Description}
pathObj = navPathControl (propagator) creates a path object with the specified state propagator. The propagator argument specifies the StatePropagator
path0bj = navPathControl(propagator,states, controls,targets,durations) initializes the path with a sequence of specified states, controls, targets, and durations. The input states must have one more row than the other input vectors and matrices.

\section*{Properties}

\section*{StatePropagator - State propagator}
object of subclass of nav. StatePropagator
State propagator, specified as an object of a subclass of nav.StatePropagator. For example, the mobileRobotPropagator object represents the state space and kinematic control behavior for different mobile robot vehicle models.

Data Types: double

\section*{States - Series of states for path}
[ ] (default) | \(n\)-by-m matrix
Series of states for the path, specified as an \(n\)-by- \(m\) matrix. \(n\) is the number of points in the path. \(m\) is the dimension of the state vector.

You can specify this property at object creation by using the states argument.
Data Types: double

\section*{Controls - Control input for each state}
[ ] (default) | (n-1)-by-m matrix
Control input for each state, specified as an (n-1)-by-m matrix. \(n\) is the number of points in the path. \(m\) is the dimension of the state vector.

You can specify this property at object creation by using the controls argument.
Data Types: double
TargetStates - Target state for each state in path
[ ] (default) | (n-1)-by-m matrix
Target state for each state in the path, specified as an ( \(n-1\) )-by-m matrix. \(n\) is the number of points in the path. \(m\) is the dimension of the state vector.

You can specify this property at object creation by using the targets argument.
Data Types: double

\section*{Durations - Duration of each control input}
[ ] (default) | (n-1)-element vector in seconds
Duration of each control input, specified as an (n-1)-element vector in seconds. \(n\) is the number of points in the path.

You can specify this property at object creation by using the durations argument.
Data Types: double
NumStates - Number of states in path
0 (default) | nonnegative integer
Number of states in the path, specified as a positive integer.
Data Types: double
NumSegments - Number of segments between states
0 (default) | nonnegative integer
Number of segments between states in the path, specified as a positive integer, which must be one less than the number of states.
Data Types: double

\section*{Object Functions}
append interpolate pathDuration

Add states to end of path
Interpolate path based on propagator step size
Total elapsed duration of control path

\section*{Examples}

\section*{Plan Kinodynamic Path with Controls for Mobile Robot}

Plan control paths for a bicycle kinematic model with the mobileRobotPropagator object. Specify a map for the environment, set state bounds, and define a start and goal location. Plan a path using the control-based RRT algorithm, which uses a state propagator for planning motion and the required control commands.

\section*{Set State and State Propagator Parameters}

Load a ternary map matrix and create an occupancyMap object. Create the state propagator using the map. By default, the state propagator uses a bicycle kinematic model.
```

load('exampleMaps','ternaryMap')
map = occupancyMap(ternaryMap,10);
propagator = mobileRobotPropagator(Environment=map); % Bicycle model

```

Set the state bounds on the state space based on the map world limits.
```

propagator.StateSpace.StateBounds(1:2,:) = ...
[map.XWorldLimits; map.YWorldLimits];

```

\section*{Plan Path}

Create the path planner from the state propagator.
```

planner = plannerControlRRT(propagator);

```

Specify the start and goal states.
```

start = [10 15 0];
goal = [40 30 0];

```

Plan a path between the states. For repeatable results, reset the random number generator before planning. The plan function outputs a navPathControl object, which contains the states, control commands, and durations.
```

rng("default")
path = plan(planner,start,goal)
path =
navPathControl with properties:
StatePropagator: [1x1 mobileRobotPropagator]
States: [192x3 double]
Controls: [191x2 double]
Durations: [191x1 double]
TargetStates: [191x3 double]
NumStates: 192
NumSegments: 191

```

\section*{Visualize Results}

Visualize the map and plot the path states.
```

show(map)
hold on

```
```

plot(start(1),start(2),"rx")
plot(goal(1),goal(2),"go")
plot(path.States(:,1),path.States(:,2),"b")
hold off

```


Display the [ v psi] control inputs of forward velocity and steering angle.
plot(path.Controls)
ylim([-1 1])
legend(["Velocity (m/s)","Steering Angle (rad)"])


\section*{See Also}

Objects
navPath | mobileRobotPropagator

\section*{Functions}
append | interpolate | pathDuration
Introduced in R2021b

\section*{append}

Add states to end of path

\section*{Syntax}
append(path0bj,states, controls,durations,targets)

\section*{Description}
append(pathObj,states, controls,durations,targets) adds a sequence of states, controls, durations and targets to the end of the path. If the path is empty, the states input must have one more row than the other input vectors and matrices. If the path contains points already, the function applies the first control to the last state in the current path.

\section*{Input Arguments}

\section*{path0bj - Control path}
navControlPath
Control path, specified as a navPathControl object.
Data Types: double

\section*{states - Series of states for path}
\(n\)-by-m matrix
Series of states for the path, specified as an \(n\)-by- \(m\) matrix. \(n\) is the number of points to add to the path. \(m\) is the dimension of the state vector.

Note If the path object is empty, the states input should be an ( \(n+1\) )-by-m matrix.

Data Types: double
controls - Control input for each state
\(n\)-by-m matrix
Control input for each state, specified as an \(n\)-by- \(m\) matrix. \(n\) is the number of points to add to the path. \(m\) is the dimension of the state vector.

Data Types: double

\section*{durations - Duration of each control input}
\(n\)-element vector in seconds
Duration of each control input, specified as an \(n\)-element vector in seconds. \(n\) is the number of points to add to the path.

\section*{targets - Target state for each state in path}
\(n\)-element vector in seconds
Target state for each state in the path,specified as an \(n\)-by- \(m\) matrix. \(n\) is the number of points to add to the path. \(m\) is the dimension of the state vector.

Data Types: double

\section*{See Also}

\section*{Objects}
navPathControl|navPath | mobileRobotPropagator
Functions
interpolate|pathDuration

Introduced in R2021b

\section*{interpolate}

Interpolate path based on propagator step size

\section*{Syntax}
interpolate(path0bj)

\section*{Description}
interpolate(pathObj) evaluates the path based on the ControlStepSize property of pathObj, and adds all intermediate points to the path.

\section*{Examples}

\section*{Create navPath Based on Multiple Waypoints}

Create a navPath object based on multiple waypoints in a Dubins space.
```

dubinsSpace = stateSpaceDubins([0 25; 0 25; -pi pi])
dubinsSpace =
stateSpaceDubins with properties:
SE2 Properties
Name: 'SE2 Dubins'
StateBounds: [3\times2 double]
NumStateVariables: 3
Dubins Vehicle Properties
MinTurningRadius: 1
pathobj = navPath(dubinsSpace)
pathobj =
navPath with properties:
StateSpace: [1x1 stateSpaceDubins]
States: [0x3 double]
NumStates: 0
waypoints = [...
8 10 pi/2;
10 12 pi/4;
12 17 pi/2;
11 10 -pi];
append(pathobj, waypoints);

```

Interpolate that path so that it contains exactly 250 points.
```

interpolate(pathobj, 250)

```

Visualize the interpolated path and the original waypoints.
figure;
grid on;
axis equal;
hold on;
plot(pathobj.States(:,1), pathobj.States(:,2), ".b");
plot(waypoints(:,1), waypoints(:,2), "*r", "MarkerSize", 10)


Calculate length of path.
```

len = pathLength(pathobj);
disp("Path length = " + num2str(len))
Path length = 19.37

```

\section*{Input Arguments}

\section*{pathObj - Control path object}
navControlPath object
Control path, specified as a navPathControl object.
Data Types: double

\section*{See Also}

\author{
Objects \\ navPathControl|navPath|mobileRobotPropagator \\ Functions \\ append | pathDuration \\ Introduced in R2021b
}

\section*{pathDuration}

Total elapsed duration of control path

\section*{Syntax}
totalTime \(=\) pathDuration (pathObj)

\section*{Description}
totalTime = pathDuration(path0bj) returns the total elapsed duration of the control path.

\section*{Input Arguments}
path0bj - Control path object
navControlPath object
Control path, specified as a navPathCont rol object.
Data Types: double

\section*{Output Arguments}

\section*{totalTime - Total duration of control path}
positive scalar
Total duration of the control path, returned as a positive scalar in seconds.
Data Types: double

\section*{See Also}

\section*{Objects}
navPathControl|navPath | mobileRobotPropagator
Functions
append | interpolate
Introduced in R2021b

\section*{nav.StatePropagator class}

Package: nav
State propagator for control-based planning

\section*{Description}

The nav.StatePropagator class is an interface for all state propagators used with the kinodynamic path planners derived from nav. StateSpace. Derive from this class if you are defining a propagator for your custom motion model or control system. For a concrete implementation for mobile robots, see the mobileRobotPropagator object.

This class generates controls, propagates state, and estimates cost or distance between states. Controlled systems utilize two main equations for two steps:

\section*{Initial Control}
- [u(i), steps] = controlFcn(q(i-1),u(i-1), qTgt) generates the next control command from the previous state, control input, and target state.

\section*{Propagate the System}
- \(q(i)=q(i-1)+i n t e g r a t e(q, u(i)\), steps \()\) propagates the state \(q(i-1)\) using the generated command \(u(i)\) for the specified number of steps. The propagator uses a fixed step size, specified by the ControlStepSize property.

The propagateWhileValid method defines the integration and optionally, the control behavior, and also checks whether the generated states are valid within the state space. To skip state validation, use the propagate method.

When creating an instance of class, specify the StateSpace property, which defines the number of state variables, state bounds, and sampling behavior of the propagator. Also, specify the control limits on creation, which determines the value of the NumControlOutput property.

When you change properties, such as the state space, you may need to change the internal behavior of the propagator. To do this, implement the changes in the setup method and call setup (obj) before calling other methods again.

The nav.StatePropagator class is a handle class.

\section*{Creation}

\section*{Syntax}
propagator0bj = nav.StatePropagator(stateSpace,stepSize, numControlOutput)

\section*{Description}
propagatorObj = nav.StatePropagator(stateSpace,stepSize,numControlOutput) creates a state propagator object for propagating a kinodynamic system.

\section*{Properties}

\section*{Public Properties}

\section*{StateSpace - State space for sampling during planning}
object of subclass of nav. StateSpace
State space for sampling during planning, specified as an object of a subclass of nav.StateSpace.
The state space is responsible for representing configuration space of a system. The class should include all state information related to the propagated system. Systems employing multi-layer cascade controllers can append persistent low-level control information directly to the state vector, whereas the state propagator directly manages top-level control commands.

\section*{ControlStepSize - Duration of each control command}
0.1 (default) | positive scalar

Duration of each control command, specified as a positive scalar.

\section*{Protected Properties}

NumControlOutput - Number of variables in control command
positive integer
Number of variables in the control command, specified as a positive integer.

\section*{Attributes:}
\begin{tabular}{ll} 
GetAccess & protected \\
SetAccess & immutable
\end{tabular}

\section*{Methods}

\section*{Public Methods}
\begin{tabular}{ll} 
distance & Estimate cost of propagating to target state \\
propagate & Propagate system without validation \\
propagateWhileValid & Propagate system and return valid motion \\
sampleControl & Generate control command and step count \\
setup & Estimate cost of propagating to target state
\end{tabular}

\section*{See Also}

\section*{Classes}
nav.StateSpace|nav.StateValidator
Objects
stateSpaceSE2|stateSpaceDubins|stateSpaceReedsShepp|validator0ccupancyMap | validatorVehicleCostmap

Introduced in R2021b

\section*{distance}

Class: nav.StatePropagator
Package: nav
Estimate cost of propagating to target state

\section*{Syntax}
h = distance(q1,q2)

\section*{Description}
\(h=\) distance \((q 1, q 2)\) estimates the cost of propagating from an initial set of states \(q 1\) to final states q2. Each row in q1 and q2 represents a specific state in the system and the number of columns matches the number of state variables. The function outputs an \(n\)-element vector h for each q 1 -q2 pair.

\section*{Input Arguments}

\section*{q1 - Initial states}
\(n\)-by-s matrix
Initial states, specified as an \(n\)-by-s matrix.

\section*{q2 - Final states}
\(n\)-by-s matrix
Final states, specified as an \(n\)-by-s matrix.

\section*{Output Arguments}

\section*{h - Cost values}
\(n\)-element vector
Cost values, returned as an \(n\)-element vector, where \(n\) is the number of q1-q2 pairs.
Cost values returned by this function are typically used to find the nearest neighbor for sampled target states when planning.

\section*{Attributes}

Abstract
true
To learn about attributes of methods, see Method Attributes.

\section*{See Also}

\section*{Classes}
nav.StatePropagator|nav.StateSpace|nav.StateValidator
Functions
propagate | propagateWhileValid | sampleControl| setup

Introduced in R2021b

\section*{propagate}

Class: nav.StatePropagator
Package: nav
Propagate system without validation

\section*{Syntax}
[q,u,steps] = propagate(sp0bj,q0,u0,qTgt,maxSteps)

\section*{Description}
[q,u,steps] = propagate(sp0bj,q0,u0,qTgt,maxSteps) iteratively propagates the system from the current state \(q 0\) towards a target state qTgt with an initial control input u0for a maximum number of steps maxSteps. All propagations are validated and the function returns system information between q 0 and the last valid state.

At the end of each propagation step \(i\), the system returns:
- \(q(i,:)\) - Current state of the system
- u(i,: ) - Control input for step \(i+1\)
- \(\operatorname{steps}(i)-\) Number of steps between \(i-1\) and \(i\)

\section*{Input Arguments}

\section*{spObj - State propagator object}
handle from child class of nav. StatePropagator
State propagator object, specified as a handle from a child class of nav.StatePropagator.

\section*{q0 - Initial state}
\(s\)-element vector
Initial state of the system, specified as an \(s\)-element vector, where \(s\) is the number of state variables in the state space.

\section*{u0 - Initial control on the initial state}
\(c\)-element vector
Initial control input, specified as an \(c\)-element vector, where \(c\) is the number of control inputs.

\section*{qTgt - Target state}
\(s\)-element vector
Target state of the system, specified as an \(s\)-element vector, where \(s\) is the number of state variables in the state space.

\section*{maxSteps - Maximum number of steps}
positive scalar

Maximum number of steps, specified as a positive scalar.

\section*{Output Arguments}

\section*{q - Propagated states}
\(n\)-by-s matrix
Initial state of the system, specified as an \(s\)-element vector, where \(s\) is the number of state variables in the state space.
u - Control inputs for propagating states
\(n\)-by-c matrix
Control inputs for propagating states, specified as an \(s\)-element vector, where \(c\) is the number of control inputs.
steps - Number of steps between each state and control input
\(n\)-element vector of positive integers
Number of steps between each state and control input, specified as an \(n\)-element vector of positive integers.

\section*{Attributes}

Abstract
true
To learn about attributes of methods, see Method Attributes.

\section*{See Also}

\section*{Classes}
nav.StatePropagator|nav.StateSpace|nav.StateValidator
Functions
distance | propagateWhileValid| sampleControl| setup
Introduced in R2021b

\section*{propagateWhileValid}

Class: nav.StatePropagator
Package: nav
Propagate system and return valid motion

\section*{Syntax}
[q,u,steps] = propagateWhileValid(sp0bj,q0,u0,qTgt,maxSteps)

\section*{Description}
[q,u,steps] = propagateWhileValid(sp0bj,q0,u0,qTgt,maxSteps) iteratively propagates the system from the current state q0 towards a target state qTgt with an initial control input u0for a maximum number of steps maxSteps. All propagations are validated and the function returns system information between q 0 and the last valid state.

At the end of each propagation step \(i\), the system returns:
- \(q(i,:)\) - Current state of the system
- u(i,:) - Control input for step \(i+1\)
- steps(i) - Number of steps between \(i-1\) and \(i\)

\section*{Input Arguments}

\section*{spObj - State propagator object}
handle from child class of nav. StatePropagator
State propagator object, specified as a handle from a child class of nav.StatePropagator.

\section*{q0 - Initial state}
\(s\)-element vector
Initial state of the system, specified as an \(s\)-element vector, where \(s\) is the number of state variables in the state space.

\section*{u0 - Initial control on the initial state}
\(c\)-element vector
Initial control input, specified as an \(c\)-element vector, where \(c\) is the number of control inputs.

\section*{qTgt - Target state}
\(s\)-element vector
Target state of the system, specified as an \(s\)-element vector, where \(s\) is the number of state variables in the state space.

\section*{maxSteps - Maximum number of steps}
positive scalar

Maximum number of steps, specified as a positive scalar.

\section*{Output Arguments}

\section*{q - Propagated states}
n-by-s matrix
Initial state of the system, specified as an \(s\)-element vector, where \(s\) is the number of state variables in the state space.
u - Control inputs for propagating states
\(n\)-by-c matrix
Control inputs for propagating states, specified as an \(s\)-element vector, where \(c\) is the number of control inputs.
steps - Number of steps between each state and control input
\(n\)-element vector of positive integers
Number of steps between each state and control input, specified as an \(n\)-element vector of positive integers.

\section*{Attributes}

Abstract
true
To learn about attributes of methods, see Method Attributes.

\section*{See Also}

\section*{Classes}
nav.StatePropagator|nav.StateSpace|nav.StateValidator
Functions
distance | propagate | sampleControl| setup
Introduced in R2021b

\section*{sampleControl}

Class: nav.StatePropagator
Package: nav
Generate control command and step count

\section*{Syntax}
[u,steps] = sampleControl(sp0bj,q0,u0,qTgt)

\section*{Description}
[u,steps] = sampleControl(sp0bj,q0,u0,qTgt) generates a series of control commands and number of steps to move from the current state q0 with control command \(u 0\) towards the target state qTgt

\section*{Input Arguments}

\section*{spObj - State propagator object}
handle from child class of nav. StatePropagator
State propagator object, specified as a handle from a child class of nav.StatePropagator.

\section*{q0 - Initial state}
\(s\)-element vector
Initial state of the system, specified as an \(s\)-element vector, where \(s\) is the number of state variables in the state space.

\section*{u0 - Initial control on the initial state}
\(c\)-element vector
Initial control input, specified as an \(c\)-element vector, where \(c\) is the number of control inputs.
qTgt - Target state
\(s\)-element vector
Target state of the system, specified as an \(s\)-element vector, where \(s\) is the number of state variables in the state space.

\section*{Output Arguments}

\section*{u - Control inputs for propagating states}
\(n\)-by-c matrix
Control inputs for propagating states, specified as an \(s\)-element vector, where \(c\) is the number of control inputs.
steps - Number of steps between each state and control input
\(n\)-element vector of positive integers

Number of steps between each state and control input, specified as an \(n\)-element vector of positive integers.

\section*{Attributes}

Abstract true
To learn about attributes of methods, see Method Attributes.

\section*{See Also}

\section*{Classes}
nav.StatePropagator|nav.StateSpace|nav.StateValidator
Functions
distance | propagate | propagateWhileValid| setup

Introduced in R2021b

\section*{setup}

Class: nav.StatePropagator
Package: nav
Estimate cost of propagating to target state

\section*{Syntax}
setup(mobileProp)

\section*{Description}
setup (mobileProp) sets up the nav. StatePropagator object based on the specified parameters. If you change properties on the object, call this method before you sample controls, propagate the system, or calculate distances.

\section*{Input Arguments}
spObj - State propagator object
handle from child class of nav. StatePropagator
State propagator object, specified as a handle from a child class of nav. StatePropagator.

\section*{See Also}

\section*{Classes}
nav.StatePropagator|nav.StateSpace|nav.StateValidator
Functions
distance | propagate | propagateWhileValid| sampleControl
Introduced in R2021b

\section*{nav.StateSpace class}

Package: nav
Create state space for path planning

\section*{Description}

The nav.StateSpace class is an interface for state spaces used for path planning. Derive from this class if you want to define your own state space. This representation allows for sampling, interpolation, and calculating distances between spaces in the state space.

To create a sample template for generating your own state space class, call createPlanningTemplate. For specific implementations of the state validator class for general application, see State Spaces in "Motion Planning".

The nav. StateSpace class is a handle class.

\section*{Class Attributes}

Abstract true
For information on class attributes, see "Class Attributes".

\section*{Creation}

\section*{Syntax}
ssObj = nav.StateSpace(Name,NumStateVariables,StateBounds)

\section*{Description}
ssObj = nav.StateSpace(Name,NumStateVariables,StateBounds) creates a state space object with a given name, number of state variables, and state bounds. This constructor can only be called from a derived class. Create your own class definition using createPlanningTemplate.

\section*{Properties}

\section*{Public Properties}

NumStateVariables - Number of variables in state space
positive numeric scalar
Number of variables in the state space, specified as a positive numeric scalar. This property is the dimension of the state space.

Example: 3

\section*{Attributes:}

SetAccess
immutable

\section*{StateBounds - Minimum and maximum bounds of state variables}
[min max]|n-by-2 matrix
Minimum and maximum bounds of state variables, specified as a [min max] \(n\)-by- 2 matrix. This property depends on NumStateVariables, where \(n\) is the number of state variables. When specifying on construction, use the Bounds input.

Example: [-10 10; -10 10; -pi pi]
Attributes:
```

GetAccess
public
SetAccess protected
Dependent
true
Data Types: double

```

\section*{Protected Properties}

\section*{Name - Name of state space object}
string scalar | character vector
Name of the state space object, specified as a string scalar or character vector.
Example: "customSE2StateSpace"
```

Attributes:
GetAccess protected
SetAccess protected

```

\section*{Methods}

Public Methods
\begin{tabular}{ll} 
copy & Copy array of handle objects \\
distance & Distance between two states \\
enforceStateBounds & Limit state to state bounds \\
interpolate & Interpolate between states \\
sampleGaussian & Sample state using Gaussian distribution \\
sampleUniform & Sample state using uniform distribution
\end{tabular}

\section*{Examples}

\section*{Create Custom State Space for Path Planning}

This example shows how to use the createPlanningTemplate function to generate a template for customizing your own state space definition and sampler to use with path planning algorithms. A simple implementation is provided with the template.

Call the create template function. This function generates a class definition file for you to modify for your own implementation.
```

createPlanningTemplate

```

\section*{Class and Property Definition}

The first part of the template specifies the class definition and any properties for the class. Derive from the nav. StateSpace class. For this example, create a property for the uniform and normal distributions. You can specify any additional user-defined properties here.
```

classdef MyCustomStateSpace < nav.StateSpace \& ...
matlabshared.planning.internal.EnforceScalarHandle
properties
UniformDistribution
NormalDistribution
% Specify additional properties here
end

```

Save your custom state space class and ensure your file name matches the class name.

\section*{Class Constructor}

Use the constructor to set the name of the state space, the number of state variables, and define its boundaries. Alternatively, you can add input arguments to the function and pass the variables in when you create an object.
- For each state variable, define the [min max] values for the state bounds.
- Call the constructor of the base class.
- For this example, you specify the normal and uniform distribution property values using predefined NormalDistribution and UniformDistribution classes.
- Specify any other user-defined property values here.
```

methods

```
    function obj = MyCustomStateSpace
        spaceName = "MyCustomStateSpace";
        numStateVariables = 3;
        stateBounds = [-100 100; \% [min max]
        -100 100;
        -100 100];
            obj@nav.StateSpace(spaceName, numStateVariables, stateBounds);
        obj.NormalDistribution = matlabshared.tracking.internal.NormalDistribution(numStateVarial
        obj.UniformDistribution = matlabshared.tracking.internal.UniformDistribution(numStateVar:
        \% User-defined property values here
    end

\section*{Copy Semantics}

Specify the copy method definition. Copy all the values of your user-defined variables into a new object, so copyObj is a deep copy. The default behavior given in this example creates a new copy of the object with the same name, state bounds, and distributions.
```

function copyObj = copy(obj)
copyObj = feval(class(obj));
copyObj.StateBounds = obj.StateBounds;
copyObj.UniformDistribution = obj.UniformDistribution.copy;
copyObj.NormalDistribution = obj.NormalDistribution.copy;
end

```

\section*{Enforce State Bounds}

Specify how to ensure states are always within the state bounds. For this example, the state values get saturated at the minimum or maximum values for the state bounds.
```

function boundedState = enforceStateBounds(obj, state)
nav.internal.validation.validateStateMatrix(state, nan, obj.NumStateVariables, "enforceState
boundedState = state;
boundedState = min(max(boundedState, obj.StateBounds(:,1)'), ...
obj.StateBounds(:,2)');

```
end

\section*{Sample Uniformly}

Specify the behavior for sampling across a uniform distribution. support multiple syntaxes to constrain the uniform distribution to a nearby state within a certain distance and sample multiple states.
```

STATE = sampleUniform(OBJ)
STATE = sampleUniform(OBJ,NUMSAMPLES)
STATE = sampleUniform(OBJ,NEARSTATE,DIST)
STATE = sampleUniform(OBJ,NEARSTATE,DIST,NUMSAMPLES)

```

For this example, use a validation function to process a varargin input that handles the varying input arguments.
```

function state = sampleUniform(obj, varargin)
narginchk(1,4);
[numSamples, stateBounds] = obj.validateSampleUniformInput(varargin{:});
obj.UniformDistribution.RandomVariableLimits = stateBounds;
state = obj.UniformDistribution.sample(numSamples);
end

```

\section*{Sample from Gaussian Distribution}

Specify the behavior for sampling across a Gaussian distribution. Support multiple syntaxes for sampling a single state or multiple states.
```

STATE = sampleGaussian(OBJ, MEANSTATE, STDDEV)
STATE = sampleGaussian(OBJ, MEANSTATE, STDDEV, NUMSAMPLES)
function state = sampleGaussian(obj, meanState, stdDev, varargin)
narginchk(3,4);
[meanState, stdDev, numSamples] = obj.validateSampleGaussianInput(meanState, stdDev, varargi।
obj.NormalDistribution.Mean = meanState;
obj.NormalDistribution.Covariance = diag(stdDev.^2);
state = obj.NormalDistribution.sample(numSamples);
state = obj.enforceStateBounds(state);
end

```

\section*{Interpolate Between States}

Define how to interpolate between two states in your state space. Use an input, fraction, to determine how to sample along the path between two states. For this example, define a basic linear interpolation method using the difference between states.
```

function interpState = interpolate(obj, state1, state2, fraction)
narginchk(4,4);
[state1, state2, fraction] = obj.validateInterpolateInput(state1, state2, fraction);
stateDiff = state2 - statel;
interpState = state1 + fraction' * stateDiff;
end

```

\section*{Calculate Distance Between States}

Specify how to calculate the distance between two states in your state space. Use the statel and state2 inputs to define the start and end positions. Both inputs can be a single state (row vector) or multiple states (matrix of row vectors). For this example, calculate the distance based on the Euclidean distance between each pair of state positions.
```

function dist = distance(obj, state1, state2)
narginchk(3,3);
nav.internal.validation.validateStateMatrix(statel, nan, obj.NumStateVariables, "distance",
nav.internal.validation.validateStateMatrix(state2, size(state1,1), obj.NumStateVariables,
stateDiff = bsxfun(@minus, state2, state1);
dist = sqrt( sum( stateDiff.^2, 2 ) );
end
Terminate the methods and class sections.

```
end
end
Save your state space class definition. You can now use the class constructor to create an object for your state space.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® \({ }^{\circledR}\) Coder \(^{\text {TM }}\).

\section*{See Also}
nav.StateValidator| stateSpaceSE2| stateSpaceDubins| stateSpaceReedsShepp

Introduced in R2019b

\section*{distance}

Class: nav.StateSpace
Package: nav
Distance between two states

\section*{Syntax}
dist = distance(ss0bj,state1,state2)

\section*{Description}
dist \(=\) distance(ss0bj, state1,state2) calculates the distance between two states.

\section*{Input Arguments}
ssObj - State space object
object of a subclass of nav. StateSpace
State space object, specified as an object of a subclass of nav. StateSpace.
statel - Initial state position
\(n\)-element vector | \(m\)-by- \(n\) matrix of row vectors
Initial state position, specified as a \(n\)-element vector or \(m\)-by- \(n\) matrix of row vectors. \(n\) is the dimension of the state space specified in the NumStateVariables property of ssObj. \(m\) is the number of state positions provided.

If specified as a matrix, state1 and state2 should have the same dimensions.

\section*{state2 - Final state position}
\(n\)-element vector | \(m\)-by- \(n\) matrix of row vectors
Final state position, specified as a \(n\)-element vector or \(m\)-by- \(n\) matrix of row vectors. \(n\) is the dimension of the state space specified in the NumStateVariables property of ssObj. m is the number of state positions provided.

If specified as a matrix, statel and state2 should have the same dimensions.

\section*{Output Arguments}

\section*{dist - Distance between two states}
numeric scalar | \(m\)-element vector
Distance between two states, returned as a numeric scalar or \(m\)-element vector. This distance calculation is the main component of evaluating costs of paths.

\section*{Examples}

\section*{Create Custom State Space for Path Planning}

This example shows how to use the createPlanningTemplate function to generate a template for customizing your own state space definition and sampler to use with path planning algorithms. A simple implementation is provided with the template.

Call the create template function. This function generates a class definition file for you to modify for your own implementation.
```

createPlanningTemplate

```

\section*{Class and Property Definition}

The first part of the template specifies the class definition and any properties for the class. Derive from the nav. StateSpace class. For this example, create a property for the uniform and normal distributions. You can specify any additional user-defined properties here.
```

classdef MyCustomStateSpace < nav.StateSpace \& ...
matlabshared.planning.internal.EnforceScalarHandle
properties
UniformDistribution
NormalDistribution
% Specify additional properties here
end

```

Save your custom state space class and ensure your file name matches the class name.

\section*{Class Constructor}

Use the constructor to set the name of the state space, the number of state variables, and define its boundaries. Alternatively, you can add input arguments to the function and pass the variables in when you create an object.
- For each state variable, define the [min max] values for the state bounds.
- Call the constructor of the base class.
- For this example, you specify the normal and uniform distribution property values using predefined NormalDistribution and UniformDistribution classes.
- Specify any other user-defined property values here.
```

methods
function obj = MyCustomStateSpace
spaceName = "MyCustomStateSpace";
numStateVariables = 3;
stateBounds = [-100 100; % [min max]
-100 100;
-100 100];
obj@nav.StateSpace(spaceName, numStateVariables, stateBounds);
obj.NormalDistribution = matlabshared.tracking.internal.NormalDistribution(numStateVarial
obj.UniformDistribution = matlabshared.tracking.internal.UniformDistribution(numStateVar
% User-defined property values here
end

```

\section*{Copy Semantics}

Specify the copy method definition. Copy all the values of your user-defined variables into a new object, so copy 0 bj is a deep copy. The default behavior given in this example creates a new copy of the object with the same name, state bounds, and distributions.
```

function copyObj = copy(obj)
copy0bj = feval(class(obj));
copyObj.StateBounds = obj.StateBounds;
copyObj.UniformDistribution = obj.UniformDistribution.copy;
copyObj.NormalDistribution = obj.NormalDistribution.copy;
end

```

\section*{Enforce State Bounds}

Specify how to ensure states are always within the state bounds. For this example, the state values get saturated at the minimum or maximum values for the state bounds.
```

function boundedState = enforceStateBounds(obj, state)
nav.internal.validation.validateStateMatrix(state, nan, obj.NumStateVariables, "enforceState
boundedState = state;
boundedState = min(max(boundedState, obj.StateBounds(:,1)'), ...
obj.StateBounds(:,2)');
end

```

\section*{Sample Uniformly}

Specify the behavior for sampling across a uniform distribution. support multiple syntaxes to constrain the uniform distribution to a nearby state within a certain distance and sample multiple states.
```

STATE = sampleUniform(OBJ)
STATE = sampleUniform(OBJ,NUMSAMPLES)
STATE = sampleUniform(OBJ,NEARSTATE,DIST)
STATE = sampleUniform(OBJ,NEARSTATE,DIST,NUMSAMPLES)

```

For this example, use a validation function to process a varargin input that handles the varying input arguments.
```

function state = sampleUniform(obj, varargin)
narginchk(1,4);
[numSamples, stateBounds] = obj.validateSampleUniformInput(varargin{:});
obj.UniformDistribution.RandomVariableLimits = stateBounds;
state = obj.UniformDistribution.sample(numSamples);
end

```

\section*{Sample from Gaussian Distribution}

Specify the behavior for sampling across a Gaussian distribution. Support multiple syntaxes for sampling a single state or multiple states.
```

STATE = sampleGaussian(OBJ, MEANSTATE, STDDEV)
STATE = sampleGaussian(OBJ, MEANSTATE, STDDEV, NUMSAMPLES)
function state = sampleGaussian(obj, meanState, stdDev, varargin)
narginchk(3,4);

```
```

[meanState, stdDev, numSamples] = obj.validateSampleGaussianInput(meanState, stdDev, varargi।
obj.NormalDistribution.Mean = meanState;
obj.NormalDistribution.Covariance = diag(stdDev.^2);
state = obj.NormalDistribution.sample(numSamples);
state = obj.enforceStateBounds(state);

```
end

\section*{Interpolate Between States}

Define how to interpolate between two states in your state space. Use an input, fraction, to determine how to sample along the path between two states. For this example, define a basic linear interpolation method using the difference between states.
```

function interpState = interpolate(obj, state1, state2, fraction)
narginchk(4,4);
[state1, state2, fraction] = obj.validateInterpolateInput(state1, state2, fraction);
stateDiff = state2 - state1;
interpState = state1 + fraction' * stateDiff;
end

```

\section*{Calculate Distance Between States}

Specify how to calculate the distance between two states in your state space. Use the statel and state2 inputs to define the start and end positions. Both inputs can be a single state (row vector) or multiple states (matrix of row vectors). For this example, calculate the distance based on the Euclidean distance between each pair of state positions.
```

function dist = distance(obj, state1, state2)
narginchk(3,3);
nav.internal.validation.validateStateMatrix(state1, nan, obj.NumStateVariables, "distance",
nav.internal.validation.validateStateMatrix(state2, size(state1,1), obj.NumStateVariables,
stateDiff = bsxfun(@minus, state2, state1);
dist = sqrt( sum( stateDiff.^2, 2 ) );
end

```

Terminate the methods and class sections.
end
end
Save your state space class definition. You can now use the class constructor to create an object for your state space.

\section*{See Also}
nav.StateSpace|nav.StateValidator|stateSpaceSE2| stateSpaceDubins| stateSpaceReedsShepp

Introduced in R2019b

\section*{enforceStateBounds}

Class: nav.StateSpace
Package: nav
Limit state to state bounds

\section*{Syntax}
boundedState \(=\) enforceStateBounds(ss0bj,state)

\section*{Description}
boundedState \(=\) enforceStateBounds(ssObj, state) returns a bounded state that lies inside the state bounds based on the given state. Use this method to define specific bounding behavior like wrapping angular states. The bounds are specified in the StateBounds property of ssObj.

\section*{Input Arguments}

\section*{ssObj - State space object}
object of a subclass of nav. StateSpace
State space object, specified as an object of a subclass of nav. StateSpace.

\section*{state - State position}
\(n\)-element vector | \(m\)-by- \(n\) matrix of row vectors
State position, specified as a \(n\)-element vector or an \(m\)-by- \(n\) matrix of row vectors. \(n\) is the dimension of the state space specified in the NumStateVariables property of ssObj.

\section*{Output Arguments}

\section*{boundedState - State position with enforced state bounds}
\(n\)-element vector | \(m\)-by- \(n\) matrix of row vectors
State position with enforced state bounds, specified as a \(n\)-element vector or \(m\)-by-n matrix of row vectors. \(n\) is the dimension of the state space specified in the NumStateVariables property of ss0bj.

\section*{Examples}

\section*{Create Custom State Space for Path Planning}

This example shows how to use the createPlanningTemplate function to generate a template for customizing your own state space definition and sampler to use with path planning algorithms. A simple implementation is provided with the template.

Call the create template function. This function generates a class definition file for you to modify for your own implementation.
```

createPlanningTemplate

```

\section*{Class and Property Definition}

The first part of the template specifies the class definition and any properties for the class. Derive from the nav. StateSpace class. For this example, create a property for the uniform and normal distributions. You can specify any additional user-defined properties here.
```

classdef MyCustomStateSpace < nav.StateSpace \& ...
matlabshared.planning.internal.EnforceScalarHandle
properties
UniformDistribution
NormalDistribution
% Specify additional properties here
end

```

Save your custom state space class and ensure your file name matches the class name.

\section*{Class Constructor}

Use the constructor to set the name of the state space, the number of state variables, and define its boundaries. Alternatively, you can add input arguments to the function and pass the variables in when you create an object.
- For each state variable, define the [min max] values for the state bounds.
- Call the constructor of the base class.
- For this example, you specify the normal and uniform distribution property values using predefined NormalDistribution and UniformDistribution classes.
- Specify any other user-defined property values here.
methods
function obj = MyCustomStateSpace
spaceName = "MyCustomStateSpace";
numStateVariables = 3;
stateBounds = [-100 100; \% [min max]
-100 100; -100 100];
obj@nav.StateSpace(spaceName, numStateVariables, stateBounds);
obj. NormalDistribution = matlabshared.tracking.internal. NormalDistribution(numStateVarial
obj.UniformDistribution = matlabshared.tracking.internal.UniformDistribution(numStateVar
\% User-defined property values here
end

\section*{Copy Semantics}

Specify the copy method definition. Copy all the values of your user-defined variables into a new object, so copyObj is a deep copy. The default behavior given in this example creates a new copy of the object with the same name, state bounds, and distributions.
```

function copy0bj = copy(obj)
copy0bj = feval(class(obj));
copyObj.StateBounds = obj.StateBounds;
copyObj.UniformDistribution = obj.UniformDistribution.copy;
copyObj.NormalDistribution = obj.NormalDistribution.copy;
end

```

\section*{Enforce State Bounds}

Specify how to ensure states are always within the state bounds. For this example, the state values get saturated at the minimum or maximum values for the state bounds.
```

function boundedState = enforceStateBounds(obj, state)
nav.internal.validation.validateStateMatrix(state, nan, obj.NumStateVariables, "enforceState
boundedState = state;
boundedState = min(max(boundedState, obj.StateBounds(:,1)'), ...
obj.StateBounds(:,2)');

```
end

\section*{Sample Uniformly}

Specify the behavior for sampling across a uniform distribution. support multiple syntaxes to constrain the uniform distribution to a nearby state within a certain distance and sample multiple states.
```

STATE = sampleUniform(OBJ)
STATE = sampleUniform(OBJ,NUMSAMPLES)
STATE = sampleUniform(OBJ,NEARSTATE,DIST)
STATE = sampleUniform(OBJ,NEARSTATE,DIST,NUMSAMPLES)

```

For this example, use a validation function to process a varargin input that handles the varying input arguments.
```

function state = sampleUniform(obj, varargin)
narginchk(1,4);
[numSamples, stateBounds] = obj.validateSampleUniformInput(varargin{:});
obj.UniformDistribution.RandomVariableLimits = stateBounds;
state = obj.UniformDistribution.sample(numSamples);
end

```

\section*{Sample from Gaussian Distribution}

Specify the behavior for sampling across a Gaussian distribution. Support multiple syntaxes for sampling a single state or multiple states.
```

STATE = sampleGaussian(OBJ, MEANSTATE, STDDEV)
STATE = sampleGaussian(OBJ, MEANSTATE, STDDEV, NUMSAMPLES)
function state = sampleGaussian(obj, meanState, stdDev, varargin)
narginchk(3,4);
[meanState, stdDev, numSamples] = obj.validateSampleGaussianInput(meanState, stdDev, varargi।
obj.NormalDistribution.Mean = meanState;
obj.NormalDistribution.Covariance = diag(stdDev.^2);
state = obj.NormalDistribution.sample(numSamples);
state = obj.enforceStateBounds(state);
end

```

\section*{Interpolate Between States}

Define how to interpolate between two states in your state space. Use an input, fraction, to determine how to sample along the path between two states. For this example, define a basic linear interpolation method using the difference between states.
```

function interpState = interpolate(obj, state1, state2, fraction)
narginchk(4,4);
[state1, state2, fraction] = obj.validateInterpolateInput(state1, state2, fraction);
stateDiff = state2 - statel;
interpState = state1 + fraction' * stateDiff;
end

```

\section*{Calculate Distance Between States}

Specify how to calculate the distance between two states in your state space. Use the statel and state2 inputs to define the start and end positions. Both inputs can be a single state (row vector) or multiple states (matrix of row vectors). For this example, calculate the distance based on the Euclidean distance between each pair of state positions.
```

function dist = distance(obj, state1, state2)
narginchk(3,3);
nav.internal.validation.validateStateMatrix(statel, nan, obj.NumStateVariables, "distance",
nav.internal.validation.validateStateMatrix(state2, size(state1,1), obj.NumStateVariables,
stateDiff = bsxfun(@minus, state2, state1);
dist = sqrt( sum( stateDiff.^2, 2 ) );
end
Terminate the methods and class sections.

```
end
end
Save your state space class definition. You can now use the class constructor to create an object for your state space.

\section*{See Also}
nav.StateSpace|nav.StateValidator| stateSpaceSE2| stateSpaceDubins | stateSpaceReedsShepp

Introduced in R2019b

\section*{interpolate}

Class: nav.StateSpace
Package: nav
Interpolate between states

\section*{Syntax}
interpStates = interpolate(ss0bj,state1,state2,ratios)

\section*{Description}
interpStates = interpolate(ss0bj,state1,state2,ratios) interpolates between two states in your state space based on the given ratios.

\section*{Input Arguments}

\section*{ssObj - State space object}
object of a subclass of nav.StateSpace
State space object, specified as an object of a subclass of nav. StateSpace.

\section*{state1 - Initial state position}
n-element vector
Initial state position, specified as a \(n\)-element vector. \(n\) is the dimension of the state space specified in the NumStateVariables property of ssObj.

\section*{state2 - Final state position}
\(n\)-element vector | \(m\)-by- \(n\) matrix of row vectors
Final state position, specified as a \(n\)-element vector. \(n\) is the dimension of the state space specified in the NumStateVariables property of ssObj.

\section*{ratios - Ratio values for interpolating along path}
\(m\)-element vector
Ratio values for interpolating along path, specified as an \(m\)-element vector. These ratios determine how to sample between the two states.

\section*{Output Arguments}

\section*{interpStates - Interpolated states}
\(m\)-by-n matrix of row vectors
Interpolated states, returned as an \(m\)-by- \(n\) matrix of row vectors. \(m\) is the length of ratios and \(n\) is the dimension of the state space specified in the NumStateVariables property of ssObj.

\section*{Examples}

\section*{Create Custom State Space for Path Planning}

This example shows how to use the createPlanningTemplate function to generate a template for customizing your own state space definition and sampler to use with path planning algorithms. A simple implementation is provided with the template.

Call the create template function. This function generates a class definition file for you to modify for your own implementation.
createPlanningTemplate

\section*{Class and Property Definition}

The first part of the template specifies the class definition and any properties for the class. Derive from the nav. StateSpace class. For this example, create a property for the uniform and normal distributions. You can specify any additional user-defined properties here.
```

classdef MyCustomStateSpace < nav.StateSpace \& ...
matlabshared.planning.internal.EnforceScalarHandle
properties
UniformDistribution
NormalDistribution
% Specify additional properties here
end

```

Save your custom state space class and ensure your file name matches the class name.

\section*{Class Constructor}

Use the constructor to set the name of the state space, the number of state variables, and define its boundaries. Alternatively, you can add input arguments to the function and pass the variables in when you create an object.
- For each state variable, define the [min max] values for the state bounds.
- Call the constructor of the base class.
- For this example, you specify the normal and uniform distribution property values using predefined NormalDistribution and UniformDistribution classes.
- Specify any other user-defined property values here.
```

methods
function obj = MyCustomStateSpace
spaceName = "MyCustomStateSpace";
numStateVariables = 3;
stateBounds = [-100 100; % [min max]
-100 100;
-100 100];
obj@nav.StateSpace(spaceName, numStateVariables, stateBounds);
obj.NormalDistribution = matlabshared.tracking.internal.NormalDistribution(numStateVarial
obj.UniformDistribution = matlabshared.tracking.internal.UniformDistribution(numStateVar
% User-defined property values here
end

```

\section*{Copy Semantics}

Specify the copy method definition. Copy all the values of your user-defined variables into a new object, so copy 0 bj is a deep copy. The default behavior given in this example creates a new copy of the object with the same name, state bounds, and distributions.
```

function copyObj = copy(obj)
copy0bj = feval(class(obj));
copyObj.StateBounds = obj.StateBounds;
copyObj.UniformDistribution = obj.UniformDistribution.copy;
copyObj.NormalDistribution = obj.NormalDistribution.copy;
end

```

\section*{Enforce State Bounds}

Specify how to ensure states are always within the state bounds. For this example, the state values get saturated at the minimum or maximum values for the state bounds.
```

function boundedState = enforceStateBounds(obj, state)
nav.internal.validation.validateStateMatrix(state, nan, obj.NumStateVariables, "enforceState
boundedState = state;
boundedState = min(max(boundedState, obj.StateBounds(:,1)'), ...
obj.StateBounds(:,2)');
end

```

\section*{Sample Uniformly}

Specify the behavior for sampling across a uniform distribution. support multiple syntaxes to constrain the uniform distribution to a nearby state within a certain distance and sample multiple states.
```

STATE = sampleUniform(OBJ)
STATE = sampleUniform(OBJ,NUMSAMPLES)
STATE = sampleUniform(OBJ,NEARSTATE,DIST)
STATE = sampleUniform(OBJ,NEARSTATE,DIST,NUMSAMPLES)

```

For this example, use a validation function to process a varargin input that handles the varying input arguments.
```

function state = sampleUniform(obj, varargin)
narginchk(1,4);
[numSamples, stateBounds] = obj.validateSampleUniformInput(varargin{:});
obj.UniformDistribution.RandomVariableLimits = stateBounds;
state = obj.UniformDistribution.sample(numSamples);
end

```

\section*{Sample from Gaussian Distribution}

Specify the behavior for sampling across a Gaussian distribution. Support multiple syntaxes for sampling a single state or multiple states.
```

STATE = sampleGaussian(OBJ, MEANSTATE, STDDEV)
STATE = sampleGaussian(OBJ, MEANSTATE, STDDEV, NUMSAMPLES)
function state = sampleGaussian(obj, meanState, stdDev, varargin)
narginchk(3,4);

```
```

    [meanState, stdDev, numSamples] = obj.validateSampleGaussianInput(meanState, stdDev, varargi।
    obj.NormalDistribution.Mean = meanState;
    obj.NormalDistribution.Covariance = diag(stdDev.^2);
    state = obj.NormalDistribution.sample(numSamples);
    state = obj.enforceStateBounds(state);
    ```
end

\section*{Interpolate Between States}

Define how to interpolate between two states in your state space. Use an input, fraction, to determine how to sample along the path between two states. For this example, define a basic linear interpolation method using the difference between states.
```

function interpState = interpolate(obj, statel, state2, fraction)
narginchk(4,4);
[state1, state2, fraction] = obj.validateInterpolateInput(state1, state2, fraction);
stateDiff = state2 - state1;
interpState = state1 + fraction' * stateDiff;
end

```

\section*{Calculate Distance Between States}

Specify how to calculate the distance between two states in your state space. Use the statel and state2 inputs to define the start and end positions. Both inputs can be a single state (row vector) or multiple states (matrix of row vectors). For this example, calculate the distance based on the Euclidean distance between each pair of state positions.
```

function dist = distance(obj, state1, state2)
narginchk(3,3);
nav.internal.validation.validateStateMatrix(state1, nan, obj.NumStateVariables, "distance",
nav.internal.validation.validateStateMatrix(state2, size(state1,1), obj.NumStateVariables,
stateDiff = bsxfun(@minus, state2, state1);
dist = sqrt( sum( stateDiff.^2, 2 ) );
end

```

Terminate the methods and class sections.
end
end
Save your state space class definition. You can now use the class constructor to create an object for your state space.

\section*{See Also}
nav.StateSpace|nav.StateValidator| stateSpaceSE2| stateSpaceDubins| stateSpaceReedsShepp

Introduced in R2019b

\section*{sampleGaussian}

Class: nav.StateSpace
Package: nav
Sample state using Gaussian distribution

\section*{Syntax}
```

states = sampleGaussian(ssObj,meanState,stdDev)
states = sampleGaussian(ssObj,meanState,stdDev,numSamples)

```

\section*{Description}
states = sampleGaussian(ss0bj, meanState,stdDev) samples a single state in your state space from a Gaussian distribution centered on meanState with specified standard deviation.
states = sampleGaussian(ss0bj,meanState,stdDev,numSamples) samples multiple states based on numSamples.

\section*{Input Arguments}

\section*{ssObj - State space object}
object of a subclass of nav. StateSpace
State space object, specified as an object of a subclass of nav.StateSpace.

\section*{meanState - Mean state position}
\(n\)-element vector | \(m\)-by- \(n\) matrix of row vectors
Mean state position, specified as a \(n\)-element vector or \(m\)-by- \(n\) matrix of row vectors, where \(n\) is the dimension of the state space specified in the NumStateVariables property of ssObj. \(m\) is the number of samples specified in numSamples.

\section*{stdDev - Standard deviation around mean state}
\(n\)-element vector | \(m\)-by- \(n\) matrix of row vectors
Standard deviation around mean state, specified as an \(n\)-element vector or \(m\)-by- \(n\) matrix of row vectors, where each element corresponds to an element in meanState.

\section*{numSamples - Number of samples}
positive integer
Number of samples, specified as a positive integer. By default, the function assumes numSamples is 1.

\section*{Output Arguments}

\section*{states - Sampled states from state space}
\(n\)-element vector | \(m\)-by- \(n\) matrix of row vectors

Sampled states from state space, specified as a \(n\)-element vector or \(m\)-by- \(n\) matrix of row vectors. \(n\) is the dimension of the state space specified in the NumStateVariables property of ssObj. \(m\) is the number of samples specified in numSamples. All states are sampled within the StateBounds property of ssObj.

\section*{Examples}

\section*{Create Custom State Space for Path Planning}

This example shows how to use the createPlanningTemplate function to generate a template for customizing your own state space definition and sampler to use with path planning algorithms. A simple implementation is provided with the template.

Call the create template function. This function generates a class definition file for you to modify for your own implementation.
```

createPlanningTemplate

```

\section*{Class and Property Definition}

The first part of the template specifies the class definition and any properties for the class. Derive from the nav. StateSpace class. For this example, create a property for the uniform and normal distributions. You can specify any additional user-defined properties here.
```

classdef MyCustomStateSpace < nav.StateSpace \& ...
matlabshared.planning.internal.EnforceScalarHandle
properties
UniformDistribution
NormalDistribution
% Specify additional properties here
end

```

Save your custom state space class and ensure your file name matches the class name.

\section*{Class Constructor}

Use the constructor to set the name of the state space, the number of state variables, and define its boundaries. Alternatively, you can add input arguments to the function and pass the variables in when you create an object.
- For each state variable, define the [min max] values for the state bounds.
- Call the constructor of the base class.
- For this example, you specify the normal and uniform distribution property values using predefined NormalDistribution and UniformDistribution classes.
- Specify any other user-defined property values here.
methods
```

    function obj = MyCustomStateSpace
        spaceName = "MyCustomStateSpace";
        numStateVariables = 3;
        stateBounds = [-100 100; % [min max]
            -100 100;
            -100 100];
    ```
```

    obj@nav.StateSpace(spaceName, numStateVariables, stateBounds);
    ```
    obj. NormalDistribution = matlabshared.tracking.internal. NormalDistribution(numStateVarial
    obj.UniformDistribution = matlabshared.tracking.internal.UniformDistribution(numStateVar:
    \% User-defined property values here
end

\section*{Copy Semantics}

Specify the copy method definition. Copy all the values of your user-defined variables into a new object, so copyObj is a deep copy. The default behavior given in this example creates a new copy of the object with the same name, state bounds, and distributions.
```

function copyObj = copy(obj)
copy0bj = feval(class(obj));
copyObj.StateBounds = obj.StateBounds;
copyObj.UniformDistribution = obj.UniformDistribution.copy;
copyObj.NormalDistribution = obj.NormalDistribution.copy;
end

```

\section*{Enforce State Bounds}

Specify how to ensure states are always within the state bounds. For this example, the state values get saturated at the minimum or maximum values for the state bounds.
```

function boundedState = enforceStateBounds(obj, state)
nav.internal.validation.validateStateMatrix(state, nan, obj.NumStateVariables, "enforceState
boundedState = state;
boundedState = min(max(boundedState, obj.StateBounds(:,1)'), ...
obj.StateBounds(:,2)');
end

```

\section*{Sample Uniformly}
```

Specify the behavior for sampling across a uniform distribution. support multiple syntaxes to constrain the uniform distribution to a nearby state within a certain distance and sample multiple states.

```
```

STATE = sampleUniform(OBJ)
STATE = sampleUniform(OBJ,NUMSAMPLES)
STATE = sampleUniform(OBJ,NEARSTATE,DIST)
STATE = sampleUniform(OBJ,NEARSTATE,DIST,NUMSAMPLES)

```

For this example, use a validation function to process a varargin input that handles the varying input arguments.
```

function state = sampleUniform(obj, varargin)
narginchk(1,4);
[numSamples, stateBounds] = obj.validateSampleUniformInput(varargin{:});
obj.UniformDistribution.RandomVariableLimits = stateBounds;
state = obj.UniformDistribution.sample(numSamples);
end

```

\section*{Sample from Gaussian Distribution}

Specify the behavior for sampling across a Gaussian distribution. Support multiple syntaxes for sampling a single state or multiple states.
```

STATE = sampleGaussian(OBJ, MEANSTATE, STDDEV)
STATE = sampleGaussian(OBJ, MEANSTATE, STDDEV, NUMSAMPLES)
function state = sampleGaussian(obj, meanState, stdDev, varargin)
narginchk(3,4);
[meanState, stdDev, numSamples] = obj.validateSampleGaussianInput(meanState, stdDev, varargi
obj.NormalDistribution.Mean = meanState;
obj.NormalDistribution.Covariance = diag(stdDev.^2);
state = obj.NormalDistribution.sample(numSamples);
state = obj.enforceStateBounds(state);
end

```

\section*{Interpolate Between States}

Define how to interpolate between two states in your state space. Use an input, fraction, to determine how to sample along the path between two states. For this example, define a basic linear interpolation method using the difference between states.
```

function interpState = interpolate(obj, state1, state2, fraction)
narginchk(4,4);
[state1, state2, fraction] = obj.validateInterpolateInput(state1, state2, fraction);
stateDiff = state2 - state1;
interpState = state1 + fraction' * stateDiff;
end

```

\section*{Calculate Distance Between States}

Specify how to calculate the distance between two states in your state space. Use the state1 and state2 inputs to define the start and end positions. Both inputs can be a single state (row vector) or multiple states (matrix of row vectors). For this example, calculate the distance based on the Euclidean distance between each pair of state positions.
```

function dist = distance(obj, state1, state2)
narginchk(3,3);
nav.internal.validation.validateStateMatrix(state1, nan, obj.NumStateVariables, "distance",
nav.internal.validation.validateStateMatrix(state2, size(state1,1), obj.NumStateVariables,
stateDiff = bsxfun(@minus, state2, state1);
dist = sqrt( sum( stateDiff.^2, 2 ) );
end

```

Terminate the methods and class sections.
end
end

Save your state space class definition. You can now use the class constructor to create an object for your state space.
```

See Also
nav.StateSpace|nav.StateValidator| stateSpaceSE2| stateSpaceDubins|
stateSpaceReedsShepp

```

Introduced in R2019b

\section*{sampleUniform}

Class: nav.StateSpace
Package: nav
Sample state using uniform distribution

\section*{Syntax}
```

states = sampleUniform(ssObj)
states = sampleUniform(ssObj,numSamples)
states = sampleUniform(ssObj,meanState,distance)
states = sampleUniform(ssObj,meanState,distance,numSamples)

```

\section*{Description}
states \(=\) sampleUniform(ss0bj) samples throughout your entire state space using a uniform distribution.
states = sampleUniform(ss0bj, numSamples) samples multiple states based on numSamples.
states = sampleUniform(ssObj, meanState, distance) samples near a given mean state within a certain distance.
states = sampleUniform(ssObj,meanState,distance,numSamples) samples multiple states near a given mean state based on numSamples.

\section*{Input Arguments}

\section*{ssObj - State space object}
object of a subclass of nav. StateSpace
State space object, specified as an object of a subclass of nav. StateSpace.

\section*{meanState - Mean state position}
\(n\)-element vector
Mean state position for sampling near, specified as a \(n\)-element vector, where \(n\) is the dimension of the state space specified in the NumStateVariables property of \(\mathrm{ssObj} . m\) is the number of samples specified in numSamples.

\section*{distance - Max distance from mean state position}
\(n\)-element vector
Max distance from mean state position, nearState, specified as a \(n\)-element vector, where nearState defines the center of the sampled region and distance is the maximum distance from nearState allowed in each dimension.

\section*{numSamples - Number of samples}
positive integer
Number of samples, specified as a positive integer.

\section*{Output Arguments}

\section*{states - Sampled states from state space}
\(n\)-element vector | \(m\)-by- \(n\) matrix of row vectors
Sampled states from state space, specified as a \(n\)-element vector or \(m\)-by- \(n\) matrix of row vectors. \(n\) is the dimension of the state space specified in the NumStateVariables property of ssObj. \(m\) is the number of samples specified in numSamples. All states are sampled within the StateBounds property of ssObj.

\section*{Examples}

\section*{Create Custom State Space for Path Planning}

This example shows how to use the createPlanningTemplate function to generate a template for customizing your own state space definition and sampler to use with path planning algorithms. A simple implementation is provided with the template.

Call the create template function. This function generates a class definition file for you to modify for your own implementation.
createPlanningTemplate

\section*{Class and Property Definition}

The first part of the template specifies the class definition and any properties for the class. Derive from the nav. StateSpace class. For this example, create a property for the uniform and normal distributions. You can specify any additional user-defined properties here.
```

classdef MyCustomStateSpace < nav.StateSpace \& ...
matlabshared.planning.internal.EnforceScalarHandle
properties
UniformDistribution
NormalDistribution
% Specify additional properties here
end

```

Save your custom state space class and ensure your file name matches the class name.

\section*{Class Constructor}

Use the constructor to set the name of the state space, the number of state variables, and define its boundaries. Alternatively, you can add input arguments to the function and pass the variables in when you create an object.
- For each state variable, define the [min max] values for the state bounds.
- Call the constructor of the base class.
- For this example, you specify the normal and uniform distribution property values using predefined NormalDistribution and UniformDistribution classes.
- Specify any other user-defined property values here.
methods
function obj \(=\) MyCustomStateSpace
```

    spaceName = "MyCustomStateSpace";
    numStateVariables = 3;
    stateBounds = [-100 100; % [min max]
        -100 100;
        -100 100];
    obj@nav.StateSpace(spaceName, numStateVariables, stateBounds);
    obj.NormalDistribution = matlabshared.tracking.internal.NormalDistribution(numStateVarial
    obj.UniformDistribution = matlabshared.tracking.internal.UniformDistribution(numStateVar
    % User-defined property values here
    end

```

\section*{Copy Semantics}

Specify the copy method definition. Copy all the values of your user-defined variables into a new object, so copyObj is a deep copy. The default behavior given in this example creates a new copy of the object with the same name, state bounds, and distributions.
```

function copyObj = copy(obj)
copy0bj = feval(class(obj));
copyObj.StateBounds = obj.StateBounds;
copyObj.UniformDistribution = obj.UniformDistribution.copy;
copyObj.NormalDistribution = obj.NormalDistribution.copy;
end

```

\section*{Enforce State Bounds}

Specify how to ensure states are always within the state bounds. For this example, the state values get saturated at the minimum or maximum values for the state bounds.
```

function boundedState = enforceStateBounds(obj, state)
nav.internal.validation.validateStateMatrix(state, nan, obj.NumStateVariables, "enforceState
boundedState = state;
boundedState = min(max(boundedState, obj.StateBounds(:,1)'), ...
obj.StateBounds(:,2)');

```
end

\section*{Sample Uniformly}

Specify the behavior for sampling across a uniform distribution. support multiple syntaxes to constrain the uniform distribution to a nearby state within a certain distance and sample multiple states.
```

STATE = sampleUniform(OBJ)
STATE = sampleUniform(OBJ,NUMSAMPLES)
STATE = sampleUniform(OBJ,NEARSTATE,DIST)
STATE = sampleUniform(OBJ,NEARSTATE,DIST,NUMSAMPLES)

```

For this example, use a validation function to process a varargin input that handles the varying input arguments.
```

function state = sampleUniform(obj, varargin)
narginchk(1,4);
[numSamples, stateBounds] = obj.validateSampleUniformInput(varargin{:});
obj.UniformDistribution.RandomVariableLimits = stateBounds;

```
```

    state = obj.UniformDistribution.sample(numSamples);
    end

```

\section*{Sample from Gaussian Distribution}

Specify the behavior for sampling across a Gaussian distribution. Support multiple syntaxes for sampling a single state or multiple states.
```

STATE = sampleGaussian(OBJ, MEANSTATE, STDDEV)
STATE = sampleGaussian(OBJ, MEANSTATE, STDDEV, NUMSAMPLES)
function state = sampleGaussian(obj, meanState, stdDev, varargin)
narginchk(3,4);
[meanState, stdDev, numSamples] = obj.validateSampleGaussianInput(meanState, stdDev, varargi
obj.NormalDistribution.Mean = meanState;
obj.NormalDistribution.Covariance = diag(stdDev.^2);
state = obj.NormalDistribution.sample(numSamples);
state = obj.enforceStateBounds(state);

```
end

\section*{Interpolate Between States}

Define how to interpolate between two states in your state space. Use an input, fraction, to determine how to sample along the path between two states. For this example, define a basic linear interpolation method using the difference between states.
```

function interpState = interpolate(obj, state1, state2, fraction)
narginchk(4,4);
[state1, state2, fraction] = obj.validateInterpolateInput(state1, state2, fraction);
stateDiff = state2 - statel;
interpState = statel + fraction' * stateDiff;
end

```

\section*{Calculate Distance Between States}

Specify how to calculate the distance between two states in your state space. Use the state1 and state 2 inputs to define the start and end positions. Both inputs can be a single state (row vector) or multiple states (matrix of row vectors). For this example, calculate the distance based on the Euclidean distance between each pair of state positions.
```

function dist = distance(obj, state1, state2)
narginchk(3,3);
nav.internal.validation.validateStateMatrix(state1, nan, obj.NumStateVariables, "distance",
nav.internal.validation.validateStateMatrix(state2, size(state1,1), obj.NumStateVariables,
stateDiff = bsxfun(@minus, state2, state1);
dist = sqrt( sum( stateDiff.^2, 2 ) );
end
Terminate the methods and class sections.

```
end
end

Save your state space class definition. You can now use the class constructor to create an object for your state space.

\section*{See Also}
nav.StateSpace | nav.StateValidator| stateSpaceSE2| stateSpaceDubins |
stateSpaceReedsShepp
Introduced in R2019b

\section*{nav.StateValidator class}

Package: nav
Create state validator for path planning

\section*{Description}
nav. StateValidator is an interface for all state validators used for path planning. Derive from this class if you want to define your own state validator. This representation allows for state and motion validation.

To create a sample template for generating your own state space class, call createPlanningTemplate("StateValidator"). For specific implementations of the state validator class for general application, see State Validation in "Motion Planning".

The nav.StateValidator class is a handle class.

\section*{Class Attributes}

\section*{Abstract true}

For information on class attributes, see "Class Attributes".

\section*{Creation}

\section*{Syntax}
ssObj = nav.StateValidator(stateSpace)

\section*{Description}
ssObj = nav.StateValidator(stateSpace) creates a state validator object that validates states in the given state space. This constructor can only be called from a derived class. Create your own class definition using createPlanningTemplate.

\section*{Properties}

\section*{StateSpace - State space definition}
object of a subclass from nav. StateSpace
State space definition, specified as an object of a subclass from nav. StateSpace. Specify this property using the stateSpace input on construction. You can also specify any of our predefined objects in the State Validation section from "Motion Planning".
Example: stateSpaceSE2

\section*{Attributes:}

GetAccess
SetAccess
public
immutable

\section*{Methods}

\section*{Public Methods}
copy Copy array of handle objects
isMotionValid Check if path between states is valid
isStateValid Check if state is valid

\section*{Examples}

\section*{Create Custom State Space Validator for Path Planning}

This example shows how to use the createPlanningTemplate function to generate a template for customizing your own state validation class. State validation is used with path planning algorithms to ensure valid paths. The template function provides a basic implementation for example purposes.

Call the create template function. This function generates a class definition file for you to modify for your own implementation. Save this file.
```

createPlanningTemplate("StateValidator")

```

\section*{Class and Property Definition}

The first part of the template specifies the class definition and any properties for the class. Derive from the nav. StateValidator class. You can specify any additional user-defined properties here.
```

classdef MyCustomStateValidator < nav.StateValidator \& ...
matlabshared.planning.internal.EnforceScalarHandle
properties
% User-defined properties
end

```

Save your custom state validator class and ensure your file name matches the class name.

\section*{Class Constructor}

Use the constructor to set the name of the state space validator and specify the state space object. Set a default value for the state space if one is not provided. Call the constructor of the base class. Initialize any other user-defined properties. This example uses a default of MyCustomStateSpace, which was illustrated in the previous example.
```

methods

```
```

function obj = MyCustomStateValidator(space)
narginchk(0,1)
if nargin == 0
space = MyCustomStateSpace;
end
obj@nav.StateValidator(space);

```
```

    % Initialize user-defined properties
    end

```

\section*{Copy Semantics}

Specify the copy method definition. Copy all the values of your user-defined variables into a new object, so copyObj is a deep copy. The default behavior given in this example creates a new copy of the object with the same type.
```

function copyObj = copy(obj)
copyObj = feval(class(obj), obj.StateSpace);
end

```

\section*{Check State Validity}

Define how a given state is validated. The state input can either be a single row vector, or a matrix of row vectors for multiple states. Customize this function for any special validation behavior for your state space like collision checking against obstacles.
```

function isValid = isStateValid(obj, state)
narginchk(2,2);
nav.internal.validation.validateStateMatrix(state, nan, obj.StateSpace.NumStateVarial
"isStateValid", "state");
bounds = obj.StateSpace.StateBounds';
inBounds = state >= bounds(1,:) \& state <= bounds(2,:);
isValid = all(inBounds, 2);
end

```

\section*{Check Motion Validity}

Define how to generate the motion between states and determine if it is valid. For this example, use linspace to evenly interpolate between states and check if these states are valid using isStateValid. Customize this function to sample between states or consider other analytical methods for determining if a vehicle can move between given states.
```

function [isValid, lastValid] = isMotionValid(obj, state1, state2)
narginchk(3,3);
state1 = nav.internal.validation.validateStateVector(state1, ...
obj.StateSpace.NumStateVariables, "isMotionValid", "state1");
state2 = nav.internal.validation.validateStateVector(state2, ...
obj.StateSpace.NumStateVariables, "isMotionValid", "state2");
if (~obj.isStateValid(statel))
error("statevalidator:StartStateInvalid", "The start state of the motion is inva
end
% Interpolate at a fixed interval between states and check state validity
numInterpPoints = 100;
interpStates = obj.StateSpace.interpolate(state1, state2, linspace(0,1,numInterpPoin
interpValid = obj.isStateValid(interpStates);
% Look for invalid states. Set lastValid state to index-1.
firstInvalidIdx = find(~interpValid, 1);
if isempty(firstInvalidIdx)
isValid = true;

```
```

        lastValid = state2;
    else
    isValid = false;
    lastValid = interpStates(firstInvalidIdx-1,:);
    end
end

```

Terminate the methods and class sections.
end
end
Save your state space validator class definition. You can now use the class constructor to create an object for validation of states for a given state space.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

\author{
See Also \\ nav.StateSpace | validator0ccupancyMap|validatorVehicleCostmap \\ Introduced in R2019b
}

\section*{isMotionValid}

Class: nav.StateValidator
Package: nav
Check if path between states is valid

\section*{Syntax}
[isValid,lastValid] = isMotionValid(validatorObj,state1,state2)

\section*{Description}
[isValid,lastValid] = isMotionValid(validatorObj,state1,state2) determines if the motion between two states is valid by interpolating between states. The function also returns the last valid state along the path.

A default implementation for this method is provided when you call createPlanningTemplate.

\section*{Input Arguments}

\section*{validator0bj - State validator object}
object from a subclass of nav.StateValidator
State validator object, specified as an object from a subclass of nav.StateValidator. For provided state validator objects, see validator0ccupancyMap or validatorVehicleCostmap.

\section*{statel - Initial state position}
\(n\)-element vector | \(m\)-by- \(n\) matrix of row vectors
Initial state position, specified as a \(n\)-element vector or \(m\)-by- \(n\) matrix of row vectors. \(n\) is the dimension of the state space specified in the state space property in validator0bj.

\section*{state2 - Final state position}
\(n\)-element vector | \(m\)-by-n matrix of row vectors
Final state position, specified as a \(n\)-element vector or \(m\)-by- \(n\) matrix of row vectors. \(n\) is the dimension of the state space specified in the state space property in validator0bj.

\section*{Output Arguments}

\section*{isValid - Valid states \\ \(m\)-element vector of 1 s and 0 s}

Valid states, specified as a \(m\)-element vector of 1 s and 0 s .

\section*{Data Types: logical}

\section*{lastValid - Final valid state along path}
\(n\)-element vector

Final valid state along path, specified as a \(n\)-element vector. \(n\) is the dimension of the state space specified in the state space property in validator0bj.

\section*{Examples}

\section*{Create Custom State Space Validator for Path Planning}

This example shows how to use the createPlanningTemplate function to generate a template for customizing your own state validation class. State validation is used with path planning algorithms to ensure valid paths. The template function provides a basic implementation for example purposes.

Call the create template function. This function generates a class definition file for you to modify for your own implementation. Save this file.
```

createPlanningTemplate("StateValidator")

```

\section*{Class and Property Definition}

The first part of the template specifies the class definition and any properties for the class. Derive from the nav. StateValidator class. You can specify any additional user-defined properties here.
```

classdef MyCustomStateValidator < nav.StateValidator \& ...
matlabshared.planning.internal.EnforceScalarHandle
properties
% User-defined properties
end

```

Save your custom state validator class and ensure your file name matches the class name.

\section*{Class Constructor}

Use the constructor to set the name of the state space validator and specify the state space object. Set a default value for the state space if one is not provided. Call the constructor of the base class. Initialize any other user-defined properties. This example uses a default of MyCustomStateSpace, which was illustrated in the previous example.
```

methods
function obj = MyCustomStateValidator(space)
narginchk(0,1)
if nargin == 0
space = MyCustomStateSpace;
end
obj@nav.StateValidator(space);
% Initialize user-defined properties
end

```

\section*{Copy Semantics}

Specify the copy method definition. Copy all the values of your user-defined variables into a new object, so copyObj is a deep copy. The default behavior given in this example creates a new copy of the object with the same type.
```

function copyObj = copy(obj)
copyObj = feval(class(obj), obj.StateSpace);
end

```

\section*{Check State Validity}

Define how a given state is validated. The state input can either be a single row vector, or a matrix of row vectors for multiple states. Customize this function for any special validation behavior for your state space like collision checking against obstacles.
```

function isValid = isStateValid(obj, state)
narginchk(2,2);
nav.internal.validation.validateStateMatrix(state, nan, obj.StateSpace.NumStateVarial
"isStateValid", "state");
bounds = obj.StateSpace.StateBounds';
inBounds = state >= bounds(1,:) \& state <= bounds(2,:);
isValid = all(inBounds, 2);
end

```

\section*{Check Motion Validity}

Define how to generate the motion between states and determine if it is valid. For this example, use linspace to evenly interpolate between states and check if these states are valid using isStateValid. Customize this function to sample between states or consider other analytical methods for determining if a vehicle can move between given states.
```

function [isValid, lastValid] = isMotionValid(obj, state1, state2)
narginchk(3,3);
state1 = nav.internal.validation.validateStateVector(state1, ...
obj.StateSpace.NumStateVariables, "isMotionValid", "state1");
state2 = nav.internal.validation.validateStateVector(state2, ...
obj.StateSpace.NumStateVariables, "isMotionValid", "state2");
if (~obj.isStateValid(state1))
error("statevalidator:StartStateInvalid", "The start state of the motion is inva
end
% Interpolate at a fixed interval between states and check state validity
numInterpPoints = 100;
interpStates = obj.StateSpace.interpolate(state1, state2, linspace(0,1,numInterpPoin
interpValid = obj.isStateValid(interpStates);
% Look for invalid states. Set lastValid state to index-1.
firstInvalidIdx = find(~interpValid, 1);
if isempty(firstInvalidIdx)
isValid = true;
lastValid = state2;
else
isValid = false;
lastValid = interpStates(firstInvalidIdx-1,:);
end

```
end
Terminate the methods and class sections.
end
end
Save your state space validator class definition. You can now use the class constructor to create an object for validation of states for a given state space.

\section*{See Also \\ nav.StateValidator|nav.StateSpace | validatorOccupancyMap | validatorVehicleCostmap}

\section*{Introduced in R2019b}

\section*{isStateValid}

Class: nav.StateValidator
Package: nav
Check if state is valid

\section*{Syntax}
isValid = isStateValid(validatorObj,states)

\section*{Description}
isValid = isStateValid(validator0bj,states) determines if the states are valid.

\section*{Input Arguments}
validatorObj - State validator object
object from a subclass of nav.StateValidator
State validator object, specified as an object from a subclass of nav. StateValidator. For provided state validator objects, see validator0ccupancyMap or validatorVehicleCostmap.
states - State positions
\(n\)-element vector | \(m\)-by- \(n\) matrix of row vectors
Initial state position, specified as a \(n\)-element vector or \(m\)-by- \(n\) matrix of row vectors. \(n\) is the dimension of the state space specified in validator0bj. \(m\) is the number of states to validate.

\section*{Output Arguments}

\section*{isValid - Valid states}
\(m\)-element vector of 1 s and 0 s
Valid states, specified as a \(m\)-element vector of 1 s and 0 s .

\section*{Examples}

\section*{Create Custom State Space Validator for Path Planning}

This example shows how to use the createPlanningTemplate function to generate a template for customizing your own state validation class. State validation is used with path planning algorithms to ensure valid paths. The template function provides a basic implementation for example purposes.

Call the create template function. This function generates a class definition file for you to modify for your own implementation. Save this file.
```

createPlanningTemplate("StateValidator")

```

\section*{Class and Property Definition}

The first part of the template specifies the class definition and any properties for the class. Derive from the nav. StateValidator class. You can specify any additional user-defined properties here.
```

classdef MyCustomStateValidator < nav.StateValidator \& ...
matlabshared.planning.internal.EnforceScalarHandle
properties
% User-defined properties
end

```

Save your custom state validator class and ensure your file name matches the class name.

\section*{Class Constructor}

Use the constructor to set the name of the state space validator and specify the state space object. Set a default value for the state space if one is not provided. Call the constructor of the base class. Initialize any other user-defined properties. This example uses a default of MyCustomStateSpace, which was illustrated in the previous example.
```

methods
function obj = MyCustomStateValidator(space)
narginchk(0,1)
if nargin == 0
space = MyCustomStateSpace;
end
obj@nav.StateValidator(space);
% Initialize user-defined properties
end

```

\section*{Copy Semantics}

Specify the copy method definition. Copy all the values of your user-defined variables into a new object, so copyObj is a deep copy. The default behavior given in this example creates a new copy of the object with the same type.
```

function copyObj = copy(obj)
copyObj = feval(class(obj), obj.StateSpace);
end

```

\section*{Check State Validity}

Define how a given state is validated. The state input can either be a single row vector, or a matrix of row vectors for multiple states. Customize this function for any special validation behavior for your state space like collision checking against obstacles.
```

function isValid = isStateValid(obj, state)
narginchk(2,2);
nav.internal.validation.validateStateMatrix(state, nan, obj.StateSpace.NumStateVarial
"isStateValid", "state");
bounds = obj.StateSpace.StateBounds';
inBounds = state >= bounds(1,:) \& state <= bounds(2,:);
isValid = all(inBounds, 2);

```
end

\section*{Check Motion Validity}

Define how to generate the motion between states and determine if it is valid. For this example, use linspace to evenly interpolate between states and check if these states are valid using isStateValid. Customize this function to sample between states or consider other analytical methods for determining if a vehicle can move between given states.
```

function [isValid, lastValid] = isMotionValid(obj, state1, state2)
narginchk(3,3);
statel = nav.internal.validation.validateStateVector(state1, ...
obj.StateSpace.NumStateVariables, "isMotionValid", "state1");
state2 = nav.internal.validation.validateStateVector(state2, ...
obj.StateSpace.NumStateVariables, "isMotionValid", "state2");
if (~obj.isStateValid(statel))
error("statevalidator:StartStateInvalid", "The start state of the motion is inva
end
% Interpolate at a fixed interval between states and check state validity
numInterpPoints = 100;
interpStates = obj.StateSpace.interpolate(state1, state2, linspace(0,1,numInterpPoin
interpValid = obj.isStateValid(interpStates);
% Look for invalid states. Set lastValid state to index-1.
firstInvalidIdx = find(~interpValid, 1);
if isempty(firstInvalidIdx)
isValid = true;
lastValid = state2;
else
isValid = false;
lastValid = interpStates(firstInvalidIdx-1,:);
end
end

```

Terminate the methods and class sections.
end
end
Save your state space validator class definition. You can now use the class constructor to create an object for validation of states for a given state space.

\section*{See Also}
nav.StateValidator|nav.StateSpace | validatorOccupancyMap | validatorVehicleCostmap

Introduced in R2019b

\section*{insfilterNonholonomic}

Estimate pose with nonholonomic constraints

\section*{Description}

The insfilterNonholonomic object implements sensor fusion of inertial measurement unit (IMU) and GPS data to estimate pose in the NED (or ENU) reference frame. IMU data is derived from gyroscope and accelerometer data. The filter uses a 16 -element state vector to track the orientation quaternion, velocity, position, and IMU sensor biases. The insfilterNonholonomic object uses an extended Kalman filter to estimate these quantities.

\section*{Creation}

\section*{Syntax}
filter \(=\) insfilterNonholonomic
filter \(=\) insfilterNonholonomic('ReferenceFrame',RF)
filter \(=\) insfilterNonholonomic( \(\qquad\) ,Name, Value)

\section*{Description}
filter = insfilterNonholonomic creates an insfilterErrorState object with default property values.
filter = insfilterNonholonomic('ReferenceFrame',RF) allows you to specify the reference frame, RF, of the filter. Specify RF as 'NED' (North-East-Down) or 'ENU' (East-NorthUp). The default value is 'NED '.
filter = insfilterNonholonomic( \(\qquad\) ,Name, Value) also allows you set properties of the created filter using one or more name-value pairs. Enclose each property name in single quotes.

\section*{Properties}

\section*{IMUSampleRate - Sample rate of the IMU (Hz) \\ 100 (default) | positive scalar}

Sample rate of the IMU in Hz, specified as a positive scalar.
Data Types: single | double
ReferenceLocation - Reference location (deg, deg, meters)
[0 0 0] (default) | 3-element positive row vector
Reference location, specified as a 3 -element row vector in geodetic coordinates (latitude, longitude, and altitude). Altitude is the height above the reference ellipsoid model, WGS84. The reference location units are [degrees degrees meters].

Data Types: single|double

\section*{DecimationFactor - Decimation factor for kinematic constraint correction}

2 (default) | positive integer scalar
Decimation factor for kinematic constraint correction, specified as a positive integer scalar.
Data Types: single | double
GyroscopeNoise - Multiplicative process noise variance from gyroscope (rad/s) \({ }^{\mathbf{2}}\)
[4.8e-6 4.8e-6 4.8e-6] (default)| scalar|3-element row vector
Multiplicative process noise variance from the gyroscope in (rad/s) \({ }^{2}\), specified as a scalar or 3element row vector of positive real finite numbers.
- If GyroscopeNoise is specified as a row vector, the elements correspond to the noise in the \(x, y\), and \(z\) axes of the gyroscope, respectively.
- If GyroscopeNoise is specified as a scalar, the single element is applied to the \(x, y\), and \(z\) axes of the gyroscope.

\section*{Data Types: single | double}

\section*{GyroscopeBiasNoise - Multiplicative process noise variance from gyroscope bias (rad/s) \({ }^{\mathbf{2}}\) [4e-14 4e-14 4e-14] (default)| scalar| 3-element row vector}

Multiplicative process noise variance from the gyroscope bias in (rad/s) \({ }^{2}\), specified as a scalar or 3element row vector of positive real finite numbers. Gyroscope bias is modeled as a lowpass filtered white noise process.
- If GyroscopeBiasNoise is specified as a row vector, the elements correspond to the noise in the \(x, y\), and \(z\) axes of the gyroscope, respectively.
- If GyroscopeBiasNoise is specified as a scalar, the single element is applied to the \(x, y\), and \(z\) axes of the gyroscope.

Data Types: single | double

\section*{GyroscopeBiasDecayFactor - Decay factor for gyroscope bias \\ 0.999 (default) | scalar in the range [0,1]}

Decay factor for gyroscope bias, specified as a scalar in the range [0,1]. A decay factor of 0 models gyroscope bias as a white noise process. A decay factor of 1 models the gyroscope bias as a random walk process.

\section*{Data Types: single | double}

\section*{AccelerometerNoise - Multiplicative process noise variance from accelerometer (m/s \(\mathbf{s}^{\mathbf{2}} \mathbf{2}^{\mathbf{2}}\)}
[4.8e-2 4.8e-2 4.8e-2] (default) | scalar | 3-element row vector
Multiplicative process noise variance from the accelerometer in \(\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}\), specified as a scalar or 3element row vector of positive real finite numbers.
- If AccelerometerNoise is specified as a row vector, the elements correspond to the noise in the \(x, y\), and \(z\) axes of the accelerometer, respectively.
- If AccelerometerNoise is specified as a scalar, the single element is applied to each axis.

Data Types: single | double

AccelerometerBiasNoise - Multiplicative process noise variance from accelerometer bias \(\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}\)
[4e-14 4e-14 4e-14] (default)| positive scalar | 3-element row vector
Multiplicative process noise variance from the accelerometer bias in \(\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}\), specified as a scalar or 3 -element row vector of positive real numbers. Accelerometer bias is modeled as a lowpass filtered white noise process.
- If AccelerometerBiasNoise is specified as a row vector, the elements correspond to the noise in the \(x, y\), and \(z\) axes of the accelerometer, respectively.
- If AccelerometerBiasNoise is specified as a scalar, the single element is applied to each axis.

\section*{AccelerometerBiasDecayFactor - Decay factor for accelerometer bias}
0.9999 (default) | scalar in the range [0,1]

Decay factor for accelerometer bias, specified as a scalar in the range [0,1]. A decay factor of 0 models accelerometer bias as a white noise process. A decay factor of 1 models the accelerometer bias as a random walk process.

Data Types: single | double

\section*{State - State vector of extended Kalman filter}
[1;zeros(15,1)]|16-element column vector
State vector of the extended Kalman filter. The state values represent:
\begin{tabular}{lll} 
State & Units & Index \\
Orientation (quaternion parts) & \(\mathrm{N} / \mathrm{A}\) & \(1: 4\) \\
Gyroscope Bias (XYZ) & \(\mathrm{rad} / \mathrm{s}\) & \(5: 7\) \\
Position (NED or ENU) & m & \(8: 10\) \\
Velocity (NED or ENU) & \(\mathrm{m} / \mathrm{s}\) & \(11: 13\) \\
Accelerometer Bias (XYZ) & \(\mathrm{m} / \mathrm{s}^{2}\) & \(14: 16\)
\end{tabular}

Data Types: single | double
StateCovariance - State error covariance for extended Kalman filter
eye(16) (default) | 16-by-16 matrix
State error covariance for the extended Kalman filter, specified as a 16 -by-16-element matrix, or real numbers.

Data Types: single | double
ZeroVelocityConstraintNoise - Velocity constraints noise (m/s) \({ }^{\mathbf{2}}\)
1e-2 (default) | nonnegative scalar
Velocity constraints noise in \((\mathrm{m} / \mathrm{s})^{2}\), specified as a nonnegative scalar.
Data Types: single|double

\section*{Object Functions}
correct Correct states using direct state measurements for insfilterNonholonomic
\begin{tabular}{ll} 
residual & \begin{tabular}{l} 
Residuals and residual covariances from direct state measurements for \\
insfilterNonholonomic
\end{tabular} \\
fusegps & Correct states using GPS data for insfilterNonholonomic \\
residualgps & Residuals and residual covariance from GPS measurements for insfilterNonholonomic \\
pose & Current orientation and position estimate for insfilterNonholonomic \\
predict & Update states using accelerometer and gyroscope data for insfilterNonholonomic \\
reset & Reset internal states for insfilterNonholonomic \\
stateinfo & Display state vector information for insfilterNonholonomic \\
tune & Tune insfilterNonholonomic parameters to reduce estimation error \\
copy & Create copy of insfitlerNonholonomic
\end{tabular}

\section*{Examples}

\section*{Estimate Pose of Ground Vehicle}

This example shows how to estimate the pose of a ground vehicle from logged IMU and GPS sensor measurements and ground truth orientation and position.

Load the logged data of a ground vehicle following a circular trajectory.
```

load('loggedGroundVehicleCircle.mat','imuFs','localOrigin','initialState','initialStateCovarianc
'gyroData','gpsFs','gpsLLA','Rpos','gpsVel','Rvel','trueOrient','truePos');

```

Initialize the insfilterNonholonomic object.
```

filt = insfilterNonholonomic;
filt.IMUSampleRate = imuFs;
filt.ReferenceLocation = localOrigin;
filt.State = initialState;
filt.StateCovariance = initialStateCovariance;
imuSamplesPerGPS = imuFs/gpsFs;

```

Log data for final metric computation. Use the predict object function to estimate filter state based on accelerometer and gyroscope data. Then correct the filter state according to GPS data.
```

numIMUSamples = size(accelData,1);
estOrient = quaternion.ones(numIMUSamples,1);
estPos = zeros(numIMUSamples,3);
gpsIdx = 1;
for idx = 1:numIMUSamples
predict(filt,accelData(idx,:),gyroData(idx,:)); %Predict filter state
if (mod(idx,imuSamplesPerGPS) == 0) %Correct filter state
fusegps(filt,gpsLLA(gpsIdx,:),Rpos,gpsVel(gpsIdx,:),Rvel);
gpsIdx = gpsIdx + 1;
end
[estPos(idx,:),estOrient(idx,:)] = pose(filt); %Log estimated pose
end

```

Calculate and display RMS errors.
```

posd = estPos - truePos;
quatd = rad2deg(dist(estOrient,trueOrient));
msep = sqrt(mean(posd.^2));
fprintf('Position RMS Error\n\tX: %.2f, Y: %.2f, Z: %.2f (meters)\n\n',msep(1),msep(2),msep(3));
Position RMS Error
X: 0.15, Y: 0.11, Z: 0.01 (meters)
fprintf('Quaternion Distance RMS Error\n\t%.2f (degrees)\n\n',sqrt(mean(quatd.^2)));
Quaternion Distance RMS Error
0.26 (degrees)

```

\section*{Algorithms}

Note: The following algorithm only applies to an NED reference frame.
insfilterNonholonomic uses a 16-axis error state Kalman filter structure to estimate pose in the NED reference frame. The state is defined as:
\(x=\left[\begin{array}{c}q_{0} \\ q_{1} \\ q_{2} \\ q_{3} \\ \text { gyrobias }_{X} \\ \text { gyrobias }_{Y} \\ \text { gyrobias }_{Z} \\ \text { position }_{N} \\ \text { position }_{E} \\ \text { position }_{D} \\ v_{N} \\ v_{E} \\ v_{D} \\ \text { accelbias } \\ \text { accelbias }_{Y} \\ \text { accelbias }_{Z}\end{array}\right]\)
where
- \(q_{0}, q_{1}, q_{2}, q_{3}\)-- Parts of orientation quaternion. The orientation quaternion represents a frame rotation from the platform's current orientation to the local NED coordinate system.
- gyrobias \(_{\mathrm{X}}\), gyrobias \(_{\mathrm{Y}}\), gyrobias \(_{\mathrm{Z}}\)-- Bias in the gyroscope reading.
- position \({ }_{\mathrm{N}}\), position \(_{\mathrm{E}}\), position \(_{\mathrm{D}}\)-- Position of the platform in the local NED coordinate system.
- \(\nu_{\mathrm{N}}, \nu_{\mathrm{E}}, \nu_{\mathrm{D}}\)-- Velocity of the platform in the local NED coordinate system.
- accelbias \({ }_{\mathrm{X}}\), accelbias \(_{\mathrm{Y}}\), accelbias \(_{\mathrm{Z}}\)-- Bias in the accelerometer reading.

Given the conventional formulation of the state transition function,
\[
x_{k \mid k-1}=f\left(\widehat{x}_{k-1 \mid k-1}\right)
\]
the predicted state estimate is:
\(x_{k \mid k-1}=\)
\[
\begin{aligned}
& {\left[q_{0}+\Delta t * q_{1}\left(\text { gyrobias }_{X} / 2-\text { gyro }_{X} / 2\right)+\Delta t * q_{2} *\left(\text { gyrobias }_{Y} / 2-\text { gyro }_{Y} / 2\right)+\Delta t * q_{3} *\left(\text { gyrobias }_{Z} / 2-\text { gyro }_{Z} / 2\right)\right.} \\
& q_{1}-\Delta t * q_{0}\left(\text { gyrobias }_{X} / 2-\text { gyro }_{X} / 2\right)+\Delta t * q_{3} *\left(\text { gyrobias }_{Y} / 2-\text { gyro }_{Y} / 2\right)-\Delta t * q_{2} *\left(\text { gyrobias }_{Z} / 2-\text { gyro }_{Z} / 2\right) \\
& q_{2}-\Delta t * q_{3}\left(\text { gyrobias }_{X} / 2-\text { gyro }_{X} / 2\right)-\Delta t * q_{0} *\left(\text { gyrobias }_{Y} / 2-\text { gyro }_{Y} / 2\right)+\Delta t * q_{1} *\left(\text { gyrobias }_{Z} / 2-\text { gyro }_{Z} / 2\right) \\
& q_{3}+\Delta t * q_{2}\left(\text { gyrobias }_{X} / 2-\text { gyro }_{X} / 2\right)-\Delta t * q_{1} *\left(\text { gyrobias }_{Y} / 2-\text { gyro }_{Y} / 2\right)-\Delta t * q_{0} *\left(\text { gyrobias }_{Z} / 2-\text { gyro }_{Z} / 2\right) \\
& - \text { gryobias }_{X} *\left(\Delta t * \lambda_{\text {gyro }}-1\right) \\
& - \text { gryobias }_{Y} *\left(\Delta t * \lambda_{\text {gyro }}-1\right) \\
& - \text { gryobias }_{Z} *\left(\Delta t * \lambda_{\text {gyro }}-1\right) \\
& \text { position }_{N}+\Delta t * v_{N} \\
& \text { position }_{E}+\Delta t * v_{E} \\
& \operatorname{position}_{D}+\Delta t * v_{D}
\end{aligned}
\]
where
- \(\Delta t\)-- IMU sample time.
- \(g_{\mathrm{N}}, g_{\mathrm{E}}, g_{\mathrm{D}}--\) Constant gravity vector in the NED frame.
- accel \({ }_{X}\), accel \(_{Y}\), accel \(_{Z}-\) Acceleration vector in the body frame.
- \(\lambda_{\text {accel }}\)-- Accelerometer bias decay factor.
- \(\lambda_{\text {gyro }}\)-- Gyroscope bias decay factor.

\section*{References}
[1] Munguía, R. "A GPS-Aided Inertial Navigation System in Direct Configuration." Journal of applied research and technology. Vol. 12, Number 4, 2014, pp. 803-814.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).

\section*{See Also}
insfilterMARG|insfilterErrorState|insfilterAsync
Introduced in R2018b

\section*{correct}

Correct states using direct state measurements for insfilterNonholonomic

\section*{Syntax}
correct(FUSE,idx,measurement,measurementCovariance)

\section*{Description}
correct(FUSE,idx, measurement, measurementCovariance) corrects the state and state estimation error covariance based on the measurement and measurement covariance. The measurement maps directly to the state specified by the indices idx.

\section*{Input Arguments}

FUSE - insfilterNonholonomic object
object
insfilterNonholonomic, specified as an object.
idx - State vector Index of measurement to correct
\(N\)-element vector of increasing integers in the range \([1,16]\)
State vector index of measurement to correct, specified as an \(N\)-element vector of increasing integers in the range \([1,16]\).

The state values represent:
\begin{tabular}{lll} 
State & Units & Index \\
Orientation (quaternion parts) & & \(1: 4\) \\
Gyroscope bias (XYZ) & \(\mathrm{rad} / \mathrm{s}\) & \(5: 7\) \\
Position (NED) & m & \(8: 10\) \\
Velocity (NED) & \(\mathrm{m} / \mathrm{s}\) & \(11: 13\) \\
Accelerometer Bias (XYZ) & \(\mathrm{m} / \mathrm{s}^{2}\) & \(14: 16\)
\end{tabular}

Data Types: single | double
measurement - Direct measurement of state
\(N\)-element vector
Direct measurement of state, specified as a \(N\)-element vector. \(N\) is the number of elements of the index argument, idx.
Data Types: single | double
measurementCovariance - Covariance of measurement
scalar | \(N\)-element vector | \(N\)-by- \(N\) matrix

Covariance of measurement, specified as a scalar, \(N\)-element vector, or \(N\)-by- \(N\) matrix. \(N\) is the number of elements of the index argument, idx.

Data Types: single | double

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}
insfilter|insfilterNonholonomic
Introduced in R2018b

\section*{copy}

Create copy of insfitlerNonholonomic

\section*{Syntax}
newFilter \(=\) copy(filter)

\section*{Description}
newFilter = copy(filter) returns a copy of the insfilterNonholonomic, filter, with the exactly same property values.

\section*{Input Arguments}
filter - Filter to be copied
insfitlerNonholonomic
Filter to be copied, specified as an insfilterNonholonomic object.

\section*{Output Arguments}
newFilter - New copied filter
insfitlerNonholonomic
New copied filter, returned as an insfilterNonholonomic object.

\section*{See Also}
insfilterNonholonomic
Introduced in R2020b

\section*{fusegps}

Correct states using GPS data for insfilterNonholonomic

\section*{Syntax}
[res,resCov] = fusegps(FUSE,position,positionCovariance)
[res,resCov] = fusegps(FUSE,position,positionCovariance,velocity, velocityCovariance)

\section*{Description}
[res,resCov] = fusegps(FUSE,position, positionCovariance) fuses GPS position data to correct the state estimate.
[res,resCov] = fusegps(FUSE,position,positionCovariance,velocity, velocityCovariance) fuses GPS position and velocity data to correct the state estimate.

\section*{Input Arguments}

FUSE - insfilterNonholonomic object
object
insfilterNonholonomic, specified as an object.
position - Position of GPS receiver (LLA)
3-element row vector
Position of GPS receiver in geodetic latitude, longitude, and altitude (LLA) specified as a real finite 3element row vector. Latitude and longitude are in degrees with north and east being positive. Altitude is in meters.
Data Types: single | double
positionCovariance - Position measurement covariance of GPS receiver ( \(\mathbf{m}^{\mathbf{2}}\) )
3-by-3 matrix
Position measurement covariance of GPS receiver in \(\mathrm{m}^{2}\), specified as a 3-by-3 matrix.
Data Types: single | double
velocity - Velocity of GPS receiver in local NED coordinate system ( \(\mathrm{m} / \mathrm{s}\) )
3-element row vector
Velocity of the GPS receiver in the local NED coordinate system in \(\mathrm{m} / \mathrm{s}\), specified as a 3-element row vector.
Data Types: single | double
velocityCovariance - Velocity measurement covariance of GPS receiver ( \(\mathbf{m} / \mathbf{s}^{\mathbf{2}}\) )
3-by-3 matrix

Velocity measurement covariance of the GPS receiver in the local NED coordinate system in \(\mathrm{m} / \mathrm{s}^{2}\), specified as a 3-by-3 matrix.

Data Types: single|double

\section*{Output Arguments}

\section*{res - Position and course residual}

1 -by-4 vector of real values
Position and course residual, returned as a 1-by-6 vector of real values in \(m\) and rad/s, respectively.
resCov - Residual covariance
4-by-4 matrix of real values
Residual covariance, returned as a 4-by-4 matrix of real values.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® \({ }^{\circledR}\) Coder \(^{\text {TM }}\).

\section*{See Also}
insfilter|insfilterNonholonomic
Introduced in R2018b

\section*{pose}

Current orientation and position estimate for insfilterNonholonomic

\section*{Syntax}
[position,orientation, velocity] = pose(FUSE)
[position,orientation, velocity] = pose(FUSE,format)

\section*{Description}
[position,orientation, velocity] = pose(FUSE) returns the current estimate of the pose.
[position,orientation, velocity] = pose(FUSE,format)returns the current estimate of the pose with orientation in the specified orientation format.

\section*{Input Arguments}

FUSE - NHConstrainedIMUGPSFuser object
object
insfilterNonholonomic, specified as an object.

\section*{format - Output orientation format}
'quaternion' (default) | 'rotmat'
Output orientation format, specified as either 'quaternion' for a quaternion or 'rotmat' for a rotation matrix.
Data Types: char | string

\section*{Output Arguments}
position - Position estimate expressed in the local coordinate system (m)
three-element row vector
Position estimate expressed in the local coordinate system of the filter in meters, returned as a threeelement row vector.
Data Types: single | double
orientation - Orientation estimate expressed in the local coordinate system
quaternion (default) | 3-by-3 rotation matrix
Orientation estimate expressed in the local coordinate system of the filter, returned as a scalar quaternion or 3-by-3 rotation matrix. The quaternion or rotation matrix represents a frame rotation from the local reference frame of the filter to the body reference frame.
Data Types: single | double | quaternion
velocity - Velocity estimate expressed in local coordinate system (m/s)
3 -element row vector

Velocity estimate expressed in the local coordinate system of the filter in \(\mathrm{m} / \mathrm{s}\), returned as a 3-element row vector.

Data Types: single | double

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}
insfilter|insfilterNonholonomic
Introduced in R2018b

\section*{predict}

Update states using accelerometer and gyroscope data for insfilterNonholonomic

\section*{Syntax}
predict(FUSE, accelReadings,gyroReadings)

\section*{Description}
predict(FUSE, accelReadings,gyroReadings) fuses accelerometer and gyroscope data to update the state estimate.

\section*{Input Arguments}

FUSE - insfilterNonholonomic object
object
insfilterNonholonomic, specified as an object.
accelReadings - Accelerometer readings in local sensor body coordinate system (m/s \({ }^{\mathbf{2}}\) )
3 -element row vector
Accelerometer readings in \(\mathrm{m} / \mathrm{s}^{2}\), specified as a 3 -element row vector.
Data Types: single | double
gyroReadings - Gyroscope readings in local sensor body coordinate system (rad/s)
3-element row vector
Gyroscope readings in rad/s, specified as a 3 -element row vector.
Data Types: single | double

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also \\ insfilter|insfilterNonholonomic}

Introduced in R2018b

\section*{reset}

Reset internal states for insfilterNonholonomic

\section*{Syntax}
reset (FUSE)

\section*{Description}
reset (FUSE) resets the State, StateCovariance, and internal integrators to their default values.

\section*{Input Arguments}

FUSE - insfilterNonholonomic object
object
insfilterNonholonomic, specified as an object.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}
insfilter|insfilterNonholonomic

Introduced in R2018b

\section*{residual}

Residuals and residual covariances from direct state measurements for insfilterNonholonomic

\section*{Syntax}
[res, resCov]= residual(FUSE,idx,measurement,measurementCovariance)

\section*{Description}
[res, resCov]= residual(FUSE,idx,measurement,measurementCovariance) computes the residual, res, and the residual covariance, resCov, based on the direct state measurement and measurement covariance. The measurement maps directly to the states specified by indices, idx.

\section*{Input Arguments}

FUSE - insfilterNonholonomic object
object
insfilterNonholonomic, specified as an object.

\section*{idx - State vector Index of measurement to correct}
\(N\)-element vector of increasing integers in the range \([1,16]\)
State vector index of measurement to correct, specified as an \(N\)-element vector of increasing integers in the range [1,16].

The state values represent:
\begin{tabular}{lll} 
State & Units & Index \\
Orientation (quaternion parts) & & \(1: 4\) \\
Gyroscope bias (XYZ) & \(\mathrm{rad} / \mathrm{s}\) & \(5: 7\) \\
Position (NED) & m & \(8: 10\) \\
Velocity (NED) & \(\mathrm{m} / \mathrm{s}\) & \(11: 13\) \\
Accelerometer Bias (XYZ) & \(\mathrm{m} / \mathrm{s}^{2}\) & \(14: 16\)
\end{tabular}

Data Types: single | double

\section*{measurement - Direct measurement of state}
\(N\)-element vector
Direct measurement of state, specified as a \(N\)-element vector. \(N\) is the number of elements of the index argument, idx.

\section*{measurementCovariance - Covariance of measurement \\ \(N\)-by- \(N\) matrix}

Covariance of measurement, specified as an \(N\)-by- \(N\) matrix. \(N\) is the number of elements of the index argument, idx.

\section*{Output Arguments}
res - Measurement residual
1 -by- \(N\) vector of real values
Measurement residual, returned as a 1-by- \(N\) vector of real values.
resCov - Residual covariance
\(N\)-by- \(N\) matrix of real values
Residual covariance, returned as a \(N\)-by- \(N\) matrix of real values.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® \(\operatorname{Coder}^{\text {™ }}\).

\section*{See Also}
insfilter|insfilterNonholonomic

Introduced in R2020a

\section*{residualgps}

Residuals and residual covariance from GPS measurements for insfilterNonholonomic

\section*{Syntax}
[res,resCov] = residualgps(FUSE,position,positionCovariance)
[res,resCov] = residualgps(FUSE,position, positionCovariance,velocity, velocityCovariance)

\section*{Description}
[res,resCov] = residualgps(FUSE, position, positionCovariance) computes the residual, res, and the residual covariance, resCov, based on the GPS position measurement and covariance.
[res,resCov] = residualgps(FUSE,position, positionCovariance, velocity, velocityCovariance) computes the residual, res, and the residual covariance, resCov, based on the GPS position measurement and covariance.

\section*{Input Arguments}

FUSE - insfilterNonholonomic object
object
insfilterNonholonomic, specified as an object.
position - Position of GPS receiver (LLA)
3 -element row vector
Position of GPS receiver in geodetic latitude, longitude, and altitude (LLA) specified as a real finite 3element row vector. Latitude and longitude are in degrees with north and east being positive. Altitude is in meters.

\section*{Data Types: single | double}
positionCovariance - Position measurement covariance of GPS receiver ( \(\mathbf{m}^{\mathbf{2}}\) )
3-by-3 matrix
Position measurement covariance of GPS receiver in \(\mathrm{m}^{2}\), specified as a 3 -by- 3 matrix.
Data Types: single | double

\section*{velocity - Velocity of GPS receiver in local NED coordinate system (m/s)}

3-element row vector
Velocity of the GPS receiver in the local NED coordinate system in \(\mathrm{m} / \mathrm{s}\), specified as a 3 -element row vector.

Data Types: single | double
velocityCovariance - Velocity measurement covariance of GPS receiver ( \(\mathbf{m} / \mathbf{s}^{\mathbf{2}}\) )
3-by-3 matrix

Velocity measurement covariance of the GPS receiver in the local NED coordinate system in \(\mathrm{m} / \mathrm{s}^{2}\), specified as a 3-by-3 matrix.

Data Types: single|double

\section*{Output Arguments}

\section*{res - Position and course residual}

1-by-3 vector of real values | 1-by-4 vector of real values
Position and course residual, returned as a 1-by-3 vector of real values the inputs only contain position information, and returned as a 1-by-4 vector of real values if the inputs also contain velocity information.

\section*{resCov - Residual covariance}

3-by-3 matrix of real values | 4-by-4 matrix of real values
Residual covariance, returned as a 3-by-3 matrix of real values if the inputs only contain position information, and a 4 -by- 4 vector of real values if the inputs also contain velocity information.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).

\section*{See Also}
insfilterNonholonomic
Introduced in R2020a

\section*{stateinfo}

Display state vector information for insfilterNonholonomic

\section*{Syntax}
```

stateinfo(FUSE)
info = stateinfo(FUSE)

```

\section*{Description}
stateinfo(FUSE) displays the meaning of each index of the State property and the associated units.
info = stateinfo(FUSE) returns a structure with fields containing descriptions of the elements of the state vector of the filter, FUSE.

\section*{Examples}

\section*{State information of insfilterNonholonomic}

Create an insfilterNonholonomic object.
```

filter = insfilterErrorState;

```

Display the state information of the created filter.
```

stateinfo(filter)

| States | Units | Index |
| :--- | :--- | :--- |
| Orientation (quaternion parts) |  | $1: 4$ |
| Position (NAV) | m | $5: 7$ |
| Velocity (NAV) | $\mathrm{m} / \mathrm{s}$ | $8: 10$ |
| Gyroscope Bias (XYZ) | $\mathrm{rad} / \mathrm{s}$ | $11: 13$ |
| Accelerometer Bias (XYZ) | $\mathrm{m} / \mathrm{s}^{2}$ | $14: 16$ |
| Visual Odometry Scale |  | 17 |

```

Output the state information of the filter as a structure.
```

info = stateinfo(filter)
info = struct with fields:
Orientation: [lllll
Position: [5 6 7]
Velocity: [8 9 10]
GyroscopeBias: [11 12 13]
AccelerometerBias: [14 15 16]
VisualOdometryScale: 17

```

\section*{Input Arguments}

\section*{FUSE - insfilterNonholonomic object}
object
insfilterNonholonomic, specified as an object.

\section*{Output Arguments}

\section*{info - State information}

\section*{structure}

State information, returned as a structure. The field names of the structure are names of the elements of the state vector in the filter. The values of each field are the corresponding indices of the state vector.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}
insfilter|insfilterNonholonomic
Introduced in R2018b

\section*{tune}

Tune insfilterNonholonomic parameters to reduce estimation error

\section*{Syntax}
tunedMeasureNoise = tune(filter,measureNoise, sensorData,groundTruth) tunedMeasureNoise \(=\) tune( \(\qquad\) , config)

\section*{Description}
tunedMeasureNoise = tune(filter,measureNoise, sensorData,groundTruth) adjusts the properties of the insfilterNonholonomic filter object, filter, and measurement noises to reduce the root-mean-squared (RMS) state estimation error between the fused sensor data and the ground truth. The function also returns the tuned measurement noise, tunedMeasureNoise. The function uses the property values in the filter and the measurement noise provided in the measureNoise structure as the initial estimate for the optimization algorithm.
tunedMeasureNoise = tune( \(\qquad\) , config) specifies the tuning configuration based on a tunerconfig object, config.

\section*{Examples}

\section*{Tune insfilterNonholonomic to Optimize Pose Estimate}

Load the recorded sensor data and ground truth data.
load('insfilterNonholonomicTuneData.mat');
Create tables for the sensor data and the truth data.
```

sensorData = table(Accelerometer, Gyroscope, ...
GPSPosition, GPSVelocity);
groundTruth = table(Orientation, Position);

```

Create an insfilterNonholonimic filter object.
```

filter = insfilterNonholonomic('State', initialState, ...
'StateCovariance', initialStateCovariance, ...
'DecimationFactor', 1);

```

Create a tuner configuration object for the filter. Set the maximum number of iterations to 30 .
```

config = tunerconfig('insfilterNonholonomic','MaxIterations',30);

```

Use the tunernoise function to obtain a set of initial sensor noises used in the filter.
```

measNoise = tunernoise('insfilterNonholonomic')
measNoise = struct with fields:
GPSPositionNoise: 1

```

GPSVelocityNoise: 1

Tune the filter and obtain the tuned measurement noise.
tunedNoise = tune(filter, measNoise, sensorData,groundTruth, config);
\begin{tabular}{|c|c|c|}
\hline Iteration & Parameter & Metric \\
\hline 1 & \(\overline{\text { GyroscopeNoise }}\) & 3.4877 \\
\hline 1 & AccelerometerNoise & 3.3961 \\
\hline 1 & GyroscopeBiasNoise & 3.3961 \\
\hline 1 & GyroscopeBiasDecayFactor & 3.3961 \\
\hline 1 & AccelerometerBiasNoise & 3.3961 \\
\hline 1 & AccelerometerBiasDecayFactor & 3.3961 \\
\hline 1 & ZeroVelocityConstraintNoise & 3.3935 \\
\hline 1 & GPSPositionNoise & 3.2848 \\
\hline 1 & GPSVelocityNoise & 3.2798 \\
\hline 2 & GyroscopeNoise & 3.2641 \\
\hline 2 & AccelerometerNoise & 3.1715 \\
\hline 2 & GyroscopeBiasNoise & 3.1715 \\
\hline 2 & GyroscopeBiasDecayFactor & 2.9661 \\
\hline 2 & AccelerometerBiasNoise & 2.9661 \\
\hline 2 & AccelerometerBiasDecayFactor & 2.9661 \\
\hline 2 & ZeroVelocityConstraintNoise & 2.9617 \\
\hline 2 & GPSPositionNoise & 2.8438 \\
\hline 2 & GPSVelocityNoise & 2.8384 \\
\hline 3 & GyroscopeNoise & 2.8373 \\
\hline 3 & AccelerometerNoise & 2.7382 \\
\hline 3 & GyroscopeBiasNoise & 2.7382 \\
\hline 3 & GyroscopeBiasDecayFactor & 2.7382 \\
\hline 3 & AccelerometerBiasNoise & 2.7382 \\
\hline 3 & AccelerometerBiasDecayFactor & 2.7382 \\
\hline 3 & ZeroVelocityConstraintNoise & 2.7335 \\
\hline 3 & GPSPositionNoise & 2.6105 \\
\hline 3 & GPSVelocityNoise & 2.6045 \\
\hline 4 & GyroscopeNoise & 2.6023 \\
\hline 4 & AccelerometerNoise & 2.5001 \\
\hline 4 & GyroscopeBiasNoise & 2.5001 \\
\hline 4 & GyroscopeBiasDecayFactor & 2.5001 \\
\hline 4 & AccelerometerBiasNoise & 2.5001 \\
\hline 4 & AccelerometerBiasDecayFactor & 2.5001 \\
\hline 4 & ZeroVelocityConstraintNoise & 2.4953 \\
\hline 4 & GPSPositionNoise & 2.3692 \\
\hline 4 & GPSVelocityNoise & 2.3626 \\
\hline 5 & GyroscopeNoise & 2.3595 \\
\hline 5 & AccelerometerNoise & 2.2561 \\
\hline 5 & GyroscopeBiasNoise & 2.2561 \\
\hline 5 & GyroscopeBiasDecayFactor & 2.2508 \\
\hline 5 & AccelerometerBiasNoise & 2.2508 \\
\hline 5 & AccelerometerBiasDecayFactor & 2.2508 \\
\hline 5 & ZeroVelocityConstraintNoise & 2.2469 \\
\hline 5 & GPSPositionNoise & 2.1265 \\
\hline 5 & GPSVelocityNoise & 2.1191 \\
\hline 6 & GyroscopeNoise & 2.1148 \\
\hline 6 & AccelerometerNoise & 2.0150 \\
\hline 6 & GyroscopeBiasNoise & 2.0150 \\
\hline 6 & GyroscopeBiasDecayFactor & 2.0150 \\
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\begin{tabular}{|c|c|c|}
\hline 6 & AccelerometerBiasNoise & 2.0150 \\
\hline 6 & AccelerometerBiasDecayFactor & 2.0150 \\
\hline 6 & ZeroVelocityConstraintNoise & 2.0116 \\
\hline 6 & GPSPositionNoise & 1.8970 \\
\hline 6 & GPSVelocityNoise & 1.8888 \\
\hline 7 & GyroscopeNoise & 1.8847 \\
\hline 7 & AccelerometerNoise & 1.7921 \\
\hline 7 & GyroscopeBiasNoise & 1.7921 \\
\hline 7 & GyroscopeBiasDecayFactor & 1.7845 \\
\hline 7 & AccelerometerBiasNoise & 1.7845 \\
\hline 7 & AccelerometerBiasDecayFactor & 1.7845 \\
\hline 7 & ZeroVelocityConstraintNoise & 1.7815 \\
\hline 7 & GPSPositionNoise & 1.6794 \\
\hline 7 & GPSVelocityNoise & 1.6708 \\
\hline 8 & GyroscopeNoise & 1.6679 \\
\hline 8 & AccelerometerNoise & 1.5886 \\
\hline 8 & GyroscopeBiasNoise & 1.5886 \\
\hline 8 & GyroscopeBiasDecayFactor & 1.5866 \\
\hline 8 & AccelerometerBiasNoise & 1.5866 \\
\hline 8 & AccelerometerBiasDecayFactor & 1.5866 \\
\hline 8 & ZeroVelocityConstraintNoise & 1.5850 \\
\hline 8 & GPSPositionNoise & 1.5057 \\
\hline 8 & GPSVelocityNoise & 1.4965 \\
\hline 9 & GyroscopeNoise & 1.4950 \\
\hline 9 & AccelerometerNoise & 1.4364 \\
\hline 9 & GyroscopeBiasNoise & 1.4364 \\
\hline 9 & GyroscopeBiasDecayFactor & 1.4364 \\
\hline 9 & AccelerometerBiasNoise & 1.4364 \\
\hline 9 & AccelerometerBiasDecayFactor & 1.4364 \\
\hline 9 & ZeroVelocityConstraintNoise & 1.4355 \\
\hline 9 & GPSPositionNoise & 1.3894 \\
\hline 9 & GPSVelocityNoise & 1.3790 \\
\hline 10 & GyroscopeNoise & 1.3773 \\
\hline 10 & AccelerometerNoise & 1.3422 \\
\hline 10 & GyroscopeBiasNoise & 1.3422 \\
\hline 10 & GyroscopeBiasDecayFactor & 1.3421 \\
\hline 10 & AccelerometerBiasNoise & 1.3421 \\
\hline 10 & AccelerometerBiasDecayFactor & 1.3421 \\
\hline 10 & ZeroVelocityConstraintNoise & 1.3399 \\
\hline 10 & GPSPositionNoise & 1.3319 \\
\hline 10 & GPSVelocityNoise & 1.3190 \\
\hline 11 & GyroscopeNoise & 1.3159 \\
\hline 11 & AccelerometerNoise & 1.3102 \\
\hline 11 & GyroscopeBiasNoise & 1.3102 \\
\hline 11 & GyroscopeBiasDecayFactor & 1.3100 \\
\hline 11 & AccelerometerBiasNoise & 1.3100 \\
\hline 11 & AccelerometerBiasDecayFactor & 1.3100 \\
\hline 11 & ZeroVelocityConstraintNoise & 1.3069 \\
\hline 11 & GPSPositionNoise & 1.2964 \\
\hline 11 & GPSVelocityNoise & 1.2762 \\
\hline 12 & GyroscopeNoise & 1.2740 \\
\hline 12 & AccelerometerNoise & 1.2655 \\
\hline 12 & GyroscopeBiasNoise & 1.2655 \\
\hline 12 & GyroscopeBiasDecayFactor & 1.2641 \\
\hline 12 & AccelerometerBiasNoise & 1.2641 \\
\hline 12 & AccelerometerBiasDecayFactor & 1.2641 \\
\hline 12 & ZeroVelocityConstraintNoise & 1.2631 \\
\hline 12 & GPSPositionNoise & 1.2511 \\
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\end{tabular}

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\hline GPSVelocityNoise & 1.2198 \\
\hline GyroscopeNoise & 1.2184 \\
\hline AccelerometerNoise & 1.2058 \\
\hline GyroscopeBiasNoise & 1.2058 \\
\hline GyroscopeBiasDecayFactor & 1.2029 \\
\hline AccelerometerBiasNoise & 1.2029 \\
\hline AccelerometerBiasDecayFactor & 1.2029 \\
\hline ZeroVelocityConstraintNoise & 1.2029 \\
\hline GPSPositionNoise & 1.1874 \\
\hline GPSVelocityNoise & 1.1408 \\
\hline GyroscopeNoise & 1.1403 \\
\hline AccelerometerNoise & 1.1236 \\
\hline GyroscopeBiasNoise & 1.1236 \\
\hline GyroscopeBiasDecayFactor & 1.1186 \\
\hline AccelerometerBiasNoise & 1.1186 \\
\hline AccelerometerBiasDecayFactor & 1.1186 \\
\hline ZeroVelocityConstraintNoise & 1.1183 \\
\hline GPSPositionNoise & 1.0975 \\
\hline GPSVelocityNoise & 1.0348 \\
\hline GyroscopeNoise & 1.0347 \\
\hline AccelerometerNoise & 1.0155 \\
\hline GyroscopeBiasNoise & 1.0155 \\
\hline GyroscopeBiasDecayFactor & 1.0081 \\
\hline AccelerometerBiasNoise & 1.0081 \\
\hline AccelerometerBiasDecayFactor & 1.0081 \\
\hline ZeroVelocityConstraintNoise & 1.0076 \\
\hline GPSPositionNoise & 0.9813 \\
\hline GPSVelocityNoise & 0.9078 \\
\hline GyroscopeNoise & 0.9074 \\
\hline AccelerometerNoise & 0.8926 \\
\hline GyroscopeBiasNoise & 0.8926 \\
\hline GyroscopeBiasDecayFactor & 0.8823 \\
\hline AccelerometerBiasNoise & 0.8823 \\
\hline AccelerometerBiasDecayFactor & 0.8823 \\
\hline ZeroVelocityConstraintNoise & 0.8815 \\
\hline GPSPositionNoise & 0.8526 \\
\hline GPSVelocityNoise & 0.7926 \\
\hline GyroscopeNoise & 0.7920 \\
\hline AccelerometerNoise & 0.7870 \\
\hline GyroscopeBiasNoise & 0.7870 \\
\hline GyroscopeBiasDecayFactor & 0.7742 \\
\hline AccelerometerBiasNoise & 0.7742 \\
\hline AccelerometerBiasDecayFactor & 0.7742 \\
\hline ZeroVelocityConstraintNoise & 0.7730 \\
\hline GPSPositionNoise & 0.7665 \\
\hline GPSVelocityNoise & 0.7665 \\
\hline GyroscopeNoise & 0.7662 \\
\hline AccelerometerNoise & 0.7638 \\
\hline GyroscopeBiasNoise & 0.7638 \\
\hline GyroscopeBiasDecayFactor & 0.7495 \\
\hline AccelerometerBiasNoise & 0.7495 \\
\hline AccelerometerBiasDecayFactor & 0.7495 \\
\hline ZeroVelocityConstraintNoise & 0.7482 \\
\hline GPSPositionNoise & 0.7482 \\
\hline GPSVelocityNoise & 0.7475 \\
\hline GyroscopeNoise & 0.7474 \\
\hline AccelerometerNoise & 0.7474 \\
\hline GyroscopeBiasNoise & 0.7474 \\
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\end{tabular}
\begin{tabular}{|c|c|}
\hline GyroscopeBiasDecayFactor & 0.7474 \\
\hline AccelerometerBiasNoise & 0.7474 \\
\hline AccelerometerBiasDecayFactor & 0.7474 \\
\hline ZeroVelocityConstraintNoise & 0.7453 \\
\hline GPSPositionNoise & 0.7416 \\
\hline GPSVelocityNoise & 0.7382 \\
\hline GyroscopeNoise & 0.7378 \\
\hline AccelerometerNoise & 0.7370 \\
\hline GyroscopeBiasNoise & 0.7370 \\
\hline GyroscopeBiasDecayFactor & 0.7370 \\
\hline AccelerometerBiasNoise & 0.7370 \\
\hline AccelerometerBiasDecayFactor & 0.7370 \\
\hline ZeroVelocityConstraintNoise & 0.7345 \\
\hline GPSPositionNoise & 0.7345 \\
\hline GPSVelocityNoise & 0.7345 \\
\hline GyroscopeNoise & 0.7334 \\
\hline AccelerometerNoise & 0.7334 \\
\hline GyroscopeBiasNoise & 0.7334 \\
\hline GyroscopeBiasDecayFactor & 0.7334 \\
\hline AccelerometerBiasNoise & 0.7334 \\
\hline AccelerometerBiasDecayFactor & 0.7334 \\
\hline ZeroVelocityConstraintNoise & 0.7306 \\
\hline GPSPositionNoise & 0.7279 \\
\hline GPSVelocityNoise & 0.7268 \\
\hline GyroscopeNoise & 0.7248 \\
\hline AccelerometerNoise & 0.7247 \\
\hline GyroscopeBiasNoise & 0.7247 \\
\hline GyroscopeBiasDecayFactor & 0.7234 \\
\hline AccelerometerBiasNoise & 0.7234 \\
\hline AccelerometerBiasDecayFactor & 0.7234 \\
\hline ZeroVelocityConstraintNoise & 0.7207 \\
\hline GPSPositionNoise & 0.7206 \\
\hline GPSVelocityNoise & 0.7170 \\
\hline GyroscopeNoise & 0.7138 \\
\hline AccelerometerNoise & 0.7134 \\
\hline GyroscopeBiasNoise & 0.7134 \\
\hline GyroscopeBiasDecayFactor & 0.7134 \\
\hline AccelerometerBiasNoise & 0.7134 \\
\hline AccelerometerBiasDecayFactor & 0.7134 \\
\hline ZeroVelocityConstraintNoise & 0.7122 \\
\hline GPSPositionNoise & 0.7122 \\
\hline GPSVelocityNoise & 0.7122 \\
\hline GyroscopeNoise & 0.7081 \\
\hline AccelerometerNoise & 0.7080 \\
\hline GyroscopeBiasNoise & 0.7080 \\
\hline GyroscopeBiasDecayFactor & 0.7080 \\
\hline AccelerometerBiasNoise & 0.7080 \\
\hline AccelerometerBiasDecayFactor & 0.7080 \\
\hline ZeroVelocityConstraintNoise & 0.7080 \\
\hline GPSPositionNoise & 0.7080 \\
\hline GPSVelocityNoise & 0.7072 \\
\hline GyroscopeNoise & 0.7009 \\
\hline AccelerometerNoise & 0.7009 \\
\hline GyroscopeBiasNoise & 0.7009 \\
\hline GyroscopeBiasDecayFactor & 0.7007 \\
\hline AccelerometerBiasNoise & 0.7007 \\
\hline AccelerometerBiasDecayFactor & 0.7007 \\
\hline ZeroVelocityConstraintNoise & 0.7005 \\
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\begin{tabular}{ll} 
GPSPositionNoise & 0.6997 \\
GPSVelocityNoise & 0.6997 \\
GyroscopeNoise & 0.6912 \\
AccelerometerNoise & 0.6906 \\
GyroscopeBiasNoise & 0.6906 \\
GyroscopeBiasDecayFactor & 0.6906 \\
AccelerometerBiasNoise & 0.6906 \\
AccelerometerBiasDecayFactor & 0.6906 \\
ZeroVelocityConstraintNoise & 0.6896 \\
GPSPositionNoise & 0.6896 \\
GPSVelocityNoise & 0.6896 \\
GyroscopeNoise & 0.6840 \\
AccelerometerNoise & 0.6831 \\
GyroscopeBiasNoise & 0.6831 \\
GyroscopeBiasDecayFactor & 0.6831 \\
AccelerometerBiasNoise & 0.6831 \\
AccelerometerBiasDecayFactor & 0.6831 \\
ZeroVelocityConstraintNoise & 0.6818 \\
GPSPositionNoise & 0.6816 \\
GPSVelocityNoise & 0.6816 \\
GyroscopeNoise & 0.6816 \\
AccelerometerNoise & 0.6809 \\
GyroscopeBiasNoise & 0.6809 \\
GyroscopeBiasDecayFactor & 0.6809 \\
AccelerometerBiasNoise & 0.6809 \\
AccelerometerBiasDecayFactor & 0.6809 \\
ZeroVelocityConstraintNoise & 0.6804 \\
GPSPositionNoise & 0.6802 \\
GPSVelocityNoise & 0.6802 \\
GyroscopeNoise & 0.6793 \\
AccelerometerNoise & 0.6785 \\
GyroscopeBiasNoise & 0.6785 \\
GyroscopeBiasDecayFactor & 0.6785 \\
AccelerometerBiasNoise & 0.6785 \\
AccelerometerBiasDecayFactor & 0.6785 \\
ZeroVelocityConstraintNoise & 0.6778 \\
GPSPositionNoise & 0.6773 \\
GPSVelocityNoise & 0.6773 \\
GyroscopeNoise & 0.6773 \\
AccelerometerNoise & 0.6769 \\
GyroscopeBiasNoise & 0.6769 \\
GyroscopeBiasDecayFactor & 0.6769 \\
AccelerometerBiasNoise & 0.6769 \\
GeroVelocityConstraintNoise & 0.6769 \\
GPSVelocityNoise & 0.6769 \\
\hline
\end{tabular}

Fuse the sensor data using the tuned filter. Obtain estimated pose and orientation.
```

N = size(sensorData,1);
qEstTuned = quaternion.zeros(N,1);
posEstTuned = zeros(N,3);
for ii=1:N
predict(filter,Accelerometer(ii,:),Gyroscope(ii,:));
if all(~isnan(GPSPosition(ii,1)))
fusegps(filter, GPSPosition(ii,:), ...
tunedNoise.GPSPositionNoise,GPSVelocity(ii,:), ...

```
tunedNoise.GPSVelocityNoise);
end
[posEstTuned(ii,:),qEstTuned(ii,:)] = pose(filter);
end
Compute the RMS errors.
orientationErrorTuned \(=\) rad2deg(dist(qEstTuned,Orientation));
rmsOrientationErrorTuned \(=\) sqrt(mean(orientationErrorTuned.^2))
rmsOrientationErrorTuned \(=1.6857\)
positionErrorTuned = sqrt(sum((posEstTuned-Position).^2,2));
rmsPositionErrorTuned \(=\) sqrt(mean(positionErrorTuned.^2))
rmsPositionErrorTuned = 1.6667
Visualize the results.
```

figure;
t = (0:N-1)./filter.IMUSampleRate;
subplot(2,1,1)
plot(t,positionErrorTuned,'b');
title("Tuned insfilterNonholonomic" + newline + ...
"Euclidean Distance Position Error")
xlabel('Time (s)');
ylabel('Position Error (meters)')
subplot(2,1,2)
plot(t,orientationErrorTuned,'b');
title("Orientation Error")
xlabel('Time (s)');
ylabel('Orientation Error (degrees)');

```


\section*{Input Arguments}

\section*{filter - Filter object}
infilterAsync object
Filter object, specified as an insfilterNonholonomic object.

\section*{measureNoise - Measurement noise}
structure
Measurement noise, specified as a structure. The function uses the measurement noise input as the initial guess for tuning the measurement noise. The structure must contain these fields:
\begin{tabular}{|l|l|}
\hline Field name & Description \\
\hline GPSPositionNoise & \begin{tabular}{l} 
Variance of GPS position noise, specified as a \\
scalar in \(\mathrm{m}^{2}\)
\end{tabular} \\
\hline GPSVelocityNoise & \begin{tabular}{l} 
Variance of GPS velocity noise, specified as a \\
scalar in \((\mathrm{m} / \mathrm{s})^{2}\)
\end{tabular} \\
\hline
\end{tabular}

\section*{Data Types: struct}

\section*{sensorData - Sensor data \\ table}

Sensor data, specified as a table. In each row, the sensor data is specified as:
- Accelerometer - Accelerometer data, specified as a 1-by-3 vector of scalars in \(\mathrm{m}^{2} / \mathrm{s}\).
- Gyroscope - Gyroscope data, specified as a 1-by-3 vector of scalars in rad/s.
- GPSPosition - GPS position data, specified as a 1-by-3 vector of scalars in meters.
- GPSVelocity - GPS velocity data, specified as a 1-by-3 vector of scalars in m/s.

If the GPS sensor does not produce complete measurements, specify the corresponding entry for GPSPosition and/or GPSVelocity as NaN. If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the sensorData input based on your choice.

Data Types: table

\section*{groundTruth - Ground truth data \\ table}

Ground truth data, specified as a table. In each row, the table can optionally contain any of these variables:
- Orientation - Orientation from the navigation frame to the body frame, specified as a quaternion or a 3-by-3 rotation matrix.
- Position - Position in navigation frame, specified as a 1-by-3 vector of scalars in meters.
- Velocity - Velocity in navigation frame, specified as a 1 -by-3 vector of scalars in \(\mathrm{m} / \mathrm{s}\).
- GyroscopeBias - Gyroscope delta angle bias in body frame, specified as a 1-by-3 vector of scalars in rad/s.
- AccelerometerBias - Accelerometer delta angle bias in body frame, specified as a 1-by-3 vector of scalars in \(\mathrm{m}^{2} / \mathrm{s}\).

The function processes each row of the sensorData and groundTruth tables sequentially to calculate the state estimate and RMS error from the ground truth. State variables not present in groundTruth input are ignored for the comparison. The sensorData and the groundTruth tables must have the same number of rows.

If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the groundTruth input based on your choice.
Data Types: table
config - Tuner configuration
tunerconfig object
Tuner configuration, specified as a tunerconfig object.

\section*{Output Arguments}

\section*{tunedMeasureNoise - Tuned measurement noise}
structure
Tuned measurement noise, returned as a structure. The structure contains these fields.
\begin{tabular}{|l|l|}
\hline Field name & Description \\
\hline GPSPositionNoise & \begin{tabular}{l} 
Variance of GPS position noise, specified as a \\
scalar in \(\mathrm{m}^{2}\)
\end{tabular} \\
\hline GPSVelocityNoise & \begin{tabular}{l} 
Variance of GPS velocity noise, specified as a \\
scalar in \((\mathrm{m} / \mathrm{s})^{2}\)
\end{tabular} \\
\hline
\end{tabular}

\section*{Data Types: struct}

\section*{References}
[1] Abbeel, Pieter, et al. "Discriminative Training of Kalman Filters." Robotics: Science and Systems I, Robotics: Science and Systems Foundation, 2005. DOI.org (Crossref), doi:10.15607/ RSS.2005.I.038.

\section*{See Also}
tunerconfig|tunernoise|insfilterNonholonomic
Introduced in R2020b

\section*{occupancyMap}

Create occupancy map with probabilistic values

\section*{Description}
occupancyMap creates a 2-D occupancy grid map object. Each cell in the occupancy grid has a value representing the probability of the occupancy of that cell. Values close to 1 represent a high probability that the cell contains an obstacle. Values close to 0 represent a high probability that the cell is not occupied and obstacle free.

Occupancy maps are used in navigation algorithms such as path planning (see plannerRRT). They are also used in mapping applications for finding collision-free paths, performing collision avoidance, and calculating localization (see monteCarloLocalization). You can modify your occupancy map to fit your specific application.

The occupancyMap objects support local coordinates, world coordinates, and grid indices. The first grid location with index \((1,1)\) begins in the top-left corner of the grid.

Use the occupancyMap class to create 2-D maps of an environment with probability values representing different obstacles in your world. You can specify exact probability values of cells or include observations from sensors such as laser scanners.

Probability values are stored using a binary Bayes filter to estimate the occupancy of each grid cell. A log-odds representation is used, with values stored as int16 to reduce the map storage size and allow for real-time applications.

\section*{Creation}

\section*{Syntax}
```

map = occupancyMap(width,height)
map = occupancyMap(width,height,resolution)
map = occupancyMap(rows,cols,resolution,'grid')
map = occupancyMap(p)
map = occupancyMap(p,resolution)
map = occupancyMap(sourcemap)
map = occupancyMap(sourcemap,resolution)

```

\section*{Description}
map = occupancyMap(width, height) creates a 2-D occupancy map object representing a world space of width and height in meters. The default grid resolution is 1 cell per meter.
map = occupancyMap(width, height, resolution) creates an occupancy map with a specified grid resolution in cells per meter. resolution sets the "Resolution" on page 2-0 property.
map \(=\) occupancyMap (rows, cols, resolution, 'grid') creates an occupancy map with the specified number of rows and columns and with the resolution in cells per meter. The values of rows and cols sets the "GridSize" on page 2-0 property.
\(\operatorname{map}=\) occupancyMap \((p)\) creates an occupancy map from the values in matrix \(p\). The grid size matches the size of the matrix, with each cell probability value interpreted from the matrix location.
map \(=\) occupancyMap( \(p\), resolution) creates an occupancy map from the specified matrix and resolution in cells per meter.
map \(=\) occupancyMap(sourcemap) creates an object using values from another occupancyMap object.
map \(=\) occupancyMap (sourcemap, resolution) creates an object using values from another occupancyMap object, but resamples the matrix to have the specified resolution.

\section*{Input Arguments}
width - Map width
scalar
Map width, specified as a scalar in meters.

\section*{height - Map height}
scalar
Map height, specified as a scalar in meters.

\section*{resolution - Grid resolution}

1 (default) | scalar
Grid resolution, specified as a scalar in cells per meter.
rows - Number of rows in grid
positive scalar integer
Number of rows in grid, specified as a positive scalar integer.

\section*{cols - Number of columns in grid}
positive scalar integer
Number of columns in grid, specified as a positive scalar integer.

\section*{p - Input occupancy grid}
matrix of probability values from 0 to 1
Input occupancy grid, specified as a matrix of probability values from 0 to 1 . The size of the grid matches the size of the matrix. Each matrix element corresponds to the probability of the grid cell location being occupied. Values close to 1 represent a high certainty that the cell contains an obstacle. Values close to 0 represent certainty that the cell is not occupied and obstacle free.

\section*{sourcemap - Occupancy map object}
occupancyMap object
Occupancy map object, specified as a occupancyMap object.

\section*{Properties}

\section*{FreeThreshold - Threshold below which cells are considered obstacle-free scalar between 0 and 1}

Threshold below which cells are considered obstacle-free, specified as a scalar between 0 and 1 inclusive. Cells with probability values below this threshold are considered obstacle free. This property also defines the free locations for path planning when using objects like plannerRRT.

Data Types: double

\section*{OccupiedThreshold - Threshold above which cells are considered occupied scalar}

Threshold above which cells are considered occupied, specified as a scalar. Cells with probability values above this threshold are considered occupied.

\section*{Data Types: double}

ProbabilitySaturation - Saturation limits for probability
[0.001 0.999] (default)| two-element real-valued vector
Saturation limits for probability, specified as a 1-by-2 real-valued vector representing the minimum and maximum values, in that order. Values above or below these saturation values are set to the minimum and maximum values. This property reduces oversaturating of cells when incorporating multiple observations.
Data Types: double

\section*{GridSize - Number of rows and columns in grid}
two-element integer-valued vector
This property is read-only.
Number of rows and columns in grid, stored as a 1-by-2 real-valued vector representing the number of rows and columns, in that order.

Data Types: double

\section*{Resolution - Grid resolution}

1 (default) | scalar
This property is read-only.
Grid resolution, stored as a scalar in cells per meter representing the number and size of grid locations.
Data Types: double

\section*{XLocalLimits - Minimum and maximum values of \(x\)-coordinates in local frame \\ two-element vector}

This property is read-only.
Minimum and maximum values of \(x\)-coordinates in local frame, stored as a two-element horizontal vector of the form [min max]. Local frame is defined by LocalOriginInWorld property.
Data Types: double

\section*{YLocalLimits - Minimum and maximum values of \(\boldsymbol{y}\)-coordinates in local frame two-element vector}

This property is read-only.
Minimum and maximum values of \(y\)-coordinates in local frame, stored as a two-element horizontal vector of the form [min max]. Local frame is defined by LocalOriginInWorld property.
Data Types: double
XWorldLimits - Minimum and maximum world range values of \(\boldsymbol{x}\)-coordinates
two-element vector
This property is read-only.
Minimum and maximum world range values of \(x\)-coordinates, stored as a 1 -by-2 vector representing the minimum and maximum values, in that order.
Data Types: double
YWorldLimits - Minimum and maximum world range values of \(\boldsymbol{y}\)-coordinates
two-element vector
This property is read-only.
Minimum and maximum world range values of \(y\)-coordinates, stored as a 1 -by- 2 vector representing the minimum and maximum values, in that order.

Data Types: double
GridLocationInWorld - [xy] world coordinates of grid
[0 0] (default) | two-element vector
\([x, y]\) world coordinates of the bottom-left corner of the grid, specified as a 1-by-2 vector.
Data Types: double
LocalOriginInWorld - Location of the local frame in world coordinates
[0 0] (default)|two-element vector | [xWorld yWorld]
Location of the origin of the local frame in world coordinates, specified as a two-element vector, [xLocal yLocal]. Use the move function to shift the local frame as your vehicle moves.

Data Types: double

\section*{GridOriginInLocal - Location of the grid in local coordinates}
[0 0] (default)|two-element vector | [xLocal yLocal]
Location of the bottom-left corner of the grid in local coordinates, specified as a two-element vector, [xLocal yLocal].
Data Types: double
DefaultValue - Default value for unspecified map locations
0.5 (default) | scalar between 0 and 1

Default value for unspecified map locations including areas outside the map, specified as a scalar between 0 and 1 inclusive.

Data Types: double

\section*{Object Functions}
\begin{tabular}{ll} 
checkOccupancy & Check locations for free, occupied, or unknown values \\
copy & Create copy of occupancy grid \\
getOccupancy & Get occupancy value of locations \\
grid2local & Convert grid indices to local coordinates \\
grid2world & Convert grid indices to world coordinates \\
inflate & Inflate each occupied grid location \\
insertRay & Insert ray from laser scan observation \\
local2grid & Convert local coordinates to grid indices \\
local2world & Convert local coordinates to world coordinates \\
move & Move map in world frame \\
occupancyMatrix & Convert occupancy grid to double matrix \\
raycast & Compute cell indices along a ray \\
rayIntersection & Find intersection points of rays and occupied map cells \\
setOccupancy & Set occupancy value of locations \\
show & Show grid values in a figure \\
syncWith & Sync map with overlapping map \\
updateOccupancy & Integrate probability observations at locations \\
world2grid & Convert world coordinates to grid indices \\
world2local & Convert world coordinates to local coordinates
\end{tabular}

\section*{Examples}

\section*{Insert Laser Scans into Occupancy Map}

Create an empty occupancy grid map.
map \(=\) occupancyMap(10,10,20);
Input pose of the vehicle, ranges, angles, and the maximum range of the laser scan.
```

pose = [5,5,0];
ranges = 3*ones(100,1);
angles = linspace(-pi/2,pi/2,100);
maxrange = 20;

```

Create a lidarScan object with the specified ranges and angles.
```

scan = lidarScan(ranges,angles);

```

Insert the laser scan data into the occupancy map.
```

insertRay(map,pose,scan,maxrange);

```

Show the map to see the results of inserting the laser scan.
```

show(map)

```


Check the occupancy of the spot directly in front of the vehicle.
getOccupancy(map,[85])
ans \(=0.7000\)
Add a second reading and view the update to the occupancy values. The additional reading increases the confidence in the readings. The free and occupied values become more distinct.
insertRay(map, pose, scan,maxrange);
show(map)

getOccupancy (map,[85])
ans \(=0.8448\)

\section*{Convert PGM Image to Map}

Convert a portable graymap (PGM) file containing a ROS map into an occupancyMap for use in MATLAB.

Import the image using imread. Crop the image to the playpen area.
```

image = imread('playpen_map.pgm');
imageCropped = image(750:1250,750:1250);
imshow(imageCropped)

```


PGM values are expressed from 0 to 255 as uint8. Normalize these values by converting the cropped image to double and dividing each cell by 255 . This image shows obstacles as values close to 0 . Subtract the normalized image from 1 to get occupancy values with 1 representing occupied space.
```

imageNorm = double(imageCropped)/255;

```
imageOccupancy = 1 - imageNorm;

Create the occupancyMap object using an adjusted map image. The imported map resolution is 20 cells per meter.
```

map = occupancyMap(image0ccupancy,20);
show(map)

```


\section*{Limitations}

Occupancy values have a limited resolution of \(\pm 0.001\). The values are stored as int 16 using a logodds representation. This data type limits resolution, but saves memory when storing large maps in MATLAB. When calling set0ccupancy and then get0ccupancy, the value returned might not equal the value you set. For more information, see the log-odds representations section in "Occupancy Grids".

If memory size is a limitation, consider using binary0ccupancyMap instead. The binary occupancy map uses less memory with binary values, but still works with Navigation Toolbox \({ }^{\mathrm{TM}}\) algorithms and other applications.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and C++ code using MATLAB® \({ }^{\circledR}\) Coder \(^{\text {TM }}\).
As of MATLAB R2022a, default map behavior during code generation has changed, which may result in backwards compatibility issues. Maps such as occupancyMap now support fixed-size code generation (DynamicMemoryAllocation="off").

1 Maps that are either default-constructed or constructed with compile-time constant size information (or matrices that are of compile-time constant size) produce fixed-size maps.
2 To restore the previous behavior, use the coder.ignoreConst function when specifying size inputs, or coder.varsize matrix variable name specified as a string scalar or character vector, prior to constructing the map.

\section*{See Also}
binary0ccupancyMap | mobileRobotPRM| controllerPurePursuit|rosReadOccupancyGrid | rosWriteOccupancyGrid

\section*{Topics}
"Create Egocentric Occupancy Maps Using Range Sensors"
"Build Occupancy Map from Lidar Scans and Poses"
"Occupancy Grids"

\section*{Introduced in R2019b}

\section*{checkOccupancy}

Check locations for free, occupied, or unknown values

\section*{Syntax}
```

iOccval = checkOccupancy(map,xy)
iOccval = checkOccupancy(map,xy,'local')
iOccval = checkOccupancy(map,ij,'grid')
[iOccval,validPts] = checkOccupancy(

```
\(\qquad\)
``` )
occMatrix = checkOccupancy(map)
occMatrix = checkOccupancy(map,bottomLeft,matSize)
occMatrix = checkOccupancy(map,bottomLeft,matSize,'local')
occMatrix = checkOccupancy(map,topLeft,matSize,'grid')
```


## Description

iOccval = check0ccupancy (map, xy) returns an array of occupancy values at the xy locations. Each row is a separate xy location in the grid. Occupancy values can be obstacle free (0), occupied (1), or unknown ( -1 ) based on the OccupiedThreshold and FreeThreshold properties of the map object.
iOccval = check0ccupancy (map, xy,'local') returns an array of occupancy values at the $x y$ locations in the local frame. The local frame is based on the LocalOriginInWorld property of the map.
iOccval = check0ccupancy(map,ij,'grid') specifies ij grid cell indices instead of xy locations.
[iOccval, validPts] = checkOccupancy (__ ) also outputs an n-element vector of logical values indicating whether input coordinates are within the map limits.
occMatrix $=$ checkOccupancy(map) returns a matrix that contains the occupancy status of each location. Obstacle-free cells return 0, occupied cells return 1. Unknown locations, including outside the map, return - 1 .
occMatrix = checkOccupancy(map, bottomLeft, matSize) returns a matrix of occupancy values by specifying the bottom-left corner location in world coordinates and the matrix size in meters.
occMatrix = checkOccupancy(map,bottomLeft,matSize,' local') returns a matrix of occupancy values by specifying the bottom-left corner location in local coordinates and the matrix size in meters.
occMatrix = checkOccupancy(map,topLeft,matSize,'grid') returns a matrix of occupancy values by specifying the top-left corner location in grid coordinates and the grid size.

## Examples

## Get Occupancy Values and Check Occupancy Status

Access occupancy values and check their occupancy status based on the occupied and free thresholds of the occupancyMap object.

Create a matrix and populate it with values. Use this matrix to create an occupancy map.

```
p = 0.5*ones(20,20);
p(11:20,11:20) = 0.75*ones(10,10);
map = occupancyMap(p,10);
```

Get the occupancy of different locations and check their occupancy statuses. The occupancy status returns 0 for free space and 1 for occupied space. Unknown values return -1 .

```
pocc = getOccupancy(map,[1.5 1])
pocc = 0.7500
occupied = checkOccupancy(map,[1.5 1])
occupied = 1
pocc2 = get0ccupancy(map,[5 5],'grid')
pocc2 = 0.5000
occupied2 = checkOccupancy(map,[5 5],'grid')
occupied2 = -1
```


## Input Arguments

## map - Map representation

occupancyMap object
Map representation, specified as a occupancyMap object. This object represents the environment of the vehicle. The object contains a matrix grid with values representing the probability of the occupancy of that cell. Values close to 1 represent a high certainty that the cell contains an obstacle. Values close to 0 represent certainty that the cell is not occupied and obstacle free.

## xy - World coordinates

n-by-2 matrix
World coordinates, specified as an $n$-by-2 matrix of $\left[\begin{array}{ll}x & y\end{array}\right]$ pairs, where $n$ is the number of world coordinates.

Data Types: double

## ij - Grid positions

n-by-2 matrix
Grid positions, specified as an $n$-by-2 matrix of [ $\left.\begin{array}{ll}i & j\end{array}\right]$ pairs in [rows cols] format, where $n$ is the number of grid positions.
Data Types: double

## bottomLeft - Location of output matrix in world or local

two-element vector | [xCoord yCoord]
Location of bottom left corner of output matrix in world or local coordinates, specified as a twoelement vector, [xCoord yCoord]. Location is in world or local coordinates based on syntax.
Data Types: double
matSize - Output matrix size
two-element vector | [xLength yLength] |[gridRow gridCol]
Output matrix size, specified as a two-element vector, [xLength yLength], or [gridRow gridCol]. Size is in world, local, or grid coordinates based on syntax.
Data Types: double

## topLeft - Location of grid

two-element vector | [iCoord jCoord]
Location of top left corner of grid, specified as a two-element vector, [iCoord jCoord].
Data Types: double

## Output Arguments

## iOccval - Interpreted occupancy values

$n$-by-1 column vector
Interpreted occupancy values, returned as an $n$-by- 1 column vector equal in length to xy or ij .
Occupancy values can be obstacle free (0), occupied (1), or unknown ( -1 ). These values are determined from the actual probability values and the OccupiedThreshold and FreeThreshold properties of the map object.

## validPts - Valid map locations

$n$-by-1 column vector
Valid map locations, returned as an $n$-by- 1 column vector equal in length to xy or ij. Locations inside the map return a value of 1 . Locations outside the map limits return a value of 0 .

## occMatrix - Matrix of occupancy values <br> matrix

Matrix of occupancy values, returned as matrix with size equal to matSize or the size of your map. Occupancy values can be obstacle free (0), occupied (1), or unknown (-1).

## See Also

occupancyMap | get0ccupancy | binary0ccupancyMap

## Introduced in R2019b

## copy

Create copy of occupancy grid

## Syntax

copyMap $=$ copy (map)

## Description

copyMap $=$ copy (map) creates a deep copy of the occupancyMap object with the same properties.

## Examples

## Copy Occupancy Grid Map

Copy an occupancy grid map object. Once copied, the original object can be modified without affecting the copied map.

Create an occupancy grid with zeros for an empty map.

```
p = zeros(10);
map = occupancyMap(p);
```

Copy the occupancy grid map. Modify the original map. The copied map is not modified. Plot the two maps side by side.

```
mapCopy = copy(map);
setOccupancy(map,[1:3;1:3]',ones(3,1));
subplot(1,2,1)
show(map)
title('Original map')
subplot(1,2,2)
show(mapCopy)
title('Copied map')
```



## Input Arguments

## map - Map representation

occupancyMap object
Map representation, specified as a occupancyMap object. This object represents the environment of the vehicle. The object contains a matrix grid with values representing the probability of the occupancy of that cell. Values close to 1 represent a high probability that the cell contains an obstacle. Values close to 0 represent a high probability that the cell is not occupied and obstacle free.

## Output Arguments

copyMap - Copied map representation
occupancyMap object
Map representation, specified as a occupancyMap object. The properties are the same as the input object, map, but the copy has a different object handle.

## See Also

binary0ccupancyMap | occupancyMap | occupancyMatrix| get0ccupancy

## Topics

"Occupancy Grids"

Introduced in R2019b

## getOccupancy

Get occupancy value of locations

## Syntax

```
occVal = get0ccupancy(map,xy)
occVal = getOccupancy(map,xy,'local')
occVal = get0ccupancy(map,ij,'grid')
[occVal,validPts] = getOccupancy(
```

$\qquad$

```
occMatrix = get0ccupancy(map)
occMatrix = get0ccupancy(map,bottomLeft,matSize)
occMatrix = getOccupancy(map,bottomLeft,matSize,'local')
occMatrix = getOccupancy(map,topLeft,matSize,'grid')
```


## Description

occVal = getOccupancy (map,xy) returns an array of probability occupancy values at the xy locations in the world frame. Values close to 1 represent a high probability that the cell contains an obstacle. Values close to 0 represent a high probability that the cell is not occupied and obstacle free. Unknown locations, including outside the map, return map. DefaultValue.
occVal = getOccupancy (map, xy, 'local') returns an array of occupancy values at the $x y$ locations in the local frame.
occVal = getOccupancy(map,ij, 'grid') specifies ij grid cell indices instead of xy locations.
[occVal,validPts] = get0ccupancy( $\qquad$ ) additionally outputs an $n$-element vector of logical values indicating whether input coordinates are within the map limits.
occMatrix = get0ccupancy(map) returns all occupancy values in the map as a matrix.
occMatrix = get0ccupancy(map, bottomLeft, matSize) returns a matrix of occupancy values by specifying the bottom-left corner location in world coordinates and the matrix size in meters.
occMatrix = getOccupancy(map,bottomLeft,matSize,' local') returns a matrix of occupancy values by specifying the bottom-left corner location in local coordinates and the matrix size in meters.
occMatrix = getOccupancy(map,topLeft,matSize,'grid') returns a matrix of occupancy values by specifying the top-left corner location in grid indices and the matrix size.

## Examples

## Insert Laser Scans into Occupancy Map

Create an empty occupancy grid map.
map $=$ occupancyMap (10,10,20);

Input pose of the vehicle, ranges, angles, and the maximum range of the laser scan.

```
pose = [5,5,0];
ranges = 3*ones(100,1);
angles = linspace(-pi/2,pi/2,100);
maxrange = 20;
```

Create a lidarScan object with the specified ranges and angles.
scan = lidarScan(ranges,angles);
Insert the laser scan data into the occupancy map.
insertRay(map, pose, scan, maxrange);
Show the map to see the results of inserting the laser scan.
show(map)


Check the occupancy of the spot directly in front of the vehicle.
getOccupancy (map,[85])
ans $=0.7000$
Add a second reading and view the update to the occupancy values. The additional reading increases the confidence in the readings. The free and occupied values become more distinct.
insertRay(map,pose,scan,maxrange);
show (map)

get0ccupancy(map,[85])
ans $=0.8448$

## Get Occupancy Values and Check Occupancy Status

Access occupancy values and check their occupancy status based on the occupied and free thresholds of the occupancyMap object.

Create a matrix and populate it with values. Use this matrix to create an occupancy map.
$p=0.5 *$ ones $(20,20)$;
$p(11: 20,11: 20)=0.75 *$ ones $(10,10)$;
map $=$ occupancyMap( $p, 10$ );
Get the occupancy of different locations and check their occupancy statuses. The occupancy status returns 0 for free space and 1 for occupied space. Unknown values return -1 .
pocc $=$ getOccupancy(map,[1.5 1])
pocc $=0.7500$
occupied $=$ checkOccupancy(map,[1.5 1])

```
occupied = 1
pocc2 = getOccupancy(map,[5 5],'grid')
pocc2 = 0.5000
occupied2 = checkOccupancy(map,[5 5],'grid')
occupied2 = -1
```


## Input Arguments

## map - Map representation

occupancyMap object
Map representation, specified as a occupancyMap object. This object represents the environment of the vehicle. The object contains a matrix grid with values representing the probability of the occupancy of that cell. Values close to 1 represent a high probability that the cell contains an obstacle. Values close to 0 represent a high probability that the cell is not occupied and obstacle free.

## xy - World coordinates

$n$-by-2 matrix
World coordinates, specified as an $n$-by-2 matrix of $[x y]$ pairs, where $n$ is the number of world coordinates.
Data Types: double
ij - Grid positions
$n$-by-2 matrix
Grid positions, specified as an $n$-by-2 matrix of [ $i j$ ] pairs in [rows cols] format, where $n$ is the number of grid positions.
Data Types: double

## bottomLeft - Location of output matrix in world or local

two-element vector | [xCoord yCoord]
Location of bottom left corner of output matrix in world or local coordinates, specified as a twoelement vector, [xCoord yCoord]. Location is in world or local coordinates based on syntax.
Data Types: double
matSize - Output matrix size
two-element vector | [xLength yLength] |[gridRow gridCol]
Output matrix size, specified as a two-element vector, [xLength yLength] or [gridRow gridCol]. Size is in world, local, or grid coordinates based on syntax.
Data Types: double

## topLeft - Location of grid

two-element vector|[iCoord jCoord]
Location of top left corner of grid, specified as a two-element vector, [iCoord jCoord].

Data Types: double

## Output Arguments

## occVal - Probability occupancy values

column vector
Probability occupancy values, returned as a column vector the same length as either xy or ij .
Values close to 0 represent a high probability that the cell is not occupied and obstacle free.

## validPts - Valid map locations

$n$-by-1 column vector
Valid map locations, returned as an $n$-by- 1 column vector equal in length to xy or ij . Locations inside the map return a value of 1 . Locations outside the map limits return a value of 0 .

```
occMatrix - Matrix of occupancy values
matrix
```

Matrix of occupancy values, returned as matrix with size equal to matSize or the size of map.
Values close to 0 represent a high probability that the cell is not occupied and obstacle free.

## Limitations

Occupancy values have a limited resolution of $\pm 0.001$. The values are stored as int 16 using a logodds representation. This data type limits resolution, but saves memory when storing large maps in MATLAB. When calling setOccupancy and then getOccupancy, the value returned might not equal the value you set. For more information, see the log-odds representations section in "Occupancy Grids".

See Also<br>occupancyMap | checkOccupancy<br>Topics<br>"Occupancy Grids" (Robotics System Toolbox)

## Introduced in R2019b

## grid2local

Convert grid indices to local coordinates

## Syntax

xy = grid2local(map,ij)

## Description

xy = grid2local(map,ij) converts a [row col] array of grid indices, ij, to an array of local coordinates, xy.

## Input Arguments

map - Map representation
occupancyMap object | mapLayer object | multiLayerMap object
Map representation, specified as a occupancyMap, mapLayer, or multiLayerMap object.

## ij - Grid positions <br> $n$-by-2 vertical array

Grid positions, specified as an $n$-by-2 vertical array of [i j] pairs in [rows cols] format, where $n$ is the number of grid positions.

## Output Arguments

## xy - Local coordinates

$n$-by-2 vertical array
Local coordinates, specified as an $n$-by-2 vertical array of [ $\mathrm{x} y$ ] pairs, where $n$ is the number of local coordinates.

## See Also

grid2world| occupancyMap
Introduced in R2019b

## grid2world

Convert grid indices to world coordinates

## Syntax

xy = grid2world(map,ij)

## Description

xy = grid2world(map,ij) converts a [row col] array of grid indices, ij , to an array of world coordinates, $x y$.

## Input Arguments

map - Map representation
occupancyMap object | mapLayer object | multiLayerMap object
Map representation, specified as a occupancyMap, mapLayer, or multiLayerMap object.

## ij - Grid positions

n-by-2 matrix
Grid positions, specified as an $n$-by-2 matrix of [ $i j$ ] pairs in [rows cols] format, where $n$ is the number of grid positions. The grid cell locations are counted from the top left corner of the grid.
Data Types: double

## Output Arguments

## xy - World coordinates

n-by-2 matrix
World coordinates, returned as an $n$-by-2 matrix of [ $x y$ ] pairs, where $n$ is the number of world coordinates.

Data Types: double

## See Also

world2grid | grid2local| binary0ccupancyMap | occupancyMap
Topics
"Occupancy Grids"

Introduced in R2019b

## inflate

Inflate each occupied grid location

## Syntax

```
inflate(map,radius)
inflate(map,gridradius,'grid')
```


## Description

inflate(map,radius) inflates each occupied position of the specified map by the radius, specified in meters. Occupied location values are based on the map. OccupiedThreshold property. radius is rounded up to the nearest equivalent cell based on the resolution of the map. Values are modified using grayscale inflation to inflate higher probability values across the grid. This inflation increases the size of the occupied locations in the map.
inflate(map,gridradius,'grid') inflates each occupied position by the gridradius, specified in number of cells.

## Examples

## Create and Modify Occupancy Map

Create an empty map of 10-by-10 meters in size.
map $=$ occupancyMap(10,10,10);
Update the occupancy of specific world locations with new probability values and display the map.
$\mathrm{x}=[1.2 ; 2.3 ; 3.4 ; 4.5 ; 5.6]$;
y $=$ [5.0; 4.0; 3.0; 2.0; 1.0];
pvalues $=[0.2 ; 0.4 ; 0.6 ; 0.8 ; 1]$;
update0ccupancy(map,[x y],pvalues)
figure
show(map)


Inflate the occupied areas by a radius of 0.5 m . The larger occupancy values overwrite the smaller values.
inflate(map, 0.5)
figure
show(map)


Get the grid locations from the world locations.
ij = world2grid(map,[x y]);
Set occupancy values for the grid locations.
setOccupancy(map,ij,ones (5,1),'grid')
figure
show(map)


## Input Arguments

```
map - Map representation
occupancyMap object
```

Map representation, specified as a occupancyMap object. This object represents the environment of the vehicle. The object contains a matrix grid with values representing the probability of the occupancy of that cell. Values close to 1 represent a high probability that the cell contains an obstacle. Values close to 0 represent a high probability that the cell is not occupied and obstacle free.

## radius - Dimension that defines by how much to inflate occupied locations

scalar
Dimension that defines by how much to inflate occupied locations, specified as a scalar in meters. radius is rounded up to the nearest equivalent cell value.

Data Types: double
gridradius - Number of cells by which to inflate the occupied locations
positive integer scalar
Number of cells by which to inflate the occupied locations, specified as a positive integer scalar.
Data Types: double

## More About

## Grayscale Inflation

In grayscale inflation, the strel function creates a circular structuring element using the inflation radius. The grayscale inflation of $A(x, y)$ by $B(x, y)$ is defined as:
$(A \oplus B)(x, y)=\max \left\{A\left(x-x^{\prime}, y^{\prime}-y^{\prime}\right)+B\left(x^{\prime}, y^{\prime}\right) \mid\left(x^{\prime}, y^{\prime}\right) \in D_{B}\right\}$.
$D_{B}$ is the domain of the probability values in the structuring element $B . A(x, y)$ is assumed to be $+\infty$ outside the domain of the grid.

Grayscale inflation acts as a local maximum operator and finds the highest probability values for nearby cells. The inflate method uses this definition to inflate the higher probability values throughout the grid. This inflation increases the size of any occupied locations and creates a buffer zone for vehicles to use as they navigate.

## See Also

binary0ccupancyMap | occupancyMap | get0ccupancy

## Topics

"Occupancy Grids"

## Introduced in R2019b

## insertRay

Insert ray from laser scan observation

## Syntax

```
insertRay(map,pose,scan,maxrange)
insertRay(map, pose, ranges, angles,maxrange)
insertRay(map,startpt,endpoints)
insertRay(
```

$\qquad$

``` ,invModel)
```


## Description

insertRay (map, pose, scan, maxrange) inserts one or more lidar scan sensor observations in the occupancy grid, map, using the input lidarScan object, scan, to get ray endpoints. The ray endpoints are considered free space if the input scan ranges are below maxrange. Cells observed as occupied are updated with an observation of 0.7 . All other points along the ray are treated as obstacle free and updated with an observation of 0.4. Endpoints above maxrange are not updated. NaN values are ignored. This behavior correlates to the inverse sensor model.
insertRay(map, pose, ranges, angles, maxrange) specifies the range readings as vectors defined by the input ranges and angles.
insertRay (map, startpt, endpoints) inserts observations between the line segments from the start point to the end points. The endpoints are updated with a probability observation of 0.7 . Cells along the line segments are updated with an observation of 0.4.
insertRay (__ , invModel) inserts rays with updated probabilities given in the two-element vector, invModel, that corresponds to obstacle-free and occupied observations. Use any of the previous syntaxes to input the rays.

## Examples

## Insert Laser Scans into Occupancy Map

Create an empty occupancy grid map.

```
map = occupancyMap(10,10,20);
```

Input pose of the vehicle, ranges, angles, and the maximum range of the laser scan.

```
pose = [5,5,0];
ranges = 3*ones(100,1);
angles = linspace(-pi/2,pi/2,100);
maxrange = 20;
```

Create a lidarScan object with the specified ranges and angles.

```
scan = lidarScan(ranges,angles);
```

Insert the laser scan data into the occupancy map.
insertRay(map, pose,scan,maxrange);
Show the map to see the results of inserting the laser scan.
show(map)


Check the occupancy of the spot directly in front of the vehicle.
get0ccupancy(map,[8 5])
ans $=0.7000$
Add a second reading and view the update to the occupancy values. The additional reading increases the confidence in the readings. The free and occupied values become more distinct.
insertRay(map, pose, scan, maxrange) ; show(map)


```
getOccupancy(map,[8 5])
ans = 0.8448
```


## Input Arguments

## map - Map representation

occupancyMap object
Map representation, specified as a occupancyMap object. This object represents the environment of the vehicle. The object contains a matrix grid with values representing the probability of the occupancy of that cell. Values close to 1 represent a high probability that the cell contains an obstacle. Values close to 0 represent a high probability that the cell is not occupied and obstacle free.

## pose - Position and orientation of vehicle

three-element vector
Position and orientation of vehicle, specified as an [x y theta] vector. The vehicle pose is an $x$ and $y$ position with angular orientation theta (in radians) measured from the $x$-axis.

## scan - Lidar scan readings

lidarScan object
Lidar scan readings, specified as a lidarScan object.

## ranges - Range values from scan data

## vector

Range values from scan data, specified as a vector of elements measured in meters. These range values are distances from a sensor at given angles. The vector must be the same length as the corresponding angles vector.

## angles - Angle values from scan data

vector
Angle values from scan data, specified as a vector of elements measured in radians. These angle values correspond to the given ranges. The vector must be the same length as the corresponding ranges vector.
maxrange - Maximum range of sensor
scalar
Maximum range of laser range sensor, specified as a scalar in meters. Range values greater than or equal to maxrange are considered free along the whole length of the ray, up to maxrange.

## startpt - Start point for rays

two-element vector
Start point for rays, specified as a two-element vector, $\left[\begin{array}{ll}x & y\end{array}\right]$, in the world coordinate frame. All rays are line segments that originate at this point.

## endpoints - Endpoints for rays

$n$-by-2 matrix
Endpoints for rays, specified as an $n$-by-2 matrix of $\left[\begin{array}{ll}x & y\end{array}\right]$ pairs in the world coordinate frame, where $n$ is the length of ranges or angles. All rays are line segments that originate at startpt.

## invModel - Inverse sensor model values <br> two-element vector

Inverse sensor model values, specified as a two-element vector corresponding to obstacle-free and occupied probabilities. Points along the ray are updated according to the inverse sensor model and the specified range readings. NaN range values are ignored. Range values greater than maxrange are not updated. See "Inverse Sensor Model" on page 2-835.

## More About

## Inverse Sensor Model

The inverse sensor model determines how values are set along a ray from a range sensor reading to the obstacles in the map. You can customize this model by specifying different probabilities for free and occupied locations in the invModel argument. NaN range values are ignored. Range values greater than maxrange are not updated.


Grid locations that contain range readings are updated with the occupied probability. Locations before the reading are updated with the free probability. All locations after the reading are not updated.

## See Also

occupancyMap | raycast | binary0ccupancyMap | lidarScan

## Topics

"Occupancy Grids"
Introduced in R2019b

## local2grid

Convert local coordinates to grid indices

## Syntax

ij $=$ local2grid(map, xy)

## Description

ij = local2grid(map, xy) converts an array of local coordinates, $x y$, to an array of grid indices, ij in [row col] format.

## Input Arguments

## map - Map representation

occupancyMap object | mapLayer object | multiLayerMap object
Map representation, specified as a occupancyMap, mapLayer, or multiLayerMap object.

## xy - Local coordinates

$n$-by-2 matrix
Local coordinates, specified as an $n$-by- 2 matrix of $[x y]$ pairs, where $n$ is the number of local coordinates.

## Output Arguments

## ij - Grid positions <br> $n$-by-2 matrix

Grid positions, returned as an $n$-by-2 matrix of [i j] pairs in [row col] format, where $n$ is the number of grid positions. The grid cell locations start at $(1,1)$ and are counted from the top left corner of the grid.

## See Also

grid2world | occupancyMap | binary0ccupancyMap

## Topics

"Occupancy Grids"
Introduced in R2019b

## local2world

Convert local coordinates to world coordinates

## Syntax

xyWorld = local2world(map,xy)

## Description

xyWorld = local2world(map,xy) converts an array of local coordinates to world coordinates

## Input Arguments

## map - Map representation

occupancyMap object | mapLayer object | multiLayerMap object
Map representation, specified as a occupancyMap, mapLayer, or multiLayerMap object.
xy - Local coordinates
$n$-by-2 matrix
Local coordinates, specified as an $n$-by-2 matrix of $[x y]$ pairs, where $n$ is the number of world coordinates.

Data Types: double

## Output Arguments

## xyWorld - World coordinates <br> n-by-2 matrix

World coordinates, specified as an $n$-by-2 matrix of $[x y]$ pairs, where $n$ is the number of world coordinates.

Data Types: double

## See Also

grid2world|world2local| occupancyMap

## Topics

"Occupancy Grids"

Introduced in R2019b

## move

Move map in world frame

## Syntax

move(map, moveValue)
move(map, moveValue, Name, Value)

## Description

move(map, moveValue) moves the local origin of the map to an absolute location, moveValue, in the world frame, and updates the map limits. Move values are truncated based on the resolution of the map. By default, newly revealed regions are set to map. DefaultValue.
move (map, moveValue, Name, Value) specifies additional options specified by one or more namevalue pair arguments.

## Examples

## Move Local Map and Sync with World Map

This example shows how to move a local egocentric map and sync it with a larger world map. This process emulates a vehicle driving in an environment and getting updates on obstacles in the new areas.

Load example maps. Create an occupancy map from the ternaryMap.

```
load exampleMaps.mat
map = occupancyMap(ternaryMap);
show(map)
```



Create a smaller local map.
mapLocal = occupancyMap(ternaryMap(end-200:end,1:200)); show(mapLocal)

## Occupancy Grid



Follow a path planned in the world map and update the local map as you move your local frame. Specify path locations and plot on the map.

```
path = [100 100
    100 250
    200 250
    300 250];
show(map)
hold on
plot(path(:,1),path(:,2))
hold off
```



Create a loop for moving between points by the map resolution. Divide the difference between points by the map resolution to see how many incremental moves you can make.

```
for i = 1:length(path)-1
    moveAmount = (path(i+1,:)-path(i,:))/map.Resolution;
    for j = 1:abs(moveAmount(1)+moveAmount(2))
        moveValue = sign(moveAmount).*map.Resolution;
        move(mapLocal,moveValue, ...
            "MoveType","relative", "SyncWith",map)
        show(mapLocal)
        drawnow limitrate
    end
end
```

Occupancy Grid


## Input Arguments

## map - Map representation

occupancyMap object | mapLayer object | multiLayerMap object
Map representation, specified as a occupancyMap, mapLayer, or multiLayerMap object.
moveValue - Local map origin move value
[ $x$ y] vector
Local map origin move value, specified as an [ $x$ y] vector. By default, the value is an absolute location to move the local origin to in the world frame. Use the MoveType name-value pair to specify a relative move.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . , NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: 'MoveType','relative'

## MoveType - Type of move

```
'absolute' (default)|'relative'
```

Type of move, specified as 'absolute' or 'relative'. For relative moves, specify a relative [x y] vector for moveValue based on your current local frame.

## FillValue - Fill value for revealed locations

0 (default) | 1
Fill value for revealed locations because of the shifted map limits, specified as 0 or 1.

## SyncWith - Secondary map to sync with

occupancyMap object
Secondary map to sync with, specified as a occupancyMap object. Any revealed locations based on the move are updated with values in this map using the world coordinates.

## See Also

Objects
multiLayerMap | mapLayer |occupancyMap| binaryOccupancyMap
Functions
occupancyMatrix

Introduced in R2019b

## occupancyMatrix

Convert occupancy grid to double matrix

## Syntax

mat = occupancyMatrix(map)
mat $=$ occupancyMatrix(map,'ternary')

## Description

mat = occupancyMatrix(map) returns probability values stored in the occupancy grid object as a matrix.
mat = occupancyMatrix(map,'ternary') returns the occupancy status of each grid cell as a matrix. The OccupiedThreshold and FreeThreshold properties on the occupancy grid determine the obstacle free cells ( 0 ) and occupied cells (1). Unknown values are returned as -1 .

## Input Arguments

## map - Map representation

occupancyMap object
Map representation, specified as a occupancyMap object. This object represents the environment of the vehicle. The object contains a matrix grid with values representing the probability of the occupancy of that cell. Values close to 1 represent a high probability that the cell contains an obstacle. Values close to 0 represent a high probability that the cell is not occupied and obstacle free.

## Output Arguments

## mat - Occupancy grid values

matrix
Occupancy grid values, returned as an $h$-by- $w$ matrix, where $h$ and $w$ are defined by the two elements of the GridSize property of the occupancy grid object.
Data Types: double

## See Also

occupancyMap | get0ccupancy | show | binary0ccupancyMap
Topics
"Occupancy Grids"

Introduced in R2019b

## raycast

Compute cell indices along a ray

## Syntax

```
[endpoints,midpoints] = raycast(map,pose,range,angle)
[endpoints,midpoints] = raycast(map,p1,p2)
```


## Description

[endpoints,midpoints] = raycast(map, pose, range,angle) returns cell indices of the specified map for all cells traversed by a ray originating from the specified pose at the specified angle and range values. endpoints contains all indices touched by the end of the ray, with all other points included in midpoints.
[endpoints,midpoints] = raycast(map, p1, p2) returns the cell indices of the line segment between the two specified points.

## Examples

## Get Grid Cells Along A Ray

Use the raycast method to generate cell indices for all cells traversed by a ray.
Create an empty map. A low-resolution map is used to illustrate the effected grid locations.

```
map = occupancyMap(10,10,1);
```

show(map)


Get the grid indices of the midpoints and end points of a ray from [2 3] to [8.5 8]. Set occupancy values for these grid indices. Midpoints are treated as open space. Update endpoints with an occupied observation.

```
p1 = [2 3];
p2 = [8.5 8];
[endPts,midPts] = raycast(map,p1,p2);
set0ccupancy(map,midPts,zeros(length(midPts),1),'grid');
setOccupancy(map,endPts,ones(length(endPts),1),'grid');
```

Plot the original ray over the map. Each grid cell touched by the line is updated. The starting point overlaps multiple cells, and the line touches the edge of certain cells, but all the cells are still updated.

```
show(map)
hold on
plot([p1(1) p2(1)],[p1(2) p2(2)],'-b','LineWidth',2)
plot(p2(1),p2(2),'or')
grid on
```



## Input Arguments

## map - Map representation

occupancyMap object
Map representation, specified as a occupancyMap object. This object represents the environment of the sensor. The object contains a matrix grid with values representing the probability of the occupancy of that cell. Values close to 1 represent a high probability that the cell contains an obstacle. Values close to 0 represent a high probability that the cell is not occupied and obstacle free.

## pose - Position and orientation of sensor

three-element vector
Position and orientation of sensor, specified as an [ $x$ y theta] vector. The sensor pose is an $x$ and $y$ position with angular orientation theta (in radians) measured from the $x$-axis.

## range - Range of ray

scalar
Range of ray, specified as a scalar in meters.

## angle - Angle of ray

scalar
Angle of ray, specified as a scalar in radians. The angle value is for the corresponding range.

## p1 - Starting point of ray

two-element vector
Starting point of ray, specified as an [ $\left.\begin{array}{ll}x & y\end{array}\right]$ two-element vector. The point is defined in the world frame.

## p2 - Endpoint of ray

two-element vector
Endpoint of ray, specified as an $\left[\begin{array}{ll}x & y\end{array}\right]$ two-element vector. The point is defined in the world frame.

## Output Arguments

## endpoints - Endpoint grid indices

$n$-by-2 matrix
Endpoint indices, returned as an $n$-by-2 matrix of [ $i j$ ] pairs, where $n$ is the number of grid indices. The endpoints are where the range value hits at the specified angle. Multiple indices are returned when the endpoint lies on the boundary of multiple cells.

## midpoints - Midpoint grid indices

n-by-2 matrix
Midpoint indices, returned as an $n$-by- 2 matrix of [ $i \quad j$ ] pairs, where $n$ is the number of grid indices. This argument includes all grid indices the ray intersects, excluding the endpoint.

See Also<br>occupancyMap<br>\section*{Topics}<br>"Occupancy Grids"<br>\section*{Introduced in R2019b}

## rayIntersection

Find intersection points of rays and occupied map cells

## Syntax

```
intersectionPts = rayIntersection(map,pose,angles,maxrange)
intersectionPts = rayIntersection(map,pose,angles,maxrange,threshold)
```


## Description

intersectionPts = rayIntersection(map, pose, angles, maxrange) returns intersection points of rays and occupied cells in the specified map. Rays emanate from the specified pose and angles. Intersection points are returned in the world coordinate frame. If there is no intersection up to the specified maxrange, [ $\mathrm{NaN} \mathrm{NaN]}$ is returned. By default, the 0ccupiedThreshold property is used to determine occupied cells.
intersectionPts = rayIntersection(map,pose,angles,maxrange,threshold) returns intersection points based on the specified threshold for the occupancy values. Values greater than or equal to the threshold are considered occupied.

## Examples

## Get Ray Intersection Points on Occupancy Map

Create an occupancy grid map. Add obstacles and inflate them. A lower resolution map is used to illustrate the importance of using grid cells. Show the map.

```
map = occupancyMap(10,10,2);
obstacles = [4 10; 3 5; 7 7];
set0ccupancy(map,obstacles,ones(length(obstacles),1))
inflate(map,0.25)
show(map)
```



Find the intersection points of occupied cells and rays that emit from the given vehicle pose. Specify the max range and angles for these rays. The last ray does not intersect with an obstacle within the max range, so it has no collision point.

```
maxrange = 6;
angles = [pi/4,-pi/4,0,-pi/8];
vehiclePose = [4,4,pi/2];
intsectionPts = rayIntersection(map,vehiclePose,angles,maxrange,0.7)
intsectionPts = 4×2
    3.5000 4.5000
    6.0000 6.0000
    4.0000 9.0000
        NaN NaN
```

Plot the intersection points and rays from the pose.

```
hold on
plot(intsectionPts(:,1),intsectionPts(:,2),'*r') % Intersection points
plot(vehiclePose(1),vehiclePose(2),'ob') % Vehicle pose
for i = 1:3
    plot([vehiclePose(1),intsectionPts(i,1)],...
        [vehiclePose(2),intsectionPts(i,2)],'-b') % Plot intersecting rays
end
plot([vehiclePose(1),vehiclePose(1)-6*sin(angles(4))],...
    [vehiclePose(2),vehiclePose(2)+6*\operatorname{cos(angles(4))],'-b') % No intersection ray}
```

```
legend('Collision Points','Vehicle Position','Rays','Location','SouthEast')
```



## Input Arguments

## map - Map representation

occupancyMap object
Map representation, specified as a occupancyMap object. This object represents the environment of the sensor. The object contains a matrix grid with values representing the probability of the occupancy of that cell. Values close to 1 represent a high probability that the cell contains an obstacle. Values close to 0 represent a high probability that the cell is not occupied and obstacle free.

## pose - Position and orientation of sensor

three-element vector
Position and orientation of sensor, specified as an [x $\begin{aligned} & x \\ & \text { theta] vector. The sensor pose is an } x \text { and } y\end{aligned}$ position with angular orientation theta (in radians) measured from the $x$-axis.

## angles - Ray angles emanating from sensor

vector
Ray angles emanating from the sensor, specified as a vector with elements in radians. These angles are relative to the specified sensor pose.

## maxrange - Maximum range of sensor <br> scalar

Maximum range of laser range sensor, specified as a scalar in meters. Range values greater than or equal to maxrange are considered free along the whole length of the ray, up to maxrange.

## threshold - Threshold for occupied cells

scalar from 0 to 1
Threshold for occupied cells, specified as a scalar from 0 to 1. Occupancy values greater than or equal to the threshold are treated as occupied cells to trigger intersections.

## Output Arguments

## intersectionPts - Intersection points

n-by-2 matrix
Intersection points, returned as $n$-by-2 matrix of $\left[\begin{array}{ll}x & y\end{array}\right]$ pairs in the world frame, where $n$ is the length of angles.

## See Also

occupancyMap | raycast|update0ccupancy | binary0ccupancyMap

## Topics

"Occupancy Grids"
Introduced in R2019b

## setOccupancy

Set occupancy value of locations

## Syntax

```
set0ccupancy(map,xy,occval)
setOccupancy(map,xy,occval,'local')
setOccupancy(map,ij,occval,'grid')
validPts = setOccupancy(
```

$\qquad$

```
setOccupancy(map,bottomLeft,inputMatrix)
setOccupancy(map,bottomLeft,inputMatrix,'local')
setOccupancy(map,topLeft,inputMatrix,'grid')
```


## Description

setOccupancy (map, $x y$, occval) assigns the occupancy values to each coordinate specified in $x y$. occval can be a column vector the same size of $x y$ or a scalar, which is applied to all coordinates.
setOccupancy (map, xy, occval, ' local') assigns occupancy values, occval, to the input array of local coordinates, $x y$, as local coordinates.
setOccupancy(map,ij, occval,'grid') assigns occupancy values, occval, to the input array of grid indices, ij , as [rows cols].
validPts = set0ccupancy (__ ) outputs an n-element vector of logical values indicating whether input coordinates are within the map limits.
setOccupancy (map, bottomLeft, inputMatrix) assigns a matrix of occupancy values by specifying the bottom-left corner location in world coordinates.
setOccupancy(map, bottomLeft,inputMatrix, 'local') assigns a matrix of occupancy values by specifying the bottom-left corner location in local coordinates.
setOccupancy(map,topLeft,inputMatrix,'grid') assigns a matrix of occupancy values by specifying the top-left cell index in grid indices and the matrix size.

## Examples

## Create and Modify Occupancy Map

Create an empty map of 10-by-10 meters in size.

```
map = occupancyMap(10,10,10);
```

Update the occupancy of specific world locations with new probability values and display the map.

```
x = [1.2; 2.3; 3.4; 4.5; 5.6];
y = [5.0; 4.0; 3.0; 2.0; 1.0];
```

```
pvalues = [0.2; 0.4; 0.6; 0.8; 1];
updateOccupancy(map,[x y],pvalues)
figure
show(map)
```



Inflate the occupied areas by a radius of 0.5 m . The larger occupancy values overwrite the smaller values.
inflate(map, 0.5)
figure
show(map)


Get the grid locations from the world locations.
ij = world2grid(map,[x y]);
Set occupancy values for the grid locations.
set0ccupancy(map,ij,ones ( 5,1 ),'grid')
figure
show(map)


## Input Arguments

## map - Map representation

occupancyMap object
Map representation, specified as a occupancyMap object. This object represents the environment of the vehicle. The object contains a matrix grid with values representing the probability of the occupancy of that cell. Values close to 1 represent a high probability that the cell contains an obstacle. Values close to 0 represent a high probability that the cell is not occupied and obstacle free.

## xy - World coordinates

n-by-2 matrix
World coordinates, specified as an $n$-by-2 matrix of [ $x y$ ] pairs, where $n$ is the number of world coordinates.

Data Types: double

## ij - Grid positions

$n$-by-2 matrix
Grid positions, specified as an $n$-by-2 matrix of [ $i j$ ] pairs in [rows cols] format, where $n$ is the number of grid positions.
Data Types: double

## occval - Probability occupancy values

scalar | column vector
Probability occupancy values, specified as a scalar or a column vector the same size as either xy or ij . A scalar input is applied to all coordinates in either xy or ij .

Values close to 0 represent a high probability that the cell is not occupied and obstacle free.

## inputMatrix - Occupancy values

matrix
Occupancy values, specified as a matrix. Values are given between 0 and 1 inclusively.

## bottomLeft - Location of output matrix in world or local

two-element vector | [xCoord yCoord]
Location of bottom left corner of output matrix in world or local coordinates, specified as a twoelement vector, [xCoord yCoord]. Location is in world or local coordinates based on syntax.

## Data Types: double

## topLeft - Location of grid

two-element vector | [iCoord jCoord]
Location of top left corner of grid, specified as a two-element vector, [iCoord jCoord].
Data Types: double

## Output Arguments

## validPts - Valid map locations

$n$-by- 1 column vector
Valid map locations, returned as an $n$-by- 1 column vector equal in length to xy or ij. Locations inside the map return a value of 1 . Locations outside the map limits return a value of 0 .

## Limitations

Occupancy values have a limited resolution of $\pm 0.001$. The values are stored as int 16 using a logodds representation. This data type limits resolution, but saves memory when storing large maps in MATLAB. When calling set0ccupancy and then get0ccupancy, the value returned might not equal the value you set. For more information, see the log-odds representations section in "Occupancy Grids".

See Also<br>occupancyMap | get0ccupancy | binary0ccupancyMap<br>Topics<br>"Occupancy Grids"

Introduced in R2019b

## show

Show grid values in a figure

## Syntax

```
show(map)
show(map,'local')
show(map,'grid')
show(_,Name,Value)
mapImage = show(___)
```


## Description

show (map) displays the occupancy grid map in the current axes, with the axes labels representing the world coordinates.
show(map, 'local') displays the occupancy grid map in the current axes, with the axes labels representing the local coordinates instead of world coordinates.
show(map, 'grid') displays the occupancy grid map in the current axes, with the axes labels representing the grid coordinates.
show (__ ,Name, Value) specifies additional options specified by one or more name-value pair arguments.
mapImage $=\operatorname{show}(\ldots \quad$ ) returns the handle to the image object created by show.

## Examples

## Create and Modify Occupancy Map

Create an empty map of 10-by-10 meters in size.

```
map = occupancyMap(10,10,10);
```

Update the occupancy of specific world locations with new probability values and display the map.

```
x = [1.2; 2.3; 3.4; 4.5; 5.6];
y = [5.0; 4.0; 3.0; 2.0; 1.0];
pvalues = [0.2; 0.4; 0.6; 0.8; 1];
updateOccupancy(map,[x y],pvalues)
figure
show(map)
```



Inflate the occupied areas by a radius of 0.5 m . The larger occupancy values overwrite the smaller values.
inflate(map, 0.5)
figure
show(map)


Get the grid locations from the world locations.
ij = world2grid(map,[x y]);
Set occupancy values for the grid locations.
set0ccupancy(map,ij,ones ( 5,1 ),'grid')
figure
show(map)


## Convert PGM Image to Map

Convert a portable graymap (PGM) file containing a ROS map into an occupancyMap for use in MATLAB.

Import the image using imread. Crop the image to the playpen area.

```
image = imread('playpen_map.pgm');
imageCropped = image(750:1250,750:1250);
imshow(imageCropped)
```



PGM values are expressed from 0 to 255 as uint8. Normalize these values by converting the cropped image to double and dividing each cell by 255 . This image shows obstacles as values close to 0 . Subtract the normalized image from 1 to get occupancy values with 1 representing occupied space.

```
imageNorm = double(imageCropped)/255;
```

imageOccupancy = 1 - imageNorm;

Create the occupancyMap object using an adjusted map image. The imported map resolution is 20 cells per meter.

```
map = occupancyMap(image0ccupancy,20);
show(map)
```



## Input Arguments

## map - Map representation

occupancyMap object
Map representation, specified as a occupancyMap object. This object represents the environment of the vehicle. The object contains a matrix grid with values representing the probability of the occupancy of that cell. Values close to 1 represent a high probability that the cell contains an obstacle. Values close to 0 represent a high probability that the cell is not occupied and obstacle free.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . , NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: 'Parent', axHandle

## Parent - Axes to plot the map

Axes object | UIAxes object
Axes to plot the map specified as either an Axes or UIAxes object. See axes or uiaxes.

## FastUpdate - Update existing map plot

0 (default) | 1
Update existing map plot, specified as 0 or 1 . If you previously plotted your map on your figure, set to 1 for a faster update to the figure. This is useful for updating the figure in a loop for fast animations.

## Outputs

## mapImage - Map image

object handle
Map image, specified as an object handle.

## See Also

axes | occupancyMap | occupancyMatrix | binaryOccupancyMap

## Introduced in R2019b

## syncWith

Sync map with overlapping map

## Syntax

```
mat = syncWith(map,sourcemap)
```


## Description

mat = syncWith(map, sourcemap) updates map with data from another occupancyMap object, sourcemap. Locations in map that are also found in sourcemap are updated. All other cells in map retain their current values.

## Examples

## Move Local Map and Sync with World Map

This example shows how to move a local egocentric map and sync it with a larger world map. This process emulates a vehicle driving in an environment and getting updates on obstacles in the new areas.

Load example maps. Create an occupancy map from the ternaryMap.
load exampleMaps.mat
map = occupancyMap(ternaryMap);
show (map)


Create a smaller local map.
mapLocal = occupancyMap(ternaryMap(end-200:end,1:200)); show(mapLocal)

Occupancy Grid


Follow a path planned in the world map and update the local map as you move your local frame.
Specify path locations and plot on the map.

```
path = [100 100
    100 250
    200 250
    300 250];
show(map)
hold on
plot(path(:,1),path(:,2))
hold off
```



Create a loop for moving between points by the map resolution. Divide the difference between points by the map resolution to see how many incremental moves you can make.

```
for i = 1:length(path)-1
    moveAmount = (path(i+1,:)-path(i,:))/map.Resolution;
    for j = 1:abs(moveAmount(1)+moveAmount(2))
        moveValue = sign(moveAmount).*map.Resolution;
        move(mapLocal,moveValue, ...
            "MoveType","relative", "SyncWith",map)
        show(mapLocal)
        drawnow limitrate
    end
end
```

Occupancy Grid


## Input Arguments

## map - Map representation

occupancyMap object | mapLayer object | multiLayerMap object
Map representation, specified as a occupancyMap, mapLayer, or multiLayerMap object.
sourcemap - Source map data
occupancyMap object | mapLayer object | multiLayerMap object
Source map data, specified as a occupancyMap, mapLayer, or multiLayerMap object.

## See Also

occupancyMap | binary0ccupancyMap

## Topics

"Occupancy Grids"
Introduced in R2019b

## updateOccupancy

Integrate probability observations at locations

## Syntax

```
update0ccupancy(map,occMatrix)
updateOccupancy(map,locations,obs)
updateOccupancy(map,xy,obs,'world')
updateOccupancy(map,xy,obs,'local')
updateOccupancy(map,ij,obs,'grid')
updateOccupancy(map, bottomLeft,obsMatrix)
update0ccupancy(map,bottomLeft,obsMatrix,'world')
updateOccupancy(map,bottomLeft,obsMatrix,'local')
updateOccupancy(map,topLeft,obsMatrix,'grid')
```


## Description

update0ccupancy (map,occMatrix) probabilistically integrates a matrix of occupancy values, occMatrix, with the current occupancy matrix of the occupancyMap object map. The size of the matrix must be equal to the GridSize property of map.
updateOccupancy (map, locations,obs) probabilistically integrates observation values, obs, into the occupancy map cells corresponding to the $n$-by- 2 matrix of world coordinates locations. Observation values are determined based on the "Inverse Sensor Model" on page 2-876.
updateOccupancy (map, xy, obs,'world') probabilistically integrates observation values, obs, into the cells corresponding to the $n$-by- 2 matrix of world coordinates xy .
updateOccupancy (map, xy, obs,' local') probabilistically integrates observation values, obs, into the cells corresponding to the $n$-by- 2 matrix of local coordinates xy .
updateOccupancy (map,ij, obs,'grid') probabilistically integrates observation values, obs, into the cells corresponding to the $n$-by- 2 matrix of grid indices ij .
updateOccupancy (map, bottomLeft, obsMatrix) probabilistically integrates an $m$-by- $n$ matrix of observation values, obsMatrix, into a subregion in the map. Specify the bottom-left corner of the subregion as a world position, bottomLeft. The subregion extends $m$ rows up and $n$ columns to the right from the specified position.
updateOccupancy (map, bottomLeft, obsMatrix, 'world') probabilistically integrates an $m$-by$n$ matrix of observation values, obsMatrix, into a subregion in the map. Specify the bottom-left corner of the subregion as a world position, bottomLeft. The subregion extends $m$ rows up and $n$ columns to the right from the specified position.
updateOccupancy (map, bottomLeft, obsMatrix, ' local') probabilistically integrates an m-by$n$ matrix of observation values, obsMatrix, into a subregion in the map. Specify the bottom-left corner of the subregion as a local position, bottomLeft. The subregion extends $m$ rows up and $n$ columns to the right from the specified position.
updateOccupancy(map,topLeft,obsMatrix,'grid') probabilistically integrates an $m$-by-n matrix of observation values, obsMatrix, into a subregion in the map. Specify the top-left corner of the subregion as a grid index, topLeft. The subregion extends $m$ rows down and $n$ columns to the right from the specified index.

## Examples

## Create and Modify Occupancy Map

Create an empty map of 10 -by-10 meters in size.
map $=$ occupancyMap(10,10,10);
Update the occupancy of specific world locations with new probability values and display the map.

```
x = [1.2; 2.3; 3.4; 4.5; 5.6];
y = [5.0; 4.0; 3.0; 2.0; 1.0];
pvalues = [0.2; 0.4; 0.6; 0.8; 1];
updateOccupancy(map,[x y],pvalues)
figure
show(map)
```



Inflate the occupied areas by a radius of 0.5 m . The larger occupancy values overwrite the smaller values.

```
inflate(map,0.5)
```

figure
show (map)


Get the grid locations from the world locations.
ij = world2grid(map,[x y]);
Set occupancy values for the grid locations.
set0ccupancy(map,ij,ones $(5,1)$,'grid')
figure
show(map)


## Input Arguments

## map - Map representation

occupancyMap object
Map representation, specified as an occupancyMap object. This object represents the environment of the vehicle. The object contains a matrix grid with each value representing the probability of the occupancy of that cell. Values close to 1 represent a high probability that the cell contains an obstacle. Values close to 0 represent a high probability that the cell is not occupied and contains no obstacles.

## occMatrix - Matrix of occupancy values

numeric matrix | logical matrix
Matrix of occupancy values, specified as a matrix. The size of the matrix must be equal to the GridSize property of map.

The occupancy values can be of any numeric type, with values between 0 and 1 . If the matrix is logical, the default occupancy values of 0.7 (true) and 0.4 (false) are used.

Example: updateOccupancy (map,ones(map.GridSize)*0.6)
Data Types: single | double | logical

## locations - Cell locations in world coordinates <br> $n$-by-2 matrix

Cell locations in world coordinates, specified as an $n$-by-2 matrix with rows of the form [ $x y$ ], where $n$ is the number of world coordinates. The function ignores locations outside of the map boundaries.
Example: updateOccupancy (map,[1 1; 3 3; 5 5],false)
Data Types: single | double
bottomLeft - Location of bottom-left corner of observation matrix
two-element vector
Location of the bottom-left corner of the observation matrix, specified as a two-element vector of the form [xCoord yCoord]. The location is in world or local coordinates, based on the syntax.
Example: update0ccupancy (map,[2 2],[0.2 0.4; 0.6 0.8],'world')
Data Types: single | double

## topLeft - Location of top-left corner of grid

two-element vector
Location of the top-left corner of the grid, specified as a two-element vector of form [iCoord jCoord].
Example: update0ccupancy (map,[2 2],[0.2 0.4; 0.6 0.8],'grid')
Data Types: single|double
xy - World or local coordinates
n-by-2 matrix
World or local coordinates, specified as an $n$-by-2 matrix with rows of the form $\left[\begin{array}{ll}x & y\end{array}\right]$, where $n$ is the number of coordinates.

Example: updateOccupancy (map,[2 2; 4 4; 6 6],[0.2; 0.4; 0.6],'world')
Data Types: single | double
ij - Grid positions
n-by-2 matrix
Grid positions, specified as an n-by-2 matrix with rows of the form [ij] in [rows cols] format, where $n$ is the number of grid positions.

Example: updateOccupancy (map,[2 2; $44 ; 6$ 6],[0.2; 0.4; 0.6],'grid')
Data Types: single|double

## obs - Probability observation values

$n$-element numeric column vector $\mid$ n-element logical column vector | numeric scalar | logical scalar
Probability observation values, specified as a numeric or logical scalar or a numeric or logical $n$ element column vector the same size as either locations, $x y$, or $i j$.
obs values can be any value from 0 to 1 , but if obs is a logical vector, the default observation values of 0.7 (true) and 0.4 (false) are used. If obs is a numeric or a logical scalar, the value is applied to all coordinates in locations, $x y$, or $i j$. These values correlate to the "Inverse Sensor Model" on page 2-876 for ray casting.
Example: update0ccupancy(map,[2 2; 4 4; 6 6],[0.2; 0.4; 0.6],'local')

Data Types: single | double | logical
obsMatrix - Matrix of probability observation values
$m$-by-n numeric matrix | m-by-n logical matrix
Matrix of probability observation values, specified as an $m$-by- $n$ numeric or logical matrix.
The observation values can be of any numeric type with value between 0 and 1 . If the matrix is logical, the default observation values of 0.7 (true) and 0.4 (false) are used.

Example: updateOccupancy(map,[2 2],[0.2 0.4; 0.6 0.8])
Data Types: single | double | logical

## More About

## Inverse Sensor Model

The inverse sensor model determines how values are set along a ray from a range sensor reading to the obstacles in the map. NaN range values are ignored. Range values greater than max range are not updated.


Grid locations that contain range readings are updated with the occupied probability. Locations before the reading are updated with the free probability. All locations after the reading are not updated.

## See Also

occupancyMap | set0ccupancy | binary0ccupancyMap

## Topics

"Occupancy Grids"
Introduced in R2019b

## world2grid

Convert world coordinates to grid indices

## Syntax

ij $=$ world2grid (map,xy)

## Description

ij = world2grid(map, xy) converts an array of world coordinates, $x y$, to an array of grid indices, ij in [row col] format.

## Examples

## Create and Modify Occupancy Map

Create an empty map of 10-by-10 meters in size.

```
map = occupancyMap(10,10,10);
```

Update the occupancy of specific world locations with new probability values and display the map.

```
x = [1.2; 2.3; 3.4; 4.5; 5.6];
y = [5.0; 4.0; 3.0; 2.0; 1.0];
pvalues = [0.2; 0.4; 0.6; 0.8; 1];
update0ccupancy(map,[x y],pvalues)
figure
show(map)
```



Inflate the occupied areas by a radius of 0.5 m . The larger occupancy values overwrite the smaller values.
inflate(map, 0.5)
figure
show(map)


Get the grid locations from the world locations.
ij = world2grid(map,[x y]);
Set occupancy values for the grid locations.
set0ccupancy(map,ij,ones ( 5,1 ),'grid')
figure
show(map)


## Input Arguments

## map - Map representation

occupancyMap object | mapLayer object | multiLayerMap object
Map representation, specified as a occupancyMap, mapLayer, or multiLayerMap object.
xy - World coordinates
$n$-by-2 matrix
World coordinates, specified as an $n$-by-2 matrix of [ $x y$ ] pairs, where $n$ is the number of world coordinates.

Data Types: double

## Output Arguments

## ij - Grid indices

$n$-by-2 matrix
Grid indices, returned as an $n$-by-2 matrix of [ $i j$ ] pairs in [row col] format, where $n$ is the number of grid positions. The grid cell locations are counted from the top left corner of the grid.
Data Types: double

## See Also

## Objects

multiLayerMap|mapLayer |occupancyMap | binaryOccupancyMap

## Functions

grid2world

## Topics

"Occupancy Grids"
Introduced in R2019b

## rangeSensor

Simulate range-bearing sensor readings

## Description

The rangeSensor System object is a range-bearing sensor that is capable of outputting range and angle measurements based on the given sensor pose and occupancy map. The range-bearing readings are based on the obstacles in the occupancy map.

To simulate a range-bearing sensor using this object:
1 Create the rangeSensor object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

```
rbsensor = rangeSensor
rbsensor = rangeSensor(Name,Value)
```


## Description

rbsensor $=$ rangeSensor returns a rangeSensor System object, rbsensor. The sensor is capable of outputting range and angle measurements based on the sensor pose and an occupancy map.
rbsensor = rangeSensor(Name, Value) sets properties for the sensor using one or more namevalue pairs. Unspecified properties have default values. Enclose each property name in quotes.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## Range - Minimum and maximum detectable range

[0 20] (default) | 1-by-2 positive real-valued vector
The minimum and maximum detectable range, specified as a 1-by-2 positive real-valued vector. Units are in meters.

Example: [1 15]
Tunable: Yes
Data Types: single | double

## HorizontalAngle - Minimum and maximum horizontal detection angle

[-pi pi] (default)| 1-by-2 real-valued vector
Minimum and maximum horizontal detection angle, specified as a 1-by-2 real-valued vector. Units are in radians.

Example: [-pi/3 pi/3]
Data Types: single | double

## HorizontalAngleResolution - Resolution of horizontal angle readings

0.0244 (default) | positive scalar

Resolution of horizontal angle readings, specified as a positive scalar. The resolution defines the angular interval between two consecutive sensor readings. Units are in radians.
Example: 0.01
Data Types: single | double

## RangeNoise - Standard deviation of range noise

0 (default) | positive scalar
The standard deviation of range noise, specified as a positive scalar. The range noise is modeled as a zero-mean white noise process with the specified standard deviation. Units are in meters.

Example: 0.01
Tunable: Yes
Data Types: single | double

## HorizontalAngleNoise - Standard deviation of horizontal angle noise

0 (default) | positive scalar
The standard deviation of horizontal angle noise, specified as a positive scalar. The range noise is modeled as a zero-mean white noise process with the specified standard deviation. Units are in radians.

Example: 0.01
Tunable: Yes
Data Types: single | double

## NumReadings - Number of output readings <br> 258 (default) | positive integer

This property is read-only.
Number of output readings for each pose of the sensor, specified as a positive integer. This property depends on the HorizonalAngle and HorizontalAngleResolution properties.
Data Types: single|double

## Usage

## Syntax

[ranges,angles] = rbsensor(pose,map)

## Description

[ranges,angles] = rbsensor(pose, map) returns the range and angle readings from the 2-D pose information and the ground-truth map.

## Input Arguments

## pose - Pose of sensor in map

$N$-by-3 real-valued matrix
Poses of the sensor in the 2-D map, specified as an $N$-by- 3 real-valued matrix, where $N$ is the number of poses to simulate the sensor. Each row of the matrix corresponds to a pose of the sensor in the order of $[x, y, \theta] . x$ and $y$ represent the position of the sensor in the map frame. The units of $x$ and $y$ are in meters. $\theta$ is the heading angle of the sensor with respect to the positive $x$-direction of the map frame. The units of $\theta$ are in radians.

## map - Ground-truth map

occupancyMap object | binary0ccupancyMap object
Ground-truth map, specified as an occupancyMap or a binary0ccupancyMap object. For the occupancyMap input, the range-bearing sensor considers a cell as occupied and returns a range reading if the occupancy probability of the cell is greater than the value specified by the OccupiedThreshold property of the occupancy map.

## Output Arguments

## ranges - Range readings

$R$-by- $N$ real-valued matrix
Range readings, specified as an $R$-by- $N$ real-valued matrix. $N$ is the number of poses for which the sensor is simulated, and $R$ is the number of sensor readings per pose of the sensor. $R$ is same as the value of the NumReadings property.

## angles - Angle readings

$R$-by-1 real-valued vector
Angle readings, specified as an $R$-by- 1 real-valued vector. $R$ is the number of sensor readings per pose of the sensor. $R$ is same as the value of the NumReadings property.

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Common to All System Objects

step Run System object algorithm
clone Create duplicate System object

## Examples

## Obtain Range and Bearing Readings

Create a range-bearing sensor.

```
rbsensor = rangeSensor;
```

Specify the pose of the sensor and the ground-truth map.
truePose = [0 0 pi/4];
trueMap = binary0ccupancyMap(eye(10));
Generate the sensor readings.
[ranges, angles] = rbsensor(truePose, trueMap);
Visualize the results using lidarScan.
scan = lidarScan(ranges, angles);
figure
plot(scan)


## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:

- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

occupancyMap | binaryOccupancyMap | lidarScan

Introduced in R2019b

## world2local

Convert world coordinates to local coordinates

## Syntax

xyLocal $=$ world2local(map,xy)

## Description

xyLocal $=$ world2local (map, $x y$ ) converts an array of world coordinates to local coordinates.

## Input Arguments

map - Map representation
occupancyMap object | mapLayer object | multiLayerMap object
Map representation, specified as a occupancyMap, mapLayer, or multiLayerMap object.
xy - World coordinates
$n$-by-2 vertical array
World coordinates, specified as an $n$-by-2 vertical array of [ $\mathrm{x} y$ ] pairs, where $n$ is the number of world coordinates.

## Output Arguments

xyLocal - Local coordinates
$n$-by-2 vertical array
Local coordinates, specified as an $n$-by-2 vertical array of [ $\mathrm{x} y$ ] pairs, where $n$ is the number of local coordinates.

## See Also

## Objects

multiLayerMap | mapLayer |occupancyMap | binaryOccupancyMap
Functions
grid2world|local2world
Introduced in R2019b

## occupancyMap3D

Create 3-D occupancy map

## Description

The occupancyMap3D class stores a 3-D map and map information. The map is stored as probabilistic values in an octree data structure on page 2-893. The class handles arbitrary environments and expands its size dynamically based on observation inputs. You can add observations as point clouds or as specific xyz locations. These observations update the probability values. Probabilistic values represent the occupancy of locations. The octree data structure trims data appropriately to remain efficient both in memory and on disk.

## Creation

## Syntax

```
omap = occupancyMap3D
omap = occupancyMap3D(res)
omap = occupancyMap3D(res,Name,Value)
```


## Description

omap = occupancyMap3D creates an empty 3-D occupancy map with no observations and default property values.
omap = occupancyMap3D(res) specifies a map resolution in cells/meter and sets the Resolution property.
omap = occupancyMap3D(res,Name,Value) creates an object with additional options specified by one or more Name, Value pair arguments. For example, ' FreeThreshold' , 0. 25 sets the threshold to consider cells obstacle-free as a probability value of 0.25 . Enclose each property name in quotes.

## Properties

## Resolution - Grid resolution

1 (default) | positive scalar
Grid resolution in cells per meter, specified as a scalar. Specify resolution on construction. Inserting observations with precisions higher than this value are rounded down and applied at this resolution.

## FreeThreshold - Threshold to consider cells as obstacle-free

## 0.2 (default) | positive scalar

Threshold to consider cells as obstacle-free, specified as a positive scalar. Probability values below this threshold are considered obstacle-free.

## OccupiedThreshold - Threshold to consider cells as occupied <br> 0.65 (default) | positive scalar

Threshold to consider cells as occupied, specified as a positive scalar. Probability values above this threshold are considered occupied.

## ProbabilitySaturation - Saturation limits on probability values <br> [0.001 0.999] (default) |[min max] vector

Saturation limits on probability values, specified as a [min max] vector. Values above or below these saturation values are set to the min or max values. This property reduces oversaturating of cells when incorporating multiple observations.

## Object Functions

| checkOccupancy | Check if locations are free or occupied |
| :--- | :--- |
| getOccupancy | Get occupancy probability of locations |
| inflate | Inflate map |
| insertPointCloud | Insert 3-D points or point cloud observation into map |
| rayIntersection | Find intersection points of rays and occupied map cells |
| setOccupancy | Set occupancy probability of locations |
| show | Show occupancy map |
| updateOccupancy | Update occupancy probability at locations |

## Examples

## Create 3-D Occupancy Map and Inflate Points

The occupancyMap3D object stores obstacles in 3-D space, using sensor observations to map an environment. Create a map and add points from a point cloud to identify obstacles. Then inflate the obstacles in the map to ensure safe operating space around obstacles.

Create an occupancyMap3D object with a map resolution of 10 cells/meter.
map3D = occupancyMap3D(10);
Define a set of 3-D points as an observation from a pose [xyzqu qx qy qz]. This pose is for the sensor that observes these points and is centered on the origin. Define two sets of points to insert multiple observations.

```
pose = [ 0 0 0 1 0 0 0];
points = repmat((0:0.25:2)', 1, 3);
points2 = [(0:0.25:2)' (2:-0.25:0)' (0:0.25:2)'];
maxRange = 5;
```

Insert the first set of points using insertPointCloud. The function uses the sensor pose and the given points to insert observations into the map. The colors displayed correlate to the height of the point only for illustrative purposes.

```
insertPointCloud(map3D,pose,points,maxRange)
show(map3D)
```


## Occupancy Map



Insert the second set of points. The ray between the sensor pose (origin) and these points overlap points from the previous insertion. Therefore, the free space between the sensor and the new points are updated and marked as free space.
insertPointCloud(map3D, pose, points2,maxRange) show(map3D)

## Occupancy Map



Inflate the map to add a buffer zone for safe operation around obstacles. Define the vehicle radius and safety distance and use the sum of these values to define the inflation radius for the map.
vehicleRadius = 0.2;
safetyRadius = 0.3;
inflationRadius = vehicleRadius + safetyRadius;
inflate(map3D, inflationRadius);
show(map3D)


## Algorithms

## Octree Data Structure

The octree data structure is a hierarchical structure used for subdivision of an environment into cubic volumes called voxels. For a given map volume, the space is recursively subdivided into eight voxels until achieving a desired map resolution (voxel size) is achieved. This subdivision can be represented as a tree, which stores probability values for locations in the map.


The probability values in the tree have a log-odds representation. Using this representation, locations easily recover from dynamic observations and numerical errors due to small probabilities are reduced. To remain efficient in memory, lower branches of the tree are pruned in the structure if they share the same occupancy values using this log-odds representation.


The class internally handles the organization of this data structure, including the pruning of branches. Specify all observations as spatial coordinates when using functions such as set0ccupancy, get0ccupancy, or insertPointCloud. Insertions into the tree, and navigation through the tree, is determined based on the spatial coordinates and the resolution of the map.

## References

[1] Hornung, Armin, Kai M. Wurm, Maren Bennewitz, Cyrill Stachniss, and Wolfram Burgard.
"OctoMap: an efficient probabilistic 3D mapping framework based on octrees." Autonomous
Robots, Vol. 34, No. 3, 2013, pp. 189-206.. doi:10.1007/s10514-012-9321-0.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

## Classes

occupancyMap | binary0ccupancyMap
Functions

```
insertPointCloud|inflate| set0ccupancy| show| rosReadOccupancyMap3D
```

Introduced in R2019b

## checkOccupancy

Check if locations are free or occupied

## Syntax

iOccval = check0ccupancy (map3D,xyz)

## Description

iOccval = checkOccupancy(map3D,xyz) returns an array of occupancy values specified at the xyz locations using the 0ccupiedThreshold and FreeThreshold properties of the input
occupancyMap3D object. Each row is a separate xyz location in the map to check the occupancy of. Occupancy values can be obstacle-free (0), occupied (1), or unknown (-1).

## Examples

## Check Occupancy Status and Get Occupancy Values in 3-D Occupancy Map

Import a 3-D occupancy map.

```
map3D = import0ccupancyMap3D("citymap.ot")
map3D =
    occupancyMap3D with properties:
        ProbabilitySaturation: [1.0000e-03 0.9990]
            Resolution: 1
            OccupiedThreshold: 0.6500
                FreeThreshold: 0.2000
```

Display the map.
show(map3D)

## Occupancy Map



Check the occupancy statuses of different locations and get their occupancy values.

```
iOccVal1 = checkOccupancy(map3D,[50 15 0])
iOccVal1 = 0
OccVal1 = getOccupancy(map3D,[50 15 0])
OccVal1 = 0.0019
iOccVal2 = checkOccupancy(map3D,[50 15 15])
iOccVal2 = 1
OccVal2 = getOccupancy(map3D,[50 15 15])
OccVal2 = 0.6500
iOccVal3 = checkOccupancy(map3D,[50 15 45])
iOccVal3 = -1
OccVal3 = getOccupancy(map3D,[50 15 45])
OccVal3 = 0.5000
```


## Input Arguments

## map3D - 3-D occupancy map

occupancyMap3D object
3-D occupancy map, specified as an occupancyMap3D object.
xyz - World coordinates
n-by-3 matrix
World coordinates, specified as an $n$-by-3 matrix of $\left[\begin{array}{lll}x & y & z\end{array}\right]$ points, where $n$ is the number of world coordinates.

## Output Arguments

## iOccval - Interpreted occupancy values

column vector
Interpreted occupancy values, returned as a column vector with the same length as xyz.
Occupancy values can be obstacle-free (0), occupied (1), or unknown (-1). These values are determined from the actual probability values and the OccupiedThreshold and FreeThreshold properties of the map3D object.

## See Also

## Classes

occupancyMap3D | lidarSLAM | occupancyMap

## Functions

insertPointCloud |inflate | set0ccupancy | show

## Introduced in R2019b

## getOccupancy

Get occupancy probability of locations

## Syntax

occval = get0ccupancy(map3D,xyz)

## Description

occval = get0ccupancy (map3D, xyz) returns an array of probability occupancy values at the specified xyz locations in the occupancyMap3D object. Values close to 1 represent a high certainty that the cell contains an obstacle. Values close to 0 represent certainty that the cell is not occupied and obstacle-free.

## Examples

## Check Occupancy Status and Get Occupancy Values in 3-D Occupancy Map

Import a 3-D occupancy map.

```
map3D = importOccupancyMap3D("citymap.ot")
map3D =
    occupancyMap3D with properties:
        ProbabilitySaturation: [1.0000e-03 0.9990]
            Resolution: 1
        OccupiedThreshold: 0.6500
            FreeThreshold: 0.2000
```

Display the map.
show(map3D)

## Occupancy Map



Check the occupancy statuses of different locations and get their occupancy values.

```
iOccVal1 = checkOccupancy(map3D,[50 15 0])
iOccVal1 = 0
OccVal1 = getOccupancy(map3D,[50 15 0])
OccVal1 = 0.0019
iOccVal2 = checkOccupancy(map3D,[50 15 15])
iOccVal2 = 1
OccVal2 = getOccupancy(map3D,[50 15 15])
OccVal2 = 0.6500
iOccVal3 = checkOccupancy(map3D,[50 15 45])
iOccVal3 = -1
OccVal3 = getOccupancy(map3D,[50 15 45])
OccVal3 = 0.5000
```


## Input Arguments

```
map3D - 3-D occupancy map
```

occupancyMap3D object
3-D occupancy map, specified as an occupancyMap3D object.
xyz - World coordinates
$n$-by-3 matrix
World coordinates, specified as an $n$-by-3 matrix of $\left[\begin{array}{lll}x & y & z\end{array}\right]$ points, where $n$ is the number of world coordinates.

## Output Arguments

occval - Probability occupancy values
column vector
Probability occupancy values, returned as a column vector with the same length as xyz.
Values close to 0 represent certainty that the cell is not occupied and obstacle-free.

## See Also

Classes
occupancyMap3D | lidarSLAM | occupancyMap

## Functions

insertPointCloud |inflate | set0ccupancy | show
Introduced in R2019b

## inflate

Inflate map

## Syntax

inflate(map3D,radius)

## Description

inflate (map3D, radius) inflates each occupied position of the specified in the input occupancyMap3D object by the radius specified in meters. radius is rounded up to the nearest equivalent cell based on the resolution of the map. This inflation increases the size of the occupied locations in the map.

## Examples

## Get Ray Intersection Points on 3-D Occupancy Map

Import a 3-D occupancy map.

```
map3D = import0ccupancyMap3D("citymap.ot")
map3D =
    occupancyMap3D with properties:
    ProbabilitySaturation: [1.0000e-03 0.9990]
            Resolution: 1
        OccupiedThreshold: 0.6500
            FreeThreshold: 0.2000
```

Inflate the occupied areas by a radius of 1 m . Display the map.

```
inflate(map3D,1)
show(map3D)
```

Find the intersection points of rays and occupied map cells.

```
numRays = 10;
angles = linspace(-pi/2,pi/2,numRays);
directions = [cos(angles); sin(angles); zeros(1,numRays)]';
sensorPose = [55 40 1 1 0 0 0];
maxrange = 15;
[intersectionPts,is0ccupied] = rayIntersection(map3D,sensorPose,directions,maxrange)
intersectionPts = 10×3
\begin{tabular}{lll}
55.0000 & 32.0000 & 1.0000 \\
57.9118 & 32.0000 & 1.0000 \\
61.7128 & 32.0000 & 1.0000 \\
67.9904 & 32.5000 & 1.0000
\end{tabular}
```

```
    69.0000 37.5314 1.0000
    69.0000 42.4686 1.0000
    67.9904 47.5000 1.0000
    64.6418 51.4907 1.0000
    58.2757 49.0000 1.0000
    55.0000 49.0000 1.0000
isOccupied = 10×1
    1
    1
    1
    -1
    1
    1
    -1
    -1
    1
    1
```

Plot the intersection points and rays from the pose.
hold on
plotTransforms(sensorPose(1:3), sensorPose(4:end),...
'FrameSize',5,'MeshFilePath','groundvehicle.stl') \% Vehicle sensor pose
for $\mathrm{i}=1$ : numRays
plot3([sensorPose(1),intersectionPts(i,1)],...
[sensorPose(2), intersectionPts(i,2)],...
[sensorPose(3), intersectionPts(i,3)],'-b') \% Plot rays
if isOccupied(i) == 1
plot3(intersectionPts(i,1),intersectionPts(i,2),intersectionPts(i,3),'*r') \% Intersectio
end
end

## Occupancy Map



## Input Arguments

map3D - 3-D occupancy map
occupancyMap3D object
3-D occupancy map, specified as an occupancyMap3D object.
radius - Amount to inflate occupied locations
scalar
Amount to inflate occupied locations, specified as a scalar. radius is rounded up to the nearest cell value.

## See Also

## Classes

occupancyMap3D | lidarSLAM | occupancyMap

## Functions

insertPointCloud | setOccupancy | show

Introduced in R2019b

## insertPointCloud

Insert 3-D points or point cloud observation into map

## Syntax

insertPointCloud(map3D, pose, points, maxrange)
insertPointCloud(map3D, pose, ptcloud, maxrange)

## Description

insertPointCloud(map3D, pose, points, maxrange) inserts one or more sensor observations at the given points in the occupancy map, map3D. Occupied points are updated with an observation of 0.7 . All other points between the sensor pose and points are treated as obstacle-free and updated with an observation of 0.4. Points outside maxrange are not updated. NaN values are ignored.
insertPointCloud(map3D, pose, ptcloud, maxrange) inserts a ptcloud object into the map.

## Examples

## Create 3-D Occupancy Map and Inflate Points

The occupancyMap3D object stores obstacles in 3-D space, using sensor observations to map an environment. Create a map and add points from a point cloud to identify obstacles. Then inflate the obstacles in the map to ensure safe operating space around obstacles.

Create an occupancyMap3D object with a map resolution of 10 cells/meter.
map3D = occupancyMap3D(10);
 sensor that observes these points and is centered on the origin. Define two sets of points to insert multiple observations.

```
pose = [ 0 0 0 1 0 0 0];
points = repmat((0:0.25:2)', 1, 3);
points2 = [(0:0.25:2)' (2:-0.25:0)' (0:0.25:2)'];
maxRange = 5;
```

Insert the first set of points using insertPointCloud. The function uses the sensor pose and the given points to insert observations into the map. The colors displayed correlate to the height of the point only for illustrative purposes.

```
insertPointCloud(map3D,pose,points,maxRange)
show(map3D)
```


## Occupancy Map



Insert the second set of points. The ray between the sensor pose (origin) and these points overlap points from the previous insertion. Therefore, the free space between the sensor and the new points are updated and marked as free space.
insertPointCloud(map3D,pose, points2,maxRange)
show(map3D)

## Occupancy Map



Inflate the map to add a buffer zone for safe operation around obstacles. Define the vehicle radius and safety distance and use the sum of these values to define the inflation radius for the map.
vehicleRadius = 0.2;
safetyRadius = 0.3;
inflationRadius = vehicleRadius + safetyRadius;
inflate(map3D, inflationRadius);
show(map3D)


## Input Arguments

map3D - 3-D occupancy map
occupancyMap3D object
3-D occupancy map, specified as a occupancyMap3D object.

## points - Points of point cloud

n-by-3 matrix
Points of point cloud in sensor coordinates, specified as an $n$-by-3 matrix of [x y z] points, where $n$ is the number of points in the point cloud.

## ptcloud - Point cloud reading

pointCloud object
Point cloud reading, specified as a pointCloud object.

Note Using pointCloud objects requires Computer Vision Toolbox.

## pose - Position and orientation of vehicle

[x y z qw qx qy qz] vector

Position and orientation of vehicle, specified as an [x y z qw qx qy qz] vector. The vehicle pose is an $x y z$-position vector with a quaternion orientation vector specified as [qw qx qy qz].

## maxrange - Maximum range of sensor

scalar
Maximum range of point cloud sensor, specified as a scalar. Points outside this range are ignored.

## See Also

## Classes

occupancyMap3D | lidarSLAM| occupancyMap

## Functions

inflate | set0ccupancy| show
Introduced in R2019b

## rayIntersection

Find intersection points of rays and occupied map cells

## Syntax

[intersectionPts,is0ccupied] = rayIntersection(map3D,sensorPose,directions, maxrange)
[intersectionPts,isOccupied] = rayIntersection(map3D,sensorPose,directions, maxrange,ignoreUnknown)

## Description

[intersectionPts,is0ccupied] = rayIntersection(map3D,sensorPose,directions, maxrange) returns intersection points of rays in the specified map, map3D. Rays emanate from the specified sensorPose at the given orientations, directions. Intersection points are returned in the world coordinate frame. Use isOccupied to determine if the intersection point is at the sensor max range or if it intersects an obstacle.
[intersectionPts,isOccupied] = rayIntersection(map3D,sensorPose,directions, maxrange, ignoreUnknown) additionally accepts optional arguments for the sensors max range and whether to ignore unknown values. By default, the rays extend to the map boundary and unknown values are ignored.

## Examples

## Get Ray Intersection Points on 3-D Occupancy Map

Import a 3-D occupancy map.

```
map3D = import0ccupancyMap3D("citymap.ot")
map3D =
    occupancyMap3D with properties:
    ProbabilitySaturation: [1.0000e-03 0.9990]
            Resolution: 1
        OccupiedThreshold: 0.6500
            FreeThreshold: 0.2000
```

Inflate the occupied areas by a radius of 1 m . Display the map.

```
inflate(map3D,1)
show(map3D)
```

Find the intersection points of rays and occupied map cells.

```
numRays = 10;
angles = linspace(-pi/2,pi/2,numRays);
directions = [cos(angles); sin(angles); zeros(1,numRays)]';
```

```
sensorPose = [55 40 1 1 0 0 0];
maxrange = 15;
[intersectionPts,is0ccupied] = rayIntersection(map3D,sensorPose,directions,maxrange)
intersectionPts = 10\times3
\begin{tabular}{lll}
55.0000 & 32.0000 & 1.0000 \\
57.9118 & 32.0000 & 1.0000 \\
61.7128 & 32.0000 & 1.0000 \\
67.9904 & 32.5000 & 1.0000 \\
69.0000 & 37.5314 & 1.0000 \\
69.0000 & 42.4686 & 1.0000 \\
67.9904 & 47.5000 & 1.0000 \\
64.6418 & 51.4907 & 1.0000 \\
58.2757 & 49.0000 & 1.0000 \\
55.0000 & 49.0000 & 1.0000
\end{tabular}
is0ccupied = 10\times1
        1
        1
        1
        -1
        1
        1
    -1
    -1
        1
        1
```

Plot the intersection points and rays from the pose.
hold on
plotTransforms(sensorPose(1:3), sensorPose(4:end),...
'FrameSize',5,'MeshFilePath','groundvehicle.stl') \% Vehicle sensor pose
for $i=1: n u m R a y s$
plot3([sensorPose(1),intersectionPts(i,1)],...
[sensorPose(2), intersectionPts(i,2)],...
[sensorPose(3), intersectionPts(i,3)],'-b') \% Plot rays if isOccupied(i) == 1
plot3(intersectionPts(i,1),intersectionPts(i,2),intersectionPts(i,3),'*r') \% Intersectio end
end

## Occupancy Map



## Input Arguments

map3D - 3-D occupancy map
occupancyMap3D object
3-D occupancy map, specified as a occupancyMap3D object.

## sensorPose - Position and orientation of sensor

[x y z qw qx qy qz] vector
Position and orientation of sensor, specified as an [x y z qw qx qy qz] vector. The vehicle pose is an xyz-position vector with a quaternion orientation vector specified as [qw qx qy qz].

## directions - Orientation of rays emanating from sensor

n-by-3 [dx dy dz] matrix|n-by-2 [az el] matrix
Orientation of rays emanating from the sensor relative to the sensor coordinate frame, specified as an $n$-by-3 [dx dy dz] matrix or $n$-by-2 [az el] matrix.

- [dx dy dz] is a directional vector in xyz-coordinates.
- [az el] is a vector with azimuth angle, az, measured from the positive $x$ direction to the positive $y$ direction, and elevation angle from the $x y$-plane to the positive $z$-direction in sensor coordinate frame.


## maxrange - Maximum range of sensor <br> scalar

Maximum range of laser range sensor, specified as a scalar in meters. Range values greater than or equal to maxrange are considered free along the whole length of the ray, up to maxrange.

## ignoreUnknown - Interpret unknown values as free or occupied <br> 1 (default) | 0

Interpret unknown values in the map as free or occupied specified as 1 or 0 . Set this value to 0 to assume unknown values are occupied.

## Output Arguments

## intersectionPts - Intersection points

$n$-by-3 matrix
Intersection points, returned as $n$-by- 3 matrix of $\left[\begin{array}{lll}x & y & z\end{array}\right]$ points in the world frame, where $n$ is the length of directions.

## isOccupied - Occupancy status of ray end points

vector of zeroes and ones
Occupancy status of ray end points, returned as a vector of zeroes and ones. Use isOccupied to determine if the intersection point is at the sensor max range or if it intersects an obstacle.

## See Also

## Classes

occupancyMap3D | lidarSLAM | occupancyMap

## Functions

insertPointCloud |inflate | setOccupancy | show
Introduced in R2020a

## setOccupancy

Set occupancy probability of locations

## Syntax

set0ccupancy(map3D, xyz,occval)

## Description

set0ccupancy (map3D, xyz,occval) assigns the occupancy values to each specified xyz coordinate in the 3-D occupancy map.

## Examples

## Create and Export 3-D Occupancy Map

Create an occupancyMap3D object.

```
map3D = occupancyMap3D;
```

Create a ground plane and set occupancy values to 0 .

```
[xGround,yGround,zGround] = meshgrid(0:100,0:100,0);
xyzGround = [xGround(:) yGround(:) zGround(:)];
occval = 0;
setOccupancy(map3D,xyzGround,occval)
```

Create obstacles in specific world locations of the map.

```
[xBuilding1,yBuilding1,zBuilding1] = meshgrid(20:30,50:60,0:30);
[xBuilding2,yBuilding2,zBuilding2] = meshgrid(50:60,10:30,0:40);
[xBuilding3,yBuilding3,zBuilding3] = meshgrid(40:60,50:60,0:50);
[xBuilding4,yBuilding4,zBuilding4] = meshgrid(70:80,35:45,0:60);
xyzBuildings = [xBuilding1(:) yBuilding1(:) zBuilding1(:);...
    xBuilding2(:) yBuilding2(:) zBuilding2(:);...
    xBuilding3(:) yBuilding3(:) zBuilding3(:);...
    xBuilding4(:) yBuilding4(:) zBuilding4(:)];
```

Update the obstacles with new probability values and display the map.

```
obs = 0.65;
update0ccupancy(map3D,xyzBuildings,obs)
show(map3D)
```


## Occupancy Map



Check if the map file named citymap. ot already exist in the current directory and delete it before creating the map file.

```
if exist("citymap.ot",'file')
    delete("citymap.ot")
end
```

Export the map as an octree file.
filePath = fullfile(pwd,"citymap.ot");
export0ccupancyMap3D(map3D,filePath)

## Input Arguments

map3D - 3-D occupancy map
occupancyMap3D object
3-D occupancy map, specified as an occupancyMap3D object.
xyz - World coordinates
n-by-3 matrix
World coordinates, specified as an $n$-by-3 matrix of [lllll $\left.\begin{array}{lll}x & y & z\end{array}\right]$ points, where $n$ is the number of world coordinates.

## occval - Probability occupancy values

scalar | column vector
Probability occupancy values, specified as a scalar or a column vector with the same length as $x y z$. A scalar input is applied to all coordinates in xyz.

Values close to 0 represent certainty that the cell is not occupied and obstacle-free.

## See Also

## Classes

occupancyMap3D | lidarSLAM | occupancyMap

## Functions

insertPointCloud |inflate | set0ccupancy | show

## Introduced in R2019b

## show

Show occupancy map

## Syntax

axes $=$ show(map3D)
show(map3D,"Parent", parent)

## Description

axes $=$ show(map3D) displays the occupancy map, map3D, in the current axes, with the axes labels representing the world coordinates.

The function displays the 3-D environment using 3-D voxels for areas with occupancy values greater than the 0ccupiedThreshold property value specified in map3D. The color of the 3-D plot is strictly height-based.
show(map3D, "Parent", parent) displays the occupancy map in the axes handle specified by parent.

## Examples

## Get Ray Intersection Points on 3-D Occupancy Map

Import a 3-D occupancy map.

```
map3D = import0ccupancyMap3D("citymap.ot")
map3D =
    occupancyMap3D with properties:
        ProbabilitySaturation: [1.0000e-03 0.9990]
            Resolution: 1
            OccupiedThreshold: 0.6500
                FreeThreshold: 0.2000
```

Inflate the occupied areas by a radius of 1 m . Display the map.

```
inflate(map3D,1)
show(map3D)
```

Find the intersection points of rays and occupied map cells.

```
numRays = 10;
angles = linspace(-pi/2,pi/2,numRays);
directions = [cos(angles); sin(angles); zeros(1,numRays)]';
sensorPose = [55 40 1 1 0 0 0];
maxrange = 15;
[intersectionPts,is0ccupied] = rayIntersection(map3D,sensorPose,directions,maxrange)
```

```
intersectionPts = 10×3
\begin{tabular}{lll}
55.0000 & 32.0000 & 1.0000 \\
57.9118 & 32.0000 & 1.0000 \\
61.7128 & 32.0000 & 1.0000 \\
67.9904 & 32.5000 & 1.0000 \\
69.0000 & 37.5314 & 1.0000 \\
69.0000 & 42.4686 & 1.0000 \\
67.9904 & 47.5000 & 1.0000 \\
64.6418 & 51.4907 & 1.0000 \\
58.2757 & 49.0000 & 1.0000 \\
55.0000 & 49.0000 & 1.0000
\end{tabular}
isOccupied = 10×1
        1
        1
        1
    -1
        1
        1
    -1
    -1
        1
        1
```

Plot the intersection points and rays from the pose.
hold on
plotTransforms(sensorPose(1:3), sensorPose(4:end),...
'FrameSize',5,'MeshFilePath', groundvehicle.stl') \% Vehicle sensor pose
for $i=1$ :numRays
plot3([sensorPose(1),intersectionPts(i,1)],...
[sensorPose(2),intersectionPts(i,2)],...
[sensorPose(3),intersectionPts(i,3)],'-b') \% Plot rays
if isOccupied(i) == 1
plot3(intersectionPts(i,1),intersectionPts(i,2),intersectionPts(i,3),'*r') \% Intersectio
end
end

## Occupancy Map



## Input Arguments

map3D - 3-D occupancy map
occupancyMap3D object
3-D occupancy map, specified as an occupancyMap3D object.
parent - Axes used to plot the map
Axes object | UIAxes object
Axes used to plot the map, specified as either an Axes or UIAxes object. See axes or uiaxes.

## Output Arguments

## axes - Axes handle for map

Axes object | UIAxes object
Axes handle for map, returned as either an Axes or UIAxesobject. See axes or uiaxes.

## See Also

## Classes

occupancyMap3D | lidarSLAM | occupancyMap

## Functions <br> insertPointCloud | setOccupancy | show <br> Introduced in R2019b

## updateOccupancy

Update occupancy probability at locations

## Syntax

update0ccupancy(map3D, xyz,obs)

## Description

updateOccupancy (map3D, xyz,obs) probabilistically integrates the observation values, obs, to each specified xyz coordinate in the occupancyMap3D object, map3D.

## Examples

## Create and Export 3-D Occupancy Map

Create an occupancyMap3D object.

```
map3D = occupancyMap3D;
```

Create a ground plane and set occupancy values to 0 .

```
[xGround,yGround,zGround] = meshgrid(0:100,0:100,0);
xyzGround = [xGround(:) yGround(:) zGround(:)];
occval = 0;
setOccupancy(map3D,xyzGround,occval)
```

Create obstacles in specific world locations of the map.

```
[xBuilding1,yBuilding1,zBuilding1] = meshgrid(20:30,50:60,0:30);
[xBuilding2,yBuilding2,zBuilding2] = meshgrid(50:60,10:30,0:40);
[xBuilding3,yBuilding3,zBuilding3] = meshgrid(40:60,50:60,0:50);
[xBuilding4,yBuilding4,zBuilding4] = meshgrid(70:80,35:45,0:60);
xyzBuildings = [xBuilding1(:) yBuilding1(:) zBuilding1(:);...
    xBuilding2(:) yBuilding2(:) zBuilding2(:);...
    xBuilding3(:) yBuilding3(:) zBuilding3(:);...
    xBuilding4(:) yBuilding4(:) zBuilding4(:)];
```

Update the obstacles with new probability values and display the map.

```
obs = 0.65;
update0ccupancy(map3D,xyzBuildings,obs)
show(map3D)
```


## Occupancy Map



Check if the map file named citymap. ot already exist in the current directory and delete it before creating the map file.

```
if exist("citymap.ot",'file')
    delete("citymap.ot")
end
```

Export the map as an octree file.
filePath = fullfile(pwd,"citymap.ot");
export0ccupancyMap3D(map3D,filePath)

## Input Arguments

map3D - 3-D occupancy map
occupancyMap3D object
3-D occupancy map, specified as an occupancyMap3D object.
xyz - World coordinates
n-by-3 matrix
World coordinates, specified as an $n$-by-3 matrix of $\left[\begin{array}{lll}x & y & z\end{array}\right]$ points, where $n$ is the number of world coordinates.
obs - Probability observation values
numeric scalar | logical scalar | $n$-by-1 column vector
Probability observation values, specified as a numeric or logical scalar, or as an $n$-by- 1 column vector with the same size as $x y z$.
obs values can be from 0 to 1 , but if obs is a logical array, the function uses the default observation values of 0.7 (true) and 0.4 (false). If obs is a numeric or logical scalar, the value is applied to all coordinates in xyz.

## See Also

## Classes

occupancyMap3D | lidarSLAM | occupancyMap

## Functions

insertPointCloud |inflate | set0ccupancy | show
Introduced in R2019b

## odometryMotionModel

Create an odometry motion model

## Description

odometryMotionModel creates an odometry motion model object for differential drive vehicles. This object contains specific motion model parameters. You can use this object to specify the motion model parameters in the monteCarloLocalization object.

This motion model assumes that the vehicle makes pure rotation and translation motions to travel from one location to the other. The model propagates points for either forward or backwards motion based on these motion patterns. The elements of the Noise property refer to the variance in the motion. To see the effect of changing the noise parameters, use showNoiseDistribution.

## Creation

## Syntax

omm = odometryMotionModel

## Description

omm = odometryMotionModel creates an odometry motion model object for differential drive vehicles.

## Properties

## Noise - Gaussian noise for vehicle motion

[0.2 0.2 0.2 0.2] (default) | 4-element vector
Gaussian noise for vehicle motion, specified as a 4 -element vector. This property represents the variance parameters for Gaussian noise applied to vehicle motion. The elements of the vector correspond to the following errors in order:

- Rotational error due to rotational motion
- Rotational error due to translational motion
- Translational error due to translation motion
- Translational error due to rotational motion


## Type - Type of the odometry motion model

'DifferentialDrive' (default)
This property is read-only.
Type of the odometry motion model, returned as 'DifferentialDrive'. This read-only property indicates the type of odometry motion model being used by the object.

## Object Functions

showNoiseDistribution Display noise parameter effects

## Examples

## Predict Poses Based On An Odometry Motion Model

This example shows how to use the odometryMotionModel class to predict the pose of a vehicle. An odometryMotionModel object contains the motion model parameters for a differential drive vehicle. Use the object to predict the pose of a vehicle based on its current and previous poses and the motion model parameters.

Create odometry motion model object.
motionModel = odometryMotionModel;
Define previous poses and the current odometry reading. Each pose prediction corresponds to a row in previousPoses vector.

```
previousPoses = rand(10,3);
```

currentOdom = [0.1 0.1 0.1];

The first call to the object initializes values and returns the previous poses as the current poses.

```
currentPoses = motionModel(previousPoses, currentOdom);
```

Subsequent calls to the object with updated odometry poses returns the predicted poses based on the motion model.

```
currentOdom = currentOdom + [0.1 0.1 0.05];
predPoses = motionModel(previousPoses, currentOdom);
```


## Show Noise Distribution Effects for Odometry Motion Model

This example shows how to visualize the effect of different noise parameters on the odometryMotionModel class. An odometryMotionModel object contains the motion model noise parameters for a differential drive vehicle. Use showNoiseDistribution to visualize how changing these values affect the distribution of predicted poses.

Create a motion model object.
motionModel $=$ odometryMotionModel;
Show the distribution of particles with the existing noise parameters. Each particle is a hypothesis for the predicted pose.

```
showNoiseDistribution(motionModel);
```



Show the distribution with a specified odometry pose change and number of samples. The change in odometry is used as the final pose with hypotheses distributed around based on the Noise parameters.

```
showNoiseDistribution(motionModel, ...
    'OdometryPoseChange', [0.5 0.1 0.25], ...
    'NumSamples', 1000);
```



Change the Noise parameters and visualize the effects. Use the same odometry pose change and number of samples.

```
motionModel.Noise = [0.2 1 0.2 1];
showNoiseDistribution(motionModel, ...
    'OdometryPoseChange', [0.5 0.1 0.25], ...
    'NumSamples', 1000);
```



## Limitations

If you make changes to your motion model after using it with the monteCarloLocalization object, call release on that object beforehand. For example:

```
mcl = monteCarloLocalization;
[isUpdated,pose,covariance] = mcl(ranges,angles);
release(mcl)
mcl.MotionModel.Noise = [0.25 0.25 0.4 0.4];
```


## References

[1] Thrun, Sebatian, Wolfram Burgard, and Dieter Fox. Probabilistic Robotics. MIT Press, 2005.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

monteCarloLocalization|likelihoodFieldSensorModel

## Topics

"Localize TurtleBot Using Monte Carlo Localization"

Introduced in R2019b

## showNoiseDistribution

Display noise parameter effects

## Syntax

showNoiseDistribution(omm0bj)
showNoiseDistribution(omm0bj)
showNoiseDistribution(omm0bj, Name, Value)

## Description

showNoiseDistribution (omm0bj) shows the noise distribution for a default odometry pose update, number of samples and the current noise parameters on the input object.
axes $=$ showNoiseDistribution (omm0bj) shows the noise distribution and returns the axes handle.
showNoiseDistribution(ommObj, Name, Value) provides additional options specified by one or more Name, Value pairs. Name is the property name and Value is the corresponding value. Name must appear inside single quotes (' '). You can specify several name-value pair arguments in any order as Name1, Value1, . . . , NameN, ValueN. Properties not specified retain their default values.

## Examples

## Show Noise Distribution Effects for Odometry Motion Model

This example shows how to visualize the effect of different noise parameters on the odometryMotionModel class. An odometryMotionModel object contains the motion model noise parameters for a differential drive vehicle. Use showNoiseDistribution to visualize how changing these values affect the distribution of predicted poses.

Create a motion model object.

```
motionModel = odometryMotionModel;
```

Show the distribution of particles with the existing noise parameters. Each particle is a hypothesis for the predicted pose.

```
showNoiseDistribution(motionModel);
```



Show the distribution with a specified odometry pose change and number of samples. The change in odometry is used as the final pose with hypotheses distributed around based on the Noise parameters.

```
showNoiseDistribution(motionModel, ...
    'OdometryPoseChange', [0.5 0.1 0.25], ...
    'NumSamples', 1000);
```



Change the Noise parameters and visualize the effects. Use the same odometry pose change and number of samples.

```
motionModel.Noise = [0.2 1 0.2 1];
showNoiseDistribution(motionModel, ...
    'OdometryPoseChange', [0.5 0.1 0.25], ...
    'NumSamples', 1000);
```



## Input Arguments

## ommObj - odometryMotionModel object

handle
odometryMotionModel object, specified as a handle. Create this object using odometryMotionModel.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . , NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Example: 'OdometryPoseChange',[1 1 pi]

## OdometryPoseChange - Change in odometry

three-element vector
Change in odometry of the robot, specified as a comma-separated pair consisting of 'OdometryPoseChange' and a three-element vector, [x y theta].

## NumSamples - Number of particles to display

scalar

Number of particles to display, specified as a comma-separated pair consisting of 'NumSamples ' and a scalar.

## Parent - Axes to plot the map

Axes object | UIAxes object
Axes to plot the map, specified as a comma-separated pair consisting of 'Parent' and either an Axes or UIAxes object. See axes or uiaxes.

## See Also

monteCarloLocalization| odometryMotionModel|likelihoodFieldSensorModel
Introduced in R2019b

## optimizePathOptions

Create optimization options for optimizePath function

## Description

Optimization options are grouped into four categories:

- Trajectory Parameters - Specify the desired robot motion throughout the path.
- Obstacle Parameters - Specify the distances which dictate the influence of obstacle on the path.
- Solver Parameters - Specify the options for solver used to optimize the path.
- Weights - Specify the cost function weights.


## Creation

## Syntax

options = optimizePath0ptions

## Description

options = optimizePathOptions creates a set of default optimization options for optimizePath function.

## Properties

Trajectory Parameters
MaxPathStates - Maximum number of poses allowed in path
200 (default) | integer greater than or equal to 3
Maximum number of poses allowed in the path, specified as an integer greater than or equal to 3 .
Example: options.MaxPathStates $=100$
Data Types: single | double
ReferenceDeltaTime - Travel time between two consecutive poses
0.3 (default) | positive scalar

Travel time between two consecutive poses, specified as a positive scalar in seconds. This parameter along with MaxVelocity impacts the interpolation distance between poses. Increase this value to have lesser number of poses and reduce it to have higher number of poses in the output path.
Example: options.ReferenceDeltaTime $=0.5$
Data Types: single | double

## MinTurningRadius - Minimum turning radius in path

1 (default) | positive scalar
Minimum turning radius in the path, specified as a positive scalar in meters. Note that this is a soft constraint and may be ignored based on the value of WeightMinTurningRadius parameter with respect to other weights.

Example: options.MinTurningRadius = 1.5
Data Types: single|double
MaxVelocity - Maximum velocity along path
0.4 (default) | positive scalar

Maximum velocity along the path, specified as a positive scalar in meters per second. Note that this is a soft constraint and may be ignored based on the value of WeightVelocity parameter with respect to other weights.

Example: options.MaxVelocity $=0.5$
Data Types: single|double
MaxAngularVelocity - Maximum angular velocity along path
0.3 (default) | positive scalar

Maximum angular velocity along the path, specified as a positive scalar in radians per second. Note that this is a soft constraint and may be ignored based on the value of WeightAngularVelocity parameter with respect to other weights.
Example: options.MaxAngularVelocity $=0.5$
Data Types: single | double

## MaxAcceleration - Maximum acceleration along path <br> 0.5 (default) | positive scalar

Maximum acceleration along the path, specified as a positive scalar in meters per second squared. Note that this is a soft constraint and may be ignored based on the value of WeightAcceleration parameter with respect to other weights.

Example: options.MaxAcceleration $=0.6$
Data Types: single | double
MaxAngularAcceleration - Maximum angular acceleration along path
0.5 (default) | positive scalar

Maximum angular acceleration along path, specified as a positive scalar in radians per second squared. Note that this is a soft constraint and may be ignored based on the value of WeightAngularAcceleration parameter with respect to other weights.

Example: options.MaxAngularAcceleration $=0.6$
Data Types: single | double

## Obstacle Parameters

## ObstacleSafetyMargin - Safety distance from obstacles

0.5 (default)| positive scalar

Safety distance from the obstacles, specified as a positive scalar in meters. Note that this is a soft constraint and may be ignored based on the value of WeightObstacles parameter with respect to other weights.
Example: options.ObstacleSafetyMargin = 0.6
Data Types: single | double

## ObstacleCutOffDistance - Obstacle cutoff distance

2.5 (default) | positive scalar

Obstacle cutoff distance, specified as a positive scalar in meters. The path optimizer ignores obstacles beyond the cutoff distance.
Example: options.ObstacleCut0ffDistance = 1.5
Data Types: single | double

## ObstacleInclusionDistance - Obstacle inclusion distance

0.75 (default) | positive scalar

Obstacle inclusion distance, specified as a positive scalar in meters. The path optimizer considers all obstacles within the inclusion distance, but only the closest obstacle on the left and on the right between the inclusion and cutoff distances.

```
Example: options.ObstacleInclusionDistance = 0.5
```

Data Types: single | double

## Solver Parameters

NumIteration - Number of solver invocations
4 (default) | positive integer
Number of solver invocations, specified as a positive integer. This value also specifies the number of times interpolation occurs during optimization.
Example: options.NumIteration = 5
Data Types: single | double
MaxSolverIteration - Maximum number of iterations for each solver invocation
15 (default) | positive integer
Maximum number of iterations for each solver invocation, specified as a positive integer.
Example: options.MaxSolverIteration = 12
Data Types: single | double

## Weights

## WeightTime - Cost function weight for time

10 (default) | nonnegative scalar
Cost function weight for time, specified as a nonnegative scalar. To lower the travel time, increase this weight value.
Example: options.WeightTime $=12$
Data Types: single | double

## WeightSmoothness - Cost function weight for nonholonomic motion <br> 1000 (default) | nonnegative scalar

Cost function weight for nonholonomic motion, specified as a nonnegative scalar. To obtain smoother path, increase this weight value.

Example: options.WeightSmoothness = 500
Data Types: single|double
WeightMinTurningRadius - Cost function weight for complying with minimum turning radius
10 (default) | nonnegative scalar
Cost function weight for complying with minimum turning radius, specified as a nonnegative scalar. To ensure the turning radius is above minimum turning radius, increase this weight value.
Example: options.WeightMinTurningRadius = 15
Data Types: single | double
WeightVelocity - Cost function weight for velocity
100 (default) | nonnegative scalar
Cost function weight for velocity, specified as a nonnegative scalar. To maintain the velocity below MaxVelocity, increase this weight value.
Example: options.WeightVelocity = 120
Data Types: single|double
WeightAngularVelocity - Cost function weight for angular velocity
10 (default) | nonnegative scalar
Cost function weight for angular velocity, specified as a nonnegative scalar. To maintain the angular velocity below MaxAngularVelocity, increase this weight value.

Example: options.WeightAngularVelocity = 15
Data Types: single | double

## WeightAcceleration - Cost function weight for acceleration

10 (default) | nonnegative scalar
Cost function weight for acceleration, specified as a nonnegative scalar. To maintain the acceleration below MaxAcceleration, increase this weight value.

Example: options.WeightAcceleration = 15
Data Types: single | double
WeightAngularAcceleration - Cost function weight for angular acceleration
10 (default) | nonnegative scalar
Cost function weight for angular acceleration, specified as a nonnegative scalar. To maintain the angular acceleration below MaxAngularAcceleration, increase this weight value.
Example: options.WeightAngularAcceleration = 15
Data Types: single | double

## WeightObstacles - Cost function weight for maintaining safe distance from obstacles

50 (default) | nonnegative scalar
Cost function weight for maintaining safe distance from obstacles, specified as a nonnegative scalar. To maintain the safe distance from obstacles, increase this weight value.
Example: options.WeightObstacles = 60
Data Types: single | double

## Examples

## Optimize Planned Path

## Setup Environment

Load a map into the workspace.
map = load("exampleMaps.mat").complexMap;
Create a binary occupancy map.
map = binary0ccupancyMap(map);
Create a state validator object.
stateValidator = validatorOccupancyMap;
Assign the map to the state validator object.
stateValidator.Map = map;
Set the validation distance for the validator.
stateValidator.ValidationDistance $=0.01$;

## Plan Path

Initialize the plannerHybridAStar object with the state validator object. Specify the MinTurningRadius property of the planner as 2 meters.
planner = plannerHybridAStar(stateValidator,MinTurningRadius=2);
Define start and goal poses as [ $x$ y theta] vectors. $x$ and $y$ specify the position in meters, and theta specifies the orientation angle in radians.

```
start = [6 3 pi/2];
goal = [32 32 0];
```

Plan a path from the start pose to the goal pose.

```
path = plan(planner,start,goal);
```

inpath = path.States;

Optimize Path
Configure options for optimization.

```
options = optimizePathOptions
options =
optimizePathOptions
    Trajectory Parameters
            MaxPathStates: 200
            ReferenceDeltaTime: 0.3000
            MinTurningRadius: 1
                    MaxVelocity: 0.4000
            MaxAngularVelocity: 0.3000
            MaxAcceleration: 0.5000
        MaxAngularAcceleration: 0.5000
    Obstacle Parameters
            ObstacleSafetyMargin: 0.5000
            ObstacleCutOffDistance: 2.5000
        ObstacleInclusionDistance: 0.7500
    Solver Parameters
                            NumIteration: 4
            MaxSolverIteration: 15
    Weights
                WeightTime: 10
            WeightSmoothness: 1000
        WeightMinTurningRadius: 10
            WeightVelocity: 100
        WeightAngularVelocity: 10
            WeightAcceleration: 10
    WeightAngularAcceleration: 10
            WeightObstacles: 50
```

Set the minimum turning radius value as same as in the planner.

```
options.MinTurningRadius = 2;
```

Specify the maximum number of poses allowed in the optimized path.
options.MaxPathStates $=$ size(inpath,1) * 3;
Maintain a safe distance of 0.75 meters from the obstacles.
options.ObstacleSafetyMargin = 0.75;
Optimize the path generated by the planner.

```
optpath = optimizePath(inpath,map,options);
```


## Visualize

Visualize input path and optimized path in the map.

```
show(map)
hold on
quiver(inpath(:,1),inpath(:,2),cos(inpath(:,3)),sin(inpath(:,3)),0.1);
quiver(optpath(:,1),optpath(:,2),cos(optpath(:,3)),sin(optpath(:,3)),0.1);
legend("Input Path","Optimized Path")
```

Binary Occupancy Grid


## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.

## See Also

optimizePath
Introduced in R2022a

## pathmetrics

Information for path metrics

## Description

The pathmetrics object holds information for computing path metrics. Use object functions to calculate smoothness, clearance, and path validity based on a set of poses and the associated map environment.

## Creation

## Syntax

```
pathMetrics0bj = pathmetrics(path)
pathMetrics0bj = pathmetrics(path,validator)
Description
```

pathMetricsObj = pathmetrics(path) creates an object based on the input navPath object. The state validator is assumed to be a validator0ccupancyMap object. The path input sets the value of the "Path" on page 2-0 property.
pathMetricsObj = pathmetrics(path,validator) creates an object based on the input navPath object and associated state validator for checking the path validity. The validator input sets the value of the "StateValidator" on page 2-0 property.

## Properties

Path - Path data structure
navPath object
Path data structure, specified as a navPath object is the path whose metric is to be calculated.

## StateValidator - Validator for states on path

validator0ccupancyMap(stateSpaceSE2,binary0ccupancyMap(10)) (default)|
validatorOccupancyMap object | validatorVehicleCostmap object
Validator for states on path, specified either as a validator0ccupancyMap or validatorVehicleCostmap object.

## Object Functions

clearance Minimum clearance of path
isPathValid Determine if planned path is obstacle free
show
Visualize path metrics in map environment
smoothness Smoothness of path

## Examples

## Compute Path Metrics

Compute smoothness, clearance, and validity of a planned path based on a set of poses and the associated map environment.

## Load and Assign Map to State Validator

Create an occupancy map from an example map and set the map resolution.

```
load exampleMaps.mat; % simpleMap
mapResolution = 1; % cells/meter
map = occupancyMap(simpleMap,mapResolution);
```

Create a Dubins state space.

```
statespace = stateSpaceDubins;
```

Create a state validator based on occupancy map to store the parameters and states in the Dubins state space.

```
statevalidator = validatorOccupancyMap(statespace);
```

Assign the map to the validator.

```
statevalidator.Map = map;
```

Set the validation distance for the validator.

```
statevalidator.ValidationDistance = 0.01;
```

Update the state space bounds to be the same as the map limits.

```
statespace.StateBounds = [map.XWorldLimits;map.YWorldLimits;[-pi pi]];
```


## Plan Path

Create an RRT* path planner and allow further optimization.

```
planner = plannerRRTStar(statespace,statevalidator);
planner.ContinueAfterGoalReached = true;
```

Reduce the maximum number of iterations and increase the maximum connection distance.

```
planner.MaxIterations = 2500;
planner.MaxConnectionDistance = 0.3;
```

Define start and goal states for the path planner as $[x, y$, theta] vectors. $x$ and $y$ are the Cartesian coordinates, and theta is the orientation angle.

```
start = [2.5, 2.5, 0]; % [meters, meters, radians]
goal = [22.5, 8.75, 0];
```

Plan a path from the start state to the goal state. The plan function returns a navPath object.

```
rng(100,'twister') % repeatable result
[path,solutionInfo] = plan(planner,start,goal);
```


## Compute and Visualize Path Metrics

Create a path metrics object.
pathMetrics0bj = pathmetrics(path,statevalidator);
Check path validity. The result is 1 (true) if the planned path is obstacle free. 0 (false) indicates an invalid path.
isPathValid(pathMetrics0bj)
ans $=$ logical
1

Calculate the minimum clearance of the path.
clearance(pathMetrics0bj)
ans $=1.4142$
Evaluate the smoothness of the path. Values close to 0 indicate a smoother path. Straight-line paths return a value of 0 .

```
smoothness(pathMetricsObj)
```

ans $=1.7318$
Visualize the minimum clearance of the path.

```
show(pathMetrics0bj)
legend('Planned Path','Minimum Clearance')
```



## Vehicle Path Planning and Metrics Computation in a 2-D Costmap Environment

Plan a vehicle path through a parking lot using the RRT* algorithm. Compute and visualize the smoothness, clearance, and validity of the planned path.

## Load and Assign Map to State Validator

Load a costmap of a parking lot. Plot the costmap to see the parking lot and the inflated areas that the vehicle should avoid.

```
load parkingLotCostmap.mat;
costmap = parkingLotCostmap;
plot(costmap)
xlabel('X (meters)')
ylabel('Y (meters)')
```



Create a stateSpaceDubins object and increase the minimum turing radius to 4 meters.

```
statespace = stateSpaceDubins;
statespace.MinTurningRadius = 4; % meters
```

Create a validatorVehicleCostmap object using the created state space.
statevalidator = validatorVehicleCostmap(statespace);
Assign the parking lot costmap to the state validator object.

```
statevalidator.Map = costmap;
```


## Plan Path

Define start and goal poses for the vehicle as $[x, y, \theta]$ vectors. World units for the $(x, y)$ locations are in meters. World units for the orientation angles $\theta$ are in degrees.

```
startPose = [5, 5, 90]; % [meters, meters, degrees]
goalPose = [40, 38, 180]; % [meters, meters, degrees]
```

Use a pathPlannerRRT (Automated Driving Toolbox) object and the plan (Automated Driving Toolbox) function to plan the vehicle path from the start pose to the goal pose.

```
planner = pathPlannerRRT(costmap);
refPath = plan(planner,startPose,goalPose);
```

Interpolate along the path at every one meter. Convert the orientation angles from degrees to radians.

```
poses = zeros(size(refPath.PathSegments,2)+1,3);
poses(1,:) = refPath.StartPose;
for i = 1:size(refPath.PathSegments,2)
    poses(i+1,:) = refPath.PathSegments(i).GoalPose;
end
poses(:,3) = deg2rad(poses(:,3));
```

Create a navPath object using the Dubins state space object and the states specified by poses.

```
path = navPath(statespace,poses);
```


## Compute and Visualize Path Metrics

Create a pathmetrics object.

```
pathMetricsObj = pathmetrics(path,statevalidator);
```

Check path validity. The result is 1 (true) if the planned path is obstacle free. 0 (false) indicates an invalid path.

```
isPathValid(pathMetrics0bj)
ans = logical
    1
```

Compute and visualize the minimum clearance of the path.

```
clearance(pathMetrics0bj)
ans = 0.5000
show(pathMetrics0bj)
legend('Inflated Areas','Planned Path','Minimum Clearance')
xlabel('X (meters)')
ylabel('Y (meters)')
```



Compute and visualize the smoothness of the path. Values close to 0 indicate a smoother path. Straight-line paths return a value of 0 .

```
smoothness(pathMetrics0bj)
ans = 0.0842
show(pathMetrics0bj,'Metrics',{'Smoothness'})
legend('Inflated Areas','Path Smoothness')
xlabel('X (meters)')
ylabel('Y (meters)')
```



Visualize the clearance for each state of the path.
show(pathMetrics0bj,'Metrics',\{'StatesClearance'\})
legend('Inflated Areas','Planned Path','Clearance of Path States')
xlabel('X (meters)')
ylabel('Y (meters)')


## See Also

occupancyMap | occupancyMap3D | plannerRRTStar
Introduced in R2019b

## clearance

Minimum clearance of path

## Syntax

clearance(pathMetrics0bj)
clearance(pathMetrics0bj,'Type','states')

## Description

clearance(pathMetricsObj) returns the minimum clearance of the path. Clearance is measured as the minimum distance between grid cell centers of states on the path and obstacles in the specified map environment.

Note The computed clearance is accurate up to sqrt(2) times grid map cell size.
clearance(pathMetrics0bj,'Type','states') returns the set of minimum distances for each state of the path, in the form of an $n$-by- 1 vector, where $n$ is the number of states.

## Examples

## Compute Path Metrics

Compute smoothness, clearance, and validity of a planned path based on a set of poses and the associated map environment.

## Load and Assign Map to State Validator

Create an occupancy map from an example map and set the map resolution.

```
load exampleMaps.mat; % simpleMap
mapResolution = 1; % cells/meter
map = occupancyMap(simpleMap,mapResolution);
```

Create a Dubins state space.

```
statespace = stateSpaceDubins;
```

Create a state validator based on occupancy map to store the parameters and states in the Dubins state space.

```
statevalidator = validatorOccupancyMap(statespace);
```

Assign the map to the validator.
statevalidator.Map = map;
Set the validation distance for the validator.

```
statevalidator.ValidationDistance = 0.01;
```

Update the state space bounds to be the same as the map limits.

```
statespace.StateBounds = [map.XWorldLimits;map.YWorldLimits;[-pi pi]];
```


## Plan Path

Create an RRT* path planner and allow further optimization.

```
planner = plannerRRTStar(statespace,statevalidator);
```

planner.ContinueAfterGoalReached = true;

Reduce the maximum number of iterations and increase the maximum connection distance.

```
planner.MaxIterations = 2500;
planner.MaxConnectionDistance = 0.3;
```

Define start and goal states for the path planner as [ $x, y$, theta] vectors. $x$ and $y$ are the Cartesian coordinates, and theta is the orientation angle.

```
start = [2.5, 2.5, 0]; % [meters, meters, radians]
goal = [22.5, 8.75, 0];
```

Plan a path from the start state to the goal state. The plan function returns a navPath object.

```
rng(100,'twister') % repeatable result
[path,solutionInfo] = plan(planner,start,goal);
```


## Compute and Visualize Path Metrics

Create a path metrics object.
pathMetrics0bj = pathmetrics(path,statevalidator);
Check path validity. The result is 1 (true) if the planned path is obstacle free. 0 (false) indicates an invalid path.

```
isPathValid(pathMetricsObj)
ans = logical
    1
```

Calculate the minimum clearance of the path.

```
clearance(pathMetrics0bj)
```

ans $=1.4142$

Evaluate the smoothness of the path. Values close to 0 indicate a smoother path. Straight-line paths return a value of 0 .

```
smoothness(pathMetrics0bj)
```

ans $=1.7318$

Visualize the minimum clearance of the path.
show(pathMetrics0bj)
legend('Planned Path','Minimum Clearance')


## Vehicle Path Planning and Metrics Computation in a 2-D Costmap Environment

Plan a vehicle path through a parking lot using the RRT* algorithm. Compute and visualize the smoothness, clearance, and validity of the planned path.

## Load and Assign Map to State Validator

Load a costmap of a parking lot. Plot the costmap to see the parking lot and the inflated areas that the vehicle should avoid.

```
load parkingLotCostmap.mat;
costmap = parkingLotCostmap;
plot(costmap)
xlabel('X (meters)')
ylabel('Y (meters)')
```



Create a stateSpaceDubins object and increase the minimum turing radius to 4 meters.

```
statespace = stateSpaceDubins;
statespace.MinTurningRadius = 4; % meters
```

Create a validatorVehicleCostmap object using the created state space.
statevalidator = validatorVehicleCostmap(statespace);
Assign the parking lot costmap to the state validator object.

```
statevalidator.Map = costmap;
```


## Plan Path

Define start and goal poses for the vehicle as $[x, y, \theta]$ vectors. World units for the $(x, y)$ locations are in meters. World units for the orientation angles $\theta$ are in degrees.

```
startPose = [5, 5, 90]; % [meters, meters, degrees]
goalPose = [40, 38, 180]; % [meters, meters, degrees]
```

Use a pathPlannerRRT (Automated Driving Toolbox) object and the plan (Automated Driving Toolbox) function to plan the vehicle path from the start pose to the goal pose.

```
planner = pathPlannerRRT(costmap);
refPath = plan(planner,startPose,goalPose);
```

Interpolate along the path at every one meter. Convert the orientation angles from degrees to radians.

```
poses = zeros(size(refPath.PathSegments,2)+1,3);
poses(1,:) = refPath.StartPose;
for i = 1:size(refPath.PathSegments,2)
    poses(i+1,:) = refPath.PathSegments(i).GoalPose;
end
poses(:,3) = deg2rad(poses(:,3));
```

Create a navPath object using the Dubins state space object and the states specified by poses.

```
path = navPath(statespace,poses);
```


## Compute and Visualize Path Metrics

Create a pathmetrics object.

```
pathMetricsObj = pathmetrics(path,statevalidator);
```

Check path validity. The result is 1 (true) if the planned path is obstacle free. 0 (false) indicates an invalid path.

```
isPathValid(pathMetrics0bj)
ans = logical
    1
```

Compute and visualize the minimum clearance of the path.

```
clearance(pathMetrics0bj)
ans = 0.5000
show(pathMetrics0bj)
legend('Inflated Areas','Planned Path','Minimum Clearance')
xlabel('X (meters)')
ylabel('Y (meters)')
```



Compute and visualize the smoothness of the path. Values close to 0 indicate a smoother path. Straight-line paths return a value of 0 .

```
smoothness(pathMetrics0bj)
ans = 0.0842
show(pathMetrics0bj,'Metrics',{'Smoothness'})
legend('Inflated Areas','Path Smoothness')
xlabel('X (meters)')
ylabel('Y (meters)')
```



Visualize the clearance for each state of the path.
show(pathMetrics0bj,'Metrics',\{'StatesClearance'\})
legend('Inflated Areas','Planned Path','Clearance of Path States')
xlabel('X (meters)')
ylabel('Y (meters)')


## Input Arguments

## pathMetrics0bj - Information for path metrics

pathmetrics object
Information for path metrics, specified as a pathmetrics object.

## See Also

Objects
pathmetrics

## Functions

isPathValid|show|smoothness
Introduced in R2019b

## isPathValid

Determine if planned path is obstacle free

## Syntax

isPathValid(pathMetrics0bj)

## Description

isPathValid(pathMetricsObj) returns either a logical 1 (true) if the planned path is obstacle free or a logical 0 (false) if the path is invalid.

## Examples

## Compute Path Metrics

Compute smoothness, clearance, and validity of a planned path based on a set of poses and the associated map environment.

## Load and Assign Map to State Validator

Create an occupancy map from an example map and set the map resolution.

```
load exampleMaps.mat; % simpleMap
mapResolution = 1; % cells/meter
map = occupancyMap(simpleMap,mapResolution);
```

Create a Dubins state space.
statespace = stateSpaceDubins;
Create a state validator based on occupancy map to store the parameters and states in the Dubins state space.
statevalidator = validator0ccupancyMap(statespace);
Assign the map to the validator.
statevalidator.Map = map;
Set the validation distance for the validator.

```
statevalidator.ValidationDistance = 0.01;
```

Update the state space bounds to be the same as the map limits.

```
statespace.StateBounds = [map.XWorldLimits;map.YWorldLimits;[-pi pi]];
```


## Plan Path

Create an RRT* path planner and allow further optimization.

```
planner = plannerRRTStar(statespace,statevalidator);
planner.ContinueAfterGoalReached = true;
```

Reduce the maximum number of iterations and increase the maximum connection distance.

```
planner.MaxIterations = 2500;
planner.MaxConnectionDistance = 0.3;
```

Define start and goal states for the path planner as $[x, y$, theta] vectors. $x$ and $y$ are the Cartesian coordinates, and theta is the orientation angle.

```
start = [2.5, 2.5, 0]; % [meters, meters, radians]
goal = [22.5, 8.75, 0];
```

Plan a path from the start state to the goal state. The plan function returns a navPath object.

```
rng(100,'twister') % repeatable result
[path,solutionInfo] = plan(planner,start,goal);
```


## Compute and Visualize Path Metrics

Create a path metrics object.

```
pathMetricsObj = pathmetrics(path,statevalidator);
```

Check path validity. The result is 1 (true) if the planned path is obstacle free. 0 (false) indicates an invalid path.

```
isPathValid(pathMetrics0bj)
ans = logical
    1
```

Calculate the minimum clearance of the path.

```
clearance(pathMetrics0bj)
ans = 1.4142
```

Evaluate the smoothness of the path. Values close to 0 indicate a smoother path. Straight-line paths return a value of 0 .

```
smoothness(pathMetrics0bj)
```

ans $=1.7318$

Visualize the minimum clearance of the path.

```
show(pathMetrics0bj)
legend('Planned Path','Minimum Clearance')
```



## Vehicle Path Planning and Metrics Computation in a 2-D Costmap Environment

Plan a vehicle path through a parking lot using the RRT* algorithm. Compute and visualize the smoothness, clearance, and validity of the planned path.

## Load and Assign Map to State Validator

Load a costmap of a parking lot. Plot the costmap to see the parking lot and the inflated areas that the vehicle should avoid.

```
load parkingLotCostmap.mat;
costmap = parkingLotCostmap;
plot(costmap)
xlabel('X (meters)')
ylabel('Y (meters)')
```



Create a stateSpaceDubins object and increase the minimum turing radius to 4 meters.

```
statespace = stateSpaceDubins;
statespace.MinTurningRadius = 4; % meters
```

Create a validatorVehicleCostmap object using the created state space.
statevalidator = validatorVehicleCostmap(statespace);
Assign the parking lot costmap to the state validator object.

```
statevalidator.Map = costmap;
```


## Plan Path

Define start and goal poses for the vehicle as $[x, y, \theta]$ vectors. World units for the $(x, y)$ locations are in meters. World units for the orientation angles $\theta$ are in degrees.

```
startPose = [5, 5, 90]; % [meters, meters, degrees]
goalPose = [40, 38, 180]; % [meters, meters, degrees]
```

Use a pathPlannerRRT (Automated Driving Toolbox) object and the plan (Automated Driving Toolbox) function to plan the vehicle path from the start pose to the goal pose.

```
planner = pathPlannerRRT(costmap);
refPath = plan(planner,startPose,goalPose);
```

Interpolate along the path at every one meter. Convert the orientation angles from degrees to radians.

```
poses = zeros(size(refPath.PathSegments,2)+1,3);
poses(1,:) = refPath.StartPose;
for i = 1:size(refPath.PathSegments,2)
    poses(i+1,:) = refPath.PathSegments(i).GoalPose;
end
poses(:,3) = deg2rad(poses(:,3));
```

Create a navPath object using the Dubins state space object and the states specified by poses.

```
path = navPath(statespace,poses);
```


## Compute and Visualize Path Metrics

Create a pathmetrics object.

```
pathMetricsObj = pathmetrics(path,statevalidator);
```

Check path validity. The result is 1 (true) if the planned path is obstacle free. 0 (false) indicates an invalid path.

```
isPathValid(pathMetrics0bj)
ans = logical
    1
```

Compute and visualize the minimum clearance of the path.

```
clearance(pathMetrics0bj)
ans = 0.5000
show(pathMetrics0bj)
legend('Inflated Areas','Planned Path','Minimum Clearance')
xlabel('X (meters)')
ylabel('Y (meters)')
```



Compute and visualize the smoothness of the path. Values close to 0 indicate a smoother path. Straight-line paths return a value of 0 .

```
smoothness(pathMetrics0bj)
ans = 0.0842
show(pathMetrics0bj,'Metrics',{'Smoothness'})
legend('Inflated Areas','Path Smoothness')
xlabel('X (meters)')
ylabel('Y (meters)')
```



Visualize the clearance for each state of the path.
show(pathMetrics0bj,'Metrics',\{'StatesClearance'\})
legend('Inflated Areas','Planned Path','Clearance of Path States')
xlabel('X (meters)')
ylabel('Y (meters)')


## Input Arguments

## pathMetrics0bj - Information for path metrics

pathmetrics object
Information for path metrics, specified as a pathmetrics object.

## See Also

Objects
pathmetrics

## Functions

clearance | show | smoothness
Introduced in R2019b

## show

Visualize path metrics in map environment

## Syntax

show(pathMetricsObj)
show(pathMetricsObj, Name, Value)
axHandle $=$ show(pathMetricsObj)

## Description

show(pathMetricsObj) plots the path in the map environment with the minimum clearance.
show(pathMetricsObj,Name, Value) specifies additional options using one or more name-value pair arguments.
axHandle = show(pathMetrics0bj) outputs the axes handle of the figure used to plot the path.

## Examples

## Compute Path Metrics

Compute smoothness, clearance, and validity of a planned path based on a set of poses and the associated map environment.

## Load and Assign Map to State Validator

Create an occupancy map from an example map and set the map resolution.

```
load exampleMaps.mat; % simpleMap
mapResolution = 1; % cells/meter
map = occupancyMap(simpleMap,mapResolution);
```

Create a Dubins state space.

```
statespace = stateSpaceDubins;
```

Create a state validator based on occupancy map to store the parameters and states in the Dubins state space.

```
statevalidator = validatorOccupancyMap(statespace);
```

Assign the map to the validator.

```
statevalidator.Map = map;
```

Set the validation distance for the validator.

```
statevalidator.ValidationDistance = 0.01;
```

Update the state space bounds to be the same as the map limits.

```
statespace.StateBounds = [map.XWorldLimits;map.YWorldLimits;[-pi pi]];
Plan Path
```

Create an RRT* path planner and allow further optimization.

```
planner = plannerRRTStar(statespace,statevalidator);
```

planner.ContinueAfterGoalReached = true;

Reduce the maximum number of iterations and increase the maximum connection distance.

```
planner.MaxIterations = 2500;
planner.MaxConnectionDistance = 0.3;
```

Define start and goal states for the path planner as [ $x, y$, theta] vectors. $x$ and $y$ are the Cartesian coordinates, and theta is the orientation angle.

```
start = [2.5, 2.5, 0]; % [meters, meters, radians]
goal = [22.5, 8.75, 0];
```

Plan a path from the start state to the goal state. The plan function returns a navPath object.

```
rng(100,'twister') % repeatable result
[path,solutionInfo] = plan(planner,start,goal);
```


## Compute and Visualize Path Metrics

Create a path metrics object.

```
pathMetricsObj = pathmetrics(path,statevalidator);
```

Check path validity. The result is 1 (true) if the planned path is obstacle free. 0 (false) indicates an invalid path.

```
isPathValid(pathMetrics0bj)
ans = logical
    1
```

Calculate the minimum clearance of the path.

```
clearance(pathMetrics0bj)
ans = 1.4142
```

Evaluate the smoothness of the path. Values close to 0 indicate a smoother path. Straight-line paths return a value of 0 .

```
smoothness(pathMetrics0bj)
ans = 1.7318
```

Visualize the minimum clearance of the path.
show(pathMetrics0bj)
legend('Planned Path','Minimum Clearance')


## Vehicle Path Planning and Metrics Computation in a 2-D Costmap Environment

Plan a vehicle path through a parking lot using the RRT* algorithm. Compute and visualize the smoothness, clearance, and validity of the planned path.

## Load and Assign Map to State Validator

Load a costmap of a parking lot. Plot the costmap to see the parking lot and the inflated areas that the vehicle should avoid.

```
load parkingLotCostmap.mat;
costmap = parkingLotCostmap;
plot(costmap)
xlabel('X (meters)')
ylabel('Y (meters)')
```



Create a stateSpaceDubins object and increase the minimum turing radius to 4 meters.

```
statespace = stateSpaceDubins;
statespace.MinTurningRadius = 4; % meters
```

Create a validatorVehicleCostmap object using the created state space.
statevalidator = validatorVehicleCostmap(statespace);
Assign the parking lot costmap to the state validator object.

```
statevalidator.Map = costmap;
```


## Plan Path

Define start and goal poses for the vehicle as $[x, y, \theta]$ vectors. World units for the $(x, y)$ locations are in meters. World units for the orientation angles $\theta$ are in degrees.

```
startPose = [5, 5, 90]; % [meters, meters, degrees]
goalPose = [40, 38, 180]; % [meters, meters, degrees]
```

Use a pathPlannerRRT (Automated Driving Toolbox) object and the plan (Automated Driving Toolbox) function to plan the vehicle path from the start pose to the goal pose.

```
planner = pathPlannerRRT(costmap);
refPath = plan(planner,startPose,goalPose);
```

Interpolate along the path at every one meter. Convert the orientation angles from degrees to radians.

```
poses = zeros(size(refPath.PathSegments,2)+1,3);
poses(1,:) = refPath.StartPose;
for i = 1:size(refPath.PathSegments,2)
    poses(i+1,:) = refPath.PathSegments(i).GoalPose;
end
poses(:,3) = deg2rad(poses(:,3));
```

Create a navPath object using the Dubins state space object and the states specified by poses.

```
path = navPath(statespace,poses);
```


## Compute and Visualize Path Metrics

Create a pathmetrics object.

```
pathMetricsObj = pathmetrics(path,statevalidator);
```

Check path validity. The result is 1 (true) if the planned path is obstacle free. 0 (false) indicates an invalid path.

```
isPathValid(pathMetrics0bj)
ans = logical
    1
```

Compute and visualize the minimum clearance of the path.

```
clearance(pathMetrics0bj)
ans = 0.5000
show(pathMetrics0bj)
legend('Inflated Areas','Planned Path','Minimum Clearance')
xlabel('X (meters)')
ylabel('Y (meters)')
```



Compute and visualize the smoothness of the path. Values close to 0 indicate a smoother path. Straight-line paths return a value of 0 .

```
smoothness(pathMetricsObj)
ans = 0.0842
show(pathMetrics0bj,'Metrics',{'Smoothness'})
legend('Inflated Areas','Path Smoothness')
xlabel('X (meters)')
ylabel('Y (meters)')
```



Visualize the clearance for each state of the path.
show(pathMetrics0bj,'Metrics',\{'StatesClearance'\})
legend('Inflated Areas','Planned Path','Clearance of Path States')
xlabel('X (meters)')
ylabel('Y (meters)')


## Input Arguments

pathMetrics0bj - Information for path metrics
pathmetrics object
Information for path metrics, specified as a pathmetrics object.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: 'Parent', axHandle

## Parent - Axes used to plot path

Axes object | UIAxes object
Axes used to plot path, specified as the comma-separated pair consisting of 'Parent ' and either an axes or uiaxes object. If you do not specify Parent, a new figure is created.

Example: show(pathMetrics0bj, 'Parent', axHandle)

## Metrics - Display metrics option

cell array of strings

Display metrics option, specified as the comma-separated pair consisting of 'Metrics' and a cell array with any combination of these values:

- 'MinClearance' - Display minimum clearance of path.
- 'StatesClearance' - Display clearance of path states.
- 'Smoothness' - Display path smoothness.

Example: show(pathMetrics0bj,'Metrics',\{'Smoothness','StatesClearance'\})
Data Types: cell

## Output Arguments

## axHandle - Axes used to plot path

Axes object | UIAxes object
Axes used to plot path, returned as either an axes or uiaxes object.

## See Also

```
Objects
pathmetrics
Functions
clearance|isPathValid|smoothness
```

Introduced in R2019b

## smoothness

Smoothness of path

## Syntax

smoothness (pathMetrics0bj)
smoothness(pathMetrics0bj, 'Type','segments')

## Description

smoothness(pathMetricsObj) evaluates the smoothness of the planned path. Values close to 0 indicate a smoother path. Straight-line paths return a value of 0 .
smoothness(pathMetrics0bj,'Type','segments') returns individual smoothness calculations between each set of three poses on the path, in the form of a ( $n-2$ )-element vector, where $n$ is the number of poses.

## Examples

## Compute Path Metrics

Compute smoothness, clearance, and validity of a planned path based on a set of poses and the associated map environment.

## Load and Assign Map to State Validator

Create an occupancy map from an example map and set the map resolution.

```
load exampleMaps.mat; % simpleMap
mapResolution = 1; % cells/meter
map = occupancyMap(simpleMap,mapResolution);
```

Create a Dubins state space.

```
statespace = stateSpaceDubins;
```

Create a state validator based on occupancy map to store the parameters and states in the Dubins state space.

```
statevalidator = validatorOccupancyMap(statespace);
```

Assign the map to the validator.

```
statevalidator.Map = map;
```

Set the validation distance for the validator.

```
statevalidator.ValidationDistance = 0.01;
```

Update the state space bounds to be the same as the map limits.

```
statespace.StateBounds = [map.XWorldLimits;map.YWorldLimits;[-pi pi]];
Plan Path
```

Create an RRT* path planner and allow further optimization.

```
planner = plannerRRTStar(statespace,statevalidator);
```

planner.ContinueAfterGoalReached = true;

Reduce the maximum number of iterations and increase the maximum connection distance.

```
planner.MaxIterations = 2500;
planner.MaxConnectionDistance = 0.3;
```

Define start and goal states for the path planner as $[x, y$, theta] vectors. $x$ and $y$ are the Cartesian coordinates, and theta is the orientation angle.

```
start = [2.5, 2.5, 0]; % [meters, meters, radians]
goal = [22.5, 8.75, 0];
```

Plan a path from the start state to the goal state. The plan function returns a navPath object.

```
rng(100,'twister') % repeatable result
[path,solutionInfo] = plan(planner,start,goal);
```


## Compute and Visualize Path Metrics

Create a path metrics object.

```
pathMetricsObj = pathmetrics(path,statevalidator);
```

Check path validity. The result is 1 (true) if the planned path is obstacle free. 0 (false) indicates an invalid path.

```
isPathValid(pathMetrics0bj)
ans = logical
    1
```

Calculate the minimum clearance of the path.

```
clearance(pathMetrics0bj)
ans = 1.4142
```

Evaluate the smoothness of the path. Values close to 0 indicate a smoother path. Straight-line paths return a value of 0 .

```
smoothness(pathMetrics0bj)
ans = 1.7318
```

Visualize the minimum clearance of the path.
show(pathMetrics0bj)
legend('Planned Path','Minimum Clearance')


## Vehicle Path Planning and Metrics Computation in a 2-D Costmap Environment

Plan a vehicle path through a parking lot using the RRT* algorithm. Compute and visualize the smoothness, clearance, and validity of the planned path.

## Load and Assign Map to State Validator

Load a costmap of a parking lot. Plot the costmap to see the parking lot and the inflated areas that the vehicle should avoid.

```
load parkingLotCostmap.mat;
costmap = parkingLotCostmap;
plot(costmap)
xlabel('X (meters)')
ylabel('Y (meters)')
```



Create a stateSpaceDubins object and increase the minimum turing radius to 4 meters.

```
statespace = stateSpaceDubins;
```

statespace.MinTurningRadius $=4$; \% meters

Create a validatorVehicleCostmap object using the created state space.
statevalidator = validatorVehicleCostmap(statespace);
Assign the parking lot costmap to the state validator object.

```
statevalidator.Map = costmap;
```


## Plan Path

Define start and goal poses for the vehicle as $[x, y, \theta]$ vectors. World units for the $(x, y)$ locations are in meters. World units for the orientation angles $\theta$ are in degrees.

```
startPose = [5, 5, 90]; % [meters, meters, degrees]
goalPose = [40, 38, 180]; % [meters, meters, degrees]
```

Use a pathPlannerRRT (Automated Driving Toolbox) object and the plan (Automated Driving Toolbox) function to plan the vehicle path from the start pose to the goal pose.

```
planner = pathPlannerRRT(costmap);
refPath = plan(planner,startPose,goalPose);
```

Interpolate along the path at every one meter. Convert the orientation angles from degrees to radians.

```
poses = zeros(size(refPath.PathSegments,2)+1,3);
poses(1,:) = refPath.StartPose;
for i = 1:size(refPath.PathSegments,2)
    poses(i+1,:) = refPath.PathSegments(i).GoalPose;
end
poses(:,3) = deg2rad(poses(:,3));
```

Create a navPath object using the Dubins state space object and the states specified by poses.

```
path = navPath(statespace,poses);
```


## Compute and Visualize Path Metrics

Create a pathmetrics object.

```
pathMetricsObj = pathmetrics(path,statevalidator);
```

Check path validity. The result is 1 ( true ) if the planned path is obstacle free. 0 (false) indicates an invalid path.

```
isPathValid(pathMetrics0bj)
ans = logical
    1
```

Compute and visualize the minimum clearance of the path.

```
clearance(pathMetrics0bj)
ans = 0.5000
show(pathMetrics0bj)
legend('Inflated Areas','Planned Path','Minimum Clearance')
xlabel('X (meters)')
ylabel('Y (meters)')
```



Compute and visualize the smoothness of the path. Values close to 0 indicate a smoother path. Straight-line paths return a value of 0 .

```
smoothness(pathMetrics0bj)
ans = 0.0842
show(pathMetrics0bj,'Metrics',{'Smoothness'})
legend('Inflated Areas','Path Smoothness')
xlabel('X (meters)')
ylabel('Y (meters)')
```



Visualize the clearance for each state of the path.
show(pathMetrics0bj,'Metrics',\{'StatesClearance'\})
legend('Inflated Areas','Planned Path','Clearance of Path States')
xlabel('X (meters)')
ylabel('Y (meters)')


## Input Arguments

## pathMetricsObj - Information for path metrics

pathmetrics object
Information for path metrics, specified as a pathmetrics object.

## References

[1] Lindemann, Stephen R., and Steven M. LaValle. "Simple and efficient algorithms for computing smooth, collision-free feedback laws over given cell decompositions." The International Journal of Robotics Research 28, no. 5. 2009, pp. 600-621.

## See Also

## Objects

pathmetrics
Functions
clearance |isPathValid| show

Introduced in R2019b

## plannerAStarGrid

A* path planner for grid map

## Description

The plannerAStarGrid object creates an A* path planner. The planner performs an A* search on an occupancy map and finds shortest obstacle-free path between the specified start and goal grid locations as determined by heuristic cost.

## Creation

## Syntax

```
planner = plannerAStarGrid
planner = plannerAStarGrid(map)
planner = plannerAStarGrid(
,Name,Value)
```


## Description

planner = plannerAStarGrid creates a plannerAStarGrid object with a
binary0ccupancyMap object using a width and height of 10 meters and grid resolution of 1 cell per meter.
planner = plannerAStarGrid(map) creates a plannerAStarGrid object using the specified map object map. Specify map as either a binaryOccupancyMap or occupancyMap object. The map input sets the value of the Map property.
planner = plannerAStarGrid( $\qquad$ ,Name, Value) sets properties using one or more namevalue pairs. Unspecified properties have default values. Enclose each property name in quotes.

For example, plannerAStarGrid(map, 'GCost', 'Manhattan') creates an A* path planner object using the Manhattan cost function.

## Properties

## Map - Map representation

binary0ccupancyMap object (default) | occupancyMap object
Map representation, specified as either a binary0ccupancyMap or occupancyMap object. This object represents the environment of the robot as an occupancy grid. The value of each grid cell indicates the occupancy of the associated location in the map.
Example: planner.Map = binary0ccupancyMap(zeros(50,50));

## GCost - General cost of moving between any two points in grid

'Euclidean' (default)|'Chebyshev' | 'EulideanSquared'|'Manhattan'

The general cost of moving between any two points in a grid, specified as one of the following predefined cost functions 'Chebyshev', 'Euclidean', 'EulideanSquared', or 'Manhattan'.

Note You can either use the predefined cost functions or a custom cost function. To use a custom cost function, see GCostFcn property.

Example: planner = plannerAStarGrid(map,'GCost','Manhattan');
Example: planner.GCost = 'Chebyshev';
Data Types: string|char

## GCostFen - Custom GCost function

function handle
Custom GCost function, specified as a function handle. The function handle must accept two pose inputs as a [row column] vectors and return a scalar of type double.

Note You can either use the predefined cost functions or a custom cost function. To use the predefined cost functions, see GCost property.

Example: planner = plannerAStarGrid(map,'GCostFcn',@(pose1, pose2)sum(abs(pose1pose2),2));

Example: planner.GCostFcn = @(pose1,pose2)sum(abs(pose1-pose2),2);
Data Types: function_handle

## HCost - Heuristic cost between point and goal in grid

'Euclidean' (default)|'Chebyshev' | 'EulideanSquared ' | 'Manhattan'
The heuristic cost between a point and the goal in a grid, specified as one of the following predefined cost functions 'Chebyshev', 'Euclidean', 'EulideanSquared', or 'Manhattan'.

Note You can either use the predefined cost functions or a custom cost function. To use a custom cost function, see HCostFcn property.

Example: planner = plannerAStarGrid(map,'HCost','Manhattan');
Example: planner.HCost = 'Chebyshev';
Data Types: string | char

## HCostFen - Custom HCost function

function handle
Custom HCost function, specified as a function handle. The function handle must accept two pose inputs as a [row column] vectors and return a scalar of type double.

Note You can either use the predefined cost functions or a custom cost function. To use the predefined cost functions, see HCost property.

Example: planner = plannerAStarGrid(map,'HCostFcn',@(pose1,pose2)sum(abs(pose1pose2),2) ) ;

Example: planner.HCostFcn = @(pose1,pose2) sum(abs(pose1-pose2), 2);
Data Types: function_handle

## TieBreaker - Toggle tiebreaker mode

'off' (default)|'on'
Toggle tiebreaker mode, specified as either 'on' or 'off'.
When you enable the TieBreaker property, the A* path planner chooses between multiple paths of the same length by adjusting the heuristic cost value.
Example: planner = plannerAStarGrid(map,'TieBreaker', 'on');
Example: planner.TieBreaker = 'off';
Data Types: string|char

## DiagonalSearch - Toggle diagonal search mode

'on' (default)|'off'
Toggle diagonal search mode, specified as either 'on' or 'off'.
When you set this property to ' on ' , the A* path planner searches in diagonal direction along with the other four directions of the grid. When you set this property to ' off' , the A* path planner searches only in the four directions of the grid.

Data Types: char | string

## Object Functions

plan Find shortest obstacle-free path between two points
show Plot and visualize A* explored nodes and planned path

## Examples

## Plan Obstacle-Free Path in Grid Map Using A-Star Path Planner

Plan the shortest collision-free path through an obstacle grid map using the A* path planning algorithm.

Generate a binary0ccupancyMap object with randomly scattered obstacles using the mapClutter function.

```
rng('default');
map = mapClutter;
```

Use the map to create a plannerAStarGrid object.
planner = plannerAStarGrid(map);
Define the start and goal points.
start = [2 3];
goal $=$ [248 248];
Plan a path from the start point to the goal point.
plan(planner,start,goal);
Visualize the path and the explored nodes using the show object function.
show(planner)


## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

binary0ccupancyMap | occupancyMap | plannerRRT | plannerRRTStar | plannerHybridAStar

Introduced in R2020b

## plan

Find shortest obstacle-free path between two points

## Syntax

```
path = plan(planner,start,goal)
path = plan(planner,start,goal,'world')
[path,debugInfo] = plan(
```

$\qquad$

``` )
```


## Description

path $=p l a n(p l a n n e r, s t a r t, g o a l)$ finds the shortest obstacle-free path, path, between a specified start point, start, and goal point, goal, specified as [row column] in grid frame with origin at top-left corner, using the specified $\mathrm{A}^{*}$ path planner planner.
path = plan(planner,start,goal,'world') finds the shortest obstacle-free path, path, between a specified start point, start, and goal point, goal, specified as [ $x y$ ] in world coordinate frame with origin at bottom-left corner, using the specified A* path planner planner.
[path, debugInfo] = plan( $\qquad$ ) also returns debugInfo that contains the path cost, number of nodes explored, and GCost for each explored node.

## Examples

## Plan Obstacle-Free Path in Grid Map Using A-Star Path Planner

Plan the shortest collision-free path through an obstacle grid map using the A* path planning algorithm.

Generate a binary0ccupancyMap object with randomly scattered obstacles using the mapClutter function.

```
rng('default');
map = mapClutter;
```

Use the map to create a plannerAStarGrid object.
planner = plannerAStarGrid(map);
Define the start and goal points.

```
start = [2 3];
goal = [248 248];
```

Plan a path from the start point to the goal point.

```
plan(planner,start,goal);
```

Visualize the path and the explored nodes using the show object function.

```
show(planner)
```



## Input Arguments

planner - A* path planner for grid map
plannerAStarGrid object
A* path planner for a grid map, specified as a plannerAStarGrid object.
start - Start position in grid or world
two-element vector
Start position in the grid or world, specified as a two-element vector of the form [row column], or [ $x$ $y]$. The location is in grid positions or world coordinates based on syntax.

Example: [2 3]
Data Types: double

## goal - Goal position in grid or world

two-element vector

Goal position in the grid or world, specified as a two-element vector of the form [row column], or [x $y]$. The location is in grid positions or world coordinates based on syntax.
Example: [28 46]
Data Types: double

## Output Arguments

## path - Shortest obstacle-free path

n-by-2 matrix

Shortest obstacle-free path, returned as an $n$-by-2 matrix. $n$ is the number of waypoints in the path. Each row represents the [row column], or $[x y$ ] location of a waypoint along the solved path from the start location to the goal. The location is in grid positions or world coordinates based on syntax.
Data Types: double
debugInfo - Debugging information for path result
structure
Debugging information for the path result, returned as a structure with these fields:

- PathCost - Cost of the path
- NumNodesExplored - Number of nodes explored
- GCostMatrix - GCost for each explored node

Data Types: struct

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.

## See Also

plannerAStarGrid|show
Introduced in R2020b

## show

Plot and visualize A* explored nodes and planned path

## Syntax

```
show(planner)
axHandle = show(planner)
[___] = show( ___ ,Name,Value)
```


## Description

show(planner) plots and visualizes the A* explored nodes and the planned path in the associated map.
axHandle $=$ show(planner) returns the axes handle of the figure used to plot the path.
[___] = show(__ ,Name,Value) specifies options using one or more name-value pair arguments in addition to any of the arguments from previous syntaxes. Enclose argument name inside single quotes (' ').

For example, 'ExploredNodes', 'off' plots and visualizes the planned path without displaying the explored nodes.

## Examples

## Plan Obstacle-Free Path in Grid Map Using A-Star Path Planner

Plan the shortest collision-free path through an obstacle grid map using the A* path planning algorithm.

Generate a binary0ccupancyMap object with randomly scattered obstacles using the mapClutter function.

```
rng('default');
map = mapClutter;
```

Use the map to create a plannerAStarGrid object.

```
planner = plannerAStarGrid(map);
```

Define the start and goal points.

```
start = [2 3];
goal = [248 248];
```

Plan a path from the start point to the goal point.
plan(planner,start,goal);
Visualize the path and the explored nodes using the show object function.
show(planner)


## Input Arguments

## planner - A* path planner for grid map

plannerAStarGrid object
A* path planner for a grid map, specified as a plannerAStarGrid object.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: 'ExploredNodes ', 'off' plots and visualizes the planned path without displaying the explored nodes.

## Parent - Axes used to plot path

Axes object | UIAxes object
Axes used to plot path, specified as the comma-separated pair consisting of 'Parent' and either an Axes Properties or UIAxes Properties object. If you do not specify Parent, a new figure is created.

Example: 'Parent' , axHandle

## ExploredNodes - Display explored nodes

'on' (default) |'off'
Display the explored nodes, specified as the comma-separated pair consisting of 'ExploredNodes ' and either 'on' or 'off'.
Example: 'ExploredNodes','off'
Data Types: string | char

## Output Arguments

## axHandle - Axes used to plot path

Axes object | UIAxes object
Axes used to plot the path, returned as an Axes Properties or UIAxes Properties object.

## See Also

plannerAStarGrid|plan
Introduced in R2020b

## plannerBenchmark

Benchmark path planners using generated metrics

## Description

plannerBenchmark object benchmarks the 2-D path planners by running them on a specified environment with specified start and goal poses.

The plannerBenchmark object calculates the following metrics:

- clearance - Minimum distance to obstacles in the environment
- executionTime - Time taken by plan function to execute
- initializationTime - Time taken by initialization function to execute
- isPathValid - If true represent the path exists and is collision free
- pathLength - Length of the generated path
- smoothness - Smoothness of the path for all poses

The metrics like executionTime and initializationTime are calculated during the execution of planners. The metrics like clearance, isPathValid, pathLength, and smoothness are calculated from the resulting path outputs after executing planners. Calculated metrics are statistically summarized as a table and can be visualized as plots.

## Creation

## Syntax

plannerBM = plannerBenchmark(environment,start,goal)

## Description

plannerBM = plannerBenchmark(environment,start,goal) creates a plannerBenchmark object with the specified environment, start and goal poses. The inputs environment, start, and goal sets the Environment, Start, and Goal properties, respectively.

## Properties

## Environment - Environment for benchmarking path planners

occupancyMap object | binary0ccupancyMap object | validatorOccupancyMap object
Environment for benchmarking path planners, specified as occupancyMap, binary0ccupancyMap, or validatorOccupancyMap object.

## Start - Start pose of path for all planners

vector of the form $\left.\left[\begin{array}{ll}x & y\end{array}\right] \right\rvert\,$ vector of the form [ $x$ y theta]
Start pose of path for all planners, specified as a vector of the form [xy] or $\left[\begin{array}{ll}x & y \\ \text { theta }\end{array}\right]$.

Data Types: single | double

## Goal - Goal pose of path for all planners

vector of the form [ $\left.\begin{array}{ll}x & y\end{array}\right] \mid$ vector of the form [ $x$ y theta]
Goal pose of path for all planners, specified as a vector of the form [ $\left.\begin{array}{ll}x & y\end{array}\right]$ or $\left[\begin{array}{ll}x & y \\ \text { theta }\end{array}\right]$.
Data Types: single | double

## PlannerOutput - Output of planners after execution

 structureThis property is read-only.
Output of planners after execution, returned as a structure that contains the initialization function output and plan function output for all planners. The fields of the structure are named by planner name specified in addPlanner function.

Each structure contains an initialization output and a plan function output. The plan function output is further a structure containing plan function output for each run of the planner.
Data Types: struct

## Object Functions

addPlanner Add path planner for benchmarking
copy Create deep copy of plannerBenchmark object
metric Return path planner metrics
runPlanner Run path planners
show Visualize path planner metrics

## Examples

## Benchmark 2-D Path Planners

Create an occupancy map from an example map.

```
load("exampleMaps.mat","simpleMap");
map = occupancyMap(simpleMap);
```

Create a state validator with stateSpaceSE2 using the map.
sv = validatorOccupancyMap(stateSpaceSE2,Map=map);
Specify the start and goal states.

```
start = [5 8 pi/2];
```

goal = [7 18 pi/2];

Create a plannerBenchmark object.
pbo = plannerBenchmark(sv,start,goal);
Define the function handles for the initialization functions of the planners.

```
plannerHAFcn = @(sv)plannerHybridAStar(sv);
plannerRRTSFcn = @(sv)plannerRRTStar(sv.StateSpace,sv);
```

Define the function handle for the plan function, which is common for both planners.

```
plnFcn = @(initOut,s,g)plan(initOut,s,g);
```

Add the path planners for benchmarking.

```
addPlanner(pbo,plnFcn,plannerHAFcn);
addPlanner(pbo,plnFcn,plannerRRTSFcn,PlannerName="ppRRTStar");
```

Set the rng for repetitive results.

```
rng('default')
```

Run the path planners for the number of times specified in runCount to collect metrics.

```
runCount = 5;
runPlanner(pbo,runCount)
```

Initializing plannerHAFcn_plnFcn ...
Done.
Planning with plannerHAFcn_plnFcn for start pose (5 81.5708 ) and goal pose ( 718 1.5708) at run
Planning with plannerHAFcn_plnFcn for start pose (5 81.5708 ) and goal pose ( 718 1.5708) at run
Planning with plannerHAFcn_plnFcn for start pose (5 81.5708 ) and goal pose ( 718 1.5708) at run
Planning with plannerHAFcn_plnFcn for start pose (5 81.5708 ) and goal pose ( 7181.5708 ) at run
Planning with plannerHAFcn_plnFcn for start pose (5 81.5708 ) and goal pose (7 18 1.5708) at run
Initializing ppRRTStar ...
Done.
Planning with ppRRTStar for start pose (5 81.5708 ) and goal pose ( 7181.5708 ) at run count 1.
Planning with ppRRTStar for start pose (5 81.5708 ) and goal pose ( 7181.5708 ) at run count 2.
Planning with ppRRTStar for start pose ( 581.5708 ) and goal pose ( 7181.5708 ) at run count 3.
Planning with ppRRTStar for start pose ( 581.5708 ) and goal pose ( 7181.5708 ) at run count 4.
Planning with ppRRTStar for start pose (5 8 1.5708) and goal pose ( 7181.5708 ) at run count 5.

Access path length metric for all the runs on the environment.

```
[pLenSummary,pLenData] = metric(pbo,"pathLength")
```

pLenSummary=2×4 table

| Mean |  | Median |  | StdDev |  |
| ---: | ---: | ---: | ---: | ---: | ---: |


| pLenData=2×5 table |  |  |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  | Run1 |  | Run2 |  | Run3 |  | Run4 |

Visualize all the metrics.
show (pbo)


Closely inspect the clearance metric.
figure
show(pbo,"clearance")


See Also
Objects
occupancyMap | binary0ccupancyMap | validator0ccupancyMap
Functions
addPlanner | copy |metric|runPlanner | show

Introduced in R2022a

## plannerBiRRT

Create bidirectional RRT planner for geometric planning

## Description

The plannerBiRRT object is a single-query planner that uses the bidirectional rapidly exploring random tree (RRT) algorithm with an optional connect heuristic for increased speed.

The bidirectional RRT planner creates one tree with a root node at the specified start state and another tree with a root node at the specified goal state. To extend each tree, the planner generates a random state and, if valid, takes a step from the nearest node based on the MaxConnectionDistance property. The start and goal trees alternate this extension process until both trees are connected. If the EnableConnectHeuristic property is enabled, the extension process ignores the MaxConnectionDistance property. Invalid states or connections that collide with the environment are not added to the tree.

## Creation

## Syntax

planner = plannerBiRRT(stateSpace,stateVal)

## Description

planner = plannerBiRRT(stateSpace, stateVal) creates a bidirectional RRT planner from a state space object, stateSpace, and a state validator object, stateVal. The state space of stateVal must be the same as stateSpace. The stateSpace and stateVal arguments also set the StateSpace and StateValidator properties, respectively, of the planner.

## Properties

## StateSpace - State space for planner

state space object
State space for the planner, specified as a state space object. You can use state space objects such as stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp. You can also customize a state space object using the nav.StateSpace class.

## StateValidator - State validator for planner <br> state validator object

State validator for the planner, specified as a state validator object. You can use state validator objects such as validator0ccupancyMap and validatorVehicleCostmap.

## MaxConnectionDistance - Maximum length between planned configurations <br> 0.1 (default) | positive scalar

Maximum length between planned configurations, specified as a positive scalar.

If the EnableConnectHeuristic property is set to true, the object ignores this distance when connecting the two trees during the connect stage.
Data Types: single | double
MaxIterations - Maximum number of iterations
1e4 (default) | positive integer
Maximum number of iterations, specified as a positive integer.
Data Types: single | double
MaxNumTreeNodes - Maximum number of nodes in search tree
le4 (default) | positive integer
Maximum number of nodes in the search tree, specified as a positive integer.
Data Types: single | double
EnableConnectHeuristic - Directly join trees during connect phase
false or 0 (default) | true or 1
Directly join trees during the connect phase of the planner, specified as a logical 0 (false) or 1 (true).

Setting this property to true causes the object to ignore the MaxConnectionDistance property when attempting to connect the two trees together.
Data Types: logical

## Object Functions

plan Plan path between two states
copy Create deep copy of planner object

## Examples

## Plan Path Between Two States Using Bidirectional RRT

Use the plannerBiRRT object to plan a path between two states in an environment with obstacles. Visualize the planned path with interpolated states.

Create a state space.
ss = stateSpaceSE2;
Create an occupancyMap-based state validator using the created state space.
sv = validatorOccupancyMap(ss);
Create an occupancy map from an example map and set map resolution as 10 cells per meter.
load exampleMaps
map = occupancyMap(ternaryMap,10);
sv.Map = map;
Set the validation distance for the validator.
sv.ValidationDistance $=0.01$;
Update the state space bounds to be the same as the map limits.
ss.StateBounds = [map.XWorldLimits; map.YWorldLimits; [-pi pi]];
Create the path planner and increase the maximum connection distance.
planner = plannerBiRRT(ss,sv);
planner.MaxConnectionDistance = 0.3;
Specify the start and goal states.

```
start = [20 10 0];
```

goal = [40 40 0];

Plan a path. Due to the randomness of the RRT algorithm, set the rng seed for repeatability.

```
rng(100,'twister')
[pthObj,solnInfo] = plan(planner,start,goal);
```

Display the number of iterations taken for the tree to converge.

```
fprintf('Number of iterations: %d\n',solnInfo.NumIterations)
Number of iterations: 346
```

Visualize the results.

```
show(map)
hold on
plot(solnInfo.StartTreeData(:,1),solnInfo.StartTreeData(:,2),'.-','color','b') % Start tree expa
plot(solnInfo.GoalTreeData(:,1),solnInfo.GoalTreeData(:,2),'.-','color','g') % Goal tree expansi`
plot(pthObj.States(:,1),pthObj.States(:,2),'r-','LineWidth',2) % draw path
hold off
```



Replan the path with the EnableConnectHeuristic property set to true.
planner.EnableConnectHeuristic = true;
[pthObj,solnInfo] = plan(planner,start,goal);
Display the number of iterations taken for the tree to converge. Observe that the planner requires significantly fewer iterations compared to when the EnableConnectHeuristic property is set to false.
fprintf('Number of iterations: \%d\n',solnInfo.NumIterations)
Number of iterations: 135
Visualize the results.
figure
show(map)
hold on
plot(solnInfo.StartTreeData(:,1),solnInfo.StartTreeData(:,2),'.-','color','b') \% Start tree expa plot(solnInfo.GoalTreeData(:,1),solnInfo.GoalTreeData(:,2),'.-','color','g') \% Goal tree expansi plot(pthObj.States(:,1),pthObj.States(:,2),'r-','LineWidth',2) \% draw path


## References

[1] Kuffner, J. J., and S. M. LaValle. "RRT-Connect: An Efficient Approach to Single-Query Path Planning." In Proceedings 2000 ICRA. Millennium Conference. IEEE International Conference on Robotics and Automation. Symposia Proceedings (Cat. No.00CH37065), 2:995-1001. San Francisco, CA, USA: IEEE, 2000. https://doi:10.1109/ROBOT.2000.844730.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

Objects
plannerRRT|plannerRRTStar

## Functions <br> plan | copy

Introduced in R2021a

## copy

Create deep copy of planner object

## Syntax

plannerCopy $=\operatorname{copy}($ planner $)$

## Description

plannerCopy $=$ copy (planner) creates a deep copy of the planner object with the same properties.

## Examples

## Create Copy of plannerBiRRT Object

Create an occupancy map from an example map and set the map resolution as 10 cells/meter.

```
map = load("exampleMaps.mat").simpleMap;
map = occupancyMap(map,10);
```

Create a state space and update the state space bounds to be the same as the map limits.

```
ss = stateSpaceSE2;
ss.StateBounds = [map.XWorldLimits; map.YWorldLimits; [-pi pi]];
```

Create a state validator with stateSpaceSE2 using the map and set the validation distance.

```
sv = validatorOccupancyMap(ss,Map=map);
sv.ValidationDistance = 0.01;
Create a plannerBiRRT object.
planner = plannerBiRRT(ss,sv)
planner =
    plannerBiRRT with properties:
                    StateSpace: [1x1 stateSpaceSE2]
            StateValidator: [1x1 validatorOccupancyMap]
            MaxNumTreeNodes: 10000
                MaxIterations: 10000
            MaxConnectionDistance: 0.1000
        EnableConnectHeuristic: 0
```

Create a copy of the plannerBiRRT object.
plannerNew $=$ copy (planner)
plannerNew =
plannerBiRRT with properties:

```
            StateSpace: [1x1 stateSpaceSE2]
        StateValidator: [1x1 validatorOccupancyMap]
MaxNumTreeNodes: 10000
    MaxIterations: 10000
MaxConnectionDistance: 0.1000
EnableConnectHeuristic: 0
```


## Input Arguments

```
planner - Path planner
```

plannerBiRRT object
Path planner, specified as a plannerBiRRT object.

## Output Arguments

plannerCopy - Copy of path planner
plannerBiRRT object
Copy of path planner, returned as a plannerBiRRT object.

## See Also

Objects
plannerBiRRT
Functions
plan
Introduced in R2021a

## plan

Plan path between two states

## Syntax

```
path = plan(planner,startState,goalState)
[path,solnInfo] = plan(planner,startState,goalState)
```


## Description

path $=$ plan(planner,startState, goalState) returns a bidirectional rapidly exploring random tree (RRT) path from the start state to the goal state as a navPath object.
[path,solnInfo] = plan(planner,startState, goalState) also returns the solution information from path planning.

## Examples

## Plan Path Between Two States Using Bidirectional RRT

Use the plannerBiRRT object to plan a path between two states in an environment with obstacles. Visualize the planned path with interpolated states.

Create a state space.
ss = stateSpaceSE2;
Create an occupancyMap-based state validator using the created state space.
sv = validatorOccupancyMap(ss);
Create an occupancy map from an example map and set map resolution as 10 cells per meter.
load exampleMaps
map = occupancyMap(ternaryMap,10);
sv.Map = map;
Set the validation distance for the validator.
sv.ValidationDistance = 0.01;
Update the state space bounds to be the same as the map limits.

```
ss.StateBounds = [map.XWorldLimits; map.YWorldLimits; [-pi pi]];
```

Create the path planner and increase the maximum connection distance.
planner = plannerBiRRT(ss,sv);
planner.MaxConnectionDistance = 0.3;
Specify the start and goal states.

```
start = [20 10 0];
goal = [40 40 0];
```

Plan a path. Due to the randomness of the RRT algorithm, set the rng seed for repeatability.

```
rng(100,'twister')
[pthObj,solnInfo] = plan(planner,start,goal);
```

Display the number of iterations taken for the tree to converge.

```
fprintf('Number of iterations: %d\n',solnInfo.NumIterations)
```

Number of iterations: 346
Visualize the results.
show(map)
hold on
plot(solnInfo.StartTreeData(:,1),solnInfo.StartTreeData(:,2),'.-','color','b') \% Start tree expa plot(solnInfo.GoalTreeData(:,1),solnInfo.GoalTreeData(:,2),'.-','color','g') \% Goal tree expansi plot(pth0bj.States(:,1),pth0bj.States(:,2),'r-','LineWidth',2) \% draw path hold off


Replan the path with the EnableConnectHeuristic property set to true.

```
planner.EnableConnectHeuristic = true;
[pthObj,solnInfo] = plan(planner,start,goal);
```

Display the number of iterations taken for the tree to converge. Observe that the planner requires significantly fewer iterations compared to when the EnableConnectHeuristic property is set to false.

```
fprintf('Number of iterations: %d\n',solnInfo.NumIterations)
```

Number of iterations: 135
Visualize the results.
figure
show (map)
hold on
plot(solnInfo.StartTreeData(:,1),solnInfo.StartTreeData(:,2),'.-','color','b') \% Start tree expa plot(solnInfo.GoalTreeData(:,1),solnInfo.GoalTreeData(:,2),'.-','color','g') \% Goal tree expansi plot(pthObj.States(:,1),pthObj.States(:,2),'r-','LineWidth',2) \% draw path


## Input Arguments

## planner - Path planner

plannerBiRRT object
Path planner, specified as a plannerBiRRT object.

## startState - Start state of path

$N$-element real-valued vector
Start state of the path, specified as an $N$-element real-valued vector. $N$ is the number of dimensions in the state space.

Example: [1 1 pi/6]
Data Types: single | double

## goalState - Goal state of path

N -element real-valued vector
Goal state of the path, specified as an $N$-element real-valued vector. $N$ is the number of dimensions in the state space.

Example: [2 2 pi/3]
Data Types: single | double

## Output Arguments

## path - Planned path information

navPath object
Planned path information, returned as a navPath object.

```
solnInfo - Solution Information
```

structure
Solution Information, returned as a structure. The structure contains these fields:

| Field | Description |
| :--- | :--- |
| IsPathFound | Indicates whether a path is found. It returns 1 <br> (true) if a path is found. Otherwise, it returns 0 <br> (false). |
| ExitFlag | Indicates the termination cause of the planner, <br> returned as: |
|  | - $1-$ The planner reaches the goal. <br> - $2-$ The planner reaches the maximum <br> number of iterations. <br> 3- The planner reaches the maximum <br> number of nodes. |


| Field | Description |
| :--- | :--- |
| StartTreeNumNodes | Number of nodes in the start search tree when <br> the planner terminates, excluding the root node. |
| GoalTreeNumNodes | Number of nodes in the goal search tree when <br> the planner terminates, excluding the root node. |
| NumIterations | Number of combined iterations by both the start <br> tree and goal tree. |
| StartTreeData | Collection of explored states that reflect the <br> status of the start search tree when the planner <br> terminates. Note that NaN values are inserted as <br> delimiters to separate each individual edge. |
| GoalTreeData | Collection of explored states that reflect the <br> status of the goal search tree when the planner <br> terminates. Note that NaN values are inserted as <br> delimiters to separate each individual edge. |

Data Types: structure

## See Also

## Objects

plannerBiRRT | navPath

## Functions

copy

## Introduced in R2021a

## plannerControIRRT

Control-based RRT planner

## Description

The plannerControlRRT object is a rapidly exploring random tree (RRT) planner for solving kinematic and dynamic (kinodynamic) planning problems using controls. The RRT algorithm is a treebased motion planning routine that incrementally grows a search tree. In kinematic planners, the tree grows by randomly sampling states in system configuration space, and then attempts to propagate the nearest node toward that state. The state propagator samples controls for reaching the state based on the kinematic model and control policies. As the tree adds nodes, the sampled states span the search space and eventually connect the start and goal states.

These are the control-based RRT algorithm steps:

- Planner, plannerControlRRT, requests a state from the state space.
- Planner finds the nearest state in the search tree based on cost.
- State propagator, mobileRobotPropagator, samples control commands and durations to propagate toward the target state.
- State propagator propagates toward the target state.
- If the propagator returns a valid trajectory to the state, then add the state to the tree.
- Optional: Attempt to direct trajectory toward final goal based on NumGoalExtension and GoalBias properties.
- Continue searching until the search tree reaches the goal or satisfies other exit criteria.

The benefit of a kinodynamic planner like plannerControlRRT is that it is guaranteed to return a sequence of states, controls, and references which comprise a kinematically or dynamically feasibly path. The drawback to a kinodynamic planner is that the kinematic propagations cannot guarantee that new states are exactly equal to the target states unless there exists and analytic representation for a sequence of controls that drive the system between two configurations with zero residual error. This means that kinodynamic planners are typically asymptotically complete and guarantee kinematic feasibility, but often can not guarantee asymptotic optimality.

## Creation

## Syntax

```
controlPlanner = plannerControlRRT(propagator)
controlPlanner = plannerControlRRT(propagator,Name=Value)
```


## Description

controlPlanner = plannerControlRRT(propagator) creates a kinodynamic RRT planner from a state propagator object and sets the StatePropagator property.
controlPlanner = plannerControlRRT(propagator, Name=Value) specifies additional properties using name-value arguments. For example, plannerControlRRT (propagator, ContinueAfterGoalReached=1) continues to search for alternative paths after the tree first reaches the goal.

## Properties

## StatePropagator - State propagator

mobileRobotPropagator object (default)| object of subclass of nav.StatePropagator
Mobile robot state propagator, specified as a mobileRobotPropagator object or an object of a subclass of nav. StatePropagator.

## ContinueAfterGoalReached - Optimization after reaching goal

false or 0 (default) | true or 1
Optimization after reaching the goal, specified as a logical 0 (false) or 1 (true). If specified as true, the planner continues to search for alternative paths after it first reaches the goal. The planner terminates regardless of the value of this property if it reaches the maximum number of iterations or maximum number of tree nodes.

Data Types: logical

## MaxPlanningTime - Maximum time allowed for planning

Inf (default) | positive scalar in seconds
Maximum time allowed for planning, specified as a positive scalar in seconds.
Data Types: single|double

## MaxNumTreeNodes - Maximum number of nodes in search tree <br> le4 (default) | positive integer

Maximum number of nodes in the search tree, excluding the root node, specified as a positive integer.
Data Types: single|double
MaxNumIteration - Maximum number of iterations
le4 (default) | positive integer
Maximum number of iterations, specified as a positive integer.
Data Types: single | double

## NumGoalExtension - Number of times to propagate towards goal <br> 1 (default) | positive integer

The maximum number of times the planner can propagate towards the goal, specified as a positive integer. After successfully adding a new node to the tree, the planner attempts to propagate the new node toward the goal using the propagateWhileValid object function of the state propagator. The planner continues propagating until the function returns an empty state vector indicating that no valid control is found, the planner reaches the goal, or the function has been called NumGoalExtension times.

To turn this behavior off, set the property to 0 . Turning this behavior off will result in propagating randomly instead of toward the goal.

## Data Types: single |double

## GoalBias - Probability of choosing goal state during state sampling

0.1 (default) | real scalar in range [0,1]

Probability of choosing the goal state during state sampling, specified as a real scalar in the range [0, 1]. This property determines the likelihood of the planner choosing the actual goal state when randomly selecting states from the state space. You can start by setting the probability to a small value, such as 0.05.

## Data Types: single | double

## GoalReachedFcn - Callback function to determine whether goal is reached @plannerControlRRT. GoalReachedDefault | function handle

Callback function to determine whether the goal is reached, specified as a function handle. You can create your own goal-reached function. The function must follow this syntax:

```
isReached = myGoalReachedFcn(planner,currentState,goalState)
```

where:

- planner - is the created planner object, specified as a plannerControlRRT object.
- currentState - is the current state, specified as a $s$-element real vector. $s$ is the number of state variables in the state space.
- goalState - is the goal state, specified as a $s$-element real vector. $s$ is the number of state variables in the state space.
- isReached - is a boolean that indicates whether the current state has reached the goal state, returned as true or false.


## Data Types: function handle

## Object Functions

plan Plan kinematically feasible path between two states
copy Creates deep copy of planner object

## Examples

## Plan Kinodynamic Path with Controls for Mobile Robot

Plan control paths for a bicycle kinematic model with the mobileRobotPropagator object. Specify a map for the environment, set state bounds, and define a start and goal location. Plan a path using the control-based RRT algorithm, which uses a state propagator for planning motion and the required control commands.

## Set State and State Propagator Parameters

Load a ternary map matrix and create an occupancyMap object. Create the state propagator using the map. By default, the state propagator uses a bicycle kinematic model.

```
load('exampleMaps','ternaryMap')
map = occupancyMap(ternaryMap,10);
```

```
propagator = mobileRobotPropagator(Environment=map); % Bicycle model
```

Set the state bounds on the state space based on the map world limits.

```
propagator.StateSpace.StateBounds(1:2,:) = ...
    [map.XWorldLimits; map.YWorldLimits];
```


## Plan Path

Create the path planner from the state propagator.
planner = plannerControlRRT(propagator);
Specify the start and goal states.

```
start = [10 15 0];
goal = [40 30 0];
```

Plan a path between the states. For repeatable results, reset the random number generator before planning. The plan function outputs a navPathControl object, which contains the states, control commands, and durations.

```
rng("default")
path = plan(planner,start,goal)
path =
    navPathControl with properties:
        StatePropagator: [1x1 mobileRobotPropagator]
            States: [192x3 double]
            Controls: [191x2 double]
            Durations: [191x1 double]
            TargetStates: [191x3 double]
            NumStates: 192
            NumSegments: 191
```


## Visualize Results

Visualize the map and plot the path states.

```
show(map)
hold on
plot(start(1),start(2),"rx")
plot(goal(1),goal(2),"go")
plot(path.States(:,1),path.States(:,2),"b")
hold off
```



Display the [v psi] control inputs of forward velocity and steering angle.
plot(path.Controls)
ylim([-1 1])
legend(["Velocity (m/s)","Steering Angle (rad)"])


## References

[1] S.M. Lavalle, J.J. Kuffner, "Randomized kinodynamic planning", International Journal of Robotics Research, vol. 20, no. 5, pp. 378-400, May 2001
[2] Kavraki, L. and S. LaValle. "Chapter 5 Motion Planning", 1st ed., B. Siciliano et O. Khatib, Ed. New York: Springer-Verlag Berlin Heidelberg, 2008, pp. 109-131.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

## Objects

plannerAStarGrid|plannerBiRRT|plannerHybridAStar|plannerRRT|plannerRRTStar

## Functions

plan | copy

## Topics

"Reverse-Capable Motion Planning for Tractor-Trailer Model Using plannerControlRRT"

Introduced in R2021b

## plan

Plan kinematically feasible path between two states

## Syntax

```
path = plan(planner,startState,goalState)
```

[___, solutionInfo] = plan(planner,startState, goalState)
[__] = plan(planner,startState, goalSampleFcn)

## Description

path $=p l a n(p l a n n e r, s t a r t S t a t e, g o a l S t a t e)$ tries to find a valid path between startState and goalState.

The planning is carried out based on the state propagator, which leverages a kinematic model and controllers of the system to search the configuration space. The planner returns a navPathControl object, path, which contains the propagator used during planning and a sequence of states, controls, target states, and control durations.
[ ___,solutionInfo] = plan(planner,startState, goalState) also returns the solution information solutionInfo of the path planning.
[___] = plan(planner, startState, goalSampleFcn) takes in a function handle that produces a goal configuration when called. The function handle should take no inputs and generate a goal state whose size matches startState.

## Examples

## Plan Kinodynamic Path with Controls for Mobile Robot

Plan control paths for a bicycle kinematic model with the mobileRobotPropagator object. Specify a map for the environment, set state bounds, and define a start and goal location. Plan a path using the control-based RRT algorithm, which uses a state propagator for planning motion and the required control commands.

## Set State and State Propagator Parameters

Load a ternary map matrix and create an occupancyMap object. Create the state propagator using the map. By default, the state propagator uses a bicycle kinematic model.

```
load('exampleMaps','ternaryMap')
map = occupancyMap(ternaryMap,10);
propagator = mobileRobotPropagator(Environment=map); % Bicycle model
```

Set the state bounds on the state space based on the map world limits.

```
propagator.StateSpace.StateBounds(1:2,:) = ...
    [map.XWorldLimits; map.YWorldLimits];
```


## Plan Path

Create the path planner from the state propagator.
planner = plannerControlRRT(propagator);
Specify the start and goal states.

```
start = [10 15 0];
goal = [40 30 0];
```

Plan a path between the states. For repeatable results, reset the random number generator before planning. The plan function outputs a navPathControl object, which contains the states, control commands, and durations.

```
rng("default")
path = plan(planner,start,goal)
path =
    navPathControl with properties:
    StatePropagator: [1x1 mobileRobotPropagator]
                    States: [192x3 double]
                    Controls: [191\times2 double]
            Durations: [191x1 double]
            TargetStates: [191x3 double]
                    NumStates: }19
                NumSegments: }19
```


## Visualize Results

Visualize the map and plot the path states.

```
show(map)
hold on
plot(start(1),start(2),"rx")
plot(goal(1),goal(2),"go")
plot(path.States(:,1),path.States(:,2),"b")
hold off
```



Display the [v psi] control inputs of forward velocity and steering angle.
plot (path.Controls)
ylim([-1 1])
legend(["Velocity (m/s)","Steering Angle (rad)"])


## Input Arguments

## planner - Path planner

plannerControlRRT object
Path planner, specified as a plannerControlRRT object.

## startState - Start state of path

$s$-element vector
Initial state of the path, specified as an $s$-element vector. $s$ is the number of state variables in the state space. For example, a robot in the $\operatorname{SE}(2)$ space has a state vector of [x y theta].
Example: [1 1 pi/6]
Data Types: single | double

## goalState - Goal state of path

$s$-element vector
Goal state of the path, specified as an $s$-element vector. $s$ is the number of state variables in the state space. For example, a robot in the $\operatorname{SE}(2)$ space has a state vector of [x y theta].
Example: [2 2 pi/3]
Data Types: single | double

## goalSampleFcn - Goal state sample function

function handle
Goal state sample function, specified as a function handle. The function handle should take no inputs and generate a goal state whose size matches startState.
Example:
Data Types: function_handle

## Output Arguments

## path - Planned path information

navPathControl object
Planned path information, returned as a navPathControl object.

## solutionInfo - Solution Information

structure
Solution Information, returned as a structure. The structure contains these fields:

| Field | Description |
| :--- | :--- |
| IsPathFound | Indicates whether a path is found. It returns as 1 <br> if a path is found. Otherwise, it returns as 0. |
| ExitFlag | Indicates the terminate status of the planner, <br> returned as one of these options: <br> - $1-$ Goal successfully reached <br> - $2-$ Exceeded maximum number of iterations <br> - $3-$ Exceeded maximum number of nodes <br> - $\quad 4-$ Exceeded maximum planning time |
| NumTreeNode | Number of nodes in the search tree when the <br> planner terminates excluding the root node. |
| NumIterations | Number of target states propagated. |
| PlanningTime | Elapsed time while planning, returned as a scalar <br> in seconds. |
| TreeInfo | Collection of explored states that reflects the <br> status of the search tree when the planner <br> terminates. Note that the planner inserts NaN <br> values as delimiters to separate each individual <br> edge. |

## Data Types: structure

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

Objects
plannerControlRRT
Functions
copy

Introduced in R2021b

## copy

Creates deep copy of planner object

## Syntax

plannerCopy $=\operatorname{copy}($ planner $)$

## Description

plannerCopy $=$ copy ( $p$ lanner ) creates a deep copy of the planner object with the same properties.

## Examples

## Create Copy of plannerControIRRT Object

Create an occupancy map from an example map and set the map resolution as 10 cells/meter.

```
load("exampleMaps","ternaryMap")
map = occupancyMap(ternaryMap,10);
```

Create the state propagator using the map. By default, the state propagator uses a bicycle kinematic model.

```
propagator = mobileRobotPropagator(Environment=map);
```

Set the state bounds on the state space based on the map world limits.

```
propagator.StateSpace.StateBounds(1:2,:) = ...
                            [map.XWorldLimits; map.YWorldLimits];
Create a plannerControlRRT object.
planner = plannerControlRRT(propagator)
planner =
    plannerControlRRT with properties:
        StatePropagator: [1x1 mobileRobotPropagator]
        ContinueAfterGoalReached: 0
            MaxPlanningTime: Inf
            MaxNumTreeNode: 10000
            MaxNumIteration: 10000
            NumGoalExtension: 1
                        GoalBias: 0.1000
            GoalReachedFcn: @plannerControlRRT.GoalReachedDefault
```

Create a copy of the plannerControlRRT object.
plannerNew $=$ copy (planner)

```
plannerNew =
    plannerControlRRT with properties:
        StatePropagator: [1x1 mobileRobotPropagator]
        ContinueAfterGoalReached: 0
        MaxPlanningTime: Inf
            MaxNumTreeNode: 10000
            MaxNumIteration: 10000
            NumGoalExtension: 1
                GoalBias: 0.1000
                GoalReachedFcn: @plannerControlRRT.GoalReachedDefault
```


## Input Arguments

planner - Path planner
plannerControlRRT object
Path planner, specified as a plannerControlRRT object.

## Output Arguments

plannerCopy - Copy of path planner
plannerControlRRT object
Copy of path planner, returned as a plannerControlRRT object.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

Objects
plannerControlRRT
Functions
plan

Introduced in R2021b

## plannerHybridAStar

Hybrid A* path planner

## Description

The Hybrid A* path planner object generates a smooth path in a given 2-D space for vehicles with nonholonomic constraints.

Note The Hybrid A* planner checks for collisions in the map by interpolating the motion primitives and analytic expansion based on the ValidationDistance property of the stateValidator object. If the ValidationDistance property is set to Inf, the object interpolates based on the cell size of the map specified in the state validator. Inflate the occupancy map before assigning it to the planner to account for the vehicle size.

## Creation

## Syntax

planner = plannerHybridAStar(validator)
planner = plannerHybridAStar(validator, Name, Value)
Description
planner = plannerHybridAStar(validator) creates a path planner object using the Hybrid A* algorithm. Specify the validator input as a validator0ccupancyMap or validatorVehicleCostmap object. The validator input sets the value of the "StateValidator" on page 2-0 property.
planner = plannerHybridAStar(validator,Name, Value) sets "Properties" on page 2-1029 of the path planner by using one or more name-value pair arguments. Enclose each property name inside single quotes (' ').

## Properties

## StateValidator - State validator for planning

validatorOccupancyMap object | validatorVehicleCostmap object
State validator for planning, specified either as a validator0ccupancyMap or validatorVehicleCostmap object based on SE(2) state space.

MotionPrimitiveLength - Length of motion primitives to be generated ceil(sqrt(2)*map_CellSize) (default)| positive scalar

Length of motion primitives to be generated, specified as the comma-separated pair consisting of 'MotionPrimitiveLength' and a positive scalar in meters. Increase the length for large maps or sparse environments. Decrease the length for dense environments.

Note 'MotionPrimitiveLength' cannot exceed one-fourth the length of the circumference of a circle based on the 'MinTurningRadius'.

## Data Types: double

## MinTurningRadius - Minimum turning radius of vehicle

(2*motion_primitive_length)/pi (default) | positive scalar
Minimum turning radius of vehicle, specified as the comma-separated pair consisting of 'MinTurningRadius ' and a positive scalar in meters.

Note The value of 'MinTurningRadius' is set such that the 'MotionPrimitiveLength' cannot exceed one-fourth the length of the circumference of a circle based on it.

## Data Types: double

## NumMotionPrimitives - Number of motion primitives to be generated

5 (default) | positive odd integer scalar greater than or equal to 3
Number of motion primitives to be generated, specified as the comma-separated pair consisting of ' NumMotionPrimitives ' and a positive odd integer scalar greater than or equal to 3.

## ForwardCost - Cost multiplier to travel in forward direction

1 (default) | positive scalar
Cost multiplier to travel in forward direction, specified as the comma-separated pair consisting of ' ForwardCost ' and a positive scalar. Increase the cost value to penalize forward motion.

## Data Types: double

## ReverseCost - Cost multiplier to travel in reverse direction

3 (default) | positive scalar
Cost multiplier to travel in reverse direction, specified as the comma-separated pair consisting of
'ReverseCost' and a positive scalar. Increase the cost value to penalize reverse motion.
Data Types: double

## DirectionSwitchingCost - Additive cost for switching direction of motion <br> 0 (default) | positive scalar

Additive cost for switching direction of motion, specified as the comma-separated pair consisting of 'DirectionSwitchingCost ' and a positive scalar. Increase the cost value to penalize direction switching.
Data Types: double

## AnalyticExpansionInterval - Interval for attempting analytic expansion from lowest cost node available

## 5 (default) | positive integer scalar

Interval for attempting analytic expansion from the lowest cost node available at that instance, specified as the comma-separated pair consisting of 'AnalyticExpansionInterval' and a positive integer scalar.

The Hybrid A* path planner expands the motion primitives from the nodes with the lowest cost available at that instance:

- The number of nodes to be expanded depends upon the number of primitives to be generated in both the direction and their validity, the cycle repeats until 'AnalyticExpansionInterval' is reached.
- The planner then attempts an analytic expansion to reach the goal pose from the tree using a Reeds-Shepp model. If the attempt fails, the planner repeats the cycle.

Improve the algorithm performance by reducing the interval to increase the number of checks for a Reeds-Shepp connection to the final goal.

## InterpolationDistance - Distance between interpolated poses in output path

1 (default) | positive scalar
Distance between interpolated poses in output path, specified as the comma-separated pair consisting of 'InterpolationDistance' and a positive scalar in meters.

## Data Types: double

## Object Functions

plan Find obstacle-free path between two poses
show Visualize the planned path

## Examples

## Obstacle-Free Path Planning Using Hybrid A Star

Plan a collision-free path for a vehicle through a parking lot by using the Hybrid A* algorithm.

## Create and Assign Map to State Validator

Load the cost values of cells in the vehicle costmap of a parking lot.
load parkingLotCostVal.mat \% costVal
Create a binary0ccupancyMap with cost values.
map $=$ binary0ccupancyMap(costVal);
Create a state validator object for collision checking.

```
validator = validatorOccupancyMap;
```

Assign the map to the state validator object.

```
validator.Map = map;
```


## Plan and Visualize Path

Initialize the plannerHybridAStar object with the state validator object. Specify the MinTurningRadius and MotionPrimitiveLength properties of the planner.

```
planner = plannerHybridAStar(validator,'MinTurningRadius',4,'MotionPrimitiveLength',6);
```

Define start and goal poses for the vehicle as [ $x, y$, theta] vectors. $x$ and $y$ specify the position in meters, and theta specifies the orientation angle in radians.

```
startPose = [6 10 pi/2]; % [meters, meters, radians]
goalPose = [90 54 -pi/2];
```

Plan a path from the start pose to the goal pose.

```
refpath = plan(planner,startPose,goalPose);
```

Visualize the path using show function.
show(planner)

Hybrid A* Path Planner


## References

[1] Dolgov, Dmitri, Sebastian Thrun, Michael Montemerlo, and James Diebel. Practical Search Techniques in Path Planning for Autonomous Driving. American Association for Artificial Intelligence, 2008.
[2] Petereit, Janko, Thomas Emter, Christian W. Frey, Thomas Kopfstedt, and Andreas Beutel.
"Application of Hybrid A* to an Autonomous Mobile Robot for Path Planning in Unstructured Outdoor Environments." ROBOTIK 2012: 7th German Conference on Robotics. 2012, pp. 1-6.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

validatorOccupancyMap | validatorVehicleCostmap | navPath

## Topics

"Generate Code for Path Planning Using Hybrid A Star"
Introduced in R2019b

## plan

Find obstacle-free path between two poses

## Syntax

```
path = plan(planner,start,goal)
[path,directions] = plan(planner,start,goal)
[path,directions,solutionInfo] = plan(planner,start,goal)
```


## Description

path $=$ plan(planner,start,goal) computes an obstacle-free path between start and goal poses, specified as [x y theta] vectors, using the input plannerHybridAStar object.
[path, directions] = plan(planner,start, goal) also returns the direction of motion for each pose along the path, directions, as a column vector. A value of 1 indicates forward direction and a value of -1 indicates reverse direction. The function returns an empty column vector when the planner is unable to find a path.
[path,directions,solutionInfo] = plan(planner,start,goal) also returns solutionInfo that contains the solution information of the path planning as a structure.

## Examples

## Obstacle-Free Path Planning Using Hybrid A Star

Plan a collision-free path for a vehicle through a parking lot by using the Hybrid A* algorithm.

## Create and Assign Map to State Validator

Load the cost values of cells in the vehicle costmap of a parking lot.
load parkingLotCostVal.mat \% costVal
Create a binary0ccupancyMap with cost values.
map $=$ binaryOccupancyMap(costVal);
Create a state validator object for collision checking.

```
validator = validatorOccupancyMap;
```

Assign the map to the state validator object.

```
validator.Map = map;
```


## Plan and Visualize Path

Initialize the plannerHybridAStar object with the state validator object. Specify the MinTurningRadius and MotionPrimitiveLength properties of the planner.
planner = plannerHybridAStar(validator,'MinTurningRadius',4,'MotionPrimitiveLength',6);
Define start and goal poses for the vehicle as $[x, y$, theta] vectors. $x$ and $y$ specify the position in meters, and theta specifies the orientation angle in radians.

```
startPose = [6 10 pi/2]; % [meters, meters, radians]
goalPose = [90 54 -pi/2];
```

Plan a path from the start pose to the goal pose.

```
refpath = plan(planner,startPose,goalPose);
```

Visualize the path using show function.
show(planner)

Hybrid A* Path Planner


## Input Arguments

## planner - Hybrid A* path planner

plannerHybridAStar object
Hybrid A* path planner, specified as a plannerHybridAStar object.

## start - Start location of path

three-element vector

Start location of path, specified as a 1-by-3 vector in the form [x y theta]. $x$ and $y$ specify the position in meters, and theta specifies the orientation angle in radians.

Example: [5 5 pi/2]
Data Types: double

## goal - Final location of path

three-element vector
Final location of path, specified as a 1-by-3 vector in the form [ $x$ y theta]. $x$ and $y$ specify the position in meters, and theta specifies the orientation angle in radians.

Example: [45 45 pi/4]
Data Types: double

## Output Arguments

## path - Obstacle-free path

navPath object
Obstacle-free path, returned as a navPath object.

## directions - Directions of motion

column vector of 1 s (forward) and -1 s (reverse)
Direction of motion for each pose along the path, returned as a column vector of 1 s (forward) and -1 s (reverse).
Data Types: double

## solutionInfo - Solution Information

structure
Solution Information, returned as a structure. The fields of the structure are:
Fields of solutionInfo

| Fields | Description |
| :--- | :--- |
| IsPathFound | Indicates whether a path is found. It returns as 1 <br> if a path is found. Otherwise, it returns 0. |
| NumNodes | Number of nodes in the search tree when the <br> planner terminates (excluding the root node). |
| NumIterations | Number of planning iterations executed. |

Data Types: struct

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

validatorOccupancyMap | validatorVehicleCostmap | navPath
Introduced in R2019b

## show

Visualize the planned path

## Syntax

```
show(planner)
show(planner,Name,Value)
axHandle = show(planner)
```


## Description

show(planner) plots the Hybrid A* expansion tree and the planned path in the map.
show(planner, Name, Value) specifies additional options using one or more name-value pair arguments.
axHandle $=$ show(planner) outputs the axes handle of the figure used to plot the path.

## Examples

## Obstacle-Free Path Planning Using Hybrid A Star

Plan a collision-free path for a vehicle through a parking lot by using the Hybrid A* algorithm.

## Create and Assign Map to State Validator

Load the cost values of cells in the vehicle costmap of a parking lot.
load parkingLotCostVal.mat \% costVal
Create a binary0ccupancyMap with cost values.
map = binaryOccupancyMap(costVal);
Create a state validator object for collision checking.
validator = validatorOccupancyMap;
Assign the map to the state validator object.

```
validator.Map = map;
```


## Plan and Visualize Path

Initialize the plannerHybridAStar object with the state validator object. Specify the MinTurningRadius and MotionPrimitiveLength properties of the planner.
planner = plannerHybridAStar(validator,'MinTurningRadius',4,'MotionPrimitiveLength',6);
Define start and goal poses for the vehicle as [ $x, y$, theta] vectors. $x$ and $y$ specify the position in meters, and theta specifies the orientation angle in radians.

```
startPose = [6 10 pi/2]; % [meters, meters, radians]
goalPose = [90 54 -pi/2];
```

Plan a path from the start pose to the goal pose.
refpath $=$ plan(planner,startPose,goalPose);
Visualize the path using show function.
show(planner)


## Input Arguments

## planner - Hybrid A* path planner

plannerHybridAStar object
Hybrid A* path planner, specified as a plannerHybridAStar object.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: 'Positions','none'

## Parent - Axes used to plot path

Axes object | UIAxes object
Axes used to plot path, specified as the comma-separated pair consisting of 'Parent' and either an axes or uiaxes object. If you do not specify ' Parent', a new figure is created.

## Tree - Display expansion tree

'on' (default)|'off'
Display expansion tree option, specified as the comma-separated pair consisting of 'Tree' and either 'on' or 'off'.

Example: show(planner,'Tree','off')
Data Types: string

## Path - Display planned path

```
'on' (default)| 'off
```

Display planned path option, specified as the comma-separated pair consisting of 'Path' and either 'on' or 'off'.

Example: show(planner,'Path','off')
Data Types: string

## Positions - Display start and goal points

'both' (default)|'start'|'goal'| 'none'
Display the start and goal points, specified as the comma-separated pair consisting of 'Positions ' and one of the following:

- 'start' - Display the start point.
- 'goal' - Display the goal point.
- 'both ' - Display the start and goal points.
- 'none ' - Do not display any points.

Example: show(planner,'Positions','start')
Data Types: string

## Output Arguments

## axHandle - Axes used to plot path

Axes object | UIAxes object
Axes used to plot path, returned as either an axes or uiaxes object.

## See Also

validatorOccupancyMap | validatorVehicleCostmap | navPath

## Introduced in R2019b

## plannerPRM

Create probabilistic roadmap path planner

## Description

The probabilistic roadmap path planner constructs a roadmap without start and goal states. Use the plan function to find an obstacle-free path between the specified start and goal states. If the plan function does not find a connected path between the start and the goal states, it returns an empty path.

## Creation

## Syntax

planner = plannerPRM(stateSpace,stateVal)
planner = plannerPRM( $\qquad$ , Name=Value)

## Description

planner = plannerPRM(stateSpace, stateVal) creates a PRM planner from a state space object, stateSpace, and a state validator object, stateVal. The state space of stateVal must be the same as stateSpace. stateSpace and stateVal also sets the StateSpace and StateValidator properties, respectively, of the planner.
planner = plannerPRM( $\qquad$ ,Name=Value) sets properties using one or more name-value pair arguments in addition to the input arguments in the previous syntax. You can specify the MaxNumNodes or MaxConnectionDistance properties as name-value pairs.

## Properties

## StateSpace - State space for planner

state space object
State space for the planner, specified as a state space object. You can use state space objects such as stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp. You can also customize a state space object using the nav. StateSpace object.

## StateValidator - State validator for planner

state validator object
State validator for the planner, specified as a state validator object. You can use state validator objects such as validator0ccupancyMap and validatorVehicleCostmap. You can also customize a state validator object using the nav.StateValidator object.

## MaxNumNodes - Maximum number of nodes in graph

50 (default) | positive scalar

Maximum number of nodes in the graph, specified as a positive scalar. By increasing this value, the chance of finding a path increases while also increasing the computation time for the path planner.

## MaxConnectionDistance - Maximum connection distance between two states

inf (default) | positive scalar
Maximum distance between two connected nodes, specified as a positive scalar in meters. Nodes with distance greater than this value will not be connected in the graph.

## Object Functions

copy Create deep copy of plannerPRM object
graphData Retrieve graph as digraph object
plan Plan path between start and goal states on roadmap

## Examples

## Plan Obstacle-Free Path Using Probabilistic Roadmap Path Planner

Create an occupancy map from an example map and set the map resolution as 10 cells/meter.

```
map = load("exampleMaps.mat").simpleMap;
map = occupancyMap(map,10);
```

Create a state space and update the state space bounds to be the same as the map limits.

```
ss = stateSpaceSE2;
ss.StateBounds = [map.XWorldLimits; map.YWorldLimits; [-pi pi]];
```

Create a state validator with stateSpaceSE2 using the map and set the validation distance.

```
sv = validatorOccupancyMap(ss,Map=map);
sv.ValidationDistance = 0.01;
```

Create a plannerPRM object.
planner = plannerPRM(ss,sv);
Retrieve graph as a digraph object.
graph = graphData(planner);
Extract nodes and edges from graph.

```
edges = table2array(graph.Edges);
```

nodes $=$ table2array(graph.Nodes);

Specify the start and goal states.

```
start = [0.5 0.5 0];
goal = [2.5 0.2 0];
```

Plot map and graph.

```
show(sv.Map)
```

hold on

```
plot(nodes(:,1),nodes(:,2),"*","Color","b","LineWidth",2)
for i = 1:size(edges,1)
    % Samples states at distance 0.02 meters.
    states = interpolate(ss,nodes(edges(i,1),:), ...
                                    nodes(edges(i,2),:),0:0.02:1);
    plot(states(:,1),states(:,2),"Color","b")
end
plot(start(1),start(2),"*","Color","g","LineWidth",3)
plot(goal(1),goal(2),"*","Color","r","LineWidth",3)
```

Plan a path with default settings. Set the rng seed for repeatability.
rng(100,"twister");
[pthObj, solnInfo] = plan(planner,start,goal);

Visualize the results.

```
if solnInfo.IsPathFound
    interpolate(pthObj,1000);
    plot(pth0bj.States(:,1),pth0bj.States(:,2), ...
                            "Color",[0.85 0.325 0.098],"LineWidth",2)
else
    disp("Path not found")
end
hold off
```



## References

[1] L.E. Kavraki, P. Svestka, J.C. Latombe, M.H. Overmars, "Probabilistic roadmaps for path planning in high-dimensional configuration spaces," IEEE Transactions on Robotics and Automation, Vol. 12, No. 4, pp. 566-580, Aug 1996.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

## Functions

copy | graphData|plan
Introduced in R2022a

## plannerRRT

Create an RRT planner for geometric planning

## Description

The plannerRRT object creates a rapidly-exploring random tree (RRT) planner for solving geometric planning problems. RRT is a tree-based motion planner that builds a search tree incrementally from samples randomly drawn from a given state space. The tree eventually spans the search space and connects the start state to the goal state. The general tree growing process is as follows:

1 The planner samples a random state $x_{\text {rand }}$ in the state space.
2 The planner finds a state $x_{\text {near }}$ that is already in the search tree and is closest (based on the distance definition in the state space) to $x_{\text {rand }}$.
3 The planner expands from $x_{\text {near }}$ towards $x_{\text {rand }}$, until a state $x_{\text {new }}$ is reached.
4 Then new state $x_{\text {new }}$ is added to the search tree.
For geometric RRT, the expansion and connection between two states can be found analytically without violating the constraints specified in the state space of the planner object.

## Creation

## Syntax

planner = plannerRRT(stateSpace,stateVal)

## Description

planner = plannerRRT(stateSpace,stateVal) creates an RRT planner from a state space object, stateSpace, and a state validator object, stateVal. The state space of stateVal must be the same as stateSpace. stateSpace and stateVal also sets the StateSpace and StateValidator properties of the planner.

## Properties

## StateSpace - State space for the planner

state space object
State space for the planner, specified as a state space object. You can use state space objects such as stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp. You can also customize a state space object using the nav.StateSpace object.

## StateValidator - State validator for the planner <br> state validator object

State validator for the planner, specified as a state validator object. You can use state validator objects such as validatorOccupancyMap and validatorVehicleCostmap.

## MaxNumTreeNodes - Maximum number of nodes in the search tree <br> 1e4 (default) | positive integer

Maximum number of nodes in the search tree (excluding the root node), specified as a positive integer.
Data Types: single | double

## MaxIterations - Maximum number of iterations

le4 (default) | positive integer
Maximum number of iterations, specified as a positive integer.
Data Types: single | double
MaxConnectionDistance - Maximum length of motion
0.1 (default) | positive scalar

Maximum length of a motion allowed in the tree, specified as a scalar.
Data Types: single | double
GoalReachedFcn - Callback function to evaluate whether goal is reached @nav.algs.checkIfGoalIsReached | function handle

Callback function to evaluate whether the goal is reached, specified as a function handle. You can create your own goal reached function. The function must follow this syntax:

```
function isReached = myGoalReachedFcn(planner,currentState,goalState)
```

where:

- planner - The created planner object, specified as plannerRRT object.
- currentState - The current state, specified as a three element real vector.
- goalState - The goal state, specified as a three element real vector.
- isReached - A boolean variable to indicate whether the current state has reached the goal state, returned as true or false.

To use custom GoalReachedFcn in code generation workflow, this property must be set to a custom function handle before calling the plan function and it cannot be changed after initialization.
Data Types: function handle
GoalBias - Probability of choosing goal state during state sampling
0.05 (default) | real scalar in [0,1]

Probability of choosing the goal state during state sampling, specified as a real scalar in [0,1]. The property defines the probability of choosing the actual goal state during the process of randomly selecting states from the state space. You can start by setting the probability to a small value such as 0.05 .

Data Types: single | double

## Object Functions

plan Plan path between two states
copy Create copy of planner object

## Examples

## Plan Path Between Two States

Create a state space.
ss = stateSpaceSE2;
Create an occupanyMap-based state validator using the created state space.
sv = validator0ccupancyMap(ss);
Create an occupany map from an example map and set map resolution as 10 cells/meter.

```
load exampleMaps
```

map $=$ occupancyMap(simpleMap,10);
sv.Map = map;

Set validation distance for the validator.

```
sv.ValidationDistance = 0.01;
```

Update state space bounds to be the same as map limits.

```
ss.StateBounds = [map.XWorldLimits;map.YWorldLimits; [-pi pi]];
```

Create the path planner and increase max connection distance.

```
planner = plannerRRT(ss,sv);
planner.MaxConnectionDistance = 0.3;
```

Set the start and goal states.

```
start = [0.5,0.5,0];
goal = [2.5,0.2,0];
```

Plan a path with default settings.

```
rng(100,'twister'); % for repeatable result
[pthObj,solnInfo] = plan(planner,start,goal);
```

Visualize the results.

```
show(map)
hold on
plot(solnInfo.TreeData(:,1),solnInfo.TreeData(:,2),'.-'); % tree expansion
plot(pthObj.States(:,1),pthObj.States(:,2),'r-','LineWidth',2) % draw path
```



## References

[1] S.M. Lavalle and J.J. Kuffner. "Randomized Kinodynamic Planning." The International Journal of Robotics Research. Vol. 20, Number 5, 2001, pp. 378-400.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:

- To use custom GoalReachedFcn in code generation workflow, this property must be set to a custom function handle before calling the plan function and it cannot be changed after initialization.


## See Also

navPath|plannerRRTStar|stateSpaceReedsShepp|stateSpaceDubins|stateSpaceSE2

## Introduced in R2019b

## plannerRRTStar

Create an optimal RRT path planner (RRT*)

## Description

The plannerRRTStar object creates an asymptotically-optimal RRT planner, RRT*. The RRT* algorithm converges to an optimal solution in terms of the state space distance. Also, its runtime is a constant factor of the runtime of the RRT algorithm. RRT* is used to solve geometric planning problems. A geometric planning problem requires that any two random states drawn from the state space can be connected.

## Creation

## Syntax

planner = plannerRRTStar(stateSpace,stateVal)

## Description

planner = plannerRRTStar(stateSpace,stateVal) creates an RRT* planner from a state space object, stateSpace, and a state validator object, stateVal. The state space of stateVal must be the same as stateSpace. stateSpace and stateVal also sets the StateSpace and StateValidator properties of the planner object.

## Properties

## BallRadiusConstant - Constant used to estimate the near neighbors search radius <br> 100 (default) | positive scalar

Constant used to estimate the near neighbors search radius, specified as a positive scalar. With a larger ball radius, the searching radius reduces slower as the number of nodes in the tree increases.

Data Types: single | double

## ContinueAfterGoalReached - Continue to optimize after goal is reached

 false (default) | trueDecide if the planner continues to optimize after the goal is reached, specified as false or true. The planner also terminates regardless of the value of this property if the maximum number of iterations or maximum number of tree nodes is reached.

## Data Types: logical

## StateSpace - State space for the planner

state space object
State space for the planner, specified as a state space object. You can use state space objects such as stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp. You can also customize a state space object using the nav.StateSpace object.

## StateValidator - State validator for the planner <br> state validator object

State validator for the planner, specified as a state validator object. You can use state validator objects such as validatorOccupancyMap and validatorVehicleCostmap.

## MaxNumTreeNodes - Maximum number of nodes in the search tree <br> 1e4 (default) | positive integer

Maximum number of nodes in the search tree (excluding the root node), specified as a positive integer.

Data Types: single | double
MaxIterations - Maximum number of iterations
le4 (default) | positive integer
Maximum number of iterations, specified as a positive integer.
Data Types: single | double
MaxConnectionDistance - Maximum length of motion
0.1 (default) | positive scalar

Maximum length of a motion allowed in the tree, specified as a scalar.
Data Types: single | double

## GoalReachedFcn - Callback function to determine whether goal is reached <br> @nav.algs.checkIfGoalIsReached | function handle

Callback function to determine whether the goal is reached, specified as a function handle. You can create your own goal reached function. The function must follow this syntax:

```
function isReached = myGoalReachedFcn(planner,currentState,goalState)
```

where:

- planner - The created planner object, specified as plannerRRTStar object.
- currentState - The current state, specified as a three element real vector.
- goalState - The goal state, specified as a three element real vector.
- isReached - A boolean variable to indicate whether the current state has reached the goal state, returned as true or false.

To use custom GoalReachedFcn in code generation workflow, this property must be set to a custom function handle before calling the plan function and it cannot be changed after initialization.

## Data Types: function handle

## GoalBias - Probability of choosing goal state during state sampling <br> 0.05 (default) | real scalar in [0,1]

Probability of choosing the goal state during state sampling, specified as a real scalar in [0,1]. The property defines the probability of choosing the actual goal state during the process of randomly selecting states from the state space. You can start by setting the probability to a small value such as 0.05 .

Data Types: single | double

## Object Functions

plan Plan path between two states
copy Create copy of planner object

## Examples

## Plan Optimal Path Between Two States

Create a state space.

```
ss = stateSpaceSE2;
```

Create a occupancyMap-based state validator using the created state space.
sv = validator0ccupancyMap(ss);
Create an occupany map from an example map and set map resolution as 10 cells/meter.

```
load exampleMaps.mat
map = occupancyMap(simpleMap, 10);
sv.Map = map;
```

Set validation distance for the validator.

```
sv.ValidationDistance = 0.01;
```

Update state space bounds to be the same as map limits.

```
ss.StateBounds = [map.XWorldLimits; map.YWorldLimits; [-pi pi]];
```

Create RRT* path planner and allow further optimization after goal is reached.

```
planner = plannerRRTStar(ss,sv);
planner.ContinueAfterGoalReached = true;
```

Reduce max iterations and increase max connection distance.

```
planner.MaxIterations = 2500;
planner.MaxConnectionDistance = 0.3;
```

Set the start and goal states.

```
start = [0.5, 0.5 0];
goal = [2.5, 0.2, 0];
```

Plan a path with default settings.

```
rng(100, 'twister') % repeatable result
[pthObj, solnInfo] = plan(planner,start,goal);
```

Visualize the results.
map.show;
hold on;
plot(solnInfo.TreeData(:,1),solnInfo.TreeData(:,2), '.-'); \% tree expansion plot(pthObj.States(:,1),pthObj.States(:,2),'r-','LineWidth',2); \% draw path


## References

[1] Karaman, S. and E. Frazzoli. "Sampling-Based Algorithms for Optimal Motion Planning." The International Journal of Robotics Research. Vol. 30, Number 7, 2011, pp 846-894.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{Tm}}$.
Usage notes and limitations:

- To use custom GoalReachedFcn in code generation workflow, this property must be set to a custom function handle before calling the plan function and it cannot be changed after initialization.


## See Also

navPath | plannerRRT | stateSpaceSE2 | stateSpaceReedsShepp | stateSpaceDubins

Introduced in R2019b

## plan

Plan path between two states

## Syntax

```
path = plan(planner,startState,goalState)
[path,solutionInfo] = plan(planner,startState,goalState)
```


## Description

path = plan(planner,startState, goalState) returns a path from the start state to the goal state.
[path, solutionInfo] = plan(planner,startState, goalState) also returns solInfo that contains the solution information of the path planning.

## Examples

## Plan Path Between Two States

Create a state space.
ss = stateSpaceSE2;
Create an occupanyMap-based state validator using the created state space.
sv = validatorOccupancyMap(ss);
Create an occupany map from an example map and set map resolution as 10 cells/meter.
load exampleMaps
map = occupancyMap(simpleMap,10);
sv.Map = map;
Set validation distance for the validator.

```
sv.ValidationDistance = 0.01;
```

Update state space bounds to be the same as map limits.
ss.StateBounds = [map.XWorldLimits;map.YWorldLimits; [-pi pi]];
Create the path planner and increase max connection distance.
planner = plannerRRT(ss,sv);
planner.MaxConnectionDistance = 0.3;
Set the start and goal states.

```
start = [0.5,0.5,0];
```

goal $=[2.5,0.2,0]$;

Plan a path with default settings.

```
rng(100,'twister'); % for repeatable result
[pthObj,solnInfo] = plan(planner,start,goal);
```

Visualize the results.
show(map)
hold on
plot(solnInfo.TreeData(:,1), solnInfo.TreeData(:,2),'.-'); \% tree expansion plot(pthObj.States(:,1),pthObj.States(:,2),'r-','LineWidth',2) \% draw path


## Input Arguments

## planner - Path planner

plannerRRT object | plannerRRTStar object
Path planner, specified as a plannerRRT object or a plannerRRTStar object.

## startState - Start state of the path

$N$-element real-valued vector
Start state of the path, specified as an $N$-element real-valued vector. $N$ is the dimension of the state space.

Example: [1 1 pi/6]

Data Types: single|double

## goalState - Goal state of the path

$N$-element real-valued vector
Goal state of the path, specified as an $N$-element real-valued vector. $N$ is the dimension of the state space.

Example: [2 2 pi/3]
Data Types: single | double

## Output Arguments

path - Object that holds planned path information
navPath object
An object that holds the planned path information, returned as a navPath object.
solutionInfo - Solution Information
structure
Solution Information, returned as a structure. The fields of the structure are:

Fields of solutionInfo

| Fields | Description |
| :--- | :--- |
| IsPathFound | Indicates whether a path is found. It returns as 1 <br> if a path is found. Otherwise, it returns 0. |
| ExitFlag | Indicates the terminate status of the planner, <br> returned as |
| NumNodes $1-$ if the goal is reached |  |
| - $2-$ if the maximum number of iterations is |  |
| reached |  |
| $3-$ if the maximum number of nodes is |  |
| reached |  |\(\left|\begin{array}{l}Number of nodes in the search tree when the <br>


planner terminates (excluding the root node).\end{array}\right|\)| NumIterations | Aumber of "extend" routines executed. <br> A collection of explored states that reflects the <br> status of the search tree when planner <br> terminates. Note that NaN values are inserted as <br> delimiters to separate each individual edge. |
| :--- | :--- |
| TreeData | Contains the cost of the path at each iteration. <br> Value for iterations when path has not reached <br> the goal is denoted by a NaN. Size of the array is |
| PathCosts | NumIterations-by-1. Last element contains the <br> cost of the final path. |
| Note This field is applicable only for <br> plannerRRTStar object. |  |

## Data Types: structure

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

navPath | plannerRRT|plannerRRTStar|stateSpaceReedsShepp| stateSpaceDubins| stateSpaceSE2

## Introduced in R2019b

## copy

Create copy of planner object

## Syntax

planner2 = copy(planner1)

## Description

planner2 = copy(planner1) creates a planner object, planner2, form a planner object, plannerl.

## Examples

## Create Copy of plannerRRT Object

Create an occupancy map from an example map and set the map resolution as 10 cells/meter.

```
map = load("exampleMaps.mat").simpleMap;
```

map = occupancyMap(map,10);

Create a state space and update the state space bounds to be the same as the map limits.

```
ss = stateSpaceSE2;
ss.StateBounds = [map.XWorldLimits; map.YWorldLimits; [-pi pi]];
```

Create a state validator with stateSpaceSE2 using the map and set the validation distance.

```
sv = validatorOccupancyMap(ss,Map=map);
sv.ValidationDistance = 0.01;
```

Create a plannerRRT object.
planner = plannerRRT(ss,sv)
planner =
plannerRRT with properties:
StateSpace: [1x1 stateSpaceSE2]
StateValidator: [1x1 validator0ccupancyMap]
MaxNumTreeNodes: 10000
MaxIterations: 10000
MaxConnectionDistance: 0.1000
GoalReachedFcn: @nav.algs.checkIfGoalIsReached
GoalBias: 0.0500

Create a copy of the plannerRRT object.
plannerNew $=\operatorname{copy}($ planner $)$
plannerNew =
plannerRRT with properties:

```
            StateSpace: [1x1 stateSpaceSE2]
        StateValidator: [1x1 validatorOccupancyMap]
    MaxNumTreeNodes: 10000
        MaxIterations: 10000
MaxConnectionDistance: 0.1000
    GoalReachedFcn: @nav.algs.checkIfGoalIsReached
        GoalBias: 0.0500
```


## Input Arguments

planner1 - Path planner
plannerRRT object | plannerRRTStar object
Path planner, specified as a plannerRRT object or a plannerRRTStar object.

## Output Arguments

planner2 - Path planner
plannerRRT object | plannerRRTStar object
Path planner, returned as a plannerRRT object or a plannerRRTStar object.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

navPath | plannerRRT | plannerRRTStar| stateSpaceReedsShepp|stateSpaceDubins | stateSpaceSE2

Introduced in R2018b

## poseGraph

Create 2-D pose graph

## Description

A poseGraph object stores information for a 2-D pose graph representation. A pose graph contains nodes connected by edges. Each node estimate is connected to the graph by edge constraints that define the relative pose between nodes and the uncertainty on that measurement.

To construct a pose graph iteratively, use the addRelativePose function to add relative pose estimates and connect them to an existing node with specified edge constraints. Pose nodes must be specified relative to a pose node. Specify the uncertainty of the measurement using an information matrix.


## Pose Node Estimates

Adding an edge between two nonsequential nodes creates a loop closure in the graph. Multiple edges or multiedges between node pairs are also supported, which includes loop closures. To add additional edge constraints or loop closures, specify the node IDs using the addRelativePose function. When optimizing the pose graph, the optimizePoseGraph function finds a solution to satisfy all these edge constraints.


To add landmark point nodes, use the addPointLandmark function. This function specifies nodes as xy-points without orientation estimates. Landmarks must be specified relative to a pose node.


## Point landmarks

The lidarSLAM object performs lidar-based simultaneous localization and mapping, which is based around the optimization of a 2-D pose graph.

For 3-D pose graphs, see the poseGraph3D object or the "Landmark SLAM Using AprilTag Markers" example.

## Creation

## Syntax

poseGraph = poseGraph
poseGraph = poseGraph('MaxNumEdges', maxEdges,'MaxNumNodes',maxNodes)

## Description

poseGraph = poseGraph creates a 2-D pose graph object. Add poses using addRelativePose to construct a pose graph iteratively.
poseGraph = poseGraph('MaxNumEdges',maxEdges,'MaxNumNodes',maxNodes) specifies an upper bound on the number of edges and nodes allowed in the pose graph when generating code.
This syntax is only required when generating code.

## Properties

## NumNodes - Number of nodes in pose graph

1 (default) | positive integer
This property is read-only.
Number of nodes in pose graph, specified as a positive integer. Each node represents a pose measurement or a point landmark measurement. To specify relative poses between nodes, use addRelativePose. To specify a landmark pose, use addLandmarkPose. To get a list of all nodes, use edgeNodePairs.

## NumEdges - Number of edges in pose graph

0 (default) | nonnegative integer
This property is read-only.
Number of edges in pose graph, specified as a nonnegative integer. Each edge connects two nodes in the pose graph. Loop closure edges and landmark edges are included.

## NumLoopClosureEdges - Number of loop closures

0 (default) | nonnegative integer
This property is read-only.
Number of loop closures in pose graph, specified as a nonnegative integer. To get the edge IDs of the loop closures, use the LoopClosureEdgeIDs property.

## LoopClosureEdgeIDs - Loop closure edge IDs

vector
This property is read-only.
Loop closure edges IDs, specified as a vector of edge IDs.

## LandmarkNodeIDs - Landmark node IDs

vector

This property is read-only.
Landmark node IDs, specified as a vector of IDs for each node.

## Object Functions

| addPointLandmark | Add landmark point node to pose graph |
| :--- | :--- |
| addRelativePose | Add relative pose to pose graph |
| copy | Create copy of pose graph |
| edgeNodePairs | Edge node pairs in pose graph |
| edgeConstraints | Edge constraints in pose graph |
| edgeResidualErrors | Compute pose graph edge residual errors |
| findEdgeID | Find edge ID of edge |
| nodeEstimates | Poses of nodes in pose graph |
| removeEdges | Remove loop closure edges from graph |
| show | Plot pose graph |

## Examples

## Optimize a 2-D Pose Graph

Optimize a pose graph based on the nodes and edge constraints. The pose graph used in this example is from the Intel Research Lab Dataset and was generated from collecting wheel odometry and a laser range finder sensor information in an indoor lab.

Load the Intel data set that contains a 2-D pose graph. Inspect the poseGraph object to view the number of nodes and loop closures.

```
load intel-2d-posegraph.mat pg
disp(pg)
    poseGraph with properties:
            NumNodes: 1228
            NumEdges: 1483
        NumLoopClosureEdges: 256
        LoopClosureEdgeIDs: [1228 1229 1230 1231 1232 1233 1234 1235 1236 ... ]
            LandmarkNodeIDs: [1x0 double]
```

Plot the pose graph with IDs off. Red lines indicate loop closures identified in the dataset.

```
show(pg,'IDs','off');
title('Original Pose Graph')
```



Optimize the pose graph. Nodes are adjusted based on the edge constraints and loop closures. Plot the optimized pose graph to see the adjustment of the nodes with loop closures.
updatedPG = optimizePoseGraph(pg);
figure
show(updatedPG,'IDs', 'off');
title('Updated Pose Graph')


## References

[1] Grisetti, G., R. Kummerle, C. Stachniss, and W. Burgard. "A Tutorial on Graph-Based SLAM." IEEE Intelligent Transportation Systems Magazine. Vol. 2, No. 4, 2010, pp. 31-43. doi:10.1109/ mits.2010.939925.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder ${ }^{\mathrm{TM}}$.
Use this syntax when constructing poseGraph objects for code generation: poseGraph = poseGraph('MaxNumEdges', maxEdges,'MaxNumNodes', maxNodes) specifies an upper bound on the number of edges and nodes allowed in the pose graph when generating code. This limit is only required when generating code.

## See Also

## Functions

optimizePoseGraph | addRelativePose | addPointLandmark | show

## Objects

lidarSLAM | poseGraph3D

# Topics <br> "Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans" <br> "Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans" <br> "Landmark SLAM Using AprilTag Markers" 

Introduced in R2019b

## addPointLandmark

Add landmark point node to pose graph

## Syntax

```
addPointLandmark(poseGraph,measurement)
addPointLandmark(poseGraph,measurement,infoMat)
addPointLandmark(poseGraph,measurement,infoMat,poseNodeID)
addPointLandmark(poseGraph,measurement,infoMat,poseNodeID,pointNodeID)
[nodePair,edgeID] = addPointLandmark(
```

$\qquad$

``` )
```


## Description

addPointLandmark(poseGraph,measurement) adds a landmark point node, based on the input position measurement that connects to the last pose node in the pose graph. To add pose measurement nodes, see the addRelativePose function.
addPointLandmark(poseGraph,measurement,infoMat) also specifies the information matrix as part of the edge constraint, which represents the uncertainty of the landmark measurement.
addPointLandmark(poseGraph,measurement,infoMat, poseNodeID) adds a new landmark point node and connects it to the pose node specified by poseNodeID.
addPointLandmark(poseGraph,measurement,infoMat, poseNodeID, pointNodeID) creates an edge by specifying a point measurement between existing nodes, specified by poseNodeID and pointNodeID. If the node pair already exists, the function appends the new measurement.
[nodePair,edgeID] = addPointLandmark( $\qquad$ ) returns the newly added edge and edge ID using any combination of inputs from the previous syntaxes.

## Input Arguments

poseGraph - Pose graph
poseGraph object | poseGraph3D object
Pose graph, specified as a poseGraph or poseGraph3D object.

## measurement - Position of landmark point

two-element vector of form [x y$] \mid$ three-element vector of form $\left[\begin{array}{lll}x & y & z\end{array}\right]$
Position of landmark point, specified as one of the following:
For poseGraph (2-D), the pose is a two-element vector of form of the form [ $x y$ ], which defines an $x y$-position for the landmark.

For poseGraph3D, the pose is a three-element vector of the form [ $\left.\begin{array}{lll}x & y & z\end{array}\right]$, which defines an $x y z$ position for the landmark.

## infoMat - Information matrix for landmark

three-element vector | six-element vector

Information matrix for the landmark, specified as a three-element or six-element vector.
Each vector is the compact form of the upper triangle of the square information matrix. An information matrix represents the uncertainty of the measurement. The matrix is calculated as the inverse of the covariance. If the measurement is an $[x y]$ vector, the covariance matrix is a 2 -by- 2 matrix of pairwise covariance calculations. Typically, the uncertainty is determined by the sensor model.

For poseGraph3D, each information matrix is a six-element vector. The default is [llllll $\left.\begin{array}{llll}1 & 0 & 1 & 0\end{array}\right]$.

## poseNodeID - Pose node to attach from

positive integer
Pose node to attach from, specified as a positive integer. This integer corresponds to the node ID of a pose node in poseGraph. When specified without the pointNodeID input, addPointLandmark creates a new landmark point node and adds an edge between the new node and the poseNodeID node.

## pointNodeID - Landmark point node to attach to <br> positive integer

Landmark point node to attach to, specified as a positive integer. This integer corresponds to the ID of a landmark node in the pose graph. See the LandmarkNodeIDs property of the pose graph.

## Output Arguments

nodePair - Edge node pair in pose graph
two-element vector
Edge node pair in the pose graph, returned as a two-element vector that lists the IDs of the two nodes that the edge connects. Multiple edges may exist between the same pair of nodes.

## edgeID - ID of added edge

positive integer
ID of added edge, returned as a positive integer.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.
Use this syntax when constructing poseGraph or poseGraph3D objects for code generation:
poseGraph = poseGraph('MaxNumEdges', maxEdges,'MaxNumNodes', maxNodes) specifies an upper bound on the number of edges and nodes allowed in the pose graph when generating code.
This limit is only required when generating code.
poseGraph = poseGraph3D('MaxNumEdges',maxEdges,'MaxNumNodes',maxNodes)

## See Also

```
Functions
optimizePoseGraph | findEdgeID|edgeNodePairs|edgeConstraints|nodeEstimates|
removeEdges
Objects
poseGraph | poseGraph3D| lidarSLAM
```


## Topics

```
"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
"Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
"Landmark SLAM Using AprilTag Markers"
```

Introduced in R2021a

## addRelativePose

Add relative pose to pose graph

## Syntax

```
addRelativePose(poseGraph,measurement)
addRelativePose(poseGraph,measurement,infoMat)
addRelativePose(poseGraph,measurement,infoMat,fromNodeID)
addRelativePose(poseGraph,measurement,infoMat,fromNodeID,toNodeID)
[nodePair,edgeID] = addRelativePose(
```

$\qquad$

``` )
```


## Description

addRelativePose(poseGraph, measurement) creates a node based on the input measurement that connects to the last pose node in the pose graph. To add landmark nodes, see the addPointLandmark function.
addRelativePose(poseGraph,measurement,infoMat) also specifies the information matrix as part of the edge constraint, which represents the uncertainty of the pose measurement.
addRelativePose(poseGraph, measurement,infoMat,fromNodeID) creates a new pose node and connects it to the specific node specified by fromNodeID.
addRelativePose(poseGraph, measurement,infoMat,fromNodeID,toNodeID) creates an edge by specifying a relative pose measurement between existing nodes specified by fromNodeID and toNodeID. This edge is called a loop closure. If a loop closure already exists, the function appends the new measurement. Calling the optimizePoseGraph function combines multiple appended measurements into a single edge. This syntax does not support adding edges to a landmark node.
[nodePair,edgeID] = addRelativePose( $\qquad$ ) returns the newly added edge and edge ID using any of the previous syntaxes.

## Input Arguments

## poseGraph - Pose graph

poseGraph object | poseGraph3D object
Pose graph, specified as a poseGraph or poseGraph3D object.

## measurement - Relative pose between nodes

[x y theta] vector|[x y z qw qx qy qz] vector
Relative pose between nodes, specified as one of the following:
For poseGraph (2-D), the pose is a [x y theta] vector, which defines a $x y$-position and orientation angle, theta.

For poseGraph3D, the pose is a [ $x$ y $z$ qw $q x$ qy $q z$ ] vector, which defines by an xyz-position and quaternion orientation, [qw qx qy qz]

Note Many other sources for 3-D pose graphs, including .g2o formats, specify the quaternion orientation in a different order, for example, [qx qy qz qw]. Check the source of your pose graph data before adding nodes to your poseGraph3D object.

## infoMat - Information matrix

6 -element vector | 21 -element vector
Information matrices, specified in compact form as a 6 -element vector or 21 -element vector.
Each row is the upper triangle of the square information matrix. An information matrix represents the uncertainty of the measurement. The matrix is calculated as the inverse of the covariance. If the measurement is an [x y theta] vector, the covariance matrix is a 3-by-3 of pairwise covariance calculations. Typically, the uncertainty is determined by the sensor model.

For poseGraph (2-D), each information matrix is a six-element vector. The default is [1 0010 1]. For landmark nodes, the last three elements are returned as NaN .

For poseGraph3D, each information matrix is a 21 -element vector. The default is [100001 $00001000100101]$.

## fromNodeID - Node to attach from

positive integer
Node to attach from, specified as a positive integer. This integer corresponds to the node ID of a node in poseGraph. When specified without toNodeID, addRelativePose creates a new node and adds an edge between the new node and the fromNodeID node.

## toNodeID - Node to attach to

positive integer
Node to attach to, specified as a positive integer. This integer corresponds to the node ID of a node in poseGraph. addRelativePose adds an edge between this node and the fromNodeID node.

## Output Arguments

## nodePair - Edge node pair in pose graph

two-element vector
Edge node pairs in pose graph, returned as two-element vector that lists the IDs of the two nodes that each edge connects. Multiple edges may exist between the same pair of nodes.

```
edgeID - ID of added edge
positive integer
```

ID of added edge, returned as a positive integer.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Use this syntax when constructing poseGraph or poseGraph3D objects for code generation:
poseGraph = poseGraph('MaxNumEdges',maxEdges,'MaxNumNodes',maxNodes) specifies an upper bound on the number of edges and nodes allowed in the pose graph when generating code.
This limit is only required when generating code.
poseGraph = poseGraph3D('MaxNumEdges',maxEdges,'MaxNumNodes', maxNodes)

## See Also

## Functions

optimizePoseGraph | findEdgeID | edgeNodePairs |edgeConstraints|nodeEstimates | removeEdges

Objects
poseGraph | poseGraph3D | lidarSLAM

## Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
"Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
"Landmark SLAM Using AprilTag Markers"

Introduced in R2019b

## copy

Create copy of pose graph

## Syntax

poseGraph2 = copy(poseGraph1)

## Description

poseGraph2 = copy (poseGraph1) creates a deep copy of the pose graph object with the same properties.

## Examples

## Create Copy of Pose Graph

Create a 2-D pose graph object.

```
pg = poseGraph
pg =
    poseGraph with properties:
            NumNodes: 1
            NumEdges: 0
        NumLoopClosureEdges: 0
            LoopClosureEdgeIDs: [1x0 double]
                LandmarkNodeIDs: []
```

Create copy of the pose graph object.
pgNew $=\operatorname{copy}(\mathrm{pg})$
pgNew =
poseGraph with properties:
NumNodes: 1
NumEdges: 0
NumLoopClosureEdges: 0
LoopClosureEdgeIDs: [1x0 double]
LandmarkNodeIDs: []

## Input Arguments

poseGraph1 - Pose graph
poseGraph object | poseGraph3D object
Pose graph, specified as a poseGraph or poseGraph3D object.

## Output Arguments

poseGraph2 - Copy of pose graph
poseGraph object | poseGraph3D object
Copy of pose graph, returned as a poseGraph or poseGraph3D object.

## See Also

poseGraph | poseGraph3D
Introduced in R2019b

## edgeConstraints

Edge constraints in pose graph

## Syntax

measurements $=$ edgeConstraints(poseGraph)
[measurements,infoMats] = edgeConstraints(poseGraph)
[measurements,infoMats] = edgeConstraints(poseGraph,edgeIDs)

## Description

measurements = edgeConstraints(poseGraph) lists all edge constraints in the specified pose graph as a relative pose.
[measurements,infoMats] = edgeConstraints(poseGraph) also returns the information matrices for each edge. The information matrix is the inverse of the covariance of the pose measurement.
[measurements,infoMats] = edgeConstraints(poseGraph,edgeIDs) returns edge constraints for the specified edge IDs.

## Input Arguments

poseGraph - Pose graph
poseGraph object | poseGraph3D object
Pose graph, specified as a poseGraph or poseGraph3D object.

## edgeIDs - Edge IDs

vector of positive integers
Edge IDs, specified as a vector of positive integers.

## Output Arguments

## measurements - Measurements between nodes

$n$-by-3 matrix | $n$-by-7 matrix
Measurements between nodes, returned as an $n$-by- 3 matrix or $n$-by- 7 matrix.
For poseGraph (2-D), each row is an [x y theta] vector, which defines the relative $x y$-position and orientation angle, theta, of a pose in the graph. For landmark positions, theta is returned as NaN .

For poseGraph3D, each row is an [x y z qw qx qy qz] vector, which defines the relative xyzposition and quaternion orientation, [qw qx qy qz], of a pose in the graph.

Note Many other sources for 3-D pose graphs, including .g2o formats, specify the quaternion orientation in a different order, for example, [qx qy qz qw]. Check the source of your pose graph data before adding nodes to your poseGraph3D object.

## infoMats - Information matrices

## n-by-6 matrix | $n$-by-21 matrix

Information matrices, specified in compact form as a $n$-by- 6 or $n$-by- 21 matrix, where $n$ is the number of poses in the pose graph.

Each row is the upper triangle of the square information matrix. An information matrix represents the uncertainty of the measurement. The matrix is calculated as the inverse of the covariance. If the measurement is an [x y theta] vector, the covariance matrix is a 3-by-3 of pairwise covariance calculations. Typically, the uncertainty is determined by the sensor model.

For poseGraph (2-D), each information matrix is a six-element vector. The default is [100180 1]. For landmark nodes, the last three elements are returned as NaN .

For poseGraph3D, each information matrix is a 21 -element vector. The default is [100001 $00001000100101]$.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Use this syntax when constructing poseGraph or poseGraph3D objects for code generation:
poseGraph = poseGraph('MaxNumEdges',maxEdges,'MaxNumNodes',maxNodes) specifies an upper bound on the number of edges and nodes allowed in the pose graph when generating code.
This limit is only required when generating code.

## See Also

## Functions

edgeNodePairs |optimizePoseGraph|addRelativePose | findEdgeID | nodeEstimates | removeEdges

## Objects

poseGraph | poseGraph3D|lidarSLAM

## Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
"Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

## Introduced in R2019b

## edgeNodePairs

Edge node pairs in pose graph

## Syntax

nodePairs = edgeNodePairs(poseGraph)
nodePairs = edgeNodePairs(poseGraph,edgeIDs)

## Description

nodePairs = edgeNodePairs(poseGraph) returns all edges in the specified pose graph as a list of node ID pairs. Each row of the edges output is a pair of nodes that form an edge. Multiple edges may exist between the same pair of nodes.
nodePairs = edgeNodePairs(poseGraph,edgeIDs) returns edges corresponding to the specified edge IDs. Each edge in the pose graph has a unique ID even if the node pairs are the same.

## Input Arguments

poseGraph - Pose graph
poseGraph object | poseGraph3D object
Pose graph, specified as a poseGraph or poseGraph3D object.
edgeIDs - Edge IDs
vector of positive integers
Edge IDs, specified as a vector of positive integers.

## Output Arguments

## nodePairs - Edge node pairs in pose graph

$n$-by-2 matrix
Edge node pairs in pose graph, returned as n-by-2 matrix that lists the IDs of the two nodes that each edge connects. Each row is a pair of nodes that form an edge. Multiple edges may exist between the same pair of nodes, so the matrix may contain duplicate entries.

## Compatibility Considerations

## edgeNodePairs was renamed

Behavior change in future release
The edgeNodePairs object function was renamed from edges. Use edgeNodePairs when calling the function.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Use this syntax when constructing poseGraph or poseGraph3D objects for code generation:
poseGraph = poseGraph('MaxNumEdges',maxEdges,'MaxNumNodes',maxNodes) specifies an upper bound on the number of edges and nodes allowed in the pose graph when generating code.
This limit is only required when generating code.

## See Also

## Functions

optimizePoseGraph | addRelativePose | findEdgeID | edgeConstraints|nodeEstimates | removeEdges

## Objects

poseGraph | poseGraph3D | lidarSLAM

## Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
"Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
Introduced in R2019b

## edgeResidualErrors

Compute pose graph edge residual errors

## Syntax

resErrorVec = edgeResidualErrors(poseGraphObj)

## Description

resErrorVec = edgeResidualErrors(poseGraphObj) returns the residual errors for each edge in the pose graph with the current pose node estimates. The residual errors order matches the order of edge IDs in poseGraph.

## Examples

## Optimize and Trim Loop Closures For 2-D Pose Graphs

Optimize a pose graph based on the nodes and edge constraints. Trim loop closed based on their edge residual errors.

Load the data set that contains a 2-D pose graph. Inspect the poseGraph object to view the number of nodes and loop closures.

```
load grid-2d-posegraph.mat pg
disp(pg)
    poseGraph with properties:
            NumNodes: 120
            NumEdges: 193
        NumLoopClosureEdges: 74
        LoopClosureEdgeIDs: [120 121 122 123 124 125 126 127 128 129 130 ... ]
            LandmarkNodeIDs: [1x0 double]
```

Plot the pose graph with IDs off. Red lines indicate loop closures identified in the dataset. The poses in the graph should follow a grid pattern, but show evidence of drift over time.

```
show(pg,'IDs','off');
title('Original Pose Graph')
```



Optimize the pose grap using the optimizePoseGraph function. By default, this function uses the "builtin-trust-region" solver. Because the pose graph contains some bad loop closures, the resulting pose graph is actual not desirable.
pgOptim $=$ optimizePoseGraph(pg);
figure;
show(pgOptim);


Look at the edge residual errors for the original pose graph. Large outlier error values at the end indicate bad loop closures.

```
resErrorVec = edgeResidualErrors(pg);
plot(resErrorVec);
title('Edge Residual Errors by Edge ID')
```



Certain loop closures should be trimmed from the pose graph based on their residual error. Use the trimLoopClosures function to trim therse bad loop closures. Set the maximum and truncation threshold for the trimmer parameters. This threshold is set based on the measurement accuracy and should be tuned for your system.
trimParams.MaxIterations = 100;
trimParams.TruncationThreshold = 25;
solverOptions = poseGraphSolverOptions;
Use the trimLoopClosures function with the trimmer parameters and solver options.
[pgNew, trimInfo, debugInfo] = trimLoopClosures(pg,trimParams,solverOptions);
From the trimInfo output, plot the loop closures removed from the optimized pose graph. By plotting with the residual errors plot before, you can see the large error loop closures were removed.

```
removedLCs = trimInfo.LoopClosuresToRemove;
hold on
plot(removedLCs,zeros(length(removedLCs)),'or')
title('Edge Residual Errors and Removed Loop Closures')
legend('Residual Errors', 'Removed Loop Closures')
xlabel('Edge IDs')
ylabel('Edge Residual Error')
hold off
```



Show the new pose graph with the bad loop closures trimmed.
show(pgNew, "IDs","off");


## Input Arguments

poseGraph0bj - Pose graph
poseGraph object | poseGraph3D object
Pose graph, specified as a poseGraph or poseGraph3D object.

## Output Arguments

## resErrorVec - Edge residual errors for pose graph

vector of positive scalars
Edge residual errors for pose graph, specified as a vector of positive scalars.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Use this syntax when constructing poseGraph or poseGraph3D objects for code generation:
poseGraph = poseGraph('MaxNumEdges',maxEdges,'MaxNumNodes',maxNodes) specifies an upper bound on the number of edges and nodes allowed in the pose graph when generating code. This limit is only required when generating code.

## See Also

## Functions

edgeNodePairs|optimizePoseGraph|addRelativePose|findEdgeID|nodeEstimates | removeEdges

Objects
poseGraph | poseGraph3D | lidarSLAM

Introduced in R2020b

## findEdgelD

Find edge ID of edge

## Syntax

edgeID = findEdgeID(poseGraph, nodePairs)

## Description

edgeID = findEdgeID(poseGraph, nodePairs) finds the edge ID for a specified edge. Edges are defined by the IDs of the two nodes that connect them.

## Input Arguments

poseGraph - Pose graph
poseGraph object | poseGraph3D object
Pose graph, specified as a poseGraph or poseGraph3D object.
nodePairs - Edge node pairs in pose graph
two-element vector
Edge node pairs in pose graph, specified as a two-element vector that lists the IDs of the two nodes that the edge connects.

## Output Arguments

## edgeID - Edge ID

positive integer | vector
Edge IDs, returned as a positive integer or vector of positive integers. The pose graph can contain multiple edges between each node pair, so multiple edge IDs may be returned for a single edge ID.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Use this syntax when constructing poseGraph or poseGraph3D objects for code generation:
poseGraph = poseGraph('MaxNumEdges',maxEdges,'MaxNumNodes',maxNodes) specifies an upper bound on the number of edges and nodes allowed in the pose graph when generating code.
This limit is only required when generating code.

## See Also

```
Functions
optimizePoseGraph | addRelativePose| edgeNodePairs| edgeConstraints|
nodeEstimates| removeEdges
Objects
poseGraph | poseGraph3D | lidarSLAM
```


## Topics

```
"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
"Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
Introduced in R2019b
```


## nodeEstimates

Poses of nodes in pose graph

## Syntax

measurements $=$ nodeEstimates(poseGraph)
measurements $=$ nodeEstimates(poseGraph,nodeIDs)

## Description

measurements = nodeEstimates(poseGraph) lists all poses in the specified pose graph.
measurements = nodeEstimates(poseGraph, nodeIDs) lists the poses with the specified node IDs.

## Input Arguments

poseGraph - Pose graph
poseGraph object | poseGraph3D object
Pose graph, specified as a poseGraph or poseGraph3D object.
nodeIDs - Node IDs
positive integer | vector of positive integers
Node IDs, specified as a positive integer or vector of positive integers. Each node added gets an ID sequentially in the graph.

## Output Arguments

## measurements - Measurements between nodes

$n$-by-3 matrix | $n$-by-7 matrix
Measurements between nodes, returned as an $n$-by- 3 matrix or $n$-by- 7 matrix.
For poseGraph (2-D), each row is an [ $x$ y theta] vector, which defines the relative $x y$-position and orientation angle, theta, of a pose in the graph. For landmark positions, theta is returned as NaN .

For poseGraph3D, each row is an [x y z qw $q x$ qy $q z$ ] vector, which defines the relative $x y z$ position and quaternion orientation, [qw qx qy qz], of a pose in the graph.

Note Many other sources for 3-D pose graphs, including .g2o formats, specify the quaternion orientation in a different order, for example, [qx qy qz qw]. Check the source of your pose graph data before adding nodes to your poseGraph3D object.

## Compatibility Considerations

## nodeEstimates was renamed

Behavior change in future release
The nodeEstimates object function was renamed from nodes. Use nodeEstimates when calling the function.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Use this syntax when constructing poseGraph or poseGraph3D objects for code generation:
poseGraph = poseGraph('MaxNumEdges',maxEdges,'MaxNumNodes',maxNodes) specifies an upper bound on the number of edges and nodes allowed in the pose graph when generating code.
This limit is only required when generating code.

## See Also

## Functions

optimizePoseGraph | addRelativePose | edgeNodePairs | findEdgeID | removeEdges | edgeConstraints

## Objects

poseGraph | poseGraph3D | lidarSLAM

## Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
"Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
Introduced in R2019b

## removeEdges

Remove loop closure edges from graph

## Syntax

removeEdges(poseGraph,edgeIDs)

## Description

removeEdges(poseGraph, edgeIDs) removes loop closure edges, landmark edges, or duplicate incremental edges from the pose graph.

## Input Arguments

poseGraph - Pose graph
poseGraph object | poseGraph3D object
Pose graph, specified as a poseGraph or poseGraph3D object.
edgeIDs - Edge IDs
vector of positive integers
Edge IDs, specified as a vector of positive integers. To get edge IDs based on node pairs, see the findEdgeID function.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Use this syntax when constructing poseGraph or poseGraph3D objects for code generation:
poseGraph = poseGraph('MaxNumEdges',maxEdges,'MaxNumNodes',maxNodes) specifies an upper bound on the number of edges and nodes allowed in the pose graph when generating code. This limit is only required when generating code.

## See Also

## Functions

optimizePoseGraph | findEdgeID | addRelativePose | edgeNodePairs |edgeConstraints | nodeEstimates

## Objects

poseGraph | poseGraph3D | lidarSLAM

## Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
"Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

Introduced in R2019b

## show

Plot pose graph

## Syntax

show(poseGraph)
show(poseGraph,Name, Value)
axes $=$ show( $\qquad$ )

## Description

show (poseGraph) plots the specified pose graph in a figure.
show (poseGraph, Name, Value) specifies options using Name, Value pair arguments. For example, 'IDs', 'on ' plots all node and edge IDs of the pose graph.
axes = show $\qquad$ ) returns the axes handle that the pose graph is plotted to using any of previous syntaxes.

## Examples

## Optimize a 2-D Pose Graph

Optimize a pose graph based on the nodes and edge constraints. The pose graph used in this example is from the Intel Research Lab Dataset and was generated from collecting wheel odometry and a laser range finder sensor information in an indoor lab.

Load the Intel data set that contains a 2-D pose graph. Inspect the poseGraph object to view the number of nodes and loop closures.

```
load intel-2d-posegraph.mat pg
disp(pg)
    poseGraph with properties:
            NumNodes: 1228
            NumEdges: 1483
        NumLoopClosureEdges: 256
        LoopClosureEdgeIDs: [1228 1229 1230 1231 1232 1233 1234 1235 1236 ... ]
            LandmarkNodeIDs: [1x0 double]
```

Plot the pose graph with IDs off. Red lines indicate loop closures identified in the dataset.

```
show(pg,'IDs','off');
title('Original Pose Graph')
```



Optimize the pose graph. Nodes are adjusted based on the edge constraints and loop closures. Plot the optimized pose graph to see the adjustment of the nodes with loop closures.
updatedPG = optimizePoseGraph(pg);
figure
show(updatedPG,'IDs', 'off');
title('Updated Pose Graph')


## Optimize a 3-D Pose Graph

Optimize a pose graph based on the nodes and edge constraints. The pose graph used in this example is taken from the MIT Dataset and was generated using information extracted from a parking garage.

Load the pose graph from the MIT dataset. Inspect the poseGraph3D object to view the number of nodes and loop closures.

```
load parking-garage-posegraph.mat pg
disp(pg);
    poseGraph3D with properties:
    NumNodes: 1661
    NumEdges: 6275
    NumLoopClosureEdges: 4615
        LoopClosureEdgeIDs: [\begin{array}{lllllllllllll}{128}&{129}&{130}&{132}&{133}&{134}&{135}&{137}&{138}&{139}&{140... ]}\end{array}]
            LandmarkNodeIDs: [1x0 double]
```

Plot the pose graph with IDs off. Red lines indicate loop closures identified in the dataset.

```
title('Original Pose Graph')
show(pg,'IDs','off');
view(-30,45)
```



Optimize the pose graph. Nodes are adjusted based on the edge constraints and loop closures. Plot the optimized pose graph to see the adjustment of the nodes with loop closures.

```
updatedPG = optimizePoseGraph(pg);
figure
title('Updated Pose Graph')
show(updatedPG,'IDs','off');
view(-30,45)
```



## Input Arguments

## poseGraph - Pose graph

poseGraph object | poseGraph3D object
Pose graph, specified as a poseGraph or poseGraph3D object.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, ... , NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: 'IDs','off'

## Parent - Axes used to plot pose graph

Axes object | UIAxes object
Axes used to plot the pose graph, specified as the comma-separated pair consisting of 'Parent ' and either an Axes or UIAxesobject. See axes or uiaxes.

```
IDs - Display of IDs on pose graph
    'loopclosures'(default)|'all'|'nodes'|'landmarks'|'off'
```

Display of IDs on pose graph, specified as the comma-separated pair consisting of ' IDs ' and one of the following:

- 'all' - Plot all node and edge IDs.
- 'nodes ' - Plot all node IDs and loop closure IDs.
- 'loopclosures ' - Plot only loop closure edge IDs.
- ' landmarks ' - Plot landmark edge IDs.
- 'off' - Do not plot any IDs.


## Output Arguments

## axes - Axes used to plot the map

Axes object | UIAxes object
Axes used to plot the map, returned as either an Axes or UIAxes object. See axes or uiaxes.

## See Also

## Functions

optimizePoseGraph | addRelativePose

## Objects

poseGraph | poseGraph3D | lidarSLAM

## Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
"Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
"Landmark SLAM Using AprilTag Markers"
Introduced in R2019b

## poseGraph3D

Create 3-D pose graph

## Description

A poseGraph3D object stores information for a 3-D pose graph representation. A pose graph contains nodes connected by edges. Each node estimate is connected to the graph by edge constraints that define the relative pose between nodes and the uncertainty on that measurement.

To construct a pose graph iteratively, use the addRelativePose function to add relative pose estimates and connect them to an existing node with specified edge constraints. Pose nodes must be specified relative to a pose node. Specify the uncertainty of the measurement using an information matrix.


## Pose Node Estimates

Adding an edge between two nonsequential nodes creates a loop closure in the graph. Multiple edges or multiedges between node pairs are also supported, which includes loop closures. To add additional edge constraints or loop closures, specify the node IDs using the addRelativePose function. When optimizing the pose graph, the optimizePoseGraph function finds a solution to satisfy all these edge constraints.


To add landmark point nodes, use the addPointLandmark function. This function specifies nodes as xyz-points without orientation estimates. Landmarks must be specified relative to a pose node.


## Point landmarks

For 2-D pose graphs, see poseGraph.
For an example that builds and optimizes a 3-D pose graph from real-world sensor data, see "Landmark SLAM Using AprilTag Markers".

## Creation

## Syntax

poseGraph = poseGraph3D
poseGraph = poseGraph3D('MaxNumEdges', maxEdges,'MaxNumNodes',maxNodes)

## Description

poseGraph = poseGraph3D creates a 3-D pose graph object. Add poses using addRelativePose to construct a pose graph iteratively.
poseGraph = poseGraph3D('MaxNumEdges',maxEdges,'MaxNumNodes',maxNodes) specifies an upper bound on the number of edges and nodes allowed in the pose graph when generating code. This limit is only required when generating code.

## Properties

## NumNodes - Number of nodes in pose graph

1 (default) | positive integer
This property is read-only.
Number of nodes in pose graph, specified as a positive integer. Each node represents a pose measurement or a point landmark measurement. To specify relative poses between nodes, use addRelativePose. To specify a landmark pose, use addLandmarkPose. To get a list of all nodes, use edgeNodePairs.

## NumEdges - Number of edges in pose graph

0 (default) | nonnegative integer
This property is read-only.
Number of edges in pose graph, specified as a nonnegative integer. Each edge connects two nodes in the pose graph. Loop closure edges and landmark edges are included.

## NumLoopClosureEdges - Number of loop closures

0 (default) | nonnegative integer
This property is read-only.
Number of loop closures in pose graph, specified as a nonnegative integer. To get the edge IDs of the loop closures, use the LoopClosureEdgeIDs property.

## LoopClosureEdgeIDs - Loop closure edge IDs

vector
This property is read-only.
Loop closure edges IDs, specified as a vector of edge IDs.

## LandmarkNodeIDs - Landmark node IDs

vector

This property is read-only.
Landmark node IDs, specified as a vector of IDs for each node.

## Object Functions

| addPointLandmark | Add landmark point node to pose graph |
| :--- | :--- |
| addRelativePose | Add relative pose to pose graph |
| copy | Create copy of pose graph |
| edgeNodePairs | Edge node pairs in pose graph |
| edgeConstraints | Edge constraints in pose graph |
| edgeResidualErrors | Compute pose graph edge residual errors |
| findEdgeID | Find edge ID of edge |
| nodeEstimates | Poses of nodes in pose graph |
| removeEdges | Remove loop closure edges from graph |
| show | Plot pose graph |

## Examples

## Optimize a 3-D Pose Graph

Optimize a pose graph based on the nodes and edge constraints. The pose graph used in this example is taken from the MIT Dataset and was generated using information extracted from a parking garage.

Load the pose graph from the MIT dataset. Inspect the poseGraph3D object to view the number of nodes and loop closures.

```
load parking-garage-posegraph.mat pg
disp(pg);
    poseGraph3D with properties:
            NumNodes: 1661
            NumEdges: 6275
        NumLoopClosureEdges: 4615
        LoopClosureEdgeIDs: [128 129 130 132 133 134 135 137 138 139 140 ... ]
            LandmarkNodeIDs: [1x0 double]
```

Plot the pose graph with IDs off. Red lines indicate loop closures identified in the dataset.

```
title('Original Pose Graph')
show(pg,'IDs','off');
view(-30,45)
```



Optimize the pose graph. Nodes are adjusted based on the edge constraints and loop closures. Plot the optimized pose graph to see the adjustment of the nodes with loop closures.

```
updatedPG = optimizePoseGraph(pg);
```

figure
title('Updated Pose Graph')
show(updatedPG,'IDs', 'off');
view(-30,45)


## References

[1] Carlone, Luca, Roberto Tron, Kostas Daniilidis, and Frank Dellaert. "Initialization Techniques for 3D SLAM: a Survey on Rotation Estimation and its Use in Pose Graph Optimization." 2015 IEEE International Conference on Robotics and Automation (ICRA). 2015, pp. 4597-4604.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Use this syntax when constructing poseGraph3D objects for code generation:
poseGraph = poseGraph3D('MaxNumEdges',maxEdges,'MaxNumNodes',maxNodes) specifies an upper bound on the number of edges and nodes allowed in the pose graph when generating code. This limit is only required when generating code.

## See Also

## Functions

optimizePoseGraph | addRelativePose | addPointLandmark

## Objects

poseGraph | lidarSLAM

## Topics

"Landmark SLAM Using AprilTag Markers"

Introduced in R2019b

## quaternion

Create a quaternion array

## Description

A quaternion is a four-part hyper-complex number used in three-dimensional rotations and orientations.

A quaternion number is represented in the form $a+b \mathrm{i}+c \mathrm{j}+d \mathrm{k}$, where $a, b, c$, and $d$ parts are real numbers, and $\mathrm{i}, \mathrm{j}$, and k are the basis elements, satisfying the equation: $\mathrm{i}^{2}=\mathrm{j}^{2}=\mathrm{k}^{2}=\mathrm{ijk}=-1$.

The set of quaternions, denoted by $\mathbf{H}$, is defined within a four-dimensional vector space over the real numbers, $\mathbf{R}^{4}$. Every element of $\mathbf{H}$ has a unique representation based on a linear combination of the basis elements, $\mathrm{i}, \mathrm{j}$, and k .

All rotations in 3-D can be described by an axis of rotation and angle about that axis. An advantage of quaternions over rotation matrices is that the axis and angle of rotation is easy to interpret. For example, consider a point in $\mathbf{R}^{3}$. To rotate the point, you define an axis of rotation and an angle of rotation.


The quaternion representation of the rotation may be expressed as $q=\cos (\theta / 2)+\sin (\theta / 2)\left(u_{b} \mathrm{i}+u_{c} \mathrm{j}+u_{d} \mathrm{k}\right)$, where $\theta$ is the angle of rotation and $\left[u_{b}, u_{c}\right.$, and $\left.u_{d}\right]$ is the axis of rotation.

## Creation

## Syntax

quat = quaternion()
quat $=$ quaternion ( $\mathrm{A}, \mathrm{B}, \mathrm{C}, \mathrm{D}$ )
quat $=$ quaternion(matrix)
quat = quaternion(RV,'rotvec')

```
quat = quaternion(RV,'rotvecd')
quat = quaternion(RM,'rotmat',PF)
quat = quaternion(E,'euler',RS,PF)
quat = quaternion(E,'eulerd',RS,PF)
```


## Description

quat $=$ quaternion() creates an empty quaternion.
quat $=$ quaternion $(A, B, C, D)$ creates a quaternion array where the four quaternion parts are taken from the arrays $A, B, C$, and $D$. All the inputs must have the same size and be of the same data type.
quat $=$ quaternion(matrix) creates an $N$-by-1 quaternion array from an $N$-by-4 matrix, where each column becomes one part of the quaternion.
quat $=$ quaternion(RV, 'rotvec' ) creates an $N$-by-1 quaternion array from an $N$-by- 3 matrix of rotation vectors, RV. Each row of RV represents a rotation vector in radians.
quat = quaternion(RV, 'rotvecd ') creates an $N$-by-1 quaternion array from an $N$-by-3 matrix of rotation vectors, RV. Each row of RV represents a rotation vector in degrees.
quat $=$ quaternion (RM, 'rotmat', PF ) creates an $N$-by-1 quaternion array from the 3-by-3-by- $N$ array of rotation matrices, RM. PF can be either 'point' if the Euler angles represent point rotations or 'frame' for frame rotations.
quat $=$ quaternion(E, 'euler', RS, PF) creates an $N$-by-1 quaternion array from the $N$-by- 3 matrix, E. Each row of E represents a set of Euler angles in radians. The angles in E are rotations about the axes in sequence RS.
quat $=$ quaternion(E, 'eulerd' , RS, PF) creates an $N$-by-1 quaternion array from the $N$-by- 3 matrix, $E$. Each row of $E$ represents a set of Euler angles in degrees. The angles in $E$ are rotations about the axes in sequence RS.

## Input Arguments

## A, B, C, D - Quaternion parts

comma-separated arrays of the same size
Parts of a quaternion, specified as four comma-separated scalars, matrices, or multi-dimensional arrays of the same size.
Example: quat $=$ quaternion $(1,2,3,4)$ creates a quaternion of the form $1+2 i+3 j+4 k$.
Example: quat $=$ quaternion( $[1,5],[2,6],[3,7],[4,8])$ creates a 1 -by-2 quaternion array where quat $(1,1)=1+2 i+3 j+4 k$ and quat $(1,2)=5+6 i+7 j+8 k$
Data Types: single | double

## matrix - Matrix of quaternion parts

$N$-by-4 matrix
Matrix of quaternion parts, specified as an $N$-by- 4 matrix. Each row represents a separate quaternion. Each column represents a separate quaternion part.

Example: quat $=$ quaternion $(r a n d(10,4)$ ) creates a 10-by-1 quaternion array.

Data Types: single | double

## RV - Matrix of rotation vectors

$N$-by-3 matrix
Matrix of rotation vectors, specified as an $N$-by-3 matrix. Each row of RV represents the [X Y Z] elements of a rotation vector. A rotation vector is a unit vector representing the axis of rotation scaled by the angle of rotation in radians or degrees.

To use this syntax, specify the first argument as a matrix of rotation vectors and the second argument as the 'rotvec' or 'rotvecd'.

Example: quat $=$ quaternion $(\operatorname{rand}(10,3)$, 'rotvec') creates a 10 -by-1 quaternion array.
Data Types: single|double

## RM - Rotation matrices

3-by-3 matrix | 3-by-3-by-N array
Array of rotation matrices, specified by a 3-by-3 matrix or 3-by-3-by- $N$ array. Each page of the array represents a separate rotation matrix.

Example: quat $=$ quaternion $(r a n d(3), ' r o t m a t ', ' p o i n t ')$
Example: quat $=$ quaternion (rand $(3)$, 'rotmat', 'frame')
Data Types: single|double

## PF - Type of rotation matrix <br> 'point'|'frame'

Type of rotation matrix, specified by 'point ' or 'frame'.
Example: quat $=$ quaternion $(r a n d(3), ' r o t m a t ', ' p o i n t ')$
Example: quat $=$ quaternion (rand(3),'rotmat','frame')
Data Types: char \| string

## E - Matrix of Euler angles

$N$-by-3 matrix
Matrix of Euler angles, specified by an $N$-by-3 matrix. If using the 'euler' syntax, specify E in radians. If using the 'eulerd ' syntax, specify E in degrees.

Example: quat $=$ quaternion(E,'euler','YZY','point')
Example: quat $=$ quaternion(E,'euler','XYZ','frame')
Data Types: single \| double

## RS - Rotation sequence

character vector | scalar string
Rotation sequence, specified as a three-element character vector:

- 'YZY'
- 'YXY'
- 'ZYZ'
- 'ZXZ'
- 'XYX'
- 'XZX'
- 'XYZ'
- 'YZX'
- 'ZXY'
- 'XZY'
- 'ZYX'
- 'YXZ'

Assume you want to determine the new coordinates of a point when its coordinate system is rotated using frame rotation. The point is defined in the original coordinate system as:

```
point = [sqrt(2)/2,sqrt(2)/2,0];
```

In this representation, the first column represents the $x$-axis, the second column represents the $y$ axis, and the third column represents the $z$-axis.

You want to rotate the point using the Euler angle representation [45,45,0]. Rotate the point using two different rotation sequences:

- If you create a quaternion rotator and specify the ' $Z Y X$ ' sequence, the frame is first rotated $45^{\circ}$ around the $z$-axis, then $45^{\circ}$ around the new $y$-axis.

```
quatRotator = quaternion([45,45,0],'eulerd','ZYX','frame');
newPointCoordinate = rotateframe(quatRotator,point)
newPointCoordinate =
\[
0.7071 \quad-0.0000 \quad 0.7071
\]
```



- If you create a quaternion rotator and specify the 'YZX' sequence, the frame is first rotated $45^{\circ}$ around the $y$-axis, then $45^{\circ}$ around the new $z$-axis.

```
quatRotator = quaternion([45,45,0],'eulerd','YZX','frame');
newPointCoordinate = rotateframe(quatRotator,point)
newPointCoordinate =
    0.8536 0.1464 0.5000
```




Data Types: char|string

## Object Functions

| angvel | Angular velocity from quaternion array |
| :--- | :--- |
| classUnderlying | Class of parts within quaternion |
| compact | Convert quaternion array to N-by-4 matrix |
| conj | Complex conjugate of quaternion |
| dist | Complex conjugate transpose of quaternion array |
| euler | Angular distance in radians |
| eulerd | Convert quaternion to Euler angles (radians) |
| exp | Convert quaternion to Euler angles (degrees) |
| .$l$, ldivide | Exponential of quaternion array |
| log | Element-wise quaternion left division |
| meanrot | Natural logarithm of quaternion array |
| - | Quaternion mean rotation |
| * | Quaternion subtraction |
| norm | Quaternion multiplication |
| normalize | Quaternion norm |
| ones | Quaternion normalization |
| parts | Create quaternion array with real parts set to one and imaginary parts set to zero |
| A,power | Extract quaternion parts |
| prod | Element-wise quaternion power |
| randrot | Product of a quaternion array |
| /,rdivide | Uniformly distributed random rotations |
| rotateframe | Element-wise quaternion right division |
| rotatepoint | Quaternion frame rotation |
| rotmat | Quaternion point rotation |
| rotvec | Convert quaternion to rotation matrix |
| rotvecd | Convert quaternion to rotation vector (radians) |
| slerp | Convert quaternion to rotation vector (degrees) |
| *,times | Spherical linear interpolation |
| 1 | Element-wise quaternion multiplication |
| - | Transpose a quaternion array |
| zeros | Quaternion unary minus |

## Examples

## Create Empty Quaternion

quat $=$ quaternion()

```
quat =
    0x0 empty quaternion array
```

By default, the underlying class of the quaternion is a double.

```
classUnderlying(quat)
ans =
    'double'
```


## Create Quaternion by Specifying Individual Quaternion Parts

You can create a quaternion array by specifying the four parts as comma-separated scalars, matrices, or multidimensional arrays of the same size.

## Define quaternion parts as scalars.

```
A = 1.1;
B = 2.1;
C = 3.1;
D = 4.1;
quatScalar = quaternion(A,B,C,D)
quatScalar = quaternion
    1.1 + 2.1i + 3.1j + 4.1k
```


## Define quaternion parts as column vectors.

```
A = [1.1;1.2];
B = [2.1;2.2];
C = [3.1;3.2];
D = [4.1;4.2];
quatVector = quaternion(A, B,C,D)
quatVector = 2x1 quaternion array
    1.1 + 2.1i + 3.1j + 4.1k
    1.2 + 2.2i + 3.2j + 4.2k
```


## Define quaternion parts as matrices.

```
A = [1.1,1.3; ...
    1.2,1.4];
B = [2.1,2.3; ...
    2.2,2.4];
C = [3.1,3.3; ...
    3.2,3.4];
D = [4.1,4.3; ...
    4.2,4.4];
quatMatrix = quaternion(A,B,C,D)
quatMatrix = 2x2 quaternion array
    1.1 + 2.1i + 3.1j + 4.1k 1.3 + 2.3i + 3.3j + 4.3k
    1.2 + 2.2i + 3.2j + 4.2k 1.4 + 2.4i + 3.4j + 4.4k
```


## Define quaternion parts as three dimensional arrays.

```
A = randn(2,2,2);
B = zeros(2,2,2);
C = zeros(2,2,2);
D = zeros(2,2,2);
quatMultiDimArray = quaternion(A,B,C,D)
quatMultiDimArray = 2x2x2 quaternion array
quatMultiDimArray(:,:,1) =
\begin{tabular}{rccccccc}
\(0.53767+\) & \(0 i+\) & \(0 j+\) & \(0 k\) & \(-2.2588+\) & \(0 i+\) & \(0 j+\) & \(0 k\) \\
\(1.8339+\) & \(0 i+\) & \(0 j+\) & \(0 k\) & \(0.86217+\) & \(0 i+\) & \(0 j+\) & \(0 k\)
\end{tabular}
quatMultiDimArray(:,:,2) =
    0.31877 + 
```


## Create Quaternion by Specifying Quaternion Parts Matrix

You can create a scalar or column vector of quaternions by specify an $N$-by-4 matrix of quaternion parts, where columns correspond to the quaternion parts A, B, C, and D.

Create a column vector of random quaternions.

```
quatParts = rand(3,4)
quatParts = 3×4
\begin{tabular}{llll}
0.8147 & 0.9134 & 0.2785 & 0.9649 \\
0.9058 & 0.6324 & 0.5469 & 0.1576 \\
0.1270 & 0.0975 & 0.9575 & 0.9706
\end{tabular}
quat = quaternion(quatParts)
quat = 3x1 quaternion array
    0.81472 + 0.91338i + 0.2785j + 0.96489k
    0.90579 + 0.63236i + 0.54688j + 0.15761k
    0.12699 + 0.09754i + 0.95751j + 0.97059k
```

To retrieve the quatParts matrix from quaternion representation, use compact.

```
retrievedquatParts = compact(quat)
retrievedquatParts = 3×4
\begin{tabular}{llll}
0.8147 & 0.9134 & 0.2785 & 0.9649 \\
0.9058 & 0.6324 & 0.5469 & 0.1576 \\
0.1270 & 0.0975 & 0.9575 & 0.9706
\end{tabular}
```


## Create Quaternion by Specifying Rotation Vectors

You can create an $N$-by-1 quaternion array by specifying an $N$-by- 3 matrix of rotation vectors in radians or degrees. Rotation vectors are compact spatial representations that have a one-to-one relationship with normalized quaternions.

## Rotation Vectors in Radians

Create a scalar quaternion using a rotation vector and verify the resulting quaternion is normalized.

```
rotationVector = [0.3491,0.6283,0.3491];
quat = quaternion(rotationVector,'rotvec')
quat = quaternion
    0.92124 + 0.16994i + 0.30586j + 0.16994k
norm(quat)
ans = 1.0000
```

You can convert from quaternions to rotation vectors in radians using the rotvec function. Recover the rotationVector from the quaternion, quat.

```
rotvec(quat)
ans = 1\times3
    0.3491 0.6283 0.3491
```


## Rotation Vectors in Degrees

Create a scalar quaternion using a rotation vector and verify the resulting quaternion is normalized.

```
rotationVector = [20,36,20];
quat = quaternion(rotationVector,'rotvecd')
quat = quaternion
    0.92125 + 0.16993i + 0.30587j + 0.16993k
```

norm(quat)
ans $=1$

You can convert from quaternions to rotation vectors in degrees using the rotvecd function. Recover the rotationVector from the quaternion, quat.

```
rotvecd(quat)
ans = 1\times3
    20.0000 36.0000 20.0000
```


## Create Quaternion by Specifying Rotation Matrices

You can create an N -by-1 quaternion array by specifying a 3-by-3-by-N array of rotation matrices. Each page of the rotation matrix array corresponds to one element of the quaternion array.

Create a scalar quaternion using a 3-by-3 rotation matrix. Specify whether the rotation matrix should be interpreted as a frame or point rotation.

```
rotationMatrix = [1 0 0; ...
    0 sqrt(3)/2 0.5; ...
    0-0.5 sqrt(3)/2];
quat = quaternion(rotationMatrix,'rotmat','frame')
quat = quaternion
    0.96593 + 0.25882i + 0j + 0k
```

You can convert from quaternions to rotation matrices using the rotmat function. Recover the rotationMatrix from the quaternion, quat.

```
rotmat(quat,'frame')
ans = 3\times3
    1.0000 
```


## Create Quaternion by Specifying Euler Angles

You can create an $N$-by-1 quaternion array by specifying an $N$-by- 3 array of Euler angles in radians or degrees.

## Euler Angles in Radians

Use the euler syntax to create a scalar quaternion using a 1-by-3 vector of Euler angles in radians. Specify the rotation sequence of the Euler angles and whether the angles represent a frame or point rotation.

```
E = [pi/2,0,pi/4];
quat = quaternion(E,'euler','ZYX','frame')
quat = quaternion
    0.65328 + 0.2706i + 0.2706j + 0.65328k
```

You can convert from quaternions to Euler angles using the euler function. Recover the Euler angles, $E$, from the quaternion, quat.

```
euler(quat,'ZYX','frame')
ans = 1\times3
    1.5708 0 0.7854
```


## Euler Angles in Degrees

Use the eulerd syntax to create a scalar quaternion using a 1-by-3 vector of Euler angles in degrees. Specify the rotation sequence of the Euler angles and whether the angles represent a frame or point rotation.

```
E = [90,0,45];
quat = quaternion(E,'eulerd','ZYX','frame')
quat = quaternion
    0.65328 + 0.2706i + 0.2706j + 0.65328k
```

You can convert from quaternions to Euler angles in degrees using the eulerd function. Recover the Euler angles, E , from the quaternion, quat.

```
eulerd(quat,'ZYX','frame')
ans = 1\times3
    90.0000 0 45.0000
```


## Quaternion Algebra

Quaternions form a noncommutative associative algebra over the real numbers. This example illustrates the rules of quaternion algebra.

## Addition and Subtraction

Quaternion addition and subtraction occur part-by-part, and are commutative:

```
Q1 = quaternion(1,2,3,4)
Q1 = quaternion
    1 + 2i + 3j + 4k
Q2 = quaternion(9, 8,7,6)
Q2 = quaternion
    9 + 8i + 7j + 6k
Q1plusQ2 = Q1 + Q2
Q1plusQ2 = quaternion
    10 + 10i + 10j + 10k
Q2plusQ1 = Q2 + Q1
Q2plusQ1 = quaternion
    10 + 10i + 10j + 10k
Q1minusQ2 = Q1 - Q2
```

```
Q1minusQ2 = quaternion
    -8 - 6i - 4j - 2k
Q2minusQ1 = Q2 - Q1
Q2minusQ1 = quaternion
    8 + 6i + 4j + 2k
```

You can also perform addition and subtraction of real numbers and quaternions. The first part of a quaternion is referred to as the real part, while the second, third, and fourth parts are referred to as the vector. Addition and subtraction with real numbers affect only the real part of the quaternion.

```
Q1plusRealNumber = Q1 + 5
Q1plusRealNumber = quaternion
        6 + 2i + 3j + 4k
Q1minusRealNumber = Q1 - 5
Q1minusRealNumber = quaternion
    -4 + 2i + 3j + 4k
```


## Multiplication

Quaternion multiplication is determined by the products of the basis elements and the distributive law. Recall that multiplication of the basis elements, $i, j$, and $k$, are not commutative, and therefore quaternion multiplication is not commutative.

```
Q1timesQ2 = Q1 * Q2
Q1timesQ2 = quaternion
    -52 + 16i + 54j + 32k
Q2timesQ1 = Q2 * Q1
Q2timesQ1 = quaternion
    -52 + 36i + 14j + 52k
isequal(Q1timesQ2,Q2timesQ1)
ans = logical
    0
```

You can also multiply a quaternion by a real number. If you multiply a quaternion by a real number, each part of the quaternion is multiplied by the real number individually:

```
Q1times5 = Q1*5
Q1times5 = quaternion
    5 + 10i + 15j + 20k
```

Multiplying a quaternion by a real number is commutative.

```
isequal(Q1*5,5*Q1)
ans = logical
    1
```


## Conjugation

The complex conjugate of a quaternion is defined such that each element of the vector portion of the quaternion is negated.

```
Q1
Q1 = quaternion
    1 + 2i + 3j + 4k
conj(Q1)
ans = quaternion
    1-2i - 3j - 4k
```

Multiplication between a quaternion and its conjugate is commutative:

```
isequal(Q1*conj(Q1),conj(Q1)*Q1)
ans = logical
    1
```


## Quaternion Array Manipulation

You can organize quaternions into vectors, matrices, and multidimensional arrays. Built-in MATLAB® functions have been enhanced to work with quaternions.

## Concatenate

Quaternions are treated as individual objects during concatenation and follow MATLAB rules for array manipulation.

```
Q1 = quaternion(1,2,3,4);
Q2 = quaternion(9,8,7,6);
qVector = [Q1,Q2]
qVector = 1x2 quaternion array
    1 + 2i + 3j + 4k 9 + 8i + 7j + 6k
Q3 = quaternion(-1,-2,-3,-4);
Q4 = quaternion(-9,-8,-7,-6);
qMatrix = [qVector;Q3,Q4]
qMatrix = 2x2 quaternion array
    1 + 2i + 3j + 4k 9 + 8i + 7j + 6k
```

```
    -1 - 2i - 3j - 4k -9 - 8i - 7j - 6k
qMultiDimensionalArray(:,:,1) = qMatrix;
qMultiDimensionalArray(:,:,2) = qMatrix
qMultiDimensionalArray = 2x2x2 quaternion array
qMultiDimensionalArray(:,:,1) =
    1+2i + 3j+4k 9 + 8i + 7j + 6k
    -1 - 2i - 3j - 4k -9 - 8i - 7j - 6k
qMultiDimensionalArray(:,:,2) =
    1 + 2i + 3j + 4k 
```


## Indexing

To access or assign elements in a quaternion array, use indexing.

```
qLoc2 = qMultiDimensionalArray(2)
qLoc2 = quaternion
    -1 - 2i - 3j - 4k
```

Replace the quaternion at index two with a quaternion one.

```
qMultiDimensionalArray(2) = ones('quaternion')
qMultiDimensionalArray = 2x2x2 quaternion array
qMultiDimensionalArray(:,:,1) =
    1 + 2i + 3j + 4k 9 + 8i + 7j + 6k
    1 + 0i + 0j + 0k -9 - 8i - 7j - 6k
qMultiDimensionalArray(:,:,2) =
    1 + 2i + 3j + 4k 9 + 8i + 7j + 6k
    -1 - 2i - 3j - 4k -9 - 8i - 7j - 6k
```


## Reshape

To reshape quaternion arrays, use the reshape function.

```
qMatReshaped = reshape(qMatrix,4,1)
qMatReshaped = 4x1 quaternion array
    1 + 2i + 3j + 4k
    -1 - 2i - 3j - 4k
    9 + 8i + 7j + 6k
    -9 - 8i - 7j - 6k
```


## Transpose

To transpose quaternion vectors and matrices, use the transpose function.

```
qMatTransposed = transpose(qMatrix)
qMatTransposed = 2x2 quaternion array
    1 + 2i + 3j + 4k -1 - 2i - 3j - 4k
    9+8i + 7j + 6k -9 - 8i - 7j - 6k
```


## Permute

To permute quaternion vectors, matrices, and multidimensional arrays, use the permute function.

```
qMultiDimensionalArray
qMultiDimensionalArray = 2x2x2 quaternion array
qMultiDimensionalArray(:,:,1) =
    1 + 2i + 3j + 4k 9 + 8i + 7j + 6k
    1 + 0i + 0j + 0k -9 - 8i - 7j - 6k
qMultiDimensionalArray(:,:,2) =
    1 + 2i + 3j + 4k 9 + 8i + 7j + 6k
    -1 - 2i - 3j - 4k -9 - 8i - 7j - 6k
qMatPermute = permute(qMultiDimensionalArray,[3,1,2])
qMatPermute = 2\times2\times2 quaternion array
qMatPermute(:,:,1) =
    1 + 2i + 3j + 4k 1 + 0i + 0j + 0k
    1 + 2i + 3j + 4k -1 - 2i - 3j - 4k
qMatPermute(:,:,2) =
    9 + 8i + 7j + 6k -9 - 8i - 7j - 6k
    9 + 8i + 7j + 6k -9 - 8i - 7j - 6k
```


## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{Tm}}$.

## See Also

## Topics

"Rotations, Orientation, and Quaternions"
"Lowpass Filter Orientation Using Quaternion SLERP"

Introduced in R2019b

## angvel

Angular velocity from quaternion array

## Syntax

AV = angvel(Q,dt,'frame')
AV = angvel(Q,dt,'point')
$[A V, q f]=\operatorname{angvel}(Q, d t, f p, q i)$

## Description

$\mathrm{AV}=\operatorname{angvel}(\mathrm{Q}, \mathrm{dt}$, 'frame') returns the angular velocity array from an array of quaternions, Q. The quaternions in Q correspond to frame rotation. The initial quaternion is assumed to represent zero rotation.
$\mathrm{AV}=\operatorname{angvel}(\mathrm{Q}, \mathrm{dt}$, 'point') returns the angular velocity array from an array of quaternions, Q. The quaternions in Q correspond to point rotation. The initial quaternion is assumed to represent zero rotation.
[AV, $q f]=\operatorname{angvel(Q,dt,fp,qi)~allows~you~to~specify~the~initial~quaternion,~qi,~and~the~type~of~}$ rotation, fp . It also returns the final quaternion, qf .

## Examples

## Generate Angular Velocity From Quaternion Array

Create an array of quaternions.

```
eulerAngles = [(0:10:90).',zeros(numel(0:10:90),2)];
q = quaternion(eulerAngles,'eulerd','ZYX','frame');
```

Specify the time step and generate the angular velocity array.

```
dt = 1;
av = angvel(q,dt,'frame') % units in rad/s
av = 10\times3
```

| 0 | 0 | 0 |
| ---: | ---: | ---: |
| 0 | 0 | 0.1743 |
| 0 | 0 | 0.1743 |
| 0 | 0 | 0.1743 |
| 0 | 0 | 0.1743 |
| 0 | 0 | 0.1743 |
| 0 | 0 | 0.1743 |
| 0 | 0 | 0.1743 |
| 0 | 0 | 0.1743 |
| 0 | 0 | 0.1743 |

## Input Arguments

## Q - Quaternions

$N$-by-1 vector of quaternions
Quaternions, specified as an N -by- 1 vector of quaternions.
Data Types: quaternion

## dt - Time step

nonnegative scalar
Time step, specified as a nonnegative scalar.
Data Types: single | double
fp - Type of rotation
'frame'|'point'
Type of rotation, specified as 'frame' or 'point'.
qi - Initial quaternion
quaternion
Initial quaternion, specified as a quaternion.
Data Types: quaternion

## Output Arguments

AV - Angular velocity
N -by-3 real matrix
Angular velocity, returned as an $N$-by- 3 real matrix. $N$ is the number of quaternions given in the input $Q$. Each row of the matrix corresponds to an angular velocity vector.

## qf - Final quaternion

quaternion
Final quaternion, returned as a quaternion. $q \mathbf{f}$ is the same as the last quaternion in the $Q$ input.
Data Types: quaternion

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

quaternion

## Topics

"Rotations, Orientation, and Quaternions"

Introduced in R2020a

## classUnderlying

Class of parts within quaternion

## Syntax

underlyingClass = classUnderlying(quat)

## Description

underlyingClass = classUnderlying(quat) returns the name of the class of the parts of the quaternion quat.

## Examples

## Get Underlying Class of Quaternion

A quaternion is a four-part hyper-complex number used in three-dimensional representations. The four parts of the quaternion are of data type single or double.

Create two quaternions, one with an underlying data type of single, and one with an underlying data type of double. Verify the underlying data types by calling classUnderlying on the quaternions.

```
qSingle = quaternion(single([1,2,3,4]))
qSingle = quaternion
    1 + 2i + 3j + 4k
classUnderlying(qSingle)
ans =
'single'
qDouble = quaternion([1,2,3,4])
qDouble = quaternion
    1 + 2i + 3j + 4k
classUnderlying(qDouble)
ans =
'double'
```

You can separate quaternions into their parts using the parts function. Verify the parts of each quaternion are the correct data type. Recall that double is the default MATLAB® type.

```
[aS,bS,cS,dS] = parts(qSingle)
aS = single
    1
```

```
bS = single
        2
cS = single
    3
dS = single
    4
[aD,bD,cD,dD] = parts(qDouble)
aD = 1
bD = 2
cD = 3
dD = 4
```

Quaternions follow the same implicit casting rules as other data types in MATLAB. That is, a quaternion with underlying data type single that is combined with a quaternion with underlying data type double results in a quaternion with underlying data type single. Multiply qDouble and qSingle and verify the resulting underlying data type is single.

```
q = qDouble*qSingle;
classUnderlying(q)
ans =
'single'
```


## Input Arguments

## quat - Quaternion to investigate

scalar | vector | matrix | multi-dimensional array
Quaternion to investigate, specified as a quaternion or array of quaternions.
Data Types: quaternion

## Output Arguments

```
underlyingClass - Underlying class of quaternion object
    'single'|'double'
```

Underlying class of quaternion, returned as the character vector 'single' or 'double'.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

## Functions

compact | parts

## Objects

quaternion

## Topics

"Rotations, Orientation, and Quaternions"
Introduced in R2019b

## compact

Convert quaternion array to N -by-4 matrix

## Syntax

matrix $=$ compact(quat)

## Description

matrix = compact(quat) converts the quaternion array, quat, to an $N$-by- 4 matrix. The columns are made from the four quaternion parts. The $i^{\text {th }}$ row of the matrix corresponds to quat (i).

## Examples

## Convert Quaternion Array to Compact Representation of Parts

Create a scalar quaternion with random parts. Convert the parts to a 1 -by- 4 vector using compact.

```
randomParts = randn(1,4)
randomParts = 1×4
    0.5377 1.8339 -2.2588 0.8622
quat = quaternion(randomParts)
quat = quaternion
    0.53767 + 1.8339i - 2.2588j + 0.86217k
quatParts = compact(quat)
quatParts = 1×4
    0.5377 1.8339 -2.2588 0.8622
```

Create a 2-by-2 array of quaternions, then convert the representation to a matrix of quaternion parts. The output rows correspond to the linear indices of the quaternion array.

```
quatArray = [quaternion([1:4;5:8]),quaternion([9:12;13:16])]
quatArray = 2x2 quaternion array
    1 + 2i + 3j + 4k 9 + 10i + 11j + 12k
    5 + 6i + 7j + 8k 13 + 14i + 15j + 16k
quatArrayParts = compact(quatArray)
quatArrayParts = 4×4
```

| 1 | 2 | 3 | 4 |
| ---: | ---: | ---: | ---: |
| 5 | 6 | 7 | 8 |
| 9 | 10 | 11 | 12 |
| 13 | 14 | 15 | 16 |

## Input Arguments

quat - Quaternion to convert
scalar | vector | matrix | multidimensional array
Quaternion to convert, specified as scalar, vector, matrix, or multidimensional array of quaternions.
Data Types: quaternion

## Output Arguments

## matrix - Quaternion in matrix form

$N$-by-4 matrix
Quaternion in matrix form, returned as an $N$-by-4 matrix, where $N=$ numel (quat).
Data Types: single | double

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{Tm}}$.

## See Also

## Functions

parts|classUnderlying
Objects
quaternion
Topics
"Rotations, Orientation, and Quaternions"
Introduced in R2019b

## conj

Complex conjugate of quaternion

## Syntax

quatConjugate $=$ conj(quat)

## Description

quatConjugate $=$ conj(quat) returns the complex conjugate of the quaternion, quat.
If $q=a+b \mathrm{i}+c \mathrm{j}+d \mathrm{k}$, the complex conjugate of $q$ is $q^{*}=a-b \mathrm{i}-c \mathrm{j}-d \mathrm{k}$. Considered as a rotation operator, the conjugate performs the opposite rotation. For example,

```
q = quaternion(deg2rad([16 45 30]),'rotvec');
a = q*
rotatepoint(a,[0,1,0])
ans =
    0 1 0
```


## Examples

## Complex Conjugate of Quaternion

Create a quaternion scalar and get the complex conjugate.

```
q = normalize(quaternion([0.9 0.3 0.3 0.25]))
q = quaternion
    0.87727 + 0.29242i + 0.29242j + 0.24369k
qConj = conj(q)
qConj = quaternion
    0.87727 - 0.29242i - 0.29242j - 0.24369k
```

Verify that a quaternion multiplied by its conjugate returns a quaternion one.

```
q*qConj
ans = quaternion
    1 + 0i + 0j + 0k
```


## Input Arguments

quat - Quaternion
scalar | vector | matrix | multidimensional array
Quaternion to conjugate, specified as a scalar, vector, matrix, or array of quaternions.
Data Types: quaternion

## Output Arguments

quatConjugate - Quaternion conjugate
scalar | vector | matrix | multidimensional array
Quaternion conjugate, returned as a quaternion or array of quaternions the same size as quat.
Data Types: quaternion

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\mathrm{Tm}}$.

## See Also

## Functions

norm|.*,times
Objects
quaternion

## Topics

"Rotations, Orientation, and Quaternions"
Introduced in R2019b

## ctranspose, '

Complex conjugate transpose of quaternion array

## Syntax

quatTransposed = quat'

## Description

quatTransposed $=$ quat' returns the complex conjugate transpose of the quaternion, quat.

## Examples

## Vector Complex Conjugate Transpose

Create a vector of quaternions and compute its complex conjugate transpose.

```
quat = quaternion(randn(4,4))
quat = 4x1 quaternion array
    0.53767 + 0.31877i + 3.5784j + 0.7254k
    1.8339 - 1.3077i + 2.7694j - 0.063055k
    -2.2588 - 0.43359i - 1.3499j + 0.71474k
    0.86217 + 0.34262i + 3.0349j - 0.20497k
quatTransposed = quat'
quatTransposed = 1x4 quaternion array
    0.53767 - 0.31877i - 3.5784j - 0.7254k 1.8339 + 1.3077i - 2.7694j + 0.06305
```


## Matrix Complex Conjugate Transpose

Create a matrix of quaternions and compute its complex conjugate transpose.

```
quat = [quaternion(randn(2,4)),quaternion(randn(2,4))]
quat = 2x2 quaternion array
    0.53767-2.2588i + 0.31877j - 0.43359k 3.5784-1.3499i + 0.7254j + 0.7147
    1.8339 + 0.86217i - 1.3077j + 0.34262k 2.7694 + 3.0349i - 0.063055j - 0.2049
quatTransposed = quat'
quatTransposed = 2x2 quaternion array
    0.53767 + 2.2588i - 0.31877j + 0.43359k 1.8339 - 0.86217i + 1.3077j - 0.3426
        3.5784 + 1.3499i - 0.7254j - 0.71474k 2.7694 - 3.0349i + 0.063055j + 0.2049
```


## Input Arguments

quat - Quaternion to transpose
scalar | vector | matrix
Quaternion to transpose, specified as a vector or matrix or quaternions. The complex conjugate transpose is defined for 1-D and 2-D arrays.
Data Types: quaternion

## Output Arguments

quatTransposed - Conjugate transposed quaternion
scalar | vector | matrix
Conjugate transposed quaternion, returned as an $N$-by- $M$ array, where quat was specified as an $M$ -by- $N$ array.
Data Types: quaternion

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

Functions
transpose, '
Objects
quaternion

## Topics

"Rotations, Orientation, and Quaternions"
Introduced in R2019b

## dist

Angular distance in radians

## Syntax

distance $=$ dist(quatA, quatB)

## Description

distance $=$ dist(quatA, quatB) returns the angular distance in radians between two quaternions, quatA and quatB.

## Examples

## Calculate Quaternion Distance

Calculate the quaternion distance between a single quaternion and each element of a vector of quaternions. Define the quaternions using Euler angles.

```
q = quaternion([0,0,0],'eulerd','zyx','frame')
q = quaternion
    1 + 0i + 0j + 0k
qArray = quaternion([0,45,0;0,90,0;0,180,0;0,-90,0;0,-45,0],'eulerd','zyx','frame')
qArray = 5x1 quaternion array
    0.92388 + 0i + 0.38268j + 0k
    0.70711 + 0i + 0.70711j + 0k
    6.1232e-17 + 0i + 0k
        0.70711 + 0i - 0.70711j + 0k
        0.92388 + 0i - 0.38268j + 0k
quaternionDistance = rad2deg(dist(q,qArray))
quaternionDistance = 5×1
    45.0000
    90.0000
    180.0000
    90.0000
    45.0000
```

If both arguments to dist are vectors, the quaternion distance is calculated between corresponding elements. Calculate the quaternion distance between two quaternion vectors.

```
angles1 = [30,0,15; ...
    30,5,15; ...
```

```
        30,10,15; ...
        30,15,15];
angles2 = [30,6,15; ...
            31,11,15; ...
            30,16,14; ...
            30.5,21,15.5];
qVector1 = quaternion(angles1,'eulerd','zyx','frame');
qVector2 = quaternion(angles2,'eulerd','zyx','frame');
rad2deg(dist(qVector1,qVector2))
ans = 4\times1
    6.0000
    6.0827
    6.0827
    6.0287
```

Note that a quaternion represents the same rotation as its negative. Calculate a quaternion and its negative.

```
qPositive = quaternion([30,45,-60],'eulerd','zyx','frame')
qPositive = quaternion
    0.72332 - 0.53198i + 0.20056j + 0.3919k
qNegative = -qPositive
qNegative = quaternion
    -0.72332 + 0.53198i - 0.20056j - 0.3919k
```

Find the distance between the quaternion and its negative.

```
dist(qPositive,qNegative)
ans = 0
```

The components of a quaternion may look different from the components of its negative, but both expressions represent the same rotation.

## Input Arguments

quat $A$, quatB - Quaternions to calculate distance between
scalar | vector | matrix | multidimensional array
Quaternions to calculate distance between, specified as comma-separated quaternions or arrays of quaternions. quatA and quatB must have compatible sizes:

- size(quatA) == size(quatB), or
- numel (quatA) $==1$, or
- numel(quatB) $==1$, or
- if [Adim1,...,AdimN] = size(quatA) and [Bdim1,...,BdimN] = size(quatB), then for $i=$ 1:N, either Adimi==Bdimi or Adim==1 or Bdim==1.

If one of the quaternion arguments contains only one quaternion, then this function returns the distances between that quaternion and every quaternion in the other argument.

Data Types: quaternion

## Output Arguments

## distance - Angular distance (radians)

scalar | vector | matrix | multidimensional array
Angular distance in radians, returned as an array. The dimensions are the maximum of the union of size(quatA) and size(quatB).

Data Types: single|double

## Algorithms

The dist function returns the angular distance between two quaternions.
A quaternion may be defined by an axis $\left(u_{b}, u_{c}, u_{d}\right)$ and angle of rotation $\theta_{q}$ :
$q=\cos \left(\theta_{q} / 2\right)+\sin \left(\theta_{q} / 2\right)\left(u_{b} \mathrm{i}+u_{c} \mathrm{j}+u_{d} \mathrm{k}\right)$.


Given a quaternion in the form, $q=a+b i+c j+d \mathrm{k}$, where $a$ is the real part, you can solve for the angle of $q$ as $\theta_{q}=2 \cos ^{-1}(a)$.

Consider two quaternions, $p$ and $q$, and the product $z=p^{*}$ conjugate $(q)$. As $p$ approaches $q$, the angle of $z$ goes to 0 , and $z$ approaches the unit quaternion.

The angular distance between two quaternions can be expressed as $\theta_{\mathrm{z}}=2 \cos ^{-1}(\operatorname{real}(z))$.
Using the quaternion data type syntax, the angular distance is calculated as:

```
angularDistance = 2*acos(abs(parts(p*conj(q))));
```


## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

## Functions

parts | conj
Objects
quaternion

## Topics

"Rotations, Orientation, and Quaternions"

Introduced in R2019b

## euler

Convert quaternion to Euler angles (radians)

## Syntax

```
eulerAngles = euler(quat,rotationSequence,rotationType)
```


## Description

eulerAngles = euler(quat,rotationSequence, rotationType) converts the quaternion, quat, to an $N$-by-3 matrix of Euler angles.

## Examples

## Convert Quaternion to Euler Angles in Radians

Convert a quaternion frame rotation to Euler angles in radians using the 'ZYX' rotation sequence.

```
quat = quaternion([0.7071 0.7071 0 0]);
eulerAnglesRandians = euler(quat,'ZYX','frame')
eulerAnglesRandians = 1\times3
```

$$
\begin{array}{lll}
0 & 0 & 1.5708
\end{array}
$$

## Input Arguments

quat - Quaternion to convert to Euler angles
scalar | vector | matrix | multidimensional array
Quaternion to convert to Euler angles, specified as a scalar, vector, matrix, or multidimensional array of quaternions.
Data Types: quaternion
rotationSequence - Rotation sequence
'ZYX'|'ZYZ'|'ZXY'|'ZXZ'|'YXZ'|'YXY'|'YZX'|'XYZ'|'XYX'|'XZY'|'XZX'
Rotation sequence of Euler representation, specified as a character vector or string.
The rotation sequence defines the order of rotations about the axes. For example, if you specify a rotation sequence of 'YZX':

1 The first rotation is about the y-axis.
2 The second rotation is about the new z -axis.
3 The third rotation is about the new x -axis.
Data Types: char|string

## rotationType - Type of rotation

'point'|'frame'
Type of rotation, specified as 'point' or 'frame'.
In a point rotation, the frame is static and the point moves. In a frame rotation, the point is static and the frame moves. Point rotation and frame rotation define equivalent angular displacements but in opposite directions.


Data Types: char|string

## Output Arguments

## eulerAngles - Euler angle representation (radians)

$N$-by-3 matrix
Euler angle representation in radians, returned as a $N$-by- 3 matrix. $N$ is the number of quaternions in the quat argument.

For each row of eulerAngles, the first element corresponds to the first axis in the rotation sequence, the second element corresponds to the second axis in the rotation sequence, and the third element corresponds to the third axis in the rotation sequence.

The data type of the Euler angles representation is the same as the underlying data type of quat.
Data Types: single | double

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

## Functions

eulerd| rotateframe | rotatepoint
Objects
quaternion

## Topics

"Rotations, Orientation, and Quaternions"

Introduced in R2019b

## eulerd

Convert quaternion to Euler angles (degrees)

## Syntax

eulerAngles $=$ eulerd(quat, rotationSequence, rotationType)

## Description

eulerAngles = eulerd(quat, rotationSequence, rotationType) converts the quaternion, quat, to an $N$-by- 3 matrix of Euler angles in degrees.

## Examples

## Convert Quaternion to Euler Angles in Degrees

Convert a quaternion frame rotation to Euler angles in degrees using the 'ZYX' rotation sequence.

```
quat = quaternion([0.7071 0.7071 0 0]);
eulerAnglesDegrees = eulerd(quat,'ZYX','frame')
eulerAnglesDegrees = 1\times3
```

$0 \quad 0 \quad 90.0000$

## Input Arguments

quat - Quaternion to convert to Euler angles
scalar | vector | matrix | multidimensional array
Quaternion to convert to Euler angles, specified as a scalar, vector, matrix, or multidimensional array of quaternions.
Data Types: quaternion
rotationSequence - Rotation sequence
'ZYX'|'ZYZ'|'ZXY'|'ZXZ'|'YXZ'|'YXY'|'YZX'|'XYZ'|'XYX'|'XZY'|'XZX'
Rotation sequence of Euler angle representation, specified as a character vector or string.
The rotation sequence defines the order of rotations about the axes. For example, if you specify a rotation sequence of 'YZX':

1 The first rotation is about the $y$-axis.
2 The second rotation is about the new $z$-axis.
3 The third rotation is about the new $x$-axis.
Data Types: char|string

## rotationType - Type of rotation

'point'|'frame'
Type of rotation, specified as 'point' or 'frame'.
In a point rotation, the frame is static and the point moves. In a frame rotation, the point is static and the frame moves. Point rotation and frame rotation define equivalent angular displacements but in opposite directions.

Point Rotation


Frame Rotation


Data Types: char|string

## Output Arguments

## eulerAngles - Euler angle representation (degrees)

$N$-by-3 matrix
Euler angle representation in degrees, returned as a $N$-by- 3 matrix. $N$ is the number of quaternions in the quat argument.

For each row of eulerAngles, the first column corresponds to the first axis in the rotation sequence, the second column corresponds to the second axis in the rotation sequence, and the third column corresponds to the third axis in the rotation sequence.

The data type of the Euler angles representation is the same as the underlying data type of quat.
Data Types: single | double

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

## Functions

euler| rotateframe | rotatepoint
Objects
quaternion

## Topics

"Rotations, Orientation, and Quaternions"
Introduced in R2019b

## exp

Exponential of quaternion array

## Syntax

$B=\exp (A)$

## Description

$B=\exp (A)$ computes the exponential of the elements of the quaternion array $A$.

## Examples

## Exponential of Quaternion Array

Create a 4-by-1 quaternion array A.

```
A = quaternion(magic(4))
A = 4x1 quaternion array
    16 + 2i + 3j + 13k
        5 + 11i + 10j + 8k
        9 + 7i + 6j + 12k
        4+14i + 15j + 1k
```

Compute the exponential of A.

```
B = exp(A)
B = 4x1 quaternion array
    5.3525e+06 + 1.0516e+06i + 1.5774e+06j + 6.8352e+06k
        -57.359 - 89.189i - 81.081j - 64.865k
        -6799.1 + 2039.1i + 1747.8j + 3495.6k
            -6.66 + 36.931i + 39.569j + 2.6379k
```


## Input Arguments

A - Input quaternion
scalar | vector | matrix | multidimensional array
Input quaternion, specified as a scalar, vector, matrix, or multidimensional array.
Data Types: quaternion

## Output Arguments

B - Result<br>scalar | vector | matrix | multidimensional array

Result of quaternion exponential, returned as a scalar, vector, matrix, or multidimensional array.
Data Types: quaternion

## Algorithms

Given a quaternion $A=a+b \mathrm{i}+c \mathrm{j}+d \mathrm{k}=a+\bar{v}$, the exponential is computed by

$$
\exp (A)=e^{a}\left(\cos \|\bar{v}\|+\frac{\bar{v}}{\|\bar{v}\|} \sin \|\bar{v}\|\right)
$$

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{Tm}}$.

## See Also

## Functions

.^, power | log

## Objects

quaternion

## Topics

"Rotations, Orientation, and Quaternions"
Introduced in R2019b

## Idivide, . $\$

Element-wise quaternion left division

## Syntax

$C=A . \backslash B$

## Description

$\mathrm{C}=\mathrm{A} . \backslash \mathrm{B}$ performs quaternion element-wise division by dividing each element of quaternion B by the corresponding element of quaternion $A$.

## Examples

## Divide a Quaternion Array by a Real Scalar

Create a 2-by-1 quaternion array, and divide it element-by-element by a real scalar.

```
A = quaternion([1:4;5:8])
A = 2x1 quaternion array
    1 + 2i + 3j + 4k
    5 + 6i + 7j + 8k
B = 2;
C = A.\B
C = 2x1 quaternion array
    0.066667 - 0.13333i - 0.2j - 0.26667k
    0.057471 - 0.068966i - 0.08046j - 0.091954k
```


## Divide a Quaternion Array by Another Quaternion Array

Create a 2-by-2 quaternion array, and divide it element-by-element by another 2-by-2 quaternion array.
q1 $=$ quaternion([1:4;2:5;4:7;5:8]);
A = reshape(q1,2,2)
$\mathrm{A}=2 \times 2$ quaternion array
$1+2 i+3 j+4 k \quad 4+5 i+6 j+7 k$
$2+3 i+4 j+5 k \quad 5+6 i+7 j+8 k$
q2 = quaternion(magic(4));
$B=$ reshape(q2,2,2)

```
B = 2x2 quaternion array
    16 + 2i + 3j + 13k 9 + 7i + 6j + 12k
    5+11i + 10j + 8k 4 + 14i + 15j + 1k
```

$C=A . \backslash B$
$C=2 \times 2$ quaternion array

| $2.7-$ | $1.9 i$ | $0.9 j-r$ |
| ---: | ---: | ---: |$\quad 1.7 k$

$1.5159-0.37302 i-0.15079 j-$
$1.2471+0.91379 i-0.33908 j-$

## Input Arguments

## A - Divisor

scalar | vector | matrix | multidimensional array
Divisor, specified as a quaternion, an array of quaternions, a real scalar, or an array of real numbers.
$A$ and $B$ must have compatible sizes. In the simplest cases, they can be the same size or one can be a scalar. Two inputs have compatible sizes if, for every dimension, the dimension sizes of the inputs are the same or one of the dimensions is 1 .

Data Types: quaternion | single | double
B - Dividend
scalar | vector | matrix | multidimensional array
Dividend, specified as a quaternion, an array of quaternions, a real scalar, or an array of real numbers.
$A$ and $B$ must have compatible sizes. In the simplest cases, they can be the same size or one can be a scalar. Two inputs have compatible sizes if, for every dimension, the dimension sizes of the inputs are the same or one of the dimensions is 1.

Data Types: quaternion | single | double

## Output Arguments

## C - Result

scalar | vector | matrix | multidimensional array
Result of quaternion division, returned as a scalar, vector, matrix, or multidimensional array.
Data Types: quaternion

## Algorithms

## Quaternion Division

Given a quaternion $A=a_{1}+a_{2} \mathrm{i}+a_{3} \mathrm{j}+a_{4} \mathrm{k}$ and a real scalar $p$,

$$
C=p . \backslash A=\frac{a_{1}}{p}+\frac{a_{2}}{p} \mathrm{i}+\frac{a_{3}}{p} \mathrm{j}+\frac{a_{4}}{p} \mathrm{k}
$$

Note For a real scalar $p, A . / p=A . \mid p$.

## Quaternion Division by a Quaternion Scalar

Given two quaternions $A$ and $B$ of compatible sizes, then

$$
C=A \cdot \backslash B=A^{-1} \cdot * B=\left(\frac{\operatorname{conj}(A)}{\operatorname{norm}(A)^{2}}\right) \cdot * B
$$

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® $\mathrm{Coder}^{\mathrm{TM}}$.

## See Also

## Functions

.*,times | conj| norm | ./,ldivide

## Objects

quaternion

## Topics

"Rotations, Orientation, and Quaternions"

Introduced in R2019b

## log

Natural logarithm of quaternion array

## Syntax

$B=\log (A)$

## Description

$B=\log (A)$ computes the natural logarithm of the elements of the quaternion array $A$.

## Examples

## Logarithmic Values of Quaternion Array

Create a 3-by-1 quaternion array A.

```
A = quaternion(randn(3,4))
A = 3x1 quaternion array
    0.53767 + 0.86217i - 0.43359j + 2.7694k
    1.8339 + 0.31877i + 0.34262j - 1.3499k
    -2.2588 - 1.3077i + 3.5784j + 3.0349k
```

Compute the logarithmic values of A.
$B=\log (A)$
$B=3 x 1$ quaternion array
$1.0925+0.40848 i-0.20543 j+1.3121 k$
$0.8436+0.14767 i+0.15872 j-0.62533 k$
$1.6807-0.53829 i+1.473 j+1.2493 k$

## Input Arguments

A - Input array
scalar | vector | matrix | multidimensional array
Input array, specified as a scalar, vector, matrix, or multidimensional array.
Data Types: quaternion

## Output Arguments

## $B$ - Logarithm values

scalar | vector | matrix | multidimensional array

Quaternion natural logarithm values, returned as a scalar, vector, matrix, or multidimensional array.
Data Types: quaternion

## Algorithms

Given a quaternion $A=a+\bar{v}=a+b \mathrm{i}+c \mathrm{j}+d \mathrm{k}$, the logarithm is computed by

$$
\log (A)=\log \|A\|+\frac{\bar{v}}{\|\bar{v}\|} \arccos \frac{a}{\|A\|}
$$

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

## Functions

exp|.^, power
Objects
quaternion
Topics
"Rotations, Orientation, and Quaternions"
Introduced in R2019b

## meanrot

Quaternion mean rotation

## Syntax

```
quatAverage = meanrot(quat)
quatAverage = meanrot(quat,dim)
quatAverage = meanrot(
```

$\qquad$

``` ,nanflag)
```


## Description

quatAverage $=$ meanrot(quat) returns the average rotation of the elements of quat along the first array dimension whose size not does equal 1.

- If quat is a vector, meanrot (quat) returns the average rotation of the elements.
- If quat is a matrix, meanrot (quat) returns a row vector containing the average rotation of each column.
- If quat is a multidimensional array, then mearot (quat) operates along the first array dimension whose size does not equal 1 , treating the elements as vectors. This dimension becomes 1 while the sizes of all other dimensions remain the same.

The mean rot function normalizes the input quaternions, quat, before calculating the mean.
quatAverage $=$ meanrot (quat, dim) return the average rotation along dimension dim. For example, if quat is a matrix, then meanrot (quat, 2 ) is a column vector containing the mean of each row.
quatAverage $=$ meanrot $($ $\qquad$ , nanflag) specifies whether to include or omit NaN values from the calculation for any of the previous syntaxes. meanrot (quat, 'includenan') includes all NaN values in the calculation while mean(quat, 'omitnan') ignores them.

## Examples

## Quaternion Mean Rotation

Create a matrix of quaternions corresponding to three sets of Euler angles.

```
eulerAngles = [40 20 10; ...
    50 10 5; ...
    45 70 1];
quat = quaternion(eulerAngles,'eulerd','ZYX','frame');
```

Determine the average rotation represented by the quaternions. Convert the average rotation to Euler angles in degrees for readability.

```
quatAverage = meanrot(quat)
```

```
quatAverage = quaternion
    0.88863 - 0.062598i + 0.27822j + 0.35918k
eulerAverage = eulerd(quatAverage,'ZYX','frame')
eulerAverage = 1×3
    45.7876 32.6452 6.0407
```


## Average Out Rotational Noise

Use mean rot over a sequence of quaternions to average out additive noise.
Create a vector of 1 e 6 quaternions whose distance, as defined by the dist function, from quaternion $(1,0,0,0)$ is normally distributed. Plot the Euler angles corresponding to the noisy quaternion vector.

```
nrows = 1e6;
ax = 2*rand(nrows,3) - 1;
ax = ax./sqrt(sum(ax.^2,2));
ang = 0.5*randn(size(ax,1),1);
q = quaternion(ax.*ang ,'rotvec');
noisyEulerAngles = eulerd(q,'ZYX','frame');
figure(1)
subplot(3,1,1)
plot(noisyEulerAngles(:,1))
title('Z-Axis')
ylabel('Rotation (degrees)')
hold on
subplot(3,1,2)
plot(noisyEulerAngles(:,2))
title('Y-Axis')
ylabel('Rotation (degrees)')
hold on
subplot(3,1,3)
plot(noisyEulerAngles(:,3))
title('X-Axis')
ylabel('Rotation (degrees)')
hold on
```



Use mean rot to determine the average quaternion given the vector of quaternions. Convert to Euler angles and plot the results.

```
qAverage = meanrot(q);
```

qAverageInEulerAngles = eulerd(qAverage,'ZYX','frame');
figure(1)

```
subplot(3,1,1)
plot(ones(nrows,1)*qAverageInEulerAngles(:,1))
title('Z-Axis')
subplot(3,1,2)
plot(ones(nrows,1)*qAverageInEulerAngles(:,2))
title('Y-Axis')
subplot(3,1,3)
plot(ones(nrows,1)*qAverageInEulerAngles(:,3))
title('X-Axis')
```



## The meanrot Algorithm and Limitations

## The meanrot Algorithm

The meanrot function outputs a quaternion that minimizes the squared Frobenius norm of the difference between rotation matrices. Consider two quaternions:

- q0 represents no rotation.
- $q 90$ represents a 90 degree rotation about the $x$-axis.

```
q0 = quaternion([0 0 0],'eulerd','ZYX','frame');
q90 = quaternion([0 0 90],'eulerd','ZYX','frame');
```

Create a quaternion sweep, qSweep, that represents rotations from 0 to 180 degrees about the $x$-axis.

```
eulerSweep = (0:1:180)';
```

qSweep = quaternion([zeros(numel(eulerSweep), 2), eulerSweep], ...
'eulerd','ZYX','frame');

Convert q0, q90, and qSweep to rotation matrices. In a loop, calculate the metric to minimize for each member of the quaternion sweep. Plot the results and return the value of the Euler sweep that corresponds to the minimum of the metric.

```
r0 = rotmat(q0,'frame');
r90 = rotmat(q90,'frame');
```

```
rSweep = rotmat(qSweep,'frame');
metricToMinimize = zeros(size(rSweep,3),1);
for i = 1:numel(qSweep)
    metricToMinimize(i) = norm((rSweep(:,:,i) - r0),'fro').^2 + ...
        norm((rSweep(:,:,i) - r90),'fro').^2;
end
plot(eulerSweep,metricToMinimize)
xlabel('Euler Sweep (degrees)')
ylabel('Metric to Minimize')
```


[~,eulerIndex] = min(metricToMinimize);
eulerSweep(eulerIndex)
ans $=45$
The minimum of the metric corresponds to the Euler angle sweep at 45 degrees. That is, meanrot defines the average between quaterion([0 0 0],' ZYX','frame') and quaternion([0 0 90],'ZYX','frame') as quaternion([0 0 45],'ZYX','frame'). Call meanrot with q0 and q90 to verify the same result.

```
eulerd(meanrot([q0,q90]),'ZYX','frame')
ans = 1\times3
```

0
045.0000

## Limitations

The metric that meanrot uses to determine the mean rotation is not unique for quaternions significantly far apart. Repeat the experiment above for quaternions that are separated by 180 degrees.

```
q180 = quaternion([0 0 180],'eulerd','ZYX','frame');
r180 = rotmat(q180,'frame');
for i = 1:numel(qSweep)
    metricToMinimize(i) = norm((rSweep(:,:,i) - r0),'fro').^2 + ...
                        norm((rSweep(:,:,i) - r180),'fro').^2;
end
plot(eulerSweep,metricToMinimize)
xlabel('Euler Sweep (degrees)')
ylabel('Metric to Minimize')
```


[~,eulerIndex] = min(metricToMinimize); eulerSweep(eulerIndex)
ans $=159$

Quaternion means are usually calculated for rotations that are close to each other, which makes the edge case shown in this example unlikely in real-world applications. To average two quaternions that are significantly far apart, use the slerp function. Repeat the experiment using slerp and verify that the quaternion mean returned is more intuitive for large distances.

```
qMean = slerp(q0,q180,0.5);
q0_q180 = eulerd(qMean,'ZYX','frame')
q0_q180 = 1×3
    0 0 90.0000
```


## Input Arguments

## quat - Quaternion

scalar | vector | matrix | multidimensional array
Quaternion for which to calculate the mean, specified as a scalar, vector, matrix, or multidimensional array of quaternions.
Data Types: quaternion

## dim - Dimension to operate along

positive integer scalar
Dimension to operate along, specified as a positive integer scalar. If no value is specified, then the default is the first array dimension whose size does not equal 1.

Dimension dim indicates the dimension whose length reduces to 1 . The size(quatAverage, dim) is 1, while the sizes of all other dimensions remain the same.
Data Types: double | single

## nanflag - NaN condition

'includenan' (default) |'omitnan'
NaN condition, specified as one of these values:

- 'includenan ' -- Include NaN values when computing the mean rotation, resulting in NaN .
- 'omitnan' -- Ignore all NaN values in the input.

Data Types: char | string

## Output Arguments

## quatAverage - Quaternion average rotation

scalar | vector | matrix | multidimensional array
Quaternion average rotation, returned as a scalar, vector, matrix, or multidimensional array.
Data Types: single | double

## Algorithms

mean rot determines a quaternion mean, $\bar{q}$, according to [1]. $\bar{q}$ is the quaternion that minimizes the squared Frobenius norm of the difference between rotation matrices:

$$
\bar{q}=\arg \min _{q \in \mathrm{~S}^{3}} \sum_{i=1}^{n}\left\|A(q)-A\left(q_{i}\right)\right\|_{F}^{2}
$$

## References

[1] Markley, F. Landis, Yang Chen, John Lucas Crassidis, and Yaakov Oshman. "Average Quaternions." Journal of Guidance, Control, and Dynamics. Vol. 30, Issue 4, 2007, pp. 1193-1197.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder ${ }^{\text {TM }}$.

## See Also

## Functions

dist|slerp
Objects
quaternion
Topics
"Rotations, Orientation, and Quaternions"

Introduced in R2019b

## minus, -

Quaternion subtraction

## Syntax

$C=A-B$

## Description

$C=A-B$ subtracts quaternion $B$ from quaternion $A$ using quaternion subtraction. Either $A$ or $B$ may be a real number, in which case subtraction is performed with the real part of the quaternion argument.

## Examples

## Subtract a Quaternion from a Quaternion

Quaternion subtraction is defined as the subtraction of the corresponding parts of each quaternion. Create two quaternions and perform subtraction.

Q1 = quaternion([1,0, -2, 7]);
Q2 = quaternion([1, 2, 3, 4]);
Q1minusQ2 = Q1 - Q2
Q1minusQ2 = quaternion
0-2i - $5 \mathrm{j}+3 \mathrm{k}$

## Subtract a Real Number from a Quaternion

Addition and subtraction of real numbers is defined for quaternions as acting on the real part of the quaternion. Create a quaternion and then subtract 1 from the real part.

Q = quaternion([1, $1,1,1]$ )
Q = quaternion
1 + 1i + 1j + 1k

Qminus1 = Q - 1
Qminusl = quaternion
$0+1 i+1 j+1 k$

## Input Arguments

## A - Input

scalar | vector $\mid$ matrix $\mid$ multidimensional array
Input, specified as a quaternion, array of quaternions, real number, or array of real numbers.
Data Types: quaternion | single | double
B - Input
scalar | vector | matrix | multidimensional array
Input, specified as a quaternion, array of quaternions, real number, or array of real numbers.
Data Types: quaternion | single | double

## Output Arguments

## C - Result

scalar | vector | matrix | multidimensional array
Result of quaternion subtraction, returned as a scalar, vector, matrix, or multidimensional array of quaternions.

Data Types: quaternion

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

## Functions

-,uminus|.*,times|*,mtimes

## Objects

quaternion

## Topics

"Rotations, Orientation, and Quaternions"
Introduced in R2019b

## mtimes, *

Quaternion multiplication

## Syntax

quat $C=A * B$

## Description

quat $C=A * B$ implements quaternion multiplication if either $A$ or $B$ is a quaternion. Either $A$ or $B$ must be a scalar.

You can use quaternion multiplication to compose rotation operators:

- To compose a sequence of frame rotations, multiply the quaternions in the order of the desired sequence of rotations. For example, to apply a $p$ quaternion followed by a $q$ quaternion, multiply in the order $p q$. The rotation operator becomes $(p q)^{*} v(p q)$, where $v$ represents the object to rotate specified in quaternion form. * represents conjugation.
- To compose a sequence of point rotations, multiply the quaternions in the reverse order of the desired sequence of rotations. For example, to apply a $p$ quaternion followed by a $q$ quaternion, multiply in the reverse order, $q p$. The rotation operator becomes $(q p) v(q p)^{*}$.


## Examples

## Multiply Quaternion Scalar and Quaternion Vector

Create a 4-by-1 column vector, A, and a scalar, b. Multiply A times b.

```
A = quaternion(randn(4,4))
A = 4x1 quaternion array
    0.53767 + 0.31877i + 3.5784j + 0.7254k
        1.8339 - 1.3077i + 2.7694j - 0.063055k
    -2.2588 - 0.43359i - 1.3499j + 0.71474k
    0.86217 + 0.34262i + 3.0349j - 0.20497k
b = quaternion(randn(1,4))
b = quaternion
    -0.12414 + 1.4897i + 1.409j + 1.4172k
C = A*b
C = 4x1 quaternion array
\begin{tabular}{rrrr}
-6.6117 & \(4.8105 i\) & \(+0.94224 j-\) & \(4.2097 k\) \\
\(-2.0925+\) & \(6.9079 i+3.9995 j-\) & \(3.3614 k\) \\
\(1.8155-6.2313 i\) & \(1.336 j-\) & \(1.89 k\) \\
\(-4.6033+\) & \(5.8317 i\) & \(0.047161 j-\) & \(2.791 k\)
\end{tabular}
```


## Input Arguments

## A - Input

scalar | vector | matrix | multidimensional array
Input to multiply, specified as a quaternion, array of quaternions, real scalar, or array of real scalars.
If B is nonscalar, then A must be scalar.
Data Types: quaternion | single | double
B - Input
scalar | vector | matrix | multidimensional array
Input to multiply, specified as a quaternion, array of quaternions, real scalar, or array of real scalars.
If $A$ is nonscalar, then $B$ must be scalar.
Data Types: quaternion | single | double

## Output Arguments

## quatC - Quaternion product

scalar | vector | matrix | multidimensional array
Quaternion product, returned as a quaternion or array of quaternions.
Data Types: quaternion

## Algorithms

## Quaternion Multiplication by a Real Scalar

Given a quaternion

$$
q=a_{\mathrm{q}}+b_{\mathrm{q}} \mathrm{i}+c_{\mathrm{q}} \mathrm{j}+d_{\mathrm{q}} \mathrm{k},
$$

the product of $q$ and a real scalar $\beta$ is

$$
\beta q=\beta a_{\mathrm{q}}+\beta b_{\mathrm{q}} \mathrm{i}+\beta c_{\mathrm{q}} \mathrm{j}+\beta d_{\mathrm{q}} \mathrm{k}
$$

## Quaternion Multiplication by a Quaternion Scalar

The definition of the basis elements for quaternions,

$$
\mathrm{i}^{2}=\mathrm{j}^{2}=\mathrm{k}^{2}=\mathrm{ijk}=-1,
$$

can be expanded to populate a table summarizing quaternion basis element multiplication:

|  | $\mathbf{1}$ | $\mathbf{i}$ | $\mathbf{j}$ | $\mathbf{k}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | 1 | i | j | k |
| $\mathbf{i}$ | i | -1 | k | -j |


| $\mathbf{j}$ | j | -k | -1 | i |
| :--- | :--- | :--- | :--- | :--- |
| $\mathbf{k}$ | k | j | -i | -1 |

When reading the table, the rows are read first, for example: $\mathrm{ij}=\mathrm{k}$ and $\mathrm{ji}=-\mathrm{k}$.
Given two quaternions, $q=a_{\mathrm{q}}+b_{\mathrm{q}} \mathrm{i}+c_{\mathrm{q}} \mathrm{j}+d_{\mathrm{q}} \mathrm{k}$, and $p=a_{\mathrm{p}}+b_{\mathrm{p}} \mathrm{i}+c_{\mathrm{p}} \mathrm{j}+d_{\mathrm{p}} \mathrm{k}$, the multiplication can be expanded as:

$$
\begin{aligned}
z= & p q=\left(a_{\mathrm{p}}+b_{\mathrm{p}} \mathrm{i}+c_{\mathrm{p}} \mathrm{j}+d_{\mathrm{p}} \mathrm{k}\right)\left(a_{\mathrm{q}}+b_{\mathrm{q}} \mathrm{i}+c_{\mathrm{q}} \mathrm{j}+d_{\mathrm{q}} \mathrm{k}\right) \\
& =a_{\mathrm{p}} a_{\mathrm{q}}+a_{\mathrm{p}} b_{\mathrm{q}} \mathrm{i}+a_{\mathrm{p}} c_{\mathrm{q}} \mathrm{j}+a_{\mathrm{p}} d_{\mathrm{q}} \mathrm{k} \\
& +b_{\mathrm{p}} a_{\mathrm{q}} \mathrm{i}+b_{\mathrm{p}} b_{\mathrm{q}} \mathrm{i}^{2}+b_{\mathrm{p}} c_{\mathrm{q}} \mathrm{j}+b_{\mathrm{p}} d_{\mathrm{q}} \mathrm{i} \mathrm{k} \\
& +c_{\mathrm{p}} a_{\mathrm{q}} \mathrm{j}+c_{\mathrm{p}} b_{\mathrm{q}} \mathrm{ji}+c_{\mathrm{p}} c_{\mathrm{q}} \mathrm{j}^{2}+c_{\mathrm{p}} d_{\mathrm{q}} \mathrm{jk} \\
& +d_{\mathrm{p}} a_{\mathrm{q}} k+d_{\mathrm{p}} b_{\mathrm{q}} \mathrm{ki}+d_{\mathrm{p}} c_{\mathrm{q}} \mathrm{kj}+d_{\mathrm{p}} d_{\mathrm{q}^{2}} \mathrm{k}^{2}
\end{aligned}
$$

You can simplify the equation using the quaternion multiplication table:

$$
\begin{aligned}
z= & p q=a_{\mathrm{p}} a_{\mathrm{q}}+a_{\mathrm{p}} b_{\mathrm{q}} \mathrm{i}+a_{\mathrm{p}} c_{\mathrm{q}} \mathrm{j}+a_{\mathrm{p}} d_{\mathrm{q}} \mathrm{k} \\
& +b_{\mathrm{p}} a_{\mathrm{q}} \mathrm{i}-b_{\mathrm{p}} b_{\mathrm{q}}+b_{\mathrm{p}} c_{\mathrm{q}} \mathrm{k}-b_{\mathrm{p}} d_{\mathrm{q}} \mathrm{j} \\
& +c_{\mathrm{p}} a_{\mathrm{q}} \mathrm{j}-c_{\mathrm{p}} b_{\mathrm{q}} \mathrm{k}-c_{\mathrm{p}} c_{\mathrm{q}}+c_{\mathrm{p}} d_{\mathrm{q}^{\mathrm{i}}} \\
& +d_{\mathrm{p}} a_{\mathrm{q}} k+d_{\mathrm{p}} b_{\mathrm{q}} \mathrm{j}-d_{\mathrm{p}} c_{\mathrm{q}} \mathrm{i}-d_{\mathrm{p}} d_{\mathrm{q}}
\end{aligned}
$$

## References

[1] Kuipers, Jack B. Quaternions and Rotation Sequences: A Primer with Applications to Orbits, Aerospace, and Virtual Reality. Princeton, NJ: Princeton University Press, 2007.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

## Functions

.*,times

## Objects

quaternion

## Topics

"Rotations, Orientation, and Quaternions"

## Introduced in R2019b

## norm

Quaternion norm

## Syntax

$\mathrm{N}=$ norm(quat)

## Description

$\mathrm{N}=$ norm(quat) returns the norm of the quaternion, quat.
Given a quaternion of the form $Q=a+b \mathrm{i}+c \mathrm{j}+d \mathrm{k}$, the norm of the quaternion is defined as $\operatorname{norm}(Q)=\sqrt{a^{2}+b^{2}+c^{2}+d^{2}}$.

## Examples

## Calculate Quaternion Norm

Create a scalar quaternion and calculate its norm.

```
quat = quaternion(1,2,3,4);
norm(quat)
ans = 5.4772
```

The quaternion norm is defined as the square root of the sum of the quaternion parts squared. Calculate the quaternion norm explicitly to verify the result of the norm function.

```
[a,b,c,d] = parts(quat);
sqrt(a^2+b^2++\mp@subsup{c}{}{\wedge}2+\mp@subsup{d}{}{\wedge}2)
ans = 5.4772
```


## Input Arguments

## quat - Quaternion

scalar | vector | matrix | multidimensional array
Quaternion for which to calculate the norm, specified as a scalar, vector, matrix, or multidimensional array of quaternions.

Data Types: quaternion

## Output Arguments

## N - Quaternion norm

scalar | vector | matrix | multidimensional array

Quaternion norm. If the input quat is an array, the output is returned as an array the same size as quat. Elements of the array are real numbers with the same data type as the underlying data type of the quaternion, quat.
Data Types: single|double

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.

## See Also

## Functions

normalize | parts | conj
Objects
quaternion

## Topics

"Rotations, Orientation, and Quaternions"

Introduced in R2019b

## normalize

Quaternion normalization

## Syntax

quatNormalized = normalize(quat)

## Description

quatNormalized $=$ normalize(quat) normalizes the quaternion.
Given a quaternion of the form $Q=a+b \mathrm{i}+c \mathrm{j}+d \mathrm{k}$, the normalized quaternion is defined as $Q / \sqrt{a^{2}+b^{2}+c^{2}+d^{2}}$.

## Examples

## Normalize Elements of Quaternion Vector

Quaternions can represent rotations when normalized. You can use normalize to normalize a scalar, elements of a matrix, or elements of a multi-dimensional array of quaternions. Create a column vector of quaternions, then normalize them.

```
quatArray = quaternion([1,2,3,4; ...
    2,3,4,1; ...
    3,4,1,2]);
quatArrayNormalized = normalize(quatArray)
quatArrayNormalized = 3x1 quaternion array
    0.18257 + 0.36515i + 0.54772j + 0.7303k
    0.36515 + 0.54772i + 0.7303j + 0.18257k
    0.54772 + 0.7303i + 0.18257j + 0.36515k
```


## Input Arguments

## quat - Quaternion to normalize

scalar | vector | matrix | multidimensional array
Quaternion to normalize, specified as a scalar, vector, matrix, or multidimensional array of quaternions.
Data Types: quaternion

## Output Arguments

## quatNormalized - Normalized quaternion

scalar | vector | matrix | multidimensional array

Normalized quaternion, returned as a quaternion or array of quaternions the same size as quat.
Data Types: quaternion

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{rm}}$.

## See Also

## Functions

norm|.*,times | conj
Objects
quaternion
Topics
"Rotations, Orientation, and Quaternions"

Introduced in R2019b

## ones

Create quaternion array with real parts set to one and imaginary parts set to zero

## Syntax

```
quatOnes = ones('quaternion')
quatOnes = ones(n,'quaternion')
quatOnes = ones(sz,'quaternion')
quatOnes = ones(sz1,...,szN,'quaternion')
quatOnes = ones(
```

$\qquad$

``` ,'like',prototype,'quaternion')
```


## Description

quatOnes $=$ ones('quaternion') returns a scalar quaternion with the real part set to 1 and the imaginary parts set to 0 .

Given a quaternion of the form $Q=a+b \mathrm{i}+c \mathrm{j}+d \mathrm{k}$, a quaternion one is defined as $Q=1+0 \mathrm{i}+0 \mathrm{j}+0 \mathrm{k}$.
quatOnes $=$ ones ( n, ' quaternion') returns an n -by-n quaternion matrix with the real parts set to 1 and the imaginary parts set to 0 .
quatOnes $=$ ones(sz,'quaternion') returns an array of quaternion ones where the size vector, sz, defines size(qOnes).
Example: ones ([1, 4, 2], 'quaternion') returns a 1-by-4-by-2 array of quaternions with the real parts set to 1 and the imaginary parts set to 0 .
quatOnes $=$ ones(sz1, ...,szN, 'quaternion') returns a sz1-by-...-by-szN array of ones where $\mathrm{sz1}, \ldots, \mathrm{szN}$ indicates the size of each dimension.
quatOnes = ones( $\qquad$ ,'like',prototype,'quaternion') specifies the underlying class of the returned quaternion array to be the same as the underlying class of the quaternion prototype.

## Examples

## Quaternion Scalar One

Create a quaternion scalar one.

```
quatOnes = ones('quaternion')
quatOnes = quaternion
    1 + 0i + 0j + 0k
```


## Square Matrix of Quaternion Ones

Create an $n$-by-n matrix of quaternion ones.
n = 3;
quatOnes $=$ ones( n, 'quaternion')
quatOnes $=3 \times 3$ quaternion array

| $1+0 i+0 j+0 k$ | $1+0 i+0 j+0 k$ | $1+0 i+0 j+0 k$ |
| :--- | :--- | :--- |
| $1+0 i+0 j+0 k$ | $1+0 i+0 j+0 k$ | $1+0 i+0 j+0 k$ |
| $1+0 i+0 j+0 k$ | $1+0 i+0 j+0 k$ | $1+0 i+0 j+0 k$ |

## Multidimensional Array of Quaternion Ones

Create a multidimensional array of quaternion ones by defining array dimensions in order. In this example, you create a 3-by-1-by-2 array. You can specify dimensions using a row vector or commaseparated integers. Specify the dimensions using a row vector and display the results:

```
dims = [3,1,2];
quatOnesSyntax1 = ones(dims,'quaternion')
quatOnesSyntax1 = 3x1x2 quaternion array
quatOnesSyntax1(:,:,1) =
    1 + 0i + 0j + 0k
    1 + 0i + 0j + 0k
    1 + 0i + 0j + 0k
quatOnesSyntax1(:,:,2) =
    1 + 0i + 0j + 0k
    1 + 0i + 0j + 0k
    1 + 0i + 0j + 0k
```

Specify the dimensions using comma-separated integers, and then verify the equivalency of the two syntaxes:

```
quatOnesSyntax2 = ones(3,1,2,'quaternion');
isequal(quatOnesSyntax1,quatOnesSyntax2)
ans = logical
    1
```


## Underlying Class of Quaternion Ones

A quaternion is a four-part hyper-complex number used in three-dimensional rotations and orientations. You can specify the underlying data type of the parts as single or double. The default is double.

Create a quaternion array of ones with the underlying data type set to single.

```
quatOnes = ones(2,'like',single(1),'quaternion')
```

quatOnes $=2 \times 2$ quaternion array

```
    1 + 0i + 0j + 0k 1 + 0i + 0j + 0k
```

    \(1+0 i+0 j+0 k \quad 1+0 i+0 j+0 k\)
    Verify the underlying class using the classUnderlying function.

```
classUnderlying(quatOnes)
ans =
'single'
```


## Input Arguments

## n - Size of square quaternion matrix

integer value
Size of square quaternion matrix, specified as an integer value.
If n is zero or negative, then quatOnes is returned as an empty matrix.
Example: ones (4, 'quaternion') returns a 4-by-4 matrix of quaternions with the real parts set to 1 and the imaginary parts set to 0 .

Data Types: single | double | int8 | int16 | int32 | int64 | uint8 | uint16| uint32 | uint64

## sz - Output size

row vector of integer values
Output size, specified as a row vector of integer values. Each element of sz indicates the size of the corresponding dimension in quatOnes. If the size of any dimension is 0 or negative, then quatOnes is returned as an empty array.
Data Types: single | double | int8 | int16 | int32 | int64 | uint8 | uint16|uint32 |uint64

## prototype - Quaternion prototype

variable
Quaternion prototype, specified as a variable.
Example: ones(2,'like',quat,' quaternion') returns a 2-by-2 matrix of quaternions with the same underlying class as the prototype quaternion, quat.
Data Types: quaternion

## sz1, ...,szN - Size of each dimension

two or more integer values
Size of each dimension, specified as two or more integers. If the size of any dimension is 0 or negative, then quatOnes is returned as an empty array.
Example: ones ( 2,3 , 'quaternion' ) returns a 2 -by- 3 matrix of quaternions with the real parts set to 1 and the imaginary parts set to 0 .

Data Types: single|double | int8| int16|int32|int64|uint8|uint16|uint32|uint64

## Output Arguments

## quat0nes - Quaternion ones

scalar | vector | matrix | multidimensional array
Quaternion ones, returned as a scalar, vector, matrix, or multidimensional array of quaternions.
Given a quaternion of the form $Q=a+b \mathrm{i}+c \mathrm{j}+d \mathrm{k}$, a quaternion one is defined as $Q=1+0 \mathrm{i}+0 \mathrm{j}+0 \mathrm{k}$.

Data Types: quaternion

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® $\mathrm{Coder}^{\mathrm{TM}}$.

## See Also

Functions
zeros
Objects
quaternion

## Topics

"Rotations, Orientation, and Quaternions"

Introduced in R2019b

## parts

Extract quaternion parts

## Syntax

[a,b, c,d] = parts(quat)

## Description

[ $a, b, c, d]=$ parts(quat) returns the parts of the quaternion array as arrays, each the same size as quat.

## Examples

## Convert Quaternion to Matrix of Quaternion Parts

Convert a quaternion representation to parts using the parts function.
Create a two-element column vector of quaternions by specifying the parts.

```
quat = quaternion([1:4;5:8])
quat = 2x1 quaternion array
    1 + 2i + 3j + 4k
    5 + 6i + 7j + 8k
```

Recover the parts from the quaternion matrix using the parts function. The parts are returned as separate output arguments, each the same size as the input 2-by-1 column vector of quaternions.

```
[qA,qB,qC,qD] = parts(quat)
qA = 2 x 1
    1
    5
qB = 2×1
    2
    6
qC = 2×1
    3
    7
qD = 2×1
```


## Input Arguments

quat - Quaternion
scalar | vector | matrix | multidimensional array
Quaternion, specified as a quaternion or array of quaternions.
Data Types: quaternion

## Output Arguments

[a,b,c,d]-Quaternion parts
scalar | vector | matrix | multidimensional array
Quaternion parts, returned as four arrays: a, b, c, and d. Each part is the same size as quat.
Data Types: single | double

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

Functions
classUnderlying|compact
Objects
quaternion

## Topics

"Rotations, Orientation, and Quaternions"
Introduced in R2019b

## power, .^

Element-wise quaternion power

## Syntax

$\mathrm{C}=\mathrm{A} \cdot \wedge \mathrm{b}$

## Description

$\mathrm{C}=\mathrm{A} .{ }^{\wedge} \mathrm{b}$ raises each element of A to the corresponding power in b .

## Examples

## Raise a Quaternion to a Real Scalar Power

Create a quaternion and raise it to a real scalar power.

```
\(\mathrm{A}=\) quaternion(1, \(2,3,4\) )
A = quaternion
    \(1+2 i+3 j+4 k\)
b \(=3\);
\(\mathrm{C}=\mathrm{A} \cdot \wedge \mathrm{B}\)
\(C=\) quaternion
    -86-52i - 78j - 104k
```


## Raise a Quaternion Array to Powers from a Multidimensional Array

Create a 2-by-1 quaternion array and raise it to powers from a 2-D array.

```
A = quaternion([1:4;5:8])
A \(=2 x 1\) quaternion array
    \(1+2 i+3 j+4 k\)
    \(5+6 i+7 j+8 k\)
\(\mathrm{b}=\left[\begin{array}{lllll}1 & 0 & 2 ; & 3 & 2\end{array}\right]\)
b \(=2 \times 3\)
    \(\begin{array}{lll}1 & 0 & 2 \\ 3 & 2 & 1\end{array}\)
\(C=A \cdot{ }^{\wedge} b\)
```

```
C = 2x3 quaternion array
```



## Input Arguments

A - Base
scalar | vector | matrix | multidimensional array
Base, specified as a scalar, vector, matrix, or multidimensional array.
Data Types: quaternion | single | double
b - Exponent
scalar | vector | matrix | multidimensional array
Exponent, specified as a real scalar, vector, matrix, or multidimensional array.
Data Types: single | double

## Output Arguments

## C - Result <br> scalar | vector | matrix | multidimensional array

Each element of quaternion A raised to the corresponding power in b, returned as a scalar, vector, matrix, or multidimensional array.

Data Types: quaternion

## Algorithms

The polar representation of a quaternion $A=a+b \mathrm{i}+c \mathrm{j}+d \mathrm{k}$ is given by

$$
A=\|A\|(\cos \theta+\widehat{u} \sin \theta)
$$

where $\theta$ is the angle of rotation, and $\hat{u}$ is the unit quaternion.
Quaternion $A$ raised by a real exponent $b$ is given by

$$
P=A .^{\wedge} b=\|A\|^{b}(\cos (b \theta)+\widehat{u} \sin (b \theta))
$$

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

Functions
log | exp

## Objects

quaternion

## Topics

"Rotations, Orientation, and Quaternions"

Introduced in R2019b

## prod

Product of a quaternion array

## Syntax

```
quatProd = prod(quat)
quatProd = prod(quat,dim)
```


## Description

quatProd $=$ prod(quat) returns the quaternion product of the elements of the array.
quatProd $=$ prod(quat, dim) calculates the quaternion product along dimension dim.

## Examples

## Product of Quaternions in Each Column

Create a 3-by-3 array whose elements correspond to their linear indices.

```
A = reshape(quaternion(randn(9,4)),3,3)
```

```
A = 3x3 quaternion array
    0.53767 + 2.7694i + 1.409j - 0.30344k 0.86217 + 0.7254i - 1.2075j + 0.888
    1.8339 - 1.3499i + 1.4172j + 0.29387k 0.31877 - 0.063055i + 0.71724j - 1.147%
    -2.2588 + 3.0349i + 0.6715j - 0.78728k -1.3077 + 0.71474i + 1.6302j - 1.068
```

Find the product of the quaternions in each column. The length of the first dimension is 1 , and the length of the second dimension matches size ( $\mathrm{A}, 2$ ).

```
B = prod(A)
B = 1x3 quaternion array
    -19.837 - 9.1521i + 15.813j - 19.918k -5.4708 - 0.28535i + 3.077j - 1.2295k
```


## Product of Specified Dimension of Quaternion Array

You can specify which dimension of a quaternion array to take the product of.
Create a 2-by-2-by-2 quaternion array.
$A=r e s h a p e(q u a t e r n i o n(r a n d n(8,4)), 2,2,2) ;$
Find the product of the elements in each page of the array. The length of the first dimension matches $\operatorname{size}(A, 1)$, the length of the second dimension matches $\operatorname{size}(A, 2)$, and the length of the third dimension is 1 .

```
dim = 3;
B = prod(A,dim)
B = 2x2 quaternion array
    -2.4847 + 1.1659i - 0.37547j + 2.8068k 0.28786 - 0.29876i - 0.51231j - 4.2972k
    0.38986-3.6606i - 2.0474j - 6.047k -1.741 - 0.26782i + 5.4346j + 4.1452k
```


## Input Arguments

## quat - Quaternion

scalar | vector | matrix | multidimensional array
Quaternion, specified as scalar, vector, matrix, or multidimensional array of quaternions.
Example: qProd $=$ prod(quat) calculates the quaternion product along the first non-singleton dimension of quat.
Data Types: quaternion

## dim - Dimension

first non-singleton dimension (default) | positive integer
Dimension along which to calculate the quaternion product, specified as a positive integer. If dim is not specified, prod operates along the first non-singleton dimension of quat.
Data Types: single | double | int8 | int16 | int32 | int64 | uint8 | uint16|uint32 |uint64

## Output Arguments

quatProd - Quaternion product
positive integer
Quaternion product, returned as quaternion array with one less non-singleton dimension than quat.
For example, if quat is a 2-by-2-by-5 array,

- prod(quat, 1) returns a 1-by-2-by-5 array.
- prod(quat, 2 ) returns a 2-by-1-by-5 array.
- prod(quat,3) returns a 2-by-2 array.

Data Types: quaternion

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

Functions
mtimes|.*,times

## Objects

quaternion

## Topics

"Rotations, Orientation, and Quaternions"

Introduced in R2019b

## rdivide, ./

Element-wise quaternion right division

## Syntax

$C=A . / B$

## Description

$\mathrm{C}=\mathrm{A} . / \mathrm{B}$ performs quaternion element-wise division by dividing each element of quaternion A by the corresponding element of quaternion $B$.

## Examples

## Divide a Quaternion Array by a Real Scalar

Create a 2-by-1 quaternion array, and divide it element-by-element by a real scalar.

```
A = quaternion([1:4;5:8])
A = 2x1 quaternion array
    1 + 2i + 3j + 4k
    5 + 6i + 7j + 8k
B = 2;
C = A./B
C = 2x1 quaternion array
    0.5 + 1i + 1.5j + 2k
    2.5 + 3i + 3.5j + 4k
```


## Divide a Quaternion Array by Another Quaternion Array

Create a 2-by-2 quaternion array, and divide it element-by-element by another 2-by-2 quaternion array.
q1 = quaternion(magic(4));
A = reshape(q1,2,2)
$\mathrm{A}=2 \times 2$ quaternion array
$16+2 i+3 j+13 k \quad 9+7 i+6 j+12 k$ $5+11 i+10 j+8 k \quad 4+14 i+15 j+1 k$

```
q2 = quaternion([1:4;3:6;2:5;4:7]);
```

$B=$ reshape $(q 2,2,2)$

```
B = 2x2 quaternion array
    1 + 2i + 3j + 4k 2 + 3i + 4j + 5k
    3+4i + 5j + 6k 4 + 5i + 6j + 7k
```

$C=A . / B$
$C=2 \times 2$ quaternion array


## Input Arguments

## A - Dividend

scalar | vector | matrix | multidimensional array
Dividend, specified as a quaternion, an array of quaternions, a real scalar, or an array of real numbers.
$A$ and $B$ must have compatible sizes. In the simplest cases, they can be the same size or one can be a scalar. Two inputs have compatible sizes if, for every dimension, the dimension sizes of the inputs are the same or one of the dimensions is 1.

Data Types: quaternion | single | double
B - Divisor
scalar | vector | matrix | multidimensional array
Divisor, specified as a quaternion, an array of quaternions, a real scalar, or an array of real numbers.
$A$ and $B$ must have compatible sizes. In the simplest cases, they can be the same size or one can be a scalar. Two inputs have compatible sizes if, for every dimension, the dimension sizes of the inputs are the same or one of the dimensions is 1.
Data Types: quaternion | single | double

## Output Arguments

## C - Result

scalar | vector | matrix | multidimensional array
Result of quaternion division, returned as a scalar, vector, matrix, or multidimensional array.
Data Types: quaternion

## Algorithms

## Quaternion Division

Given a quaternion $A=a_{1}+a_{2} \mathrm{i}+a_{3} \mathrm{j}+a_{4} \mathrm{k}$ and a real scalar p ,

$$
C=A . / p=\frac{a_{1}}{p}+\frac{a_{2}}{p} \mathrm{i}+\frac{a_{3}}{p} \mathrm{j}+\frac{a_{4}}{p} \mathrm{k}
$$

Note For a real scalar $p, A . / p=A . \mid p$.

## Quaternion Division by a Quaternion Scalar

Given two quaternions $A$ and $B$ of compatible sizes,

$$
C=A \cdot / B=A \cdot * B^{-1}=A \cdot *\left(\frac{\operatorname{conj}(B)}{\operatorname{norm}(B)^{2}}\right)
$$

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

## Functions

conj|./,ldivide|norm|.*,times
Objects
quaternion

## Topics

"Rotations, Orientation, and Quaternions"
Introduced in R2019b

## randrot

Uniformly distributed random rotations

## Syntax

$R=$ randrot
$R=\operatorname{randrot}(m)$
$R=\operatorname{randrot}(m 1, \ldots, m N)$
$R=\operatorname{randrot}([m 1, \ldots, m N])$

## Description

$R=$ randrot returns a unit quaternion drawn from a uniform distribution of random rotations.
$R=\operatorname{randrot}(m)$ returns an $m$-by- $m$ matrix of unit quaternions drawn from a uniform distribution of random rotations.
$R=$ randrot $(m 1, \ldots, m N)$ returns an $m 1-$ by-...-by-mN array of random unit quaternions, where $m 1$, $\ldots, \mathrm{mN}$ indicate the size of each dimension. For example, randrot $(3,4)$ returns a 3 -by-4 matrix of random unit quaternions.
$R=\operatorname{randrot}([m 1, \ldots, m N])$ returns an $m 1$-by-...-by-mN array of random unit quaternions, where $\mathrm{m} 1, \ldots, \mathrm{mN}$ indicate the size of each dimension. For example, randrot ( $[3,4]$ ) returns a 3-by-4 matrix of random unit quaternions.

## Examples

## Matrix of Random Rotations

Generate a 3-by-3 matrix of uniformly distributed random rotations.

```
r = randrot(3)
```

$r=3 x 3$ quaternion array

| $0.17446+0.59506 i-0.73295 j+0.27976 k$ | $0.69704-0.060589 i+0.68679 j-0.1969$ |
| ---: | ---: | ---: | ---: |
| $0.21908-0.89875 i-0.298 j+0.23548 k$ | $-0.049744+0.59691 i+0.56459 j+0.5678$ |
| $0.6375+0.49338 i-0.24049 j+0.54068 k$ | $0.2979-0.53568 i+0.31819 j+0.7232$ |

## Create Uniform Distribution of Random Rotations

Create a vector of 500 random quaternions. Use rotatepoint to visualize the distribution of the random rotations applied to point ( $1,0,0$ ).

```
q = randrot(500,1);
pt = rotatepoint(q, [1 0 0]);
```

figure
scatter3(pt(:,1), pt(:,2), pt(:,3))
axis equal


## Input Arguments

## m - Size of square matrix

integer
Size of square quaternion matrix, specified as an integer value. If $m$ is 0 or negative, then $R$ is returned as an empty matrix.
Data Types: single | double | int8 | int16 | int32 | int64 | uint8|uint16|uint32|uint64

## $\mathrm{ml}, \ldots, \mathrm{mN}$ - Size of each dimension

two or more integer values
Size of each dimension, specified as two or more integer values. If the size of any dimension is 0 or negative, then $R$ is returned as an empty array.
Example: randrot $(2,3)$ returns a 2 -by- 3 matrix of random quaternions.
Data Types: single | double | int8 | int16 | int32 | int64 | uint8|uint16|uint32|uint64
[ $\mathrm{m} 1, \ldots, \mathrm{mN}$ ] - Vector of size of each dimension
row vector of integer values

Vector of size of each dimension, specified as a row vector of two or more integer values. If the size of any dimension is 0 or negative, then $R$ is returned as an empty array.

Example: randrot ( $[2,3]$ ) returns a 2-by-3 matrix of random quaternions.
Data Types: single | double |int8|int16|int32|int64|uint8|uint16|uint32|uint64

## Output Arguments

## R-Random quaternions

scalar | vector | matrix | multidimensional array
Random quaternions, returned as a quaternion or array of quaternions.
Data Types: quaternion

## References

[1] Shoemake, K. "Uniform Random Rotations." Graphics Gems III (K. David, ed.). New York: Academic Press, 1992.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

quaternion

## Topics

"Rotations, Orientation, and Quaternions"
Introduced in R2019b

## rotateframe

Quaternion frame rotation

## Syntax

rotationResult $=$ rotateframe(quat,cartesianPoints)

## Description

rotationResult = rotateframe(quat, cartesianPoints) rotates the frame of reference for the Cartesian points using the quaternion, quat. The elements of the quaternion are normalized before use in the rotation.


## Examples

## Rotate Frame Using Quaternion Vector

Define a point in three dimensions. The coordinates of a point are always specified in the order $x, y$, and $z$. For convenient visualization, define the point on the $x-y$ plane.

```
x = 0.5;
y = 0.5;
z = 0;
plot(x,y,'ko')
hold on
axis([-1 1 -1 1])
```



Create a quaternion vector specifying two separate rotations, one to rotate the frame 45 degrees and another to rotate the point -90 degrees about the $z$-axis. Use rotateframe to perform the rotations.

```
quat = quaternion([0,0,pi/4; ...
    0,0,-pi/2],'euler','XYZ','frame');
rereferencedPoint = rotateframe(quat, [x,y,z])
rereferencedPoint = 2×3
    rrrre
```

Plot the rereferenced points.
plot(rereferencedPoint ( 1,1 ), rereferencedPoint $(1,2)$, 'bo') plot(rereferencedPoint $(2,1)$,rereferencedPoint $(2,2)$, 'go')


## Rereference Group of Points using Quaternion

Define two points in three-dimensional space. Define a quaternion to rereference the points by first rotating the reference frame about the $z$-axis 30 degrees and then about the new $y$-axis 45 degrees.
a = [1,0,0];
b = [0, 1, 0];
quat = quaternion([30,45,0],'eulerd','ZYX','point');
Use rotateframe to reference both points using the quaternion rotation operator. Display the result.

```
rP = rotateframe(quat,[a;b])
rP = 2\times3
```

| 0.6124 | -0.3536 | 0.7071 |
| ---: | ---: | ---: |
| 0.5000 | 0.8660 | -0.0000 |

Visualize the original orientation and the rotated orientation of the points. Draw lines from the origin to each of the points for visualization purposes.

```
plot3(a(1),a(2),a(3),'bo');
hold on
```

```
grid on
axis([-1 1 -1 1 -1 1])
xlabel('x')
ylabel('y')
zlabel('z')
plot3(b(1),b(2),b(3),'ro');
plot3(rP(1,1),rP(1,2),rP(1,3),'bd')
plot3(rP(2,1),rP(2,2),rP(2,3),'rd')
plot3([0;rP(1,1)],[0;rP(1,2)],[0;rP(1,3)],'k')
plot3([0;rP(2,1)],[0;rP(2,2)],[0;rP(2,3)],'k')
plot3([0;a(1)],[0;a(2)],[0;a(3)],'k')
plot3([0;b(1)],[0;b(2)],[0;b(3)],'k')
```



## Input Arguments

## quat - Quaternion that defines rotation

scalar|vector
Quaternion that defines rotation, specified as a scalar quaternion or vector of quaternions.
Data Types: quaternion

## cartesianPoints - Three-dimensional Cartesian points

1-by-3 vector | $N$-by-3 matrix

Three-dimensional Cartesian points, specified as a 1-by-3 vector or $N$-by-3 matrix.
Data Types: single|double

## Output Arguments

## rotationResult - Re-referenced Cartesian points

vector | matrix
Cartesian points defined in reference to rotated reference frame, returned as a vector or matrix the same size as cartesianPoints.

The data type of the re-referenced Cartesian points is the same as the underlying data type of quat.
Data Types: single | double

## Algorithms

Quaternion frame rotation re-references a point specified in $\mathbf{R}^{3}$ by rotating the original frame of reference according to a specified quaternion:

$$
L_{q}(u)=q^{*} u q
$$

where $q$ is the quaternion, * represents conjugation, and $u$ is the point to rotate, specified as a quaternion.

For convenience, the rotateframe function takes a point in $\mathbf{R}^{3}$ and returns a point in $\mathbf{R}^{3}$. Given a function call with some arbitrary quaternion, $q=a+b i+c j+d \mathrm{k}$, and arbitrary coordinate, $[\mathrm{x}, \mathrm{y}, \mathrm{z}]$,

```
point = [x,y,z];
rereferencedPoint = rotateframe(q,point)
```

the rotateframe function performs the following operations:
1 Converts point [ $x, y, z$ ] to a quaternion:

$$
u_{q}=0+x i+y j+z k
$$

2 Normalizes the quaternion, $q$ :

$$
q_{n}=\frac{q}{\sqrt{a^{2}+b^{2}+c^{2}+d^{2}}}
$$

3 Applies the rotation:

$$
v_{q}=q^{*} u_{q} q
$$

4 Converts the quaternion output, $v_{q}$, back to $\mathbf{R}^{3}$

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

## Functions

rotatepoint
Objects
quaternion

## Topics

"Rotations, Orientation, and Quaternions"
Introduced in R2019b

## rotatepoint

Quaternion point rotation

## Syntax

rotationResult $=$ rotatepoint(quat,cartesianPoints)

## Description

rotationResult = rotatepoint(quat, cartesianPoints) rotates the Cartesian points using the quaternion, quat. The elements of the quaternion are normalized before use in the rotation.
z



## Examples

## Rotate Point Using Quaternion Vector

Define a point in three dimensions. The coordinates of a point are always specified in order $x, y, z$. For convenient visualization, define the point on the $x$ - $y$ plane.

```
x = 0.5;
y = 0.5;
z = 0;
plot(x,y,'ko')
hold on
axis([-1 1 - - 1])
```



Create a quaternion vector specifying two separate rotations, one to rotate the point 45 and another to rotate the point -90 degrees about the $z$-axis. Use rotatepoint to perform the rotation.

```
quat = quaternion([0,0,pi/4; ...
    0,0,-pi/2],'euler','XYZ','point');
rotatedPoint = rotatepoint(quat, [x,y,z])
rotatedPoint = 2×3
    -0.0000 rrernerr 0
```

Plot the rotated points.
plot(rotatedPoint (1,1), rotatedPoint(1,2), 'bo') plot(rotatedPoint $(2,1)$, rotatedPoint $(2,2)$, go')


## Rotate Group of Points Using Quaternion

Define two points in three-dimensional space. Define a quaternion to rotate the point by first rotating about the $z$-axis 30 degrees and then about the new $y$-axis 45 degrees.
a = [1,0,0];
b = [0, 1, 0];
quat = quaternion([30,45,0],'eulerd','ZYX','point');
Use rotatepoint to rotate both points using the quaternion rotation operator. Display the result.

```
rP = rotatepoint(quat,[a;b])
rP = 2\times3
\begin{tabular}{lll}
0.6124 & 0.5000 & -0.6124
\end{tabular}
```

Visualize the original orientation and the rotated orientation of the points. Draw lines from the origin to each of the points for visualization purposes.

```
plot3(a(1),a(2),a(3),'bo');
hold on
```

```
grid on
axis([-1 1 -1 1 -1 1])
xlabel('x')
ylabel('y')
zlabel('z')
plot3(b(1),b(2),b(3),'ro');
plot3(rP(1,1),rP(1,2),rP(1,3),'bd')
plot3(rP(2,1),rP(2,2),rP(2,3),'rd')
plot3([0;rP(1,1)],[0;rP(1,2)],[0;rP(1,3)],'k')
plot3([0;rP(2,1)],[0;rP(2,2)],[0;rP(2,3)],'k')
plot3([0;a(1)],[0;a(2)],[0;a(3)],'k')
plot3([0;b(1)],[0;b(2)],[0;b(3)],'k')
```



## Input Arguments

quat - Quaternion that defines rotation
scalar | vector
Quaternion that defines rotation, specified as a scalar quaternion, row vector of quaternions, or column vector of quaternions.

## cartesianPoints - Three-dimensional Cartesian points

## 1 -by-3 vector | $N$-by-3 matrix

Three-dimensional Cartesian points, specified as a 1-by-3 vector or N -by-3 matrix.
Data Types: single | double

## Output Arguments

## rotationResult - Repositioned Cartesian points

vector | matrix
Rotated Cartesian points defined using the quaternion rotation, returned as a vector or matrix the same size as cartesianPoints.

Data Types: single | double

## Algorithms

Quaternion point rotation rotates a point specified in $\mathbf{R}^{3}$ according to a specified quaternion:

$$
L_{q}(u)=q u q^{*}
$$

where $q$ is the quaternion, * represents conjugation, and $u$ is the point to rotate, specified as a quaternion.

For convenience, the rotatepoint function takes in a point in $\mathbf{R}^{3}$ and returns a point in $\mathbf{R}^{3}$. Given a function call with some arbitrary quaternion, $q=a+b \mathrm{i}+c \mathrm{j}+d \mathrm{k}$, and arbitrary coordinate, $[x, y, z]$, for example,
rereferencedPoint $=$ rotatepoint $(q,[x, y, z])$
the rotatepoint function performs the following operations:
1 Converts point $[x, y, z]$ to a quaternion:

$$
u_{q}=0+x i+y j+z k
$$

2 Normalizes the quaternion, $q$ :

$$
q_{n}=\frac{q}{\sqrt{a^{2}+b^{2}+c^{2}+d^{2}}}
$$

3 Applies the rotation:

$$
v_{q}=q u_{q} q^{*}
$$

4 Converts the quaternion output, $v_{q}$, back to $\mathbf{R}^{3}$

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.

## See Also

## Functions

rotateframe
Objects
quaternion

## Topics

"Rotations, Orientation, and Quaternions"
Introduced in R2019b

## rotmat

Convert quaternion to rotation matrix

## Syntax

rotationMatrix $=$ rotmat(quat, rotationType)

## Description

rotationMatrix = rotmat(quat, rotationType) converts the quaternion, quat, to an equivalent rotation matrix representation.

## Examples

## Convert Quaternion to Rotation Matrix for Point Rotation

Define a quaternion for use in point rotation.

```
theta = 45;
gamma = 30;
quat = quaternion([0,theta,gamma],'eulerd','ZYX','point')
quat = quaternion
    0.8924 + 0.23912i + 0.36964j + 0.099046k
```

Convert the quaternion to a rotation matrix.

```
rotationMatrix = rotmat(quat,'point')
rotationMatrix = 3×3
\begin{tabular}{rrr}
0.7071 & -0.0000 & 0.7071 \\
0.3536 & 0.8660 & -0.3536 \\
-0.6124 & 0.5000 & 0.6124
\end{tabular}
```

To verify the rotation matrix, directly create two rotation matrices corresponding to the rotations about the $y$-and $x$-axes. Multiply the rotation matrices and compare to the output of rotmat.

```
theta = 45;
gamma = 30;
ry = [cosd(theta) 0 sind(theta) ; ...
    0 1 0 ; ...
    -sind(theta) 0 cosd(theta)];
rx = [1 0 % 0 cosd(gamma) 0-sind(gamma); ; ...
    0 sind(gamma) cosd(gamma)];
rotationMatrixVerification = rx*ry
```

```
rotationMatrixVerification = 3×3
```

| 0.7071 | 0 | 0.7071 |
| ---: | ---: | ---: |
| 0.3536 | 0.8660 | -0.3536 |
| -0.6124 | 0.5000 | 0.6124 |

## Convert Quaternion to Rotation Matrix for Frame Rotation

Define a quaternion for use in frame rotation.

```
theta = 45;
gamma = 30;
quat = quaternion([0,theta,gamma],'eulerd','ZYX','frame')
quat = quaternion
    0.8924 + 0.23912i + 0.36964j - 0.099046k
```

Convert the quaternion to a rotation matrix.

```
rotationMatrix = rotmat(quat,'frame')
rotationMatrix = 3×3
    0.7071 rr0.0000 - -0.7071
    0.6124 -0.5000 0.6124
```

To verify the rotation matrix, directly create two rotation matrices corresponding to the rotations about the $y$ - and $x$-axes. Multiply the rotation matrices and compare to the output of rotmat.

```
theta = 45;
gamma = 30;
ry = [cosd(theta) 
rx = [1 [lll
rotationMatrixVerification = rx*ry
rotationMatrixVerification = 3×3
```

| 0.7071 | 0 | -0.7071 |
| ---: | ---: | ---: |
| 0.3536 | 0.8660 | 0.3536 |
| 0.6124 | -0.5000 | 0.6124 |

## Convert Quaternion Vector to Rotation Matrices

Create a 3-by-1 normalized quaternion vector.
qVec $=$ normalize(quaternion(randn(3,4)));
Convert the quaternion array to rotation matrices. The pages of rotmatArray correspond to the linear index of qVec.

```
rotmatArray = rotmat(qVec,'frame');
```

Assume qVec and rotmatArray correspond to a sequence of rotations. Combine the quaternion rotations into a single representation, then apply the quaternion rotation to arbitrarily initialized Cartesian points.

```
loc = normalize(randn(1,3));
quat = prod(qVec);
rotateframe(quat,loc)
ans = 1\times3
    0.9524 0.5297 0.9013
```

Combine the rotation matrices into a single representation, then apply the rotation matrix to the same initial Cartesian points. Verify the quaternion rotation and rotation matrix result in the same orientation.

```
totalRotMat = eye(3);
for i = 1:size(rotmatArray,3)
    totalRotMat = rotmatArray(:,:,i)*totalRotMat;
end
totalRotMat*loc'
ans = 3\times1
    0.9524
    0.5297
    0.9013
```


## Input Arguments

## quat - Quaternion to convert

scalar | vector | matrix | multidimensional array
Quaternion to convert, specified as a scalar, vector, matrix, or multidimensional array.
Data Types: quaternion
rotationType - Type or rotation
'frame'|'point'
Type of rotation represented by the rotationMatrix output, specified as 'frame' or 'point'.
Data Types: char | string

## Output Arguments

## rotationMatrix - Rotation matrix representation

3-by-3 matrix | 3-by-3-by-N multidimensional array
Rotation matrix representation, returned as a 3-by-3 matrix or 3-by-3-by-N multidimensional array.

- If quat is a scalar, rotationMatrix is returned as a 3-by-3 matrix.
- If quat is non-scalar, rotationMatrix is returned as a 3 -by- 3 -by- $N$ multidimensional array, where rotationMatrix(:, :,i) is the rotation matrix corresponding to quat(i).

The data type of the rotation matrix is the same as the underlying data type of quat.

## Data Types: single | double

## Algorithms

Given a quaternion of the form

$$
q=a+b i+c j+d k,
$$

the equivalent rotation matrix for frame rotation is defined as

$$
\left[\begin{array}{ccc}
2 a^{2}-1+2 b^{2} & 2 b c+2 a d & 2 b d-2 a c \\
2 b c-2 a d & 2 a^{2}-1+2 c^{2} & 2 c d+2 a b \\
2 b d+2 a c & 2 c d-2 a b & 2 a^{2}-1+2 d^{2}
\end{array}\right] .
$$

The equivalent rotation matrix for point rotation is the transpose of the frame rotation matrix:

$$
\left[\begin{array}{ccc}
2 a^{2}-1+2 b^{2} & 2 b c-2 a d & 2 b d+2 a c \\
2 b c+2 a d & 2 a^{2}-1+2 c^{2} & 2 c d-2 a b \\
2 b d-2 a c & 2 c d+2 a b & 2 a^{2}-1+2 d^{2}
\end{array}\right] .
$$

## References

[1] Kuipers, Jack B. Quaternions and Rotation Sequences: A Primer with Applications to Orbits, Aerospace, and Virtual Reality. Princeton, NJ: Princeton University Press, 2007.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.

## See Also

## Functions

rotvec| rotvecd | euler |eulerd

## Objects

quaternion

## Topics

"Rotations, Orientation, and Quaternions"

Introduced in R2019b

## rotvec

Convert quaternion to rotation vector (radians)

## Syntax

rotationVector $=$ rotvec (quat)

## Description

rotationVector $=$ rotvec (quat) converts the quaternion array, quat, to an $N$-by- 3 matrix of equivalent rotation vectors in radians. The elements of quat are normalized before conversion.

## Examples

## Convert Quaternion to Rotation Vector in Radians

Convert a random quaternion scalar to a rotation vector in radians

```
quat = quaternion(randn(1,4));
rotvec(quat)
ans = 1\times3
    1.6866 -2.0774 0.7929
```


## Input Arguments

quat - Quaternion to convert
scalar | vector | matrix \| multidimensional array
Quaternion to convert, specified as scalar quaternion, vector, matrix, or multidimensional array of quaternions.

Data Types: quaternion

## Output Arguments

rotationVector - Rotation vector (radians)
$N$-by-3 matrix
Rotation vector representation, returned as an $N$-by-3 matrix of rotations vectors, where each row represents the [X Y Z] angles of the rotation vectors in radians. The ith row of rotationVector corresponds to the element quat (i).

The data type of the rotation vector is the same as the underlying data type of quat.
Data Types: single | double

## Algorithms

All rotations in 3-D can be represented by a three-element axis of rotation and a rotation angle, for a total of four elements. If the rotation axis is constrained to be unit length, the rotation angle can be distributed over the vector elements to reduce the representation to three elements.

Recall that a quaternion can be represented in axis-angle form

$$
q=\cos (\theta / 2)+\sin (\theta / 2)(x i+y j+z \mathrm{k}),
$$

where $\theta$ is the angle of rotation and $[x, y, z]$ represent the axis of rotation.
Given a quaternion of the form

$$
q=a+b i+c j+d k,
$$

you can solve for the rotation angle using the axis-angle form of quaternions:

$$
\theta=2 \cos ^{-1}(a) .
$$

Assuming a normalized axis, you can rewrite the quaternion as a rotation vector without loss of information by distributing $\theta$ over the parts $b, c$, and $d$. The rotation vector representation of $q$ is

$$
q_{\mathrm{rv}}=\frac{\theta}{\sin (\theta / 2)}[b, c, d] .
$$

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

## Functions

rotvecd | euler | eulerd

## Objects

quaternion

## Topics

"Rotations, Orientation, and Quaternions"

## Introduced in R2019b

## rotvecd

Convert quaternion to rotation vector (degrees)

## Syntax

```
rotationVector = rotvecd(quat)
```


## Description

rotationVector $=$ rotvecd(quat) converts the quaternion array, quat, to an N -by-3 matrix of equivalent rotation vectors in degrees. The elements of quat are normalized before conversion.

## Examples

## Convert Quaternion to Rotation Vector in Degrees

Convert a random quaternion scalar to a rotation vector in degrees.

```
quat = quaternion(randn(1,4));
rotvecd(quat)
ans = 1\times3
    96.6345-119.0274 45.4312
```


## Input Arguments

## quat - Quaternion to convert

scalar | vector | matrix | multidimensional array
Quaternion to convert, specified as scalar, vector, matrix, or multidimensional array of quaternions.
Data Types: quaternion

## Output Arguments

## rotationVector - Rotation vector (degrees)

N -by-3 matrix
Rotation vector representation, returned as an N -by-3 matrix of rotation vectors, where each row represents the $[x y z]$ angles of the rotation vectors in degrees. The ith row of rotationVector corresponds to the element quat (i).

The data type of the rotation vector is the same as the underlying data type of quat.
Data Types: single | double

## Algorithms

All rotations in 3-D can be represented by four elements: a three-element axis of rotation and a rotation angle. If the rotation axis is constrained to be unit length, the rotation angle can be distributed over the vector elements to reduce the representation to three elements.

Recall that a quaternion can be represented in axis-angle form

$$
q=\cos (\theta / 2)+\sin (\theta / 2)(x i+y j+z \mathrm{k}),
$$

where $\theta$ is the angle of rotation in degrees, and $[x, y, z]$ represent the axis of rotation.
Given a quaternion of the form

$$
q=a+b i+c j+d k,
$$

you can solve for the rotation angle using the axis-angle form of quaternions:

$$
\theta=2 \cos ^{-1}(a) .
$$

Assuming a normalized axis, you can rewrite the quaternion as a rotation vector without loss of information by distributing $\theta$ over the parts $b, c$, and $d$. The rotation vector representation of $q$ is

$$
q_{\mathrm{rv}}=\frac{\theta}{\sin (\theta / 2)}[b, c, d] .
$$

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

## Functions

rotvec|euler |eulerd
Objects
quaternion

## Topics

"Rotations, Orientation, and Quaternions"

## Introduced in R2019b

## slerp

Spherical linear interpolation

## Syntax

$\mathrm{q} 0=\operatorname{slerp}(\mathrm{q} 1, \mathrm{q} 2, \mathrm{~T})$

## Description

$q 0=s \operatorname{lerp}(q 1, q 2, T)$ spherically interpolates between q1 and q2 by the interpolation coefficient T . The function always chooses the shorter interpolation path between q 1 and q 2 .

## Examples

## Interpolate Between Two Quaternions

Create two quaternions with the following interpretation:
$1 \mathrm{a}=45$ degree rotation around the $z$-axis
$2 \mathrm{c}=-45$ degree rotation around the $z$-axis
a = quaternion([45,0,0],'eulerd','ZYX','frame');
c = quaternion([-45,0,0],'eulerd','ZYX','frame');
Call slerp with the quaternions a and c and specify an interpolation coefficient of 0.5.
interpolationCoefficient $=0.5$;
b = slerp(a, c,interpolationCoefficient);
The output of slerp, $b$, represents an average rotation of $a$ and $c$. To verify, convert $b$ to Euler angles in degrees.

```
averageRotation = eulerd(b,'ZYX','frame')
averageRotation = 1×3
```

    \(0 \quad 0 \quad 0\)
    The interpolation coefficient is specified as a normalized value between 0 and 1, inclusive. An interpolation coefficient of 0 corresponds to the a quaternion, and an interpolation coefficient of 1 corresponds to the c quaternion. Call slerp with coefficients 0 and 1 to confirm.

```
b = slerp(a,c,[0,1]);
eulerd(b,'ZYX','frame')
ans = 2\times3
```

    45.000000
    You can create smooth paths between quaternions by specifying arrays of equally spaced interpolation coefficients.

```
path = 0:0.1:1;
interpolatedQuaternions = slerp(a,c,path);
```

For quaternions that represent rotation only about a single axis, specifying interpolation coefficients as equally spaced results in quaternions equally spaced in Euler angles. Convert interpolatedQuaternions to Euler angles and verify that the difference between the angles in the path is constant.

```
k = eulerd(interpolatedQuaternions,'ZYX','frame');
abc = abs(diff(k))
abc = 10\times3
\begin{tabular}{lll}
9.0000 & 0 & 0 \\
9.0000 & 0 & 0 \\
9.0000 & 0 & 0 \\
9.0000 & 0 & 0 \\
9.0000 & 0 & 0 \\
9.0000 & 0 & 0 \\
9.0000 & 0 & 0 \\
9.0000 & 0 & 0 \\
9.0000 & 0 & 0 \\
9.0000 & 0 & 0
\end{tabular}
```

Alternatively, you can use the dist function to verify that the distance between the interpolated quaternions is consistent. The dist function returns angular distance in radians; convert to degrees for easy comparison.

```
def = rad2deg(dist(interpolatedQuaternions(2:end),interpolatedQuaternions(1:end-1)))
def = 1\times10
\begin{tabular}{lllllllll}
9.0000 & 9.0000 & 9.0000 & 9.0000 & 9.0000 & 9.0000 & 9.0000 & 9.0000 & 9.0000
\end{tabular}
```


## SLERP Minimizes Great Circle Path

The SLERP algorithm interpolates along a great circle path connecting two quaternions. This example shows how the SLERP algorithm minimizes the great circle path.

Define three quaternions:
1 q0-quaternion indicating no rotation from the global frame
2 q179-quaternion indicating a 179 degree rotation about the $z$-axis
3 q180-quaternion indicating a 180 degree rotation about the $z$-axis

4 q181-quaternion indicating a 181 degree rotation about the $z$-axis

```
q0 = ones(1,'quaternion');
```

q179 = quaternion([179,0,0],'eulerd','ZYX','frame');
q180 = quaternion([180,0,0],'eulerd','ZYX','frame');
q181 = quaternion([181,0,0],'eulerd','ZYX','frame');

Use slerp to interpolate between $q 0$ and the three quaternion rotations. Specify that the paths are traveled in 10 steps.

```
T = linspace(0,1,10);
q179path = slerp(q0,q179,T);
q180path = slerp(q0,q180,T);
q181path = slerp(q0,q181,T);
```

Plot each path in terms of Euler angles in degrees.
q179pathEuler = eulerd(q179path,'ZYX','frame');
q180pathEuler = eulerd(q180path,'ZYX','frame');
q181pathEuler = eulerd(q181path,'ZYX','frame');
plot(T,q179pathEuler(:,1),'bo', ...
T,q180pathEuler(:,1),'r*', ...
T,q181pathEuler(:,1),'gd');
legend('Path to 179 degrees', ...
'Path to 180 degrees', ...
'Path to 181 degrees')
xlabel('Interpolation Coefficient')
ylabel('Z-Axis Rotation (Degrees)')


The path between $q 0$ and $q 179$ is clockwise to minimize the great circle distance. The path between $q 0$ and q181 is counterclockwise to minimize the great circle distance. The path between q0 and q180 can be either clockwise or counterclockwise, depending on numerical rounding.

## Show Interpolated Quaternions on Sphere

Create two quaternions.
q1 = quaternion([75,-20,-10], 'eulerd','ZYX','frame');
q2 = quaternion([-45,20,30],'eulerd','ZYX','frame');
Define the interpolation coefficient.
T = 0:0.01:1;
Obtain the interpolated quaternions.
quats $=\operatorname{slerp}(q 1, q 2, T)$;
Obtain the corresponding rotate points.

```
pts = rotatepoint(quats,[1 0 0]);
```

Show the interpolated quaternions on a unit sphere.
figure
[X,Y,Z] = sphere;

```
surf(X,Y,Z,'FaceColor',[0.57 0.57 0.57])
hold on;
scatter3(pts(:,1),pts(:,2),pts(:,3))
view([69.23 36.60])
axis equal
```



Note that the interpolated quaternions follow the shorter path from q1 to q2.

## Input Arguments

## q1 - Quaternion

scalar | vector | matrix | multidimensional array
Quaternion to interpolate, specified as a scalar, vector, matrix, or multidimensional array of quaternions.
q1, q2, and T must have compatible sizes. In the simplest cases, they can be the same size or any one can be a scalar. Two inputs have compatible sizes if, for every dimension, the dimension sizes of the inputs are either the same or one of them is 1 .

Data Types: quaternion

## q2 - Quaternion

scalar | vector | matrix | multidimensional array

Quaternion to interpolate, specified as a scalar, vector, matrix, or multidimensional array of quaternions.
q1, q2, and T must have compatible sizes. In the simplest cases, they can be the same size or any one can be a scalar. Two inputs have compatible sizes if, for every dimension, the dimension sizes of the inputs are either the same or one of the dimension sizes is 1 .

## Data Types: quaternion

## T- Interpolation coefficient

scalar | vector | matrix | multidimensional array
Interpolation coefficient, specified as a scalar, vector, matrix, or multidimensional array of numbers with each element in the range $[0,1]$.
q1, q2, and T must have compatible sizes. In the simplest cases, they can be the same size or any one can be a scalar. Two inputs have compatible sizes if, for every dimension, the dimension sizes of the inputs are either the same or one of the dimension sizes is 1 .
Data Types: single | double

## Output Arguments

## q0 - Interpolated quaternion

scalar | vector | matrix | multidimensional array
Interpolated quaternion, returned as a scalar, vector, matrix, or multidimensional array.
Data Types: quaternion

## Algorithms

Quaternion spherical linear interpolation (SLERP) is an extension of linear interpolation along a plane to spherical interpolation in three dimensions. The algorithm was first proposed in [1]. Given two quaternions, $q_{1}$ and $q_{2}$, SLERP interpolates a new quaternion, $q_{0}$, along the great circle that connects $q_{1}$ and $q_{2}$. The interpolation coefficient, $T$, determines how close the output quaternion is to either $q_{1}$ and $q_{2}$.

The SLERP algorithm can be described in terms of sinusoids:

$$
q_{0}=\frac{\sin ((1-T) \theta)}{\sin (\theta)} q_{1}+\frac{\sin (T \theta)}{\sin (\theta)} q_{2}
$$

where $q_{1}$ and $q_{2}$ are normalized quaternions, and $\theta$ is half the angular distance between $q_{1}$ and $q_{2}$.

## References

[1] Shoemake, Ken. "Animating Rotation with Quaternion Curves." ACM SIGGRAPH Computer Graphics Vol. 19, Issue 3, 1985, pp. 345-354.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

## Functions

dist|meanrot
Objects
quaternion

## Topics

"Lowpass Filter Orientation Using Quaternion SLERP"
"Rotations, Orientation, and Quaternions"

Introduced in R2019b

## times, .*

Element-wise quaternion multiplication

## Syntax

quatC $=A . * B$

## Description

quatC $=\mathrm{A} . * \mathrm{~B}$ returns the element-by-element quaternion multiplication of quaternion arrays.
You can use quaternion multiplication to compose rotation operators:

- To compose a sequence of frame rotations, multiply the quaternions in the same order as the desired sequence of rotations. For example, to apply a $p$ quaternion followed by a $q$ quaternion, multiply in the order $p q$. The rotation operator becomes $(p q)^{*} v(p q)$, where $v$ represents the object to rotate in quaternion form. * represents conjugation.
- To compose a sequence of point rotations, multiply the quaternions in the reverse order of the desired sequence of rotations. For example, to apply a $p$ quaternion followed by a $q$ quaternion, multiply in the reverse order, $q p$. The rotation operator becomes $(q p) v(q p)^{*}$.


## Examples

## Multiply Two Quaternion Vectors

Create two vectors, $A$ and $B$, and multiply them element by element.

```
A = quaternion([1:4;5:8]);
B = A;
C = A.*B
C = 2x1 quaternion array
    -28 + 4i + 6j + 8k
    -124 + 60i + 70j + 80k
```


## Multiply Two Quaternion Arrays

Create two 3-by-3 arrays, A and B, and multiply them element by element.

```
A = reshape(quaternion(randn(9,4)),3,3);
B = reshape(quaternion(randn(9,4)),3,3);
C = A.*B
C = 3x3 quaternion array
    0.60169 + 2.4332i - 2.5844j + 0.51646k -0.49513 + 1.1722i + 4.4401j - 1.217k
```

```
-4.4159 + 2.1926i + 1.9037j - 4.0303k -2.0232 + 0.4205i - 0.17288j + 3.8529k
```

Note that quaternion multiplication is not commutative:

```
isequal(C,B.*A)
ans = logical
```

    0
    
## Multiply Quaternion Row and Column Vectors

Create a row vector a and a column vector b, then multiply them. The 1 -by- 3 row vector and 4 -by- 1 column vector combine to produce a 4 -by- 3 matrix with all combinations of elements multiplied.

```
a = [zeros('quaternion'),ones('quaternion'),quaternion(randn(1,4))]
a = 1x3 quaternion array
```



```
b = quaternion(randn(4,4))
b = 4x1 quaternion array
    0.31877 + 3.5784i + 0.7254j - 0.12414k
    -1.3077 + 2.7694i - 0.063055j + 1.4897k
    -0.43359 - 1.3499i + 0.71474j + 1.409k
    0.34262 + 3.0349i - 0.20497j + 1.4172k
a.*b
ans = 4x3 quaternion array
\begin{tabular}{llllrlr}
\(0+\) & \(0 i+\) & \(0 j+\) & \(0 k\) & \(0.31877+\) & \(3.5784 i+0.7254 j-\) & 0.1241 \\
\(0+\) & \(0 i+\) & \(0 j+\) & \(0 k\) & \(-1.3077+\) & \(2.7694 i-0.063055 j+\) & 1.489 \\
\(0+\) & \(0 i+\) & \(0 j+\) & \(0 k\) & \(-0.43359-\) & \(1.3499 i+0.71474 j+\) & 1.40 \\
\(0+\) & \(0 i+\) & \(0 j+\) & \(0 k\) & \(0.34262+\) & \(3.0349 i-0.20497 j+\) & 1.417
\end{tabular}
```


## Input Arguments

## A - Array to multiply

scalar | vector $\mid$ matrix | multidimensional array
Array to multiply, specified as a quaternion, an array of quaternions, a real scalar, or an array of real numbers.
$A$ and $B$ must have compatible sizes. In the simplest cases, they can be the same size or one can be a scalar. Two inputs have compatible sizes if, for every dimension, the dimension sizes of the inputs are the same or one of them is 1 .
Data Types: quaternion | single | double

## B - Array to multiply

scalar | vector | matrix | multidimensional array
Array to multiply, specified as a quaternion, an array of quaternions, a real scalar, or an array of real numbers.
$A$ and $B$ must have compatible sizes. In the simplest cases, they can be the same size or one can be a scalar. Two inputs have compatible sizes if, for every dimension, the dimension sizes of the inputs are the same or one of them is 1 .

Data Types: quaternion | single | double

## Output Arguments

## quatC - Quaternion product

scalar | vector | matrix | multidimensional array
Quaternion product, returned as a scalar, vector, matrix, or multidimensional array.
Data Types: quaternion

## Algorithms

## Quaternion Multiplication by a Real Scalar

Given a quaternion,

$$
q=a_{\mathrm{q}}+b_{\mathrm{q}} \mathrm{i}+c_{\mathrm{q}} \mathrm{j}+d_{\mathrm{q}} \mathrm{k},
$$

the product of $q$ and a real scalar $\beta$ is

$$
\beta q=\beta a_{\mathrm{q}}+\beta b_{\mathrm{q}} \mathrm{i}+\beta c_{\mathrm{q}} \mathrm{j}+\beta d_{\mathrm{q}} \mathrm{k}
$$

## Quaternion Multiplication by a Quaternion Scalar

The definition of the basis elements for quaternions,

$$
\mathrm{i}^{2}=\mathrm{j}^{2}=\mathrm{k}^{2}=\mathrm{ijk}=-1,
$$

can be expanded to populate a table summarizing quaternion basis element multiplication:

|  | $\mathbf{1}$ | $\mathbf{i}$ | $\mathbf{j}$ | k |
| :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | 1 | i | -1 | j |
| $\mathbf{i}$ | i | -k | -1 | k |
| $\mathbf{j}$ | j | j | -i | -j |
| $\mathbf{k}$ | k | j |  |  |

When reading the table, the rows are read first, for example: $\mathrm{ij}=\mathrm{k}$ and $\mathrm{ji}=-\mathrm{k}$.
Given two quaternions, $q=a_{\mathrm{q}}+b_{\mathrm{q}} \mathrm{i}+c_{\mathrm{q}} \mathrm{j}+d_{\mathrm{q}} \mathrm{k}$, and $p=a_{\mathrm{p}}+b_{\mathrm{p}} \mathrm{i}+c_{\mathrm{p}} \mathrm{j}+d_{\mathrm{p}} \mathrm{k}$, the multiplication can be expanded as:

$$
\begin{aligned}
z= & p q=\left(a_{\mathrm{p}}+b_{\mathrm{p}} \mathrm{i}+c_{\mathrm{p}} \mathrm{j}+d_{\mathrm{p}} \mathrm{k}\right)\left(a_{\mathrm{q}}+b_{\mathrm{q}} \mathrm{i}+c_{\mathrm{q}} \mathrm{j}+d_{\mathrm{q}} \mathrm{k}\right) \\
& =a_{\mathrm{p}} a_{\mathrm{q}}+a_{\mathrm{p}} b_{\mathrm{q}} \mathrm{i}+a_{\mathrm{p}} c_{\mathrm{q}} \mathrm{j}+a_{\mathrm{p}} d_{\mathrm{q}} \mathrm{k} \\
& +b_{\mathrm{p}} a_{\mathrm{q}} \mathrm{i}+b_{\mathrm{p}} b_{\mathrm{q}^{2}}{ }^{2}+b_{\mathrm{p}} c_{\mathrm{q}} \mathrm{j} \mathrm{j}+b_{\mathrm{p}} d_{\mathrm{q}} \mathrm{k} \\
& +c_{\mathrm{p}} a_{\mathrm{q}} \mathrm{j}+c_{\mathrm{p}} b_{\mathrm{q}} \mathrm{ji}+c_{\mathrm{p}} c_{\mathrm{q}} j^{2}+c_{\mathrm{p}} d_{\mathrm{q}} \mathrm{k} \\
& +d_{\mathrm{p}} a_{\mathrm{q}} k+d_{\mathrm{p}} b_{\mathrm{q}} \mathrm{ki}+d_{\mathrm{p}} c_{\mathrm{q}} \mathrm{kj}+d_{\mathrm{p}} d_{\mathrm{q}} \mathrm{k}^{2}
\end{aligned}
$$

You can simplify the equation using the quaternion multiplication table.

$$
\begin{aligned}
z= & p q=a_{\mathrm{p}} a_{\mathrm{q}}+a_{\mathrm{p}} b_{\mathrm{q}} \mathrm{i}+a_{\mathrm{p}} c_{\mathrm{q}} \mathrm{j}+a_{\mathrm{p}} d_{\mathrm{q}} \mathrm{k} \\
& +b_{\mathrm{p}} a_{\mathrm{q}} \mathrm{i}-b_{\mathrm{p}} b_{\mathrm{q}}+b_{\mathrm{p}} c_{\mathrm{q}} \mathrm{k}-b_{\mathrm{p}} d_{\mathrm{q}} \mathrm{j} \\
& +c_{\mathrm{p}} a_{\mathrm{q}} \mathrm{j}-c_{\mathrm{p}} b_{\mathrm{q}} \mathrm{k}-c_{\mathrm{p}} c_{\mathrm{q}}+c_{\mathrm{p}} d_{\mathrm{q}} \mathrm{i} \\
& +d_{\mathrm{p}} a_{\mathrm{q}} k+d_{\mathrm{p}} b_{\mathrm{q}} \mathrm{j}-d_{\mathrm{p}} c_{\mathrm{q}} \mathrm{i}-d_{\mathrm{p}} d_{\mathrm{q}}
\end{aligned}
$$

## References

[1] Kuipers, Jack B. Quaternions and Rotation Sequences: A Primer with Applications to Orbits, Aerospace, and Virtual Reality. Princeton, NJ: Princeton University Press, 2007.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® $\mathrm{Coder}^{\mathrm{TM}}$.

## See Also

## Functions

prod|mtimes, *

## Objects

quaternion

## Topics

"Rotations, Orientation, and Quaternions"

## Introduced in R2019b

## transpose, .'

Transpose a quaternion array

## Syntax

$Y=$ quat. ${ }^{\prime}$

## Description

$Y=$ quat. ' returns the non-conjugate transpose of the quaternion array, quat.

## Examples

## Vector Transpose

Create a vector of quaternions and compute its nonconjugate transpose.

```
quat = quaternion(randn(4,4))
quat = 4x1 quaternion array
    0.53767 + 0.31877i + 3.5784j + 0.7254k
    1.8339 - 1.3077i + 2.7694j - 0.063055k
    -2.2588 - 0.43359i - 1.3499j + 0.71474k
    0.86217 + 0.34262i + 3.0349j - 0.20497k
quatTransposed = quat.'
quatTransposed = 1x4 quaternion array
    0.53767 + 0.31877i + 3.5784j + 0.7254k 1.8339 - 1.3077i + 2.7694j - 0.06305
```


## Matrix Transpose

Create a matrix of quaternions and compute its nonconjugate transpose.

```
quat = [quaternion(randn(2,4)),quaternion(randn(2,4))]
quat = 2x2 quaternion array
    0.53767-2.2588i + 0.31877j - 0.43359k 3.5784-1.3499i + 0.7254j + 0.7147
    1.8339 + 0.86217i - 1.3077j + 0.34262k 2.7694 + 3.0349i - 0.063055j - 0.2049
quatTransposed = quat.'
quatTransposed = 2x2 quaternion array
    0.53767-2.2588i + 0.31877j - 0.43359k 1.8339 + 0.86217i - 1.3077j + 0.3426
        3.5784 - 1.3499i + 0.7254j + 0.71474k 2.7694 + 3.0349i - 0.063055j - 0.2049
```


## Input Arguments

quat - Quaternion array to transpose
vector | matrix
Quaternion array to transpose, specified as a vector or matrix of quaternions. transpose is defined for 1-D and 2-D arrays. For higher-order arrays, use permute.

Data Types: quaternion

## Output Arguments

## Y - Transposed quaternion array <br> vector | matrix

Transposed quaternion array, returned as an $N$-by- $M$ array, where quat was specified as an $M$-by- $N$ array.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder ${ }^{\mathrm{TM}}$.

## See Also

Functions
ctranspose, '
Objects
quaternion

## Topics

"Rotations, Orientation, and Quaternions"
Introduced in R2019b

## uminus, -

Quaternion unary minus

## Syntax

mQuat $=$-quat

## Description

mQuat $=$-quat negates the elements of quat and stores the result in mQuat.

## Examples

## Negate Elements of Quaternion Matrix

Unary minus negates each part of a the quaternion. Create a 2 -by- 2 matrix, Q .
Q = quaternion (randn (2), randn (2), randn(2), randn (2) )
Q $=2 \times 2$ quaternion array


Negate the parts of each quaternion in $\mathbf{Q}$.
$R=-Q$
$\begin{array}{rlr}\mathrm{R}=2 \times 2 \text { quaternion array } & \\ & -0.53767-0.31877 \mathrm{i}- & 3.5784 \mathrm{j}-\quad 0.7254 \mathrm{k} \\ & -1.8339+\quad 1.3077 \mathrm{i}-\quad 2.7694 \mathrm{j}+0.063055 \mathrm{k}\end{array}$
$2.2588+0.43359 i+1.3499 j-0.7147$
$-0.86217-0.34262 i-3.0349 j+0.2049$

## Input Arguments

quat - Quaternion array
scalar | vector | matrix | multidimensional array
Quaternion array, specified as a scalar, vector, matrix, or multidimensional array.
Data Types: quaternion

## Output Arguments

## mQuat - Negated quaternion array

scalar | vector | matrix | multidimensional array
Negated quaternion array, returned as the same size as quat.
Data Types: quaternion

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

## Functions

minus,
Objects
quaternion

## Topics

"Rotations, Orientation, and Quaternions"

Introduced in R2019b

## zeros

Create quaternion array with all parts set to zero

## Syntax

```
quatZeros = zeros('quaternion')
quatZeros = zeros(n,'quaternion')
quatZeros = zeros(sz,'quaternion')
quatZeros = zeros(sz1,...,szN,'quaternion')
quatZeros = zeros(___,'like',prototype,'quaternion')
```


## Description

quatZeros $=$ zeros('quaternion') returns a scalar quaternion with all parts set to zero.
quatZeros $=$ zeros( $n$,'quaternion') returns an $n$-by-n matrix of quaternions.
quatZeros $=$ zeros(sz,'quaternion') returns an array of quaternions where the size vector, sz, defines size(quatZeros).
quatZeros $=$ zeros(sz1,...,szN,'quaternion') returns a sz1-by-...-by-szN array of quaternions where $s z 1, \ldots, s z N$ indicates the size of each dimension.
quatZeros $=$ zeros( $\qquad$ ,'like',prototype,'quaternion') specifies the underlying class of the returned quaternion array to be the same as the underlying class of the quaternion prototype.

## Examples

## Quaternion Scalar Zero

Create a quaternion scalar zero.

```
quatZeros = zeros('quaternion')
```

quatZeros = quaternion
$0+0 i+0 j+0 k$

## Square Matrix of Quaternions

Create an n-by-n array of quaternion zeros.

```
n = 3;
quatZeros = zeros(n,'quaternion')
quatZeros = 3x3 quaternion array
    0 + 0i + 0j + 0k 0 + 0i + 0j + 0k 0 + 0i + 0j + 0k
```

```
0 + 0i + 0j + 0k 0 + 0i + 0j + 0k 0 + 0i + 0j + 0k
0 + 0i + 0j + 0k 0 + 0i + 0j + 0k 0 + 0i + 0j + 0k
```


## Multidimensional Array of Quaternion Zeros

Create a multidimensional array of quaternion zeros by defining array dimensions in order. In this example, you create a 3-by-1-by-2 array. You can specify dimensions using a row vector or commaseparated integers.

Specify the dimensions using a row vector and display the results:

```
dims = [3,1,2];
quatZerosSyntax1 = zeros(dims,'quaternion')
quatZerosSyntax1 = 3x1x2 quaternion array
quatZerosSyntax1(:,:,1) =
    0 + 0i + 0j + 0k
    0 + 0i + 0j + 0k
    0 + 0i + 0j + 0k
quatZerosSyntax1(:,:,2) =
    0 + 0i + 0j + 0k
    0 + 0i + 0j + 0k
    0 + 0i + 0j + 0k
```

Specify the dimensions using comma-separated integers, and then verify the equivalence of the two syntaxes:

```
quatZerosSyntax2 = zeros(3,1,2,'quaternion');
isequal(quatZerosSyntax1,quatZerosSyntax2)
ans = logical
    1
```


## Underlying Class of Quaternion Zeros

A quaternion is a four-part hyper-complex number used in three-dimensional representations. You can specify the underlying data type of the parts as single or double. The default is double.

Create a quaternion array of zeros with the underlying data type set to single.

```
quatZeros = zeros(2,'like',single(1),'quaternion')
quatZeros = 2x2 quaternion array
    0 + 0i + 0j + 0k 0 + 0i + 0j + 0k
    0 + 0i + 0j + 0k 0 + 0i + 0j + 0k
```

Verify the underlying class using the classUnderlying function.

```
classUnderlying(quatZeros)
ans =
'single'
```


## Input Arguments

## n - Size of square quaternion matrix

integer value
Size of square quaternion matrix, specified as an integer value. If $n$ is 0 or negative, then quatZeros is returned as an empty matrix.
Example: zeros (4, 'quaternion') returns a 4-by-4 matrix of quaternion zeros.
Data Types: single|double | int8| int16|int32|int64|uint8|uint16|uint32|uint64
sz - Output size
row vector of integer values
Output size, specified as a row vector of integer values. Each element of sz indicates the size of the corresponding dimension in quatZeros. If the size of any dimension is 0 or negative, then quatZeros is returned as an empty array.

Example: zeros ([1, 4, 2], 'quaternion' ) returns a 1-by-4-by-2 array of quaternion zeros.
Data Types: single|double|int8|int16|int32|int64|uint8|uint16|uint32|uint64

## prototype - Quaternion prototype

variable
Quaternion prototype, specified as a variable.
Example: zeros(2,'like', quat, 'quaternion') returns a 2-by-2 matrix of quaternions with the same underlying class as the prototype quaternion, quat.

Data Types: quaternion

## sz1,...,szN - Size of each dimension

two or more integer values
Size of each dimension, specified as two or more integers.

- If the size of any dimension is 0 , then quatZeros is returned as an empty array.
- If the size of any dimension is negative, then it is treated as 0.

Example: zeros ( 2,3 , 'quaternion' ) returns a 2-by-3 matrix of quaternion zeros.
Data Types: single | double | int8| int16|int32|int64|uint8|uint16|uint32|uint64

## Output Arguments

## quatZeros - Quaternion zeros

scalar | vector | matrix | multidimensional array

Quaternion zeros, returned as a quaternion or array of quaternions.
Given a quaternion of the form $Q=a+b \mathrm{i}+c \mathrm{j}+d \mathrm{k}$, a quaternion zero is defined as $Q=0+0 \mathrm{i}+0 \mathrm{j}+0 \mathrm{k}$.
Data Types: quaternion

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

Functions
ones
Objects
quaternion

## Topics

"Rotations, Orientation, and Quaternions"
Introduced in R2019b

## rateControl

Execute loop at fixed frequency

## Description

The rateControl object enables you to run a loop at a fixed frequency. It also collects statistics about the timing of the loop iterations. Use waitfor in the loop to pause code execution until the next time step. The loop operates every DesiredPeriod seconds, unless the enclosed code takes longer to operate. The object uses the OverrunAction property to determine how it handles longer loop operation times. The default setting, 'slip', immediately executes the loop if LastPeriod is greater than DesiredPeriod. Using 'drop' causes the waitfor method to wait until the next multiple of DesiredPeriod is reached to execute the next loop.

Tip The scheduling resolution of your operating system and the level of other system activity can affect rate execution accuracy. As a result, accurate rate timing is limited to 100 Hz for execution of MATLAB code. To improve performance and execution speeds, use code generation.

## Creation

## Syntax

rateObj = rateControl(desiredRate)
Description
rateObj = rateControl(desiredRate) creates an object that operates loops at a fixed-rate based on your system time and directly sets the DesireRate property.

## Properties

## DesiredRate - Desired execution rate

## scalar

Desired execution rate of loop, specified as a scalar in Hz. When using waitfor, the loop operates every DesiredRate seconds, unless the loop takes longer. It then begins the next loop based on the specified OverrunAction.

## DesiredPeriod - Desired time period between executions

scalar
Desired time period between executions, specified as a scalar in seconds. This property is equal to the inverse of DesiredRate.

## TotalElapsedTime - Elapsed time since construction or reset <br> scalar

Elapsed time since construction or reset, specified as a scalar in seconds.

## LastPeriod - Elapsed time between last two calls to waitfor

NaN (default) | scalar
Elapsed time between last two calls to waitfor, specified as a scalar. By default, LastPeriod is set to NaN until waitfor is called for the first time. After the first call, LastPeriod equals TotalElapsedTime.

## OverrunAction - Method for handling overruns

'slip' (default) |'drop'
Method for handling overruns, specified as one of these character vectors:

- 'drop ' - waits until the next time interval equal to a multiple of DesiredPeriod
- 'slip' - immediately executes the loop again


Each code section calls waitfor at the end of execution.

## Object Functions

waitfor Pause code execution to achieve desired execution rate statistics Statistics of past execution periods
reset Reset Rate object

## Examples

## Run Loop at Fixed Rate

Create a rate object that runs at 1 Hz .
r = rateControl(1);
Start a loop using the rateControl object inside to control the loop execution. Reset the object prior to the loop execution to reset timer. Print the iteration and time elapsed.

```
reset(r)
for i = 1:10
    time = r.TotalElapsedTime;
    fprintf('Iteration: %d - Time Elapsed: %f\n',i,time)
    waitfor(r);
end
Iteration: 1 - Time Elapsed: 0.002257
Iteration: 2 - Time Elapsed: 1.011465
Iteration: 3 - Time Elapsed: 2.011186
Iteration: 4 - Time Elapsed: 3.014202
Iteration: 5 - Time Elapsed: 4.001980
Iteration: 6 - Time Elapsed: 5.001219
Iteration: 7 - Time Elapsed: 6.000373
Iteration: 8 - Time Elapsed: 7.000181
Iteration: 9 - Time Elapsed: 8.000670
Iteration: 10 - Time Elapsed: 9.000240
```

Each iteration executes at a 1 -second interval.

## Get Statistics From Rate Object Execution

Create a rateControl object for running at 20 Hz .

```
r = rateControl(20);
```

Start a loop and control operation using the rateControl object.

```
for i = 1:30
    % Your code goes here
    waitfor(r);
end
Get Rate object statistics after loop operation.
```

```
stats = statistics(r)
```

stats = statistics(r)
stats = struct with fields:
stats = struct with fields:
Periods: [0.0633 0.0452 0.0446 0.0606 0.0458 0.0450 0.0460 ... ]
Periods: [0.0633 0.0452 0.0446 0.0606 0.0458 0.0450 0.0460 ... ]
NumPeriods: 30
NumPeriods: 30
AveragePeriod: 0.0501
AveragePeriod: 0.0501
StandardDeviation: 0.0076
StandardDeviation: 0.0076
NumOverruns: 0

```
        NumOverruns: 0
```


## Run Loop At Fixed Rate and Reset Rate Object

Create a rateControl object for running at 20 Hz .

```
r = rateControl(2);
```

Start a loop and control operation using the Rate object.

```
for i = 1:30
    % Your code goes here
    waitfor(r);
end
```

Display the rateControl object properties after loop operation.

```
disp(r)
    rateControl with properties:
        DesiredRate: 2
        DesiredPeriod: 0.5000
        OverrunAction: 'slip'
        TotalElapsedTime: 15.0107
            LastPeriod: 0.5000
```

Reset the object to restart the time statistics.

```
reset(r);
disp(r)
    rateControl with properties:
        DesiredRate: 2
        DesiredPeriod: 0.5000
        OverrunAction: 'slip'
    TotalElapsedTime: 0.0044
            LastPeriod: NaN
```


## Compatibility Considerations

## rateControl was renamed

Behavior change in future release
The rateControl object was renamed from robotics. Rate. Use rateControl for all object creation.

## See Also

rosrate|waitfor|statistics|reset
Topics
"Execute Code at a Fixed-Rate"

Introduced in R2016a

## reset

Reset Rate object

## Syntax

reset(rate)

## Description

reset (rate) resets the state of the Rate object, including the elapsed time and all statistics about previous periods. reset is useful if you want to run multiple successive loops at the same rate, or if the object is created before the loop is executed.

## Input Arguments

## rate - Rate object

handle
Rate object, specified as a handle. This object contains the information for the desired rate and other information about the execution. See rateControl for more information.

## Examples

## Run Loop At Fixed Rate and Reset Rate Object

Create a rateControl object for running at 20 Hz .
$r=$ rateControl(2);
Start a loop and control operation using the Rate object.

```
for i = 1:30
    % Your code goes here
    waitfor(r);
end
```

Display the rateControl object properties after loop operation.

```
disp(r)
    rateControl with properties:
            DesiredRate: 2
        DesiredPeriod: 0.5000
        OverrunAction: 'slip'
        TotalElapsedTime: 15.0107
            LastPeriod: 0.5000
```

Reset the object to restart the time statistics.

```
reset(r);
disp(r)
rateControl with properties:
            DesiredRate: 2
        DesiredPeriod: 0.5000
        OverrunAction: 'slip'
        TotalElapsedTime: 0.0044
            LastPeriod: NaN
```


## See Also

rateControl|waitfor

## Topics

"Execute Code at a Fixed-Rate"

Introduced in R2016a

## statistics

Statistics of past execution periods

## Syntax

stats = statistics(rate)

## Description

stats $=$ statistics(rate) returns statistics of previous periods of code execution. stats is a struct with these fields: Periods, NumPeriods, AveragePeriod, StandardDeviation, and NumOverruns.

Here is a sample execution graphic using the default setting, 'slip', for the OverrunAction property in the Rate object. See OverrunAction for more information on overrun code execution.


The output of statistics is:
stats $=$
Periods: [0.7 0.11 0.7 0.11]
NumPeriods: 4
AveragePeriod: 0.09
StandardDeviation: 0.0231
NumOverruns: 2

## Input Arguments

## rate - Rate object

handle
Rate object, specified as an object handle. This object contains the information for the DesiredRate and other info about the execution. See rateControl for more information.

## Output Arguments

## stats - Time execution statistics

structure

Time execution statistics, returned as a structure. This structure contains the following fields:

- Period - All time periods (returned in seconds) used to calculate statistics as an indexed array. stats. Period(end) is the most recent period.
- NumPeriods - Number of elements in Periods
- AveragePeriod - Average time in seconds
- StandardDeviation - Standard deviation of all periods in seconds, centered around the mean stored in AveragePeriod
- NumOverruns - Number of periods with overrun


## Examples

## Get Statistics From Rate Object Execution

Create a rateControl object for running at 20 Hz .
$r=$ rateControl(20);
Start a loop and control operation using the rateControl object.

```
for i = 1:30
    % Your code goes here
    waitfor(r);
end
Get Rate object statistics after loop operation.
```

```
stats = statistics(r)
```

stats = statistics(r)
stats = struct with fields:
Periods: [0.0633 0.0452 0.0446 0.0606 0.0458 0.0450 0.0460 ... ]
NumPeriods: 30
AveragePeriod: 0.0501
StandardDeviation: 0.0076
NumOverruns: 0

```

\section*{See Also}
rateControl|waitfor
Topics
"Execute Code at a Fixed-Rate"
Introduced in R2016a

\section*{waitfor}

Package: robotics
Pause code execution to achieve desired execution rate

\section*{Syntax}
waitfor(rate)
numMisses = waitfor(rate)

\section*{Description}
waitfor (rate) pauses execution until the code reaches the desired execution rate. The function accounts for the time that is spent executing code between wait for calls.
numMisses = waitfor(rate) returns the number of iterations missed while executing code between calls.

\section*{Examples}

\section*{Run Loop at Fixed Rate}

Create a rate object that runs at 1 Hz .
```

r = rateControl(1);

```

Start a loop using the rateControl object inside to control the loop execution. Reset the object prior to the loop execution to reset timer. Print the iteration and time elapsed.
```

reset(r)
for i = 1:10
time = r.TotalElapsedTime;
fprintf('Iteration: %d - Time Elapsed: %f\n',i,time)
waitfor(r);
end
Iteration: 1 - Time Elapsed: 0.002257
Iteration: 2 - Time Elapsed: 1.011465
Iteration: 3 - Time Elapsed: 2.011186
Iteration: 4 - Time Elapsed: 3.014202
Iteration: 5 - Time Elapsed: 4.001980
Iteration: 6 - Time Elapsed: 5.001219
Iteration: 7 - Time Elapsed: 6.000373
Iteration: 8 - Time Elapsed: 7.000181
Iteration: 9 - Time Elapsed: 8.000670
Iteration: 10 - Time Elapsed: 9.000240

```

Each iteration executes at a 1-second interval.

\section*{Input Arguments}

\section*{rate - Rate object}
handle
Rate object, specified as a handle. This object contains the information for the desired rate and other information about the execution. See rateControl for more information.

\section*{Output Arguments}
numMisses - Number of missed task executions
scalar
Number of missed task executions, returned as a scalar. waitfor returns the number of times the task was missed in the Rate object based on the LastPeriod time. For example, if the desired rate is 1 Hz and the last period was 3.2 seconds, numMisses returns 3 .

\section*{See Also}
rateControl
Topics
"Execute Code at a Fixed-Rate"

Introduced in R2016a

\section*{reedsSheppConnection}

Reeds-Shepp path connection type

\section*{Description}

The reedSheppConnection object holds information for computing a reedsSheppPathSegment object to connect between poses. A Reeds-Shepp path segment connects two poses as a sequence of five motions. The motion options are:
- Straight
- Left turn at maximum steer
- Right turn at maximum steer
- No movement

A Reeds-Shepp path segment supports both forward and backward motion.
Use this connection object to define parameters for a vehicle motion model, including the minimum turning radius and options for path types. To generate a path segment between poses using this connection type, call the connect function.

\section*{Creation}

\section*{Syntax}
reedsConnObj = reedsSheppConnection
reedsConnObj = reedsSheppConnection(Name,Value)

\section*{Description}
reedsConnObj = reedsSheppConnection creates an object using default property values.
reedsConnObj = reedsSheppConnection(Name, Value) specifies property values using namevalue pairs. To set multiple properties, specify multiple name-value pairs.

\section*{Properties}

\section*{MinTurningRadius - Minimum turning radius}

1 (default) | positive scalar in meters
Minimum turning radius for the vehicle, specified as a positive scalar in meters. The minimum turning radius is for the smallest circle the vehicle can make with maximum steer in a single direction.

Data Types: double

\section*{DisabledPathTypes - Path types to disable}
\{\} (default) | vector of string scalars | cell array of character vectors

Path types to disable, specified as a vector of string scalars or cell array of character vectors.
\begin{tabular}{|l|l|}
\hline Motion Type & Description \\
\hline "Sp", "Sn" & Straight ( \(p=\) forward, \(n=\) reverse \()\) \\
\hline "Lp", "Ln" & \begin{tabular}{l} 
Left turn at the maximum steering angle of the \\
vehicle ( \(p=\) forward, \(n=\) reverse \()\)
\end{tabular} \\
\hline "Rp", "Rn" & \begin{tabular}{l} 
Right turn at the maximum steering angle of the \\
vehicle \((p=\) forward, \(n=\) reverse \()\)
\end{tabular} \\
\hline "N" & No motion \\
\hline
\end{tabular}

If a path segment has fewer than five motion types, the remaining elements are " N " (no motion).
To see all available path types, see the AllPathTypes property.
Example: ["LpSnLp", "LnSnRpSn", "LnSnRpSnLp"]
Data Types: cell

\section*{AllPathTypes - All possible path types}
cell array of character vectors
This property is read-only.
All possible path types, specified as a cell array of character vectors. This property lists all types. To disable certain types, specify types from this list in DisabledPathTypes.

For Reeds-Shepp connections, there are 44 possible combinations of motion types.
Data Types: cell

\section*{ForwardCost - Cost multiplier to travel forward}

1 (default) | positive numeric scalar
Cost multiple to travel forward, specified as a positive numeric scalar. Increase this property to penalize forward motion.
Data Types: double

\section*{ReverseCost - Cost multiplier to travel in reverse}

1 (default) | positive numeric scalar
Cost multiple to travel in reverse, specified as a positive numeric scalar. Increase this property to penalize reverse motion.

Data Types: double

\section*{Object Functions}
connect Connect poses for given connection type

\section*{Examples}

\section*{Connect Poses Using ReedsShepp Connection Path}

Create a reedsSheppConnection object.
reedsConnObj = reedsSheppConnection;
Define start and goal poses as [x y theta] vectors.
startPose = [0 0 0];
goalPose = [1 1 pi];
Calculate a valid path segment to connect the poses.
[pathSegObj,pathCosts] = connect(reedsConnObj,startPose,goalPose);
Show the generated path.
show(pathSeg0bj\{1\})


\section*{Modify Connection Types for Reeds-Shepp Path}

Create a reedsSheppConnection object.
reedsConnObj \(=\) reedsSheppConnection;
Define start and goal poses as [x y theta] vectors.
```

startPose = [0 0 0];
goalPose = [1 1 pi];

```

Calculate a valid path segment to connect the poses.
```

[pathSegObj,pathCosts] = connect(reedsConnObj,startPose,goalPose);

```

Show the generated path. Notice the direction of the turns.
```

show(pathSegObj{1})

```

pathSeg0bj\{1\}.MotionTypes
ans \(=1 \times 5\) cell
\{'L'\} \{'R'\} \{'L'\} \{'N'\} \{'N'\}
pathSegObj\{1\}.MotionDirections
ans \(=1 \times 5\)
\(\begin{array}{lllll}1 & -1 & 1 & 1 & 1\end{array}\)

Disable this specific motion sequence in a new connection object. Reduce the MinTurningRadius if the robot is more maneuverable. Increase the reverse cost to reduce the likelihood of reverse directions being used. Connect the poses again to get a different path.
```

reedsConnObj = reedsSheppConnection('DisabledPathTypes',{'LpRnLp'});
reedsConnObj.MinTurningRadius = 0.5;
reedsConnObj.ReverseCost = 5;
[pathSegObj,pathCosts] = connect(reedsConnObj,startPose,goalPose);
pathSegObj{1}.MotionTypes
ans = 1x5 cell
{'L'} {'S'} {'L'} {'N'} {'N'}

```
show(pathSeg0bj\{1\})
xlim([0 1.5])
ylim([0 1.5])


\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}

\section*{Objects}
reedsSheppPathSegment | dubinsConnection | dubinsPathSegment

\section*{Functions}
connect | interpolate|show

Introduced in R2019b

\section*{reedsSheppPathSegment}

Reeds-Shepp path segment connecting two poses

\section*{Description}

The reedSheppPathSegment object holds information for a Reeds-Shepp path segment to connect between poses. A Reeds-Shepp path segment connects two poses as a sequence of five motion types. The motion options are:
- Straight
- Left turn at maximum steer
- Right turn at maximum steer
- No movement

\section*{Creation}

To generate a reedSheppPathSegment object, use the connect function with a reedsSheppConnection object:
reedsPathSegObj \(=\) connect (connectionObj, start, goal) connects the start and goal poses using the specified connection type object.

To specifically define a path segment:
reedsPathSeg0bj =
reedsSheppPathSegment(connectionObj, start, goal, motionLengths, motionTypes) specifies the Reeds-Shepp connection type, the start and goal poses, and the corresponding motion lengths and types. These values are set to the corresponding properties in the object.

\section*{Properties}

\section*{MinTurningRadius - Minimum turning radius of vehicle \\ positive scalar}

This property is read-only.
Minimum turning radius of the vehicle, specified as a positive scalar in meters. This value corresponds to the radius of the turning circle at the maximum steering angle of the vehicle.

Data Types: double

\section*{StartPose - Initial pose of vehicle}
\([x, y, \Theta]\) vector
This property is read-only.
Initial pose of the vehicle at the start of the path segment, specified as an \([x, y, \Theta]\) vector. \(x\) and \(y\) are in meters. \(\Theta\) is in radians.

\section*{Data Types: double}

\section*{GoalPose - Goal pose of vehicle}

\section*{\([x, y, \Theta]\) vector}

This property is read-only.
Goal pose of the vehicle at the end of the path segment, specified as an \([x, y, \Theta]\) vector. \(x\) and \(y\) are in meters. \(\Theta\) is in radians.

Data Types: double

\section*{MotionLengths - Length of each motion}
five-element numeric vector
This property is read-only.
Length of each motion in the path segment, specified as a five-element numeric vector in meters. Each motion length corresponds to a motion type specified in MotionTypes.
Data Types: double

\section*{MotionTypes - Type of each motion}
five-element string cell array
This property is read-only.
Type of each motion in the path segment, specified as a five-element string cell array.
\begin{tabular}{|l|l|}
\hline Motion Type & Description \\
\hline "S" & Straight (forward, p or reverse, n ) \\
\hline "L" & \begin{tabular}{l} 
Left turn at the maximum steering angle of the \\
vehicle (forward, p or reverse, n )
\end{tabular} \\
\hline "R" & \begin{tabular}{l} 
Right turn at the maximum steering angle of the \\
vehicle (forward, p or reverse, n )
\end{tabular} \\
\hline "N" & No motion \\
\hline
\end{tabular}

If a path segment has fewer than five motion types, the remaining elements are " \(N\) " (no motion).
Example: \{"L", "S", "R", "L", "R"\}
Data Types: cell

\section*{MotionDirections - Direction of each motion}
five-element vector of 1 s (forward motion) and -1 s (reverse motion)
This property is read-only.
Direction of each motion in the path segment, specified as a five-element vector of 1s (forward motion) and -1 s (reverse motion). Each motion direction corresponds to a motion length specified in MotionLengths and a motion type specified in MotionTypes.

When no motion occurs, that is, when a MotionTypes value is " N ", then the corresponding MotionDirections element is 1 .

Example: [-1 1 1 -1111\(]\)

Data Types: double

\section*{Length - Length of path segment}
positive scalar
This property is read-only.
Length of the path segment, specified as a positive scalar in meters. This length is just a sum of the elements in MotionLengths.
Data Types: double

\section*{Object Functions}
interpolate Interpolate poses along path segment show Visualize path segment

\section*{Examples}

\section*{Connect Poses Using ReedsShepp Connection Path}

Create a reedsSheppConnection object.
reedsConn0bj \(=\) reedsSheppConnection;
Define start and goal poses as [x y theta] vectors.
```

startPose = [0 0 0];
goalPose = [1 1 pi];

```

Calculate a valid path segment to connect the poses.
```

[pathSegObj,pathCosts] = connect(reedsConnObj,startPose,goalPose);

```

Show the generated path.
```

show(pathSeg0bj{1})

```


\section*{References}
[1] Reeds, J. A., and L. A. Shepp. "Optimal Paths for a Car That Goes Both Forwards and Backwards." Pacific Journal of Mathematics. Vol. 145, Number 2, 1990, pp. 367-393.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and C++ code using MATLAB® Coder \(^{\text {TM }}\).

\section*{See Also}
```

Objects
reedsSheppConnection | dubinsConnection|dubinsPathSegment
Functions
interpolate | show| connect
Introduced in R2019b

```

\section*{referencePathFrenet}

Smooth reference path fit to waypoints

\section*{Description}

The referencePathFrenet object fits a smooth, piecewise, continuous curve to a set of waypoints given as [ \(\mathrm{x} y\) ] or [ \(\mathrm{x} y\) theta]. After fitting, points along the curve, the path points are expressed as [x y theta kappa dkappa s], where:
- \(x y\) and theta- \(\operatorname{SE}(2)\) state expressed in global coordinates, with \(x\) and \(y\) in meters and theta in radians
- kappa - Curvature, or inverse of the radius, in meters
- dkappa - Derivative of curvature with respect to arc length in meters per second
- \(s\) - Arc length, or distance along path from path origin, in meters


Using this object, convert trajectories between global and Frenet coordinate systems, interpolate states along the path based on arc length, and query the closest point on a path from a global state.

The object expresses Frenet states as a vector of form [S dS ddS L dL ddL], where \(S\) is the arc length and \(L\) is the perpendicular deviation from the direction of the reference path. Derivatives of \(S\) are relative to time. Derivatives of \(L\) are relative to the arc length, \(S\).


Frenet States: [s \(\delta s \delta^{2} s L \delta L \delta^{2} L\) ]

\section*{Creation}

\section*{Syntax}
```

refPathObj = referencePathFrenet(waypoints)
refPathObj = referencePathFrenet(
waypoints,'DiscretizationDistance',discretionDist)
Description

```
refPathObj = referencePathFrenet(waypoints) fits a piecewise, continuous set of curves to the specified waypoints. The waypoints argument sets the Waypoints property.
```

refPathObj = referencePathFrenet(

```
waypoints,'DiscretizationDistance', discretionDist) fits a piecewise, continuous set of
curves to waypoints using the specified distance between interpolated path points. The
discretionDist argument sets the DiscretizationDistance property.

\section*{Properties}

\section*{Waypoints - Presampled points along path}
\(P\)-by-2 numeric matrix | \(P\)-by-3 numeric matrix
Presampled points along the path, specified as a \(P\)-by-2 matrix with rows of form [x y] or \(P\)-by-3 matrix with rows of form [ \(\mathrm{x} y\) theta]. Specify x and y in meters and theta in radians. \(P\) is the number of presampled points, and must be greater than or equal to two.

Data Types: single | double

\section*{PathLength - Total arclength along the path}

\section*{nonnegative scalar}

This property is read-only.
Total arclength along the path in meters.
Data Types: single | double

\section*{SegmentParameters - Clothoid parameters at start of segments}
\(N\)-by-6 matrix
This property is read-only.
Clothoid parameters at start of segments, specified as an \(N\)-by- 6 matrix where \(N\) is the total number of waypoints. Each row contains the parameters of the clothoidal segment to connect to the next consecutive waypoint and is in the form [ \(x\) y theta \(k d k s\) ] where:
- \(x y\) and theta \(-\operatorname{SE}(2)\) state expressed in global coordinates, with \(x\) and \(y\) in meters and theta in radians
- kappa - Curvature, or inverse of the radius, in meters
- dkappa - Derivative of curvature with respect to arc length in meters per second
- s-Arc length, or distance along path from path origin, in meters

\section*{Data Types: single|double}

\section*{Name-Value Pair Arguments}

Specify optional pairs of arguments as Name1=Value1, . . . ,NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: refPath = referencePathFrenet(waypoints,DiscretizationDistance=0.4)

\section*{DiscretizationDistance - Arc length between interpolated path points 0.05 (default) | positive scalar}

This property is read-only.
Arc length between interpolated path points, specified as a positive scalar in meters. The object uses interpolated path points to accelerate performance of the transformation functions frenet2global and global2frenet. A smaller discretization distance can improve accuracy at the expense of memory and computational efficiency.
Example: refPath = referencePathFrenet(waypoints,DiscretizationDistance=0.4)
Data Types: single | double
MaxNumWaypoints - Maximum waypoints allowed in path
Inf (default) | positive integer
This property is read-only.
Maximum number of waypoints allowed in the path, specified as either Inf for resizeable path or a positive integer to enforce a static limit.

If MaxNumWaypoints is set to Inf, to generate code, DynamicMemoryAllocation must be set to 'on'.

Example: refPath = referencePathFrenet(waypoints,MaxNumWaypoints=10)
Data Types: single | double

\section*{Object Functions}
closestPoint
closestPointsToSequence
closestProjections
curvature
changeInCurvature
tangentAngle frenet2global global2frenet interpolate show

Find closest point on reference path to global point
Projects sequence of points onto path
Find orthogonal projections between path tangent vector and query point
Return curvature at arclength
Return change-in-curvature at arclength
Return tangent angle at arclength
Convert Frenet states to global states
Convert global states to Frenet states
Interpolate reference path at provided arc lengths
Display reference path in figure

\section*{Examples}

\section*{Generate Alternative Trajectories for Reference Path}

Generate alternative trajectories for a reference path using Frenet coordinates. Specify different initial and terminal states for your trajectories. Tune your states based on the generated trajectories.

Generate a reference path from a set of waypoints. Create a trajectoryGeneratorFrenet object from the reference path.
```

waypoints = [0 0; ...
50 20; ...
100 0; ...
150 10];
refPath = referencePathFrenet(waypoints);
connector = trajectoryGeneratorFrenet(refPath);

```

Generate a five-second trajectory between the path origin and a point 30 m down the path as Frenet states.
```

initState = [0 0 0 0 0 0]; % [S ds ddS L dL ddL]
termState = [30 0 0 0 0 0]; % [S ds ddS L dL ddL]
[~,trajGlobal] = connect(connector,initState,termState,5);

```

Display the trajectory in global coordinates.
```

show(refPath);
hold on
axis equal
plot(trajGlobal.Trajectory(:,1),trajGlobal.Trajectory(:,2),'b')
legend(["Waypoints","Reference Path","Trajectory to 30m"])

```


Create a matrix of terminal states with lateral deviations between -3 m and 3 m . Generate trajectories that cover the same arc length in 10 seconds, but deviate laterally from the reference path. Display the new alternative paths.
```

termStateDeviated = termState + ([-3:3]' * [0 0 0 1 0 0]);
[~,trajGlobal] = connect(connector,initState,termStateDeviated,10);
clf
show(refPath);
hold on
axis equal
for i = 1:length(trajGlobal)
plot(trajGlobal(i).Trajectory(:,1),trajGlobal(i).Trajectory(:,2),'g')
end
legend(["Waypoints","Reference Path","Alternative Trajectories"])
hold off

```


Specify a new terminal state to generate a new trajectory. This trajectory is not desirable because it requires reverse motion to achieve a lateral velocity of \(10 \mathrm{~m} / \mathrm{s}\).
newTermState = [5 10 0 5 0 0];
[~,newTrajGlobal] = connect(connector,initState,newTermState,3);
clf
show(refPath);
hold on
axis equal
plot(newTrajGlobal.Trajectory(:,1),newTrajGlobal.Trajectory(:,2),'b'); legend(["Waypoint","Reference Path","New Trajectory"]) hold off


Relax the restriction on the longitudinal state by specifying an arc length of NaN. Generate and display the trajectory again. The new position shows a good alternative trajectory that deviates off the reference path.
```

relaxedTermState = [NaN 10 0 5 0 0];
[~,trajGlobalRelaxed] = connect(connector,initState,relaxedTermState,3);
clf
show(refPath);
hold on
axis equal
plot(trajGlobalRelaxed.Trajectory(:,1),trajGlobalRelaxed.Trajectory(:,2),'g');
hold off

```


\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and C++ code using MATLAB® Coder \(^{\text {TM }}\).
Starting in MATLAB R2022a, default behavior for referencePathFrenet has changed which may result in backwards compatibility issues. referencePathFrenet now supports fixed-size code generation (DynamicMemoryAllocation="off"). To restore previous behavior, the MaxNumWaypoints property and DynamicMemoryAllocation must be set to Inf and 'on' respectively.
- If MaxNumWaypoints is specified, the returned path is variably-sized but the maximum size of the path is set is by the MaxNumWaypoints property, regardless of DynamicMemoryAllocation.
- If DynamicMemoryAllocation is set to 'on' and:
- If waypoints are compile-time constant, then the returned path is fixed-size.
- If waypoints are variably-sized, then the returned path is variably-sized and unbounded.
- If DynamicMemoryAllocation is set to 'on' and:
- If waypoints are fixed-sized, then the returned path is fixed-size.
- If waypoints are variably sized without specifying MaxNumWaypoints, then the path is invalid and causes an error.

\section*{See Also}
```

Objects
trajectoryGeneratorFrenet | navPath
Functions
closestPoint|frenet2global|global2frenet|interpolate| show
Topics
"Highway Trajectory Planning Using Frenet Reference Path"
Introduced in R2020b

```

\section*{changeInCurvature}

Return change-in-curvature at arclength

\section*{Syntax}
dkappa = changeInCurvature(refPath,S)

\section*{Description}
dkappa = changeInCurvature(refPath,S) calculates the change-in-curvature with respect to change-in-arclength, dkappa, of the reference path at a given arclength, S .

\section*{Input Arguments}
refPath - Reference path
referencePathFrenet object
Reference path, specified as a referencePathFrenet object.

\section*{S - Path arclengths}
\(N\)-element column vector
Path arclengths, specified as an \(N\)-element column vector in meters, where \(N\) is the total number of desired arclengths to calculate.

\section*{Output Arguments}

\section*{dkappa - Change-in-curvature angles}
\(N\)-element vector
Change-in-curvature angles, specified as an \(N\)-element vector in radians, where \(N\) is the total number of desired arclengths to calculate.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder \(^{\text {TM }}\).

\section*{See Also}
```

Objects
referencePathFrenet | trajectoryGeneratorFrenet | navPath
Functions
frenet2global|global2frenet|closestPoint| closestPointsToSequence|
closestProjections|curvature| tangentAngle| interpolate| show

```

\section*{Topics}
"Highway Trajectory Planning Using Frenet Reference Path" Introduced in R2022a

\section*{closestPoint}

Find closest point on reference path to global point

\section*{Syntax}
```

pathPoints = closestPoint(refPath,points)
[pathPoints,inWindow] = closestPoint(refPath,points)
[_] = closestPoint(refPath,points,searchWindow)

```

\section*{Description}
pathPoints \(=\) closestPoint(refPath, points) finds the closest point on the reference path to each of the specified ( \(x, y\) )-positions points.
[pathPoints,inWindow] = closestPoint(refPath,points) optionally returns a logical vector inWindow, specifying whether each point for the corresponding \(x y\) coordinate in points is projected within the search window..
[_] = closestPoint(refPath, points,searchWindow) optionally accepts a nondecreasing row vector searchWindow, which defines the interval of the path to use to find the closest points.

\section*{Examples}

\section*{Generate Trajectory from Reference Path}

Generate a reference path from a set of waypoints.
```

waypoints = [0 0; 50 20; 100 0; 150 10];
refPath = referencePathFrenet(waypoints);

```

Create a trajectoryGeneratorFrenet object from the reference path.
```

connector = trajectoryGeneratorFrenet(refPath);

```

Generate a five-second trajectory between the path origin and a point 30 m down the path as Frenet states.
```

initState = [0 0 0 0 0 0]; % [S dS ddS L dL ddL]
termState = [30 0 0 0 0 0]; % [S dS ddS L dL ddL]
frenetTraj = connect(connector,initState,termState,5);

```

Convert the trajectory to the global states.
```

globalTraj = frenet2global(refPath,frenetTraj.Trajectory);

```

Display the reference path and the trajectory.
```

show(refPath);
axis equal
hold on
plot(globalTraj(:,1),globalTraj(:,2),'b')

```

Specify global points and find the closest points on reference path.
```

globalPoints = waypoints(2:end,:) + [20 -50];
nearestPathPoint = closestPoint(refPath,globalPoints);

```

Display the global points and the closest points on reference path.
```

plot(globalPoints(:,1),globalPoints(:,2),'r*','MarkerSize',10)
plot(nearestPathPoint(:,1),nearestPathPoint(:,2),'b*','MarkerSize',10)

```

Interpolate between the arc lengths of the first two closest points along the reference path.
```

arclengths = linspace(nearestPathPoint(1,6),nearestPathPoint(2,6),10);
pathStates = interpolate(refPath,arclengths);

```

Display the interpolated path points.
```

plot(pathStates(:,1),pathStates(:,2),'g')

```
legend(["Waypoints", "Reference Path","Trajectory to 30m",...
    "Global Points","Closest Points","Interpolated Path Points"])


\section*{Input Arguments}

\section*{refPath - Reference path}
referencePathFrenet object
Reference path, specified as a referencePathFrenet object.

\section*{points - Global points}
\(P\)-by-2 numeric matrix
Global points, specified as a \(P\)-by-2 numeric matrix with rows of the form \([x y] . P\) is the number of points. Positions are in meters.

\section*{Output Arguments}

\section*{pathPoints - Closest points on reference path}
\(N\)-by-6 numeric matrix
Closest points on the reference path, returned as an \(N\)-by-6 numeric matrix with rows of form [x y theta kappa dkappa s], where:
- \(x y\) and theta \(-\operatorname{SE}(2)\) state expressed in global coordinates, with \(x\) and \(y\) in meters and theta in radians
- kappa - Curvature, or inverse of the radius, in meters
- dkappa - Derivative of curvature with respect to arc length in meters per second
- s-Arc length, or distance along path from path origin, in meters
\(N\) is the number of points sampled along the reference path.

\section*{inWindow - Indicator of points being in search window}

\section*{\(N\)-element logical column vector}

Indication whether each point nearest to the corresponding \(x y\) coordinate in points, is projected within the search window, returned as an \(N\)-element logical row vector, where \(N\) is the number of points in points. Points being projected within the search window are true, or false if they lie at the end of a window.

\section*{searchWindow - Search window}
\(N\)-element nondecreasing row vector
Search window on path to determine closest points, specified as an \(N\)-element nondecreasing row vector, where \(N\) is the number of points in points.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}

Objects
referencePathFrenet | trajectoryGeneratorFrenet | navPath

\section*{Functions}
frenet2global|global2frenet|closestPointsToSequence|closestProjections|
curvature| changeInCurvature|tangentAngle|interpolate|show

\section*{Topics}
"Highway Trajectory Planning Using Frenet Reference Path"

Introduced in R2020b

\section*{closestPointsToSequence}

Projects sequence of points onto path

\section*{Syntax}
pathPoints = closestPointsToSequence(refPath,points,initWindow)
[pathPoints,inWindow] = closestPointsToSequence(refPath,points,initWindow)

\section*{Description}
pathPoints = closestPointsToSequence(refPath, points,initWindow) uses the closest point within a sequence of points, points, to be within the valid search window, initWindow. For each point in Points, the search window is centered at the previous point.
[pathPoints,inWindow] = closestPointsToSequence(refPath,points,initWindow) optionally returns a logical vector inWindow, specifying whether each point for the corresponding \(x y\) coordinate in points is projected within the search window.

\section*{Input Arguments}
refPath - Reference path
referencePathFrenet object
Reference path, specified as a referencePathFrenet object.

\section*{points - Global points}
\(P\)-by-2 numeric matrix
Global points, specified as a \(P\)-by-2 numeric matrix with rows of the form [xy]. \(P\) is the number of points. Positions are in meters.

\section*{initWindow - Initial search window}
two-element row vector
Initial search window, specified as a two-element row vector in the form [minimum_bound maximum_bound].

\section*{Output Arguments}

\section*{pathPoints - Closest points on reference path}
\(N\)-by-6 numeric matrix
Closest points on the reference path, returned as an \(N\)-by-6 numeric matrix with rows of form [x y theta kappa dkappa s], where:
- \(x y\) and theta-SE(2) state expressed in global coordinates, with \(x\) and \(y\) in meters and theta in radians
- kappa - Curvature, or inverse of the radius, in meters
- dkappa - Derivative of curvature with respect to arc length in meters per second
- s - Arc length, or distance along path from path origin, in meters
\(N\) is the number of points sampled along the reference path.

\section*{inWindow - Indicator of points being in search window}
\(N\)-element logical column vector
Indication whether each point nearest to the corresponding \(x y\) coordinate in points, is projected within the search window, returned as an \(N\)-element logical row vector, where \(N\) is the number of points in points. Points being projected within the search window are true, or false if they lie at the end of a window.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and \(\mathrm{C}++\) code using MATLAB® \(\mathrm{Coder}^{\mathrm{TM}}\).

\section*{See Also}
```

Objects
referencePathFrenet | trajectoryGeneratorFrenet | navPath

```

\section*{Functions}
frenet2global|global2frenet|closestPoint|closestProjections|curvature|
changeInCurvature| tangentAngle|interpolate|show

\section*{Topics}
"Highway Trajectory Planning Using Frenet Reference Path"

Introduced in R2022a

\section*{closestProjections}

Find orthogonal projections between path tangent vector and query point

\section*{Syntax}
[arclengths,distances] = closestProjections(refPath, points)
[___, projPoints] = closestProjections(refPath, points)
[__] = closestProjections(refPath, points,bestN)
[___ ] = closestProjections(refPath, points,intervals)
[___] = closestProjections(refPath, points,intervals,bestN)

\section*{Description}
[arclengths,distances] = closestProjections(refPath, points) attempts to project each \(x y\) point in the points matrix, onto each clothoid segment contained in the reference path, refPath, such that the projection vector is orthogonal to the path tangent-angle. Returns closest orthogonal projection between the curve and query point in each segment as a pair of two cell arrays, arclengths and distances containing the arclengths and distances respectively.
\(\qquad\) ,projPoints] = closestProjections(refPath, points) optionally returns the projected points, projPoints as a cell array containing path data evaluated at the corresponding arclengths element.
[ ___ ] = closestProjections(refPath, points,bestN) returns the nearest projections, bestNfor each xy point in points.
[___ ] = closestProjections(refPath, points,intervals) accepts an optional matrix of arclengths intervals, intervals, where each row contains a lower and upper arclength bounds.
[___] = closestProjections(refPath, points,intervals, bestN) returns up to the nearest projections bestN for each xy point in points.

\section*{Input Arguments}

\section*{refPath - Reference path}
referencePathFrenet object
Reference path, specified as a referencePathFrenet object.

\section*{points - Global points}
\(P\)-by-2 numeric matrix
Global points, specified as a \(P\)-by-2 numeric matrix with rows of the form [x y]. \(P\) is the number of points. Positions are in meters.

\section*{bestN - Best \(\boldsymbol{N}\) projections}
scalar in the range \([1, N]\)
Best \(N\) projections, specified as a scalar in the range \([1, N]\), where \(N\) is the number of segments in the path.

\section*{intervals - Arclength intervals}

\section*{N -by-2 matrix}

Arclength intervals, specified as a \(N\)-by-2 matrix, where each row is of the form [minimum_arclength, maximum_arclength] in meters, and \(N\) is the number of segments in the path.

\section*{Output Arguments}

\section*{arclengths - Arclengths between curve and query points}
\(M\)-element cell array
Arclengths between curve and query points, returned as an \(M\)-element cell array, where \(M\) is the number of query points in the points input. Each cell contains a \(P\)-element column vector, where \(P\) is in the range \([0, N]\) and \(N\) is the number of segments in the path.

\section*{distances - Distances between curve and query points}
\(M\)-element cell array
Distances between curve and query points, returned as an \(M\)-element cell array, where \(M\) is the number of query points in the points input. Each cell contains a \(P\)-element column vector, where \(P\) is in the range \([0, N]\) and \(N\) is the number of segments in the path.

\section*{projPoints - Projected points}
\(M\)-element cell array
Projected points, returned as an \(M\)-element cell array, where \(M\) is the number of query points in the points input. Each cell contains a \(P\)-by- 6 matrix, where \(P\) is in the range \([0, N]\) and each row is in the form [ \(x\) y theta \(k d k s\) ]. \(x, y\), theta, \(k, d k, s\), are the x and y positions, tangent angle, curvature, change in curvature, at the arclength, \(s\), respectively.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and C++ code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}

\section*{Objects}
referencePathFrenet | trajectoryGeneratorFrenet | navPath

\section*{Functions}
frenet2global|global2frenet|closestPoint|closestPointsToSequence|curvature| changeInCurvature | tangentAngle |interpolate | show

\section*{Topics}
"Highway Trajectory Planning Using Frenet Reference Path"

Introduced in R2022a

\section*{curvature}

Return curvature at arclength

\section*{Syntax}
kappa = curvature(refPath,S)

\section*{Description}
kappa \(=\) curvature(refPath, S\()\) calculates the curvature angle, kappa of the reference path at a given arclength, S.

\section*{Input Arguments}
refPath - Reference path
referencePathFrenet object
Reference path, specified as a referencePathFrenet object.

\section*{S - Path arclengths}
\(N\)-element column vector
Path arclengths, specified as an \(N\)-element column vector in meters, where \(N\) is the total number of desired arclengths to calculate.

\section*{Output Arguments}

\section*{kappa - Curvature angles}
\(N\)-element vector
Change-in-curvature angles, specified as an \(N\)-element vector in radians, where \(N\) is the total number of desired arclengths to calculate.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder \(^{\text {TM }}\).

\section*{See Also}
```

Objects
referencePathFrenet | trajectoryGeneratorFrenet | navPath
Functions
frenet2global|global2frenet|closestPoint| closestPointsToSequence|
closestProjections| changeInCurvature|tangentAngle|interpolate| show

```

\section*{Topics}
"Highway Trajectory Planning Using Frenet Reference Path" Introduced in R2022a

\section*{frenet2global}

Convert Frenet states to global states

\section*{Syntax}
globalState = frenet2global(refPath,frenetState)
globalState = frenet2global(refPath,frenetState,latTimeDerivatives)

\section*{Description}
globalState \(=\) frenet2global(refPath,frenetState) converts Frenet trajectory states to global states.
globalState = frenet2global(refPath,frenetState,latTimeDerivatives) accepts latTimeDerivatives containing 1st and 2nd order derivatives of lateral deviation with respect to time and a flag indicating if the heading should flip during the conversion to global coordinates.

\section*{Examples}

\section*{Generate Trajectory from Reference Path}

Generate a reference path from a set of waypoints.
```

waypoints = [0 0; 50 20; 100 0; 150 10];
refPath = referencePathFrenet(waypoints);

```

Create a trajectoryGeneratorFrenet object from the reference path.
```

connector = trajectoryGeneratorFrenet(refPath);

```

Generate a five-second trajectory between the path origin and a point 30 m down the path as Frenet states.
```

initState = [0 0 0 0 0 0]; % [S dS ddS L dL ddL]
termState = [30 0 0 0 0 0]; % [S dS ddS L dL ddL]
frenetTraj = connect(connector,initState,termState,5);

```

Convert the trajectory to the global states.
```

globalTraj = frenet2global(refPath,frenetTraj.Trajectory);

```

Display the reference path and the trajectory.
```

show(refPath);
axis equal
hold on
plot(globalTraj(:,1),globalTraj(:,2),'b')

```

Specify global points and find the closest points on reference path.
globalPoints = waypoints(2:end,:) + [20-50];
nearestPathPoint \(=\) closestPoint(refPath,globalPoints);

Display the global points and the closest points on reference path.
```

plot(globalPoints(:,1),globalPoints(:,2),'r*','MarkerSize',10)
plot(nearestPathPoint(:,1),nearestPathPoint(:,2),'b*','MarkerSize',10)

```

Interpolate between the arc lengths of the first two closest points along the reference path.
```

arclengths = linspace(nearestPathPoint(1,6),nearestPathPoint(2,6),10);

```
pathStates \(=\) interpolate(refPath,arclengths);

Display the interpolated path points.
plot(pathStates(:,1), pathStates(:,2),'g')
legend(["Waypoints","Reference Path","Trajectory to 30m",...
"Global Points","Closest Points","Interpolated Path Points"])


\section*{Input Arguments}
refPath - Reference path
referencePathFrenet object
Reference path, specified as a referencePathFrenet object.

\section*{frenetState - Trajectory in Frenet coordinate frame}
\(P\)-by-6 numeric matrix

Trajectory in the Frenet coordinate frame, returned as a \(P\)-by-6 numeric matrix with rows of form [S \(d S\) ddS \(L\) dL ddL], where \(S\) is the arc length and \(L\) is the perpendicular deviation from the direction of the reference path. Derivatives of \(S\) are relative to time. Derivatives of \(L\) are relative to the arc length, S. \(P\) is the number of Frenet states specified.

\section*{latTimeDerivatives - Lateral time derivatives}
\(N\)-by-3 matrix
Lateral time derivatives, specified as an \(N\)-by-3 matrix where each row is of the form [ \(d L / d t d d L / d t \wedge 2\) invertHeading] and \(N\) is the total number of points in points. Each row contains the 1st and 2nd order time derivatives of lateral deviation and a flag, invertHeading, which indicates whether the heading should be flipped when converting to global coordinates (true) or not (false).

Note If defining latTimeDerivatives without the use of global2frenet, the following rules should be followed:

1 The invertHeading flag should be true when:
a The vehicle is moving in reverse (speed is less than 0 )
b The vehicle is stationary (speed is equal to 0 ), and the vehicle is facing away from the path's tangent vector. i.e. \(\cos (\mid\) tangentAngle \((o b j, S)\)-thetaExpected \(\mid)<0\)
2 If 1 b is true, then \(d L / d S\) must be negated.

\section*{Output Arguments}

\section*{globalState - Trajectory in global coordinate frame}
\(P\)-by-6 numeric matrix
Trajectories in the global coordinate frame, specified as a \(P\)-by- 6 numeric matrix with rows of form [ x y theta kappa speed accel], where:
- \(x y\) and theta -- SE(2) state expressed in global coordinates, with \(x\) and \(y\) in meters and theta in radians
- kappa -- Curvature, or inverse of the radius, in meters
- speed -- Speed in the theta direction in \(\mathrm{m} / \mathrm{s}\)
- accel -- Acceleration in the theta direction in \(\mathrm{m} / \mathrm{s}^{2}\)
\(P\) is the number of Frenet trajectories converted to global trajectories.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}

\section*{Objects}
referencePathFrenet | trajectoryGeneratorFrenet | navPath

\section*{Functions}
global2frenet|closestPoint|closestPointsToSequence|closestProjections| curvature \| changeInCurvature \| tangentAngle \| interpolate \| show

\section*{Topics}
"Highway Trajectory Planning Using Frenet Reference Path"

Introduced in R2020b

\section*{global2frenet}

Convert global states to Frenet states

\section*{Syntax}
frenetState = global2frenet(refPath,globalState)
[_, latTimeDerivatives] = global2frenet(refPath,globalState)
[_] = global2frenet(refPath,globalState,sFrame)

\section*{Description}
frenetState \(=\) global2frenet(refPath, globalState) converts global states to Frenet trajectory states.
[_,latTimeDerivatives] = global2frenet(refPath,globalState) returns latTimeDerivatives containing 1st and 2nd order derivatives of lateral deviation with respect to time and a flag indicating if the heading should flip when converting to global coordinates.
[_] = global2frenet(refPath,globalState, sFrame) accepts a vector of arclengths, sFrame at which the Frenet frame should be centered at.

\section*{Input Arguments}
refPath - Reference path
referencePathFrenet object
Reference path, specified as a referencePathFrenet object.

\section*{globalState - Trajectory in global coordinate frame}
\(P\)-by-6 numeric matrix
Trajectories in the global coordinate frame, specified as a \(P\)-by- 6 numeric matrix with rows of form [ x y theta kappa speed accel], where:
- \(x y\) and theta -- SE(2) state expressed in global coordinates, with \(x\) and \(y\) in meters and theta in radians
- kappa -- Curvature, or inverse of the radius, in meters
- speed -- Speed in the theta direction in \(\mathrm{m} / \mathrm{s}\)
- accel -- Acceleration in the theta direction in \(\mathrm{m} / \mathrm{s}^{2}\)
\(P\) is the number of Frenet trajectories converted to global trajectories.

\section*{sFrame - Arclength frame locations}
\(N\)-element vector
Arclength center locations for the Frenet frames, specified as an \(N\)-element vector in meters. For correct results, the vector between the frame and the \(x y\) location of the globalState must be orthogonal to the tangent angle.

\section*{Output Arguments}

\section*{frenetState - Trajectory in Frenet coordinate frame}

P-by-6 numeric matrix
Trajectory in the Frenet coordinate frame, returned as a \(P\)-by- 6 numeric matrix with rows of form [S \(d S\) ddS \(L d L d d L]\), where \(S\) is the arc length and \(L\) is the perpendicular deviation from the direction of the reference path. Derivatives of \(S\) are relative to time. Derivatives of \(L\) are relative to the arc length, S. \(P\) is the number of Frenet states specified.

\section*{latTimeDerivatives - Lateral time derivatives}

N -by-3 matrix
Lateral time derivatives, specified as an \(N\)-by-3 matrix where each row is of the form [ \(d L / d t d d L / d t \wedge 2\) invertHeading] and \(N\) is the total number of points in points. Each row contains the 1 st and 2 nd order time derivatives of lateral deviation and a flag, invertHeading, which indicates whether the heading should be flipped when converting to global coordinates (true) or not (false).

Note If defining latTimeDerivatives without the use of global2frenet, the following rules should be followed:

1 The invertHeading flag should be true when:
a The vehicle is moving in reverse (speed is less than 0 )
b The vehicle is stationary (speed is equal to 0 ), and the vehicle is facing away from the path's tangent vector. i.e. \(\cos (\mid\) tangentAngle(obj,S)-thetaExpected|) \(<0\)
2 If 1 b is true, then \(d L / d S\) must be negated.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and \(\mathrm{C}++\) code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).

\section*{See Also}

\section*{Objects}
referencePathFrenet | trajectoryGeneratorFrenet | navPath

\section*{Functions}
frenet2global|closestPoint|closestPointsToSequence|closestProjections|
curvature| changeInCurvature|tangentAngle|interpolate|show

\section*{Topics}
"Highway Trajectory Planning Using Frenet Reference Path"

\section*{Introduced in R2020b}

\section*{interpolate}

Interpolate reference path at provided arc lengths

\section*{Syntax}
pathPoints = interpolate(refPath,arclengths)

\section*{Description}
pathPoints = interpolate(refPath,arclengths) interpolates the reference path at the provided arc lengths and returns the interpolated points on the path in global coordinates.

\section*{Examples}

\section*{Generate Trajectory from Reference Path}

Generate a reference path from a set of waypoints.
```

waypoints = [0 0; 50 20; 100 0; 150 10];
refPath = referencePathFrenet(waypoints);

```

Create a trajectoryGeneratorFrenet object from the reference path.
```

connector = trajectoryGeneratorFrenet(refPath);

```

Generate a five-second trajectory between the path origin and a point 30 m down the path as Frenet states.
```

initState = [0 0 0 0 0 0]; % [S dS ddS L dL ddL]
termState = [30 0 0 0 0 0]; % [S dS ddS L dL ddL]
frenetTraj = connect(connector,initState,termState,5);

```

Convert the trajectory to the global states.
```

globalTraj = frenet2global(refPath,frenetTraj.Trajectory);

```

Display the reference path and the trajectory.
```

show(refPath);
axis equal
hold on
plot(globalTraj(:,1),globalTraj(:,2),'b')

```

Specify global points and find the closest points on reference path.
```

globalPoints = waypoints(2:end,:) + [20 -50];
nearestPathPoint = closestPoint(refPath,globalPoints);

```

Display the global points and the closest points on reference path.
```

plot(globalPoints(:,1),globalPoints(:,2),'r*','MarkerSize',10)

```
plot(nearestPathPoint(:,1), nearestPathPoint(:,2),'b*','MarkerSize',10)

Interpolate between the arc lengths of the first two closest points along the reference path.
```

arclengths = linspace(nearestPathPoint(1,6),nearestPathPoint(2,6),10);
pathStates = interpolate(refPath,arclengths);

```

Display the interpolated path points.
plot(pathStates(:,1), pathStates(:,2),'g')
legend(["Waypoints","Reference Path","Trajectory to 30m",...
"Global Points","Closest Points","Interpolated Path Points"])


\section*{Input Arguments}
refPath - Reference path
referencePathFrenet object
Reference path, specified as a referencePathFrenet object.

\section*{arclengths - Distances along reference path}
\(N\)-element vector
Distances along the reference path, specified as an \(N\)-element vector. \(N\) is the number of arc lengths at which to sample points. Each distance is in meters.

\section*{Output Arguments}

\section*{pathPoints - Points on reference path}
\(N\)-by-6 numeric matrix
Points on the reference path, returned as an \(N\)-by- 6 numeric matrix with rows of form [x y theta kappa dkappa s], where:
- \(x y\) and theta-SE(2) state expressed in global coordinates, with \(x\) and \(y\) in meters and theta in radians
- kappa - Curvature, or inverse of the radius, in meters
- dkappa - Derivative of curvature with respect to arc length in meters per second
- s - Arc length, or distance along path from path origin, in meters
\(N\) is the number of points sampled along the reference path.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}
```

Objects
referencePathFrenet | trajectoryGeneratorFrenet | navPath

```

\section*{Functions}
closestPoint|closestPointsToSequence |closestProjections|curvature| changeInCurvature|tangentAngle|frenet2global|global2frenet|show

\section*{Topics}
"Highway Trajectory Planning Using Frenet Reference Path"

\section*{Introduced in R2020b}

\section*{show}

Display reference path in figure

\section*{Syntax}
```

show(refPath)
show(refPath,'Parent',parentAx)
ax = show(

```
\(\qquad\)
``` )
```


## Description

show (refPath) displays the reference path and its lateral states in the current figure.
show(refPath, 'Parent', parentAx) displays the reference path on the specified axes. parentAx is specified as an Axes handle.
ax = show( $\qquad$ ) displays the reference path using any of the previous input combinations and returns the axes handle on which the reference path is plotted.

## Examples

## Generate Alternative Trajectories for Reference Path

Generate alternative trajectories for a reference path using Frenet coordinates. Specify different initial and terminal states for your trajectories. Tune your states based on the generated trajectories.

Generate a reference path from a set of waypoints. Create a trajectoryGeneratorFrenet object from the reference path.

```
waypoints = [0 0; ...
    50 20; ...
    100 0; ...
    150 10];
refPath = referencePathFrenet(waypoints);
connector = trajectoryGeneratorFrenet(refPath);
```

Generate a five-second trajectory between the path origin and a point 30 m down the path as Frenet states.

```
initState = [0 0 0 0 0 0]; % [S ds ddS L dL ddL]
termState = [30 0 0 0 0 0]; % [S ds ddS L dL ddL]
[~,trajGlobal] = connect(connector,initState,termState,5);
```

Display the trajectory in global coordinates.

```
show(refPath);
hold on
axis equal
plot(trajGlobal.Trajectory(:,1),trajGlobal.Trajectory(:,2),'b')
legend(["Waypoints","Reference Path","Trajectory to 30m"])
```



Create a matrix of terminal states with lateral deviations between -3 m and 3 m . Generate trajectories that cover the same arc length in 10 seconds, but deviate laterally from the reference path. Display the new alternative paths.

```
termStateDeviated = termState + ([-3:3]' * [0 0 0 1 0 0]);
[~,trajGlobal] = connect(connector,initState,termStateDeviated,10);
clf
show(refPath);
hold on
axis equal
for i = 1:length(trajGlobal)
    plot(trajGlobal(i).Trajectory(:,1),trajGlobal(i).Trajectory(:,2),'g')
end
legend(["Waypoints","Reference Path","Alternative Trajectories"])
hold off
```



Specify a new terminal state to generate a new trajectory. This trajectory is not desirable because it requires reverse motion to achieve a lateral velocity of $10 \mathrm{~m} / \mathrm{s}$.
newTermState = [5 10 050 0];
[~,newTrajGlobal] = connect(connector,initState,newTermState,3);
clf
show(refPath);
hold on
axis equal
plot(newTrajGlobal.Trajectory(:,1),newTrajGlobal.Trajectory(:,2),'b'); legend(["Waypoint","Reference Path","New Trajectory"]) hold off


Relax the restriction on the longitudinal state by specifying an arc length of NaN. Generate and display the trajectory again. The new position shows a good alternative trajectory that deviates off the reference path.

```
relaxedTermState = [NaN 10 0 5 0 0];
[~,trajGlobalRelaxed] = connect(connector,initState,relaxedTermState,3);
clf
show(refPath);
hold on
axis equal
plot(trajGlobalRelaxed.Trajectory(:,1),trajGlobalRelaxed.Trajectory(:,2),'g');
hold off
```



## Input Arguments

refPath - Reference path
referencePathFrenet object
Reference path, specified as a referencePathFrenet object.

## Output Arguments

ax - Axes on which the reference path is plotted
Axes handle
Axes on which the reference path is plotted, returned as an Axes handle.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

Objects
referencePathFrenet | trajectoryGeneratorFrenet | navPath

## Functions

closestPoint|closestPoint|closestPointsToSequence|closestProjections| curvature | changeInCurvature \| tangentAngle\|frenet2global|global2frenet| interpolate

## Topics

"Highway Trajectory Planning Using Frenet Reference Path"

## Introduced in R2020b

## tangentAngle

Return tangent angle at arclength

## Syntax

theta $=$ tangentAngle(refPath,S)

## Description

theta $=$ tangentAngle(refPath, S$)$ calculates the tangent angle, theta, of the reference path at specified arclength, S .

## Input Arguments

refPath - Reference path
referencePathFrenet object
Reference path, specified as a referencePathFrenet object.

## S - Path arclengths

$N$-element column vector
Path arclengths, specified as an $N$-element column vector in meters, where $N$ is the total number of desired arclengths to calculate.

## Output Arguments

## theta - Path tangent angles

$N$-element vector
Path tangent angles, specified as an $N$-element vector in radians, where $N$ is the total number of desired arclengths to calculate.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

```
Objects
referencePathFrenet | trajectoryGeneratorFrenet | navPath
Functions
frenet2global|global2frenet|closestPoint | closestPointsToSequence|
closestProjections|curvature| changeInCurvature|interpolate|show
```


## Topics

"Highway Trajectory Planning Using Frenet Reference Path" Introduced in R2022a

## resamplingPolicyPF

Create resampling policy object with resampling settings

## Description

The resamplingPolicyPF object stores settings for when resampling should occur when using a particle filter for state estimation. The object contains the method that triggers resampling and the relevant threshold for this resampling. Use this object as the ResamplingPolicy property of the stateEstimatorPF object.

## Creation

## Syntax

policy = resamplingPolicyPF
Description
policy $=$ resamplingPolicyPF creates a resamplingPolicyPF object policy, which contains properties to be modified to control when resampling should be triggered. Use this object as the ResamplingPolicy property of the stateEstimatorPF object.

## Properties

## TriggerMethod - Method for determining if resampling should occur <br> 'ratio' (default)| character vector

Method for determining if resampling should occur, specified as a character vector. Possible choices are 'ratio' and 'interval'. The 'interval' method triggers resampling at regular intervals of operating the particle filter. The 'ratio' method triggers resampling based on the ratio of effective total particles.

## SamplingInterval - Fixed interval between resampling

1 (default) | scalar
Fixed interval between resampling, specified as a scalar. This interval determines during which correction steps the resampling is executed. For example, a value of 2 means the resampling is executed every second correction step. A value of inf means that resampling is never executed.

This property only applies with the TriggerMethod is set to 'interval'.

## MinEffectiveParticleRatio - Minimum desired ratio of effective to total particles 0.5 (default) | scalar

Minimum desired ratio of effective to total particles, specified as a scalar. The effective number of particles is a measure of how well the current set of particles approximates the posterior distribution. A lower effective particle ratio means less particles are contributing to the estimation and resampling
might be required. If the ratio of effective particles to total particles falls below the MinEffectiveParticleRatio, a resampling step is triggered.

## See Also

stateEstimatorPF|correct
Introduced in R2019b

## SkyPlotChart Properties

Sky plot chart appearance and behavior

## Description

The SkyPlotChart properties control the appearance of a sky plot chart generated using the skyplot function. To modify the chart appearance, use dot notation on the SkyPlotChart object:

```
h = skyplot;
h.AzimuthData = [45 120 295];
h.ElevationData = [10 45 60];
h.Labels = ["G1" "G4" "G11"];
```


## Properties

## Sky Plot Properties

## AzimuthData - Azimuth angles for visible satellite positions

$n$-element vector of angles
Azimuth angles for visible satellite positions, specified as an $n$-element vector of angles. $n$ is the number of visible satellite positions in the plot. Angles are measured in degrees, clockwise-positive from the North direction.

Example: [25 45182 356]
Data Types: double

## ElevationData - Elevation angles for visible satellite positions <br> $n$-element vector of angles

Elevation angles for visible satellite positions, specified as an $n$-element vector of angles. $n$ is the number of visible satellite positions in the plot. Angles are measured from the horizon line with 90 degrees being directly up.
Example: [45 9027 74]
Data Types: double

## LabelData - Labels for visible satellite positions <br> $n$-element string array

Labels for visible satellite positions, specified as an $n$-element string array. $n$ is the number of visible satellite positions in the plot.
Example: ["G1" "G11" "G7" "G3"]

## Data Types: string

## GroupData - Group for each satellite position <br> categorical array

Group for each satellite position, specified as a categorical array. Each group has a different color label defined by the ColorOrder property.

Example: [GPS GPS Galileo Galileo]
Data Types: double

## ColorOrder - Color order

seven predefined colors (default) | three-column matrix of RGB triplets
Color order, specified as a three-column matrix of RGB triplets. This property defines the palette of colors MATLAB uses to create plot objects such as Line, Scatter, and Bar objects. Each row of the array is an RGB triplet. An RGB triplet is a three-element vector whose elements specify the intensities of the red, green, and blue components of a color. The intensities must be in the range [ 0, 1]. This table lists the default colors.

| Colors | ColorOrder Matrix |  |  |
| :---: | :---: | :---: | :---: |
|  | $\begin{array}{lr} \text { [ } 0 \\ 0.8500 \\ 0.9290 \\ 0.4940 \\ 0.4660 \\ 0.3010 \\ 0.6350 \end{array}$ | 0.4470 <br> 0.3250 <br> 0.6940 <br> 0.1840 <br> 0.6740 <br> 0.7450 <br> 0.0780 | 0.7410 <br> 0.0980 <br> 0.1250 <br> 0.5560 <br> 0.1880 <br> 0.9330 <br> $0.1840]$ |

MATLAB assigns colors to objects according to their order of creation. For example, when plotting lines, the first line uses the first color, the second line uses the second color, and so on. If there are more lines than colors, then the cycle repeats.

You can also set the color order using the colororder function.

## Label Properties

## LabelFontSize - Font size of labels

scalar numeric value
Font size of labels, specified as a scalar numeric value. The default font depends on the specific operating system and locale.

Example: h = skyplot(__,'LabelFontSize',12)
Example: h.LabelFontSize = 12

## LabelFontSizeMode - Selection mode for font size of labels

## 'auto' (default)|'manual'

Selection mode for the font size of labels, specified as one of these values:

- 'auto' - Font size specified by MATLAB. If you resize the axes to be smaller than the default size, the font size can scale down to improve readability and layout.
- 'manual ' - Font size specified manually. MATLAB does not scale the font size as the axes size changes. To specify the font size, set the LabelFontSize property.


## Chart Properties

## HandleVisibility - Visibility of object handle

'on' (default)| 'off'|'callback'
Visibility of the SkyPlotChart object handle in the Children property of the parent, specified as one of these values:

- 'on ' - Object handle is always visible.
- 'off' - Object handle is invisible at all times. This option is useful for preventing unintended changes to the UI by another function. To temporarily hide the handle during the execution of that function, set the HandleVisibility to 'off'.
- ' callback' - Object handle is visible from within callbacks or functions invoked by callbacks, but not from within functions invoked from the command line. This option blocks access to the object at the command line, but allows callback functions to access it.

If the object is not listed in the Children property of the parent, then functions that obtain object handles by searching the object hierarchy or querying handle properties cannot return it. This includes get, findobj, gca, gcf, gco, newplot, cla, clf, and close.

Hidden object handles are still valid. Set the root ShowHiddenHandles property to 'on' to list all object handles, regardless of their HandleVisibility property setting.

## Layout - Layout options

empty LayoutOptions array (default)| TiledChartLayoutOptions object | GridLayoutOptions object

Layout options, specified as a TiledChartLayoutOptions or GridLayoutOptions object. This property is useful when the chart is either in a tiled chart layout or a grid layout.

To position the chart within the grid of a tiled chart layout, set the Tile and TileSpan properties on the TiledChartLayoutOptions object. For example, consider a 3-by-3 tiled chart layout. The layout has a grid of tiles in the center, and four tiles along the outer edges. In practice, the grid is invisible and the outer tiles do not take up space until you populate them with axes or charts.


This code places the chart c in the third tile of the grid..
c. Layout.Tile = 3;

To make the chart span multiple tiles, specify the TileSpan property as a two-element vector. For example, this chart spans 2 rows and 3 columns of tiles.
c.Layout.TileSpan = [2 3];

To place the chart in one of the surrounding tiles, specify the Tile property as ' north ', 'south', 'east', or 'west'. For example, setting the value to 'east' places the chart in the tile to the right of the grid.
c.Layout.Tile = 'east';

To place the chart into a layout within an app, specify this property as a GridLayout0ptions object. For more information about working with grid layouts in apps, see uigridlayout.

If the chart is not a child of either a tiled chart layout or a grid layout (for example, if it is a child of a figure or panel) then this property is empty and has no effect.

## Parent - Parent container

Figure object | Panel object | Tab object | TiledChartLayout object | GridLayout object
Parent container, specified as a Figure, Panel, Tab, TiledChartLayout, or GridLayout object.

## Marker Properties

## MarkerEdgeAlpha - Marker edge transparency

1 (default) | scalar in range [0,1]|'flat'
Marker edge transparency, specified as a scalar in the range [ 0,1 ] or ' $f$ lat '. A value of 1 is opaque and 0 is completely transparent. Values between 0 and 1 are semitransparent.

To set the edge transparency to a different value for each point in the plot, set the AlphaData property to a vector the same size as the XData property, and set the MarkerEdgeAlpha property to 'flat'.

## MarkerEdgeColor - Marker outline color

'flat' (default) | 'auto' | RGB triplet \| hexadecimal color code | 'r'| 'g' | 'b' | ...
Marker outline color, specified as 'auto', an RGB triplet, a hexadecimal color code, a color name, or a short name. The value of 'auto' uses the same color as the Color property.

For a custom color, specify an RGB triplet or a hexadecimal color code.

- An RGB triplet is a three-element row vector whose elements specify the intensities of the red, green, and blue components of the color. The intensities must be in the range [0, 1]. For example, [0.4 0.6 0.7].
- A hexadecimal color code is a character vector or a string scalar that starts with a hash symbol (\#) followed by three or six hexadecimal digits, which can range from 0 to $F$. The values are not case sensitive. Thus, the color codes '\#FF8800', '\#ff8800', '\#F80', and '\#f80' are equivalent.

Alternatively, you can specify some common colors by name. This table lists the named color options, the equivalent RGB triplets, and the hexadecimal color codes.

| Color Name | Short Name | RGB Triplet | Hexadecimal <br> Color Code | Appearance |
| :--- | :--- | :--- | :--- | :--- |
| 'red' | 'r' | $\left[\begin{array}{lll}1 & 0 & 0\end{array}\right]$ | '\#FF0000' |  |
| 'green' | 'g' | $\left[\begin{array}{lll}0 & 1 & 0\end{array}\right]$ | $' \# 00 F F 00 '$ |  |
| 'blue' | 'b' | $\left[\begin{array}{lll}0 & 0 & 1\end{array}\right]$ | '\#0000FF' |  |
| 'cyan' | 'c' | $\left[\begin{array}{lll}0 & 1 & 1\end{array}\right]$ | '\#00FFFF' |  |
| 'magenta' | 'm' | $\left[\begin{array}{lll}1 & 0 & 1\end{array}\right]$ | '\#FF00FF' |  |
| 'yellow' | 'y' | $\left[\begin{array}{lll}1 & 1 & 0\end{array}\right]$ | '\#FFFF00' |  |
| 'black' | 'k' | $\left[\begin{array}{lll}0 & 0 & 0\end{array}\right]$ | '\#000000' |  |
| 'white' | 'w' | $\left[\begin{array}{lll}1 & 1 & 1\end{array}\right]$ | '\#FFFFFF' |  |
| 'none' | Not <br> applicable | Not applicable | Not applicable | No color |

This table shows the RGB triplets and hexadecimal color codes for the default colors MATLAB uses in many types of plots.

| RGB Triplet | Hexadecimal Color Code | Appearance |
| :---: | :---: | :---: |
| [0 0.4470 0.7410] | '\#0072BD' |  |
| [0.8500 0.3250 0.0980] | '\#D95319' |  |
| [0.9290 0.6940 0.1250] | '\#EDB120' |  |
| [0.4940 0.1840 0.5560] | '\#7E2F8E' | $\square$ |
| [0.4660 0.6740 0.1880] | '\#77AC30' | $\square$ |
| [0.3010 0.7450 0.9330] | '\#4DBEEE' | $\square$ |
| [0.6350 0.0780 0.1840] | '\#A2142F' |  |

## MarkerFaceAlpha - Marker face transparency

0.6 (default) | scalar in range [0,1] | 'flat'

Marker face transparency, specified as a scalar in the range [ 0,1 ] or ' $f$ lat'. A value of 1 is opaque and 0 is completely transparent. Values between 0 and 1 are partially transparent.

To set the marker face transparency to a different value for each point, set the AlphaData property to a vector the same size as the XData property, and set the MarkerFaceAlpha property to 'flat '.

## MarkerFaceColor - Marker fill color

'flat' (default) | 'auto' | 'none' | RGB triplet | hexadecimal color code | 'r' | 'g' | 'b' | ...
Marker fill color, specified as 'flat', 'auto', an RGB triplet, a hexadecimal color code, a color name, or a short name. The 'flat' option uses the CData values. The 'auto' option uses the same color as the Color property for the axes.

For a custom color, specify an RGB triplet or a hexadecimal color code.

- An RGB triplet is a three-element row vector whose elements specify the intensities of the red, green, and blue components of the color. The intensities must be in the range [ 0,1 ; for example, [0.4 0.6 0.7].
- A hexadecimal color code is a character vector or a string scalar that starts with a hash symbol (\#) followed by three or six hexadecimal digits, which can range from 0 to $F$. The values are not case sensitive. Thus, the color codes '\#FF8800', '\#ff8800', '\#F80', and '\#f80' are equivalent.

Alternatively, you can specify some common colors by name. This table lists the named color options, the equivalent RGB triplets, and hexadecimal color codes.

| Color Name | Short Name | RGB Triplet | Hexadecimal <br> Color Code | Appearance |
| :--- | :--- | :--- | :--- | :--- |
| 'red' | 'r' | $\left[\begin{array}{lll}1 & 0 & 0\end{array}\right]$ | $' \# F F 0000 '$ |  |
| 'green' | 'g' | $\left[\begin{array}{lll}0 & 1 & 0\end{array}\right]$ | $' \# 00 F F 00 '$ |  |
| 'blue' | 'b' | $\left[\begin{array}{lll}0 & 0 & 1\end{array}\right]$ | $' \# 0000 F F^{\prime}$ |  |
| 'cyan' | 'c' | $\left[\begin{array}{lll}0 & 1 & 1\end{array}\right]$ | $' \# 00 F F F F^{\prime}$ |  |
| 'magenta' | 'm' | $\left[\begin{array}{lll}1 & 0 & 1\end{array}\right]$ | $' \# F F 00 F F^{\prime}$ |  |
| 'yellow' | 'y' | $\left[\begin{array}{lll}1 & 1 & 0\end{array}\right]$ | $' \# F F F F 00 '$ |  |
| 'black' | 'k' | $\left[\begin{array}{lll}0 & 0 & 0\end{array}\right]$ | $' \# 000000 '$ |  |
| 'white' | 'w' | $\left[\begin{array}{lll}1 & 1 & 1\end{array}\right]$ | '\#FFFFFF' |  |
| 'none' | Not <br> applicable | Not applicable | Not applicable | No color |

Here are the RGB triplets and hexadecimal color codes for the default colors MATLAB uses in many types of plots.

| RGB Triplet | Hexadecimal Color Code | Appearance |
| :---: | :---: | :---: |
| [0 0.4470 0.7410] | '\#0072BD ' |  |
| [0.8500 0.3250 0.0980] | '\#D95319' |  |
| [0.9290 0.6940 0.1250] | '\#EDB120' |  |
| [0.4940 0.1840 0.5560] | '\#7E2F8E' |  |
| [0.4660 0.6740 0.1880] | '\#77AC30' | $\square$ |
| [0.3010 0.7450 0.9330] | '\#4DBEEE ' |  |
| [0.6350 0.0780 0.1840] | '\#A2142F' |  |

Example: [0.3 0.2 0.1]
Example: 'green'
Example: '\#D2F9A7'

## MarkerSizeData - Marker size

100 (default) | positive scalar | vector of positive values
Marker size, specified as a positive scalar or vector of positive values in points, where one point = $1 / 72$ of an inch. If specified as a vector, the vector must be of the same length as AzimuthData.

## Position

## PositionConstraint - Position to hold constant

'outerposition' | 'innerposition'

Position property to hold constant when adding, removing, or changing decorations, specified as one of the following values:

- 'outerposition' - The OuterPosition property remains constant when you add, remove, or change decorations such as a title or an axis label. If any positional adjustments are needed, MATLAB adjusts the InnerPosition property.
- 'innerposition' - The InnerPosition property remains constant when you add, remove, or change decorations such as a title or an axis label. If any positional adjustments are needed, MATLAB adjusts the OuterPosition property.

Note Setting this property has no effect when the parent container is a TiledChartLayout.

## OuterPosition - Outer size and location

[0 0 1 1] (default)|four-element vector
Outer size and location of the skyplot within the parent container (typically a figure, panel, or tab), specified as a four-element vector of the form [left bottom width height]. The outer position includes the colorbar, title, and axis labels.

- The left and bottom elements define the distance from the lower-left corner of the container to the lower-left corner of the skyplot.
- The width and height elements are the skyplot dimensions, which include the skyplot cells, plus a margin for the surrounding text and colorbar.

The default value of [ $\left.\begin{array}{llll}0 & 0 & 1 & 1\end{array}\right]$ covers the whole interior of the container. The units are normalized relative to the size of the container. To change the units, set the Units property.

Note Setting this property has no effect when the parent container is a TiledChartLayout.

## InnerPosition - Inner size and location

[0.1300 0.11000 .77500 .8114$]$ (default)|four-element vector
Inner size and location of the skyplot within the parent container (typically a figure, panel, or tab), specified as a four-element vector of the form [left bottom width height]. The inner position does not include the colorbar, title, or axis labels.

- The left and bottom elements define the distance from the lower-left corner of the container to the lower-left corner of the skyplot.
- The width and height elements are the skyplot dimensions, which include only the skyplot cells.

Note Setting this property has no effect when the parent container is a TiledChartLayout.

## Position - Inner size and location

four-element vector
Inner size and location of the skyplot within the parent container (typically a figure, panel, or tab), specified as a four-element vector of the form [left bottom width height]. This property is equivalent to the InnerPosition property.

Note Setting this property has no effect when the parent container is a TiledChartLayout.

## Units - Position units

'normalized' (default)|'inches' |'centimeters'|'points'|'pixels'|'characters'
Position units, specified as one of these values.

| Units | Description |
| :---: | :---: |
| 'normalized' (default) | Normalized with respect to the container, which is typically the figure or a panel. The lower left corner of the container maps to ( 0,0 ), and the upper right corner maps to $(1,1)$. |
| 'inches' | Inches. |
| 'centimeters' | Centimeters. |
| 'characters' | Based on the default uicontrol font of the graphics root object: <br> - Character width $=$ width of letter x . <br> - Character height $=$ distance between the baselines of two lines of text. |
| 'points' | Typography points. One point equals 1/72 inch. |
| 'pixels' | Pixels. <br> Starting in R2015b, distances in pixels are independent of your system resolution on Windows ${ }^{\circledR}$ and Macintosh systems: <br> - On Windows systems, a pixel is $1 / 96$ th of an inch. <br> - On Macintosh systems, a pixel is $1 / 72$ nd of an inch. <br> On Linux ${ }^{\circledR}$ systems, the size of a pixel is determined by your system resolution. |

When specifying the units as a name-value argument during object creation, you must set the Units property before specifying the properties that you want to use these units, such as OuterPosition.

## Visible - State of visibility <br> ' on ' (default) | on/off logical value

State of visibility, specified as ' on ' or 'off', or as numeric or logical 1 (true) or 0 (false). A value of 'on' is equivalent to true, and 'off' is equivalent to false. Thus, you can use the value of this property as a logical value. The value is stored as an on/off logical value of type matlab.lang.OnOffSwitchState.

- 'on' - Display the skyplot.
- 'off' - Hide the skyplot without deleting it. You can still access the properties of an invisible SkyPlotChart object.


## See Also

## Functions

skyplot | polarscatter
Objects
gnssSensor|nmeaParser

Introduced in R2021a

## stateEstimatorPF

Create particle filter state estimator

## Description

The stateEstimatorPF object is a recursive, Bayesian state estimator that uses discrete particles to approximate the posterior distribution of the estimated state.

The particle filter algorithm computes the state estimate recursively and involves two steps: prediction and correction. The prediction step uses the previous state to predict the current state based on a given system model. The correction step uses the current sensor measurement to correct the state estimate. The algorithm periodically redistributes, or resamples, the particles in the state space to match the posterior distribution of the estimated state.

The estimated state consists of state variables. Each particle represents a discrete state hypothesis of these state variables. The set of all particles is used to help determine the final state estimate.

You can apply the particle filter to arbitrary nonlinear system models. Process and measurement noise can follow arbitrary non-Gaussian distributions.

For more information on the particle filter workflow and setting specific parameters, see:

- "Particle Filter Workflow"
- "Particle Filter Parameters"


## Creation

## Syntax

pf = stateEstimatorPF

## Description

pf = stateEstimatorPF creates an object that enables the state estimation for a simple system with three state variables. Use the initialize method to initialize the particles with a known mean and covariance or uniformly distributed particles within defined bounds. To customize the particle filter's system and measurement models, modify the StateTransitionFcn and MeasurementLikelihoodFcn properties.

After you create the object, use initialize to initialize the NumStateVariables and NumParticles properties. The initialize function sets these two properties based on your inputs.

## Properties

## NumStateVariables - Number of state variables

3 (default) | scalar

This property is read-only.
Number of state variables, specified as a scalar. This property is set based on the inputs to the initialize method. The number of states is implicit based on the specified matrices for initial state and covariance.

## NumParticles - Number of particles used in the filter

1000 (default) | scalar
This property is read-only.
Number of particles using in the filter, specified as a scalar. You can specify this property only by calling the initialize method.

## StateTransitionFcn - Callback function for determining the state transition between particle filter steps

function handle
Callback function for determining the state transition between particle filter steps, specified as a function handle. The state transition function evolves the system state for each particle. The function signature is:

```
function predictParticles = stateTransitionFcn(pf,prevParticles,varargin)
```

The callback function accepts at least two input arguments: the stateEstimatorPF object, pf, and the particles at the previous time step, prevParticles. These specified particles are the predictParticles returned from the previous call of the object. predictParticles and prevParticles are the same size: NumParticles-by-NumStateVariables.

You can also use varargin to pass in a variable number of arguments from the predict function. When you call:
predict(pf,arg1,arg2)
MATLAB essentially calls stateTranstionFcn as:
stateTransitionFcn(pf,prevParticles,arg1,arg2)

## MeasurementLikelihoodFcn - Callback function calculating the likelihood of sensor measurements

function handle
Callback function calculating the likelihood of sensor measurements, specified as a function handle. Once a sensor measurement is available, this callback function calculates the likelihood that the measurement is consistent with the state hypothesis of each particle. You must implement this function based on your measurement model. The function signature is:

```
function likelihood = measurementLikelihoodFcn(PF,predictParticles,measurement,varargin)
```

The callback function accepts at least three input arguments:
1 pf - The associated stateEstimatorPF object
2 predictParticles - The particles that represent the predicted system state at the current time step as an array of size NumParticles-by-NumStateVariables
3 measurement - The state measurement at the current time step

You can also use varargin to pass in a variable number of arguments. These arguments are passed by the correct function. When you call:
correct(pf, measurement, arg1, arg2)
MATLAB essentially calls measurementLikelihoodFcn as:
measurementLikelihoodFcn(pf,predictParticles, measurement, arg1, arg2)
The callback needs to return exactly one output, likelihood, which is the likelihood of the given measurement for each particle state hypothesis.

## IsStateVariableCircular - Indicator if state variables have a circular distribution [0 0 0] (default) | logical array

Indicator if state variables have a circular distribution, specified as a logical array. Circular (or angular) distributions use a probability density function with a range of [-pi, pi]. If the object has multiple state variables, then IsStateVariableCircular is a row vector. Each vector element indicates if the associated state variable is circular. If the object has only one state variable, then IsStateVariableCircular is a scalar.

## ResamplingPolicy - Policy settings that determine when to trigger resampling

 objectPolicy settings that determine when to trigger resampling, specified as an object. You can trigger resampling either at fixed intervals, or you can trigger it dynamically, based on the number of effective particles. See resamplingPolicyPF for more information.

## ResamplingMethod - Method used for particle resampling

'multinomial' (default)| 'residual'| 'stratified'|'systematic'
Method used for particle resampling, specified as 'multinomial', 'residual', 'stratified', and 'systematic'.

## StateEstimationMethod - Method used for state estimation

'mean' (default)|'maxweight'
Method used for state estimation, specified as 'mean' and 'maxweight'.

## Particles - Array of particle values

NumParticles-by-NumStateVariables matrix
Array of particle values, specified as a NumParticles-by-NumStateVariables matrix. Each row corresponds to the state hypothesis of a single particle.

## Weights - Particle weights

NumParticles-by-1 vector
Particle weights, specified as a NumParticles-by-1 vector. Each weight is associated with the particle in the same row in the Particles property.

## State - Best state estimate

vector
This property is read-only.

Best state estimate, returned as a vector with length NumStateVariables. The estimate is extracted based on the StateEstimationMethod property.

## State Covariance - Corrected system covariance

$N$-by- $N$ matrix | [ ]
This property is read-only.
Corrected system variance, returned as an $N$-by- $N$ matrix, where $N$ is equal to the NumStateVariables property. The corrected state is calculated based on the StateEstimationMethod property and the MeasurementLikelihoodFcn. If you specify a state estimate method that does not support covariance, then the property is set to [].

## Object Functions

initialize Initialize the state of the particle filter
getStateEstimate Extract best state estimate and covariance from particles
predict
Predict state of robot in next time step
correct
Adjust state estimate based on sensor measurement

## Examples

## Particle Filter Prediction and Correction

Create a stateEstimatorPF object, and execute a prediction and correction step for state estimation. The particle filter gives a predicted state estimate based on the return value of StateTransitionFcn. It then corrects the state based on a given measurement and the return value of MeasurementLikelihoodFcn.

Create a particle filter with the default three states.

```
pf = stateEstimatorPF
pf =
    stateEstimatorPF with properties:
            NumStateVariables: 3
                        NumParticles: 1000
        StateTransitionFcn: @nav.algs.gaussianMotion
        MeasurementLikelihoodFcn: @nav.algs.fullStateMeasurement
        IsStateVariableCircular: [0 0 0]
            ResamplingPolicy: [1x1 resamplingPolicyPF]
            ResamplingMethod: 'multinomial'
        StateEstimationMethod: 'mean'
            StateOrientation: 'row'
                        Particles: [1000x3 double]
                        Weights: [1000x1 double]
                            State: 'Use the getStateEstimate function to see the value.'
            StateCovariance: 'Use the getStateEstimate function to see the value.'
```

Specify the mean state estimation method and systematic resampling method.

```
pf.StateEstimationMethod = 'mean';
pf.ResamplingMethod = 'systematic';
```

Initialize the particle filter at state [4 19] with unit covariance (eye (3)). Use 5000 particles.

```
initialize(pf,5000,[4 1 9],eye(3));
```

Assuming a measurement [4.2 0.9 9], run one predict and one correct step.

```
[statePredicted,stateCov] = predict(pf);
[stateCorrected,stateCov] = correct(pf,[4.2 0.9 9]);
```

Get the best state estimate based on the StateEstimationMethod algorithm.

```
stateEst = getStateEstimate(pf)
stateEst = 1×3
    4.1562 0.9185 9.0202
```


## Estimate Robot Position in a Loop Using Particle Filter

Use the stateEstimatorPF object to track a robot as it moves in a 2-D space. The measured position has random noise added. Using predict and correct, track the robot based on the measurement and on an assumed motion model.

Initialize the particle filter and specify the default state transition function, the measurement likelihood function, and the resampling policy.

```
pf = stateEstimatorPF;
pf.StateEstimationMethod = 'mean';
pf.ResamplingMethod = 'systematic';
```

Sample 1000 particles with an initial position of [0 0] and unit covariance.

```
initialize(pf,1000,[0 0],eye(2));
```

Prior to estimation, define a sine wave path for the dot to follow. Create an array to store the predicted and estimated position. Define the amplitude of noise.

```
t = 0:0.1:4*pi;
dot = [t; sin(t)]';
robotPred = zeros(length(t),2);
robotCorrected = zeros(length(t),2);
noise = 0.1;
```

Begin the loop for predicting and correcting the estimated position based on measurements. The resampling of particles occurs based on theResamplingPolicy property. The robot moves based on a sine wave function with random noise added to the measurement.

```
for i = 1:length(t)
    % Predict next position. Resample particles if necessary.
    [robotPred(i,:),robotCov] = predict(pf);
    % Generate dot measurement with random noise. This is
    % equivalent to the observation step.
    measurement(i,:) = dot(i,:) + noise*(rand([1 2])-noise/2);
    % Correct position based on the given measurement to get best estimation.
```

```
    % Actual dot position is not used. Store corrected position in data array.
    [robotCorrected(i,:),robotCov] = correct(pf,measurement(i,:));
end
```

Plot the actual path versus the estimated position. Actual results may vary due to the randomness of particle distributions.

```
plot(dot(:,1),dot(:,2),robotCorrected(:,1),robotCorrected(:,2),'or')
xlim([0 t(end)])
ylim([-1 1])
legend('Actual position','Estimated position')
grid on
```



The figure shows how close the estimate state matches the actual position of the robot. Try tuning the number of particles or specifying a different initial position and covariance to see how it affects tracking over time.

## Compatibility Considerations

## stateEstimatorPF was renamed

Behavior change in future release
The stateEstimatorPF object was renamed from robotics. ParticleFilter. Use stateEstimatorPF for all object creation.

## References

[1] Arulampalam, M.S., S. Maskell, N. Gordon, and T. Clapp. "A Tutorial on Particle Filters for Online Nonlinear/Non-Gaussian Bayesian Tracking." IEEE Transactions on Signal Processing. Vol. 50, No. 2, Feb 2002, pp. 174-188.
[2] Chen, Z. "Bayesian Filtering: From Kalman Filters to Particle Filters, and Beyond." Statistics. Vol. 182, No. 1, 2003, pp. 1-69.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

resamplingPolicyPF|initialize|getStateEstimate|predict|correct
Topics
"Track a Car-Like Robot Using Particle Filter" (Robotics System Toolbox)
"Particle Filter Parameters"
"Particle Filter Workflow"

Introduced in R2016a

## copy

Create copy of particle filter

## Syntax

b $=\operatorname{copy}(\mathrm{a})$

## Description

$b=\operatorname{copy}(a)$ copies each element in the array of handles, $a$, to the new array of handles, $b$.
The copy method does not copy dependent properties. MATLAB does not call copy recursively on any handles contained in property values. MATLAB also does not call the class constructor or property-set methods during the copy operation.

## Input Arguments

a - Object array
handle
Object array, specified as a handle.

## Output Arguments

## b - Object array containing copies of the objects in a handle

Object array containing copies of the object in a, specified as a handle.
$b$ has the same number of elements and is the same size and class of $a$. $b$ is the same class $a s a$. If $a$ is empty, b is also empty. If a is heterogeneous, b is also heterogeneous. If a contains deleted handles, then copy creates deleted handles of the same class in b . Dynamic properties and listeners associated with objects in a are not copied to objects in b.

## See Also

stateEstimatorPF| resamplingPolicyPF |initialize| getStateEstimate|predict| correct

## Topics

"Track a Car-Like Robot Using Particle Filter" (Robotics System Toolbox)
"Particle Filter Parameters"
"Particle Filter Workflow"

Introduced in R2016a

## correct

Adjust state estimate based on sensor measurement

## Syntax

[stateCorr,stateCov] = correct(pf,measurement)
[stateCorr,stateCov] = correct(pf,measurement, varargin)

## Description

[stateCorr,stateCov] = correct(pf,measurement) calculates the corrected system state and its associated uncertainty covariance based on a sensor measurement at the current time step. correct uses the MeasurementLikelihoodFcn property from the particle filter object, pf, as a function to calculate the likelihood of the sensor measurement for each particle. The two inputs to the MeasurementLikelihoodFcn function are:

1 pf - The stateEstimatorPF object, which contains the particles of the current iteration
2 measurement - The sensor measurements used to correct the state estimate
The MeasurementLikelihoodFcn function then extracts the best state estimate and covariance based on the setting in the StateEstimationMethod property.
[stateCorr,stateCov] = correct(pf,measurement,varargin) passes all additional arguments in varargin to the underlying MeasurementLikelihoodFcn after the first three required inputs.

## Examples

## Particle Filter Prediction and Correction

Create a stateEstimatorPF object, and execute a prediction and correction step for state estimation. The particle filter gives a predicted state estimate based on the return value of StateTransitionFcn. It then corrects the state based on a given measurement and the return value of MeasurementLikelihoodFcn.

Create a particle filter with the default three states.

```
pf = stateEstimatorPF
pf =
    stateEstimatorPF with properties:
            NumStateVariables: 3
                    NumParticles: 1000
            StateTransitionFcn: @nav.algs.gaussianMotion
        MeasurementLikelihoodFcn: @nav.algs.fullStateMeasurement
        IsStateVariableCircular: [0 0 0]
            ResamplingPolicy: [1x1 resamplingPolicyPF]
            ResamplingMethod: 'multinomial'
        StateEstimationMethod: 'mean'
```

```
StateOrientation: 'row'
    Particles: [1000x3 double]
        Weights: [1000x1 double]
            State: 'Use the getStateEstimate function to see the value.'
StateCovariance: 'Use the getStateEstimate function to see the value.'
```

Specify the mean state estimation method and systematic resampling method.

```
pf.StateEstimationMethod = 'mean';
pf.ResamplingMethod = 'systematic';
```

Initialize the particle filter at state [4 19] with unit covariance (eye (3)). Use 5000 particles.

```
initialize(pf,5000,[4 1 9],eye(3));
```

Assuming a measurement [4.2 0.9 9], run one predict and one correct step.

```
[statePredicted,stateCov] = predict(pf);
[stateCorrected,stateCov] = correct(pf,[4.2 0.9 9]);
```

Get the best state estimate based on the StateEstimationMethod algorithm.

```
stateEst = getStateEstimate(pf)
stateEst = 1\times3
    4.1562 0.9185 9.0202
```


## Input Arguments

pf - stateEstimatorPF object
handle
stateEstimatorPF object, specified as a handle. See stateEstimatorPF for more information.
measurement - Sensor measurements
array
Sensor measurements, specified as an array. This input is passed directly into the MeasurementLikelihoodFcn property of pf. It is used to calculate the likelihood of the sensor measurement for each particle.

## varargin - Variable-length input argument list

comma-separated list
Variable-length input argument list, specified as a comma-separated list. This input is passed directly into the MeasurementLikelihoodFcn property of pf. It is used to calculate the likelihood of the sensor measurement for each particle. When you call:
correct (pf, measurement, arg1, arg2)
MATLAB essentially calls measurementLikelihoodFcn as:
measurementLikelihoodFcn(pf, measurement, arg1, arg2)

## Output Arguments

## stateCorr - Corrected system state

vector with length NumStateVariables
Corrected system state, returned as a row vector with length NumStateVariables. The corrected state is calculated based on the StateEstimationMethod algorithm and the MeasurementLikelihoodFcn.
stateCov - Corrected system covariance
$N$-by- $N$ matrix | [ ]
Corrected system variance, returned as an $N$-by- $N$ matrix, where $N$ is the value of NumStateVariables property from pf. The corrected state is calculated based on the StateEstimationMethod algorithm and the MeasurementLikelihoodFcn. If you specify a state estimate method that does not support covariance, then the function returns stateCov as [].

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

stateEstimatorPF|resamplingPolicyPF|initialize|getStateEstimate|predict| correct

## Topics

"Track a Car-Like Robot Using Particle Filter" (Robotics System Toolbox)
"Particle Filter Parameters"
"Particle Filter Workflow"

Introduced in R2016a

## getStateEstimate

Extract best state estimate and covariance from particles

## Syntax

```
stateEst = getStateEstimate(pf)
```

[stateEst, stateCov] = getStateEstimate(pf)

## Description

stateEst = getStateEstimate(pf) returns the best state estimate based on the current set of particles. The estimate is extracted based on the StateEstimationMethod property from the stateEstimatorPF object, pf.
[stateEst, stateCov] = getStateEstimate(pf) also returns the covariance around the state estimate. The covariance is a measure of the uncertainty of the state estimate. Not all state estimate methods support covariance output. In this case, getStateEstimate returns stateCov as [].

## Examples

## Particle Filter Prediction and Correction

Create a stateEstimatorPF object, and execute a prediction and correction step for state estimation. The particle filter gives a predicted state estimate based on the return value of StateTransitionFcn. It then corrects the state based on a given measurement and the return value of MeasurementLikelihoodFcn.

Create a particle filter with the default three states.

```
pf = stateEstimatorPF
pf =
    stateEstimatorPF with properties:
            NumStateVariables: 3
                    NumParticles: 1000
            StateTransitionFcn: @nav.algs.gaussianMotion
        MeasurementLikelihoodFcn: @nav.algs.fullStateMeasurement
        IsStateVariableCircular: [0 0 0]
            ResamplingPolicy: [1x1 resamplingPolicyPF]
            ResamplingMethod: 'multinomial'
        StateEstimationMethod: 'mean'
            StateOrientation: 'row'
                        Particles: [1000x3 double]
                Weights: [1000x1 double]
                        State: 'Use the getStateEstimate function to see the value.'
            StateCovariance: 'Use the getStateEstimate function to see the value.'
```

Specify the mean state estimation method and systematic resampling method.

```
pf.StateEstimationMethod = 'mean';
pf.ResamplingMethod = 'systematic';
```

Initialize the particle filter at state [4 19] with unit covariance (eye (3)). Use 5000 particles.

```
initialize(pf,5000,[4 1 9],eye(3));
```

Assuming a measurement [4.2 0.9 9], run one predict and one correct step.

```
[statePredicted,stateCov] = predict(pf);
[stateCorrected,stateCov] = correct(pf,[4.2 0.9 9]);
```

Get the best state estimate based on the StateEstimationMethod algorithm.

```
stateEst = getStateEstimate(pf)
stateEst = 1\times3
    4.1562 0.9185 9.0202
```


## Input Arguments

pf - stateEstimatorPF object
handle
stateEstimatorPF object, specified as a handle. See stateEstimatorPF for more information.

## Output Arguments

## stateEst - Best state estimate

vector
Best state estimate, returned as a row vector with length NumStateVariables. The estimate is extracted based on the StateEstimationMethod algorithm specified in pf.

## stateCov - Corrected system covariance

$N$-by- $N$ matrix | [ ]
Corrected system variance, returned as an $N$-by- $N$ matrix, where $N$ is the value of NumStateVariables property from pf. The corrected state is calculated based on the StateEstimationMethod algorithm and the MeasurementLikelihoodFcn. If you specify a state estimate method that does not support covariance, then the function returns stateCov as [].

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

stateEstimatorPF|resamplingPolicyPF|initialize| getStateEstimate|predict| correct

Topics<br>"Track a Car-Like Robot Using Particle Filter" (Robotics System Toolbox)<br>"Particle Filter Parameters"<br>"Particle Filter Workflow"<br>Introduced in R2016a

## initialize

Initialize the state of the particle filter

## Syntax

```
initialize(pf,numParticles,mean,covariance)
initialize(pf,numParticles,stateBounds)
initialize(
```

$\qquad$

``` ,Name, Value)
```


## Description

initialize(pf,numParticles,mean, covariance) initializes the particle filter object, pf, with a specified number of particles, numParticles. The initial states of the particles in the state space are determined by sampling from the multivariate normal distribution with the specified mean and covariance.
initialize(pf,numParticles,stateBounds) determines the initial location of the particles by sample from the multivariate uniform distribution within the specified stateBounds.
initialize (__ ,Name, Value) initializes the particles with additional options specified by one or more Name, Value pair arguments.

## Examples

## Particle Filter Prediction and Correction

Create a stateEstimatorPF object, and execute a prediction and correction step for state estimation. The particle filter gives a predicted state estimate based on the return value of StateTransitionFcn. It then corrects the state based on a given measurement and the return value of MeasurementLikelihoodFcn.

Create a particle filter with the default three states.

```
pf = stateEstimatorPF
pf =
    stateEstimatorPF with properties:
            NumStateVariables: 3
                    NumParticles: 1000
            StateTransitionFcn: @nav.algs.gaussianMotion
        MeasurementLikelihoodFcn: @nav.algs.fullStateMeasurement
        IsStateVariableCircular: [0 0 0]
            ResamplingPolicy: [1x1 resamplingPolicyPF]
            ResamplingMethod: 'multinomial'
        StateEstimationMethod: 'mean'
            StateOrientation: 'row'
                        Particles: [1000x3 double]
                    Weights: [1000x1 double]
                        State: 'Use the getStateEstimate function to see the value.'
```

Specify the mean state estimation method and systematic resampling method.

```
pf.StateEstimationMethod = 'mean';
pf.ResamplingMethod = 'systematic';
```

Initialize the particle filter at state [4 19] with unit covariance (eye (3)). Use 5000 particles.

```
initialize(pf,5000,[4 1 9],eye(3));
```

Assuming a measurement [4.2 0.9 9], run one predict and one correct step.

```
[statePredicted,stateCov] = predict(pf);
[stateCorrected,stateCov] = correct(pf,[4.2 0.9 9]);
```

Get the best state estimate based on the StateEstimationMethod algorithm.

```
stateEst = getStateEstimate(pf)
```

stateEst $=1 \times 3$
$4.1562 \quad 0.9185 \quad 9.0202$

## Input Arguments

pf - stateEstimatorPF object
handle
stateEstimatorPF object, specified as a handle. See stateEstimatorPF for more information.
numParticles - Number of particles used in the filter
scalar
Number of particles used in the filter, specified as a scalar.

## mean - Mean of particle distribution <br> vector

Mean of particle distribution, specified as a vector. The NumStateVariables property of pf is set based on the length of this vector.

## covariance - Covariance of particle distribution

$N$-by- $N$ matrix
Covariance of particle distribution, specified as an $N$-by- $N$ matrix, where $N$ is the value of NumStateVariables property from pf.

## stateBounds - Bounds of state variables

n-by-2 matrix
Bounds of state variables, specified as an $n$-by-2 matrix. The NumStateVariables property of pf is set based on the value of $n$. Each row corresponds to the lower and upper limit of the corresponding state variable.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . , NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: "CircularVariables", [0 0 1]

## CircularVariables - Circular variables

logical vector
Circular variables, specified as a logical vector. Each state variable that uses circular or angular coordinates is indicated with a 1 . The length of the vector is equal to the NumStateVariables property of pf .

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

stateEstimatorPF|resamplingPolicyPF|initialize| getStateEstimate|predict| correct

## Topics

"Track a Car-Like Robot Using Particle Filter" (Robotics System Toolbox)
"Particle Filter Parameters"
"Particle Filter Workflow"

## Introduced in R2016a

## predict

Predict state of robot in next time step

## Syntax

[statePred,stateCov] = predict(pf)
[statePred,stateCov] = predict(pf,varargin)

## Description

[statePred,stateCov] = predict(pf) calculates the predicted system state and its associated uncertainty covariance. predict uses the StateTransitionFcn property of stateEstimatorPF object, pf, to evolve the state of all particles. It then extracts the best state estimate and covariance based on the setting in the StateEstimationMethod property.
[statePred,stateCov] = predict(pf,varargin) passes all additional arguments specified in varargin to the underlying StateTransitionFen property of pf . The first input to
StateTransitionFcn is the set of particles from the previous time step, followed by all arguments in varargin.

## Examples

## Particle Filter Prediction and Correction

Create a stateEstimatorPF object, and execute a prediction and correction step for state estimation. The particle filter gives a predicted state estimate based on the return value of StateTransitionFcn. It then corrects the state based on a given measurement and the return value of MeasurementLikelihoodFcn.

Create a particle filter with the default three states.

```
pf = stateEstimatorPF
pf =
    stateEstimatorPF with properties:
            NumStateVariables: 3
                    NumParticles: 1000
            StateTransitionFcn: @nav.algs.gaussianMotion
        MeasurementLikelihoodFcn: @nav.algs.fullStateMeasurement
        IsStateVariableCircular: [0 0 0]
            ResamplingPolicy: [1x1 resamplingPolicyPF]
            ResamplingMethod: 'multinomial'
        StateEstimationMethod: 'mean'
            StateOrientation: 'row'
                Particles: [1000x3 double]
                        Weights: [1000x1 double]
                            State: 'Use the getStateEstimate function to see the value.'
            StateCovariance: 'Use the getStateEstimate function to see the value.'
```

Specify the mean state estimation method and systematic resampling method.

```
pf.StateEstimationMethod = 'mean';
pf.ResamplingMethod = 'systematic';
```

Initialize the particle filter at state [4 19] with unit covariance (eye (3)). Use 5000 particles.

```
initialize(pf,5000,[4 1 9],eye(3));
```

Assuming a measurement [4.2 0.9 9], run one predict and one correct step.

```
[statePredicted,stateCov] = predict(pf);
[stateCorrected,stateCov] = correct(pf,[4.2 0.9 9]);
```

Get the best state estimate based on the StateEstimationMethod algorithm.

```
stateEst = getStateEstimate(pf)
stateEst = 1\times3
    4.1562 0.9185 9.0202
```


## Input Arguments

pf - stateEstimatorPF object
handle
stateEstimatorPF object, specified as a handle. See stateEstimatorPF for more information.

## varargin - Variable-length input argument list

comma-separated list
Variable-length input argument list, specified as a comma-separated list. This input is passed directly into the StateTransitionFcn property of $p f$ to evolve the system state for each particle. When you call:
predict(pf,arg1,arg2)
MATLAB essentially calls the stateTranstionFcn as:
stateTransitionFcn(pf,prevParticles,arg1,arg2)

## Output Arguments

## statePred - Predicted system state

vector
Predicted system state, returned as a vector with length NumStateVariables. The predicted state is calculated based on the StateEstimationMethod algorithm.

## stateCov - Corrected system covariance

## $N$-by- $N$ matrix | [ ]

Corrected system variance, returned as an $N$-by- $N$ matrix, where $N$ is the value of NumStateVariables property from pf. The corrected state is calculated based on the

StateEstimationMethod algorithm and the MeasurementLikelihoodFcn. If you specify a state estimate method that does not support covariance, then the function returns stateCov as [].

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

stateEstimatorPF| resamplingPolicyPF | initialize| getStateEstimate|predict| correct

## Topics

"Track a Car-Like Robot Using Particle Filter" (Robotics System Toolbox)
"Particle Filter Parameters"
"Particle Filter Workflow"

Introduced in R2016a

## stateSpaceSE2

SE(2) state space

## Description

The stateSpaceSE2 object stores parameters and states in the $\operatorname{SE}(2)$ state space, which is composed of state vectors represented by $[x, y, \theta] . x$ and $y$ are Cartesian coordinates, and $\theta$ is the orientation angle. The object uses Euclidean distance to calculate distance and uses linear interpolation to calculate translation and rotation of the state.

## Creation

## Syntax

space $=$ stateSpaceSE2
space $=$ stateSpaceSE2(bounds)

## Description

space $=$ stateSpaceSE2 creates an $\operatorname{SE}(2)$ state space object with default state bounds for $x, y$, and $\theta$.
space $=$ stateSpaceSE2 (bounds) specifies the bounds for $x, y$, and $\theta$. The state values beyond the bounds are truncated to the bounds. The input, bounds, allows you to set the value of the StateBounds property.

## Properties

## Name - Name of state space

'SE2' (default)| string
Name of state space, specified as a string.

## NumStateVariables - Dimension of the state space

3 (default) | positive integer
This property is read-only.
Dimension of the state space, specified as a positive integer.

## StateBounds - Bounds of state variables

[-100 100; -100 100; -3.1416 3.1416] (default)| 3-by-2 real-valued matrix
Bounds of state variables, specified as a 3-by-2 real-valued matrix.

- The first row specifies the lower and upper bounds of the $x$ state in meters.
- The second row specifies the lower and upper bounds of the $y$ state in meters.
- The third row specifies the lower and upper bounds of the $\theta$ state in radians.

Data Types: double

## WeightXY - Weight applied to $x$ and $y$ distance calculation

1 (default) | nonnegative real scalar
Weight applied to x and y distance calculation, specified as a nonnegative real scalar.
In the object, the distance calculated as:

$$
d=\sqrt{\left(w_{x y}\left(d_{x}^{2}+d_{y}^{2}\right)\right)+w_{\theta} d_{\theta}^{2}}
$$

$w_{x y}$ is weight applied to $x$ and $y$ coordinates, and $w_{\theta}$ is the weight applied to the $\theta$ coordinate. $d_{x}, d_{y}$, and $d_{\theta}$ are the distances in the $x, y$, and $\theta$ direction, respectively.
Data Types: double

## WeightTheta - Weight applied to theta distance calculation

0.1 (default) | nonnegative real scalar

Weight applied to $\theta$ distance calculation, specified as a nonnegative real scalar.
In the object, the distance calculated as:

$$
d=\sqrt{\left(w_{x y}\left(d_{x}^{2}+d_{y}^{2}\right)\right)+w_{\theta} d_{\theta}^{2}}
$$

$w_{x y}$ is weight applied to $x$ and $y$ coordinates, and $w_{\theta}$ is the weight applied to the $\theta$ coordinate. $d_{x}, d_{y}$, and $d_{\theta}$ are the distances in the $x, y$, and $\theta$ direction, respectively.
Data Types: double

## Object Functions

copy
distance
enforceStateBounds
interpolate
sampleGaussian
sampleUniform

Create deep copy of state space object
Distance between two states
Reduce state to state bounds
Interpolate between states
Sample state using Gaussian distribution
Sample state using uniform distribution

## Examples

## Plan Path Between Two SE(2) States

Create an $\mathrm{SE}(2)$ state space.
ss = stateSpaceSE2;
Create an occupancyMap-based state validator using the created state space.
sv = validator0ccupancyMap(ss);
Create an occupancy map from an example map and set map resolution as 10 cells/meter.

```
load exampleMaps
map = occupancyMap(simpleMap,10);
sv.Map = map;
```

Set validation distance for the validator.

```
sv.ValidationDistance = 0.01;
```

Update state space bounds to be the same as map limits.

```
ss.StateBounds = [map.XWorldLimits;map.YWorldLimits; [-pi pi]];
```

Create the path planner and increase maximum connection distance.

```
planner = plannerRRT(ss,sv);
planner.MaxConnectionDistance = 0.3;
```

Set the start and goal states.

```
start = [0.5,0.5,0];
goal = [2.5,0.2,0];
```

Plan a path with default settings.

```
rng(100,'twister'); % for repeatable result
[pthObj,solnInfo] = planner.plan(start,goal);
```

Visualize the results.

```
map.show; hold on;
plot(solnInfo.TreeData(:,1),solnInfo.TreeData(:,2),'.-'); % tree expansion
plot(pthObj.States(:,1), pthObj.States(:,2),'r-','LineWidth',2) % draw path
```



## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

stateSpaceDubins| stateSpaceReedsShepp
Introduced in R2019b

## stateSpaceSE3

SE(3) state space

## Description

The stateSpaceSE3 object stores parameters and states in the $\operatorname{SE}(3)$ state space, which is composed of state vectors represented by $[x, y, z, q w, q x, q y, q z] . x, y$, and $z$ are Cartesian coordinates. $q w, q x, q y$, and $q z$ represent the orientation in a quaternion. The object uses Euclidean distance calculation and linear interpolation for the translation component of the state. The object uses quaternion distance calculation and spherical linear interpolation for the rotation component of the state.

## Creation

## Syntax

space = stateSpaceSE3
space = stateSpaceSE3(bounds)

## Description

space $=$ stateSpaceSE3 creates an SE(3) state space object with default state bounds for $x, y$, and $z$. The state variables $q w, q x, q y$, and $q z$ corresponding to orientation are not bounded.
space $=$ stateSpaceSE3(bounds) creates an SE(3) state space object with state bounds specified as a 7-by-2 matrix. Each row specifies the minimum and maximum value for a dimension of the state in the order $x, y, z, q w, q x, q y$, and $q z$. The input bounds sets the StateBounds property.

## Properties

## Name - Name of state space

'SE3 ' (default) | character vector
This property is read-only.
Name of state space, specified as a character vector.
Data Types: char

## NumStateVariables - Number of state space dimensions

7 (default) | positive integer
This property is read-only.
Number of state space dimensions, specified dimensions, returned as a positive integer.
Data Types: double

## StateBounds - Bounds of state variables

[-100 100; -100 100; -100 100; Inf Inf; Inf Inf; Inf Inf; Inf Inf] (default)|7-by-2 matrix of real values

Bounds of state variables, specified as a 7-by-2 matrix of real values.

- The first row specifies the lower and upper bounds of the $x$ state in meters.
- The second row specifies the lower and upper bounds of the $y$ state in meters.
- The third row specifies the lower and upper bounds of the $z$ state in meters.
- The fourth through the seventh rows specify the lower and upper bounds of the state variables $q w, q x, q y$, and $q z$ respectively, corresponding to orientation as a quaternion.

Note The StateBounds property only affect the Cartesian components of the state. The state variables corresponding to orientation are not bounded.

Example: stateSpaceSE3([-10 10; -10 10; -10 10; Inf Inf; Inf Inf; Inf Inf; Inf Inf])

Example: space.StateBounds $=$ [-10 10; -10 10; -10 10; Inf Inf; Inf Inf; Inf Inf; Inf Inf]

Data Types: double

## WeightXYZ - Weight applied to $x, y$, and $z$ distance calculation <br> 1 (default) | positive real scalar

Weight applied to the $x, y$, and $z$ distance calculation, specified as a positive real scalar. By default, the weight for translation is chosen to be greater than the weight for rotation.

The object calculates distance as:

$$
d=\sqrt{w_{x y z}\left(d_{x}^{2}+d_{y}^{2}+d_{z}^{2}\right)+w_{q} d_{q}^{2}}
$$

where $w_{x y z}$ is the weight applied to $x, y$, and $z$ coordinates, and $w_{q}$ is the weight applied to the orientation in quaternion. $d_{x}, d_{y}$, and $d_{z}$ are the distances in the $x, y$, and $z$ directions, respectively. $d_{q}$ is the quaternion distance.

Example: space.WeightXYZ = 2
Data Types: double

## WeightQuaternion - Weight applied to quaternion distance calculation

0.1 (default) | positive real scalar

Weight applied to quaternion distance calculation, specified as a positive real scalar. By default, the weight for rotation is chosen to be less than the weight for translation.

The object calculates distance as:

$$
d=\sqrt{w_{x y z}\left(d_{x}^{2}+d_{y}^{2}+d_{z}^{2}\right)+w_{q} d_{q}^{2}}
$$

where $w_{x y z}$ is weight applied to $x, y$, and $z$ coordinates, and $w_{q}$ is the weight applied to the orientation in quaternion. $d_{x}, d_{y}$, and $d_{z}$ are the distances in the $x, y$, and $z$ direction, respectively. $d_{q}$ is the quaternion distance.

Example: space. WeightQuaternion $=0.5$
Data Types: double

## Object Functions

| copy | Create deep copy of state space object |
| :--- | :--- |
| distance | Distance between two states |
| enforceStateBounds | Reduce state to state bounds |
| interpolate | Interpolate between states |
| sampleUniform | Sample state using uniform distribution |

## Examples

## Validate Path Through 3-D Occupancy Map Environment

Create a 3-D occupancy map and associated state validator. Plan, validate, and visualize a path through the occupancy map.

## Load and Assign Map to State Validator

Load a 3-D occupancy map of a city block into the workspace. Specify a threshold for which cells to consider as obstacle-free.

```
mapData = load('dMapCityBlock.mat');
omap = mapData.omap;
omap.FreeThreshold = 0.5;
```

Inflate the occupancy map to add a buffer zone for safe operation around the obstacles.

```
inflate(omap,1)
```

Create an $\operatorname{SE}(3)$ state space object with bounds for state variables.
ss = stateSpaceSE3([-20 220;
-20 220;
-10 100;
inf inf;
inf inf;
inf inf;
inf inf]);
Create a 3-D occupancy map state validator using the created state space.
sv = validatorOccupancyMap3D(ss);
Assign the occupancy map to the state validator object. Specify the sampling distance interval.

```
sv.Map = omap;
sv.ValidationDistance = 0.1;
```


## Plan and Visualize Path

Create a path planner with increased maximum connection distance. Reduce the maximum number of iterations.

```
planner = plannerRRT(ss,sv);
planner.MaxConnectionDistance = 50;
planner.MaxIterations = 1000;
```

Create a user-defined evaluation function for determining whether the path reaches the goal. Specify the probability of choosing the goal state during sampling.

```
planner.GoalReachedFcn = @(~,x,y)(norm(x(1:3)-y(1:3))<5);
planner.GoalBias = 0.1;
```

Set the start and goal states.

```
start = [40 180 25 0.7 0.2 0 0.1];
goal = [150 33 35 0.3 0 0.1 0.6];
```

Plan a path using the specified start, goal, and planner.
[pthObj, solnInfo] = plan(planner,start, goal);
Check that the points of the path are valid states.

```
isValid = isStateValid(sv,pthObj.States)
isValid = 7x1 logical array
    1
    1
    1
    1
    1
    1
    1
```

Check that the motion between each sequential path state is valid.

```
isPathValid = zeros(size(pth0bj.States,1)-1,1,'logical');
for i = 1:size(pthObj.States,1)-1
    [isPathValid(i),~] = isMotionValid(sv,pthObj.States(i,:),...
            pthObj.States(i+1,:));
end
isPathValid
isPathValid = 6x1 logical array
    1
    1
    1
    1
    1
    1
```

Visualize the results.

```
show(omap)
hold on
scatter3(start(1,1),start(1,2),start(1,3),'g','filled') % draw start state
scatter3(goal(1,1),goal(1,2),goal(1,3),'r','filled') % draw goal state
plot3(pth0bj.States(:,1),pth0bj.States(:,2),pth0bj.States(:,3),...
    'r-','LineWidth',2) % draw path
```

Occupancy Map


## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

stateSpaceSE2 | validator0ccupancyMap3D
Introduced in R2020b

## stateSpaceDubins

State space for Dubins vehicles

## Description

The stateSpaceDubins object stores parameters and states in the Dubins state space, which is composed of state vectors represented by $[x, y, \theta] . x$ and $y$ are Cartesian coordinates, and $\theta$ is the orientation angle. The Dubins state space has a lower limit on the turning radius (specified by the MinTurningRadius property in the object) for navigating between states and uses the shortest feasible curve to connect states.

## Creation

## Syntax

space = stateSpaceDubins
space $=$ stateSpaceDubins(bounds)

## Description

space $=$ stateSpaceDubins creates a Dubins state space object with default state bounds for $x, y$, and $\theta$.
space $=$ stateSpaceDubins(bounds) specifies the bounds for $x, y$, and $\theta$. The state values beyond the bounds are truncated to the bounds. The input, bounds, allows you to set the value of the StateBounds property.

## Properties

## Name - Name of state space

'SE2 Dubins' (default) | string
Name of state space, specified as a string.

## NumStateVariables - Dimension of the state space

3 (default) | positive integer
This property is read-only.
Dimension of the state space, specified as a positive integer.

## StateBounds - Bounds of state variables

[-100 100; -100 100; -3.1416 3.1416] (default)| 3-by-2 real-valued matrix
Bounds of state variables, specified as a 3-by-2 real-valued matrix.

- The first row specifies the lower and upper bounds for the $x$ state in meters.
- The second row specifies the lower and upper bounds for the y state in meters.
- The third row specifies the lower and upper bounds for the $\theta$ state in radians.

Data Types: double

## MinTurningRadius - Minimum turning radius

1 (default) | positive scalar
Minimum turning radius in meters, specified as a positive scalar. The minimum turning radius is for the smallest circle the vehicle can make with maximum steer in a single direction.

## Object Functions

| copy | Create deep copy of state space object |
| :--- | :--- |
| distance | Distance between two states |
| enforceStateBounds | Reduce state to state bounds |
| interpolate | Interpolate between states |
| sampleGaussian | Sample state using Gaussian distribution |
| sampleUniform | Sample state using uniform distribution |

## Examples

## Plan Path Between Two States in Dubins State Space

Create a Dubins state space and set the minimum turing radius to 0.2.

```
ss = stateSpaceDubins;
ss.MinTurningRadius = 0.2;
```

Create an occupancyMap-based state validator using the created state space.
sv = validatorOccupancyMap(ss);
Create an occupancy map from an example map and set map resolution as 10 cells/meter.

```
load exampleMaps
map = occupancyMap(simpleMap,10);
```

sv.Map = map;

Set validation distance for the validator.

```
sv.ValidationDistance = 0.01;
```

Update state space bounds to be the same as map limits.

```
ss.StateBounds = [map.XWorldLimits;map.YWorldLimits; [-pi pi]];
```

Create the path planner and increase max connection distance.

```
planner = plannerRRT(ss,sv);
planner.MaxConnectionDistance = 0.3;
```

Set the start and goal states.

```
start = [0.5,0.5,0];
goal = [2.5,0.2,0];
```

Plan a path with default settings.
rng(100,'twister'); \% repeatable result
[pthObj,solnInfo] = planner.plan(start,goal);
Visualize the results.
show(map);
hold on;
plot(solnInfo.TreeData(:,1), solnInfo.TreeData(:,2),'.-'); \% tree expansion plot(pthObj.States(:,1), pthObj.States(:,2),'r-','LineWidth',2) \% draw path


## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

stateSpaceSE2 | stateSpaceReedsShepp | dubinsConnection
Introduced in R2019b

## stateSpaceReedsShepp

State space for Reeds-Shepp vehicles

## Description

The stateSpaceReedsShepp object stores parameters and states in the Reeds-Shepp state space, which is composed of state vectors represented by $[x, y, \theta]$. $x$ and $y$ are Cartesian coordinates, and $\theta$ is the orientation angle. The Reeds-Shepp state space has a lower limit on the turning radius (specified by the MinTurningRadius property in the object) and forward and reverse costs (specified by the ForwardCost and ReverseCost properties in the object) for navigating between states.

## Creation

## Syntax

space = stateSpaceReedsShepp
sapce = stateSpaceReedsShepp(bounds)

## Description

space = stateSpaceReedsShepp creates a Reeds-Shepp state space object with default state bounds for $x, y$, and $\theta$.
sapce $=$ stateSpaceReedsShepp(bounds) specifies the bounds for $x, y$, and $\theta$. The state values beyond the bounds are truncated to the bounds. The input, bounds, sets the value of the StateBounds property.

## Properties

## Name - Name of state space

'SE2 Dubins' (default) | string
Name of state space, specified as a string.

## NumStateVariables - Dimension of the state space

3 (default) | positive integer
This property is read-only.
Dimension of the state space, specified as a positive integer.

## StateBounds - Bounds of state variables

[-100 100; -100 100; -3.1416 3.1416] (default) | 3-by-2 real-valued matrix
Bounds of state variables, specified as a 3-by-2 real-valued matrix.

- The first row specifies the lower and upper bounds for the $x$ state in meters.
- The second row specifies the lower and upper bounds for the $y$ state in meters.
- The third row specifies the lower and upper bounds for the $\theta$ state in radians.

Data Types: double

## MinTurningRadius - Minimum turning radius

1 (default) | positive scalar
Minimum turning radius in meters, specified as a positive scalar. The minimum turning radius is for the smallest circle the vehicle can make with maximum steer in a single direction.

## ForwardCost - Cost multiplier for forward motion

1 (default) | positive scalar
Cost multiplier for forward motion, specified as a positive scalar. Increase the cost to penalize forward motion.

## ReverseCost - Cost multiplier for reverse motion

1 (default) | positive scalar
Cost multiplier for reverse motion, specified as a positive scalar. Increase the cost to penalize reverse motion.

## Object Functions

| copy | Create deep copy of state space object |
| :--- | :--- |
| distance | Distance between two states |
| enforceStateBounds | Reduce state to state bounds |
| interpolate | Interpolate between states |
| sampleGaussian | Sample state using Gaussian distribution |
| sampleUniform | Sample state using uniform distribution |

## Examples

## Plan Path Between Two States in ReedsShepp State Space

Create a ReedsShepp state space.
ss = stateSpaceReedsShepp;
Create an occupanyMap-based state validator using the created state space.
sv = validatorOccupancyMap(ss);
Create an occupany map from an example map and set map resolution as 10 cells/meter.

```
load exampleMaps
map = occupancyMap(simpleMap,10);
sv.Map = map;
```

Set validation distance for the validator.

```
sv.ValidationDistance = 0.01;
```

Update state space bounds to be the same as map limits.

```
ss.StateBounds = [map.XWorldLimits;map.YWorldLimits; [-pi pi]];
```

Create the path planner and increase max connection distance.
planner = plannerRRT(ss,sv);
planner.MaxConnectionDistance = 0.3;
Set the start and goal states.

```
start = [0.5,0.5,0];
goal = [2.5,0.2,0];
```

Plan a path with default settings.

```
rng(100,'twister'); % repeatable result
[pthObj,solnInfo] = planner.plan(start,goal);
```

Visualize the results.
show(map);
hold on;
plot(solnInfo.TreeData(:,1), solnInfo.TreeData(:,2),'.-'); \% tree expansion plot(pthObj.States(:,1), pthObj.States(:,2),'r-','LineWidth',2) \% draw path


## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

stateSpaceDubins| stateSpaceSE2|reedsSheppConnection
Introduced in R2019b

## distance

Distance between two states

## Syntax

dist $=$ distance(space,states1,states2)

## Description

dist $=$ distance(space, states1,states2) returns the distance between states1 and states2 in the specified state space space.

## Examples

## Calculate Distance Between Two States in SE3

Create an SE(3) state space.

```
space = stateSpaceSE3
space =
    stateSpaceSE3 with properties:
                            Name: 'SE3'
            StateBounds: [7x2 double]
        NumStateVariables: 7
            WeightXYZ: 1
        WeightQuaternion: 0.1000
```

Calculate distance between two states.

```
dist = distance(space,[2 10 3 0.2 0 0 0.8],[0 -2.5 4 0.7 0.3 0 0])
dist = 12.7269
```

Calculate Euclidean distance between two states.
space.WeightQuaternion = 0;
distEuc = distance(space,[2 10 3 0.2 0 0 0.8; 4 5 2 1 2 4 2],[62 5 33 0.2 0 0 0.8; 9 9 312.1
distEuc = 2×1
67.2681
6.4807

## Input Arguments

## space - State space object

stateSpaceSE2 object | stateSpaceSE3 object | stateSpaceDubins object |
stateSpaceReedsShepp object
State space object, specified as a stateSpaceSE2, stateSpaceSE3, stateSpaceDubins, or stateSpaceReedsShepp object.

## states1 - Initial states for distance calculation

$n$-by- 3 matrix of real values | $n$-by-7 matrix of real values
Initial states for distance calculation, specified as an $n$-by- 3 or $n$-by- 7 matrix of real values. $n$ is the number of specified states.

For the 2-D state space objects stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp, each row is of form [x y theta], which defines the $x y$-position and orientation angle theta of a state in the state space.

For the 3-D state space object stateSpaceSE3, each row is of form [x y z qw qx qy qz], which defines the $x y z$-position and quaternion orientation [qw qx qy qz] of a state in the state space.

The function supports following combinations for distance calculation:

- $n$-to- $n-n$ number of states in states 1 and $n$ number of states in states 2 .

For example, distance(space, rand $(10,7)$, rand $(10,7)$ )

- 1-to-n -1 state in states 1 and $n$ number of states in states 2.

For example, distance (space, rand $(1,7)$, rand $(10,7))$

- $n$-to- $1-n$ number of states in states 1 and 1 state in states 2 .

For example, distance (space, rand $(10,7)$, rand $(1,7)$ )

## Data Types: single | double

## states2 - Final states for distance calculation

$n$-by- 3 matrix of real values | $n$-by-7 matrix of real values
Final states for distance calculation, specified as an $n$-by- 3 or $n$-by- 7 matrix of real values. $n$ is the number of specified states.

For the 2-D state space objects stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp, each row is of form [x y theta], which defines the $x y$-position and orientation angle theta of a state in the state space.

For the 3-D state space object stateSpaceSE3, each row is of form [x y z qw qx qy qz], which defines the xyz-position and quaternion orientation [qw qx qy qz] of a state in the state space.

The function supports following combinations for distance calculation:

- $n$-to- $n-n$ number of states in states 1 and $n$ number of states in states2.

For example, distance(space, rand $(10,7)$, rand $(10,7))$

- 1-to-n -1 state in states 1 and $n$ number of states in states2.

For example, distance (space, rand $(1,7)$, rand $(10,7)$ )

- $n$-to- $1-n$ number of states in states 1 and 1 state in states 2 .

For example, distance(space, rand $(10,7), r a n d(1,7))$
Data Types: single | double

## Output Arguments

## dist - Distance between states

$n$-element column vector
Distance between states, returned as an $n$-element column vector. $n$ is the number of specified states.
The function supports following combinations for distance calculation:

- $n$-to- $n-n$ number of states in states 1 and $n$ number of states in states2.
- 1-to-n -1 state in states 1 and $n$ number of states in states 2 .
- $n$-to- $1-n$ number of states in states 1 and 1 state in states 2 .

Data Types: single | double

## See Also

stateSpaceSE2 | stateSpaceSE3| stateSpaceDubins | stateSpaceReedsShepp

## Introduced in R2019b

## interpolate

Interpolate between states

## Syntax

interpStates = interpolate(space,state1,state2,ratio)

## Description

interpStates $=$ interpolate(space, state1,state2, ratio) interpolates states between the specified start state statel and end state state2 based on the specified interpolation ratio ratio.

## Examples

## Interpolate Between States in SE(2)

Create an $\mathrm{SE}(2)$ state space with default properties.

```
space = stateSpaceSE2
space =
    stateSpaceSE2 with properties:
                            Name: 'SE2'
        StateBounds: [3\times2 double]
        NumStateVariables: 3
            WeightXY: 1
                WeightTheta: 0.1000
```

Create a pair of states in 2-D space.

```
state1 = [2 10 -pi];
```

state2 $=\left[\begin{array}{lll}0 & -2.5 & -\mathrm{pi} / 4\end{array}\right]$;

Interpolate halfway between two states.

```
state = interpolate(space,state1,state2,0.5)
state = 1×3
    1.0000 3.7500 -1.9635
```

Interpolate multiple points with a fixed interval.

```
states = interpolate(space,state1,state2,0:0.02:1)
states = 51\times3
    2.0000 10.0000 -3.1416
    1.9600 9.7500 -3.0945
```

| 1.9200 | 9.5000 | -3.0473 |
| :--- | :--- | :--- |
| 1.8800 | 9.2500 | -3.0002 |
| 1.8400 | 9.0000 | -2.9531 |
| 1.8000 | 8.7500 | -2.9060 |
| 1.7600 | 8.5000 | -2.8588 |
| 1.7200 | 8.2500 | -2.8117 |
| 1.6800 | 8.0000 | -2.7646 |
| 1.6400 | 7.7500 | -2.7175 |

## Interpolate Between States in SE(3)

Create an SE(3) state space with default properties.

```
space = stateSpaceSE3
space =
    stateSpaceSE3 with properties:
                            Name: 'SE3'
            StateBounds: [7×2 double]
        NumStateVariables: 7
            WeightXYZ: 1
        WeightQuaternion: 0.1
```

Create a pair of states in 3-D space.

```
statel = [2 10 3 0.2 0 0 0.8];
state2 = [0 -2.5 4 0.7 0.3 0 0];
```

Interpolate halfway between two states.

```
state = interpolate(space,state1,state2,0.5)
state = 1\times7
```

1
3.75
3.5
0.7428
0.25188
0
0.62033

Interpolate multiple points with a fixed interval.

```
states = interpolate(space,state1,state2,0:0.02:1)
states = 51\times7
```

| 2 |  | 10 | 3 | 0.24254 | 0 | 0 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1.96 | 9.75 | 3.02 | 0.26633 | 0.010877 | 0.97014 |  |
| 1.92 | 9.5 | 3.04 | 0.28994 | 0.021745 | 0.96382 |  |
| 1.88 | 9.25 | 3.06 | 0.31333 | 0.032598 | 0 | 0.9568 |
| 1.84 | 9 | 3.08 | 0.3365 | 0.043428 | 0.94908 |  |
| 1.8 | 8.75 | 3.1 | 0.35943 | 0.054225 | 0 | 0.94068 |
| 1.76 | 8.5 | 3.12 | 0.38209 | 0.064984 | 0 | 0.9316 |
| 1.72 | 8.25 | 3.14 | 0.40448 | 0.075695 | 0 | 0.92184 |
| 1.68 | 8 | 3.16 | 0.42657 | 0.086352 | 0 | 0.91141 |
|  |  |  |  | 0 | 0.90032 |  |

1.64
7.75
3.18
0.44835
0.096946
0
0.88858

## Input Arguments

space - State space object
stateSpaceSE2 object | stateSpaceSE3 object | stateSpaceDubins object |
stateSpaceReedsShepp object
State space object, specified as a stateSpaceSE2, stateSpaceSE3, stateSpaceDubins, or stateSpaceReedsShepp object.
statel - Start state for interpolation
three-element vector of real values | seven-element vector of real values
Start state for interpolation, specified as a three-element or seven-element vector of real values.
For the 2-D state space objects stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp, the state is a vector of form [x y theta], which defines the $x y$-position and orientation angle theta of a state in the state space.

For the 3-D state space object stateSpaceSE3, the state is a vector of form [x y z qw qx qy $q z$ ], which defines the $x y z$-position and quaternion orientation [qw $q x$ qy $q z$ ] of a state in the state space.
Data Types: single | double

## state2 - End state for interpolation

three-element vector of real values | seven-element vector of real values
End state for interpolation, specified as a three-element or seven-element vector of real values.
For the 2-D state space objects stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp, the state is a vector of form [x y theta], which defines the $x y$-position and orientation angle theta of a state in the state space.

For the 3-D state space object stateSpaceSE3, the state is a vector of form $[x$ y z qw qx qy qz ], which defines the $x y z$-position and quaternion orientation [qw $q x$ qy $q z$ ] of a state in the state space.
Data Types: single | double

## ratio - Interpolation ratio

scalar in range $[0,1] \mid n$-element column vector of values in the range [0, 1]
Interpolation ratio, specified as a scalar in the range of [ 0,1 ], or an $n$-element column vector of values in the range $[0,1] . n$ is the number of desired interpolation points.

Data Types: single | double

## Output Arguments

## interpStates - Interpolated states <br> $n$-by-3 matrix of real values | $n$-by-7 matrix of real values

Interpolated states, returned as an $n$-by- 3 or $n$-by- 7 matrix of real values. $n$ is the number of interpolation points specified by the ratio input argument.

For the 2-D state space objects stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp, each row is of form [x y theta], which defines the $x y$-position and orientation angle theta of the interpolated states.

For the 3-D state space object stateSpaceSE3, each row is of form [x y z qw qx qy qz], which defines the $x y z$-position and quaternion orientation [qw qx qy qz] of the interpolated states.
Data Types: single | double

## See Also

stateSpaceSE2|stateSpaceSE3|stateSpaceDubins|stateSpaceReedsShepp

## Introduced in R2019b

## enforceStateBounds

Reduce state to state bounds

## Syntax

boundedStates = enforceStateBounds(space,states)

## Description

boundedStates $=$ enforceStateBounds(space,states) reduces the specified states states to the state bounds in the StateBounds property of the specified state space object space.

## Examples

## Enforce State Bounds for SE(3) States

Create an $\mathrm{SE}(3)$ state space object.

```
space = stateSpaceSE3([-1 1; ...
    -2 2; ...
    -10 10; ..
    -inf inf; ...
    -inf inf; ...
    -inf inf; ...
    -inf inf])
space =
    stateSpaceSE3 with properties:
                                    Name: 'SE3'
                StateBounds: [7x2 double]
        NumStateVariables: 7
                WeightXYZ: 1
            WeightQuaternion: 0.1000
```

Create a pair of states in 3-D space.

```
statel = [2 10 3 2 0 0 0.8];
```

state2 = [223 100 32212 5];

Enforce state bounds for a single state.

```
boundedState = enforceStateBounds(space,state1)
boundedState = 1×7
    1.0000 2.0000 3.0000 2.0000 0 0 0 0.8000
```

Enforce state bounds for multiple states.

```
boundedStates = enforceStateBounds(space,[state1; state2])
boundedStates = 2×7
\begin{tabular}{rrrrrrr}
1.0000 & 2.0000 & 3.0000 & 2.0000 & 0 & 0 & 0.8000 \\
1.0000 & 2.0000 & 3.0000 & 2.0000 & 2.0000 & 12.0000 & 5.0000
\end{tabular}
```


## Input Arguments

space - State space object
stateSpaceSE2 object|stateSpaceSE3 object | stateSpaceDubins object | stateSpaceReedsShepp object

State space object, specified as a stateSpaceSE2, stateSpaceSE3, stateSpaceDubins, or stateSpaceReedsShepp object.
states - Unbounded states
$n$-by-3 matrix of real values | $n$-by-7 matrix of real values
Unbounded states, specified as an $n$-by- 3 or $n$-by- 7 matrix of real values.
For the 2-D state space objects stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp, each row is of form [x y theta], which defines the $x y$-position and orientation angle theta of a state in the state space.

For the 3-D state space object stateSpaceSE3, each row is of form [x y z qw qx qy qz], which defines the xyz-position and quaternion orientation [qw qx qy qz] of a state in the state space.

Data Types: single | double

## Output Arguments

## boundedStates - Bounded states

$n$-by- 3 matrix of real values | $n$-by-7 matrix of real values
Bounded states, returned as an $n$-by- 3 or $n$-by- 7 matrix of real values. The value of $n$ is same as for states input argument.

The function truncates each of the specified unbounded states to the bounds specified in the StateBounds property of the state space object space.

For the 2-D state space objects stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp, each row is of form [x y theta], which defines the $x y$-position and orientation angle theta of the bounded states.

For the 3-D state space object stateSpaceSE3, each row is of form [x y z qw qx qy qz], which defines the xyz-position and quaternion orientation [qw qx qy qz] of the bounded states.
Data Types: single | double

## See Also

stateSpaceSE2 | stateSpaceSE3| stateSpaceDubins | stateSpaceReedsShepp

Introduced in R2019b

## copy

Create deep copy of state space object

## Syntax

```
space2 = copy(space1)
```


## Description

space2 $=$ copy(space1) creates a deep copy of the specified state space object.

## Examples

## Create Deep Copy of SE(3) State Space Object

Create a default SE(3) state space object.

```
space = stateSpaceSE3;
```

Specify weight for the quaternion distance in state space calculation.

```
space.WeightQuaternion = 2/3
space =
    stateSpaceSE3 with properties:
                            Name: 'SE3'
            StateBounds: [7\times2 double]
        NumStateVariables: 7
            WeightXYZ: 1
        WeightQuaternion: 0.6667
```

Create a deep copy of the state space object.
space2 $=$ copy(space)
space2 =
stateSpaceSE3 with properties:
Name: 'SE3'
StateBounds: [7x2 double]
NumStateVariables: 7
WeightXYZ: 1
WeightQuaternion: 0.6667

Verify that the WeightQuaternion property values of the two state space objects are equal.
isequal(space.WeightQuaternion, space2.WeightQuaternion)

```
ans = logical
```

    1
    
## Input Arguments

```
space1 - State space object
stateSpaceSE2 object| stateSpaceSE3 object| stateSpaceDubins object|
stateSpaceReedsShepp object
```

State space object, specified as a stateSpaceSE2, stateSpaceSE3, stateSpaceDubins, or stateSpaceReedsShepp object.

## Output Arguments

space2 - State space object
stateSpaceSE2 object | stateSpaceSE3 object | stateSpaceDubins object |
stateSpaceReedsShepp object
State space object, returned as a stateSpaceSE2, stateSpaceSE3, stateSpaceDubins, or stateSpaceReedsShepp object.

## See Also

stateSpaceSE2 | stateSpaceSE3| stateSpaceDubins | stateSpaceReedsShepp

## Introduced in R2019b

## sampleGaussian

Sample state using Gaussian distribution

## Syntax

state $=$ sampleGaussian(space,meanState,stdDev)
state $=$ sampleGaussian(space,meanState,stdDev, numSamples)

## Description

state $=$ sampleGaussian(space, meanState, stdDev) returns a sample state of the state space based on a Gaussian (normal) distribution with specified mean, meanState, and standard deviation, stdDev.
state $=$ sampleGaussian(space,meanState,stdDev, numSamples) returns a number of state samples. The number is equal to numSamples.

## Input Arguments

## space - State space object

spaceSE2 object | spaceDubins object | spaceReedsShepp object
State space object, specified as a stateSpaceSE2, a stateSpaceDubins, or a stateSpaceReedsShepp object.
Data Types: object
meanState - Mean state
3 -element vector of real values
Mean state of the Gaussian distribution for sampling, specified as a 3-element vector of real values.
Example: [5 5 pi/3]
Data Types: single | double

## stdDev - Standard deviation

3 -element vector of nonnegative values
Standard deviation of the Gaussian distribution for sampling, specified as a 3-element vector of nonnegative values.
Example: [0.1 0.1 pi/18]
Data Types: single | double

## numSamples - Number of samples

positive integer
Number of samples, specified as a positive integer.
Data Types: single | double

## Output Arguments

## state - State samples

$N$-by-3 real-valued matrix
State samples, returned as an $N$-by-3 real-valued matrix. $N$ is the number of samples. Each row of the matrix corresponds to one incidence of state in the state space.
Data Types: single | double

## See Also

stateSpaceSE2 | stateSpaceDubins | stateSpaceReedsShepp

Introduced in R2019b

## sampleUniform

Sample state using uniform distribution

## Syntax

```
state = sampleUniform(space)
state = sampleUniform(space,numSamples)
state = sampleUniform(space,nearState,distVector,numSamples)
```


## Description

state = sampleUniform(space) samples a state within the bounds in the StateBounds property of the specified state space object space using a uniform probability distribution. For a stateSpaceSE3 object, the state variables corresponding to orientation are bound to a unit quaternion using a uniform distribution of random rotations.
state $=$ sampleUniform(space, numSamples) returns a specified number of state samples numSamples within the bounds of the state space object.
state = sampleUniform(space, nearState,distVector, numSamples) samples states in a specified subregion of the bounds of the state space object. Specify the center of the sampling region nearState and the distance from the center of the sampling region to its boundaries distVector.

Note The stateSpaceSE3 object does not support this syntax.

## Examples

## Sample State Using Uniform Distribution in SE(3)

Create an $\mathrm{SE}(3)$ state space.

```
space = stateSpaceSE3([-10 10; -10 10; -10 10; inf inf; inf inf; inf inf; inf inf])
space =
    stateSpaceSE3 with properties:
                            Name: 'SE3'
            StateBounds: [7x2 double]
        NumStateVariables: 7
            WeightXYZ: 1
        WeightQuaternion: 0.1000
```

Sample 3 states within full state bounds.

```
state = sampleUniform(space,3)
state = 3\times7
```

| 6.2945 | 8.1158 | -7.4603 | 0.6316 | 0.3078 | -0.6921 | -0.1654 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 8.2675 | 2.6472 | -8.0492 | -0.0834 | -0.9448 | 0.2709 | 0.1641 |
| -4.4300 | 0.9376 | 9.1501 | 0.5771 | -0.5458 | -0.5490 | -0.2601 |

## Input Arguments

space - State space object
stateSpaceSE2 object|stateSpaceSE3 object | stateSpaceDubins object | stateSpaceReedsShepp object

State space object, specified as a stateSpaceSE2, stateSpaceSE3, stateSpaceDubins, or stateSpaceReedsShepp object.
numSamples - Number of samples
positive integer
Number of samples, specified as a positive integer.
Data Types: single | double
nearState - Center of sampling region
three-element vector of real values
Center of the sampling region, specified as a three-element vector of real values.
For the 2-D state space objects stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp, the state is a vector of form [x y theta], which defines the $x y$-position and orientation angle theta of a state in the state space.

Note The stateSpaceSE3 object does not support this argument.

Data Types: single | double

## distVector - Distance of sampling region boundary from center

three-element vector of positive numbers
Distance of sampling region boundary from the center, specified as a three-element vector of positive numbers.

For the 2-D state space objects stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp, the state is a vector of form [x y theta], which defines the xy-position and orientation angle theta of a state in the state space.

Note The stateSpaceSE3 object does not support this argument.

Data Types: single | double

## Output Arguments

## state - State samples

n-by-3 matrix of real values | $n$-by- 7 matrix of real values
State samples, returned as an $n$-by- 3 or $n$-by- 7 matrix of real values. $n$ is the number of samples.
For the 2-D state space objects stateSpaceSE2, stateSpaceDubins, and stateSpaceReedsShepp, each row is of form [x y theta], which defines the $x y$-position and orientation angle theta of the sampled states.

For the 3-D state space object stateSpaceSE3, each row is of form [x y z qw qx qy qz], which defines the xyz-position and quaternion orientation [qw qx qy qz] of the sampled states.
Data Types: single | double

## See Also

stateSpaceSE2 | stateSpaceSE3|stateSpaceDubins | stateSpaceReedsShepp

## Introduced in R2019b

## trajectoryGeneratorFrenet

Find optimal trajectory along reference path

## Description

The trajectoryGeneratorFrenet object generates alternate trajectories using fourth or fifthorder polynomials relative to a given reference path. Each trajectory defines a motion between Frenet states over a specified time span.

Frenet states describe their position, velocity and acceleration relative to a static reference path, specified as a referencePathFrenet object.

The object expresses Frenet states as a vector of form [S dS ddS L dL ddL], where $S$ is the arc length and $L$ is the perpendicular deviation from the direction of the reference path. Derivatives of $S$ are relative to time. Derivatives of $L$ are relative to the arc length, $S$.


To generate alternative trajectories, specify the initial and terminal frenet states with a given time span to the connect object function.

## Creation

## Syntax

```
connectorFrenet = trajectoryGeneratorFrenet(refPath)
connectorFrenet = trajectoryGeneratorFrenet(
refPath,'TimeResolution',timeValue)
```


## Description

connectorFrenet $=$ trajectoryGeneratorFrenet (refPath) generates trajectories between initial and terminal states relative to a reference path refPath specified as a referencePathFrenet object. The refPath input argument sets the ReferencePath property.
connectorFrenet = trajectoryGeneratorFrenet(
refPath, 'TimeResolution', timeValue) specifies the time interval for discretization. The timeValue argument sets the TimeResolution property.

## Properties

## TimeResolution - Discretization time interval between sampled Frenet states

## 0.1 (default) | positive scalar in seconds

Discretization time interval between sampled Frenet states, specified as a positive scalar in seconds. When using the connect object function, this property determines the resolution of the Times field of the generated trajectory structures, frenetTrajectory and globalTrajectory.
Data Types: double
ReferencePath - Reference path in Frenet coordinates
referencePathFrenet
Reference path in Frenet coordinates, specified as a referencePathFrenet object.

## Object Functions

connect Connect initial and terminal Frenet states
createParallelState Create states using Frenet and global parameters

## Examples

## Generate Alternative Trajectories for Reference Path

Generate alternative trajectories for a reference path using Frenet coordinates. Specify different initial and terminal states for your trajectories. Tune your states based on the generated trajectories.

Generate a reference path from a set of waypoints. Create a trajectoryGeneratorFrenet object from the reference path.

```
waypoints = [0 0; ...
    50 20; ...
    100 0; ...
    150 10];
refPath = referencePathFrenet(waypoints);
connector = trajectoryGeneratorFrenet(refPath);
```

Generate a five-second trajectory between the path origin and a point 30 m down the path as Frenet states.

```
initState = [0 0 0 0 0 0]; % [S ds ddS L dL ddL]
termState = [30 0 0 0 0 0]; % [S ds ddS L dL ddL]
[~,trajGlobal] = connect(connector,initState,termState,5);
```

Display the trajectory in global coordinates.

```
show(refPath);
hold on
axis equal
```

plot(trajGlobal.Trajectory(:,1),trajGlobal.Trajectory(:,2), 'b')
legend(["Waypoints","Reference Path","Trajectory to 30m"])


Create a matrix of terminal states with lateral deviations between -3 m and 3 m . Generate trajectories that cover the same arc length in 10 seconds, but deviate laterally from the reference path. Display the new alternative paths.

```
termStateDeviated = termState + ([-3:3]' * [0 0 0 1 0 0]);
[~,trajGlobal] = connect(connector,initState,termStateDeviated,10);
clf
show(refPath);
hold on
axis equal
for i = 1:length(trajGlobal)
    plot(trajGlobal(i).Trajectory(:,1),trajGlobal(i).Trajectory(:,2),'g')
end
legend(["Waypoints","Reference Path","Alternative Trajectories"])
hold off
```



Specify a new terminal state to generate a new trajectory. This trajectory is not desirable because it requires reverse motion to achieve a lateral velocity of $10 \mathrm{~m} / \mathrm{s}$.
newTermState = [5 10 050 0];
[~,newTrajGlobal] = connect(connector,initState,newTermState,3);
clf
show(refPath);
hold on
axis equal
plot(newTrajGlobal.Trajectory(:,1),newTrajGlobal.Trajectory(:,2),'b'); legend(["Waypoint","Reference Path","New Trajectory"]) hold off


Relax the restriction on the longitudinal state by specifying an arc length of NaN. Generate and display the trajectory again. The new position shows a good alternative trajectory that deviates off the reference path.

```
relaxedTermState = [NaN 10 0 5 0 0];
[~,trajGlobalRelaxed] = connect(connector,initState,relaxedTermState,3);
clf
show(refPath);
hold on
axis equal
plot(trajGlobalRelaxed.Trajectory(:,1),trajGlobalRelaxed.Trajectory(:,2),'g');
hold off
```



## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
trajectoryGeneratorFrenet now supports code generation with DynamicMemoryAllocation='off'.

## See Also

## Objects

referencePathFrenet

## Functions

connect |closestPoint|closestPointsToSequence |closestProjections|curvature | changeInCurvature| tangentAngle|frenet2global|global2frenet|interpolate| show

## Topics

"Highway Trajectory Planning Using Frenet Reference Path"

Introduced in R2020b

## connect

Connect initial and terminal Frenet states

## Syntax

frenetTrajectory = connect(connectorFrenet,initialState,terminalState, timeSpan)
[ $\qquad$ ,globalTrajectory] = connect( $\qquad$ )

## Description

frenetTrajectory = connect(connectorFrenet,initialState,terminalState, timeSpan) connects the specified initial Frenet states to the specified terminal states over a span of time in seconds. This object function supports 1-to-n, $n$-to- 1 , or $n$-to- $n$ pairwise trajectory connections.
[ __ ,globalTrajectory] = connect( $\qquad$ ) returns the trajectories in global coordinates in addition to all arguments in the previous syntax.

## Examples

## Generate Alternative Trajectories for Reference Path

Generate alternative trajectories for a reference path using Frenet coordinates. Specify different initial and terminal states for your trajectories. Tune your states based on the generated trajectories.

Generate a reference path from a set of waypoints. Create a trajectoryGeneratorFrenet object from the reference path.

```
waypoints = [0 0; ...
    50 20; ...
    100 0; ...
    150 10];
refPath = referencePathFrenet(waypoints);
connector = trajectoryGeneratorFrenet(refPath);
```

Generate a five-second trajectory between the path origin and a point 30 m down the path as Frenet states.

```
initState = [0 0 0 0 0 0]; % [S ds ddS L dL ddL]
termState = [30 0 0 0 0 0]; % [S ds ddS L dL ddL]
[~,trajGlobal] = connect(connector,initState,termState,5);
```

Display the trajectory in global coordinates.

```
show(refPath);
hold on
axis equal
plot(trajGlobal.Trajectory(:,1),trajGlobal.Trajectory(:,2),'b')
legend(["Waypoints","Reference Path","Trajectory to 30m"])
```



Create a matrix of terminal states with lateral deviations between -3 m and 3 m . Generate trajectories that cover the same arc length in 10 seconds, but deviate laterally from the reference path. Display the new alternative paths.

```
termStateDeviated = termState + ([-3:3]' * [0 0 0 1 0 0]);
[~,trajGlobal] = connect(connector,initState,termStateDeviated,10);
clf
show(refPath);
hold on
axis equal
for i = 1:length(trajGlobal)
    plot(trajGlobal(i).Trajectory(:,1),trajGlobal(i).Trajectory(:,2),'g')
end
legend(["Waypoints","Reference Path","Alternative Trajectories"])
hold off
```



Specify a new terminal state to generate a new trajectory. This trajectory is not desirable because it requires reverse motion to achieve a lateral velocity of $10 \mathrm{~m} / \mathrm{s}$.
newTermState = [5 10 050 0];
[~,newTrajGlobal] = connect(connector,initState,newTermState,3);
clf
show(refPath);
hold on
axis equal
plot(newTrajGlobal.Trajectory(:,1),newTrajGlobal.Trajectory(:,2),'b'); legend(["Waypoint","Reference Path","New Trajectory"]) hold off


Relax the restriction on the longitudinal state by specifying an arc length of NaN. Generate and display the trajectory again. The new position shows a good alternative trajectory that deviates off the reference path.

```
relaxedTermState = [NaN 10 0 5 0 0];
[~,trajGlobalRelaxed] = connect(connector,initState,relaxedTermState,3);
clf
show(refPath);
hold on
axis equal
plot(trajGlobalRelaxed.Trajectory(:,1),trajGlobalRelaxed.Trajectory(:,2),'g');
hold off
```



## Input Arguments

connectorFrenet - Frenet trajectory generator
trajectoryGeneratorFrenet object
Frenet trajectory generator, specified as a trajectoryGeneratorFrenet object.

## initialState - Initial Frenet states

$n$-by-6 numeric matrix
Initial Frenet states, specified as an n-by-6 numeric matrix. Each row of the matrix is a set of Frenet coordinates for the initial state of a trajectory in the form [S dS ddS L dL ddL]. The value of $n$ must be equal to the number of rows in the terminalState argument or 1.

## terminalState - Final Frenet states

$n$-by-6 numeric matrix
Final Frenet states, specified as an $n$-by- 6 numeric matrix. Each row of the matrix is a set of Frenet coordinates for the initial state of a trajectory in the form [S dS ddS L dL ddL]. The value of $n$ must be equal to the number of rows in the initialState argument or 1 .

## timeSpan - Time horizon for all trajectories

positive scalar in seconds

Time horizon for all trajectories, specified as a positive scalar in seconds. The generated trajectories are sampled evenly across this time span based on the TimeResolution property of the trajectoryGeneratorFrenet object specified in the connectorFrenet argument.

## Output Arguments

## frenetTrajectory - Frenet trajectories

structure | structure array
Frenet trajectories between all initial and final states, returned as a structure array with these fields:

- Trajectory - $n$-by-6 numeric matrix. Each row of the matrix is a set of Frenet coordinates for the initial state of a trajectory in the form [ $S \mathrm{dS}$ ddS L dL ddL].
- Time - Vector of positive scalars from 0 to timeSpan in seconds.


Frenet States: [ $s \delta s \delta^{2} s L \delta L \delta^{2} L$ ]

This function supports 1-to-n, $n$-to-1, or $n$-to- $n$ pairwise trajectory connections based on the number of rows of initialState and terminalState.

## globalTrajectory - Global trajectories

structure | structure array
Global trajectories between all initial and final states, returned as structure or structure array with fields:

- Trajectory - $n$-by- 6 numeric matrix. Each row of the matrix is a set of global sates of the form [x y theta kappa dkappa s].
- Time - Vector of positive scalars from 0 to timeSpan in seconds.


This function supports 1-to-n, $n$-to-1, or $n$-to- $n$ pairwise trajectory connections based on the number of rows of initialState and terminalState.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

## Objects

referencePathFrenet | trajectoryGeneratorFrenet

## Functions

closestPoint|closestPointsToSequence |closestProjections|curvature| changeInCurvature| tangentAngle|frenet2global|global2frenet|interpolate| show

## Topics

"Highway Trajectory Planning Using Frenet Reference Path"
Introduced in R2020b

## createParalleIState

Create states using Frenet and global parameters

## Syntax

[globalState,frenetState,latTimeDerivatives] = createParallelState(refPath,S, L, V, A)
[_] = createParallelState(refPath,S,L,V,A,invertHeading)

## Description

[globalState,frenetState,latTimeDerivatives] = createParallelState(refPath,S, $\mathrm{L}, \mathrm{V}, \mathrm{A}$ ) takes an arclength, lateral deviation, body velocity, and body acceleration as S,L,V, and A respectively.
[_] = createParallelState(refPath, S, L, V, A, invertHeading) optionally accepts a vector invertHeading, indicating whether the state heading of each waypoint should be inverted or not.

## Input Arguments

## refPath - Reference path

referencePathFrenet object
Reference path, specified as a referencePathFrenet object.

## S - Path arclengths

N -element column vector
Path arclengths, specified as an $N$-element column vector in meters, where $N$ is the total number of desired arclengths to calculate.

## L - Lateral deviations

$N$-element column vector
Lateral deviation, specified as an $N$-element vector in meters. The lateral deviation is measured as the distance along the normal vector of the current path to the original path.
Data Types: single | double

## V - Body velocity

N -element column vector
Body velocity, specified as an $N$-element vector in meters per second. The velocity is derived by transforming the global velocity to the Frenet frame located at S along the path.
Data Types: single | double

## A - Body acceleration

$N$-element column vector

Body velocity, specified as an $N$-element vector in meters per second squared. The acceleration is derived by transforming the global acceleration to the Frenet frame located at S along the path.
Data Types: single | double

## invertHeading - Invert heading flag

$N$-element column vector
Invert heading flag, specified as an $N$-element column vector of binary values, indicating whether the state heading of each waypoint should be inverted or not. 0 indicates to not invert the heading, and 1 indicates to invert the heading.
Data Types: single | double

## Output Arguments

## globalState - Trajectory in global coordinate frame

$P$-by-6 numeric matrix
Trajectories in the global coordinate frame, specified as a $P$-by- 6 numeric matrix with rows of form [ x y theta kappa speed accel], where:

- $x y$ and theta -- SE(2) state expressed in global coordinates, with $x$ and $y$ in meters and theta in radians
- kappa -- Curvature, or inverse of the radius, in meters
- speed -- Speed in the theta direction in $\mathrm{m} / \mathrm{s}$
- accel -- Acceleration in the theta direction in $\mathrm{m} / \mathrm{s}^{2}$
$P$ is the number of Frenet trajectories converted to global trajectories.


## frenetState - Trajectory in Frenet coordinate frame

$P$-by-6 numeric matrix
Trajectory in the Frenet coordinate frame, returned as a $P$-by- 6 numeric matrix with rows of form [S $d S$ ddS $L$ dL ddL], where $S$ is the arc length and $L$ is the perpendicular deviation from the direction of the reference path. Derivatives of $S$ are relative to time. Derivatives of $L$ are relative to the arc length, S. $P$ is the number of Frenet states specified.

## latTimeDerivatives - Lateral time derivatives

$N$-by-3 matrix
Lateral time derivatives, specified as an $N$-by-3 matrix where each row is of the form [dL/dt $d d L / d t \wedge 2$ invertHeading] and $N$ is the total number of points in points. Each row contains the 1 st and 2nd order time derivatives of lateral deviation and a flag, invertHeading, which indicates whether the heading should be flipped when converting to global coordinates (true) or not (false).

Note If defining latTimeDerivatives without the use of global2frenet, the following rules should be followed:

1 The invertHeading flag should be true when:
a The vehicle is moving in reverse (speed is less than 0 )
b The vehicle is stationary (speed is equal to 0 ), and the vehicle is facing away from the path's tangent vector. i.e. $\cos (\mid$ tangentAngle(obj,S)-thetaExpected|) < 0
2 If 1 b is true, then $d L / d S$ must be negated.

## See Also

## Objects

referencePathFrenet | trajectoryGeneratorFrenet
Functions
closestPoint|closestPointsToSequence |closestProjections|curvature| changeInCurvature | tangentAngle \| frenet2global|global2frenet |interpolate | show

## Topics

"Highway Trajectory Planning Using Frenet Reference Path"
Introduced in R2022a

## trajectoryOptimalFrenet

Find optimal trajectory along reference path

## Description

The trajectoryOptimalFrenet object is a path planner which samples and evaluates local trajectories based on a reference path. The planner generates a set of terminal states based on the reference path and other parameters in the object. The planner then connects the state to each terminal state using $4^{\text {th }}$ or $5^{\text {th }}$ order polynomials. To choose an optimal path, sampled trajectories are evaluated for kinematic feasibility, collision, and cost.

## Creation

## Syntax

trajectoryOptimalFrenet(refPath, validator)
planner = trajectoryOptimalFrenet( __ , Name, Value)

## Description

trajectory0ptimalFrenet(refPath, validator) creates a trajectory0ptimalFrenet object with reference path, refPath, in the form of an $n$-by-2 array of $\left[\begin{array}{ll}x & y\end{array}\right]$ waypoints and a state validator, validator, specified as a validator0ccupancyMap object.
planner = trajectoryOptimalFrenet( __ , Name, Value) sets additional properties using one or more name-value pairs in any order.

## Input Arguments

## refPath - Reference path

$n$-by-2 matrix
Reference path, specified as an $n$-by- 2 matrix of $[x y]$ pairs, where $n$ is the number of waypoints.
Example: [100,100;400,400]
Data Types: double
validator - State validator object
validatorOccupancyMap object
State validator object, specified as a validator0ccupancyMap object.

## Properties

Note For the 'Weights ' and 'FeasibilityParameters ' properties, you cannot specify the entire structures at once. Instead, set their fields individually as name-value pairs. For example,
trajectory0ptimalFrenet(refPath,validator,'Deviation',0) sets the 'Deviation' field of the structure 'Weights'.

## Weights - Weights for all trajectory costs <br> structure

The weights for all trajectory costs, specified as a structure containing scalars for the cost multipliers of the corresponding trajectory attributes. The total trajectory cost is a sum of all attributes multiplied by their weights. The structure has the these fields.

## Time - Weight for time cost

0 (default) | positive scalar
The cost function multiplies the weight by the total time taken to reach the terminal state. Specify this value as the comma-separated pair of 'Time' and a positive scalar in seconds.
Data Types: double

## ArcLength - Weight for arc length cost <br> 0 (default) | positive scalar

The cost function multiplies the weight by the total length of the generated trajectories. Specify this value as the comma-separated pair of 'ArcLength' and a positive scalar in meters.

## Data Types: double

## LateralSmoothness - Weight for lateral jerk cost <br> 0 (default) | positive scalar

The cost function multiplies the weight by the integral of lateral jerk squared. This value determines the aggressiveness of the trajectory in the lateral direction (perpendicular to the reference path). Specify this value as the comma-separated pair of 'LateralSmoothness ' and a positive scalar. To penalize lateral jerk in the planned trajectory increase this cost value.
Data Types: double

## LongitudinalSmoothness - Weight for longitudinal jerk cost <br> 0 (default) | positive scalar

The cost function multiplies the weight by the integral of longitudinal jerk squared. This value determines the aggressiveness of the trajectories in the longitudinal direction (direction of the reference path). Specify this value as the comma-separated pair of 'LongitudinalSmoothness ' and a positive scalar. To penalize large change in forward and backward acceleration increase this cost value.
Data Types: double

## Deviation - Weight for deviation from reference path

1 (default) | positive scalar
The cost function multiplies the weight by the perpendicular distance from the reference path at the end of the trajectory in meters. Specify this value as the comma-separated pair of 'Deviation' and a positive scalar in meters.
Data Types: double

## Data Types: struct

## FeasibilityParameters - Structure containing feasibility parameters

structure
Feasibility parameters, specified as a structure containing scalar values to check the validity of a trajectory. The structure has the these fields.

MaxCurvature - Maximum curvature that vehicle can execute
0.1 (default) | positive real scalar

Maximum curvature that the vehicle can execute. Specify this value as the comma-separated pair of 'MaxCurvature ' and a positive real scalar in $\mathrm{m}^{-1}$. This value determines the kinematic feasibility of the trajectory.
Data Types: double

## MaxAcceleration - Maximum acceleration in direction of motion of vehicle

## 2.5 (default) | positive real scalar

Maximum acceleration in the direction of motion of the vehicle. Specify this value as the commaseparated pair of 'MaxAcceleration' and a positive real scalar in $\mathrm{m} / \mathrm{s}^{2}$. To lower the limit on the acceleration of the vehicle in the forward or reverse direction decrease this value.

Data Types: double
Data Types: struct

## TimeResolution - Trajectory discretization interval

0.1 (default) | positive real scalar

Time interval between discretized states of the trajectory. Specify this value as the comma-separated pair of 'TimeResolution' and a positive real scalar in seconds. These discretized states determine state validity and cost function.

Data Types: double

## CostFunction - User-defined cost function

nullCost (default) | function handle
The user-defined cost function, specified as a function handle. The function must accept a matrix of $n$ -by-7 states, TRAJSTATES, for each trajectory and return a cost value as a scalar. The plan function returns the path with the lowest cost.

For example, leftLaneChangeCost = @(states)((states(end,2) < refPath(end,2))*10) creates a cost function handle to prioritize left lane changes.
Data Types: function handle

## TrajectoryList - List of all possible trajectories <br> structure array

This property is read-only.
The 'TrajectoryList' property, returned as a structure array of all the candidate trajectories and their corresponding parameters. Each structure has the these fields:

- Trajectory - An n-by-7 matrix of $[x, y, ~ t h e t a, ~ k a p p a, ~ s p e e d, ~ a c c e l e r a t i o n, ~ t i m e], ~$ where $n$ is the number of trajectory waypoints.
- Cost - Cost of the trajectory.
- MaxAcceleration - Maximum acceleration of the trajectory.
- MaxCurvature - Maximum curvature of the trajectory.
- Feasible - A four-element vector [velocity, acceleration, curvature, collision] indicating the validity of the trajectory.

The value of the elements can be either,

- 1 - The trajectory is valid.
- 0 - The trajectory is invalid.
-     - 1 - The trajectory is not checked.


## Data Types: struct

## TerminalStates - Structure of all goal states

structure
A structure that contains a list of goal states relative to the reference path. These parameters define the sampling behavior for generating alternative trajectory segments between start and each goal state. The structure has the these fields.

## Longitudinal - Lengths of the trajectory segment

30:15:90 (default) | vector
Lengths of the trajectory segment, specified as a vector in meters.

## Data Types: double

## Lateral - Array of deviations from reference path in perpendicular direction at goal state <br> -2:1:2 (default) | vector

Array of deviations from reference path in perpendicular direction at goal state, specified as a vector in meters.

## Data Types: double

## Speed - Velocity at goal state in direction of motion

10 (default) | positive scalar
Velocity at the goal state in the direction of motion, specified as a positive scalar in $\mathrm{m} / \mathrm{s}$.
Data Types: double

## Acceleration - Acceleration at goal state in direction of motion <br> 0 (default) | positive scalar

Acceleration at the goal state in the direction of motion, specified as a positive scalar in $\mathrm{m} / \mathrm{s}^{2}$.
Data Types: double

## Time - Array of end-times for executing trajectory segment

7 (default) | positive vector

Array of end-times for executing the trajectory segment, specified as a positive vector in seconds.
Data Types: double
Data Types: struct

## Waypoints - Waypoints of reference path

[ ] (default) | n-by-2 matrix
Waypoints of reference path, specified as an $n$-by-2 matrix of $[x \quad y]$ pairs, where $n$ is the number of waypoints. Waypoints act as a reference for planning alternative trajectories optimized by this planner.
Data Types: double

## NumSegments - Number of longitudinal segments for each trajectory

1 (default) | positive scalar
Number of longitudinal segments for each trajectory. Specify this value as the comma-separated pair of 'NumSegments' and a positive scalar. This property generates intermediate longitudinal terminal states to which all lateral terminal states are combined with for generating more motion primitives to each terminal state.

For example, 'NumSegments' , 2 creates two partitions between each longitudinal terminal state. Trajectories are generated to reach the intermediate longitudinal states with all the available lateral terminal states.

Data Types: double

## DeviationOffset - Deviation offset from reference path in lateral direction 0 (default) | scalar

Deviation offset from the reference path in the lateral direction. Specify this value as the commaseparated pair of 'DeviationOffset' and a scalar. A negative value offset the deviation to the right, and a positive value offset the deviation to the left of the reference path in the lateral direction. Set this property to bias your solution to a certain turn direction when avoiding obstacles in the reference path.
Data Types: double

## Object Functions

cart2frenet Convert Cartesian states to Frenet states
copy $\quad$ Create deep copy of object
frenet2cart Convert Frenet states to Cartesian states
plan Plan optimal trajectory
show Visualize trajectories

## Examples

## Optimal Trajectory Planning in Frenet Space

This example shows how to plan an optimal trajectory using a trajectoryOptimalFrenet object.

## Create and Assign Map to State Validator

Create a state validator object for collision checking.

```
stateValidator = validatorOccupancyMap;
```

Create an obstacle grid map.

```
grid = zeros(50,100);
```

grid(24:26,48:53) = 1;

Create a binaryOccupancyMap with the grid map.
map = binary0ccupancyMap(grid);
Assign the map and the state bounds to the state validator.

```
stateValidator.Map = map;
stateValidator.StateSpace.StateBounds(1:2,:) = [map.XWorldLimits; map.YWorldLimits];
```

Plan and Visualize Trajectory
Create a reference path for the planner to follow.
refPath = [0,25;100,25];
Initialize the planner object with the reference path, and the state validator.
planner = trajectoryOptimalFrenet(refPath,stateValidator);
Assign longitudinal terminal state, lateral deviation, and maximum acceleration values.

```
planner.TerminalStates.Longitudinal = 100;
planner.TerminalStates.Lateral = -10:5:10;
planner.FeasibilityParameters.MaxAcceleration = 10;
```

Specify the deviation offset value close to the left lateral terminal state to prioritize left lane changes.
planner. Deviation0ffset $=5$;

## Trajectory Planning

Initial cartesian state of vehicle.

```
initCartState = [0 25 pi/9 0 0 0];
```

Convert cartesian state of vehicle to Frenet state.

```
initFrenetState = cart2frenet(planner,initCartState);
```

Plan a trajectory from initial Frenet state.
plan(planner,initFrenetState);

## Trajectory Visualization

Visualize the map and the trajectories.

```
show(map)
hold on
show(planner,'Trajectory','all')
```



## Partitioning Longitudinal Terminal States in Trajectory Generation

This example shows how to partition the longitudinal terminal states in optimal trajectory planning using a trajectoryOptimalFrenet object.

## Create and Assign Map to State Validator

Create a state validator object for collision checking.
stateValidator = validatorOccupancyMap;
Create an obstacle grid map.

```
grid = zeros(50,100);
grid(25:27,28:33) = 1;
grid(16:18,37:42) = 1;
grid(29:31,72:77) = 1;
```

Create a binary0ccupancyMap with the grid map.
map $=$ binary0ccupancyMap(grid);

Assign the map and the state bounds to the state validator.

```
stateValidator.Map = map;
stateValidator.StateSpace.StateBounds(1:2,:) = [map.XWorldLimits; map.YWorldLimits];
Plan and Visualize Trajectory
```

Create a reference path for the planner to follow.

```
refPath = [0,25;30,30;75,20;100,25];
```

Initialize the planner object with the reference path, and the state validator.

```
planner = trajectory0ptimalFrenet(refPath,stateValidator);
```

Assign longitudinal terminal state, lateral deviation, and maximum acceleration values.

```
planner.TerminalStates.Longitudinal = 100;
planner.TerminalStates.Lateral = -5:5:5;
planner.FeasibilityParameters.MaxAcceleration = 10;
```

Assign the number of partitions for the longitudinal terminal state.

```
planner.NumSegments = 3;
```


## Trajectory Planning

Initial Frenet state of vehicle.

```
initFrenetState = zeros(1,6);
```

Plan a trajectory from initial Frenet state.

```
plan(planner,initFrenetState);
```


## Trajectory Visualization

Visualize the map and the trajectories.

```
show(map)
hold on
show(planner,'Trajectory','all')
hold on
```


## Generate Lane Boundaries

Calculate end of reference path as Frenet state.

```
refPathEnd = cart2frenet(planner,[planner.Waypoints(end,:) 0 0 0 0]);
```

Calculate lane offsets on both sides of the lateral terminal states with half lane width value.

```
laneOffsets = unique([planner.TerminalStates.Lateral+2.5 planner.TerminalStates.Lateral-2.5]);
Calculate positions of lanes in Cartesian state.
numLaneOffsets = numel(laneOffsets);
xRefPathEnd = ceil(refPathEnd(1));
laneXY = zeros((numLaneOffsets*xRefPathEnd)+numLaneOffsets,2);
```

```
xIndex = 0;
for laneID = 1:numLane0ffsets
    for x = 1:xRefPathEnd
        laneCart = frenet2cart(planner,[x 0 0 laneOffsets(laneID) 0 0]);
        xIndex = xIndex + 1;
        laneXY(xIndex,:) = laneCart(1:2);
    end
    xIndex = xIndex + 1;
    laneXY(xIndex,:) = NaN(1,2);
end
```

Plot lane boundaries.
plot(laneXY(:,1),laneXY(:,2),'LineWidth',0.5,'Color',[0.5 0.5 0.5],'DisplayName','Lane Boundarie

Binary Occupancy Grid


## Limitations

- Self-intersections in the reference path can lead to unexpected behavior.
- The planner does not support reverse driving.
- Initial orientation for planning should be within - pi/2 and pi/2 to the reference path.
- Limit the number of TerminalStates for real-time applications since computational complexity grows with it.


## References

[1] Werling, Moritz, Julius Ziegler, Sören Kammel, and Sebastian Thrun. "Optimal Trajectory Generation for Dynamic Street Scenarios in a Frenet Frame." 2010 IEEE International Conference on Robotics and Automation. 2010, pp. 987-993.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{rm}}$.

## See Also

validator0ccupancyMap|nav.StateValidator|plannerHybridAStar
Introduced in R2019b

## cart2frenet

Convert Cartesian states to Frenet states

## Syntax

cart2frenet(planner, cartesianStates)

## Description

cart2frenet( $p l a n n e r$, cartesianStates) converts a six-element vector of cartesianStates [ $x, y$, theta, kappa, speed, acceleration] to a six-element vector of Frenet states [s, $\left.d s / d t, d^{2} s / d t^{2}, \quad l, d l / d s, d^{2} l / d s^{2}\right]$, where $s$ is arc length from the first point in reference path, and $l$ is normal distance from the closest point at $s$ on the reference path.

## Examples

## Optimal Trajectory Planning in Frenet Space

This example shows how to plan an optimal trajectory using a trajectoryOptimalFrenet object.

## Create and Assign Map to State Validator

Create a state validator object for collision checking.
stateValidator = validatorOccupancyMap;
Create an obstacle grid map.

```
grid = zeros(50,100);
```

grid(24:26,48:53) = 1;

Create a binaryOccupancyMap with the grid map.
map = binaryOccupancyMap(grid);
Assign the map and the state bounds to the state validator.

```
stateValidator.Map = map;
stateValidator.StateSpace.StateBounds(1:2,:) = [map.XWorldLimits; map.YWorldLimits];
Plan and Visualize Trajectory
```

Create a reference path for the planner to follow.
refPath $=[0,25 ; 100,25]$;
Initialize the planner object with the reference path, and the state validator.
planner = trajectoryOptimalFrenet(refPath,stateValidator);
Assign longitudinal terminal state, lateral deviation, and maximum acceleration values.
planner.TerminalStates.Longitudinal = 100;
planner.TerminalStates.Lateral = -10:5:10;
planner. FeasibilityParameters.MaxAcceleration = 10;
Specify the deviation offset value close to the left lateral terminal state to prioritize left lane changes.
planner. Deviation0ffset = 5;

## Trajectory Planning

Initial cartesian state of vehicle.
initCartState = [0 25 pi/9 000$]$;
Convert cartesian state of vehicle to Frenet state.
initFrenetState = cart2frenet(planner,initCartState);
Plan a trajectory from initial Frenet state.
plan(planner,initFrenetState) ;

## Trajectory Visualization

Visualize the map and the trajectories.

```
show(map)
hold on
show(planner,'Trajectory','all')
```



## Partitioning Longitudinal Terminal States in Trajectory Generation

This example shows how to partition the longitudinal terminal states in optimal trajectory planning using a trajectory0ptimalFrenet object.

## Create and Assign Map to State Validator

Create a state validator object for collision checking.

```
stateValidator = validatorOccupancyMap;
```

Create an obstacle grid map.
grid $=$ zeros(50,100);
grid(25:27,28:33) = 1;
grid(16:18,37:42) = 1;
grid(29:31,72:77) = 1;
Create a binary0ccupancyMap with the grid map.
map $=$ binary0ccupancyMap(grid);
Assign the map and the state bounds to the state validator.

```
stateValidator.Map = map;
stateValidator.StateSpace.StateBounds(1:2,:) = [map.XWorldLimits; map.YWorldLimits];
```


## Plan and Visualize Trajectory

Create a reference path for the planner to follow.
refPath $=[0,25 ; 30,30 ; 75,20 ; 100,25] ;$
Initialize the planner object with the reference path, and the state validator.

```
planner = trajectoryOptimalFrenet(refPath,stateValidator);
```

Assign longitudinal terminal state, lateral deviation, and maximum acceleration values.

```
planner.TerminalStates.Longitudinal = 100;
planner.TerminalStates.Lateral = -5:5:5;
planner.FeasibilityParameters.MaxAcceleration = 10;
```

Assign the number of partitions for the longitudinal terminal state.

```
planner.NumSegments = 3;
```


## Trajectory Planning

Initial Frenet state of vehicle.

```
initFrenetState = zeros(1,6);
```

Plan a trajectory from initial Frenet state.

```
plan(planner,initFrenetState);
```


## Trajectory Visualization

Visualize the map and the trajectories.

```
show(map)
hold on
show(planner,'Trajectory','all')
hold on
```


## Generate Lane Boundaries

Calculate end of reference path as Frenet state.

```
refPathEnd = cart2frenet(planner,[planner.Waypoints(end,:) 0 0 0 0]);
```

Calculate lane offsets on both sides of the lateral terminal states with half lane width value.

```
laneOffsets = unique([planner.TerminalStates.Lateral+2.5 planner.TerminalStates.Lateral-2.5]);
```

Calculate positions of lanes in Cartesian state.

```
numLaneOffsets = numel(laneOffsets);
xRefPathEnd = ceil(refPathEnd(1));
laneXY = zeros((numLaneOffsets*xRefPathEnd)+numLaneOffsets,2);
xIndex = 0;
for laneID = 1:numLaneOffsets
    for x = 1:xRefPathEnd
        laneCart = frenet2cart(planner,[x 0 0 laneOffsets(laneID) 0 0]);
```

```
    xIndex = xIndex + 1;
    laneXY(xIndex,:) = laneCart(1:2);
    end
    xIndex = xIndex + 1;
    laneXY(xIndex,:) = NaN(1,2);
end
```

Plot lane boundaries.
plot(laneXY(:,1),laneXY(:,2),'LineWidth',0.5,'Color',[0.5 0.5 0.5],'DisplayName','Lane Boundarie

Binary Occupancy Grid


## Input Arguments

planner - Optimal trajectory planner in Frenet space
trajectoryOptimalFrenet object
Optimal trajectory planner in Frenet space, specified as a trajectoryOptimalFrenet object.

## cartesianStates - Vector of Cartesian states

six-element vector
Vector of Cartesian states, specified as a 1-by-6 vector $[x, y, t h e t a, ~ k a p p a, ~ s p e e d$, acceleration].

- $x$ and $y$ specify the position in meters.
- theta specifies the orientation angle in radians.
- kappa specifies the curvature in $\mathrm{m}^{-1}$.
- speed specifies the velocity in $\mathrm{m} / \mathrm{s}$.
- acceleration specifies the acceleration in $\mathrm{m} / \mathrm{s}^{2}$.

Example: [110 110 pi/4 000 ]
Data Types: double

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

trajectoryOptimalFrenet | frenet2cart
Introduced in R2019b

## copy

Create deep copy of object

## Syntax

plannerCopy $=\operatorname{copy}($ planner $)$

## Description

plannerCopy $=$ copy (planner) creates a deep copy of the trajectoryOptimalFrenet object with the same properties.

## Examples

## Create Copy of trajectoryOptimalFrenet Object

Create a binary0ccupancyMap with a obstacle grid map.

```
grid = zeros(50,100);
```

$\operatorname{grid}(24: 26,48: 53)=1$;
map = binaryOccupancyMap(grid);

Create a state validator. Assign the map and the state bounds to the state validator.

```
validator = validatorOccupancyMap;
validator.Map = map;
validator.StateSpace.StateBounds(1:2,:) = [map.XWorldLimits; map.YWorldLimits];
```

Create a reference path for the planner.
refPath $=[0,25 ; 100,25]$;
Create a trajectory0ptimalFrenet object.

```
planner = trajectoryOptimalFrenet(refPath,validator)
planner =
    trajectoryOptimalFrenet with properties:
```

                            Weights: [1x1 struct]
        FeasibilityParameters: [1x1 struct]
            TimeResolution: 0.1000
                NumSegments: 1
            DeviationOffset: 0
                CostFunction: @trajectory0ptimalFrenet.nullCost
            TrajectoryList: [1x1 struct]
            TerminalStates: [1x1 struct]
                    Waypoints: [2×2 double]
    Create a copy of trajectoryOptimalFrenet object.

```
plannerNew = copy(planner)
plannerNew =
    trajectoryOptimalFrenet with properties:
                            Weights: [1x1 struct]
        FeasibilityParameters: [1x1 struct]
            TimeResolution: 0.1000
                NumSegments: 1
            DeviationOffset: 0
                CostFunction: @trajectory0ptimalFrenet.nullCost
            TrajectoryList: [1x1 struct]
            TerminalStates: [1x1 struct]
                    Waypoints: [2x2 double]
```


## Input Arguments

planner - Trajectory optimal Frenet object
trajectoryOptimalFrenet object
Trajectory optimal Frenet object, specified as a trajectory0ptimalFrenet object.

## Output Arguments

plannerCopy - Copy of trajectory optimal Frenet object
trajectoryOptimalFrenet object
Copy of trajectory optimal Frenet object, returned as a trajectoryOptimalFrenet object with the same properties.

## See Also

trajectory0ptimalFrenet
Introduced in R2020b

## frenet2cart

Convert Frenet states to Cartesian states

## Syntax

frenet2cart(planner,frenetStates)

## Description

frenet2cart(planner,frenetStates) converts a six-element vector of frenetStates [ $s$, $\left.d s / d t, d^{2} s / d t^{2}, l, d l / d s, d^{2} l / d s^{2}\right]$ to a six-element vector of Cartesian states $[x, y$, theta, kappa, speed, acceleration].

## Examples

## Optimal Trajectory Planning in Frenet Space

This example shows how to plan an optimal trajectory using a trajectoryOptimalFrenet object.

## Create and Assign Map to State Validator

Create a state validator object for collision checking.
stateValidator = validatorOccupancyMap;
Create an obstacle grid map.

```
grid = zeros(50,100);
```

grid(24:26,48:53) = 1;

Create a binary0ccupancyMap with the grid map.
map $=$ binaryOccupancyMap(grid);
Assign the map and the state bounds to the state validator.
stateValidator.Map = map;
stateValidator.StateSpace.StateBounds(1:2,:) = [map.XWorldLimits; map.YWorldLimits];

## Plan and Visualize Trajectory

Create a reference path for the planner to follow.
refPath $=[0,25 ; 100,25] ;$
Initialize the planner object with the reference path, and the state validator.
planner = trajectoryOptimalFrenet(refPath,stateValidator);
Assign longitudinal terminal state, lateral deviation, and maximum acceleration values.
planner.TerminalStates.Longitudinal = 100;
planner.TerminalStates.Lateral = -10:5:10;
planner. FeasibilityParameters.MaxAcceleration = 10;
Specify the deviation offset value close to the left lateral terminal state to prioritize left lane changes.
planner. Deviation0ffset = 5;

## Trajectory Planning

Initial cartesian state of vehicle.
initCartState = [0 25 pi/9 000$]$;
Convert cartesian state of vehicle to Frenet state.

```
initFrenetState = cart2frenet(planner,initCartState);
```

Plan a trajectory from initial Frenet state.
plan(planner,initFrenetState);

## Trajectory Visualization

Visualize the map and the trajectories.

```
show(map)
hold on
show(planner,'Trajectory','all')
```



## Partitioning Longitudinal Terminal States in Trajectory Generation

This example shows how to partition the longitudinal terminal states in optimal trajectory planning using a trajectory0ptimalFrenet object.

## Create and Assign Map to State Validator

Create a state validator object for collision checking.

```
stateValidator = validatorOccupancyMap;
```

Create an obstacle grid map.
grid $=$ zeros(50,100);
grid(25:27,28:33) = 1;
grid(16:18,37:42) = 1;
grid(29:31,72:77) = 1;
Create a binary0ccupancyMap with the grid map.
map $=$ binary0ccupancyMap(grid);
Assign the map and the state bounds to the state validator.

```
stateValidator.Map = map;
stateValidator.StateSpace.StateBounds(1:2,:) = [map.XWorldLimits; map.YWorldLimits];
```


## Plan and Visualize Trajectory

Create a reference path for the planner to follow.
refPath $=[0,25 ; 30,30 ; 75,20 ; 100,25] ;$
Initialize the planner object with the reference path, and the state validator.

```
planner = trajectoryOptimalFrenet(refPath,stateValidator);
```

Assign longitudinal terminal state, lateral deviation, and maximum acceleration values.

```
planner.TerminalStates.Longitudinal = 100;
planner.TerminalStates.Lateral = -5:5:5;
planner.FeasibilityParameters.MaxAcceleration = 10;
```

Assign the number of partitions for the longitudinal terminal state.

```
planner.NumSegments = 3;
```


## Trajectory Planning

Initial Frenet state of vehicle.

```
initFrenetState = zeros(1,6);
```

Plan a trajectory from initial Frenet state.

```
plan(planner,initFrenetState);
```


## Trajectory Visualization

Visualize the map and the trajectories.

```
show(map)
hold on
show(planner,'Trajectory','all')
hold on
```


## Generate Lane Boundaries

Calculate end of reference path as Frenet state.

```
refPathEnd = cart2frenet(planner,[planner.Waypoints(end,:) 0 0 0 0]);
```

Calculate lane offsets on both sides of the lateral terminal states with half lane width value.
laneOffsets $=$ unique([planner.TerminalStates.Lateral+2.5 planner.TerminalStates.Lateral-2.5]);
Calculate positions of lanes in Cartesian state.

```
numLaneOffsets = numel(laneOffsets);
xRefPathEnd = ceil(refPathEnd(1));
laneXY = zeros((numLaneOffsets*xRefPathEnd)+numLaneOffsets,2);
xIndex = 0;
for laneID = 1:numLaneOffsets
    for x = 1:xRefPathEnd
        laneCart = frenet2cart(planner,[x 0 0 laneOffsets(laneID) 0 0]);
```

```
    xIndex = xIndex + 1;
    laneXY(xIndex,:) = laneCart(1:2);
    end
    xIndex = xIndex + 1;
    laneXY(xIndex,:) = NaN(1,2);
end
```

Plot lane boundaries.

```
plot(laneXY(:,1),laneXY(:,2),'LineWidth',0.5,'Color',[0.5 0.5 0.5],'DisplayName','Lane Boundarie
```

Binary Occupancy Grid


## Input Arguments

## planner - Optimal trajectory planner in Frenet space <br> trajectoryOptimalFrenet object

Optimal trajectory planner in Frenet space, specified as a trajectoryOptimalFrenet object.

## frenetStates - Vector of Frenet states

six-element vector
Vector of Frenet states, specified as a 1-by-6 vector, [ $\left.s, d s / d t, d^{2} s / d t^{2}, l, d l / d s, d^{2} l / d s^{2}\right]$.

- $s$ specifies the arc length from the first point in reference path in meters.
- $d s / d t$ specifies the first derivative of arc length.
- $d^{2} s / d t^{2}$ specifies the second derivative of arc length.
- $l$ specifies the normal distance from the closest point in the reference path in meters.
- $d l / d s$ specifies the first derivative of normal distance.
- $d^{2} l / d s^{2}$ specifies the second derivative of normal distance.

Example: [10 10300$]$
Data Types: double

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{Tm}}$.

## See Also

trajectoryOptimalFrenet |cart2frenet
Introduced in R2019b

## plan

Plan optimal trajectory

## Syntax

[traj,index,cost,flag] = plan(planner,start)

## Description

[traj,index,cost,flag] = plan(planner,start) computes a feasible trajectory, traj, from a list of candidate trajectories generated from the trajectoryOptimalFrenet object, planner. start is specified as a six-element vector $\left[s, d s / d t, d^{2} s / d t^{2}, l, d l / d s, d^{2} l / d s^{2}\right]$, where $s$ is the arc length from the first point in the reference path, and $l$ is normal distance from the closest point at $s$ on the reference path.

The output trajectory, traj, also has an associated cost and index for the TrajectoryList property of the planner. flag is a numeric exit flag indicating status of the solution.

To improve the results of the planning output, modify the parameters on the planner object.

## Examples

## Optimal Trajectory Planning in Frenet Space

This example shows how to plan an optimal trajectory using a trajectoryOptimalFrenet object.

## Create and Assign Map to State Validator

Create a state validator object for collision checking.
stateValidator = validatorOccupancyMap;
Create an obstacle grid map.
grid $=$ zeros $(50,100)$;
$\operatorname{grid}(24: 26,48: 53)=1$;
Create a binary0ccupancyMap with the grid map.
map = binaryOccupancyMap(grid);
Assign the map and the state bounds to the state validator.

```
stateValidator.Map = map;
stateValidator.StateSpace.StateBounds(1:2,:) = [map.XWorldLimits; map.YWorldLimits];
Plan and Visualize Trajectory
Create a reference path for the planner to follow.
refPath \(=[0,25 ; 100,25]\);
```

Initialize the planner object with the reference path, and the state validator.

```
planner = trajectoryOptimalFrenet(refPath,stateValidator);
```

Assign longitudinal terminal state, lateral deviation, and maximum acceleration values.

```
planner.TerminalStates.Longitudinal = 100;
planner.TerminalStates.Lateral = -10:5:10;
planner.FeasibilityParameters.MaxAcceleration = 10;
```

Specify the deviation offset value close to the left lateral terminal state to prioritize left lane changes.

```
planner.DeviationOffset = 5;
```


## Trajectory Planning

Initial cartesian state of vehicle.

```
initCartState = [0 25 pi/9 0 0 0];
```

Convert cartesian state of vehicle to Frenet state.

```
initFrenetState = cart2frenet(planner,initCartState);
```

Plan a trajectory from initial Frenet state.
plan(planner,initFrenetState);

## Trajectory Visualization

Visualize the map and the trajectories.

```
show(map)
hold on
show(planner,'Trajectory','all')
```



## Partitioning Longitudinal Terminal States in Trajectory Generation

This example shows how to partition the longitudinal terminal states in optimal trajectory planning using a trajectory0ptimalFrenet object.

## Create and Assign Map to State Validator

Create a state validator object for collision checking.

```
stateValidator = validatorOccupancyMap;
```

Create an obstacle grid map.
grid $=$ zeros(50,100);
grid(25:27,28:33) = 1;
grid(16:18,37:42) = 1;
grid(29:31,72:77) = 1;
Create a binary0ccupancyMap with the grid map.
map $=$ binary0ccupancyMap(grid);
Assign the map and the state bounds to the state validator.

```
stateValidator.Map = map;
stateValidator.StateSpace.StateBounds(1:2,:) = [map.XWorldLimits; map.YWorldLimits];
```


## Plan and Visualize Trajectory

Create a reference path for the planner to follow.
refPath $=[0,25 ; 30,30 ; 75,20 ; 100,25] ;$
Initialize the planner object with the reference path, and the state validator.

```
planner = trajectoryOptimalFrenet(refPath,stateValidator);
```

Assign longitudinal terminal state, lateral deviation, and maximum acceleration values.

```
planner.TerminalStates.Longitudinal = 100;
planner.TerminalStates.Lateral = -5:5:5;
planner.FeasibilityParameters.MaxAcceleration = 10;
```

Assign the number of partitions for the longitudinal terminal state.

```
planner.NumSegments = 3;
```


## Trajectory Planning

Initial Frenet state of vehicle.

```
initFrenetState = zeros(1,6);
```

Plan a trajectory from initial Frenet state.

```
plan(planner,initFrenetState);
```


## Trajectory Visualization

Visualize the map and the trajectories.

```
show(map)
hold on
show(planner,'Trajectory','all')
hold on
```


## Generate Lane Boundaries

Calculate end of reference path as Frenet state.

```
refPathEnd = cart2frenet(planner,[planner.Waypoints(end,:) 0 0 0 0]);
```

Calculate lane offsets on both sides of the lateral terminal states with half lane width value.

```
laneOffsets = unique([planner.TerminalStates.Lateral+2.5 planner.TerminalStates.Lateral-2.5]);
```

Calculate positions of lanes in Cartesian state.

```
numLaneOffsets = numel(laneOffsets);
xRefPathEnd = ceil(refPathEnd(1));
laneXY = zeros((numLaneOffsets*xRefPathEnd)+numLaneOffsets,2);
xIndex = 0;
for laneID = 1:numLaneOffsets
    for x = 1:xRefPathEnd
        laneCart = frenet2cart(planner,[x 0 0 laneOffsets(laneID) 0 0]);
```

```
    xIndex = xIndex + 1;
    laneXY(xIndex,:) = laneCart(1:2);
    end
    xIndex = xIndex + 1;
    laneXY(xIndex,:) = NaN(1,2);
end
```

Plot lane boundaries.

```
plot(laneXY(:,1),laneXY(:,2),'LineWidth',0.5,'Color',[0.5 0.5 0.5],'DisplayName','Lane Boundarie
```

Binary Occupancy Grid


## Input Arguments

## planner - Optimal trajectory planner in Frenet space

trajectory0ptimalFrenet object
Optimal trajectory planner in Frenet space, specified as a trajectory0ptimalFrenet object.

## start - Initial Frenet state

six-element vector
Initial Frenet state, specified as a 1-by-6 vector [s, $\left.d s / d t, d^{2} s / d t^{2}, l, d l / d s, d^{2} l / d s^{2}\right]$.

- $s$ specifies the arc length from the first point in reference path in meters.
- $d s / d t$ specifies the first derivative of arc length.
- $d^{2} s / d t^{2}$ specifies the second derivative of arc length.
- $l$ specifies the normal distance from the closest point in the reference path in meters.
- $d l / d s$ specifies the first derivative of normal distance.
- $d^{2} l / d s^{2}$ specifies the second derivative of normal distance.


## Output Arguments

## traj - Feasible trajectory with minimum cost

n-by-7 matrix
Feasible trajectory with minimum cost, returned as an $n-b y-7$ matrix of $[x, y, \quad$ theta, kappa, speed, acceleration, time], where $n$ is the number of trajectory waypoints.

- $\quad x$ and $y$ specify the position in meters.
- theta specifies the orientation angle in radians.
- kappa specifies the curvature in $\mathrm{m}^{-1}$.
- speed specifies the velocity in $\mathrm{m} / \mathrm{s}$.
- acceleration specifies the acceleration in $\mathrm{m} / \mathrm{s}^{2}$.
- time specifies the time in s .
index - Index of feasible trajectory with minimum cost
positive integer scalar
Index of feasible trajectory with minimum cost, returned as a positive integer scalar.
cost - Least cost of feasible trajectory
positive scalar
Least cost of feasible trajectory, returned as a positive scalar.
flag - Exit flag indicating solution status
0| 1
Exit flag indicating the solution status, returned either as 0 or 1.
- 0 - Optimal trajectory was found.
- 1 - No feasible trajectory exists.

When no feasible trajectory exists, the planner returns an empty trajectory.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® $\mathrm{Coder}^{\mathrm{TM}}$.

## See Also

trajectory0ptimalFrenet|show

## Introduced in R2019b

## show

Visualize trajectories

## Syntax

show(planner)
show(planner, Name, Value)
axHandle $=$ show(planner)

## Description

show ( $p l a n n e r$ ) visualizes the reference path and trajectory from the candidates generated by the plan function. The trajectory is shown as a line plot. The plot also includes datatip mode, which can be used to visualize the feasibility vector and index of the trajectory from the TrajectoryList property.
show(planner, Name, Value) specifies additional options using one or more Name, Value pair arguments.
axHandle $=$ show(planner) returns the axes handle of the figure used to plot the trajectory.

## Examples

## Optimal Trajectory Planning in Frenet Space

This example shows how to plan an optimal trajectory using a trajectoryOptimalFrenet object.

## Create and Assign Map to State Validator

Create a state validator object for collision checking.
stateValidator = validatorOccupancyMap;
Create an obstacle grid map.
grid $=$ zeros (50,100);
$\operatorname{grid}(24: 26,48: 53)=1$;
Create a binary0ccupancyMap with the grid map.

```
map = binaryOccupancyMap(grid);
```

Assign the map and the state bounds to the state validator.

```
stateValidator.Map = map;
stateValidator.StateSpace.StateBounds(1:2,:) = [map.XWorldLimits; map.YWorldLimits];
Plan and Visualize Trajectory
Create a reference path for the planner to follow.
```

```
refPath = [0,25;100,25];
```

```
refPath = [0,25;100,25];
```

Initialize the planner object with the reference path, and the state validator.

```
planner = trajectoryOptimalFrenet(refPath,stateValidator);
```

Assign longitudinal terminal state, lateral deviation, and maximum acceleration values.
planner.TerminalStates.Longitudinal = 100;
planner.TerminalStates.Lateral = -10:5:10;
planner. FeasibilityParameters.MaxAcceleration = 10;
Specify the deviation offset value close to the left lateral terminal state to prioritize left lane changes.

```
planner.DeviationOffset = 5;
```


## Trajectory Planning

Initial cartesian state of vehicle.

```
initCartState = [0 25 pi/9 0 0 0];
```

Convert cartesian state of vehicle to Frenet state.

```
initFrenetState = cart2frenet(planner,initCartState);
```

Plan a trajectory from initial Frenet state.
plan(planner,initFrenetState);

## Trajectory Visualization

Visualize the map and the trajectories.

```
show(map)
hold on
show(planner,'Trajectory','all')
```



## Partitioning Longitudinal Terminal States in Trajectory Generation

This example shows how to partition the longitudinal terminal states in optimal trajectory planning using a trajectory0ptimalFrenet object.

## Create and Assign Map to State Validator

Create a state validator object for collision checking.

```
stateValidator = validatorOccupancyMap;
```

Create an obstacle grid map.
grid $=$ zeros(50,100);
grid(25:27,28:33) = 1;
grid(16:18,37:42) = 1;
grid(29:31,72:77) = 1;
Create a binary0ccupancyMap with the grid map.
map $=$ binary0ccupancyMap(grid);
Assign the map and the state bounds to the state validator.

```
stateValidator.Map = map;
stateValidator.StateSpace.StateBounds(1:2,:) = [map.XWorldLimits; map.YWorldLimits];
```


## Plan and Visualize Trajectory

Create a reference path for the planner to follow.
refPath $=[0,25 ; 30,30 ; 75,20 ; 100,25] ;$
Initialize the planner object with the reference path, and the state validator.

```
planner = trajectoryOptimalFrenet(refPath,stateValidator);
```

Assign longitudinal terminal state, lateral deviation, and maximum acceleration values.

```
planner.TerminalStates.Longitudinal = 100;
planner.TerminalStates.Lateral = -5:5:5;
planner.FeasibilityParameters.MaxAcceleration = 10;
```

Assign the number of partitions for the longitudinal terminal state.

```
planner.NumSegments = 3;
```


## Trajectory Planning

Initial Frenet state of vehicle.

```
initFrenetState = zeros(1,6);
```

Plan a trajectory from initial Frenet state.

```
plan(planner,initFrenetState);
```


## Trajectory Visualization

Visualize the map and the trajectories.

```
show(map)
hold on
show(planner,'Trajectory','all')
hold on
```


## Generate Lane Boundaries

Calculate end of reference path as Frenet state.

```
refPathEnd = cart2frenet(planner,[planner.Waypoints(end,:) 0 0 0 0]);
```

Calculate lane offsets on both sides of the lateral terminal states with half lane width value.

```
laneOffsets = unique([planner.TerminalStates.Lateral+2.5 planner.TerminalStates.Lateral-2.5]);
```

Calculate positions of lanes in Cartesian state.

```
numLaneOffsets = numel(laneOffsets);
xRefPathEnd = ceil(refPathEnd(1));
laneXY = zeros((numLaneOffsets*xRefPathEnd)+numLaneOffsets,2);
xIndex = 0;
for laneID = 1:numLaneOffsets
    for x = 1:xRefPathEnd
        laneCart = frenet2cart(planner,[x 0 0 laneOffsets(laneID) 0 0]);
```

```
    xIndex = xIndex + 1;
    laneXY(xIndex,:) = laneCart(1:2);
    end
    xIndex = xIndex + 1;
    laneXY(xIndex,:) = NaN(1,2);
end
```

Plot lane boundaries.
plot(laneXY(:,1),laneXY(:,2),'LineWidth',0.5,'Color',[0.5 0.5 0.5],'DisplayName','Lane Boundarie

Binary Occupancy Grid


## Input Arguments

## planner - Optimal trajectory planner in Frenet space <br> trajectory0ptimalFrenet object

Optimal trajectory planner in Frenet space, specified as a trajectory0ptimalFrenet object.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . , NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: 'Trajectory', 'all'

## Parent - Axes to plot trajectory

## Axes object | UIAxes object

Axes to plot trajectory, specified as the comma-separated pair consisting of 'Parent ' and either an Axes or UIAxes object. See axes or uiaxes.

Trajectory - Trajectory display option
'optimal' (default)|'all'
Trajectory display option, specified as the comma-separated pair consisting of 'Trajectory' and either 'optimal' or 'all'.

## ReferencePath - Reference path display option

'on' (default) | 'off'
Reference path display option, specified as the comma-separated pair consisting of 'ReferencePath' and either 'on' or 'off'.

TrajectoryColor - Trajectory color display option
'velocity' (default) | 'acceleration' | 'cost' | 'none'
Trajectory color display option, specified as the comma-separated pair consisting of 'TrajectoryColor' and one of the following:

- 'acceleration'
- 'cost'
- 'velocity'
- 'none'

Set this property to display the specified trajectory as a color-gradient along the specified path.

## Output Arguments

## axHandle - Axes handle used to plot trajectory

Axes object | UIAxes object
Axes handle used to plot trajectory, returned as either an axes, or uiaxes object.

## See Also

trajectory0ptimalFrenet|plan
Introduced in R2019b

## timescope

Display time-domain signals

## Description

The timescope object displays signals in the time domain.


Stopped
$T=0.125000$
Scope features:

- "Data Cursors" - Measure signal values using vertical and horizontal cursors.
- "Signal Statistics" - Display the maximum, minimum, peak-to-peak difference, mean, median, and RMS values of a selected signal.
- "Peak Finder" - Find maxima, showing the $x$-axis values at which they occur.
- "Bilevel Measurements" - Measure transitions, overshoots, undershoots, and cycles.
- "Triggers" - Set triggers to sync repeating signals and pause the display when events occur.

Use "Object Functions" on page 2-1407 to show, hide, and determine visibility of the scope window.
You can enable these measurements either programmatically or on the scope UI. For more details, see "Measurements" on page 2-1403.

## Creation

## Syntax

scope = timescope
scope = timescope(Name=Value)

## Description

scope $=$ timescope returns a timescope object, scope. This object displays real- and complexvalued floating and fixed-point signals in the time domain.
scope $=$ timescope(Name=Value) returns a timescope object with properties set to the specified value. You can specify name-value pair arguments in any order.

## Properties

Most properties can be changed from the timescope UI.

## Frequently Used

## SampleRate - Sample rate of inputs

1 (default) | finite numeric scalar | vector
Sampling rate of the input signal, in hertz, specified as a finite numeric scalar or vector of scalars.
The inverse of the sample rate determines the $x$-axis (time axis) spacing between points in the displayed signal. When the value of NumInputPorts is greater than 1 and the sample rate is scalar, the object uses the same sample rate for all inputs. To specify different sample rates for each input, use a vector.

You can only set this property when creating the object or after calling release.

## Scope Window Use

On the Scope tab, click Settings. Under Data and Axes, set Sample Rate.
Data Types: single | double | int8| int16|int32|int64|uint8|uint16|uint32|uint64

## TimeSpanSource - Source of time span

"auto" (default) | "property"
Source of the time span for frame-based input signals, specified as one of the following:

- "property" - The object derives the $x$-axis limits from the TimeDisplayOffset and TimeSpan properties.
- "auto" - The $x$-axis limits are derived from the TimeDisplayOffset property, SampleRate property, and the number of rows in each input signal (FrameSize in the equations below). The limits are calculated as:
- Minimum time-axis limit = TimeDisplay0ffset
- Maximum time-axis limit = TimeDisplayOffset $+\max (1 /$ SampleRate.*FrameSize)


## Dependency

When you set the TimeSpan property, TimeSpanSource is automatically set to "property".

## Scope Window Use

On the Scope tab, click Settings. Under Data and Axes, set Time Span.
Data Types: char|string
TimeSpan - Time span
10 (default) | positive scalar
Time span, in seconds, specified as a positive, numeric scalar value. The time-axis limits are calculated as:

- Minimum time-axis limit = TimeDisplay0ffset
- Maximum time-axis limit = TimeDisplay0ffset + TimeSpan


## Dependencies

To enable this property, set TimeSpanSource to "property".

## Scope Window Use

On the Scope tab, click Settings. Under Data and Axes, edit Time Span.
Data Types: single|double|int8|int16|int32|int64|uint8|uint16|uint32|uint64
TimeSpanOverrunAction - Data overrun behavior
"scroll" (default) | "wrap"
Specify how the scope displays new data beyond the visible time span as either:

- "scroll" - In this mode, the scope scrolls old data to the left to make room for new data on the right of the scope display. This mode is beneficial for debugging and monitoring time-varying signals.
- "wrap" - In this mode, the scope adds data to the left of the plot after overrunning the right of the plot.


## Scope Window Use

On the Scope tab, click Settings. Under Data and Axes, set Overrun Action.
Data Types: char|string

## PlotType - Type of plot

"line" (default) | "stairs"
Type of plot, specified as either:

- "line" - Line graph, similar to the line or plot function.
- "stairs" - Stair-step graph, similar to the stairs function. Stair-step graphs are useful for drawing time history graphs of digitally sampled data.


## Scope Window Use

On the Scope tab, click Settings. Under Data and Axes, set Plot Type.

## Data Types: char | string

## AxesScaling - Axes scaling mode

"onceatstop" (default) | "auto" | "manual"| "updates"
When this property is set to:

- "onceatstop" -- The limits are updated once at the end of the simulation (when release is called).
- "auto" -- The scope attempts to always keep the data in the display while minimizing the number of updates to the axes limits.
- "manual" -- The scope takes no action unless specified by the user.
- "updates" -- The scope scales the axes once after a set number of visual updates. The number of updates is determined by the value of the AxesScalingNumUpdates property.

You can set this property only when creating the object.
Data Types: char|string

## AxesScalingNumUpdates - Number of updates before scaling

100 (default) | real positive integer
Specify the number of updates before scaling as a real, positive scalar integer.

## Dependency

To enable this property, set AxesScaling to "updates".
Data Types: double

## Advanced

## LayoutDimensions - Display layout grid dimensions

[1,1] (default)| [numberOfRows, numberOfColumns]
Specify the layout grid dimensions as a two-element vector: [numberOfRows, numberOfColumns]. The grid can have a maximum of 4 rows and 4 columns.

If you create a grid of multiple axes, to modify the settings of individual axes, use the ActiveDisplay.
Example: scope.LayoutDimensions $=[2,4]$

## Scope Window Use

On the Scope tab, click Display Grid $\square$ ) and select a specific number of rows and columns from the grid.
Data Types: single | double | int8| int16|int32|int64|uint8|uint16|uint32|uint64

## TimeUnits - Units of x -axis <br> "seconds" (default) | "none" | "metric"

Specify the units used to describe the x -axis (time axis). You can select one of the following options:

- "seconds" -The scope always displays the units on the x -axis as seconds. The scope shows the word Time(s) on the x-axis.
- "none" - The scope does not display any units on the x-axis. The scope only shows the word Time on the x-axis.
- "metric" - The scope displays the units on the x -axis as Time ( s ) changing the units to day, weeks, months, or years as you plot more data points.


## Scope Window Use

On the Scope tab, click Settings. Under Data and Axes, set Time Units.
Data Types: char | string

## TimeDisplayOffset - Offset $\boldsymbol{x}$-axis limits

0 (default) | scalar | vector
Specify, in seconds, how far to move the data on the $x$-axis. The signal value does not change, only the limits displayed on the $x$-axis change.

If you specify this property as a scalar, then that value is the time display offset for all channels. If you specify this property as a vector, each input channel can be a different time display offset

## Scope Window Use

On the Scope tab, click Settings. Under Data and Axes, set Time Offset.

## TimeAxisLabels - Time-axis labels

"all" (default) | "bottom" | "none"
Time-axis labels, specified as:

- "all" - Time-axis labels appear in all displays.
- "bottom" - Time-axis labels appear in the bottom display of each column.
- "none" - No labels appear in any display.


## Scope Window Use

On the Scope tab, click Settings. Under Data and Axes, set Time Labels.

## Data Types: char | string

## MaximizeAxes - Maximize axes control

"auto" (default) | "on" | "off"
Specify whether to display the scope in the maximized-axes mode. In this mode, the axes are expanded to fit into the entire display. To conserve space, labels do not appear in each display. Instead, the tick-marks and their values appear on top of the plotted data. You can select one of the following options:

- "auto" - The axes appear maximized in all displays only if the Title and YLabel properties are empty for every display. If you enter any value in any display for either of these properties, the axes are not maximized.
- "on" - The axes appear maximized in all displays. Any values entered into the Title and YLabel properties are hidden.
- "off" - None of the axes appear maximized.


## Scope Window Use

On the scope window, click on to maximize axes, hiding all labels and insetting the axes values.
Data Types: char \| string
BufferLength - Buffer length
50000 (default) | positive integer
Specify the length of the buffer used for each input signal as a positive integer.
You can set this property only when creating the object.

## Scope Window Use

On the Scope tab, click Settings. Under Data and Axes, set Buffer Length.
Data Types: single | double | int8| int16|int32|int64|uint8|uint16|uint32|uint64

## Measurements

MeasurementChannel - Channel for which to obtain measurements
1 (default) | positive integer
Channel for which to obtain measurements, specified as a positive integer in the range [ 1 N ], where $N$ is the number of input channels.

## Scope Window Use

Click the Measurements tab on the Time Scope toolstrip. In the Channel section, select a Channel.
Data Types: double

## BilevelMeasurements - Bilevel measurements

BilevelMeasurementsConfiguration object
Bilevel measurements to measure transitions, aberrations, and cycles of bilevel signals, specified as a BilevelMeasurementsConfiguration object.

All BilevelMeasurementsConfiguration properties are tunable.

## Scope Window Use

Click the Measurements tab on the Time Scope toolstrip, and modify the bilevel measurements in the Bilevel section.

## CursorMeasurements - Cursor measurements

CursorMeasurementsConfiguration object
Cursor measurements to display screen or waveform cursors, specified as a CursorMeasurementsConfiguration object.

All CursorMeasurementsConfiguration properties are tunable.

## Scope Window Use

Click the Measurements tab on the Time Scope toolstrip and modify the cursor measurements in the Cursors section.

PeakFinder - Peak finder measurements
PeakFinderConfiguration object
Peak finder measurements to compute and display the largest calculated peak values, specified as a PeakFinderConfiguration object.

All PeakFinderConfiguration properties are tunable.

## Scope Window Use

Click the Measurements tab on the Time Scope toolstrip and modify the peak finder measurements in the Peaks section.

## SignalStatistics - Signal statistics measurements

SignalStatisticsConfiguration object
Signal statistics measurements to compute and display signal statistics, specified as a SignalStatisticsConfiguration object.

All SignalStatisticsConfiguration properties are tunable.

## Scope Window Use

Click the Measurements tab on the Time Scope toolstrip and modify the signal statistics measurements in the Statistics section.

## Trigger - Trigger measurements

TriggerConfiguration object
Trigger measurements, specified as a TriggerConfiguration object. Define a trigger event to identify the simulation time of specified input signal characteristics. You can use trigger events to stabilize periodic signals such as a sine wave or capture non-periodic signals such as a pulse that occurs intermittently.

All TriggerConfiguration properties are tunable.

## Scope Window Use

Click the Trigger tab on the Time Scope toolstrip and modify the trigger settings.

## Visualization

## Name - Window name

"Time Scope" (default) | character vector \| string scalar
Specify the name of the scope as a character vector or string scalar. This name appears as the title of the scope's figure window. To specify a title of a scope plot, use the Title property.
Data Types: char | string

## Position - Window position

screen center (default)|[left bottom width height]

Scope window position in pixels, specified by the size and location of the scope window as a fourelement vector of the form [left bottom width height]. You can place the scope window in a specific position on your screen by modifying the values of this property.

By default, the window appears in the center of your screen with a width of 800 pixels and height of 500 pixels. The exact values of the position depend on your screen resolution.

## ChannelNames - Channel names

\{' ' $\}$ (default) | cell array of character vectors
Specify the input channel names as a cell array of character vectors. The channel names appear in the legend, and on the Measurements tab under Select Channel. If you do not specify names, the channels are labeled as Channel 1, Channel 2, etc.

## Dependency

To enable this property, set ShowLegend to true.

## Data Types: char

## ActiveDisplay - Active display for setting properties

1 (default) | integer
Active display used to set properties, specified by the integer display number. The number of a display corresponds to the display's row-wise placement index. Setting this property controls which display is used for the following properties: YLimits, YLabel, ShowLegend, ShowGrid, Title, and PlotAsMagnitudePhase.

## Scope Window Use

On the Scope tab, click Settings. Under Display and Labels, set Active Display.

## Title - Display title

' ' (default) | character vector | string scalar
Specify the display title as a character vector or a string scalar.

## Dependency

When you set this property, ActiveDisplay controls the display that is updated.

## Scope Window Use

On the Scope tab, click Settings. Under Display and Labels, set Title.
Data Types: char \| string
YLabel - $\boldsymbol{y}$-axis label
"Amplitude" (default) | character vector | string scalar
Specify the text for the scope to display to the left of the $y$-axis.

## Dependencies

This property applies only when PlotAsMagnitudePhase is false. When PlotAsMagnitudePhase is true, the two $y$-axis labels are read-only values "Magnitude" and "Phase", for the magnitude plot and the phase plot, respectively.

When you set this property, ActiveDisplay controls the display that is updated.

## Scope Window Use

On the Scope tab, click Settings. Under Display and Labels, set YLabel.
Data Types: char|string

## YLimits - $\boldsymbol{y}$-axis limits

[-10, 10] (default) | [ymin, ymax]
Specify the $y$-axis limits as a two-element numeric vector, [ymin, ymax].

- If PlotAsMagnitudePhase is false, the default is [-10,10].
- If PlotAsMagnitudePhase is true, the default is [0,10]. This property specifies the y-axis limits of only the magnitude plot. The $y$-axis limits of the phase plot are always [-180, 180]


## Dependency

When you set this property, ActiveDisplay controls the display that is updated.

## Scope Window Use

On the Scope tab, click Settings. Under Display and Labels, set Y-Axis Limits.

## ShowLegend - Show legend

false (default) | true
To show a legend with the input names, set this property to true.
From the legend, you can control which signals are visible. In the scope legend, click a signal name to hide the signal in the scope. To show the signal, click the signal name again.

## Scope Window Use

On the Scope tab, click Settings. Under Display and Labels, select Show Legend.
Data Types: logical

## ShowGrid - Grid visibility

true (default) | false
Set this property to true to show grid lines on the plot.

## Scope Window Use

On the Scope tab, click Settings. Under Display and Labels, select Show Grid.

## PlotAsMagnitudePhase - Plot signal as magnitude and phase

false (default) | true
Plot signal as magnitude and phased, specified as either:

- true - The scope plots the magnitude and phase of the input signal on two separate axes within the same active display.
- false - The scope plots the real and imaginary parts of the input signal on two separate axes within the same active display.

This property is useful for complex-valued input signals. Turning on this property affects the phase for real-valued input signals. When the amplitude of the input signal is nonnegative, the phase is 0 degrees. When the amplitude of the input signal is negative, the phase is 180 degrees.

## Scope Window Use

On the Scope tab, click Settings. Under Display and Labels, select Magnitude Phase Plot.

## Object Functions

To use an object function, specify the object as the first input argument.

| hide | Hide scope window |
| :--- | :--- |
| show | Display scope window |
| isVisible | Determine visibility of scope |
| generateScript | Generate MATLAB script to create scope with current settings |
| step | Run System object algorithm |
| release | Release resources and allow changes to System object property values and input <br> characteristics |
| reset | Reset internal states of System object |

If you want to restart the simulation from the beginning, call reset to clear the scope window displays. Do not call reset after calling release.

## Examples

## View Sine Wave on Time Scope

Create a time-domain sinusoidal signal. Display the signal by calling the time scope object.
Create a sinusoidal signal with two tones, one at 0.3 kHz and the other at 3 kHz .

```
t = (0:1000)'/8e3;
xin = sin(2*pi*0.3e3*t)+sin(2*pi*3e3*t);
```

Create a timescope object and view the sinusoidal signal by calling the time scope object scope.

```
scope = timescope(SampleRate=8e3,...
    TimeSpanSource="property",...
    TimeSpan=0.1);
scope(xin)
```



Run release to allow changes to property values and input characteristics. The scope automatically scales the axes.
release(scope);

Hide the scope window.
if(isVisible(scope)) hide(scope)
end
Show the scope window.
if(~isVisible(scope))
show(scope)
end


Stopped

Use Bilevel Measurements Panel with Clock Input Signal
Create and Display Clock Input Signal
Load the clock data, $x$ and $t$. Find the sample time, $t s$.
load clockex
ts = t(2)-t(1);
Create a timescope object and call the object to display the signal. To autoscale the axes and enable changes to property values and input characteristics, call release.

```
scope = timescope(SampleRate=1/ts,TimeSpanSource="Auto");
```

scope(x);
release(scope);


Stopped
Use Bilevel Measurements Panel to Find Settling Time

1. From the Measurements tab, select Aberrations.


Initially, the Time Scope does not display the Settling Time measurement. This absence occurs because the default value of the Settle Seek parameter is longer than the entire simulation duration.
2. In the Bilevel Settings > Settle Seek box, enter 2e-6 and press Enter.


Time Scope now displays a rising edge Settling Time value of 118.392 ns .
This settling time value is actually the statistical average of the settling times for all five rising edges. To show the settling time for only one rising edge, you can zoom in on that transition.
3. Hover over the upper right corner of the scope axes, and click the zoom button.
4. Click and drag to zoom in on one of the transitions.


Time Scope updates the rising edge Settling Time value to reflect the new time window.

## Configure Bilevel Measurements Programmatically in Time Scope MATLAB Object

Create a sine wave and view it in the Time Scope. Programmatically compute the bilevel measurements related to signal transitions, aberrations, and cycles.

## Initialization

Create the input sine wave using the sin function. Create a timescope MATLAB® object to display the signal. Set the TimeSpan property to 1 second.
f = 100;
fs = 1000;
swv = sin(2.*pi.*f.*(0:1/fs:1-1/fs)).';
scope $=$ timescope(SampleRate=fs,... TimeSpanSource="property", ... TimeSpan=1);

## Transition Measurements

Enable the scope to show transition measurements programmatically by setting the ShowTransitions property to true. Display the sine wave in the scope.

Transition measurements such as rise time, fall time, and slew rate appear in the Transitions panel at the bottom of the scope.

```
scope.BilevelMeasurements.ShowTransitions = true;
scope(swv);
release(scope);
```



Transitions

| Channel 1 | Count | Rise Time (s) | Fall Time (s) | Slew Rate (ls) |
| :--- | :--- | :--- | :--- | :--- |
| + Edges |  |  |  |  |
| - Edges |  |  |  |  |
| Stopped |  |  | Frames = $1 \mathrm{~T}=0.999000$ |  |

## Aberration Measurements

Enable the scope to show aberration measurements programmatically by setting the ShowAberrations property to true. Display the sine wave in the scope.

Aberration measurements such as preshoot, overshoot, undershoot, and settling time appear in the Aberrations panel at the bottom of the scope.
scope.BilevelMeasurements. ShowAberrations = true;
scope(swv);
release(scope);


## Cycle Measurements

Enable the scope to show cycles measurements programmatically by setting the ShowCycles property to true. Display the sine wave in the scope.

Cycle measurements such as period, frequency, pulse width, and duty cycle appear in the Cycles panel at the bottom of the scope.
scope.BilevelMeasurements.ShowCycles = true;
scope(swv);
release(scope);


## Configure Signal Statistics Programmatically in Time Scope MATLAB Object

Create a sine wave and view it in the Time Scope. Enable the scope programmatically to compute the signal statistics.

The object supports the following statistics measurements:

- Maximum
- Minimum
- Mean
- Median
- RMS
- Peak to peak
- Variance
- Standard deviation
- Mean square


## Initialization

Create the input sine wave using the sin function. Create a timescope MATLAB® object to display the signal. Set the TimeSpan property to 1 second.

```
f = 100;
fs = 1000;
swv = sin(2.*pi.*f.*(0:1/fs:1-1/fs)).';
scope = timescope(SampleRate=fs,...
    TimeSpanSource="property", ...
    TimeSpan=1);
```


## Signal Statistics

Enable the scope to show signal statistics programmatically by setting the SignalStatistics > Enabled property to true.
scope.SignalStatistics.Enabled = true;
By default, the scope enables the following measurements.

```
scope.SignalStatistics
ans =
    SignalStatisticsConfiguration with properties:
                            ShowMax: 1
                    ShowMin: 1
            ShowPeakToPeak: 1
                            ShowMean: 1
                ShowVariance: 0
        ShowStandardDeviation: 1
            ShowMedian: 1
                            ShowRMS: 1
            ShowMeanSquare: 0
                    Enabled: 1
```

Display the sine wave in the scope. A Statistics panel appears at the bottom and displays the statistics for the portion of the signal that you can see in the scope.

```
scope(swv);
release(scope);
```



Statistics

| Channel 1 | Max | Min | Peak to Peak | Mean | Standard De... | Median |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Time $(\mathrm{ms})$ | $9.5300 \mathrm{e}+2$ | $9.3700 \mathrm{e}+2$ |  |  |  |  |
| Value | $9.5106 \mathrm{e}-1$ | $-9.5106 \mathrm{e}-1$ | $1.9021 \mathrm{e}+0$ | $9.5201 \mathrm{e}-4$ | $7.0717 \mathrm{e}-1$ | $1.2246 \mathrm{e}-16$ |

Stopped

If you use the zoom options on the scope, the statistics automatically adjust to the time range shown in the display.

## Visualize Multiple Inputs with Different Sample Rates

This example shows how to visualize multiple inputs with different sample rates and plot the signals on multiple axes.

Generate three different sine waves and plot them on the timescope.
freq $=1 / 500 ;$
$\mathrm{t}=(0: 100) \cdot / \mathrm{freq}$;
t2 $=(0: 0.5: 100)$ '/freq;
$x i n 1=\sin (1 / 2 * t)$;
xin2 $=\sin (1 / 4 * t 2)$;
xin $=\sin (1 / 2 * \mathrm{t} 2)+\sin (1 / 4 * \mathrm{t} 2)$;
scope $=$ timescope(SampleRate=[freq freq/2 freq],...
TimeSpanSource="property", ...
TimeSpan=0.1,...
LayoutDimensions=[2,1]);
scope(xin,xin1,xin2)
release(scope)


## Use Multiple Axes on Scope

This example show how to add titles, set $y$-axis limits, and modify properties when you have multiple axes on your timescope object.

Use the timescope to visualize three sine waves with two different sample rates.

```
freq = 1;
t = (0:100)'/freq;
t2 = (0:0.5:100)'/freq;
xin1 = sin(1/2*t);
xin2 = sin(1/4*t2);
xin = sin(1/2*t2)+sin(1/4*t2);
scope = timescope(SampleRate=[freq freq/2 freq],...
    TimeSpanSource="property",...
    TimeSpan=100);
scope(xin, xin1, xin2)
```



Change the layout to add a second axis. The second and third inputs automatically move to the new second axis.
scope.LayoutDimensions = [2,1];


Modify the settings for the first axis by specifying the ActiveDisplay property to 1 , then changing some properties for that axis.

```
scope.ActiveDisplay = 1;
scope.ShowGrid = false;
scope.Title = "Sine Wave 1";
scope.YLimits = [-2,2];
```

Repeat this process to modify the second axis.
scope.ActiveDisplay = 2;
scope.Title = "Sine Waves 2 \& 3";
scope.YLimits = [-1,1];
release(scope)


## View Sine Wave Input Signals at Different Sample Rates and Offsets

Create a dsp. SineWave object. Create a dsp.FIRDecimator object to decimate the sine wave by 2. Create a timescope object with two input ports.

```
Fs = 1000; % Sample rate
sine = dsp.SineWave(Frequency=50,...
    SampleRate=Fs,...
    SamplesPerFrame=100);
decimate = dsp.FIRDecimator; % To decimate sine by 2
scope = timescope(SampleRate=[Fs Fs/2],...
    TimeDisplayOffset=[0 38/Fs],...
    TimeSpanSource="Property",...
    TimeSpan=0.25,...
    YLimits=[-1 1],...
    ShowLegend=true);
```

Call the dsp. SineWave object to create a sine wave signal. Use the dsp.FIRDecimator object to create a second signal that equals the original signal, but decimated by a factor of 2. Display the signals by calling the timescope object.

```
for ii = 1:2
    xsine = sine();
    xdec = decimate(xsine);
```

```
        scope(xsine,xdec)
end
release(scope)
```



Close the Time Scope window and clear the variables.
clear scope Fs sine decimate ii xsine xdec

## Display Complex-Valued Input Signal

Create a vector representing a complex-valued sinusoidal signal, and create a timescope object. Call the scope to display the signal.
fs = 1000;
t = (0:1/fs:10)';
CxSine $=\cos (2 * \mathrm{pi} * 0.2 * \mathrm{t})+1 \mathrm{i}^{*} \sin (2 * \mathrm{pi} * 0.2 * \mathrm{t})$;
CxSineSum = cumsum(CxSine);
scope $=$ timescope(SampleRate=fs,...
TimeSpanSource="Auto", ShowLegend=1);
scope(CxSineSum);
release(scope)


By default, when the input is a complex-valued signal, Time Scope plots the real and imaginary portions on the same axes. These real and imaginary portions appear as different-colored lines on the same axes within the same active display.

Change the PlotAsMagnitudePhase property to true and call release.
scope.PlotAsMagnitudePhase $=$ true;
scope(CxSineSum);
release(scope)


Time Scope now plots the magnitude and phase of the input signal on two separate axes within the same active display. The top axes display magnitude and the bottom axes display the phase, in degrees.

## Display Input Signal of Changing Size

This example shows how the timescope object visualizes inputs that change dimensions halfway through.

Create a vector that represents a two-channel constant signal. Create another vector that represents a three-channel constant signal. Create a timescope object. Call the scope with two inputs to display the signal.

```
fs = 10;
sigdim2 = [ones(5*fs,1) 1+ones(5*fs,1)]; % 2-dim 0-5 s
sigdim3 = [2+ones(5*fs,1) 3+ones(5*fs,1) 4+ones(5*fs,1)]; % 3-dim 5-10 s
scope = timescope(SampleRate=fs,TimeSpanSource="Property");
scope.PlotType = "Stairs";
scope.TimeSpanOverrunAction = "Scroll";
scope.TimeDisplayOffset = [0 5];
scope([sigdim2; sigdim3(:,1:2)], sigdim3(:,3));
```



Processing
Frames $=1 \mathrm{~T}=9.90000$
In this example, the size of the input signal to the Time Scope changes as the simulation progresses. When the simulation time is less than 5 seconds, Time Scope plots only the two-channel signal, sigdim2. After 5 seconds, Time Scope also plots the three-channel signal, sigdim3.

Run the release method to enable changes to property values and input characteristics. The scope automatically scales the axes.
release(scope)


Stopped

Find Heart Rate Using Peak Finder Panel with ECG Input Signal
Use Peak Finder panel of the Time Scope to measure a heart rate.

## Create and Display ECG Signal

Create the electrocardiogram (ECG) signal. The custom ecg function helps generate the heartbeat signal.

```
function x = ecg(L)
a0 = [0, 1, 40, 1, 0, -34, 118, -99, 0, 2, 21, 2, 0, 0, 0];
d0 = [0, 27, 59, 91, 131, 141, 163, 185, 195, 275, 307, 339, 357, 390, 440];
a = a0 / max(a0);
d = round(d0 * L / d0(15));
d(15) = L;
for i = 1:14
    m = d(i) : d(i+1) - 1;
    slope = (a(i+1) - a(i)) / (d(i+1) - d(i));
    x(m+1) = a(i) + slope * (m - d(i));
end
x1 = 3.5*ecg(2700).';
y1 = sgolayfilt(kron(ones(1,13),x1),0,21);
```

```
n = (1:30000)';
del = round(2700*rand(1));
mhb = yl(n + del);
ts = 0.00025;
```

Create a timescope object and call the object to display the signal. To autoscale the axes and enable changes to property values and input characteristics, call release.
scope = timescope(SampleRate=1/ts);
scope(mhb);
release(scope)


Find Heart Rate
Use the Peak Finder measurements to measure the time between heart beats.
1 On the Measurements tab, select Peak Finder.
2 For the Num Peaks property, enter 10.
In the Peaks pane at the bottom of the window, the Time Scope displays a list of ten peak amplitude values and the times at which they occur.


Processing
The list of peak values shows a constant time difference of 0.675 second between each heartbeat. Based on the following equation, the heart rate of this ECG signal is about 89 beats per minute.

$$
\frac{60 \mathrm{~s} / \mathrm{min}}{0.675 \mathrm{~s} / \mathrm{beat}}=88.89 \mathrm{bpm}
$$

Close the Time Scope window and remove the variables you created from the workspace.
clear scope x1 yl n del mhb ts

## Tips

- To close the scope window and clear its associated data, use the MATLAB clear function.
- To hide or show the scope window, use the hide and show functions.
- Use the MATLAB mcc function to compile code containing a scope. You cannot open scope configuration dialogs if you have more than one compiled component in your application.


## See Also

Topics
"Configure Time Scope MATLAB Object"

## Introduced in R2020a

## generateScript

Generate MATLAB script to create scope with current settings

## Syntax

generateScript(scope)

## Description

generateScript(scope) generates a MATLAB script that can re-create a timescope object with the current settings in the scope.

## Examples

## Generate Script from timescope

Generate MATLAB script after making changes to the timescope object in the scope window.

Note The script only generates commands for settings that are available from the command line, applicable to the current visualization, and changed from the default value.

1 Create a timescope object.
scope = timescope; show(scope)
2 Set options in the Time Scope. For this example, on the Scope tab, click Settings. Under Display and Labels, select Show Legend and Magnitude Phase Plot. Set the Title as well.


3 Generate a script to recreate the timescope with the same modified settings. Either select Generate Script from the Scope tab, or enter:

```
generateScript(scope);
```

A new editor window opens with code to regenerate the same scope.
\% Creation Code for 'timescope'.
\% Generated by Time Scope on 8-Nov-2019 13:51:54 -0500.
timeScope = timescope('Position',[2286 355800 500], ...
'Title','My Time Scope', ...
'ShowLegend', true, .
'PlotAsMagnitudePhase', true) ;

## Input Arguments

scope - object
timescope object
Object whose settings you want to recreate with a script.

## See Also

## Functions

hide | show \| isVisible

```
Objects
timescope
```

Introduced in R2020a

## hide

Hide scope window

## Syntax

hide(scope)

## Description

hide(scope) hides the scope window.

## Examples

## View Sine Wave on Time Scope

Create a time-domain sinusoidal signal. Display the signal by calling the time scope object.
Create a sinusoidal signal with two tones, one at 0.3 kHz and the other at 3 kHz .
$t=(0: 1000) \cdot / 8 e 3 ;$
$x$ in $=\sin \left(2 *\right.$ pi $\left.^{*} 0.3 e 3 * t\right)+\sin (2 *$ pi*3e3*t);
Create a timescope object and view the sinusoidal signal by calling the time scope object scope.

```
scope = timescope(SampleRate=8e3,...
    TimeSpanSource="property",...
    TimeSpan=0.1);
scope(xin)
```



Processing

Run release to allow changes to property values and input characteristics. The scope automatically scales the axes.
release(scope);

Hide the scope window.
if(isVisible(scope)) hide(scope)
end
Show the scope window.
if(~isVisible(scope))
show(scope)
end


Stopped

## Input Arguments

scope - Scope object
timescope object
Scope object whose window you want to hide, specified as a timescope object.
Example: myScope = timescope; hide(myScope)

## See Also

## Functions

show|isVisible|generateScript
Objects
timescope

Introduced in R2020a

## isVisible

Determine visibility of scope

## Syntax

visibility = isVisible(scope)

## Description

visibility = isVisible(scope) returns the visibility of the scope as logical, with 1 (true) for visible.

## Examples

## View Sine Wave on Time Scope

Create a time-domain sinusoidal signal. Display the signal by calling the time scope object.
Create a sinusoidal signal with two tones, one at 0.3 kHz and the other at 3 kHz .

```
t = (0:1000)'/8e3;
xin = sin(2*pi*0.3e3*t)+sin(2*pi*3e3*t);
```

Create a timescope object and view the sinusoidal signal by calling the time scope object scope.

```
scope = timescope(SampleRate=8e3,...
    TimeSpanSource="property",...
    TimeSpan=0.1);
scope(xin)
```



Run release to allow changes to property values and input characteristics. The scope automatically scales the axes.
release(scope);

Hide the scope window.
if(isVisible(scope)) hide(scope)
end
Show the scope window.
if(~isVisible(scope))
show(scope)
end


Stopped
Frames = $1 \mathrm{~T}=0.125000$

## Input Arguments

scope - Scope object
timescope object
Scope object whose visibility you want to query.
Example: myScope = timescope; visibility = isVisible(myScope)

## Output Arguments

visibility - Scope visibility
1|0
If the scope window is open, the isVisible function returns 1 (true). Otherwise, the function returns 0 (false).

## See Also

## Functions

hide |show|generateScript

Objects
timescope

Introduced in R2020a

## show

Display scope window

## Syntax

show(scope)

## Description

show(scope) shows the scope window.

## Examples

## View Sine Wave on Time Scope

Create a time-domain sinusoidal signal. Display the signal by calling the time scope object.
Create a sinusoidal signal with two tones, one at 0.3 kHz and the other at 3 kHz .
$\mathrm{t}=(0: 1000) \mathrm{C} / 8 \mathrm{e} 3$;
xin $=\sin \left(2 *\right.$ pi $\left.^{*} 0.3 e 3 * t\right)+\sin \left(2 *\right.$ pi $\left.^{*} 3 \mathrm{e} 3 * \mathrm{t}\right)$;
Create a timescope object and view the sinusoidal signal by calling the time scope object scope.

```
scope = timescope(SampleRate=8e3,...
    TimeSpanSource="property",...
    TimeSpan=0.1);
scope(xin)
```



Run release to allow changes to property values and input characteristics. The scope automatically scales the axes.
release(scope);


Stopped

Hide the scope window.
if(isVisible(scope)) hide(scope)
end
Show the scope window.
if(~isVisible(scope))
show(scope)
end


Stopped

## Input Arguments

scope - Scope object
timescope object
Scope object whose window you want to show, specified as a timescope object.
Example: myScope = timescope; show(myScope)

## See Also

## Functions

hide |isVisible|generateScript
Objects
timescope
Introduced in R2020a

## BilevelMeasurementsConfiguration

Measure transitions, aberrations, and cycles of bilevel signals

## Description

Use the BilevelMeasurementsConfiguration object to measure transitions, aberrations, and cycles of bilevel signals. You can also specify the bilevel settings such as high-state level, low-state level, state-level tolerance, upper-reference level, mid-reference level, and lower-reference level.

You can control bilevel measurements from the toolstrip or from the command line. To modify bilevel measurements from the scope interface, click the Measurements tab and enable the settings in the Bilevel section. A panel appears at the bottom of the Time Scope window showing all the measurements you enabled.


| Transitions |  | Aberrations |  | Cycles |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Channel 1 | Period (ms) | Frequency (Hz) | Count | Width (ms) | Duty Cycle (\%) |
| + Pulses | 1.0000e+1 | 1.0000e+2 | 99.0000 | 5.0000e+0 | 50.6000 |
| - Pulses | 1.0000e+1 | 1.000ee+2 | 99.0000 | 5.0000e+0 | 50.0000 |

## Creation

## Syntax

bilevelMeas = BilevelMeasurementsConfiguration()

## Description

bilevelMeas = BilevelMeasurementsConfiguration() creates a bilevel measurements configuration object.

## Properties

All properties are tunable.

## AutoStateLevel - Automatic detection of high- and low-state levels <br> true (default) | false

Automatic detection of high- and low-state levels, specified as true or false. Set this property to true so that the scope automatically detects high- and low-state levels in the bilevel waveform. When you set this property to false, you can specify values for the high- and low- state levels manually using the HighStateLevel and LowStateLevel properties.

## Scope Window Use

Click the Measurements tab on the Time Scope toolstrip. In the Bilevel section, click Bilevel Settings and select the Auto State Level check box.
Data Types: logical

## HighStateLevel - High-state level

2.3 (default) | nonnegative scalar

High-state level, specified as a nonnegative scalar. The high-state level denotes a positive polarity.
If the initial transition of a pulse is positive-going, the pulse has positive polarity. The terminating state of a positive-polarity (positive-going) pulse is more positive than the originating state.

This figure shows a positive-polarity pulse.


Dependency
To enable this property, set AutoStateLevel to false.

## Scope Window Use

Click the Measurements tab on the Time Scope toolstrip. In the Bilevel section, click Bilevel Settings, clear the Auto State Level check box, and specify High to a nonnegative scalar.
Data Types: double
LowStateLevel - Low-state level
0 (default) | nonnegative scalar
High-state level, specified as a nonnegative scalar. The low-state level denotes a negative polarity.
If the initial transition of a pulse is negative-going, the pulse has negative polarity. The terminating state of a negative-polarity (negative-going) pulse is more negative than the originating state.

This figure shows a negative-polarity pulse.


Dependency
To enable this property, set AutoStateLevel to false.
Scope Window Use
Click the Measurements tab on the Time Scope toolstrip. In the Bilevel section, click Bilevel Settings, clear the Auto State Level check box, and specify Low to a nonnegative scalar.

Data Types: double
StateLevelTolerance - Tolerance level of state
2 (default) | positive scalar in the range (0 100)
Tolerance level of the state, specified as a positive scalar in the range (0 100).

This value determines how much a signal can deviate from the low- or high-state level before it is considered to be outside that state. Specify this value as a percentage of the difference between the high- and low-state levels. For more details, see "State-Level Tolerances" on page 2-1455.

## Scope Window Use

Click the Measurements tab on the Time Scope toolstrip. In the Bilevel section, click Bilevel
Settings, and specify the State Level Tol. (\%) to a positive scalar less than 100.
Data Types: double
UpperReferenceLevel - Upper-reference level
90 (default) | positive scalar in the range (0 100)
Upper-reference level, specified as a positive scalar in the range (0 100). The scope uses the upperreference level to compute the start of a fall time or the end of a rise time. Specify this value as a percentage of the difference between the high- and low-state levels.

If $S_{1}$ is the low-state level, $S_{2}$ is the high-state level, and $U$ is the upper-reference level, the waveform value corresponding to the upper-reference level is

$$
S_{1}+\frac{U}{100}\left(S_{2}-S_{1}\right) .
$$

## Scope Window Use

Click the Measurements tab on the Time Scope toolstrip. In the Bilevel section, click Bilevel Settings, and specify the Upper Ref. Level (\%) to a positive scalar less than 100.

Data Types: double

## MidReferenceLevel - Mid-reference level

50 (default) | positive scalar in the range (0 100)
Mid-reference level, specified as a positive scalar in the range (0 100). The scope uses the midreference level to determine when a transition occurs. Specify this value as a percentage of the difference between the high- and low-state levels.

The mid-reference level in a bilevel waveform with low-state level $S_{1}$ and high-state level $S_{2}$ is

$$
S_{1}+\frac{1}{2}\left(S_{2}-S_{1}\right)
$$

This figure shows the mid-reference level as a horizontal line, and shows its corresponding midreference level instant as a vertical line.


## Scope Window Use

Click the Measurements tab of the Time Scope toolstrip. In the Bilevel section, click Bilevel Settings, and specify the Mid Ref. Level (\%) to a positive scalar less than 100.
Data Types: double

## LowerReferenceLevel - Lower-reference level

10 (default) | positive scalar in the range (0 100)
Lower-reference level, specified as a positive scalar in the range (0 100). The scope uses the lowerreference level to compute the end of a fall time or the start of a rise time. Specify this value as a percentage of the difference between the high- and low-state levels.

If $S_{1}$ is the low-state level, $S_{2}$ is the high-state level, and $L$ is the lower-reference level, the waveform value corresponding to the lower-reference level is

$$
S_{1}+\frac{L}{100}\left(S_{2}-S_{1}\right) .
$$

## Scope Window Use

Click the Measurements tab on the Time Scope toolstrip. In the Bilevel section, click Bilevel Settings, and specify the Lower Ref. Level (\%) to a positive scalar less than 100.
Data Types: double
SettleSeek - Time duration over which to search for a settling time
0.02 (default) | positive scalar

Time duration over which the scope searches for a settling time, specified as a positive scalar in seconds.

## Scope Window Use

Click the Measurements tab on the Time Scope toolstrip. In the Bilevel section, click Bilevel Settings, and specify the Settle Seek (s) to a positive scalar.
Data Types: double

## ShowTransitions - Enable transition measurements

false (default) | true
Enable transition measurements, specified as true or false. For more information on the transition measurements that the scope displays, see "Transitions Pane".

## Scope Window Use

Click the Measurements tab on the Time Scope toolstrip. In the Bilevel section, select Transitions. A Transitions panel opens at the bottom of the Time Scope window to show the transition measurements.

## Data Types: logical

## ShowAberrations - Enable aberration measurements <br> false (default) | true

Enable aberration measurements, specified as true or false. Aberration measurements include distortion and damping measurements such as preshoot, overshoot, and undershoot. For more information on the aberration measurements that the scope displays, see "Overshoots / Undershoots Pane".

## Scope Window Use

Click the Measurements tab on the Time Scope toolstrip. In the Bilevel section, select Aberrations. An Aberrations panel opens at the bottom of the Time Scope window to show the aberration measurements.
Data Types: logical

## ShowCycles - Enable cycle measurements

false (default) | true
Enable cycle measurements, specified as true or false. These measurements are related to repetitions or trends in the displayed portion of the input signal. For more information on the cycle measurements, see "Cycles Pane".

## Scope Window Use

Open the Measurements tab of the Time Scope toolstrip. In the Bilevel section, select Cycles. A Cycle panel opens at the bottom of the Time Scope window and shows the cycle measurements.

Data Types: logical

## Examples

## Configure Bilevel Measurements Programmatically in Time Scope MATLAB Object

Create a sine wave and view it in the Time Scope. Programmatically compute the bilevel measurements related to signal transitions, aberrations, and cycles.

## Initialization

Create the input sine wave using the sin function. Create a timescope MATLAB® object to display the signal. Set the TimeSpan property to 1 second.

```
f = 100;
fs = 1000;
swv = sin(2.*pi.*f.*(0:1/fs:1-1/fs)).';
scope = timescope(SampleRate=fs,...
    TimeSpanSource="property",...
    TimeSpan=1);
```


## Transition Measurements

Enable the scope to show transition measurements programmatically by setting the ShowTransitions property to true. Display the sine wave in the scope.

Transition measurements such as rise time, fall time, and slew rate appear in the Transitions panel at the bottom of the scope.
scope.BilevelMeasurements. ShowTransitions = true;
scope(swv);
release(scope);


Transitions

| Channel 1 | Count | Rise Time (s) | Fall Time (s) | Slew Rate (/s) |
| :--- | :--- | :--- | :--- | :--- |
| + Edges |  |  |  |  |
| - Edges |  |  |  |  |
| Stopped |  | Frames $=1 \quad \mathrm{~T}=0.999000$ |  |  |

## Aberration Measurements

Enable the scope to show aberration measurements programmatically by setting the ShowAberrations property to true. Display the sine wave in the scope.

Aberration measurements such as preshoot, overshoot, undershoot, and settling time appear in the Aberrations panel at the bottom of the scope.
scope.BilevelMeasurements.ShowAberrations = true;
scope(swv);
release(scope);


## Cycle Measurements

Enable the scope to show cycles measurements programmatically by setting the ShowCycles property to true. Display the sine wave in the scope.

Cycle measurements such as period, frequency, pulse width, and duty cycle appear in the Cycles panel at the bottom of the scope.
scope.BilevelMeasurements.ShowCycles = true;
scope(swv);
release(scope);


## More About

## State-Level Tolerances

You can specify lower- and upper-state boundaries for each state level. Define the boundaries as the state level plus or minus a scalar multiple of the difference between the high state and the low state. To provide a useful tolerance region, specify the scalar as a small number such as $2 / 100$ or $3 / 100$. In general, the $\alpha \%$ region for the low state is defined as

$$
S_{1} \pm \frac{\alpha}{100}\left(S_{2}-S_{1}\right),
$$

where $S_{1}$ is the low-state level and $S_{2}$ is the high-state level. Replace the first term in the equation with $S_{2}$ to obtain the $\alpha \%$ tolerance region for the high state.

This figure shows lower and upper 5\% state boundaries (tolerance regions) for a positive-polarity bilevel waveform. The thick dashed lines indicate the estimated state levels.


## See Also

timescope
Topics
"Configure Time Scope MATLAB Object"
Introduced in R2022a

## SignalStatisticsConfiguration

Compute and display signal statistics

## Description

Use the SignalStatisticsConfiguration object to measure signal statistics such as maximum, minimum, peak-to-peak value, mean, variance, standard deviation, median, RMS, and mean square.

You can enable the scope to compute and display signal statistics from the toolstrip or from the command line. To enable from the scope interface, click the Measurements tab, and then click Signal Statistics in the Statistics section. A statistics panel appears at the bottom of the scope window. To enable specific statistics, click the Signal Statistics drop-down list and select a statistic from the options. The Statistics panel shows those statistics.

Time Scope


Statistics

| Channel 1 | Max | Min | Peak to P... | Mean | Variance | Standard ... | Median | RMS | Mean Squ... |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Time (ms) | $9.5300 \mathrm{e}+2$ | $9.3700 \mathrm{e}+2$ |  |  |  |  |  |  |  |
| Value | $9.5106 \mathrm{e}-1$ | $-9.5106 \mathrm{e}-1$ | $1.9021 \mathrm{e}+6$ | $9.5201 \mathrm{e}-4$ | $5.0009 \mathrm{e}-1$ | $7.0717 \mathrm{e}-1$ | $1.2246 \mathrm{e}-16$ | $7.0682 \mathrm{e}-1$ | $4.9960 \mathrm{e}-1$ |

Stopped

## Creation

## Syntax

signalStats $=$ SignalStatisticsConfiguration()
Description
signalStats = SignalStatisticsConfiguration() creates a signal statistics configuration object signalStats.

## Properties

All properties are tunable.

## ShowMax - Compute and display maximum

true (default) | false
Compute and display the maximum value, specified as true or false. The scope computes and displays the maximum value of the portion of the input signal that is currently on display in the scope.

## Scope Window Use

Click the Measurements tab on the scope toolstrip. In the Statistics section, click the Signal Statistics drop-down arrow, and select Max.
Data Types: logical
ShowMin - Compute and display minimum
true (default) | false
Compute and display the minimum value, specified as true or false. The scope computes and displays the minimum value of the portion of the input signal that is currently on display in the scope.

## Scope Window Use

Click the Measurements tab on the scope toolstrip. In the Statistics section, click the Signal Statistics drop-down arrow, and select Min.
Data Types: logical

## ShowPeakToPeak - Compute and display peak-to-peak values <br> true (default) | false

Compute and display the peak-to-peak values, specified as true or false. The scope computes and displays the peak-to-peak values from the portion of the input signal that is currently on display in the scope.

## Scope Window Use

Click the Measurements tab on the scope toolstrip. In the Statistics section, click the Signal Statistics drop-down arrow, and select Peak to Peak.
Data Types: logical

## ShowMean - Compute and display mean

## true (default) | false

Compute and display the mean value, specified as true or false. The scope computes and displays the mean value of the portion of the input signal that is currently on display in the scope.

## Scope Window Use

Click the Measurements tab on the scope toolstrip. In the Statistics section, click the Signal Statistics drop-down arrow, and select Mean.
Data Types: logical

## ShowVariance - Compute and display variance <br> false (default) | true

Compute and display the variance, specified as true or false. The scope computes and displays the variance of the portion of the input signal that is currently on display in the scope.

## Scope Window Use

Click the Measurements tab on the scope toolstrip. In the Statistics section, click the Signal Statistics drop-down arrow, and select Variance.
Data Types: logical

## ShowStandardDeviation - Compute and display standard deviation true (default) | false

Compute and display the standard deviation, specified as true or false. The scope computes and displays the standard deviation of the portion of the input signal that is currently on display in the scope.

## Scope Window Use

Click the Measurements tab on the scope toolstrip. In the Statistics section, click the Signal Statistics drop-down arrow, and select Standard Deviation.

Data Types: logical
ShowMedian - Compute and display median
true (default) | false
Compute and display the median, specified as true or false. The scope computes and displays the median of the portion of the input signal that is currently on display in the scope.

## Scope Window Use

Click the Measurements tab on the scope toolstrip. In the Statistics section, click the Signal Statistics drop-down arrow, and select Median.
Data Types: logical

## ShowRMS - Compute and display RMS

true (default) | false
Compute and display the RMS, specified as true or false. The scope computes and displays the RMS of the portion of the input signal that is currently on display in the scope.

## Scope Window Use

Click the Measurements tab on the scope toolstrip. In the Statistics section, click the Signal Statistics drop-down arrow, and select RMS.

Data Types: logical
ShowMeanSquare - Compute and display mean square
false (default)|true
Compute and display the mean square, specified as true or false. The scope computes and displays the mean square of the portion of the input signal that is currently on display in the scope.

## Scope Window Use

Click the Measurements tab on the scope toolstrip. In the Statistics section, click the Signal Statistics drop-down arrow, and select Mean Square.
Data Types: logical
Enabled - Enable signal statistics measurements
false (default) | true
Enable signal statistics measurements, specified as true or false. Set this property to true to enable signal statistics measurements.

## Scope Window Use

Click the Measurements tab on the scope toolstrip, and then click Signal Statistics


Data Types: logical

## Examples

## Configure Signal Statistics Programmatically in Time Scope MATLAB Object

Create a sine wave and view it in the Time Scope. Enable the scope programmatically to compute the signal statistics.

The object supports the following statistics measurements:

- Maximum
- Minimum
- Mean
- Median
- RMS
- Peak to peak
- Variance
- Standard deviation
- Mean square


## Initialization

Create the input sine wave using the sin function. Create a timescope MATLAB® object to display the signal. Set the TimeSpan property to 1 second.

```
f = 100;
fs = 1000;
swv = sin(2.*pi.*f.*(0:1/fs:1-1/fs)).';
scope = timescope(SampleRate=fs,...
    TimeSpanSource="property", ...
    TimeSpan=1);
```


## Signal Statistics

Enable the scope to show signal statistics programmatically by setting the SignalStatistics > Enabled property to true.
scope.SignalStatistics.Enabled = true;
By default, the scope enables the following measurements.

```
scope.SignalStatistics
ans =
    SignalStatisticsConfiguration with properties:
```

                                    ShowMax: 1
                    ShowMin: 1
            ShowPeakToPeak: 1
                                    ShowMean: 1
                            ShowVariance: 0
        ShowStandardDeviation: 1
            ShowMedian: 1
                            ShowRMS: 1
                ShowMeanSquare: 0
                        Enabled: 1
    Display the sine wave in the scope. A Statistics panel appears at the bottom and displays the statistics for the portion of the signal that you can see in the scope.

```
scope(swv);
release(scope);
```



If you use the zoom options on the scope, the statistics automatically adjust to the time range shown in the display.

See Also<br>timescope<br>Topics<br>"Configure Time Scope MATLAB Object"<br>Introduced in R2022a

## TriggerConfiguration

Trigger measurements properties for scope

## Description

Use the TriggerConfiguration object to define a trigger event to identify the simulation time of specified input signal characteristics. You can use trigger events to stabilize periodic signals such as a sine wave or capture nonperiodic signals such as a pulse that occurs intermittently.

You can enable the trigger events either from the toolstrip or from the command line. To enable a trigger event from the scope interface, open the Trigger tab and click Enable Trigger in the Controls section.


Processing

## Creation

## Syntax

trigger $=$ TriggerConfiguration()

## Description

trigger $=$ TriggerConfiguration() creates a trigger configuration object trigger.

## Properties

All properties are tunable.
For more information on these triggers and the associated parameters, see "Source/Type and Levels/ Timing Panes".

## Mode - Display update mode

"auto" (default) | "normal" | "once"
Display update mode, specified as one of these:

- "auto" -- Display data from the last trigger event. If no event occurs after one time span, display the last available data.
- "normal" -- Display data from the last trigger event. If no event occurs, the display remains blank.
- "once" -- Display data from the last trigger event and freeze the display. If no event occurs, the display remains blank. Click the Rearm button ( ${ }^{(\sqrt{c}}$ ) to look for the next trigger event.


## Scope Window Use

Click the Trigger tab on the Time Scope toolstrip. In the Setup section, set Mode to one of the available options.
Data Types: char | string
Type - Type of trigger
"edge" (default) | "pulse-width" | "transition" | "runt" | "window" | "timeout"
Type of trigger, specified as one of the following:

- "edge" -- Trigger when the signal crosses a threshold.
- "pulse-width" -- Trigger when the signal crosses a low threshold and a high threshold twice within a specified time.
- "transition" -- Trigger on the rising or falling edge of a signal that crosses the high and low levels within a specified time range.
- "runt" -- Trigger when a signal crosses a low threshold or a high threshold twice within a specified time.
- "window" -- Trigger when a signal stays within or outside a region defined by the high and low thresholds for a specified time.
- "timeout" -- Trigger when a signal stays above or below a threshold longer than a specified time.


## Scope Window Use

Click the Trigger tab on the Time Scope toolstrip. In the Setup section, set Type to one of the available options.

```
Data Types: char|string
Polarity - Trigger polarity
"rising" (default) | "falling" | "either" | "positive" | "negative" | "rise-time" | "fall-
time"| "inside" | "outside"
```

Trigger polarity, specified as one of the following:

- "rising", "falling", or "either" -- When Type is set to "edge" or "timeout".
- "positive", "negative", or "either" -- When Type is set to "pulse-width" or "runt".
- "rise-time", "fall-time", or "either" -- When Type is set to "transition".
- "inside", "outside", or "either" -- When Type is set to "window".


## Scope Window Use

Click the Trigger tab on the Time Scope toolstrip. In the Setup section, set Polarity to one of the available options.

Data Types: char | string

## AutoLevel - Automatic thresholding

true (default) | false
Automatic thresholding of edge-triggered signal, specified as true or false. When you set this property to false, specify the threshold manually using the Level property.

## Scope Window Use

Click the Trigger tab on the Time Scope toolstrip. In the Properties section, select the Auto Level check box.
Data Types: logical

## Position - Horizontal position of trigger

50 (default) | positive scalar in the range (0 100]
Horizontal position of the trigger on the screen, specified as a positive scalar in the range (0 100].

## Scope Window Use

Click the Trigger tab on the Time Scope toolstrip. In the Properties section, set Position (\%) as a positive scalar less than or equal to 100 .

Data Types: double

## Level - Threshold of edge-triggered signal

0 (default) | real scalar
Threshold of an edge-triggered signal, specified as a finite real scalar.

## Dependency

To enable this property, set AutoLevel to false and Type to "edge" or "timeout".

## Scope Window Use

Click the Trigger tab on the Time Scope toolstrip. In the Properties section, specify the Level as a real scalar.

To enable this property, clear the Auto Level check box and set Type to Edge or Timeout.

## Data Types: double

Hysteresis - Noise reject value
0 (default) | real scalar
Noise reject value, specified as a finite real scalar. For more information on hysteresis, see "Hysteresis of Trigger Signals".

## Dependency

To enable this property, set AutoLevel to false and Type to "edge" or "timeout".

## Scope Window Use

Click the Trigger tab on the Time Scope toolstrip. In the Properties section, specify the Hysteresis as a real scalar.

To enable this property, clear the Auto Level check box and set Type to Edge or Timeout.
Data Types: double

## LowLevel - Lower trigger level of window-triggered signal

0.2 (default) | real scalar

Lower trigger level of window-triggered signal, specified as a finite real scalar.

## Dependency

To enable this property, set AutoLevel to false and Type to "pulse-width", "transition", "runt", or "window".

## Scope Window Use

Click the Trigger tab on the Time Scope toolstrip. In the Properties section, specify the Low as a real scalar.

To enable this property, clear the Auto Level check box and set Type to Pulse Width, Transition, Runt, or Window.
Data Types: double

## HighLevel - Higher trigger level of window-triggered signal

2.3 (default) | real scalar

Higher trigger level of window-triggered signal, specified as a finite real scalar.

## Dependency

To enable this property, set AutoLevel to false and Type to "pulse-width", "transition",
"runt", or "window".
Scope Window Use
Click the Trigger tab on the Time Scope toolstrip. In the Properties section, specify the High as a real scalar.

To enable this property, clear the Auto Level check box and set Type to Pulse Width, Transition, Runt, or Window.

## Data Types: double

## MinPulseWidth - Minimum pulse width for pulse or runt-triggered signal <br> 0 (default) | nonnegative scalar

Minimum pulse width for a pulse or runt-triggered signal, specified as a nonnegative scalar.

## Dependency

To enable this property, set Type to "pulse-width" or "runt".

## Scope Window Use

Click the Trigger tab on the Time Scope toolstrip. In the Properties section, specify the Min Width (s) as a nonnegative scalar.

To enable this property, set Type to Pulse Width or Runt.

## Data Types: double

MaxPulseWidth - Maximum pulse width for pulse or runt-triggered signal
Inf (default) | nonnegative scalar
Maximum pulse width for a pulse or runt-triggered signal, specified as a nonnegative scalar.

## Dependency

To enable this property, set Type to "pulse-width" or "runt".

## Scope Window Use

Click the Trigger tab on the Time Scope toolstrip. In the Properties section, specify the Max Width (s) as a nonnegative scalar.

To enable this property, set Type to Pulse Width or Runt.
Data Types: double
MinDuration - Minimum duration for transition or window-triggered signal
0 (default) | nonnegative scalar
Minimum duration for a transition or window-triggered signal, specified as a nonnegative scalar.

## Dependency

To enable this property, set Type to "transition" or "window".

## Scope Window Use

Click the Trigger tab on the Time Scope toolstrip. In the Properties section, specify the Min Time (s) as a nonnegative scalar.

To enable this property, set Type to Transition or Window.
Data Types: double

## MaxDuration - Maximum duration for transition or window-triggered signal Inf (default) | nonnegative scalar

Maximum time duration for a transition or window-triggered signal, specified as a nonnegative scalar.

## Dependency

To enable this property, set Type to "transition" or "window".

## Scope Window Use

Click the Trigger tab on the Time Scope toolstrip. In the Properties section, specify the Max Time (s) as a nonnegative scalar.

To enable this property, set Type to Transition or Window.
Data Types: double

## Timeout - Timeout duration

0 (default) | nonnegative scalar
Timeout duration for a timeout-triggered signal, specified as a nonnegative scalar.

## Dependency

To enable this property, set Type to "timeout".

## Scope Window Use

Click the Trigger tab on the Time Scope toolstrip. In the Properties section, specify the Timeout (s) as a nonnegative scalar.

To enable this property, set Type to Timeout.
Data Types: double
Delay - Trigger offset
0 (default) | real scalar
Trigger offset in seconds, specified as a finite real scalar.

## Scope Window Use

Click the Trigger tab on the Time Scope toolstrip. In the Properties section, specify the Delay (s) as a real scalar.
Data Types: double

## Holdoff - Minimum time between triggers

0 (default) | nonnegative scalar
Minimum time between trigger events, specified as a finite nonnegative scalar.

## Scope Window Use

Click the Trigger tab on the Time Scope toolstrip. In the Properties section, specify the Holdoff (s) as a nonnegative scalar.
Data Types: double

## Channel - Trigger channel

1 (default) | positive integer
Trigger channel, specified as a positive integer.

## Scope Window Use

Click the Trigger tab on the Time Scope toolstrip. Select a channel from the Channel drop down.
Data Types: double

## Enabled - Enable trigger

false (default)|true
Enable trigger, specified as true or false. Set this property to true to enable trigger.

## Scope Window Use

Click the Trigger tab on the Time Scope toolstrip, and the click Enable Trigger in the Controls section.

Data Types: logical

## Examples

## Enable Trigger Programmatically in Time Scope MATLAB Object

View a sine wave in the Time Scope. This sine wave is streaming constantly in the display and cannot be captured without stabilization. To stabilize the sine wave, enable a trigger event programmatically on the scope display using the Enabled property of the TriggerConfiguration object.
Alternatively, you can enable the trigger by clicking the Enable Trigger button on the Trigger tab of the toolstrip.

## Create Sine Wave

Create the input sine wave using the sin function. Create a timescope MATLAB object to display the signal. Set the TimeSpan property to 1 second.

```
f = 100;
fs = 1000;
swv = sin(2.*pi.*f.*(0:1/fs:1-1/fs)).';
scopeNoTrigger = timescope(SampleRate=fs,...
    TimeSpanSource="property", ...
    TimeSpan=1);
```

Display the sine wave in the scope. You can see that the signal in the scope is constantly moving.

```
while(1)
    scopeNoTrigger(swv)
end
release(scopeNoTrigger)
```



## Enable Trigger

Now enable a trigger event to stabilize the signal.
You can either enable the trigger event in the scope during simulation or enable the trigger event programmatically when creating the object.

To use the programmatic approach, create another timescope object and enable the trigger event programmatically while creating the object.

```
scope = timescope(SampleRate=fs,...
    TimeSpanSource="property",...
    TimeSpan=1);
scope.Trigger.Enabled = true;
scope.Trigger.Type = "transition";
scope.Trigger
TriggerConfiguration with properties:
            Mode: 'auto'
            Type: 'transition'
            Polarity: 'rise-time'
        AutoLevel: 1
        Position: 50
        LowLevel: 0.2000
        HighLevel: 2.3000
    MinDuration: 0
```

```
MaxDuration: Inf
    Delay: 0
    Holdoff: 0
    Channel: 1
    Enabled: 1
```

Stream in the sine wave signal again.

```
while(1)
    scope(swv)
end
release(scope)
```

The display freezes as you have enabled the trigger.


The triangle markers show the trigger positions and levels. For more information on the trigger, hover over the triangle.


## See Also

timescope
Topics
"Configure Time Scope MATLAB Object"
Introduced in R2022a

## CursorMeasurementsConfiguration

Display screen or waveform cursors

## Description

Use the CursorMeasurementsConfiguration object to enable screen or waveform cursors. You can control the cursor settings from the toolstrip of the scope or from the command line.

To modify the cursor settings in the scope UI, click the Measurements tab and enable Data Cursors. Each cursor tracks a vertical line along the signal. The scope displays the difference between $x$ - and $y$-values of the signal at the two cursors in the box between the cursors.

Time Scope Toolstrip


Stopped

## Creation

## Syntax

cursormeas = CursorMeasurementsConfiguration()

## Description

cursormeas $=$ CursorMeasurementsConfiguration() creates a cursor measurements configuration object.

## Properties

All properties are tunable.

## XLocation - x-coordinates of the cursors

[2 8] (default) | two-element vector
$x$-coordinates of the cursors, specified as a two-element vector of real elements.
Data Types: double
SnapToData - Snap cursors to data
false (default) | true
Snap cursors to data, specified as true or false.

## Scope Window Use

Click the Measurements tab on the scope toolstrip. In the Cursors section, click Data Cursors, and then select the Snap to data parameter.
Data Types: logical
Enabled - Enable cursor measurements
false (default) | true
Enable cursor measurements, specified as true or false. Set this property to true to enable cursor measurements.

## Scope Window Use

Click the Measurements tab on the scope toolstrip. In the Cursors section, select Data Cursors.
Data Types: logical

## Examples

## Configure Cursor Measurements Programmatically in Time Scope MATLAB Object

Create a sine wave and view it in the Time Scope. Enable data cursors programmatically.

## Initialization

Create the input sine wave using the sin function. Create a timescope MATLAB® object to display the signal. Set the TimeSpan property to 1 second.

```
f = 100;
fs = 1000;
swv = sin(2.*pi.*f.*(0:1/fs:1-1/fs)).';
scope = timescope(SampleRate=fs,...
```

TimeSpanSource="property",...
TimeSpan=1);
Data Cursors
Enable data cursors in the scope programmatically by setting the Enabled property of the CursorMeasurementsConfiguration object to true.
scope.CursorMeasurements.Enabled = true;
scope(swv);
release(scope)


Stopped

See Also<br>timescope<br>Topics<br>"Configure Time Scope MATLAB Object"<br>Introduced in R2022a

## PeakFinderConfiguration

Compute and display the largest calculated peak values on the scope display

## Description

Use the PeakFinderConfiguration object to compute and display peaks in the scope. The scope computes and shows peaks from the portion of the input signal that is currently on display in the scope.

You can specify the number of peaks you want the scope to display, the minimum height above which you want the scope to detect peaks, the minimum distance between peaks, and label the peaks. You can control the peak finder settings from the scope toolstrip or from the command line. The algorithm defines a peak as a local maximum with lower values present on either side of the peak. It does not consider end points as peaks. For more information on the algorithm, see the findpeaks function.

To modify the peak finder settings in the scope interface, click the Measurements tab and enable Peak Finder in the Peaks section. An arrow appears on the plot at each maxima and a Peaks panel appears at the bottom of the scope window.

Time Scope Toolstrip


Peaks

| Channel 1 | P1 | P2 | P3 |
| :---: | :---: | :---: | :---: |
| Time (s) | 4.1906e+6 | $4.1949 \mathrm{e}+6$ | 4.1980e+0 |
| Value | 1.1453e+0 | $1.1133 \mathrm{e}+6$ | 1.1009e+0 |
| Stopped |  |  | Frames $=50 \mathrm{~T}=4.29184 \underline{\square}$ |

## Creation

## Syntax

pkfinder = PeakFinderConfiguration()

## Description

pkfinder $=$ PeakFinderConfiguration() creates a peak finder configuration object.

## Properties

All properties are tunable.

## MinHeight - Level above which scope detects peaks

## - Inf (default) | real scalar value

Level above which the scope detects peaks, specified as a real scalar.

## Scope Window Use

Click the Measurements tab on the scope toolstrip. In the Peaks section, set Min Height to a real scalar.
Data Types: double

## NumPeaks - Maximum number of peaks to show

3 (default) | positive integer less than 100
Maximum number of peaks to show, specified as a positive integer less than 100.
Scope Window Use
Click the Measurements tab on the scope toolstrip. In the Peaks section, set Num Peaks to a positive integer less than 100.
Data Types: double
MinDistance - Minimum number of samples between adjacent peaks
1 (default) | positive integer
Minimum number of samples between adjacent peaks, specified as a positive integer.

## Scope Window Use

Click the Measurements tab on the scope toolstrip. In the Peaks section, set Min Distance to a positive integer.
Data Types: double
Threshold - Minimum difference in height of peak and its neighboring samples
0 (default) | nonnegative scalar
Minimum difference in height of the peak and its neighboring samples, specified as a nonnegative scalar.

## Scope Window Use

Click the Measurements tab on the scope toolstrip. In the Peaks section, set Threshold to a nonnegative scalar.
Data Types: double
LabelPeaks - Label peaks
false (default) |true
Label peaks, specified as true or false. The scope displays the labels (P1, P2, ...) above the arrows in the plot.

## Scope Window Use

Click the Measurements tab on the scope toolstrip. In the Peaks section, select Label Peaks.
Data Types: logical

## LabelFormat - Coordinates to display

"x + y" (default) | "x" | "y"
Coordinates to display next to the peak value, specified as " $x$ ", " $y$ ", or " $x+y$ ".
Data Types: char | string

## Enabled - Enable peak finder measurements

## false (default) |true

Enable peak finder measurements, specified as true or false. Set this property to true to enable peak finder measurements.

## Scope Window Use

Click the Measurements tab on the scope toolstrip. In the Peaks section, select Peak Finder.
Data Types: logical

## Examples

## Enable Peak Finder Programmatically in a Time Scope Object

Create a sine wave and view it in the Time Scope. Enable the peak finder programmatically.

## Initialization

Create the input sine wave using the sin function. Create a timescope MATLAB® object to display the signal. Set the TimeSpan property to 1 second.

```
f = 100;
fs = 1000;
swv = sin(2.*pi.*f.*(0:1/fs:1-1/fs)).';
scope = timescope(SampleRate=fs,...
    TimeSpanSource="property", ...
    TimeSpan=1);
```


## Peaks

Enable the peak finder and label the peaks. Set the scope to show three peaks and label them.

```
scope.PeakFinder.Enabled = true;
scope.PeakFinder.LabelPeaks = true;
scope(swv)
release(scope)
```



Peaks


Stopped

See Also
timescope
Topics
"Configure Time Scope MATLAB Object"
Introduced in R2022a

## tunerconfig

Fusion filter tuner configuration options

## Description

The tunerconfig object creates a tuner configuration for a fusion filter used to tune the filter for reduced estimation error.

## Creation

## Syntax

config = tunerconfig(filterName)
config = tunerconfig(filter)
config = tunerconfig(filterName, Name, Value)

## Description

config = tunerconfig(filterName) creates a tunerconfig object controlling the optimization algorithm of the tune function of the fusion filter by specifying a filter name.
config = tunerconfig(filter) creates a tunerconfig object controlling the optimization algorithm of the tune function of the fusion filter by specifying a filter object.
config = tunerconfig(filterName,Name,Value) configures the created tunerconfig object properties using one or more name-value pair arguments. Name is a property name and Value is the corresponding value. Name must appear inside quotes. You can specify several name-value pair arguments in any order as Name1, Value1, . . . NameN, ValueN. Any unspecified properties take default values.

For example, tunerconfig('imufilter','MaxIterations',3) create a tunerconfig object for the imufilter object with the a maximum of three allowed iterations.

## Inputs Arguments

## filterName - Fusion filter name

'imufilter'|'ahrsfilter'|'ahrs10filter'|'insfilterAsync'|'insfilterMARG'| 'insfitlerErrorState'|'insfilterNonholonomic'

Fusion filter name, specified as one of these options:

- 'imufilter'
- 'ahrsfilter'
- 'ahrs10filter'
- 'insfilterAsync'
- 'insfilterMARG'
- 'insfitlerErrorState'
- 'insfilterNonholonomic'


## filter - Fusion filter

fusion filter object
Fusion filter, specified as one of these fusion filter objects:

- insEKF
- ahrs10filter
- insfilterAsync
- insfilterMARG
- insfilterErrorState
- insfilterNonholonomic
- ahrsfilter
- imufilter


## Properties

Filter - Class name of filter
string
This property is read-only.
Class name of filter, specified as a string. Its value is one of these strings:

- "imufilter"
- "ahrsfilter"
- "ahrs10filter"
- "insfilterAsync"
- "insfilterMARG"
- "insfitlerErrorState"
- "insfilterNonholonomic"


## TunableParameters - Tunable parameters

array of string (default) | cell array
Tunable parameters, specified as an array of strings or a cell array.

- If you want to tune all the elements in each parameter together (scaling up or down all the elements in a process noise matrix for example), then specify the property as an array of strings. Each string corresponds to a property name.

For filter objects other than the insEKF object, this is the default option. With the default option, the property contains all the tunable parameter names as an array of strings. Each string is a tunable property name of the fusion filter.

- If you want to tune a subset of elements for at least one noise parameter, specify it as a cell array. The number of cells is the number of parameters that you want to tune.
- You can specify any cell element as a character vector, representing the property that you want to tune. In this case, the filter tunes all the elements in the property together.
- You can also specify any cell element as a 1-by-2 cell array, in which the first cell is a character vector, representing the property that you want tune. The second cell in the cell array is a vector of indices, representing the elements that you want to tune in the property. These indices are column-based indices.

This is default option for the insEKF object.
For example, running the following:

```
>> filter = insEKF;
config = tunerconfig(filter);
tunable = config.TunableParameters
and you can obtain:
```

```
tunable =
    1\times3 cell array
        {1\times2 cell} {'AccelerometerNoise'} {'GyroscopeNoise'}
>> firstCell = tunable{1}
firstCell =
    1\times2 cell array
        {'AdditiveProcessNoise'} {[11 15 29 43 57 71 85 99 113 127 141 155 169]}
```

In the filter, the additive process noise matrix is a 13 -by-13 matrices, and the column-based indices represent all the diagonal elements of the matrix.

## Example: ["AccelerometerNoise" "GyroscopeNoise"]

## StepForward - Factor of forward step

1.1 (default) | scalar larger than 1

Factor of a forward step, specified as a scalar larger than 1. During the tuning process, the tuner increases or decreases the noise parameters to achieve smaller estimation errors. This property specifies the ratio of parameter increase during a parameter increase step.

## StepBackward - Factor of backward step

0.5 (default) | scalar in range ( 0,1 )

Factor of a backward step, specified as a scalar in the range of $(0,1)$. During the tuning process, the tuner increases or decreases the noise parameters to achieve smaller estimation errors. This property specifies the factor of parameter decrease during a parameter decrease step.

## MaxIterations - Maximum number of iterations

20 (default) | positive integer

Maximum number of iterations allowed by the tuning algorithm, specified as a positive integer.

## ObjectiveLimit - Cost at which to stop tuning process

0.1 (default) | positive scalar

Cost at which to stop the tuning process, specified as a positive scalar.

## FunctionTolerance - Minimum change in cost to continue tuning

0 (default) | nonnegative scalar
Minimum change in cost to continue tuning, specified as a nonnegative scalar. If the change in cost is smaller than the specified tolerance, the tuning process stops.

## Display - Enable showing the iteration details

"iter" (default)|"none"
Enable showing the iteration details, specified as "iter" or "none". When specified as:

- "iter" - The program shows the tuned parameter details in each iteration in the Command Window.
- "none" - The program does not show any tuning information.


## Cost - Metric for evaluating filter performance

"RMS" (default) | "Custom"
Metric for evaluating filter performance, specified as "RMS" or "Custom". When specified as:

- "RMS" - The program optimizes the root-mean-squared (RMS) error between the estimate and the truth.
- "Custom" - The program optimizes the filter performance by using a customized cost function specified by the CustomCostFcn property.


## CustomCostFcn - Customized cost function

[ ] (default) | function handle
Customized cost function, specified as a function handle.

## Dependencies

To enable this property, set the Cost property to 'Custom'.

## OutputFcn - Output function called at each iteration

[] (default) | function handle
Output function called at each iteration, specified as a function handle. The function must use the following syntax:

```
stop = myOutputFcn(params,tunerValues)
```

params is a structure of the current best estimate of each parameter at the end of the current iteration. tunerValues is a structure containing information of the tuner configuration, sensor data, and truth data. It has these fields:

| Field Name | Description |
| :--- | :--- |
| Iteration | Iteration count of the tuner, specified as a <br> positive integer |
| SensorData | Sensor data input to the tune function |
| GroundTruth | Ground truth input to the tune function |
| Configuration | tunerconfig object used for tuning |
| Cost | Tuning cost at the end of the current iteration |

Tip You can use the built-in function tunerPlotPose to visualize the truth data and the estimates for most of your tuning applications. See the "Visualize Tuning Results Using tunerPlotPose" on page 1-280 example for details.

## Examples

## Create Tunerconfig Object and Show Tunable Parameters

Create a tunerconfig object for the insfilterAsync object.

```
config = tunerconfig('insfilterAsync')
config =
    tunerconfig with properties:
        TunableParameters: [1×14 string]
            StepForward: 1.1000
            StepBackward: 0.5000
            MaxIterations: 20
        OptimalityTolerance: 0.1000
                Display: iter
                        Cost: RMS
```

Display the default tunable parameters.

```
config.TunableParameters
```

ans $=1 \times 14$ string
"AccelerometerNoise" "GyroscopeNoise" "MagnetometerNoise" "GPSPositionNoise"

Tune insfilterAsync to Optimize Pose Estimate
Load the recorded sensor data and ground truth data.
load('insfilterAsyncTuneData.mat');
Create timetables for the sensor data and the truth data.
sensorData $=$ timetable(Accelerometer, Gyroscope, ...
Magnetometer, GPSPosition, GPSVelocity, 'SampleRate', 100);

```
groundTruth = timetable(Orientation, Position, ...
    'SampleRate', 100);
```

Create an insfilterAsync filter object that has a few noise properties.

```
filter = insfilterAsync('State', initialState, ...
    'StateCovariance', initialStateCovariance, ...
    'AccelerometerBiasNoise', 1e-7, ...
    'GyroscopeBiasNoise', 1e-7, ...
    'MagnetometerBiasNoise', 1e-7, ...
    'GeomagneticVectorNoise', 1e-7);
```

Create a tuner configuration object for the filter. Set the maximum iterations to two. Also, set the tunable parameters as the unspecified properties.

```
config = tunerconfig('insfilterAsync','MaxIterations',8);
config.TunableParameters = setdiff(config.TunableParameters, ...
    {'GeomagneticVectorNoise', 'AccelerometerBiasNoise', ...
    'GyroscopeBiasNoise', 'MagnetometerBiasNoise'});
config.TunableParameters
ans = 1\times10 string
    "AccelerationNoise" "AccelerometerNoise" "AngularVelocityNoise" "GPSPositionNoise"
```

Use the tuner noise function to obtain a set of initial sensor noises used in the filter.

```
measNoise = tunernoise('insfilterAsync')
measNoise = struct with fields:
    AccelerometerNoise: 1
            GyroscopeNoise: 1
        MagnetometerNoise: 1
        GPSPositionNoise: 1
        GPSVelocityNoise: 1
```

Tune the filter and obtain the tuned parameters.

| tunedParams $=$ tune(filter, measNoise, sensorData,groundTruth, config); |  |  |
| :---: | :--- | :--- |
| Iteration | Parameter | Metric |
| 1 |  |  |
| 1 |  | AccelerationNoise |
| 1 | AccelerometerNoise | 2.1345 |
| 1 | AngularVelocityNoise | 2.1264 |
| 1 | GPSPositionNoise | 1.9659 |
| 1 | GPSVelocityNoise | 1.9341 |
| 1 | GyroscopeNoise | 1.8420 |
| 1 | MagnetometerNoise | 1.7589 |
| 1 | PositionNoise | 1.7362 |
| 1 | QuaternionNoise | 1.7362 |
| 2 | VelocityNoise | 1.7218 |
| 2 | AccelerationNoise | 1.7218 |
| 2 | AccelerometerNoise | 1.7190 |
| 2 | AngularVelocityNoise | 1.7170 |
| 2 | GPSPositionNoise | 1.6045 |
| 2 | GPSVelocityNoise | 1.5948 |


| 2 | MagnetometerNoise | 1.4703 |
| :---: | :---: | :---: |
| 2 | PositionNoise | 1.4703 |
| 2 | QuaternionNoise | 1.4632 |
| 2 | VelocityNoise | 1.4632 |
| 3 | AccelerationNoise | 1.4596 |
| 3 | AccelerometerNoise | 1.4548 |
| 3 | AngularVelocityNoise | 1.3923 |
| 3 | GPSPositionNoise | 1.3810 |
| 3 | GPSVelocityNoise | 1.3322 |
| 3 | GyroscopeNoise | 1.2998 |
| 3 | MagnetometerNoise | 1.2976 |
| 3 | PositionNoise | 1.2976 |
| 3 | QuaternionNoise | 1.2943 |
| 3 | VelocityNoise | 1.2943 |
| 4 | AccelerationNoise | 1.2906 |
| 4 | AccelerometerNoise | 1.2836 |
| 4 | AngularVelocityNoise | 1.2491 |
| 4 | GPSPositionNoise | 1.2258 |
| 4 | GPSVelocityNoise | 1.1880 |
| 4 | GyroscopeNoise | 1.1701 |
| 4 | MagnetometerNoise | 1.1698 |
| 4 | PositionNoise | 1.1698 |
| 4 | QuaternionNoise | 1.1688 |
| 4 | VelocityNoise | 1.1688 |
| 5 | AccelerationNoise | 1.1650 |
| 5 | AccelerometerNoise | 1.1569 |
| 5 | AngularVelocityNoise | 1.1454 |
| 5 | GPSPositionNoise | 1.1100 |
| 5 | GPSVelocityNoise | 1.0778 |
| 5 | GyroscopeNoise | 1.0709 |
| 5 | MagnetometerNoise | 1.0675 |
| 5 | PositionNoise | 1.0675 |
| 5 | QuaternionNoise | 1.0669 |
| 5 | VelocityNoise | 1.0669 |
| 6 | AccelerationNoise | 1.0634 |
| 6 | AccelerometerNoise | 1.0549 |
| 6 | AngularVelocityNoise | 1.0549 |
| 6 | GPSPositionNoise | 1.0180 |
| 6 | GPSVelocityNoise | 0.9866 |
| 6 | GyroscopeNoise | 0.9810 |
| 6 | MagnetometerNoise | 0.9775 |
| 6 | PositionNoise | 0.9775 |
| 6 | QuaternionNoise | 0.9768 |
| 6 | VelocityNoise | 0.9768 |
| 7 | AccelerationNoise | 0.9735 |
| 7 | AccelerometerNoise | 0.9652 |
| 7 | AngularVelocityNoise | 0.9652 |
| 7 | GPSPositionNoise | 0.9283 |
| 7 | GPSVelocityNoise | 0.8997 |
| 7 | GyroscopeNoise | 0.8947 |
| 7 | MagnetometerNoise | 0.8920 |
| 7 | PositionNoise | 0.8920 |
| 7 | QuaternionNoise | 0.8912 |
| 7 | VelocityNoise | 0.8912 |
| 8 | AccelerationNoise | 0.8885 |
| 8 | AccelerometerNoise | 0.8811 |
| 8 | AngularVelocityNoise | 0.8807 |
| 8 | GPSPositionNoise | 0.8479 |

```
GPSVelocityNoise 0.8238
GyroscopeNoise 0.8165
MagnetometerNoise 0.8165
PositionNoise 0.8165
QuaternionNoise 0.8159
VelocityNoise 0.8159
```

Fuse the sensor data using the tuned filter.

```
dt = seconds(diff(groundTruth.Time));
N = size(sensorData,1);
qEst = quaternion.zeros(N,1);
posEst = zeros(N,3);
% Iterate the filter for prediction and correction using sensor data.
for ii=1:N
    if ii ~= 1
        predict(filter, dt(ii-1));
    end
    if all(~isnan(Accelerometer(ii,:)))
            fuseaccel(filter,Accelerometer(ii,:), ...
                tunedParams.AccelerometerNoise);
    end
    if all(~isnan(Gyroscope(ii,:)))
            fusegyro(filter, Gyroscope(ii,:), ...
                tunedParams.GyroscopeNoise);
    end
    if all(~isnan(Magnetometer(ii,1)))
            fusemag(filter, Magnetometer(ii,:), ...
                tunedParams.MagnetometerNoise);
    end
    if all(~isnan(GPSPosition(ii,1)))
            fusegps(filter, GPSPosition(ii,:), ...
                tunedParams.GPSPositionNoise, GPSVelocity(ii,:), ...
                tunedParams.GPSVelocityNoise);
    end
    [posEst(ii,:), qEst(ii,:)] = pose(filter);
end
```

Compute the RMS errors.
orientationError = rad2deg(dist(qEst, Orientation));
rmsorientationError $=\operatorname{sqrt}($ mean(orientationError.^2))
rmsorientationError $=2.7801$
positionError $=\operatorname{sqrt}(\operatorname{sum}(($ posEst - Position).^2, 2));
rmspositionError $=$ sqrt(mean( positionError.^2))
rmspositionError $=0.5966$

Visualize the results.
figure();
$\mathrm{t}=(0: \mathrm{N}-1) . /$ groundTruth.Properties.SampleRate;
subplot $(2,1,1)$
plot(t, positionError, 'b');
title("Tuned insfilterAsync" + newline + "Euclidean Distance Position Error")
xlabel('Time (s)');
ylabel('Position Error (meters)')

```
subplot(2,1,2)
plot(t, orientationError, 'b');
title("Orientation Error")
xlabel('Time (s)');
ylabel('Orientation Error (degrees)');
```

Tuned insfilterAsync Euclidean Distance Position Error


Orientation Error


## Tune imufilter to Optimize Orientation Estimate

Load recorded sensor data and ground truth data.
ld = load('imufilterTuneData.mat');
qTrue = ld.groundTruth.Orientation; \% true orientation
Create an imufilter object and fuse the filter with the sensor data.
fuse = imufilter;
qEstUntuned = fuse(ld.sensorData.Accelerometer, ...
ld.sensorData.Gyroscope);
Create a tunerconfig object and tune the imufilter to improve the orientation estimate.
cfg = tunerconfig('imufilter');
tune(fuse, ld.sensorData, ld.groundTruth, cfg);
Iteration Parameter Metric

| 1 | AccelerometerNoise | 0.1149 |
| :---: | :---: | :---: |
| 1 | GyroscopeNoise | 0.1146 |
| 1 | GyroscopeDriftNoise | 0.1146 |
| 1 | LinearAccelerationNoise | 0.1122 |
| 1 | LinearAccelerationDecayFactor | 0.1103 |
| 2 | AccelerometerNoise | 0.1102 |
| 2 | GyroscopeNoise | 0.1098 |
| 2 | GyroscopeDriftNoise | 0.1098 |
| 2 | LinearAccelerationNoise | 0.1070 |
| 2 | LinearAccelerationDecayFactor | 0.1053 |
| 3 | AccelerometerNoise | 0.1053 |
| 3 | GyroscopeNoise | 0.1048 |
| 3 | GyroscopeDriftNoise | 0.1048 |
| 3 | LinearAccelerationNoise | 0.1016 |
| 3 | LinearAccelerationDecayFactor | 0.1002 |
| 4 | AccelerometerNoise | 0.1001 |
| 4 | GyroscopeNoise | 0.0996 |
| 4 | GyroscopeDriftNoise | 0.0996 |
| 4 | LinearAccelerationNoise | 0.0962 |
| 4 | LinearAccelerationDecayFactor | 0.0950 |
| 5 | AccelerometerNoise | 0.0950 |
| 5 | GyroscopeNoise | 0.0943 |
| 5 | GyroscopeDriftNoise | 0.0943 |
| 5 | LinearAccelerationNoise | 0.0910 |
| 5 | LinearAccelerationDecayFactor | 0.0901 |
| 6 | AccelerometerNoise | 0.0900 |
| 6 | GyroscopeNoise | 0.0893 |
| 6 | GyroscopeDriftNoise | 0.0893 |
| 6 | LinearAccelerationNoise | 0.0862 |
| 6 | LinearAccelerationDecayFactor | 0.0855 |
| 7 | AccelerometerNoise | 0.0855 |
| 7 | GyroscopeNoise | 0.0848 |
| 7 | GyroscopeDriftNoise | 0.0848 |
| 7 | LinearAccelerationNoise | 0.0822 |
| 7 | LinearAccelerationDecayFactor | 0.0818 |
| 8 | AccelerometerNoise | 0.0817 |
| 8 | GyroscopeNoise | 0.0811 |
| 8 | GyroscopeDriftNoise | 0.0811 |
| 8 | LinearAccelerationNoise | 0.0791 |
| 8 | LinearAccelerationDecayFactor | 0.0789 |
| 9 | AccelerometerNoise | 0.0788 |
| 9 | GyroscopeNoise | 0.0782 |
| 9 | GyroscopeDriftNoise | 0.0782 |
| 9 | LinearAccelerationNoise | 0.0769 |
| 9 | LinearAccelerationDecayFactor | 0.0768 |
| 10 | AccelerometerNoise | 0.0768 |
| 10 | GyroscopeNoise | 0.0762 |
| 10 | GyroscopeDriftNoise | 0.0762 |
| 10 | LinearAccelerationNoise | 0.0754 |
| 10 | LinearAccelerationDecayFactor | 0.0753 |
| 11 | AccelerometerNoise | 0.0753 |
| 11 | GyroscopeNoise | 0.0747 |
| 11 | GyroscopeDriftNoise | 0.0747 |
| 11 | LinearAccelerationNoise | 0.0741 |
| 11 | LinearAccelerationDecayFactor | 0.0740 |
| 12 | AccelerometerNoise | 0.0740 |
| 12 | GyroscopeNoise | 0.0734 |
| 12 | GyroscopeDriftNoise | 0.0734 |


| 12 | LinearAccelerationNoise | 0.0728 |
| :--- | :--- | :--- |
| 12 | LinearAccelerationDecayFactor | 0.0728 |
| 13 | AccelerometerNoise | 0.0728 |
| 13 | GyroscopeNoise | 0.0721 |
| 13 | GyroscopeDriftNoise | 0.0721 |
| 13 | LinearAccelerationNoise | 0.0715 |
| 13 | LinearAccelerationDecayFactor | 0.0715 |
| 14 | AccelerometerNoise | 0.0715 |
| 14 | GyroscopeNoise | 0.0706 |
| 14 | GyroscopeDriftNoise | 0.0706 |
| 14 | LinearAccelerationNoise | 0.0700 |
| 14 | LinearAccelerationDecayFactor | 0.0700 |
| 15 | AccelerometerNoise | 0.0700 |
| 15 | GyroscopeNoise | 0.0690 |
| 15 | GyroscopeDriftNoise | 0.0690 |
| 15 | LinearAccelerationNoise | 0.0684 |
| 15 | LinearAccelerationDecayFactor | 0.0684 |
| 16 | AccelerometerNoise | 0.0684 |
| 16 | GyroscopeNoise | 0.0672 |
| 16 | GyroscopeDriftNoise | 0.0672 |
| 16 | LinearAccelerationNoise | 0.0668 |
| 16 | LinearAccelerationDecayFactor | 0.0667 |
| 17 | AccelerometerNoise | 0.0667 |
| 17 | GyroscopeNoise | 0.0655 |
| 17 | GyroscopeDriftNoise | 0.0655 |
| 17 | LinearAccelerationNoise | 0.0654 |
| 17 | LinearAccelerationDecayFactor | 0.0654 |
| 18 | AccelerometerNoise | 0.0654 |
| 18 | GyroscopeNoise | 0.0641 |
| 18 | GyroscopeDriftNoise | 0.0641 |
| 18 | LinearAccelerationNoise | 0.0640 |
| 18 | LinearAccelerationDecayFactor | 0.0639 |
| 19 | AccelerometerNoise | 0.0639 |
| 19 | GyroscopeNoise | 0.0627 |
| 19 | GyroscopeDriftNoise | 0.0627 |
| 19 | LinearAccelerationNoise | 0.0627 |
| 19 | LinearAccelerationDecayFactor | 0.0624 |
| 20 | AccelerometerNoise | 0.0624 |
| 20 | GyroscopeNoise | 0.0614 |
| 20 | GyroscopeDriftNoise | 0.0614 |
| 20 | LinearAccelerationNoise | 0.0613 |
| 20 |  | 0.0613 |
|  |  |  |

## Fuse the sensor data again using the tuned filter.

```
qEstTuned = fuse(ld.sensorData.Accelerometer, ...
    ld.sensorData.Gyroscope);
```

Compare the tuned and untuned filter RMS error performances.

```
dUntuned = rad2deg(dist(qEstUntuned, qTrue));
dTuned = rad2deg(dist(qEstTuned, qTrue));
rmsUntuned = sqrt(mean(dUntuned.^2))
rmsUntuned = 6.5864
rmsTuned = sqrt(mean(dTuned.^2))
rmsTuned = 3.5098
```

Visualize the results.
$\mathrm{N}=$ numel(dUntuned);
$\mathrm{t}=(0: \mathrm{N}-1) . /$ fuse.SampleRate;
plot(t, dUntuned, 'r', t, dTuned, 'b');
legend('Untuned', 'Tuned');
title('imufilter - Tuned vs Untuned Error')
xlabel('Time (s)');
ylabel('Orientation Error (degrees)');


## Save Tuned Parameters in MAT File Using Output Function

Load the recorded sensor data and ground truth data.
load('insfilterAsyncTuneData.mat');
Create timetables for the sensor data and the truth data.

```
sensorData = timetable(Accelerometer, Gyroscope, ...
    Magnetometer, GPSPosition, GPSVelocity, 'SampleRate', 100);
groundTruth = timetable(Orientation, Position, ...
    'SampleRate', 100);
```

Create an insfilterAsync filter object that has a few noise properties.

```
filter = insfilterAsync('State', initialState, ...
    'StateCovariance', initialStateCovariance, ...
    'AccelerometerBiasNoise', le-7, ...
    'GyroscopeBiasNoise', 1e-7, ...
    'MagnetometerBiasNoise', 1e-7, ...
    'GeomagneticVectorNoise', 1e-7);
```

Create a tuner configuration object for the filter. Define the OutputFcn property as a customized function, myOutputFcn, which saves the latest tuned parameters in a MAT file.

```
config = tunerconfig('insfilterAsync', ...
    'MaxIterations',5, ...
    'Display','none', ...
    'OutputFcn', @myOutputFcn);
config.TunableParameters = setdiff(config.TunableParameters, ...
    {'GeomagneticVectorNoise', 'AccelerometerBiasNoise', ...
        'GyroscopeBiasNoise', 'MagnetometerBiasNoise'});
config.TunableParameters
ans = 1x10 string
    Columns 1 through 3
        "AccelerationNoise" "AccelerometerNoise" "AngularVelocityN..."
    Columns 4 through 6
        "GPSPositionNoise" "GPSVelocityNoise" "GyroscopeNoise"
    Columns 7 through 9
        "MagnetometerNoise" "PositionNoise" "QuaternionNoise"
    Column 10
    "VelocityNoise"
```

Use the tuner noise function to obtain a set of initial sensor noises used in the filter.

```
measNoise = tunernoise('insfilterAsync')
measNoise = struct with fields:
    AccelerometerNoise: 1
            GyroscopeNoise: 1
        MagnetometerNoise: 1
        GPSPositionNoise: 1
        GPSVelocityNoise: 1
```

Tune the filter and obtain the tuned parameters.

```
tunedParams = tune(filter,measNoise,sensorData,groundTruth,config);
```

Display the save parameters using the saved file.

```
fileObject = matfile('myfile.mat');
fileObject.params
ans = struct with fields:
    AccelerationNoise: [88.8995 88.8995 88.8995]
```

```
AccelerometerBiasNoise: [1.0000e-07 1.0000e-07 1.0000e-07]
        AccelerometerNoise: 0.7942
    AngularVelocityNoise: [0.0089 0.0089 0.0089]
        GPSPositionNoise: 1.1664
        GPSVelocityNoise: 0.5210
GeomagneticVectorNoise: [1.0000e-07 1.0000e-07 1.0000e-07]
        GyroscopeBiasNoise: [1.0000e-07 1.0000e-07 1.0000e-07]
            GyroscopeNoise: 0.5210
MagnetometerBiasNoise: [1.0000e-07 1.0000e-07 1.0000e-07]
        MagnetometerNoise: 1.0128
            PositionNoise: [5.2100e-07 5.2100e-07 5.2100e-07]
        QuaternionNoise: [1.3239e-06 1.3239e-06 1.3239e-06 1.3239e-06]
        ReferenceLocation: [0 0 0]
            State: [28x1 double]
        StateCovariance: [28x28 double]
            VelocityNoise: [6.3678e-07 6.3678e-07 6.3678e-07]
```

The output function

```
function stop = myOutputFcn(params, ~)
save('myfile.mat','params'); % overwrite the file with latest
stop = false;
end
```


## See Also

insfilterAsync|insfilterNonholonomic|insfilterMARG|insfilterErrorState| ahrsfilter|ahrs10filter|imufilter

Introduced in R2020b

## validatorOccupancyMap

State validator based on 2-D grid map

## Description

The validator0ccupancyMap object validates states and discretized motions based on the value in a 2-D occupancy map. An occupied map location is interpreted as an invalid state.

## Creation

## Syntax

## Description

validator = validator0ccupancyMap creates a 2-D occupancy map validator associated with an SE2 state space with default settings.
validator = validatorOccupancyMap(stateSpace) creates a validator in the given state space definition derived from nav. StateSpace.
validator = validatorOccupancyMap(stateSpace, Name, Value) specifies the Map or XYIndices properties using Name, Value pair arguments.

## Properties

## StateSpace - State space for validating states

stateSpaceSE2 (default) | subclass of nav. StateSpace
State space for validating states, specified as a subclass of nav. StateSpace. Provided state space objects include:

- stateSpaceSE2
- stateSpaceDubins
- stateSpaceReedsShepp


## Map - Map used for validating states

binary0ccupancyMap(10,10) (default)| binary0ccupancyMap object | occupancyMap object
Map used for validating states, specified as a binary0ccupancyMap or occupancyMap object.

## ValidationDistance - Interval for checking state validity

Inf (default) | positive numeric scalar
Interval for sampling between states and checking state validity, specified as a positive numeric scalar.

XYIndices - State variable mapping for $\boldsymbol{x y}$-coordinates
[1 2] (default)|[xIdx yIdx]

State variable mapping for $x y$-coordinates in state vector, specified as a two-element vector, [xIdx $y I d x$ ]. For example, if a state vector is given as [r p y x y z], the $x y$-coordinates are [4 5].

## Object Functions

copy isStateValid
isMotionValid

Create deep copy of state validator object
Check if state is valid
Check if path between states is valid

## Examples

## Validate Path Through Occupancy Map Environment

This example shows how to validate paths through an evironment.
Load example maps. Use the simple map to create a binary occupancy map.
load exampleMaps.mat
map = occupancyMap(simpleMap);
show(map)


Specify a coarse path through the map.
path $=$ [2 2 pi/2; $10150 ; 178$-pi/2];
hold on
plot(path(:,1),path(:,2),"--0")


Create a state validator using the stateSpaceSE2 definition. Specify the map and the distance for interpolating and validating path segments.

```
validator = validatorOccupancyMap(stateSpaceSE2);
validator.Map = map;
validator.ValidationDistance = 0.1;
```

Check the points of the path are valid states. All three points are in free space, so are considered valid.

```
isValid = isStateValid(validator,path)
isValid = 3x1 logical array
```

    1
    1
    Check the motion between each sequential path states. The isMotionValid function interpolates along the path between states. If a path segment is invalid, plot the last valid point along the path.

```
startStates = [path(1,:);path(2,:)];
endStates = [path(2,:);path(3,:)];
    for i = 1:2
        [isPathValid, lastValid] = isMotionValid(validator,startStates(i,:),endStates(i,:));
        if ~isPathValid
            plot(lastValid(1),lastValid(2),'or')
```



## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Specify the Map and XYIndices properties when you create the object. For example:

```
validator = validatorOccupancyMap('Map',occMap,'XYIndices',[4 5])
```

As of MATLAB R2022a, default map behavior during code generation has changed, which may result in backwards compatibility issues. Maps such as validator0ccupancyMap now support fixed-size code generation (DynamicMemoryAllocation="off").

1 Maps that are either default-constructed or constructed with compile-time constant size information (or matrices that are of compile-time constant size) produce fixed-size maps.
2 To restore the previous behavior, use the coder.ignoreConst function when specifying size inputs, or coder.varsize matrix variable name specified as a string scalar or character vector, prior to constructing the map.

## See Also

stateSpaceSE2 | nav.StateSpace|nav.StateValidator
Introduced in R2019b

## validatorOccupancyMap3D

State validator based on 3-D grid map

## Description

The validator0ccupancyMap3D object validates states and discretized motions based on occupancy values in a 3-D occupancy map. The object interprets obstacle-free map locations as valid states. The object interprets occupied and unknown map locations as invalid states.

## Creation

## Syntax

```
validator = validatorOccupancyMap3D
validator = validatorOccupancyMap3D(stateSpace)
validator = validatorOccupancyMap3D(stateSpace,Name,Value)
Description
```

validator = validator0ccupancyMap3D creates a 3-D occupancy map validator associated with an $\operatorname{SE}(3)$ state space with default settings.
validator = validator0ccupancyMap3D(stateSpace) creates a validator in the specified state space. The stateSpace input sets the value of the StateSpace property.
validator = validatorOccupancyMap3D(stateSpace, Name, Value) sets properties using one or more name-value pairs. Unspecified properties have default values. Enclose each property name in quotes.

For example, validator0ccupancyMap3D('ValidationDistance', 0.1) creates a 3-D occupancy map validator with a sampling interval of 0.1.

## Properties

## StateSpace - State space for validating states

stateSpaceSE3 object (default) | subclass of nav. StateSpace
This property is read-only.
State space for validating states, specified as a subclass of nav. StateSpace. These are the predefined state space objects:

- stateSpaceSE3
- stateSpaceSE2
- stateSpaceDubins
- stateSpaceReedsShepp

Example: validator0ccupancyMap3D(stateSpaceSE3)

## Map - Map used for validating states

occupancyMap3D (default) | occupancyMap3D object
Map used for validating states, specified as an occupancyMap3D object.
Example: validator. Map = occupancyMap3D(10)

## ValidationDistance - Interval for checking state validity

Inf (default) | positive numeric scalar
Interval for sampling between states and checking state validity, specified as a positive numeric scalar.
Example: validator.ValidationDistance = 0.1
Data Types: double

## XYZIndices - State variable mapping for xyz-coordinates

[1 2 3] (default)| three-element vector
State variable mapping for $x y z$-coordinates in the state vector, specified as a three-element vector of form [xIdx yIdx zIdx].
Data Types: double

## Object Functions

copy isMotionValid isStateValid

Create deep copy of state validator object Check if path between states is valid Check if state is valid

## Examples

## Validate Path Through 3-D Occupancy Map Environment

Create a 3-D occupancy map and associated state validator. Plan, validate, and visualize a path through the occupancy map.

## Load and Assign Map to State Validator

Load a 3-D occupancy map of a city block into the workspace. Specify a threshold for which cells to consider as obstacle-free.

```
mapData = load('dMapCityBlock.mat');
omap = mapData.omap;
omap.FreeThreshold = 0.5;
```

Inflate the occupancy map to add a buffer zone for safe operation around the obstacles.

```
inflate(omap,1)
```

Create an $\mathrm{SE}(3)$ state space object with bounds for state variables.

```
ss = stateSpaceSE3([-20 220;
    -20 220;
```

```
-10 100;
inf inf;
inf inf;
inf inf;
inf inf]);
```

Create a 3-D occupancy map state validator using the created state space.

```
sv = validatorOccupancyMap3D(ss);
```

Assign the occupancy map to the state validator object. Specify the sampling distance interval.

```
sv.Map = omap;
sv.ValidationDistance = 0.1;
```


## Plan and Visualize Path

Create a path planner with increased maximum connection distance. Reduce the maximum number of iterations.

```
planner = plannerRRT(ss,sv);
planner.MaxConnectionDistance = 50;
planner.MaxIterations = 1000;
```

Create a user-defined evaluation function for determining whether the path reaches the goal. Specify the probability of choosing the goal state during sampling.

```
planner.GoalReachedFcn = @(~,x,y)(norm(x(1:3)-y(1:3))<5);
planner.GoalBias = 0.1;
```

Set the start and goal states.

```
start = [40 180 25 0.7 0.2 0 0.1];
goal = [150 33 35 0.3 0 0.1 0.6];
```

Plan a path using the specified start, goal, and planner.

```
[pthObj,solnInfo] = plan(planner,start,goal);
```

Check that the points of the path are valid states.

```
isValid = isStateValid(sv,pthObj.States)
isValid = 7x1 logical array
    1
    1
    1
    1
    1
    1
    1
```

Check that the motion between each sequential path state is valid.

```
isPathValid = zeros(size(pth0bj.States,1)-1,1,'logical');
for i = 1:size(pth0bj.States,1)-1
    [isPathValid(i),~] = isMotionValid(sv,pthObj.States(i,:),...
```

```
    pthObj.States(i+1,:));
```

end
isPathValid
isPathValid = 6x1 logical array
1
1
1
1
1
1

Visualize the results.
show(omap)
hold on
scatter3(start(1,1), start(1,2),start(1,3),'g','filled') \% draw start state scatter3(goal(1,1),goal(1,2),goal(1,3),'r','filled') \% draw goal state plot3(pth0bj.States(:,1),pth0bj.States(:,2),pth0bj.States(:,3),...
'r-','LineWidth',2) \% draw path

Occupancy Map


## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

See Also<br>occupancyMap3D | stateSpaceSE3|validator0ccupancyMap Introduced in R2020b

## validatorVehicleCostmap

State validator based on 2-D costmap

## Description

The validator0ccupancyMap object validates states and discretized motions based on the value in a 2-D costmap. An occupied map location is interpreted as an invalid state.

## Creation

## Syntax

## Description

validator = validatorVehicleCostmap creates a vehicle cost map validator associated with an SE2 state space with default settings.
validator = validatorVehicleCostmap(stateSpace) creates a validator in the given state space definition derived from nav. StateSpace.
validator = validatorVehicleCostmap(stateSpace, xyIndices) sets the XYIndices property to specify which variables in the state vector define the $x y$-coordinates.
validator = validatorVehicleCostmap(stateSpace,Name,Value) specifies the Map or XYIndices properties using Name, Value pair arguments.

## Properties

## StateSpace - State space for validating states

stateSpaceSE2 (default) | subclass of nav. StateSpace
State space for validating states, specified as a subclass of nav. StateSpace. Provided state space objects include:

- stateSpaceSE2
- stateSpaceDubins
- stateSpaceReedsShepp


## Map - Map used for validating states

vehicleCostMap (10,10) (default) | vehicleCostMap object
Map used for validating states, specified as a vehicleCostMap object.

## ValidationDistance - Interval for checking state validity

Inf (default) | positive numeric scalar
Interval for sampling between states and checking state validity, specified as a positive numeric scalar.

## XYIndices - State variable mapping for $\boldsymbol{x y}$-coordinates

[1 2] (default)|[xIdx yIdx]
State variable mapping for $x y$-coordinates in state vector, specified as a two-element vector, [ xIdx $y I d x]$. For example, if a state vector is given as [rpy y z], the $x y$-coordinates are [4 5].

ThetaIndex - State variable mapping for theta coordinate
NaN (default) | positive integer
State variable mapping for theta coordinate in state vector, specified as a positive integer. For example, if a state vector is given as [ $\mathrm{x} y$ theta], the theta coordinate is 3 .

## Object Functions

| copy | Create deep copy of state validator object |
| :--- | :--- |
| isStateValid | Check if state is valid |

isStateValid Check if state is valid
isMotionValid Check if path between states is valid

## Examples

## Validate Path Through Vehicle Costmap Environment

This example shows how to validate paths through an evironment.
Load example maps. Use the simple map to create a vehicle cost map. Specify an inflation raidus of 1 meter.

```
load exampleMaps.mat
map = vehicleCostmap(double(simpleMap));
map.CollisionChecker = inflationCollisionChecker("InflationRadius",1);
plot(map)
```



Specify a coarse path through the map.

```
path = [3 3 pi/2; 8 15 0; 17 8 -pi/2];
hold on
plot(path(:,1),path(:,2),"--0")
```



Create a state validator using the stateSpaceSE2 definition. Specify the map and the distance for interpolating and validating path segments.

```
validator = validatorVehicleCostmap(stateSpaceSE2);
validator.Map = map;
validator.ValidationDistance = 0.1;
```

Check the points of the path are valid states. All three points are in free space, so are considered valid.

```
isValid = isStateValid(validator,path)
isValid = 3x1 logical array
```

    1
    1
    1
    Check the motion between each sequential path states. The isMotionValid function interpolates along the path between states. If a path segment is invalid, plot the last valid point along the path.

```
startStates = [path(1,:);path(2,:)];
endStates = [path(2,:);path(3,:)];
    for i = 1:2
        [isPathValid, lastValid] = isMotionValid(validator,startStates(i,:),endStates(i,:));
        if ~isPathValid
            plot(lastValid(1),lastValid(2),'or')
```



## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
For code generation, the map used inside the object must remain constant.

## See Also

validator0ccupancyMap|stateSpaceSE2|nav.StateSpace|nav.StateValidator

Introduced in R2019b

## copy

Create deep copy of state validator object

## Syntax

validator2 = copy(validator1)

## Description

validator2 $=$ copy (validator1) creates a deep copy of the specified state validator object.

## Examples

## Create Deep Copy of 3-D Occupancy Map State Validator Object

Create a validator object and set a custom validation distance.

```
validator = validatorOccupancyMap3D;
validator.ValidationDistance = 4.5
validator =
    validatorOccupancyMap3D with properties:
                            Map: [1x1 occupancyMap3D]
                StateSpace: [1x1 stateSpaceSE3]
                XYZIndices: [1 2 3]
        ValidationDistance: 4.5000
```

Create a deep copy of the state validator object.

```
validator2 = copy(validator)
validator2 =
    validatorOccupancyMap3D with properties:
                            Map: [1x1 occupancyMap3D]
            StateSpace: [1x1 stateSpaceSE3]
                XYZIndices: [1 2 3]
        ValidationDistance: 4.5000
```

Verify that the ValidationDistance property values of the two state validator objects are equal.

```
isequal(validator.ValidationDistance,validator2.ValidationDistance)
ans = logical
    1
```


## Input Arguments

## validator1 - State validator object

validatorOccupancyMap object | validatorOccupancyMap3D object |
validatorVehicleCostmap object
State validator object, specified as a validator0ccupancyMap, validator0ccupancyMap3D, or validatorVehicleCostmap object.

## Output Arguments

validator2 - State validator object
validatorOccupancyMap object | validator0ccupancyMap3D object |
validatorVehicleCostmap object
State validator object, returned as a validator0ccupancyMap, validator0ccupancyMap3D, or validatorVehicleCostmap object.

See Also<br>validator0ccupancyMap | validator0ccupancyMap3D | validatorVehicleCostmap<br>Introduced in R2020b

## isMotionValid

Check if path between states is valid

## Syntax

[isValid,lastValid] = isMotionValid(validator,state1,state2)

## Description

[isValid,lastValid] = isMotionValid(validator,state1,state2) checks if the path between two states is valid by interpolating between states. The function also returns the last valid state along the path.

## Examples

## Validate Path Through Occupancy Map Environment

This example shows how to validate paths through an evironment.
Load example maps. Use the simple map to create a binary occupancy map.

```
load exampleMaps.mat
map = occupancyMap(simpleMap);
show(map)
```



Specify a coarse path through the map.

```
path = [2 2 pi/2; 10 15 0; 17 8 -pi/2];
hold on
plot(path(:,1),path(:,2),"--0")
```



Create a state validator using the stateSpaceSE2 definition. Specify the map and the distance for interpolating and validating path segments.
validator = validatorOccupancyMap(stateSpaceSE2);
validator.Map = map;
validator.ValidationDistance = 0.1;
Check the points of the path are valid states. All three points are in free space, so are considered valid.

```
isValid = isStateValid(validator,path)
isValid = 3x1 logical array
```

    1
    1
    Check the motion between each sequential path states. The isMotionValid function interpolates along the path between states. If a path segment is invalid, plot the last valid point along the path.

```
startStates = [path(1,:);path(2,:)];
endStates = [path(2,:);path(3,:)];
    for i = 1:2
        [isPathValid, lastValid] = isMotionValid(validator,startStates(i,:),endStates(i,:));
        if ~isPathValid
            plot(lastValid(1),lastValid(2),'or')
```



## Validate Path Through Vehicle Costmap Environment

This example shows how to validate paths through an evironment.
Load example maps. Use the simple map to create a vehicle cost map. Specify an inflation raidus of 1 meter.
load exampleMaps.mat
map = vehicleCostmap(double(simpleMap));
map.CollisionChecker = inflationCollisionChecker("InflationRadius",1); plot(map)


Specify a coarse path through the map.
path = [3 3 pi/2; $8150 ; 178$-pi/2];
hold on
plot(path(:,1), path(: , 2), "--o")


Create a state validator using the stateSpaceSE2 definition. Specify the map and the distance for interpolating and validating path segments.

```
validator = validatorVehicleCostmap(stateSpaceSE2);
validator.Map = map;
validator.ValidationDistance = 0.1;
```

Check the points of the path are valid states. All three points are in free space, so are considered valid.

```
isValid = isStateValid(validator,path)
isValid = 3x1 logical array
```

    1
    1
    1
    Check the motion between each sequential path states. The isMotionValid function interpolates along the path between states. If a path segment is invalid, plot the last valid point along the path.

```
startStates = [path(1,:);path(2,:)];
endStates = [path(2,:);path(3,:)];
    for i = 1:2
        [isPathValid, lastValid] = isMotionValid(validator,startStates(i,:),endStates(i,:));
        if ~isPathValid
            plot(lastValid(1),lastValid(2),'or')
```



## Validate Path Through 3-D Occupancy Map Environment

Create a 3-D occupancy map and associated state validator. Plan, validate, and visualize a path through the occupancy map.

## Load and Assign Map to State Validator

Load a 3-D occupancy map of a city block into the workspace. Specify a threshold for which cells to consider as obstacle-free.

```
mapData = load('dMapCityBlock.mat');
omap = mapData.omap;
omap.FreeThreshold = 0.5;
```

Inflate the occupancy map to add a buffer zone for safe operation around the obstacles.

```
inflate(omap,1)
```

Create an $\mathrm{SE}(3)$ state space object with bounds for state variables.
ss = stateSpaceSE3([-20 220;
-20 220;

```
-10 100;
inf inf;
inf inf;
inf inf;
inf inf]);
```

Create a 3-D occupancy map state validator using the created state space.

```
sv = validatorOccupancyMap3D(ss);
```

Assign the occupancy map to the state validator object. Specify the sampling distance interval.

```
sv.Map = omap;
sv.ValidationDistance = 0.1;
```


## Plan and Visualize Path

Create a path planner with increased maximum connection distance. Reduce the maximum number of iterations.

```
planner = plannerRRT(ss,sv);
planner.MaxConnectionDistance = 50;
planner.MaxIterations = 1000;
```

Create a user-defined evaluation function for determining whether the path reaches the goal. Specify the probability of choosing the goal state during sampling.

```
planner.GoalReachedFcn = @(~,x,y)(norm(x(1:3)-y(1:3))<5);
planner.GoalBias = 0.1;
```

Set the start and goal states.

```
start = [40 180 25 0.7 0.2 0 0.1];
goal = [150 33 35 0.3 0 0.1 0.6];
```

Plan a path using the specified start, goal, and planner.

```
[pthObj,solnInfo] = plan(planner,start,goal);
```

Check that the points of the path are valid states.

```
isValid = isStateValid(sv,pthObj.States)
isValid = 7x1 logical array
    1
    1
    1
    1
    1
    1
    1
```

Check that the motion between each sequential path state is valid.

```
isPathValid = zeros(size(pth0bj.States,1)-1,1,'logical');
for i = 1:size(pth0bj.States,1)-1
    [isPathValid(i),~] = isMotionValid(sv,pthObj.States(i,:),...
```

```
    pthObj.States(i+1,:));
end
isPathValid
isPathValid = 6x1 logical array
    1
```

Visualize the results.

```
show(omap)
```

hold on
scatter3(start(1,1), start(1,2), start(1,3),'g','filled') \% draw start state
scatter3(goal(1,1), goal(1,2),goal(1,3),'r','filled') \% draw goal state
plot3(pth0bj.States(:,1),pth0bj.States(:,2),pth0bj.States(:,3),...
'r-','LineWidth',2) \% draw path

Occupancy Map


## Input Arguments

## validator - State validator object

object of subclass of nav. StateValidator

State validator object, specified as an object of subclass of nav. StateValidator. These are the predefined state validator objects:

- validator0ccupancyMap
- validatorVehicleCostmap
- validator0ccupancyMap3D
state1 - Initial state positions
$n$-element row vector | $m$-by- $n$ matrix
Initial state positions, specified as an $n$-element row vector or $m$-by- $n$ matrix. $n$ is the dimension of the state space specified in validator. $m$ is the number of states to validate.

Data Types: single|double

## state2 - Final state positions

$n$-element row vector | $m$-by- $n$ matrix
Final state positions, specified as an $n$-element row vector or m-by-n matrix. $n$ is the dimension of the state space specified in validator. $m$ is the number of states to validate.
Data Types: single | double

## Output Arguments

## isValid - Valid states

$m$-element logical column vector
Valid states, returned as an m-element logical column vector.

## Data Types: logical

## lastValid - Final valid state along each path

$n$-element row vector | m-by-n matrix
Final valid state along each path, returned as an $n$-element row vector or $m$-by- $n$ matrix. $n$ is the dimension of the state space specified in the state space property in validator. $m$ is the number of paths validated. Each row contains the final valid state along the associated path.
Data Types: single|double

## See Also

isStateValid|stateSpaceSE2|nav.StateSpace|nav.StateValidator
Introduced in R2019b

## isStateValid

Check if state is valid

## Syntax

isValid = isStateValid(validator,states)

## Description

isValid = isStateValid(validator,states) checks if a set of given states are valid.

## Examples

## Validate Path Through Occupancy Map Environment

This example shows how to validate paths through an evironment.
Load example maps. Use the simple map to create a binary occupancy map.
load exampleMaps.mat
map = occupancyMap(simpleMap);
show(map)


Specify a coarse path through the map.
path $=$ [2 2 pi/2; $10150 ; 178$-pi/2];
hold on
plot(path(:,1),path(:,2),"--o")


Create a state validator using the stateSpaceSE2 definition. Specify the map and the distance for interpolating and validating path segments.

```
validator = validatorOccupancyMap(stateSpaceSE2);
validator.Map = map;
validator.ValidationDistance = 0.1;
```

Check the points of the path are valid states. All three points are in free space, so are considered valid.

```
isValid = isStateValid(validator,path)
isValid = 3x1 logical array
    1
    1
    1
```

Check the motion between each sequential path states. The isMotionValid function interpolates along the path between states. If a path segment is invalid, plot the last valid point along the path.

```
startStates = [path(1,:);path(2,:)];
endStates = [path(2,:);path(3,:)];
        for i = 1:2
            [isPathValid, lastValid] = isMotionValid(validator,startStates(i,:),endStates(i,:));
            if ~isPathValid
                    plot(lastValid(1),lastValid(2),'or')
            end
        end
hold off
```



## Validate Path Through Vehicle Costmap Environment

This example shows how to validate paths through an evironment.
Load example maps. Use the simple map to create a vehicle cost map. Specify an inflation raidus of 1 meter.
load exampleMaps.mat
map $=$ vehicleCostmap(double(simpleMap));
map.CollisionChecker = inflationCollisionChecker("InflationRadius",1); plot(map)


Specify a coarse path through the map.

```
path = [3 3 pi/2; 8 15 0; 17 8 -pi/2];
hold on
plot(path(:,1),path(:,2),"--0")
```



Create a state validator using the stateSpaceSE2 definition. Specify the map and the distance for interpolating and validating path segments.

```
validator = validatorVehicleCostmap(stateSpaceSE2);
validator.Map = map;
validator.ValidationDistance = 0.1;
```

Check the points of the path are valid states. All three points are in free space, so are considered valid.

```
isValid = isStateValid(validator,path)
isValid = 3x1 logical array
```

    1
    1
    1
    Check the motion between each sequential path states. The isMotionValid function interpolates along the path between states. If a path segment is invalid, plot the last valid point along the path.

```
startStates = [path(1,:);path(2,:)];
endStates = [path(2,:);path(3,:)];
    for i = 1:2
        [isPathValid, lastValid] = isMotionValid(validator,startStates(i,:),endStates(i,:));
        if ~isPathValid
            plot(lastValid(1),lastValid(2),'or')
```



## Validate Path Through 3-D Occupancy Map Environment

Create a 3-D occupancy map and associated state validator. Plan, validate, and visualize a path through the occupancy map.

## Load and Assign Map to State Validator

Load a 3-D occupancy map of a city block into the workspace. Specify a threshold for which cells to consider as obstacle-free.

```
mapData = load('dMapCityBlock.mat');
omap = mapData.omap;
omap.FreeThreshold = 0.5;
```

Inflate the occupancy map to add a buffer zone for safe operation around the obstacles.

```
inflate(omap,1)
```

Create an SE (3) state space object with bounds for state variables.

```
ss = stateSpaceSE3([-20 220;
```

    -20 220;
    ```
-10 100;
inf inf;
inf inf;
inf inf;
inf inf]);
```

Create a 3-D occupancy map state validator using the created state space.

```
sv = validatorOccupancyMap3D(ss);
```

Assign the occupancy map to the state validator object. Specify the sampling distance interval.

```
sv.Map = omap;
sv.ValidationDistance = 0.1;
```


## Plan and Visualize Path

Create a path planner with increased maximum connection distance. Reduce the maximum number of iterations.

```
planner = plannerRRT(ss,sv);
planner.MaxConnectionDistance = 50;
planner.MaxIterations = 1000;
```

Create a user-defined evaluation function for determining whether the path reaches the goal. Specify the probability of choosing the goal state during sampling.

```
planner.GoalReachedFcn = @(~,x,y)(norm(x(1:3)-y(1:3))<5);
planner.GoalBias = 0.1;
```

Set the start and goal states.

```
start = [40 180 25 0.7 0.2 0 0.1];
goal = [150 33 35 0.3 0 0.1 0.6];
```

Plan a path using the specified start, goal, and planner.

```
[pthObj,solnInfo] = plan(planner,start,goal);
```

Check that the points of the path are valid states.

```
isValid = isStateValid(sv,pthObj.States)
isValid = 7x1 logical array
    1
    1
    1
    1
    1
    1
    1
```

Check that the motion between each sequential path state is valid.

```
isPathValid = zeros(size(pth0bj.States,1)-1,1,'logical');
for i = 1:size(pth0bj.States,1)-1
    [isPathValid(i),~] = isMotionValid(sv,pthObj.States(i,:),...
```

```
    pthObj.States(i+1,:));
```

end
isPathValid
isPathValid = 6x1 logical array
1
1
1
1
1
1

Visualize the results.
show(omap)
hold on
scatter3(start(1,1), start(1,2), start(1,3),'g','filled') \% draw start state scatter3(goal(1,1),goal(1,2),goal(1,3),'r','filled') \% draw goal state plot3(pth0bj.States(:,1),pth0bj.States(:,2), pth0bj.States(:,3),...
'r-','LineWidth',2) \% draw path

Occupancy Map


## Input Arguments

## validator - State validator object

object of subclass of nav. StateValidator

State validator object, specified as an object of subclass of nav. StateValidator. These are the predefined state validator objects:

- validatorOccupancyMap
- validatorVehicleCostmap
- validatorOccupancyMap3D
states - State positions
$n$-element row vector | $m$-by- $n$ matrix
State positions, specified as an $n$-element row vector or $m$-by- $n$ matrix. $n$ is the dimension of the state space specified in validator. $m$ is the number of states to validate.

Data Types: single | double

## Output Arguments

isValid - Valid states<br>$m$-element logical column vector

Valid states, returned as an m-element logical column vector.
Data Types: logical

```
See Also
isMotionValid|stateSpaceSE2|nav.StateSpace|nav.StateValidator
```

Introduced in R2019b

## waypointTrajectory

Waypoint trajectory generator

## Description

The waypointTrajectory System object generates trajectories using specified waypoints. When you create the System object, you can optionally specify the time of arrival, velocity, and orientation at each waypoint. See "Algorithms" on page 2-1558 for more details.

To generate a trajectory from waypoints:
1 Create the waypointTrajectory object and set its properties.
2 Call the object as if it were a function.
To learn more about how System objects work, see What Are System Objects?.

## Creation

## Syntax

trajectory = waypointTrajectory
trajectory = waypointTrajectory (Waypoints,TimeOfArrival)
trajectory = waypointTrajectory(Waypoints,TimeOfArrival,Name,Value)

## Description

trajectory = waypointTrajectory returns a System object, trajectory, that generates a trajectory based on default stationary waypoints.
trajectory = waypointTrajectory(Waypoints,TimeOfArrival) specifies the Waypoints that the generated trajectory passes through and the TimeOfArrival at each waypoint.
trajectory = waypointTrajectory(Waypoints,TimeOfArrival,Name, Value) sets each creation argument or property Name to the specified Value. Unspecified properties and creation arguments have default or inferred values.

Example: trajectory = waypointTrajectory([10,10,0;20,20,0;20,20,10],[0,0.5,10]) creates a waypoint trajectory System object, trajectory, that starts at waypoint [10, 10, 0], and then passes through [20,20,0] after 0.5 seconds and [20,20,10] after 10 seconds.

## Creation Arguments

Creation arguments are properties which are set during creation of the System object and cannot be modified later. If you do not explicitly set a creation argument value, the property value is inferred.

If you specify any creation argument, then you must specify both the Waypoints and TimeOfArrival creation arguments. You can specify Waypoints and TimeOfArrival as value-only arguments or name-value pairs.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## SampleRate - Sample rate of trajectory (Hz)

100 (default) | positive scalar
Sample rate of trajectory in Hz , specified as a positive scalar.
Tunable: Yes
Data Types: double
SamplesPerFrame - Number of samples per output frame
1 (default) | positive scalar integer
Number of samples per output frame, specified as a positive scalar integer.
Tunable: Yes
Data Types: double

## Waypoints - Positions in the navigation coordinate system (m) <br> N -by-3 matrix

Positions in the navigation coordinate system in meters, specified as an $N$-by- 3 matrix. The columns of the matrix correspond to the first, second, and third axes, respectively. The rows of the matrix, $N$, correspond to individual waypoints.

## Dependencies

To set this property, you must also set valid values for the TimeOfArrival property.

## Data Types: double

## TimeOfArrival - Time at each waypoint (s)

$N$-element column vector of nonnegative increasing numbers
Time corresponding to arrival at each waypoint in seconds, specified as an $N$-element column vector. The first element of TimeOfArrival must be 0 . The number of samples, $N$, must be the same as the number of samples (rows) defined by Waypoints.

## Dependencies

To set this property, you must also set valid values for the Waypoints property.

## Data Types: double

## Velocities - Velocity in navigation coordinate system at each waypoint (m/s) <br> N -by-3 matrix

Velocity in the navigation coordinate system at each waypoint in meters per second, specified as an $N$-by-3 matrix. The columns of the matrix correspond to the first, second, and third axes, respectively.

The number of samples, $N$, must be the same as the number of samples (rows) defined by Waypoints.

If the velocity is specified as a non-zero value, the object automatically calculates the course of the trajectory. If the velocity is specified as zero, the object infers the course of the trajectory from adjacent waypoints.

## Dependencies

To set this property, you must also set valid values for the Waypoints and TimeOfArrival properties.
Data Types: double

## Course - Horizontal direction of travel (degree)

$N$-element real vector
Horizontal direction of travel, specified as an $N$-element real vector in degrees. The number of samples, $N$, must be the same as the number of samples (rows) defined by Waypoints. If neither Velocities nor Course is specified, course is inferred from the waypoints.

## Dependencies

To set this property, the Velocities property must not be specified in object creation.
Data Types: double

## GroundSpeed - Groundspeed at each waypoint (m/s)

$N$-element real vector
Groundspeed at each waypoint, specified as an $N$-element real vector in $\mathrm{m} / \mathrm{s}$. If the property is not specified, it is inferred from the waypoints. The number of samples, $N$, must be the same as the number of samples (rows) defined by Waypoints.

## Dependencies

To set this property, the Velocities property must not be specified at object creation.

## Data Types: double

## ClimbRate - Climb rate at each waypoint (m/s)

$N$-element real vector
Climb Rate at each waypoint, specified as an $N$-element real vector in degrees. The number of samples, $N$, must be the same as the number of samples (rows) defined by Waypoints. If neither Velocities nor Course is specified, climb rate is inferred from the waypoints.

## Dependencies

To set this property, the Velocities property must not be specified at object creation.

## Data Types: double

## Orientation - Orientation at each waypoint

$N$-element quaternion column vector | 3 -by-3-by- $N$ array of real numbers
Orientation at each waypoint, specified as an $N$-element quaternion column vector or 3-by-3-by- N array of real numbers. Each quaternion must have a norm of 1. Each 3-by-3 rotation matrix must be an orthonormal matrix. The number of quaternions or rotation matrices, $N$, must be the same as the number of samples (rows) defined by Waypoints.

If Orientation is specified by quaternions, the underlying class must be double.

## Dependencies

To set this property, you must also set valid values for the Waypoints and TimeOfArrival properties.
Data Types: double

## AutoPitch - Align pitch angle with direction of motion

false (default) |true
Align pitch angle with the direction of motion, specified as true or false. When specified as true, the pitch angle automatically aligns with the direction of motion. If specified as false, the pitch angle is set to zero (level orientation).

## Dependencies

To set this property, the Orientation property must not be specified at object creation.

## AutoBank - Align roll angle to counteract centripetal force

false (default) | true
Align roll angle to counteract the centripetal force, specified as true or false. When specified as true, the roll angle automatically counteracts the centripetal force. If specified as false, the roll angle is set to zero (flat orientation).

## Dependencies

To set this property, the Orientation property must not be specified at object creation.

## ReferenceFrame - Reference frame of trajectory <br> 'NED' (default)|'ENU'

Reference frame of the trajectory, specified as 'NED ' (North-East-Down) or 'ENU ' (East-North-Up).

## Usage

## Syntax

[position,orientation, velocity, acceleration, angularVelocity] = trajectory()
Description
[position,orientation, velocity, acceleration, angularVelocity] = trajectory() outputs a frame of trajectory data based on specified creation arguments and properties.

## Output Arguments

## position - Position in local navigation coordinate system (m)

M-by-3 matrix
Position in the local navigation coordinate system in meters, returned as an $M$-by-3 matrix.
$M$ is specified by the SamplesPerFrame property.
Data Types: double

## orientation - Orientation in local navigation coordinate system

$M$-element quaternion column vector | 3 -by-3-by- $M$ real array
Orientation in the local navigation coordinate system, returned as an $M$-by- 1 quaternion column vector or a 3-by-3-by-M real array.

Each quaternion or 3-by-3 rotation matrix is a frame rotation from the local navigation coordinate system to the current body coordinate system.
$M$ is specified by the SamplesPerFrame property.
Data Types: double
velocity - Velocity in local navigation coordinate system (m/s)
M-by-3 matrix
Velocity in the local navigation coordinate system in meters per second, returned as an $M$-by-3 matrix.
$M$ is specified by the SamplesPerFrame property.
Data Types: double

## acceleration - Acceleration in local navigation coordinate system (m/s ${ }^{\mathbf{2}}$ )

$M$-by-3 matrix
Acceleration in the local navigation coordinate system in meters per second squared, returned as an $M$-by-3 matrix.
$M$ is specified by the SamplesPerFrame property.
Data Types: double

## angularVelocity - Angular velocity in local navigation coordinate system (rad/s)

 M-by-3 matrixAngular velocity in the local navigation coordinate system in radians per second, returned as an $M$ -by-3 matrix.
$M$ is specified by the SamplesPerFrame property.
Data Types: double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:
release(obj)

## Specific to waypointTrajectory

waypointInfo Get waypoint information table lookupPose Obtain pose information for certain time perturbations Perturbation defined on object perturb Apply perturbations to object

## Common to All System Objects

clone Create duplicate System object
step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object
isDone End-of-data status

## Examples

## Create Default waypointTrajectory

```
trajectory = waypointTrajectory
trajectory =
    waypointTrajectory with properties:
            SampleRate: 100
        SamplesPerFrame: 1
            Waypoints: [2x3 double]
            TimeOfArrival: [2x1 double]
            Velocities: [2\times3 double]
                    Course: [2x1 double]
            GroundSpeed: [2x1 double]
                ClimbRate: [2x1 double]
            Orientation: [2x1 quaternion]
                AutoPitch: 0
                    AutoBank: 0
        ReferenceFrame: 'NED'
```

Inspect the default waypoints and times of arrival by calling waypointInfo. By default, the waypoints indicate a stationary position for one second.

```
waypointInfo(trajectory)
ans=2\times2 table
    TimeOfArrival Waypoints
            0 0 0 0
            1 0 0 0
```


## Create Square Trajectory

Create a square trajectory and examine the relationship between waypoint constraints, sample rate, and the generated trajectory.

Create a square trajectory by defining the vertices of the square. Define the orientation at each waypoint as pointing in the direction of motion. Specify a 1 Hz sample rate and use the default SamplesPerFrame of 1 .

```
waypoints = [0,0,0; ... % Initial position
        0,1,0; ...
        1,1,0; ...
        1,0,0; ...
        0,0,0]; % Final position
toa = 0:4; % time of arrival
orientation = quaternion([0,0,0; ...
            45,0,0; ...
            135,0,0; ...
            225,0,0; ...
            0,0,0], ...
            'eulerd','ZYX','frame');
trajectory = waypointTrajectory(waypoints, ...
    'TimeOfArrival',toa, ...
    'Orientation',orientation, ...
    'SampleRate',1);
```

Create a figure and plot the initial position of the platform.

```
figure(1)
plot(waypoints(1,1),waypoints(1,2),'b*')
title('Position')
axis([-1,2,-1,2])
axis square
xlabel('X')
ylabel('Y')
grid on
hold on
```



In a loop, step through the trajectory to output the current position and current orientation. Plot the current position and log the orientation. Use pause to mimic real-time processing.

```
orientationLog = zeros(toa(end)*trajectory.SampleRate,1,'quaternion');
count = 1;
while ~isDone(trajectory)
    [currentPosition,orientationLog(count)] = trajectory();
    plot(currentPosition(1),currentPosition(2),'bo')
    pause(trajectory.SamplesPerFrame/trajectory.SampleRate)
    count = count + 1;
end
hold off
```



Convert the orientation quaternions to Euler angles for easy interpretation, and then plot orientation over time.

```
figure(2)
eulerAngles = eulerd([orientation(1);orientationLog],'ZYX','frame');
plot(toa,eulerAngles(:,1),'ko', ...
    toa,eulerAngles(:,2),'bd', ...
    toa,eulerAngles(:,3),'r.');
title('Orientation Over Time')
legend('Rotation around Z-axis','Rotation around Y-axis','Rotation around X-axis')
xlabel('Time (seconds)')
ylabel('Rotation (degrees)')
grid on
```


## Orientation Over Time



So far, the trajectory object has only output the waypoints that were specified during construction. To interpolate between waypoints, increase the sample rate to a rate faster than the time of arrivals of the waypoints. Set the trajectory sample rate to 100 Hz and call reset.

```
trajectory.SampleRate = 100;
reset(trajectory)
```

Create a figure and plot the initial position of the platform. In a loop, step through the trajectory to output the current position and current orientation. Plot the current position and log the orientation. Use pause to mimic real-time processing.

```
figure(1)
plot(waypoints(1,1),waypoints(1,2),'b*')
title('Position')
axis([-1,2,-1,2])
axis square
xlabel('X')
ylabel('Y')
grid on
hold on
orientationLog = zeros(toa(end)*trajectory.SampleRate,1,'quaternion');
count = 1;
while ~isDone(trajectory)
    [currentPosition,orientationLog(count)] = trajectory();
    plot(currentPosition(1),currentPosition(2),'bo')
```

pause(trajectory.SamplesPerFrame/trajectory.SampleRate)
count = count + 1;
end
hold off


The trajectory output now appears circular. This is because the waypointTrajectory System object ${ }^{\mathrm{TM}}$ minimizes the acceleration and angular velocity when interpolating, which results in smoother, more realistic motions in most scenarios.

Convert the orientation quaternions to Euler angles for easy interpretation, and then plot orientation over time. The orientation is also interpolated.

```
figure(2)
eulerAngles = eulerd([orientation(1);orientationLog],'ZYX','frame');
t = 0:1/trajectory.SampleRate:4;
plot(t,eulerAngles(:,1),'ko', ...
    t,eulerAngles(:,2),'bd', ...
    t,eulerAngles(:,3),'r.');
title('Orientation Over Time')
legend('Rotation around Z-axis','Rotation around Y-axis','Rotation around X-axis')
xlabel('Time (seconds)')
ylabel('Rotation (degrees)')
grid on
```



The waypointTrajectory algorithm interpolates the waypoints to create a smooth trajectory. To return to the square trajectory, provide more waypoints, especially around sharp changes. To track corresponding times, waypoints, and orientation, specify all the trajectory info in a single matrix.

```
    % Time, Waypoint, Orientation
trajectoryInfo = [0, 0,0,0, 0,0,0; ... % Initial position
    0.1, 0,0.1,0, 0,0,0; ...
    0.9, 0,0.9,0, 0,0,0; ...
    1, 0,1,0, 45,0,0; ...
    1.1, 0.1,1,0, 90,0,0; ...
    1.9, 0.9,1,0, 90,0,0; ...
    2, 1,1,0, 135,0,0; ...
    2.1, 1,0.9,0, 180,0,0; ...
    2.9, 1,0.1,0, 180,0,0; ...
    3, 1,0,0, 225,0,0; ...
    3.1, 0.9,0,0, 270,0,0; ...
    3.9, 0.1,0,0, 270,0,0; ...
    4, 0,0,0, 270,0,0]; % Final position
trajectory = waypointTrajectory(trajectoryInfo(:,2:4), ...
    'TimeOfArrival',trajectoryInfo(:,1), ...
    'Orientation',quaternion(trajectoryInfo(:,5:end),'eulerd','ZYX','frame'), ...
    'SampleRate',100);
```

Create a figure and plot the initial position of the platform. In a loop, step through the trajectory to output the current position and current orientation. Plot the current position and log the orientation. Use pause to mimic real-time processing.

```
figure(1)
plot(waypoints(1,1),waypoints(1,2),'b*')
title('Position')
axis([-1,2,-1,2])
axis square
xlabel('X')
ylabel('Y')
grid on
hold on
orientationLog = zeros(toa(end)*trajectory.SampleRate,1,'quaternion');
count = 1;
while ~isDone(trajectory)
    [currentPosition,orientationLog(count)] = trajectory();
    plot(currentPosition(1),currentPosition(2),'bo')
    pause(trajectory.SamplesPerFrame/trajectory.SampleRate)
    count = count+1;
end
hold off
```

Position


The trajectory output now appears more square-like, especially around the vertices with waypoints.

Convert the orientation quaternions to Euler angles for easy interpretation, and then plot orientation over time.

```
figure(2)
eulerAngles = eulerd([orientation(1);orientationLog],'ZYX','frame');
t = 0:1/trajectory.SampleRate:4;
eulerAngles = plot(t,eulerAngles(:,1),'ko', ...
    t,eulerAngles(:,2),'bd', ...
    t,eulerAngles(:,3),'r.');
title('Orientation Over Time')
legend('Rotation around Z-axis', ...
    'Rotation around Y-axis', ...
    'Rotation around X-axis', ...
    'Location', 'SouthWest')
xlabel('Time (seconds)')
ylabel('Rotation (degrees)')
grid on
```



## Create Arc Trajectory

This example shows how to create an arc trajectory using the waypointTrajectory System object ${ }^{\mathrm{TM}}$. waypointTrajectory creates a path through specified waypoints that minimizes acceleration and angular velocity. After creating an arc trajectory, you restrict the trajectory to be within preset bounds.

## Create an Arc Trajectory

Define a constraints matrix consisting of waypoints, times of arrival, and orientation for an arc trajectory. The generated trajectory passes through the waypoints at the specified times with the specified orientation. The waypointTrajectory System object requires orientation to be specified using quaternions or rotation matrices. Convert the Euler angles saved in the constraints matrix to quaternions when specifying the Orientation property.

```
    % Arrival, Waypoints, Orientation
constraints = [0, 20,20,0, 90,0,0;
        3, 50,20,0, 90,0,0;
        4, 58,15.5,0, 162,0,0;
        5.5, 59.5,0,0 180,0,0];
trajectory = waypointTrajectory(constraints(:,2:4), ...
    'Time0fArrival',constraints(:,1), ...
    'Orientation',quaternion(constraints(:,5:7),'eulerd','ZYX','frame'));
```

Call waypointInfo on trajectory to return a table of your specified constraints. The creation properties Waypoints, TimeOfArrival, and Orientation are variables of the table. The table is convenient for indexing while plotting.

```
tInfo = waypointInfo(trajectory)
tInfo =
    4x3 table
    TimeOfArrival Waypoints Orientation
\begin{tabular}{rrrrrl} 
& & & & & \\
0 & 20 & 20 & 0 & & \(\{1 \times 1\) quaternion \(\}\) \\
3 & 50 & 20 & 0 & \(\{1 \times 1\) quaternion \(\}\) \\
4 & 58 & 15.5 & 0 & \(\{1 \times 1\) quaternion \(\}\) \\
5.5 & 59.5 & 0 & 0 & \(\{1 \times 1\) quaternion \(\}\)
\end{tabular}
```

The trajectory object outputs the current position, velocity, acceleration, and angular velocity at each call. Call trajectory in a loop and plot the position over time. Cache the other outputs.

```
figure(1)
plot(tInfo.Waypoints(1,1),tInfo.Waypoints(1,2),'b*')
title('Position')
axis([20,65,0,25])
xlabel('North')
ylabel('East')
grid on
daspect([1 1 1])
hold on
orient = zeros(tInfo.TimeOfArrival(end)*trajectory.SampleRate,1,'quaternion');
vel = zeros(tInfo.TimeOfArrival(end)*trajectory.SampleRate,3);
acc = vel;
angVel = vel;
count = 1;
while ~isDone(trajectory)
```

```
    [pos,orient(count),vel(count,:),acc(count,:),angVel(count,:)] = trajectory();
    plot(pos(1),pos(2),'bo')
    pause(trajectory.SamplesPerFrame/trajectory.SampleRate)
    count = count + 1;
```

end


Inspect the orientation, velocity, acceleration, and angular velocity over time. The waypointTrajectory System object ${ }^{T M}$ creates a path through the specified constraints that minimized acceleration and angular velocity.

```
figure(2)
timeVector = 0:(1/trajectory.SampleRate):tInfo.TimeOfArrival(end);
eulerAngles = eulerd([tInfo.Orientation{1};orient],'ZYX','frame');
plot(timeVector,eulerAngles(:,1), ...
    timeVector,eulerAngles(:,2), ...
    timeVector,eulerAngles(:,3));
title('Orientation Over Time')
legend('Rotation around Z-axis', ...
    'Rotation around Y-axis', ...
    'Rotation around X-axis', ...
    'Location','southwest')
xlabel('Time (seconds)')
ylabel('Rotation (degrees)')
grid on
```

```
figure(3)
plot(timeVector(2:end),vel(:,1), ...
    timeVector(2:end),vel(:,2), ...
    timeVector(2:end),vel(:,3));
title('Velocity Over Time')
legend('North','East','Down')
xlabel('Time (seconds)')
ylabel('Velocity (m/s)')
grid on
figure(4)
plot(timeVector(2:end),acc(:,1), ...
    timeVector(2:end),acc(:,2), ...
    timeVector(2:end),acc(:,3));
title('Acceleration Over Time')
legend('North','East','Down','Location','southwest')
xlabel('Time (seconds)')
ylabel('Acceleration (m/s^2)')
grid on
figure(5)
plot(timeVector(2:end),angVel(:,1), ...
    timeVector(2:end),angVel(:,2), ...
    timeVector(2:end), angVel(:,3));
title('Angular Velocity Over Time')
legend('North','East','Down')
xlabel('Time (seconds)')
ylabel('Angular Velocity (rad/s)')
grid on
```






## Restrict Arc Trajectory Within Preset Bounds

You can specify additional waypoints to create trajectories within given bounds. Create upper and lower bounds for the arc trajectory.

```
figure(1)
xUpperBound = [(20:50)';50+10*sin(0:0.1:pi/2)';60*ones(11,1)];
yUpperBound = [20.5.*ones(31,1);10.5+10*cos(0:0.1:pi/2)';(10:-1:0)'];
xLowerBound = [(20:49)';50+9*sin(0:0.1:pi/2)';59*ones(11,1)];
yLowerBound = [19.5.*ones(30,1);10.5+9*cos(0:0.1:pi/2)';(10:-1:0)'];
plot(xUpperBound,yUpperBound,'r','LineWidth',2);
plot(xLowerBound,yLowerBound,'r','LineWidth',2)
```



To create a trajectory within the bounds, add additional waypoints. Create a new waypointTrajectory System object ${ }^{\mathrm{TM}}$, and then call it in a loop to plot the generated trajectory. Cache the orientation, velocity, acceleration, and angular velocity output from the trajectory object.

```
    % Time, Waypoint, Orientation
constraints = [0, 20,20,0, 90,0,0;
    1.5, 35,20,0, 90,0,0;
    2.5 45,20,0, 90,0,0;
    3, 50,20,0, 90,0,0;
    3.3, 53,19.5,0, 108,0,0;
    3.6, 55.5,18.25,0, 126,0,0;
    3.9, 57.5,16,0, 144,0,0;
    4.2, 59,14,0, 162,0,0;
    4.5, 59.5,10,0 180,0,0;
    5, 59.5,5,0 180,0,0;
    5.5, 59.5,0,0 180,0,0];
trajectory = waypointTrajectory(constraints(:,2:4), ...
    'TimeOfArrival',constraints(:,1), ...
    'Orientation',quaternion(constraints(:,5:7),'eulerd','ZYX','frame'));
tInfo = waypointInfo(trajectory);
figure(1)
plot(tInfo.Waypoints(1,1),tInfo.Waypoints(1,2),'b*')
count = 1;
```

while ~isDone(trajectory)
[pos,orient(count), vel(count,:),acc(count,:), angVel(count,:)] = trajectory();
plot(pos(1), pos(2),'gd')
pause(trajectory. SamplesPerFrame/trajectory.SampleRate) count = count + 1;
end


The generated trajectory now fits within the specified boundaries. Visualize the orientation, velocity, acceleration, and angular velocity of the generated trajectory.

```
figure(2)
timeVector = 0:(1/trajectory.SampleRate):tInfo.TimeOfArrival(end);
eulerAngles = eulerd(orient,'ZYX','frame');
plot(timeVector(2:end),eulerAngles(:,1), ...
    timeVector(2:end),eulerAngles(:,2), ...
    timeVector(2:end),eulerAngles(:,3));
title('Orientation Over Time')
legend('Rotation around Z-axis', ...
    'Rotation around Y-axis', ...
    'Rotation around X-axis', ...
    'Location','southwest')
xlabel('Time (seconds)')
ylabel('Rotation (degrees)')
grid on
figure(3)
```

```
plot(timeVector(2:end),vel(:,1), ...
    timeVector(2:end),vel(:,2), ...
    timeVector(2:end),vel(:,3));
title('Velocity Over Time')
legend('North','East','Down')
xlabel('Time (seconds)')
ylabel('Velocity (m/s)')
grid on
figure(4)
plot(timeVector(2:end),acc(:,1), ...
    timeVector(2:end),acc(:,2), ...
    timeVector(2:end),acc(:,3));
title('Acceleration Over Time')
legend('North','East','Down')
xlabel('Time (seconds)')
ylabel('Acceleration (m/s^2)')
grid on
figure(5)
plot(timeVector(2:end),angVel(:,1), ...
    timeVector(2:end), angVel(:,2), ...
    timeVector(2:end),angVel(:,3));
title('Angular Velocity Over Time')
legend('North','East','Down')
xlabel('Time (seconds)')
ylabel('Angular Velocity (rad/s)')
grid on
```






Note that while the generated trajectory now fits within the spatial boundaries, the acceleration and angular velocity of the trajectory are somewhat erratic. This is due to over-specifying waypoints.

## Algorithms

The waypointTrajectory System object defines a trajectory that smoothly passes through waypoints. The trajectory connects the waypoints through an interpolation that assumes the gravity direction expressed in the trajectory reference frame is constant. Generally, you can use waypointTrajectory to model platform or vehicle trajectories within a hundreds of kilometers distance span.

The planar path of the trajectory (the $x-y$ plane projection) consists of piecewise, clothoid curves. The curvature of the curve between two consecutive waypoints varies linearly with the curve length between them. The tangent direction of the path at each waypoint is chosen to minimize discontinuities in the curvature, unless the course is specified explicitly via the Course property or implicitly via the Velocities property. Once the path is established, the object uses cubic Hermite interpolation to compute the location of the vehicle throughout the path as a function of time and the planar distance traveled.

The normal component ( $z$-component) of the trajectory is subsequently chosen to satisfy a shapepreserving piecewise spline (PCHIP) unless the climb rate is specified explicitly via the ClimbRate property or the third column of the Velocities property. Choose the sign of the climb rate based on the selected ReferenceFrame:

- When an 'ENU' reference frame is selected, specifying a positive climb rate results in an increasing value of $z$.
- When an 'NED' reference frame is selected, specifying a positive climb rate results in a decreasing value of $z$.

You can define the orientation of the vehicle through the path in two primary ways:

- If the Orientation property is specified, then the object uses a piecewise-cubic, quaternion spline to compute the orientation along the path as a function of time.
- If the Orientation property is not specified, then the yaw of the vehicle is always aligned with the path. The roll and pitch are then governed by the AutoBank and AutoPitch property values, respectively.

| AutoBank | AutoPitch | Description |
| :--- | :--- | :--- |
| false | false | The vehicle is always level <br> (zero pitch and roll). This is <br> typically used for large <br> marine vessels. |
| false | true | The vehicle pitch is aligned <br> with the path, and its roll is <br> always zero. This is typically <br> used for ground vehicles. |
| true | false | The vehicle pitch and roll are <br> chosen so that its local $z$-axis <br> is aligned with the net <br> acceleration (including <br> gravity). This is typically used <br> for rotary-wing craft. |
| true | true | The vehicle roll is chosen so <br> that its local transverse plane <br> aligns with the net <br> acceleration (including <br> gravity). The vehicle pitch is <br> aligned with the path. This is <br> typically used for two-wheeled <br> vehicles and fixed-wing <br> aircraft. |

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
The object function, waypointInfo, does not support code generation.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

See Also
Objects
kinematicTrajectory
Introduced in R2019b

## lookupPose

Obtain pose information for certain time

## Syntax

[position,orientation, velocity,acceleration, angularVelocity] = lookupPose( traj, sampleTimes)

## Description

[position,orientation, velocity,acceleration,angularVelocity] = lookupPose( traj, sampleTimes) returns the pose information of the waypoint trajectory at the specified sample times. If any sample time is beyond the duration of the trajectory, the corresponding pose information is returned as NaN .

## Input Arguments

traj - Waypoint trajectory
waypointTrajectory object
Waypoint trajectory, specified as a waypointTrajectory object.

## sampleTimes - Sample times

$M$-element vector of nonnegative scalar
Sample times in seconds, specified as an $M$-element vector of nonnegative scalars.

## Output Arguments

## position - Position in local navigation coordinate system (m)

M-by-3 matrix
Position in the local navigation coordinate system in meters, returned as an M-by-3 matrix.
$M$ is specified by the sampleTimes input.
Data Types: double
orientation - Orientation in local navigation coordinate system
$M$-element quaternion column vector | 3 -by- 3 -by- $M$ real array
Orientation in the local navigation coordinate system, returned as an $M$-by-1 quaternion column vector or a 3-by-3-by-M real array.

Each quaternion or 3-by-3 rotation matrix is a frame rotation from the local navigation coordinate system to the current body coordinate system.
$M$ is specified by the sampleTimes input.
Data Types: double

## velocity - Velocity in local navigation coordinate system (m/s)

$M$-by-3 matrix
Velocity in the local navigation coordinate system in meters per second, returned as an $M$-by-3 matrix.
$M$ is specified by the sampleTimes input.
Data Types: double
acceleration - Acceleration in local navigation coordinate system (m/s²)
$M$-by-3 matrix
Acceleration in the local navigation coordinate system in meters per second squared, returned as an $M$-by-3 matrix.
$M$ is specified by the sampleTimes input.

## Data Types: double

angularVelocity - Angular velocity in local navigation coordinate system (rad/s)
M-by-3 matrix
Angular velocity in the local navigation coordinate system in radians per second, returned as an M-by-3 matrix.
$M$ is specified by the sampleTimes input.
Data Types: double

## See Also

Objects
waypointTrajectory
Functions
waypointInfo|perturbations | perturb

Introduced in R2019b

## waypointInfo

Get waypoint information table

## Syntax

trajectoryInfo = waypointInfo(trajectory)

## Description

trajectoryInfo = waypointInfo(trajectory) returns a table of waypoints, times of arrival, velocities, and orientation for the trajectory System object.

## Input Arguments

trajectory - Object of waypointTrajectory
object
Object of the waypointTrajectory System object.

## Output Arguments

## trajectoryInfo - Trajectory information

table
Trajectory information, returned as a table with variables corresponding to set creation properties: Waypoints, TimeOfArrival, Velocities, and Orientation.

The trajectory information table always has variables Waypoints and TimeOfArrival. If the Velocities property is set during construction, the trajectory information table additionally returns velocities. If the Orientation property is set during construction, the trajectory information table additionally returns orientation.

## See Also

## Objects

waypointTrajectory

## Functions

lookupPose | perturbations | perturb

## Introduced in R2019b

## perturb

Apply perturbations to object

## Syntax

offsets = perturb(obj)

## Description

offsets = perturb(obj) applies the perturbations defined on the object, obj and returns the offset values. You can define perturbations on the object by using the perturbations function.

## Examples

## Perturb Waypoint Trajectory

Define a waypoint trajectory. By default, this trajectory contains two waypoints.

```
traj = waypointTrajectory
traj =
    waypointTrajectory with properties:
        SampleRate: 100
        SamplesPerFrame: 1
            Waypoints: [2x3 double]
            TimeOfArrival: [2x1 double]
            Velocities: [2\times3 double]
            Course: [2x1 double]
            GroundSpeed: [2x1 double]
                ClimbRate: [2x1 double]
            Orientation: [2x1 quaternion]
                AutoPitch: 0
                    AutoBank: 0
        ReferenceFrame: 'NED'
```

Define perturbations on the Waypoints property and the TimeOfArrival property.

```
rng(2020);
perturbs1 = perturbations(traj,'Waypoints','Normal',1,1)
perturbs1=2\times3 table
        Property Type Value
    "Waypoints" "Normal" {[ [ 1]} {[ 1]}
    "TimeOfArrival" "None" {[NaN]} {[NaN]}
perturbs2 = perturbations(traj,'Time0fArrival','Selection',{[0;1],[0;2]})
```

```
perturbs2=2\times3 table
        Property Type Value
    "Waypoints"
"Normal"
"Selection" {1\times2 cell}
```

Perturb the trajectory.

```
offsets = perturb(traj)
offsets=2\times1 struct array with fields:
    Property
    Offset
    PerturbedValue
```

The Waypoints property and the TimeOfArrival property have changed.

```
traj.Waypoints
ans = 2×3
\begin{tabular}{rrr}
1.8674 & 1.0203 & 0.7032 \\
2.3154 & -0.3207 & 0.0999
\end{tabular}
traj.TimeOfArrival
ans = 2\times1
    0
    2
```


## Perturb Accuracy of insSensor

Create an insSensor object.

```
sensor = insSensor
sensor =
    insSensor with properties:
            MountingLocation: [0 0 0] m
                RollAccuracy: 0.2 deg
                    PitchAccuracy: 0.2 deg
                            YawAccuracy: 1 deg
            PositionAccuracy: [1 1 1] m
            VelocityAccuracy: 0.05 m/s
                AccelerationAccuracy: 0 m/s2
        AngularVelocityAccuracy: 0 deg/s
            TimeInput: 0
            RandomStream: 'Global stream'
```

Define the perturbation on the RollAccuracy property as three values with an equal possibility each.

```
values = {0.1 0.2 0.3}
values=1\times3 cell array
    {[0.1000]} {[0.2000]} {[0.3000]}
probabilities = [1/3 1/3 1/3]
probabilities = 1\times3
    0.3333 0.3333 0.3333
perturbations(sensor,'RollAccuracy','Selection',values,probabilities)
ans=7\times3 table
            Property
                                    Type
    "RollAccuracy"
    "PitchAccuracy"
    "YawAccuracy"
    "PositionAccuracy"
    "VelocityAccuracy"
    "AccelerationAccuracy"
    "AngularVelocityAccuracy"
"Selection"
"None"
"None"
"None"
"None"
"None"
"None"
```

Perturb the sensor object using the perturb function.

```
rng(2020)
```

perturb(sensor);
sensor
sensor =
insSensor with properties:
MountingLocation: [0 0 0] m
RollAccuracy: 0.5 deg
PitchAccuracy: 0.2 deg
YawAccuracy: 1 deg
PositionAccuracy: [lll 111$] ~ m$
VelocityAccuracy: $0.05 \mathrm{~m} / \mathrm{s}$
AccelerationAccuracy: $0 \mathrm{~m} / \mathrm{s}^{2}$
AngularVelocityAccuracy: 0 deg/s
TimeInput: 0
RandomStream: 'Global stream'

The RollAccuracy is perturbed to 0.5 deg.

## Perturb imuSensor Parameters

Create an imuSensor object and show its perturbable properties.

```
imu = imuSensor;
perturbations(imu)
ans=17\times3 table
```

Property Type
$\qquad$
"None" $\quad\{[\mathrm{NaN}]\} \quad\{[\mathrm{NaN}]\}$
"None" $\{[\mathrm{NaN}]\} \quad\{[\mathrm{NaN}]\}$
"None" $\{[\mathrm{NaN}]\} \quad\{[\mathrm{NaN}]\}$
"None" $\{[\mathrm{NaN}]\} \quad\{[\mathrm{NaN}]\}$
"None" $\quad\{[\mathrm{NaN}]\} \quad\{[\mathrm{NaN}]\}$
"None" $\{[\mathrm{NaN}]\} \quad\{[\mathrm{NaN}]\}$
"None" $\{[\mathrm{NaN}]\} \quad\{[\mathrm{NaN}]\}$
"None" $\quad\{[\mathrm{NaN}]\} \quad\{[\mathrm{NaN}]\}$
"None" $\{[\mathrm{NaN}]\} \quad\{[\mathrm{NaN}]\}$
"None" $\{[\mathrm{NaN}]\} \quad\{[\mathrm{NaN}]\}$
"None" $\quad\{[\mathrm{NaN}]\} \quad\{[\mathrm{NaN}]\}$
"None" $\quad\{[\mathrm{NaN}]\} \quad\{[\mathrm{NaN}]\}$
"None" $\{[\mathrm{NaN}]\} \quad\{[\mathrm{NaN}]\}$
"None" $\{[\mathrm{NaN}]\} \quad\{[\mathrm{NaN}]\}$
"None" $\{[\mathrm{NaN}]\} \quad\{[\mathrm{NaN}]\}$
"None" $\{[\mathrm{NaN}]\} \quad\{[\mathrm{NaN}]\}$

Specify the perturbation for the NoiseDensity property of the accelerometer as a uniform distribution.
perturbations(imu, 'Accelerometer.NoiseDensity', ...
'Uniform',1e-5,1e-3);
Specify the perturbation for the RandomWalk property of the gyroscope as a truncated normal distribution.

```
perts = perturbations(imu,'Gyroscope.RandomWalk', ...
    'TruncatedNormal',2,1e-5,0,Inf);
```

Load prerecorded IMU data.

```
load imuSensorData.mat
numSamples = size(orientations);
```

Simulate the imuSensor three times with different perturbation realizations.

```
rng(2021); % For repeatable results
numRuns = 3;
colors = ['b' 'r' 'g'];
for idx = 1:numRuns
    % Clone IMU to maintain original values
    imuCopy = clone(imu);
    % Perturb noise values
```

```
    offsets = perturb(imuCopy);
    % Obtain the measurements
    [accelReadings,gyroReadings] = imuCopy(accelerations,angularVelocities,orientations);
    % Plot the results
    plot(times,gyroReadings(:,3),colors(idx));
    hold on;
end
xlabel('Time (s)')
ylabel('Z-Component of Gyro Readings (rad/s)')
legend("First Pass","Second Pass","Third Pass");
hold off
```



## Input Arguments

obj - Object for perturbation
objects
Object for perturbation, specified as an object. The objects that you can perturb include:

- waypointTrajectory
- kinematicTrajectory
- insSensor
- imuSensor


## Output Arguments

offsets - Property offsets
array of structure
Property offsets, returned as an array of structures. Each structure contains these fields:

| Field Name | Description |
| :--- | :--- |
| Property | Name of perturbed property |
| Offset | Offset values applied in the perturbation |
| PerturbedValue | Property values after the perturbation |

## See Also

perturbations

## Introduced in R2020b

## perturbations

Perturbation defined on object

## Syntax

```
perturbs = perturbations(obj)
perturbs = perturbations(obj,property)
perturbs = perturbations(obj,property,'None')
perturbs = perturbations(obj,property,'Selection',values,probabilities)
perturbs = perturbations(obj,property,'Normal',mean,deviation)
perturbs = perturbations(obj,property,'TruncatedNormal',mean,deviation,
lowerLimit,upperLimit)
perturbs = perturbations(obj,property,'Uniform',minVal,maxVal)
perturbs = perturbations(obj,property,'Custom',perturbFcn)
```


## Description

perturbs = perturbations(obj) returns the list of property perturbations, perturbs, defined on the object, obj. The returned perturbs lists all the perturbable properties. If any property is not perturbed, then its corresponding Type is returned as "Null" and its corresponding Value is returned as $\{\mathrm{Null}, \mathrm{Null}\}$.
perturbs = perturbations(obj, property) returns the current perturbation applied to the specified property.
perturbs = perturbations(obj, property, 'None') defines a property that must not be perturbed.
perturbs = perturbations(obj,property,'Selection', values, probabilities) defines the property perturbation offset drawn from a set of values that have corresponding probabilities.
perturbs = perturbations(obj, property,'Normal',mean,deviation) defines the property perturbation offset drawn from a normal distribution with specified mean and standard deviation.
perturbs = perturbations(obj, property,'TruncatedNormal',mean, deviation, lowerLimit, upperLimit) defines the property perturbation offset drawn from a normal distribution with specified mean, standard deviation, lower limit, and upper limit.
perturbs = perturbations(obj, property,'Uniform',minVal,maxVal) defines the property perturbation offset drawn from a uniform distribution on an interval [minVal, maxValue].
perturbs = perturbations(obj, property, 'Custom', perturbFcn) enables you to define a custom function, perturbFcn, that draws the perturbation offset value.

## Examples

## Default Perturbation Properties of waypointTrajectory

Create a waypointTrajectory object.
traj = waypointTrajectory;
Show the default perturbation properties using the perturbations method.

```
perturbs = perturbations(traj)
perturbs=2\times3 table
        Property Type Value
    "Waypoints" "None"
    "TimeOfArrival" "None" {[NaN]} {[NaN]}
```


## Perturb Accuracy of insSensor

Create an insSensor object.

```
sensor = insSensor
sensor =
    insSensor with properties:
            MountingLocation: [0 0 0] m
            RollAccuracy: 0.2 deg
            PitchAccuracy: 0.2 deg
                            YawAccuracy: 1 deg
            PositionAccuracy: [l 1 1] m
            VelocityAccuracy: 0.05 m/s
            AccelerationAccuracy: 0 m/s}\mp@subsup{}{}{2
        AngularVelocityAccuracy: 0 deg/s
            TimeInput: 0
                        RandomStream: 'Global stream'
```

Define the perturbation on the RollAccuracy property as three values with an equal possibility each.

```
values = {0.1 0.2 0.3}
values=1\times3 cell array
    {[0.1000]} {[0.2000]} {[0.3000]}
probabilities = [1/3 1/3 1/3]
probabilities = 1×3
    0.3333 0.3333 0.3333
perturbations(sensor,'RollAccuracy','Selection',values,probabilities)
```

```
ans=7\times3 table
```

| Property | Type | Value |  |  |
| :---: | :---: | :---: | :---: | :---: |
| "RollAccuracy" | "Selection" | \{1x3 cell $\}$ | \{[0.3333 0.3333 | 0.3333] $\}$ |
| "PitchAccuracy" | "None" | \{[ NaN]\} | \{[ | NaN]\} |
| "YawAccuracy" | "None" | \{[ NaN]\} | \{ [ | NaN] $\}$ |
| "PositionAccuracy" | "None" | \{[ NaN]\} | \{ [ | NaN] $\}$ |
| "VelocityAccuracy" | "None" | \{[ NaN]\} | \{ [ | NaN] $\}$ |
| "AccelerationAccuracy" | "None" | \{[ NaN]\} | \{ [ | NaN]\} |
| "AngularVelocityAccuracy" | "None" | \{[ NaN]\} | \{ [ | NaN]\} |

Perturb the sensor object using the perturb function.

```
rng(2020)
```

perturb(sensor);
sensor
sensor =
insSensor with properties:
MountingLocation: [0 0 0] m
RollAccuracy: 0.5 deg
PitchAccuracy: 0.2 deg
YawAccuracy: 1 deg
PositionAccuracy: [1 1 1] m
VelocityAccuracy: $0.05 \mathrm{~m} / \mathrm{s}$
AccelerationAccuracy: $0 \mathrm{~m} / \mathrm{s}^{2}$
AngularVelocityAccuracy: 0 deg/s
TimeInput: 0
RandomStream: 'Global stream'

The RollAccuracy is perturbed to 0.5 deg.

## Perturb Waypoint Trajectory

Define a waypoint trajectory. By default, this trajectory contains two waypoints.

```
traj = waypointTrajectory
traj =
    waypointTrajectory with properties:
        SampleRate: 100
        SamplesPerFrame: 1
            Waypoints: [2x3 double]
        TimeOfArrival: [2x1 double]
            Velocities: [2x3 double]
            Course: [2x1 double]
            GroundSpeed: [2x1 double]
                ClimbRate: [2x1 double]
            Orientation: [2x1 quaternion]
                AutoPitch: 0
            AutoBank: 0
```

```
ReferenceFrame: 'NED'
```

Define perturbations on the Waypoints property and the TimeOfArrival property.
rng(2020);
perturbs1 = perturbations(traj,'Waypoints','Normal',1,1)
perturbs1=2×3 table
Property Type Value
"Waypoints" "Normal" \{[ 1$]\} \quad\left\{\left[\begin{array}{ll}1\end{array}\right]\right\}$
"TimeOfArrival" "None" \{[NaN]\} \{[NaN]\}

```
perturbs2 = perturbations(traj,'TimeOfArrival','Selection',{[0;1],[0;2]})
perturbs2=2\times3 table
    Property Type Value
    "Waypoints" "Normal" {[ 1]} {[ 1]}
    "TimeOfArrival" "Selection" {1x2 cell} {[0.5000 0.5000]}
```

Perturb the trajectory.

```
offsets = perturb(traj)
offsets=2\times1 struct array with fields:
    Property
    Offset
    PerturbedValue
```

The Waypoints property and the Time0fArrival property have changed.

```
traj.Waypoints
ans = 2\times3
    1.8674 }r\mathrm{ 1.0203 
traj.TimeOfArrival
ans = 2\times1
    0
    2
```


## Perturb imuSensor Parameters

Create an imuSensor object and show its perturbable properties.

```
imu = imuSensor;
perturbations(imu)
ans=17\times3 table
```

Property Type
"Accelerometer.MeasurementRange"
"Accelerometer.Resolution"
"Accelerometer. ConstantBias"
"Accelerometer.NoiseDensity"
"Accelerometer.BiasInstability"
"Accelerometer.RandomWalk"
"Accelerometer. TemperatureBias"
"Accelerometer.TemperatureScaleFactor"
"Gyroscope.MeasurementRange"
"Gyroscope. Resolution"
"Gyroscope. ConstantBias"
"Gyroscope. NoiseDensity"
"Gyroscope. BiasInstability"
"Gyroscope.RandomWalk"
"Gyroscope. TemperatureBias"
"Gyroscope.TemperatureScaleFactor"

| "None" | $\{[\mathrm{NaN}]\}$ | $\{[\mathrm{NaN}]\}$ |
| :--- | :--- | :--- |
| "None" | $\{[\mathrm{NaN}]\}$ | $\{[\mathrm{NaN}]\}$ |
| "None" | $\{[\mathrm{NaN}]\}$ | $\{[\mathrm{NaN}]\}$ |
| "None" | $\{[\mathrm{NaN}]\}$ | $\{[\mathrm{NaN}]\}$ |
| "None" | $\{[\mathrm{NaN}]\}$ | $\{[\mathrm{NaN}]\}$ |
| "None" | $\{[\mathrm{NaN}]\}$ | $\{[\mathrm{NaN}]\}$ |
| "None" | $\{[\mathrm{NaN}]\}$ | $\{[\mathrm{NaN}]\}$ |
| "None" | $\{[\mathrm{NaN}]\}$ | $\{[\mathrm{NaN}]\}$ |
| "None" | $\{[\mathrm{NaN}]\}$ | $\{[\mathrm{NaN}]\}$ |
| "None" | $\{[\mathrm{NaN}]\}$ | $\{[\mathrm{NaN}]\}$ |
| "None" | $\{[\mathrm{NaN}]\}$ | $\{[\mathrm{NaN}]\}$ |
| "None" | $\{[\mathrm{NaN}]\}$ | $\{[\mathrm{NaN}]\}$ |
| "None" | $\{[\mathrm{NaN}]\}$ | $\{[\mathrm{NaN}]\}$ |
| "None" | $\{[\mathrm{NaN}]\}$ | $\{[\mathrm{NaN}]\}$ |
| "None" | $\{[\mathrm{NaN}]\}$ | $\{[\mathrm{NaN}]\}$ |
| "None" | $\{[\mathrm{NaN}]\}$ | $\{[\mathrm{NaN}]\}$ |

Specify the perturbation for the NoiseDensity property of the accelerometer as a uniform distribution.

```
perturbations(imu,'Accelerometer.NoiseDensity', ...
```

    'Uniform',1e-5,1e-3) ;
    Specify the perturbation for the RandomWalk property of the gyroscope as a truncated normal distribution.

```
perts = perturbations(imu,'Gyroscope.RandomWalk', ...
    'TruncatedNormal',2,1e-5,0,Inf);
```

Load prerecorded IMU data.

```
load imuSensorData.mat
numSamples = size(orientations);
```

Simulate the imuSensor three times with different perturbation realizations.

```
rng(2021); % For repeatable results
numRuns = 3;
colors = ['b' 'r' 'g'];
for idx = 1:numRuns
    % Clone IMU to maintain original values
    imuCopy = clone(imu);
    % Perturb noise values
    offsets = perturb(imuCopy);
    % Obtain the measurements
    [accelReadings,gyroReadings] = imuCopy(accelerations,angularVelocities,orientations);
```

```
    % Plot the results
    plot(times,gyroReadings(:,3),colors(idx));
    hold on;
end
xlabel('Time (s)')
ylabel('Z-Component of Gyro Readings (rad/s)')
legend("First Pass","Second Pass","Third Pass");
hold off
```



## Input Arguments

obj - Object to be perturbed
objects
Object to be perturbed, specified as an object. The objects that you can perturb include:

- waypointTrajectory
- kinematicTrajectory
- insSensor
- imuSensor
property - Perturbable property
property name

Perturbable property, specified as a property name. Use perturbations to obtain a full list of perturbable properties for the specified obj.

For the imuSensor System object, you can perturb properties of its accelerometer, gyroscope, and magnetometer components. For more details, see the "Perturb imuSensor Parameters" on page 21573 example.

## values - Perturbation offset values

n-element cell array of property values
Perturbation offset values, specified as an n-element cell array of property values. The function randomly draws the perturbation value for the property from the cell array based on the values' corresponding probabilities specified in the probabilities input.

## probabilities - Drawing probabilities for each perturbation value

$n$-element array of nonnegative scalar
Drawing probabilities for each perturbation value, specified as an n-element array of nonnegative scalars, where $n$ is the number of perturbation values provided in the values input. The sum of all elements must be equal to one.

For example, you can specify a series of perturbation value-probability pair as $\{x 1, x 2, \ldots, x n\}$ and $\{p 1, p 2, \ldots, p n\}$, where the probability of drawing xi is pi ( $i=1,2, \ldots, n$ ).

## mean - Mean of normal or truncated normal distribution

scalar | vector | matrix
Mean of normal or truncated normal distribution, specified as a scalar, vector, or matrix. The dimension of mean must be compatible with the corresponding property that you perturb.

## deviation - Standard deviation of normal or truncated normal distribution <br> nonnegative scalar | vector of nonnegative scalar | matrix of nonnegative scalar

Standard deviation of normal or truncated normal distribution, specified as a nonnegative scalar, vector of nonnegative scalars, or matrix of nonnegative scalars. The dimension of deviation must be compatible with the corresponding property that you perturb.

## lowerLimit - Lower limit of truncated normal distribution scalar | vector | matrix

Lower limit of the truncated normal distribution, specified as a scalar, vector, or matrix. The dimension of lowerLimit must be compatible with the corresponding property that you perturb.

```
upperLimit - Upper limit of truncated normal distribution
scalar | vector | matrix
```

Upper limit of the truncated normal distribution, specified as a scalar, vector, or matrix. The dimension of upperLimit must be compatible with the corresponding property that you perturb.

## minVal - Minimum value of uniform distribution interval

scalar | vector | matrix
Minimum value of the uniform distribution interval, specified as a scalar, vector, or matrix. The dimension of minVal must be compatible with the corresponding property that you perturb.

## maxVal - Maximum value of uniform distribution interval

scalar | vector | matrix
Maximum value of the uniform distribution interval, specified as a scalar, vector, or matrix. The dimension of maxVal must be compatible with the corresponding property that you perturb.

## perturbFcn - Perturbation function

function handle
Perturbation function, specified as a function handle. The function must have this syntax:

```
offset = myfun(propVal)
```

where propVal is the value of the property and offset is the perturbation offset for the property.

## Output Arguments

## perturbs - Perturbations defined on object <br> table of perturbation property

Perturbations defined on the object, returned as a table of perturbation properties. The table has three columns:

- Property - Property names.
- Type - Type of perturbations, returned as "None", "Selection", "Normal", "TruncatedNormal", "Uniform", or "Custom".
- Value - Perturbation values, returned as a cell array.


## More About

## Specify Perturbation Distributions

You can specify the distribution for the perturbation applied to a specific property.

- Selection distribution - The function defines the perturbation offset as one of the specified values with the associated probability. For example, if you specify the values as [1 2] and specify the probabilities as [0.7 0.3], then the perturb function adds an offset value of 1 to the property with a probability of 0.7 and add an offset value of 2 to the property with a probability of 0.3 . Use selection distribution when you only want to perturb the property with a number of discrete values.
- Normal distribution - The function defines the perturbation offset as a value drawn from a normal distribution with the specified mean and standard deviation (or covariance). Normal distribution is the most commonly used distribution since it mimics the natural perturbation of parameters in most cases.
- Truncated normal distribution - The function defines the perturbation offset as a value drawn from a truncated normal distribution with the specified mean, standard deviation (or covariance), lower limit, and upper limit. Different from the normal distribution, the values drawn from a truncated normal distribution are truncated by the lower and upper limit. Use truncated normal distribution when you want to apply a normal distribution, but the valid values of the property are confined in an interval.
- Uniform distribution - The function defines the perturbation offset as a value drawn from a uniform distribution with the specified minimum and maximum values. All the values in the interval (specified by the minimum and maximum values) have the same probability of realization.
- Custom distribution - Customize your own perturbation function. The function must have this syntax:

```
offset = myfun(propVal)
```

where propVal is the value of the property and offset is the perturbation offset for the property.

This figure shows probability density functions for a normal distribution, a truncated normal distribution, and a uniform distribution, respectively.


## See Also

perturb

Introduced in R2020b

## wheelEncoderAckermann

Simulate wheel encoder sensor readings for Ackermann vehicle

## Description

The wheelEncoderAckermann System object computes wheel encoder tick readings based on the pose input of an Ackermann vehicle.

To obtain the encoder tick readings:
1 Create the wheelEncoderAckermann object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

encoder = wheelEncoderAckermann
encoder= wheelEncoderAckermann(Name,Value)

## Description

encoder = wheelEncoderAckermann creates a wheelEncoderAckermann System object, encoder.
encoder= wheelEncoderAckermann(Name,Value) sets properties for the encoder using one or more name-value pairs. For example, wheelAckermann('SampleRate' '120) sets the sample rate of the encoder to 120 Hz . Unspecified properties have default values. Enclose each property name in quotes.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## SampleRate - Sample rate of encoder

100 (default) | positive scalar
Sample rate of the encoder, specified as a positive scalar in Hz .
Example: 'SampleRate',100

Data Types: double

## TicksPerRevolution - Number of encoder ticks per wheel revolution <br> [2048 20482048 2048] (default) | four-element vector of positive integers

Number of encoder ticks per wheel revolution, specified as a four-element vector of positive integers. The first, second, third, and fourth elements are for the back-left, back-right, front-left, and frontright wheels, respectively.
Data Types: double
WheelRadius - Wheel radius
[0.35 0.35 0.35 0.35] (default)|four-element vector of positive scalars
Wheel radius, specified as a four-element vector of positive scalars in meters. The first, second, third, and fourth elements are for the back-left, back-right, front-left, and front-right wheels, respectively.
Data Types: double
WheelRadiusBias - Bias of wheel radius
[0 0 0 0] (default) |four-element vector of scalars
Bias of the wheel radius, specified as a four-element vector of scalars in meters. The first, second, third, and fourth elements are for the back-left, back-right, front-left, and front-right wheels, respectively.
Data Types: double
WheelPositionAccuracy - Standard deviation of wheel position error
[0 0 0 0] (default) |four-element vector of nonnegative scalars
Standard deviation of wheel position error, specified as a four-element vector of nonnegative scalars in radians. The first, second, third, and fourth elements are for the back-left, back-right, front-left, and front-right wheels, respectively.
Data Types: double

## SlipRatio - Slip or skid ratio of wheel

[00000] (default) |four-element vector of scalars
Slip or skid ratio of the wheel, specified as a four-element vector of scalars in which each scalar is larger than or equal to -1 . The first, second, third, and fourth elements are for the back-left, backright, front-left, and front-right wheels, respectively.

- For a wheel that slips (over rotation), specify it as a positive value. A higher value denotes more slipping.
- For a wheel that skids (under rotation), specify it as a negative value larger than or equal to -1. A lower value denotes more skidding. For a wheel that does not rotate, specify it as -1 .

Data Types: double

## TrackWidth - Distance between wheel axles

## [1.572 1.572] (default) | two-element vector of positive scalars

Distance between the wheel axles, specified as a two-element vector of positive scalars in meters. The first element is for the back track, and the second element is for the front track.

## Data Types: double

TrackWidthBias - Bias of track width
0 (default) | two-element vector of scalars
Bias of track width, specified as a two-element vector of scalars in meters. The first element is for the back track, and the second element is for the front track.
Data Types: double

## WheelBase - Distance between front and rear axles

### 2.818 (default) | positive scalar

Distance between the front and the rear axles, specified as a positive scalar in meters.
Data Types: double

## RandomStream - Random number source

'Global stream' (default)|'mt19937ar with seed'
Random number source, specified as a character vector or string:

- 'Global stream' -- Random numbers are generated using the current global random number stream.
- 'mt19937ar with seed' -- Random numbers are generated using the mt19937ar algorithm with the seed specified by the Seed property.

Data Types: char | string

## Seed - Initial seed

67 (default) | nonnegative integer
Initial seed of an mt19937ar random number generator algorithm, specified as a nonnegative integer.

## Dependencies

To enable this property, set RandomStream to 'mt19937ar with seed'.

## Usage

## Syntax

ticks = encoder(velocity, angularVelocity,orientation)

## Description

ticks = encoder(velocity, angularVelocity,orientation) return the wheel tick readings, ticks, form velocity, angular velocity, and orientation information.

## Input Arguments

## velocity - Velocity of vehicle

N -by-3 matrix of scalars
Velocity of the vehicle in the local navigation frame, specified as an $N$-by- 3 matrix of scalars in $\mathrm{m} / \mathrm{s}$. $N$ is the number of samples.

## angularVelocity - Angular velocity of vehicle

## N -by-3 matrix of scalars

Angular velocity of the vehicle in the local navigation frame, specified as an $N$-by- 3 matrix of scalars in rad/s. $N$ is the number of samples.

## orientation - orientation of vehicle

$N$-element vector of quaternion | 3-by-3-by- $N$ array of rotation matrices
Orientation of the vehicle in the local navigation frame, specified as an $N$-element vector of quaternion or a 3 -by-3-by- $N$ array of rotation matrices. $N$ is the number of samples. Each quaternion or rotation matrix is a frame rotation from the local navigation coordinate system to the current vehicle body coordinate system.

## Output Arguments

## ticks - Number of wheel ticks per time step

$N$-by-4 matrix of nonnegative integers
Number of wheel ticks the vehicle moved per time step, returned as an $N$-by-4 matrix of nonnegative integers. $N$ is the number of samples. The first, second, third, and fourth columns are for the backleft, back-right, front-left, and front-right wheels, respectively.

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Common to All System Objects

```
clone Create duplicate System object
step Run System object algorithm
release Release resources and allow changes to System object property values and input
    characteristics
reset Reset internal states of System object
isLocked Determine if System object is in use
```


## Examples

## Generate Wheel Ticks from Ackermann Vehicle Pose

Create the wheel encoder sensor.
encoder = wheelEncoderAckermann;
Define poses of the vehicle.

```
orient = [quaternion([60 0 0],'eulerd','ZYX','frame'); quaternion([45 0 0], 'eulerd', 'ZYX', 'fr
vel = [1 0 0; 0 1 0];
angvel = [0 0 0.2; 0 0 0.1];
Generate wheel ticks from the poses.
```

ticks = encoder(vel, angvel,orient)
ticks $=2 \times 4$

| 3 | 6 | 6 | 8 |
| :--- | :--- | :--- | :--- |

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

Introduced in R2020b

## wheelEncoderBicycle

Simulate wheel encoder sensor readings for bicycle vehicle

## Description

The wheelEncoderBicycle System object computes wheel encoder tick readings based on the pose input for a bicycle vehicle.

To obtain the encoder tick readings:
1 Create the wheelEncoderBicycle object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

encoder $=$ wheelEncoderBicycle
encoder= wheelEncoderBicycle(Name,Value)

## Description

encoder $=$ wheelEncoderBicycle creates a wheelEncoderBicycle System object, encoder.
encoder= wheelEncoderBicycle(Name,Value) sets properties for the encoder using one or more name-value pairs. For example, wheelEncoderBicycle('SampleRate', 120) sets the sample rate of the encoder to 120 Hz . Unspecified properties have default values. Enclose each property name in quotes.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## SampleRate - Sample rate of encoder

100 (default) | positive scalar
Sample rate of the encoder, specified as a positive scalar in Hz.
Data Types: double

## TicksPerRevolution - Number of encoder ticks per wheel revolution

## [2048 2048] (default) | two-element vector of positive integers

Number of encoder ticks per wheel revolution, specified as a two-element vector of positive integers. The first element is for the back wheel, and the second element is for the front wheel.

Data Types: double

## WheelRadius - Wheel radius

[0.35 0.35] (default) | two-element vector of positive scalars
Wheel radius, specified as a two-element vector of positive scalars in meters. The first element is for the back wheel, and the second element is for the front wheel.
Data Types: double

## WheelRadiusBias - Bias of wheel radius

[0 0] (default) | two-element vector of scalars
Bias of the wheel radius, specified as a two-element vector of scalars in meters. The first element is for the back wheel, and the second element is for the front wheel.
Data Types: double

## WheelPositionAccuracy - Standard deviation of wheel position error

[0 0 ] (default) | two-element vector of nonnegative scalars
Standard deviation of wheel position error, specified as a two-element vector of nonnegative scalars in radians. The first element is for the back wheel, and the second element is for the front wheel.
Data Types: double

## SlipRatio - Slip or skid ratio of wheel

[0 0 ] (default) | two-element vector of scalar
Slip or skid ratio of the wheel, specified as a two-element vector of scalars in which each scalar is larger than or equal to -1 . The first element is for the back wheel, and the second element is for the front wheel.

- For a wheel that slips (over rotation), specify it as a positive value. A higher value denotes more slipping.
- For a wheel that skids (under rotation), specify it as a negative value larger than or equal to -1 . A lower value denotes more skidding. For a wheel that does not rotate, specify it as -1 .

Data Types: double

## WheelBase - Distance between front and rear wheels

2.818 (default) | positive scalar

Distance between the front and the rear wheels, specified as a positive scalar in meters.
Data Types: double
RandomStream - Random number source
'Global stream' (default)|'mt19937ar with seed'
Random number source, specified as a character vector or string:

- 'Global stream' -- Random numbers are generated using the current global random number stream.
- 'mt19937ar with seed' -- Random numbers are generated using the mt19937ar algorithm with the seed specified by the Seed property.

Data Types: char|string

## Seed - Initial seed of mt19937ar random number generator <br> 67 (default) | nonnegative integer

Initial seed of an mt19937ar random number generator algorithm, specified as a nonnegative integer.

## Dependencies

To enable this property, set RandomStream to 'mt19937ar with seed'.

## Usage

## Syntax

ticks = encoder(velocity, angularVelocity,orientation)

## Description

ticks = encoder(velocity, angularVelocity,orientation) return the wheel tick readings, ticks, from velocity, angular velocity, and orientation information.

## Input Arguments

## velocity - Velocity of vehicle

N -by-3 matrix of scalars
Velocity of the vehicle in the local navigation frame, specified as an $N$-by- 3 matrix of scalars in $\mathrm{m} / \mathrm{s}$. $N$ is the number of samples.

## angularVelocity - Angular velocity of vehicle

## N -by-3 matrix of scalars

Angular velocity of the vehicle in the local navigation frame, specified as an N -by- 3 matrix of scalars in rad/s. $N$ is the number of samples.

## orientation - orientation of vehicle

$N$-element vector of quaternion | 3-by-3-by- $N$ array of rotation matrices
Orientation of the vehicle in the local navigation frame, specified as an $N$-element vector of quaternion or a 3-by-3-by- $N$ array of rotation matrices. $N$ is the number of samples. Each quaternion or rotation matrix is a frame rotation from the local navigation coordinate system to the current vehicle body coordinate system.

## Output Arguments

## ticks - Number of wheel ticks per time step

$N$-by-2 matrix of integer

Number of wheel ticks the vehicle moved per time step, returned as an $N$-by- 2 matrix of integers. $N$ is the number of samples. The first column is for the back wheel, and the second column is for the front wheel.

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:
release(obj)

## Common to All System Objects

clone Create duplicate System object
step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object
isLocked Determine if System object is in use

## Examples

## Generate Wheel Ticks from Bicycle Vehicle Pose

Create the wheel encoder sensor.
encoder = wheelEncoderBicycle;
Define poses of the vehicle.
orient = [quaternion([90 0 0],'eulerd','ZYX','frame'); quaternion([45 0 0], 'eulerd', 'ZYX', 'fr vel = [1 00; 0 1 0];
angvel = [0 0 0.2; 000.1$]$;
Generate wheel ticks from the poses.
ticks = encoder(vel,angvel,orient)
ticks $=2 \times 2$
$0 \quad 5$
$6 \quad 7$

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

See Also

Introduced in R2020b

## wheelEncoderDifferentialDrive

Simulate wheel encoder sensor readings for differential drive vehicle

## Description

The wheelEncoderDifferentialDrive System object computes wheel encoder tick readings based on the pose input of a differential drive vehicle.

To obtain the encoder tick readings:
1 Create the wheelEncoderDifferentialDrive object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

encoder = wheelEncoderDifferentialDrive encoder= wheelEncoderDifferentialDrive(Name,Value)

## Description

encoder = wheelEncoderDifferentialDrive creates a wheelEncoderDifferentialDrive System object, encoder.
encoder= wheelEncoderDifferentialDrive(Name,Value) sets properties for the encoder using one or more name-value pairs. For example, wheelEncoderDifferentialDrive('SampleRate',120) sets the sample rate of the encoder to 120 Hz . Unspecified properties have default values. Enclose each property name in quotes.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## SampleRate - Sample rate of encoder

100 (default) | positive scalar
Sample rate of the encoder, specified as a positive scalar in Hz .
Data Types: double

## TicksPerRevolution - Number of encoder ticks per wheel revolution

[2048 2048] (default)| two-element vector of positive integers
Number of encoder ticks per wheel revolution, specified as a two-element vector of positive integers. The first element is for the left wheel, and the second element is for the right wheel.

Data Types: double
WheelRadius - Wheel radius
[0.35 0.35] (default) |two-element vector of positive scalars
Wheel radius, specified as a two-element vector of positive scalars in meters. The first element is for the left wheel, and the second element is for the right wheel.

Data Types: double

## WheelRadiusBias - Bias of wheel radius

[0 0] (default) | two-element vector of scalars
Bias of the wheel radius, specified as a two-element vector of scalars in meters. The first element is for the left wheel, and the second element is for the right wheel.

## Data Types: double

## WheelPositionAccuracy - Standard deviation of wheel position error

[0 0] (default) | two-element vector of nonnegative scalar
Standard deviation of wheel position error, specified as a two-element vector of nonnegative scalars in radians. The first element is for the left wheel, and the second element is for the right wheel.
Data Types: double

## SlipRatio - Slip or skid ratio of wheel

[0 0] (default) | two-element vector of scalar
Slip or skid ratio of the wheel, specified as a two-element vector of scalars in which each scalar is larger than or equal to - 1 . The first element is for the left wheel, and the second element is for the right wheel.

- For a wheel that slips (over rotation), specify it as a positive value. A higher value denotes more slipping.
- For a wheel that skids (under rotation), specify it as a negative value larger than or equal to -1. A lower value denotes more skidding. For a wheel that does not rotate, specify it as -1 .

Data Types: double

## TrackWidth - Distance between wheel axles

1.572 (default) | positive scalar

Distance between the wheel axles, specified as a positive scalar in meters.
Data Types: double
TrackWidthBias - Bias of track width
0 (default) | scalar
Bias of track width, specified as a scalar in meters.

## Data Types: double

## RandomStream - Random number source

'Global stream' (default)|'mt19937ar with seed'
Random number source, specified as a character vector or string:

- 'Global stream' -- Random numbers are generated using the current global random number stream.
- 'mt19937ar with seed' -- Random numbers are generated using the mt19937ar algorithm with the seed specified by the Seed property.

Data Types: char|string

## Seed - Initial seed

67 (default) | nonnegative integer
Initial seed of an mt19937ar random number generator algorithm, specified as a nonnegative integer.

## Dependencies

To enable this property, set RandomStream to 'mt19937ar with seed'.

## Usage

## Syntax

ticks = encoder(velocity,angularVelocity,orientation)

## Description

ticks = encoder(velocity, angularVelocity,orientation) return the wheel tick readings, ticks, form velocity, angular velocity, and orientation information.

## Input Arguments

## velocity - Velocity of vehicle

N -by-3 matrix of scalars
Velocity of the vehicle in the local navigation frame, specified as an $N$-by- 3 matrix of scalars in $\mathrm{m} / \mathrm{s}$. $N$ is the number of samples.

## angularVelocity - Angular velocity of vehicle

N -by-3 matrix of scalars
Angular velocity of the vehicle in the local navigation frame, specified as an N -by- 3 matrix of scalars in rad/s. $N$ is the number of samples.

## orientation - orientation of vehicle

$N$-element vector of quaternion | 3-by-3-by- $N$ array of rotation matrices
Orientation of the vehicle in the local navigation frame, specified as an $N$-element vector of quaternion or a 3 -by-3-by- $N$ array of rotation matrices. $N$ is the number of samples. Each quaternion or rotation matrix is a frame rotation from the local navigation coordinate system to the current vehicle body coordinate system.

## Output Arguments

## ticks - Number of wheel ticks per time step

$N$-by-2 matrix of nonnegative integers
Number of wheel ticks the vehicle moved per time step, returned as an $N$-by- 2 matrix of integers. $N$ is the number of samples. The first column is for the left wheel, and the second column is for the right wheel.

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:
release(obj)

## Common to All System Objects

| clone | Create duplicate System object |
| :--- | :--- |
| step | Run System object algorithm |
| release | Release resources and allow changes to System object property values and input |
| characteristics |  |
| reset | Reset internal states of System object |
| isLocked | Determine if System object is in use |

## Examples

## Generate Wheel Ticks from Differential Drive Vehicle Pose

Create the wheel encoder sensor.

```
encoder = wheelEncoderDifferentialDrive;
```

Define poses of the vehicle.

```
orient = [quaternion([60 0 0],'eulerd','ZYX','frame'); quaternion([45 0 0], 'eulerd', 'ZYX', 'fr
vel = [1 0 0; 0 1 0];
angvel = [0 0 0.2; 0 0 0.1];
Generate wheel ticks from the poses.
ticks = encoder(vel, angvel,orient)
ticks \(=2 \times 2\)
36
\(6 \quad 7\)
```


## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{Tm}}$.

Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

Introduced in R2020b

## wheelEncoderUnicycle

Simulate wheel encoder sensor readings for unicycle vehicle

## Description

The wheelEncoderUnicycle System object computes wheel encoder tick readings based on the pose input of a unicycle vehicle.

To obtain the encoder tick readings:
1 Create the wheelEncoderUnicycle object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

encoder = wheelEncoderUnicycle encoder = wheelEncoderUnicycle(Name,Value)

## Description

encoder $=$ wheelEncoderUnicycle creates a wheelEncoderUnicycle System object encoder.
encoder = wheelEncoderUnicycle(Name,Value) sets properties for the encoder using one or more name-value pairs. For example, wheelEncoderUnicycle('SampleRate', 120) sets the sample rate of the encoder to 120 Hz . Unspecified properties have default values. Enclose each property name in quotes.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## SampleRate - Sample rate of encoder

100 (default) | positive scalar
Sample rate of the encoder, specified as a positive scalar in Hz .
Data Types: double

## TicksPerRevolution - Number of encoder ticks per wheel revolution 2048 (default) | positive integer

Number of encoder ticks per wheel revolution, specified as a positive integer.
Data Types: double

## WheelRadius - Wheel radius

0.35 (default) | positive scalar

Wheel radius, specified as a positive scalar in meters.
Data Types: double

## WheelRadiusBias - Bias of wheel radius

0 (default) | scalar
Bias of the wheel radius, specified as a scalar in meters.
Data Types: double

## WheelPositionAccuracy - Standard deviation of wheel position error

0 (default) | nonnegative scalar
Standard deviation of wheel position error, specified as a nonnegative scalar in radians.
Data Types: double

## SlipRatio - Slip or skid ratio of wheel <br> 0 (default) | scalar

Slip or skid ratio of the wheel, specified as a scalar larger than or equal to -1 .

- For a wheel that slips (over rotation), specify it as a positive value. A higher value denotes more slipping.
- For a wheel that skids (under rotation), specify it as a negative value larger than or equal to -1. A lower value denotes more skidding. For a wheel that does not rotate, specify it as -1 .


## Data Types: double

## RandomStream - Random number source

'Global stream' (default)|'mt19937ar with seed'
Random number source, specified as a character vector or string:

- 'Global stream' -- Random numbers are generated using the current global random number stream.
- 'mt19937ar with seed' -- Random numbers are generated using the mt19937ar algorithm with the seed specified by the Seed property.

Data Types: char | string

## Seed - Initial seed of mt19937ar random number generator algorithm

67 (default) | nonnegative integer
Initial seed of an mt19937ar random number generator algorithm, specified as a nonnegative integer.

## Dependencies

To enable this property, set RandomStream to 'mt19937ar with seed'.

## Usage

## Syntax

ticks = encoder(velocity,angularVelocity,orientation)

## Description

ticks = encoder(velocity, angularVelocity,orientation) return the wheel tick readings ticks from the specified velocity, angular velocity, and orientation information.

## Input Arguments

## velocity - Velocity of vehicle

N -by-3 matrix of scalars
Velocity of the vehicle in the local navigation frame, specified as an $N$-by- 3 matrix of scalars in $\mathrm{m} / \mathrm{s} . N$ is the number of samples.

## angularVelocity - Angular velocity of vehicle

$N$-by-3 matrix of scalars
Angular velocity of the vehicle in the local navigation frame, specified as an N -by- 3 matrix of scalars in rad/s. $N$ is the number of samples.

## orientation - orientation of vehicle

$N$-element vector of quaternion | 3 -by- 3 -by- $N$ array of rotation matrices
Orientation of the vehicle in the local navigation frame, specified as an $N$-element vector of quaternion or a 3 -by-3-by- $N$ array of rotation matrices. $N$ is the number of samples. Each quaternion or rotation matrix is a frame rotation from the local navigation coordinate system to the current vehicle body coordinate system.

## Output Arguments

## ticks - Number of wheel ticks per time step

$N$-element vector of nonnegative integers
Number of wheel ticks the vehicle moved per time step, returned as an $N$-element vector of nonnegative integers. $N$ is the number of samples.

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Common to All System Objects

| clone | Create duplicate System object |
| :--- | :--- |
| step | Run System object algorithm |
| release | Release resources and allow changes to System object property values and input |
| characteristics |  |
| reset | Reset internal states of System object |
| isLocked | Determine if System object is in use |

## Examples

## Generate Wheel Ticks from Unicycle Vehicle Pose

Create the wheel encoder sensor.
encoder = wheelEncoderUnicycle;
Define poses of the vehicle.

```
orient = [quaternion([90 0 0],'eulerd','ZYX','frame'); quaternion([45 0 0], 'eulerd', 'ZYX', 'fr
vel = [1 0 0; 0 1 0];
angvel = [0 0 0.2; 0 0 0.1];
```

Generate wheel ticks from the poses.
ticks = encoder(vel, angvel,orient)
ticks $=2 \times 1$
0
6

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

Introduced in R2020b

## wheelEncoderOdometryAckermann

Compute Ackermann vehicle odometry using wheel encoder ticks and steering angle

## Description

The wheelEncoderOdometryAckermann System object computes Ackermann vehicle odometry using the wheel encoder ticks and steering angle of the vehicle.

To compute Ackermann vehicle odometry:
1 Create the wheelEncoderOdometryAckermann object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

```
whlEncOdom = wheelEncoderOdometryAckermann
whlEncOdom = wheelEncoderOdometryAckermann(encoder)
whlEncOdom = wheelEncoderOdometryAckermann(Name,Value)
```


## Description

whlEncOdom = wheelEncoderOdometryAckermann creates a wheelEncoderOdometryAckermann System object with default property values.
whlEncOdom = wheelEncoderOdometryAckermann(encoder) creates a wheelEncoder0dometryAckermann System object using the specified wheelEncoderAckermann System object, encoder, to set properties.
whlEncOdom = wheelEncoderOdometryAckermann(Name,Value) sets properties using one or more name-value pairs. Unspecified properties have default values. Enclose each property name in quotes.

For example, whlEncOdom = wheelEncoderOdometryAckermann('SampleRate',100) sets the sample rate of the sensor to 100 Hz .

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## SampleRate - Sample rate of sensor

100 (default) | positive scalar
Sample rate of sensor, specified as a positive scalar in hertz.
Example: 'SampleRate',100
Data Types: double

## TicksPerRevolution - Number of encoder ticks per wheel revolution

[2048 2048] (default) | positive integer | two-element vector of positive integers
Number of encoder ticks per wheel revolution, specified as a positive integer or two-element vector of positive integers.

When specifying this value as a two-element vector, the first element corresponds to the back left wheel and the second to the back right wheel.
Example: 'TicksPerRevolution',[2048 2048]
Data Types: double

## WheelRadius - Wheel radius

[0.35 0.35] (default) | positive scalar | two-element vector of positive numbers
Wheel radius, specified as a positive scalar or two-element vector of positive numbers in meters.
When specifying this value as a two-element vector, the first element corresponds to the back left wheel and the second to the back right wheel.
Example: 'WheelRadius',[0.35 0.35]
Data Types: double

## TrackWidth - Distance between wheels on axle

1.572 (default) | positive scalar

Distance between the wheels on the axle, specified as a positive scalar in meters.
Example: 'TrackWidth',1.572
Data Types: double

## WheelBase - Distance between front and rear axle

2.818 (default) | positive scalar

Distance between the front and rear axle, specified as a positive scalar in meters.
Example: 'WheelBase',2.818
Data Types: double
InitialPose - Initial pose of vehicle
[0 0 0] (default)| three-element vector
Initial pose of the vehicle, specified as three-element vector of the form [ $X$ Y Yaw]. $X$ and $Y$ specify the vehicle position in meters. Yaw specifies the vehicle orientation in radians. All values are in the local navigation coordinate system.
Example: 'InitialPose', [0 0 0]

## Usage

## Syntax

pose $=$ whlEncOdom(ticks,steer)
[pose,velocity] = whlEncOdom(ticks,steer)

## Description

pose $=$ whlEncOdom(ticks,steer) computes the odometry of an Ackermann vehicle using the specified wheel encoder ticks ticks and steering angle steer, and returns the position and orientation of the vehicle in the local navigation coordinate system.
[pose, velocity] = whlEncOdom(ticks,steer) additionally returns the linear and angular velocity of the vehicle in the local navigation coordinate system.

## Input Arguments

## ticks - Number of wheel encoder ticks

$n$-by-2 matrix
Number of wheel encoder ticks, specified as an $n$-by- 2 matrix. $n$ is the number of samples in the current frame.

Each row of the matrix specifies wheel encoder ticks in the form [ticksBackLeft ticksBackRight], where ticksBackLeft and ticksBackRight specify the number of ticks for the back left and back right wheels, respectively.

```
Example: [5 5; 2 2]
```

Data Types: single | double

## steer - Steering angle of vehicle

$n$-element column vector
Steering angle of the vehicle, specified as an $n$-element column vector in radians. $n$ is the number of samples in the current frame.

Example: [0.2; 0.2]
Data Types: single | double

## Output Arguments

## pose - Position and orientation of vehicle

n-by-3 matrix
Position and orientation of the vehicle, returned as an $n$-by- 3 matrix. $n$ is the number of samples in the current frame. Each row of the matrix specifies the position and orientation of a sample in the form [ $X$ Y Yaw]. $X$ and $Y$ specify the vehicle position in meters. Yaw specifies the vehicle orientation in radians. All values are in the local navigation coordinate system.
Data Types: single|double

## velocity - Linear and angular velocity of vehicle

$n$-by-3 matrix
Linear and angular velocity of the vehicle, returned as an $n$-by- 3 matrix. $n$ is the number of samples in the current frame. Each row of the matrix specifies the linear and angular velocity of a sample in the form [velX velY yawRate]. velX and velY specify the linear velocity of the vehicle in meters per second. yawRate specifies the angular velocity of the vehicle in radians per second. All values are in the local navigation coordinate system.
Data Types: single | double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Common to All System Objects

```
clone Create duplicate System object
step Run System object algorithm
release Release resources and allow changes to System object property values and input
    characteristics
reset Reset internal states of System object
isLocked Determine if System object is in use
```


## Examples

## Compute Ackermann Vehicle Odometry Using Wheel Encoder Ticks and Steering Angle

Create a wheelEncoderOdometryAckermann System object.
whlEncOdom = wheelEncoderOdometryAckermann;
Specify the number of wheel encoder ticks and the steering angle.

```
ticks = [5 5; 2 2];
steer = [0.2; 0.2];
```

Compute the Ackermann vehicle odometry.

```
[pose,vel] = whlEncOdom(ticks,steer)
pose = 2\times3
    0.0053689 1.0368e-06 
vel = 2\times3
    0.53689 0.00020735 0.038621
    0.21476 0.00011612 0.015448
```


## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

wheelEncoderAckermann | wheelEncoderOdometryBicycle | wheelEncoderOdometryDifferentialDrive | wheelEncoderOdometryUnicycle

Introduced in R2020b

## wheelEncoderOdometryBicycle

Compute bicycle odometry using wheel encoder ticks and steering angle

## Description

The wheelEncoderOdometryBicycle System object computes bicycle odometry using the wheel encoder ticks and steering angle of the vehicle.

To compute bicycle odometry:
1 Create the wheelEncoderOdometryBicycle object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

```
whlEncOdom = wheelEncoderOdometryBicycle
whlEncOdom = wheelEncoderOdometryBicycle(encoder)
whlEncOdom = wheelEncoderOdometryBicycle(Name,Value)
Description
```

whlEncOdom = wheelEncoderOdometryBicycle creates a wheelEncoder0dometryBicycle System object with default property values.
whlEncOdom = wheelEncoderOdometryBicycle(encoder) creates a wheelEncoderOdometryBicycle System object using the specified wheelEncoderBicycle System object, encoder, to set properties.
whlEncOdom = wheelEncoderOdometryBicycle(Name,Value) sets properties using one or more name-value pairs. Unspecified properties have default values. Enclose each property name in quotes.

For example, whlEncOdom = wheelEncoderOdometryBicycle('SampleRate',100) sets the sample rate of the sensor to 100 Hz .

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## SampleRate - Sample rate of sensor

100 (default) | positive scalar
Sample rate of sensor, specified as a positive scalar in hertz.
Example: 'SampleRate',100
Data Types: double

## TicksPerRevolution - Number of encoder ticks per wheel revolution

2048 (default) | positive integer
Number of encoder ticks per wheel revolution, specified as a positive integer. This value corresponds to the rear wheel of the bicycle.

## Example: 'TicksPerRevolution',2048

Data Types: double

## WheelRadius - Wheel radius

0.35 (default) | positive scalar

Wheel radius, specified as a positive scalar in meters.
Example: 'WheelRadius',0.35
Data Types: double

## WheelBase - Distance between front and rear axle

2.818 (default) | positive scalar

Distance between front and rear axle, specified as a positive scalar in meters.
Example: 'WheelBase',2.818
Data Types: double

## InitialPose - Initial pose of vehicle

[0 0 0] (default)| three-element vector
Initial pose of the vehicle, specified as three-element vector of the form [ $X$ Y Yaw]. $X$ and $Y$ specify the vehicle position in meters. Yaw specifies the vehicle orientation in radians. All values are in the local navigation coordinate system.
Example: 'InitialPose',[0 0 0]
Tunable: No
Data Types: double

## Usage

## Syntax

```
pose = whlEncOdom(ticks,steer)
[pose,velocity] = whlEncOdom(ticks,steer)
```


## Description

pose $=$ whlEncOdom(ticks,steer) computes the odometry of a bicycle using the specified wheel encoder ticks ticks and steering angle steer, and returns the position and orientation of the vehicle in the local navigation coordinate system.
[pose, velocity] = whlEncOdom(ticks,steer) additionally returns the linear and angular velocity of the vehicle in the local navigation coordinate system.

Input Arguments

## ticks - Number of wheel encoder ticks

$n$-element column vector
Number of wheel encoder ticks, specified as an $n$-element column vector. $n$ is the number of samples in the current frame. Each element is the number of ticks for the rear wheel of the bicycle in the corresponding sample.
Example: [5; 2]
Data Types: single | double

## steer - Steering angle of vehicle

n-element column vector
Steering angle of the vehicle, specified as an $n$-element column vector in radians. $n$ is the number of samples in the current frame.

Example: [0.2; 0.2]
Data Types: single | double

## Output Arguments

## pose - Position and orientation of vehicle

n-by-3 matrix
Position and orientation of the vehicle, returned as an $n$-by- 3 matrix. $n$ is the number of samples in the current frame. Each row of the matrix specifies the position and orientation of a sample in the form [ $X$ Y Yaw]. $X$ and $Y$ specify the vehicle position in meters. Yaw specifies the vehicle orientation in radians. All values are in the local navigation coordinate system.
Data Types: single | double

## velocity - Linear and angular velocity of vehicle

n-by-3 matrix
Linear and angular velocity of the vehicle, returned as an $n$-by- 3 matrix. $n$ is the number of samples in the current frame. Each row of the matrix specifies the linear and angular velocity of a sample in the form [velX velY yawRate]. velX and velY specify the linear velocity of the vehicle in meters per second. yawRate specifies the angular velocity of the vehicle in radians per second. All values are in the local navigation coordinate system.

Data Types: single | double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Common to All System Objects

| clone | Create duplicate System object |
| :--- | :--- |
| step | Run System object algorithm |
| release | Release resources and allow changes to System object property values and input |
| characteristics |  |
| reset | Reset internal states of System object |
| isLocked | Determine if System object is in use |

## Examples

## Compute Bicycle Odometry Using Wheel Encoder Ticks and Steering Angle

Create a wheelEncoderOdomet ryBicycle System object.
whlEncOdom = wheelEncoderOdometryBicycle;
Specify the number of wheel encoder ticks and the steering angle.

```
ticks = [5; 2];
steer = [0.2; 0.2];
```

Compute the bicycle odometry.

```
[pose,vel] = whlEncOdom(ticks,steer)
pose = 2\times3
    0.0054 0.0000 0.0004
    0.0075 0.0000 0.0005
vel = 2\times3
    0.5369 0.0002 0.0386
    0.2148 0.0001 0.0154
```


## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{Tm}}$.

## See Also

wheelEncoderBicycle | wheelEncoderOdometryAckermann | wheelEncoderOdometryDifferentialDrive | wheelEncoderOdometryUnicycle

Introduced in R2020b

## wheelEncoderOdometryDifferentialDrive

Compute differential-drive vehicle odometry using wheel encoder ticks

## Description

The wheelEncoderOdometryDifferentialDrive System object computes differential-drive vehicle odometry using the wheel encoder ticks.

To compute differential-drive vehicle odometry:
1 Create the wheelEncoderOdometryDifferentialDrive object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

```
whlEncOdom = wheelEncoderOdometryDifferentialDrive
whlEncOdom = wheelEncoderOdometryDifferentialDrive(encoder)
whlEncOdom = wheelEncoderOdometryDifferentialDrive(Name,Value)
```


## Description

whlEncOdom = wheelEncoderOdometryDifferentialDrive creates a wheelEncoderOdometryDifferentialDrive System object with default property values.
whlEncOdom = wheelEncoderOdometryDifferentialDrive(encoder) creates a wheelEncoderOdometryDifferentialDrive System object using the specified wheelEncoderDifferentialDrive System object, encoder, to set properties.
whlEncOdom = wheelEncoderOdometryDifferentialDrive(Name,Value) sets properties using one or more name-value pairs. Unspecified properties have default values. Enclose each property name in quotes.

For example, whlEncOdom =
wheelEncoder0dometryDifferentialDrive('SampleRate',100) sets the sample rate of the sensor to 100 Hz .

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

## SampleRate - Sample rate of sensor

100 (default) | positive scalar
Sample rate of sensor, specified as a positive scalar in hertz.
Example: 'SampleRate',100
Data Types: double

## TicksPerRevolution - Number of encoder ticks per wheel revolution

[2048 2048] (default) | positive integer | two-element vector of positive integers
Number of encoder ticks per wheel revolution, specified as a positive integer or two-element vector of positive integers.

When specifying this value as a two-element vector, the first element corresponds to the left wheel and the second to the right wheel.
Example: 'TicksPerRevolution', [2048 2048]
Data Types: double

## WheelRadius - Wheel radius

[0.35 0.35] (default) | positive scalar | two-element vector of positive numbers
Wheel radius, specified as a positive scalar or two-element vector of positive numbers in meters.
When specifying this value as a two-element vector, the first element corresponds to the left wheel and the second to the right wheel.
Example: 'WheelRadius',[0.35 0.35]
Data Types: double

## TrackWidth - Distance between wheels on axle

1.572 (default) | positive scalar

Distance between the wheels on the axle, specified as a positive scalar in meters.
Example: 'TrackWidth', 1.572
Data Types: double
InitialPose - Initial pose of vehicle
[0 0 0 0 $]$ (default) |three-element vector
Initial pose of the vehicle, specified as three-element vector of the form [ $X$ Y Yaw]. $X$ and $Y$ specify the vehicle position in meters. Yaw specifies the vehicle orientation in radians. All values are in the local navigation coordinate system.
Example: 'InitialPose',[0 0 0]
Data Types: double

## Usage

## Syntax

```
pose = whlEncOdom(ticks)
```

[pose,velocity] = whlEncOdom(ticks)

## Description

pose $=$ whlEncOdom(ticks) computes the odometry of a differential-drive vehicle using the specified wheel encoder ticks ticks, and returns the position and orientation of the vehicle in the local navigation coordinate system.
[pose, velocity] = whlEnc0dom(ticks) additionally returns the linear and angular velocity of the vehicle in the local navigation coordinate system.

Input Arguments
ticks - Number of wheel encoder ticks
n-by-2 matrix
Number of wheel encoder ticks, specified as an $n$-by- 2 matrix. $n$ is the number of samples in the current frame.

Each row of the matrix specifies wheel encoder ticks in the form [ticksLeft ticksRight], where ticksLeft and ticksRight specify the number of ticks for the left and right wheels, respectively.

Example: [5 5; 2 2]
Data Types: single | double

## Output Arguments

pose - Position and orientation of vehicle
$n$-by-3 matrix
Position and orientation of the vehicle, returned as an $n$-by- 3 matrix. $n$ is the number of samples in the current frame. Each row of the matrix specifies the position and orientation of a sample in the form [ $X$ Y Yaw]. $X$ and $Y$ specify the vehicle position in meters. Yaw specifies the vehicle orientation in radians. All values are in the local navigation coordinate system.
Data Types: single | double

## velocity - Linear and angular velocity of vehicle

$n$-by-3 matrix
Linear and angular velocity of the vehicle, returned as an $n$-by- 3 matrix. $n$ is the number of samples in the current frame. Each row of the matrix specifies the linear and angular velocity of a sample in the form [velX velY yawRate]. velX and velY specify the linear velocity of the vehicle in meters per second. yawRate specifies the angular velocity of the vehicle in radians per second. All values are in the local navigation coordinate system.
Data Types: single | double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:
release(obj)

## Common to All System Objects

| clone | Create duplicate System object |
| :--- | :--- |
| step | Run System object algorithm |
| release | Release resources and allow changes to System object property values and input |
| characteristics |  |
| reset | Reset internal states of System object |
| isLocked | Determine if System object is in use |

## Examples

## Compute Differential-Drive Vehicle Odometry Using Wheel Encoder Ticks

Create a wheelEncoderOdometryDifferentialDrive System object.
whlEncOdom = wheelEncoderOdometryDifferentialDrive;
Specify the number of wheel encoder ticks.
ticks = [5 5; 2 2];
Compute the differential-drive vehicle odometry.

```
[pose,vel] = whlEncOdom(ticks)
pose = 2\times3
    0.0054 0 0
    0.0075 0 0
vel = 2×3
    0.5369 0 0
    0.2148 0 0
```


## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder ${ }^{\text {TM }}$.

## See Also

wheelEncoderDifferentialDrive | wheelEncoderOdometryAckermann | wheelEncoderOdometryBicycle|wheelEncoderOdometryUnicycle

Introduced in R2020b

## wheelEncoderOdometryUnicycle

Compute unicycle odometry using wheel encoder ticks and angular velocity

## Description

The wheelEncoderOdometryUnicycle System object computes unicycle odometry using the wheel encoder ticks and angular velocity.

To compute unicycle odometry:
1 Create the wheelEncoderOdometryUnicycle object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

```
whlEncOdom = wheelEncoderOdometryUnicycle
whlEncOdom = wheelEncoderOdometryUnicycle(encoder)
whlEncOdom = wheelEncoderOdometryUnicycle(Name,Value)
Description
```

whlEncOdom = wheelEncoderOdometryUnicycle creates a wheelEncoderOdometryUnicycle System object with default property values.
whlEncOdom = wheelEncoderOdometryUnicycle(encoder) creates a wheelEncoderOdometryUnicycle System object using the specified wheelEncoderUnicycle System object, encoder, to set properties.
whlEncOdom = wheelEncoderOdometryUnicycle(Name,Value) sets properties using one or more name-value pairs. Unspecified properties have default values. Enclose each property name in quotes.

For example, whlEncOdom = wheelEncoderOdometryUnicycle('SampleRate',100) sets the sample rate of the sensor to 100 Hz .

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## SampleRate - Sample rate of sensor

100 (default) | positive scalar
Sample rate of sensor, specified as a positive scalar in hertz.
Example: 'SampleRate',100
Data Types: double

## TicksPerRevolution - Number of encoder ticks per wheel revolution <br> 2048 (default) | positive integer

Number of encoder ticks per wheel revolution, specified as a positive integer.
Example: 'TicksPerRevolution',2048
Data Types: double

## WheelRadius - Wheel radius

0.35 (default) | positive scalar

Wheel radius, specified as a positive scalar in meters.
Example: 'WheelRadius',0.35
Data Types: double
InitialPose - Initial pose of vehicle
[0 0 0] (default) | three-element vector
Initial pose of the vehicle, specified as three-element vector of the form [ $X$ Y Yaw]. $X$ and $Y$ specify the vehicle position in meters. Yaw specifies the vehicle orientation in radians. All values are in the local navigation coordinate system.
Example: 'InitialPose',[0 0 0]
Tunable: No
Data Types: double

## Usage

## Syntax

pose $=$ whlEncOdom(ticks,angVel)
[pose,velocity] = whlEncOdom(ticks,angVel)

## Description

pose $=$ whlEncOdom(ticks,angVel) computes the odometry of a unicycle using the specified wheel encoder ticks ticks and angular velocity angVel, and returns the position and orientation of the vehicle in the local navigation coordinate system.
[pose, velocity] = whlEncOdom(ticks, angVel) additionally returns the linear and angular velocity of the vehicle in the local navigation coordinate system.

## Input Arguments

## ticks - Number of wheel encoder ticks <br> n-element column vector

Number of wheel encoder ticks, specified as an $n$-element column vector. $n$ is the number of samples in the current frame.

Example: [5; 2]
Data Types: single | double
angVel - Angular velocity of vehicle in vehicle body coordinate system
$n$-element column vector
Angular velocity of the vehicle in the vehicle body coordinate system, specified as an $n$-element column vector in radians per second. $n$ is the number of samples in the current frame.

Example: [0.2; 0.2]
Data Types: single | double

## Output Arguments

## pose - Position and orientation of vehicle

n-by-3 matrix
Position and orientation of the vehicle, returned as an $n$-by- 3 matrix. $n$ is the number of samples in the current frame. Each row of the matrix specifies the position and orientation of a sample in the form [ $X$ Y Yaw]. $X$ and $Y$ specify the vehicle position in meters. Yaw specifies the vehicle orientation in radians. All values are in the local navigation coordinate system.
Data Types: single | double

## velocity - Linear and angular velocity of vehicle

n-by-3 matrix
Linear and angular velocity of the vehicle, returned as an $n$-by- 3 matrix. $n$ is the number of samples in the current frame. Each row of the matrix specifies the linear and angular velocity of a sample in the form [velX velY yawRate]. velX and velY specify the linear velocity of the vehicle in meters per second. yawRate specifies the angular velocity of the vehicle in radians per second. All values are in the local navigation coordinate system.
Data Types: single | double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Common to All System Objects

| clone | Create duplicate System object |
| :--- | :--- |
| step | Run System object algorithm |

step Run System object algorithm

```
release
    Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object
isLocked Determine if System object is in use
```


## Examples

## Compute Unicycle Odometry Using Wheel Encoder Ticks and Angular Velocity

Create a wheelEncoderOdometryUnicycle System object.
whlEncOdom = wheelEncoderOdometryUnicycle;
Specify the number of wheel encoder ticks and angular velocity.

```
ticks = [5; 2];
```

angVel $=[0.2 ; 0.2]$;

Compute the unicycle odometry.

```
[pose,vel] = whlEncOdom(ticks,angVel)
pose = 2×3
    0.0054 0.0000 0.0020
    0.0075 0.0000 0.0040
vel = 2×3
    0.5369 0.0011 0.2000
    0.2148 0.0009 0.2000
```


## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

wheelEncoderUnicycle| wheelEncoderOdometryAckermann | wheelEncoderOdometryBicycle|wheelEncoderOdometryDifferentialDrive

Introduced in R2020b

## bicycleKinematics

Bicycle vehicle model

## Description

bicycleKinematics creates a bicycle vehicle model to simulate simplified car-like vehicle dynamics. This model represents a vehicle with two axles separated by a distance, WheelBase. The state of the vehicle is defined as a three-element vector, [ $x$ y theta], with a global $x y$-position, specified in meters, and a vehicle heading angle, theta, specified in radians. The front wheel can be turned with steering angle psi. The vehicle heading, theta, is defined at the center of the rear axle. To compute the time derivative states of the model, use the derivative function with input commands and the current robot state.


## Creation

## Syntax

kinematicModel = bicycleKinematics
kinematicModel = bicycleKinematics(Name,Value)

## Description

kinematicModel = bicycleKinematics creates a bicycle kinematic model object with default property values.
kinematicModel = bicycleKinematics(Name, Value) sets additional properties to the specified values. You can specify multiple properties in any order.

## Properties

WheelBase - Distance between front and rear axles
1 (default) | positive numeric scalar
The wheel base refers to the distance between the front and rear vehicle axles, specified in meters.

```
VehicleSpeedRange - Range of vehicle speeds
[-Inf Inf] (default) | positive numeric scalar
```

The vehicle speed range is a two-element vector that provides the minimum and maximum vehicle speeds, [MinSpeed MaxSpeed], specified in meters per second.

## MaxSteeringAngle - Maximum steering angle

pi/4 (default) | numeric scalar
The maximum steering angle, psi, refers to the maximum angle the vehicle can be steered to the right or left, specified in radians. A value of pi/2 provides the vehicle with a minimum turning radius of 0 . This property is used to validate the user-provided state input.

## MinimumTurningRadius - Minimum vehicle turning radius <br> 1.0000 (default) | numeric scalar

This read-only property returns the minimum vehicle turning radius in meters. The minimum radius is computed using the wheel base and the maximum steering angle.

## VehicleInputs - Type of motion inputs for vehicle

"VehicleSpeedSteeringAngle" (default)| character vector | string scalar
The VehicleInputs property specifies the format of the model input commands when using the derivative function. The property has two valid options, specified as a string or character vector:

- "VehicleSpeedSteeringAngle" - Vehicle speed and steering angle
- "VehicleSpeedHeadingRate" - Vehicle speed and heading angular velocity


## Object Functions

derivative Time derivative of bicycle vehicle model

## Examples

## Plot Path of Bicycle Kinematic Robot

Create a robot and set its initial starting position and orientation.

```
kinematicModel = bicycleKinematics;
initialState = [0 0 0];
```

Set the timespan of the simulation to 1 s with 0.05 s timesteps and the input commands to $2 \mathrm{~m} / \mathrm{s}$ and left turn. Simulate the motion of the robot by using the ode45 solver on the derivative function.

```
tspan = 0:0.05:1;
inputs = [2 pi/4]; %Turn left
[t,y] = ode45(@(t,y)derivative(kinematicModel,y,inputs),tspan,initialState);
```

Plot the path.
figure
plot(y(:,1),y(:,2))


## References

[1] Lynch, Kevin M., and Frank C. Park. Modern Robotics: Mechanics, Planning, and Control 1st ed. Cambridge, MA: Cambridge University Press, 2017.
[2] Corke, Peter I. Robotics, Vision and Control: Fundamental Algorithms in MATLAB. Springer, 2011.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

Topics
"Mobile Robot Kinematics Equations" (Robotics System Toolbox)
Introduced in R2021b

## derivative

Time derivative of bicycle vehicle model

## Syntax

stateDot $=$ derivative(kinematicModel,state,cmds)

## Description

stateDot = derivative(kinematicModel,state,cmds) returns the current state derivative, stateDot, as a three-element vector [xDot yDot thetaDot] for a bicycle kinematics vehicle motion model, kinematicModel. xDot and yDot refer to the vehicle velocity, specified in meters per second. thetaDot is the angular velocity of the vehicle heading, specified in radians per second.

## Examples

## Plot Path of Bicycle Kinematic Robot

Create a robot and set its initial starting position and orientation.
kinematicModel = bicycleKinematics;
initialState = [0 0 0];
Set the timespan of the simulation to 1 s with 0.05 s timesteps and the input commands to $2 \mathrm{~m} / \mathrm{s}$ and left turn. Simulate the motion of the robot by using the ode45 solver on the derivative function.

```
tspan = 0:0.05:1;
inputs = [2 pi/4]; %Turn left
[t,y] = ode45(@(t,y)derivative(kinematicModel,y,inputs),tspan,initialState);
```

Plot the path.
figure
plot(y(:,1),y(:,2))


## Input Arguments

## kinematicModel - Bicycle kinematic motion model

bicycleKinematics object
Bicycle kinematic motion model, specified as a bicycleKinematics object.

## state - Current vehicle state

three-element vector | four-element vector
Current vehicle state returned as a three-element vector of the form $[x y$ theta].
$x$ and $y$ refer to the vehicle position, specified in meters per second. theta is the vehicle heading, specified in radians per second.

## cmds - Input commands to motion model

two-element vector
Input commands to the motion model, specified as a two-element vector. The VehicleInputs property value of motionModel determines the format of this command vector. These are the valid VehicleInputs values for a bicycleKinematics object:

- "VehicleSpeedSteeringAngle" -- [v psiDot]
- "VehicleSpeedHeadingRate" -- [v omegaDot]
$v$ is the vehicle velocity in the direction of motion in meters per second. psiDot is the steering angle rate in radians per second. omegaDot is the angular velocity at the rear axle.


## Output Arguments

## stateDot - Derivative of current state

three-element vector of form [xDot yDot thetaDot]
Derivative of current state, returned as a three-element vector of the form [xDot yDot thetaDot]. $x D o t$ and $y$ Dot refer to the vehicle velocity, returned in meters per second. thetaDot is the angular velocity of the vehicle heading, returned in radians per second.

## References

[1] Lynch, Kevin M., and Frank C. Park. Modern Robotics: Mechanics, Planning, and Control. 1st ed. Cambridge, MA: Cambridge University Press, 2017.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

bicycleKinematics
Introduced in R2021b

## insEKF

Inertial Navigation Using Extended Kalman Filter

## Description

The insEKF object creates a continuous-discrete extended Kalman Filter (EKF), in which the state prediction uses a continuous-time model and the state correction uses a discrete-time model. The filter uses data from inertial sensors to estimate platform states such as position, velocity, and orientation. The toolbox provides a few sensor models, such as insAccelerometer, insGyroscope, insGPS, and insMagnetometer, that you can use to enable the corresponding measurements in the EKF. You can also customize your own sensor models by inheriting from the positioning.insSensorModel interface class. The toolbox also provides motion models, such as insMotionOrientation and insMotionPose, that you can use to enable the corresponding state propagation in the EKF. You can also customize your own motion models by inheriting from the positioning.insMotionModel interface class.

## Creation

## Syntax

```
filter = insEKF
filter = insEKF(sensor1,sensor2,...,sensorN)
filter = insEKF(___,motionModel)
filter = insEKF(__,options)
```


## Description

filter = insEKF creates an insEKF filter object with default property values. With the default settings, the filter can estimate orientation by fusing accelerometer and gyroscope data.
filter = insEKF(sensor1, sensor2,..., sensorN) configures the filter to accept and fuse data from one or more sensors. The filter saves these sensors in its Sensors property.
filter = insEKF( $\qquad$ , motionModel) configures the filter to use the motion model to predict and estimate state, in addition to any combination of input arguments from previous syntaxes. The filter saves the specified motion model in the MotionModel property.
filter = insEKF(__ , options) configures the filter using the insOptions object options.

## Properties

## State - State vector of extended Kalman filter

$N$-element real-valued vector
State vector of the extended Kalman filter, specified as an $N$-element real-valued vector. $N$ is the dimension of the filter state, determined by the specific sensors and motion model used to construct the filter.

Note In the State property, if a state variable named Orientation has a length of four, the object assumes it is a quaternion. In that case, the filter renormalizes the quaternion and ensures that the real part of the quaternion is always positive.

## Data Types: single | double

## StateCovariance - State error covariance of extended Kalman filter

$N$-by- $N$ real-valued positive-definite matrix
State error covariance for the extended Kalman filter, specified as an $N$-by- $N$ real-valued positivedefinite matrix. $N$ is the dimension of the state, specified in the State property of the filter.
Data Types: single | double

## AddtiveProcessNoise - Additive process noise for extended Kalman filter

$N$-by- $N$ real-valued positive definite matrix
Additive process noise for the extended Kalman filter, specified as an $N$-by- $N$ real-valued positive definite matrix. $N$ is the dimension of the state, specified in the State of the filter.

## Data Types: single|double

## MotionModel - Motion model used in extended Kalman filter

insMotionOrientation object|insMotionPose object|object inheriting from positioning. INSMotionModel class

This property is read-only.
Motion model used in the extended Kalman filter, specified as an insMotion0rientation object, an insMotionPose object, or an object inheriting from the positioning. INSMotionModel interface class. Specify a motion model using the motionModel input argument.

Data Types: object

## Sensors - Sensors fused in extended Kalman filter

\{insAccelerometer,insGyroscope\} (default) | cell array of inertial sensor objects
This property is read-only.
Sensors fused in the extended Kalman filter, specified as a cell array of inertial sensor objects. An inertial sensor object is one of these objects:

- An insAccelerometer object
- An insMagnetometer object
- An insGPS object
- An insGyroscope object
- An object inheriting from the positioning. INSSensorModel interface class

Data Types: cell

## SensorNames - Names of sensors

cell array of character vectors
This property is read-only.

Names of the sensors, specified as a cell array of character vectors. By default, the filter names the sensors using the format 'sensorname_n', where sensorname is the name of the sensor, such as Accelerometer, and $n$ is the index for additional sensors of the same type.

To customize the sensor names, specify the options input when constructing the filter.

```
Example: {'Accelerometer' 'Accelerometer_1' 'Accelerometer_2' 'Gyroscope'}
```

Data Types: cell

## ReferenceFrame - Reference frame of extended Kalman filter "NED" (default) | "ENU"

This property is read-only.
Reference frame of the extended Kalman filter, specified as "NED" for the north-east-down frame or "ENU" for the east-north-up frame.

To specify the reference frame as "ENU", specify the options input when constructing the filter.
Data Types: char|string

## Object Functions

predict
fuse
residual
correct
stateparts
statecovparts
stateinfo
estimateStates
tune
createTunerCostTemplate
tunerCostFcnParam

Predict state estimates forward in time for insEKF
Fuse sensor data for state estimation in insEKF
Residual and residual covariance from state measurement for insEKF
Correct state estimates in insEKF using direct state measurements
Get and set part of state vector in insEKF
Get and set part of state covariance matrix in insEKF
State vector information for insEKF
Batch fusion of sensor data
Tune insEKF parameters to reduce estimation error
Create template of tuner cost function
First parameter example for tuning cost function

## Examples

## Create insEKF with Different Configurations

Create a default insEKF object. By default, the filter fuses the measurement data from an accelerometer and a gyroscope assuming orientation-only motion.

```
filter1 = insEKF
filter1 =
    insEKF with properties:
                    State: [13x1 double]
            StateCovariance: [13\times13 double]
        AdditiveProcessNoise: [13x13 double]
            MotionModel: [1x1 insMotionOrientation]
                    Sensors: {[1x1 insAccelerometer] [1x1 insGyroscope]}
            SensorNames: {'Accelerometer' 'Gyroscope'}
            ReferenceFrame: 'NED'
```

Create a second insEKF object that fuses data from an accelerometer, a gyroscope, and a magnetometer, as well as models both rotational motion and translational motion.

```
filter2 = insEKF(insAccelerometer,insGyroscope,insMagnetometer,insMotionPose)
filter2 =
    insEKF with properties:
                            State: [28x1 double]
            StateCovariance: [28x28 double]
        AdditiveProcessNoise: [28\times28 double]
            MotionModel: [1x1 insMotionPose]
                Sensors: {1x3 cell}
            SensorNames: {'Accelerometer' 'Gyroscope' 'Magnetometer'}
            ReferenceFrame: 'NED'
```

Create a third insEKF object that fuses data from a gyroscope and a GPS. Specify the reference frame of the filter as the east-north-up (ENU) frame. Note that the motion model that the filter uses is the insMotionPose object because a GPS measures platform positions.

```
option = insOptions(ReferenceFrame="ENU");
filter3 = insEKF(insGyroscope,insGPS,option)
filter3 =
    insEKF with properties:
                    State: [19x1 double]
            StateCovariance: [19x19 double]
        AdditiveProcessNoise: [19x19 double]
            MotionModel: [1x1 insMotionPose]
                    Sensors: {[1x1 insGyroscope] [1x1 insGPS]}
            SensorNames: {'Gyroscope' 'GPS'}
            ReferenceFrame: 'ENU'
```


## Sequential Fusion of Accelerometer and Gyroscope Data Using insEKF

Load measurement data from an accelerometer and a gyroscope.
load("accelGyroINSEKFData.mat");
Create an insEKF filter object. Specify the orientation part of the state in the filter using the initial orientation from the measurement data. Specify the diagonal elements of the state estimate error covariance matrix corresponding to the orientation state as 0.01 .

```
accel = insAccelerometer;
gyro = insGyroscope;
filt = insEKF(accel,gyro);
stateparts(filt,"Orientation",compact(ld.init0rient));
statecovparts(filt,"Orientation",1e-2);
```

Specify the measurement noise and the additive process noise. You can obtain these values by using the tune object function of the filter object.

```
accNoise = 0.1739;
gyroNoise = 1.1129;
processNoise = diag([ ...
    2.8586 1.3718 0.8956 3.2148 4.3574 2.5411 3.2148 0.5465 0.2811 ...
    1.7149 0.1739 0.7752 0.1739]);
filt.AdditiveProcessNoise = processNoise;
```

Sequentially fuse the measurement data using the predict and fuse object functions of the filter object.

```
N = size(ld.sensorData,1);
estOrient = quaternion.zeros(N,1);
dt = seconds(diff(ld.sensorData.Properties.RowTimes));
for ii = 1:N
    if ii ~= 1
            % Step forward in time.
            predict(filt,dt(ii-1));
        end
        % Fuse accelerometer data.
        fuse(filt,accel,ld.sensorData.Accelerometer(ii,:),accNoise);
        % Fuse gyroscope data.
        fuse(filt,gyro,ld.sensorData.Gyroscope(ii,:),gyroNoise);
        % Extract the orientation state estimate using the stateparts object
        % function.
        estOrient(ii) = quaternion(stateparts(filt,"Orientation"));
end
```

Visualize the estimate error, in quaternion distance, using the dist object function of the quaternion object.
figure
plot(rad2deg(dist(est0rient,ld.groundTruth.Orientation)))
xlabel("Samples")
ylabel("Distance (degrees)")
title("Orientation Estimate Error")


## Batch Fusion of Accelerometer and Gyroscope Data Using insEKF

Load measurement data from an accelerometer and a gyroscope.

```
load("accelGyroINSEKFData.mat");
```

Create an insEKF filter object. Specify the orientation part of the state in the filter using the initial orientation from the measurement data. Specify the diagonal elements of the state estimate error covariance matrix corresponding to the orientation state as 0.01 .

```
filt = insEKF;
stateparts(filt,"0rientation",compact(ld.init0rient));
statecovparts(filt,"Orientation",1e-2);
```

Specify the measurement noise and the additive process noise. You can obtain these values by using the tune object function of the filter object.

```
measureNoise = struct("AccelerometerNoise", 0.1739, ...
    "GyroscopeNoise", 1.1129);
processNoise = diag([ ...
    2.8586 1.3718 0.8956 3.2148 4.3574 2.5411 3.2148 0.5465 0.2811 ...
    1.7149 0.1739 0.7752 0.1739]);
filt.AdditiveProcessNoise = processNoise;
```

Batch-estimate the states using the estimateStates object function.

```
estimates = estimateStates(filt,ld.sensorData,measureNoise);
```

Visualize the estimate error, in quaternion distance, using the dist object function of the quaternion object.
figure
plot(rad2deg(dist(estimates.Orientation,ld.groundTruth.Orientation))) xlabel("Samples")
ylabel("Distance (degrees)")
title("Orientation Estimate Error")


## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder ${ }^{\mathrm{TM}}$.

## See Also

insOptions |insAccelerometer|insGPS | insGyroscope |insMagnetometer | insMotionOrientation |insMotionPose| positioning.INSMotionModel| positioning. INSSensorModel|tunerconfig|tunernoise | tunerPlotPose

## predict

Predict state estimates forward in time for insEKF

## Syntax

[state,stateCovariance] = predict(filter,dt)
$\qquad$ ] = predict( $\qquad$ , varargin)

## Description

[state, stateCovariance] = predict(filter, dt) predicts the state estimates forward in time by dt seconds based on the motion model of the filter and returns the predicted state and state estimate error covariance.
[___] ] = predict( __ , , varargin) specifies arguments used in the state transition functions or state transition Jacobian functions of the sensor models or the motion model used in the filter, in addition to all arguments from the previous syntax.

## Examples

## Predict insEKF Filter Object

Create an insEKF filter object. Specify the angular velocity of filter as [.1 0 0] rad/s.

```
filter = insEKF;
stateparts(filter,"AngularVelocity",[.1 0 0]);
```

Show the orientation quaternion at time $t=0$ seconds.

```
orientation0 = quaternion(stateparts(filter,"Orientation"))
orientation0 = quaternion
    1 + 0i + 0j + 0k
```

Predict the filter by 1 second and show the orientation quaternion.

```
[state, statecov] = predict(filter,1);
orientation1 = quaternion(stateparts(filter,"Orientation"))
orientation1 = quaternion
    0.99875 + 0.049938i + 0j + 0k
```


## Input Arguments

filter - INS filter
insEKF object
INS filter, specified as an insEKF object.

## dt - Time step of prediction

positive scalar
Time step of prediction, specified as a positive scalar.
Data Types: single | double

## varargin - Additional arguments

any data type
Additional arguments passed to the state transition functions and state transition Jacobian functions of the motion model and sensor models used in the filter, specified as any data type accepted by the two functions. You can use these arguments to simulate control or drive inputs, such as a throttle.
Data Types: single | double

## Output Arguments

## state - Predicted state vector

$N$-element real-valued vector
Predicted state vector, returned as an $N$-element real-valued vector, where $N$ is the dimension of the filter state.

Data Types: single | double
stateCovariance - State estimate error covariance
$N$-by- $N$ real-valued positive definite matrix
State estimate error covariance, returned as an $N$-by- $N$ real-valued positive definite matrix, where $N$ is the dimension of the state.
Data Types: single | double

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

fuse | residual|correct| stateparts | statecovparts|stateinfo|estimateStates| tune |createTunerCostTemplate|tunerCostFcnParam

Introduced in R2022a

## fuse

Fuse sensor data for state estimation in insEKF

## Syntax

[state,stateCovariance] = fuse(filter,sensor,measurement,measurementNoise)

## Description

[state,stateCovariance] = fuse(filter,sensor,measurement, measurementNoise) fuses the measurement from a sensor, based on the measurement noise, for state estimation.

## Examples

## Fuse Gyroscope Data Using insEKF

Create an insAccelerometer sensor object and insGyroscope sensor object.
acc = insAccelerometer;
gyro = insGyroscope;
Construct an insEKF object using the two sensor objects.
filter = insEKF(acc,gyro);
Fuse a gyroscope measurement of [0.1 0.2-0.04] rad/s with a measurement noise covariance of diag([0.2 0.20 .2$])(\mathrm{deg} / \mathrm{s})^{2}$.
[state,stateCov] = fuse(filter,gyro,[0.1 0.2 -0.04],diag([0.2 0.2 0.2]));
Show the fused state.
state
state $=13 \times 1$
1.0000

0
0
0
0.0455
0.0909
$-0.0182$

## Input Arguments

## filter - INS filter

insEKF object
INS filter, specified as an insEKF object.

## sensor - Inertial sensor

insAccelerometer object | insGyroscope object | insMagnetometer object | insGPS object | object inheriting from positioning.insSensorModel interface class

Inertial sensor, specified as one of these objects used to construct the insEKF filter object:

- An insAccelerometer object
- An insGyroscope object
- An insMagnetometer object
- An insGPS object
- An object inheriting from the positioning.insSensorModel interface class


## measurement - Measurement from sensor

$M$-element real-valued vector
Measurement from the sensor, specified as an $M$-element real-valued vector, where $M$ is the dimension of the measurement from the sensor object.
Data Types: single|double

## measurementNoise - Measurement noise

$M$-by- $M$ real-valued positive-definite matrix | $M$-element vector of positive values | positive scalar
Measurement noise, specified as an $M$-by- $M$ real-valued positive-definite matrix, an $M$-element vector of positive values, or a positive scalar. $M$ is the dimension of the measurement from the sensor object. When specified as a vector, the vector expands to the diagonal of an $M$-by- $M$ diagonal matrix. When specified as a scalar, the value of the property is the product of the scalar and an $M$-by- $M$ identity matrix.
Data Types: single | double

## Output Arguments

## state - State vector after measurement fusion

N -element real-valued vector
State vector after measurement fusion, returned as an $N$-element real-valued vector, where $N$ is the dimension of the filter state.

Data Types: single | double
stateCovariance - State estimate error covariance after measurement fusion
N -by- N real-valued positive definite matrix
State estimate error covariance after measurement fusion, returned as an $N$-by- $N$ real-valued positive definite matrix, where $N$ is the dimension of the state.

Data Types: single | double

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

predict|residual|correct|stateparts | statecovparts| stateinfo|estimateStates | tune | createTunerCostTemplate | tunerCostFcnParam

Introduced in R2022a

## residual

Residual and residual covariance from state measurement for insEKF

## Syntax

[residual, residualCovariance] = residual(filter,sensor,measurement, measurementNoise)

## Description

[residual,residualCovariance] = residual(filter,sensor,measurement, measurementNoise) computes the residual and the residual covariance based on the measurement from the sensor and the measurement covariance.

## Examples

## Obtain Gyroscope Measurement Residuals Using insEKF

Create an insAccelerometer sensor object and insGyroscope sensor object.

```
acc = insAccelerometer;
gyro = insGyroscope;
```

Construct an insEKF object using the two sensor objects. Specify the angular velocity as [0.1 0.1 $0.1] \mathrm{rad} / \mathrm{s}$.

```
filter = insEKF(acc,gyro);
stateparts(filter,"AngularVelocity",[0.1 0.1 0.1]);
```

Obtain the residuals for a gyroscope measurement of [0.1 $0.2-0.04]$ rad $/ s$ with a measurement noise covariance of diag ([0.2 0.2 0.2]) ( $\mathrm{deg} / \mathrm{s})^{2}$.
[residual, residualCov] = residual(filter,gyro,[0.1 0.2-0.04], diag([0.2 0.2 0.2]))
residual = 3×1
0
0. 1000
$-0.1400$
residualCov $=3 \times 3$

| 2.2000 | 0 | 0 |
| ---: | ---: | ---: |
| 0 | 2.2000 | 0 |
| 0 | 0 | 2.2000 |

## Input Arguments

filter - INS filter
insEKF object
INS filter, specified as an insEKF object.

## sensor - Inertial sensor

insAccelerometer object | insGyroscope object | insMagnetometer object | insGPS object |
object inheriting from positioning.insSensorModel interface class
Inertial sensor, specified as one of these objects used to construct the insEKF filter object:

- An insAccelerometer object
- An insGyroscope object
- An insMagnetometer object
- An insGPS object
- An object inheriting from the positioning.insSensorModel interface class


## measurement - Measurement from sensor

$M$-element real-valued vector
Measurement from the sensor, specified as an $M$-element real-valued vector, where $M$ is the dimension of the measurement from the sensor object.
Data Types: single|double

## measurementNoise - Measurement noise

$M$-by- $M$ real-valued positive-definite matrix | $M$-element vector of positive values | positive scalar
Measurement noise, specified as an $M$-by- $M$ real-valued positive-definite matrix, an $M$-element vector of positive values, or a positive scalar. $M$ is the dimension of the measurement from the sensor object. When specified as a vector, the vector expands to the diagonal of an $M$-by- $M$ diagonal matrix. When specified as a scalar, the value of the property is the product of the scalar and an $M$-by- $M$ identity matrix.
Data Types: single | double

## Output Arguments

## residual - Measurement residual

$M$-element real-valued vector
Measurement residual, returned as an $M$-element real-valued vector, where $M$ is the dimension of the measurement.
Data Types: single | double

## residualCovariance - Residual covariance

$M$-by- $M$ real-valued positive definite matrix
Residual covariance, returned as an $M$-by- $M$ real-valued positive definite matrix, where $M$ is the dimension of the measurement.

Data Types: single | double

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

predict | fuse | correct | stateparts | statecovparts | stateinfo|estimateStates | tune | createTunerCostTemplate | tunerCostFcnParam

Introduced in R2022a

## correct

Correct state estimates in insEKF using direct state measurements

## Syntax

[state,stateCovariance] = correct(filter,indices,measurement, measurementNoise)

## Description

[state,stateCovariance] = correct(filter,indices,measurement, measurementNoise) corrects filter estimates based on a measurement, the associated index of the measurement, and the measurement noise. The measurement must be a direct measurement of the state vector. For fusing indirect measurements, use the fuse object function.

## Examples

## Correct Angular Velocity State in insEKF

Create a default insEKF object and show its state.

```
filter = insEKF;
filter.State
ans = 13\times1
    1
    0
    0
    0
    0
    0
    0
    0
    0
    0
```

Obtain the indices corresponding to the angular velocity state.

```
idx = stateinfo(filter,"AngularVelocity");
```

Correct the angular velocity state and show the corrected state.

```
state = correct(filter,idx,[1 1 1], diag([0.1 0.1 0.1]))
state = 13x1
    1.0000
        0
```

0
0
0.9091
0.9091
0.9091

0
0
0

## Input Arguments

## filter - INS filter

insEKF object
INS filter, specified as an insEKF object.

## indices - State indices

$M$-element vector of state indices
State indices of the measurement, specified as an $M$-element vector of state indices, where $M$ is the dimension of the measurement. For example, if the measurement is the first and third elements in the


## measurement - Direct state measurement <br> $M$-element real-valued vector

Direct state measurement, specified as an $M$-element real-valued vector, where $M$ is the dimension of the measurement.

## Data Types: single | double

measurementNoise - Measurement noise
$M$-by- $M$ real-valued positive-definite matrix | $M$-element vector of positive values | positive scalar
Measurement noise, specified as an $M$-by- $M$ real-valued positive-definite matrix, an $M$-element vector of positive values, or a positive scalar. $M$ is the dimension of the measurement. When specified as a vector, the vector expands to the diagonal of an $M$-by- $M$ diagonal matrix. When specified as a scalar, the value of the property is the product of the scalar and an $M$-by- $M$ identity matrix.
Data Types: single | double

## Output Arguments

## state - Corrected state vector

$N$-element real-valued vector
Corrected state vector, returned as an $N$-element real-valued vector, where $N$ is the dimension of the filter state.
Data Types: single | double
stateCovariance - Corrected state estimate error covariance
$N$-by- $N$ real-valued positive definite matrix

Corrected state estimate error covariance, returned as an $N$-by- $N$ real-valued positive definite matrix, where $N$ is the dimension of the state.

Data Types: single | double

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

predict|fuse|residual|correct|stateparts|stateinfo|estimateStates|tune| createTunerCostTemplate|tunerCostFcnParam

Introduced in R2022a

## stateparts

Get and set part of state vector in insEKF

## Syntax

```
part = stateparts(filter,stateName)
part = stateparts(filter,sensor,stateName)
stateparts(filter,stateName,value)
stateparts(filter,sensor,stateName,value)
```


## Description

part = stateparts(filter, stateName) returns the components of the state vector corresponding to the specified state name of the filter.
part = stateparts(filter,sensor,stateName) returns the components of the state vector corresponding to the specified state name of the specified sensor.
stateparts(filter,stateName, value) sets the components of the state vector corresponding to the specified state name of the filter to the specified value.
stateparts(filter, sensor, stateName, value) sets the components of the state vector corresponding to the specified state name of the specified sensor to the specified value.

## Examples

## Set and Get Accelerometer Biases in insEKF

Create an insAccelerometer sensor object and insGyroscope sensor object.

```
acc = insAccelerometer;
```

gyro = insGyroscope;

Construct an insEKF object using the two sensor objects.

```
filter = insEKF(acc,gyro);
```

Set the bias of the accelerometer to [ $\left.\begin{array}{lll}10 & 0 & 1\end{array}\right] \mathrm{m} / \mathrm{s}^{2}$.

```
stateparts(filter,acc,"Bias",[10 0 1])
```

Get the bias of the accelerometer via the sensor.

```
accBias = stateparts(filter,acc,"Bias")
accBias = 1×3
    10 0 1
```

Get the bias of the accelerometer via the filter.

```
accBias2 = stateparts(filter,"Accelerometer_Bias")
accBias2 = 1\times3
    10 0 1
```

Set the bias of the accelerometer back to $\left[\begin{array}{lll}0 & 0 & 0\end{array}\right]$.
stateparts(filter,"Accelerometer_Bias",[0 0 0])

## Input Arguments

## filter - INS filter

insEKF object
INS filter, specified as an insEKF object.

## stateName - Name of part of state

string scalar | character vector
Name of a part of the state for the filter or the sensor, specified as a string scalar or character vector.
Use the stateinfo object function to find the names of state parts in the filter.
Example: "AngularVelocity"
Example: "Bias"
Data Types: char \| string

## sensor - Inertial sensor

insAccelerometer object | insGyroscope object | insMagnetometer object | insGPS object |
object inheriting from positioning.insSensorModel interface class
Inertial sensor, specified as one of these objects used to construct the insEKF filter object:

- An insAccelerometer object
- An insGyroscope object
- An insMagnetometer object
- An insGPS object
- An object inheriting from the positioning.insSensorModel interface class


## value - Value for filter state or sensor state part

$N$-element real-valued vector
Value for the filter state or sensor state part, specified as an $N$-element real-valued vector, where $N$ is the number of elements in the state part.
Example: [. 2 .3]
Data Types: single | double

## Output Arguments

## part - Part of state vector

$N$-element real-valued vector
Part of the state vector, returned as a real-valued vector, where $N$ is the number of elements in the state part.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

Introduced in R2022a

## statecovparts

Get and set part of state covariance matrix in insEKF

## Syntax

```
covparts = statecovparts(filter,stateName)
covparts = statecovparts(filter,sensor,stateName)
statecovparts(filter,stateName,value)
statecovparts(filter,sensor,stateName,value)
```


## Description

covparts = statecovparts(filter,stateName) returns the covariance submatrix corresponding to the specified state name of the filter. The returned submatrix is a square matrix extracted from along the main diagonal of the full state covariance matrix of the filter.
covparts = statecovparts(filter, sensor,stateName) returns the covariance submatrix corresponding to the specified state name of the sensor.
statecovparts(filter, stateName, value) sets the covariance submatrix corresponding to the specified state name of the filter to the specified value.
statecovparts(filter, sensor, stateName, value) sets the covariance submatrix corresponding to the specified state name of the specified sensor to the specified value.

## Examples

## Set and Get Accelerometer Bias Covariances in insEKF

Create an insAccelerometer sensor object.
acc = insAccelerometer;
Construct an insEKF object using the two sensor objects.

```
filter = insEKF(acc);
```

View the state covariance matrix of the filter. By default, the state covariance matrix is a 10 -by-10 identity matrix.

```
filter.StateCovariance
ans = 10\times10
```

| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |


| 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |

Set the diagonal of the covariance submatrix corresponding to the accelerometer to 3 , and show the submatrix.

```
statecovparts(filter,acc,"Bias",3);
statecovparts(filter,acc,"Bias")
ans = 3\times3
```

| 3 | 0 | 0 |
| :--- | :--- | :--- |
| 0 | 3 | 0 |
| 0 | 0 | 3 |

Set the diagonal of the covariance submatrix corresponding to the accelerometer to [llllllat and show the submatrix.

```
statecovparts(filter,acc,"Bias",[1 2 3]);
statecovparts(filter,acc,"Bias")
ans = 3\times3
\begin{tabular}{lll}
1 & 0 & 0 \\
0 & 2 & 0 \\
0 & 0 & 3
\end{tabular}
```

Set the covariance submatrix corresponding to the accelerometer to magic(3), and show the submatrix.

```
statecovparts(filter,acc,"Bias",magic(3));
```

statecovparts(filter,acc,"Bias")
ans $=3 \times 3$

| 8 | 1 | 6 |
| :--- | :--- | :--- |
| 3 | 5 | 7 |
| 4 | 9 | 2 |

Show the covariance submatrix corresponding to the accelerometer directly through the filter.

```
statecovparts(filter,"Accelerometer_Bias")
ans = 3\times3
```

| 8 | 1 | 6 |
| :--- | :--- | :--- |
| 3 | 5 | 7 |
| 4 | 9 | 2 |

View the altered state covariance matrix.
filter.StateCovariance
ans $=10 \times 10$

| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 8 | 1 | 6 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 3 | 5 | 7 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 4 | 9 | 2 |

## Input Arguments

filter - INS filter
insEKF object
INS filter, specified as an insEKF object.
stateName - Name of part of state
string scalar | character vector
Name of a part of the state for the filter or the sensor, specified as a string scalar or character vector.
Use the stateinfo object function to find the names of state parts in the filter.
Example: "AngularVelocity"
Example: "Bias"
Data Types: char|string

## sensor - Inertial sensor

insAccelerometer object|insGyroscope object|insMagnetometer object|insGPS object| object inheriting from positioning.insSensorModel interface class

Inertial sensor, specified as one of these objects used to construct the insEKF filter object:

- An insAccelerometer object
- An insGyroscope object
- An insMagnetometer object
- An insGPS object
- An object inheriting from the positioning.insSensorModel interface class
value - Value for filter or sensor state part covariance matrix
scalar | $N$-element real-valued vector | $N$-by- $N$ real-valued matrix
Value for filter or sensor state part covariance matrix, specified as one of these options:
- Real scalar - The diagonal elements of the resulting state part covariance matrix are all equal to the scalar.
- $N$-element real-valued vector - The diagonal of the resulting state part covariance matrix is equal to the vector, where $N$ is the dimension of the state corresponding to the stateName argument.
- $N$-by- $N$ real-valued matrix - The resulting state part covariance matrix is equal to the matrix, where $N$ is the dimension of the state corresponding to the stateName argument.

Data Types: single | double

## Output Arguments

covparts - Covariance matrix corresponding to state name
$N$-by- $N$ real-valued matrix
Covariance matrix corresponding to the state name, returned as an $N$-by- $N$ real-valued matrix.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

```
See Also
predict|fuse| residual| correct|stateparts|stateinfo| estimateStates|tune|
createTunerCostTemplate|tunerCostFcnParam
Introduced in R2022a
```


## stateinfo

State vector information for insEKF

## Syntax

```
info = stateinfo(filter)
indices = stateinfo(filter,stateName)
indices = stateinfo(filter,sensor,stateName)
```


## Description

info = stateinfo(filter) returns a structure whose fields contain descriptions of the elements of the state vector in the filter.
indices = stateinfo(filter,stateName) returns the indices of the components of the filter state vector corresponding to the specified state name.
indices = stateinfo(filter, sensor,stateName) returns the indices of the components of the sensor state vector corresponding to the specified state name.

## Examples

## Obtain State Information of insEKF

Create an insGyroscope object and use it to construct an insEKF object.

```
sensor = insGyroscope;
filt = insEKF(sensor);
```

Show the information for all the state components.

```
stateinfo(filt)
ans = struct with fields:
    Orientation: [lllll
    AngularVelocity: [5 6 7]
    Gyroscope_Bias: [8 9 10]
```

Obtain the indices for the orientation state.

```
stateinfo(filt,"Orientation")
ans \(=1 \times 4\)
```

    \(\begin{array}{llll}1 & 2 & 3 & 4\end{array}\)
    Obtain the indices for the sensor bias by using the sensor object input.

```
stateinfo(filt,sensor,"Bias")
```

ans $=1 \times 3$
$8 \quad 9 \quad 10$

Obtain the indices for the sensor bias directly from the filter.

```
stateinfo(filt,"Gyroscope_Bias")
```

ans $=1 \times 3$
$8 \quad 910$

## Input Arguments

## filter - INS filter

insEKF object
INS filter, specified as an insEKF object.
stateName - Name of part of state
string scalar | character vector
Name of a part of the state for the filter or the sensor, specified as a string scalar or character vector.
Use the stateinfo object function to find the names of state parts in the filter.
Example: "AngularVelocity"
Example: "Bias"
Data Types: char|string

## sensor - Inertial sensor

insAccelerometer object|insGyroscope object|insMagnetometer object|insGPS object| object inheriting from positioning.insSensorModel interface class

Inertial sensor, specified one of these objects used to construct the insEKF filter object:

- An insAccelerometer object
- An insGyroscope object
- An insMagnetometer
- An insGPS object
- An object inheriting from the positioning.insSensorModel interface class


## Output Arguments

## info - State information

structure
State information, returned as a structure. The field names of the structure are names of the elements of the state vector in the filter. The values of each field are the corresponding indices of the state vector.

## indices - State indices

$M$-element vector of state indices
State indices, returned as an $M$-element vector of state indices, where $M$ is the dimension of the state part corresponding to the stateName. For example, if the state name corresponds to the first, second, and third elements in the state vector of the filter, then the function returns indices as [1 2 3].

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

predict|fuse| residual|correct|stateparts|statecovparts|estimateStates|tune | createTunerCostTemplate|tunerCostFcnParam

Introduced in R2022a

## estimateStates

Batch fusion of sensor data

## Syntax

estimates = estimateStates(filter,sensorData,measurementNoise)

## Description

estimates $=$ estimateStates(filter,sensorData, measurementNoise) returns the state estimates based on the motion model used in the filter, the sensor data, and the measurement noise. The function predicts the filter state estimates forward in time based on the row times in sensorData and fuses data from each column of the table one by one.

## Examples

## Batch Fusion of Accelerometer and Gyroscope Data Using insEKF

Load measurement data from an accelerometer and a gyroscope.

```
load("accelGyroINSEKFData.mat");
```

Create an insEKF filter object. Specify the orientation part of the state in the filter using the initial orientation from the measurement data. Specify the diagonal elements of the state estimate error covariance matrix corresponding to the orientation state as 0.01 .

```
filt = insEKF;
stateparts(filt,"Orientation",compact(ld.init0rient));
statecovparts(filt,"Orientation",1e-2);
```

Specify the measurement noise and the additive process noise. You can obtain these values by using the tune object function of the filter object.

```
measureNoise = struct("AccelerometerNoise", 0.1739, ...
    "GyroscopeNoise", 1.1129);
processNoise = diag([ ...
    2.8586 1.3718 0.8956 3.2148 4.3574 2.5411 3.2148 0.5465 0.2811 ...
    1.7149 0.1739 0.7752 0.1739]);
filt.AdditiveProcessNoise = processNoise;
```

Batch-estimate the states using the estimateStates object function.

```
estimates = estimateStates(filt,ld.sensorData,measureNoise);
```

Visualize the estimate error, in quaternion distance, using the dist object function of the quaternion object.
figure
plot(rad2deg(dist(estimates.Orientation,ld.groundTruth.Orientation)))
xlabel("Samples")
ylabel("Distance (degrees)")
title("Orientation Estimate Error")


## Input Arguments

filter - INS filter
insEKF object
INS filter, specified as an insEKF object.

## sensorData - Sensor data

timetable
Sensor data, specified as a timetable. Each variable name (as a column) in the timetable must match one of the sensor names specified in the SensorNames property of the filter. Each entry in the table is the measurement from the sensor at the corresponding row time.

If a sensor does not produce measurements at a row time, specify the corresponding entry as NaN .

## measurementNoise - Measurement noise

structure
Measurement noise of the sensors, specified as a structure. Each field name must match one of the sensor names specified in the SensorNames property of the filter. The field value is the
corresponding measurement noise covariance matrix. If you specify a field value as a scalar, the function extends the scalar to the diagonal of the matrix.

Data Types: struct

## Output Arguments

## estimates - State estimates

timetable
State estimates, returned as a timetable. Each variable name of the table is a state name that you can obtain using the stateinfo object function of the filter. The last column of the table is the state estimate error covariance matrix for the complete state vector of the filter at each of the row times.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

predict|fuse|residual|correct|stateparts|statecovparts|stateinfo|tune| createTunerCostTemplate|tunerCostFcnParam

Introduced in R2022a

## tune

Tune insEKF parameters to reduce estimation error

## Syntax

tunedMeasureNoise = tune(filter,measureNoise, sensorData,groundTruth) tunedMeasureNoise = tune( $\qquad$ , config)

## Description

tunedMeasureNoise = tune(filter,measureNoise, sensorData,groundTruth) tunes the AdditiveProcessNoise property of the insEKF filter object filter, and the measurement noise, to reduce the root-mean-squared (RMS) state estimation error between the fused sensor data and the ground truth. The function also returns the tuned measurement noise tunedMeasureNoise. The function uses the property values in the filter and the measurement noise provided in the measureNoise structure as the initial estimate for the optimization algorithm.
tunedMeasureNoise = tune( $\qquad$ , config) specifies the tuning configuration using a tunerconfig object config, in addition to all input arguments from the previous syntax.

## Examples

## Tune insEKF to Optimize Orientation Estimation

Load the recorded sensor data and ground truth data.
load("accelGyroINSEKFData.mat");
Create an insEKF filter object. Specify the orientation part of the state in the filter using the initial orientation from the measurement data. Specify the diagonal elements of the state estimate error covariance matrix corresponding to the orientation state as 0.01 .

```
filt = insEKF;
stateparts(filt,"Orientation",compact(ld.initOrient));
statecovparts(filt,"Orientation",1e-2);
```

Obtain a representative measurement noise structure and use it to estimate states before tuning.

```
mnoise = tunernoise(filt);
untunedEst = estimateStates(filt,ld.sensorData,mnoise);
```

Reinitialize the filter, set up a tunerconfig object, and tune the filter.

```
stateparts(filt,"0rientation",compact(ld.init0rient));
statecovparts(filt,"Orientation",1e-2);
cfg = tunerconfig(filt,MaxIterations=10,ObjectiveLimit=1e-4);
tunedmn = tune(filt,mnoise,ld.sensorData,ld.groundTruth,cfg);
    Iteration Parameter Metric
```

| sNoise(1) | 0.3787 |
| :---: | :---: |
| AdditiveProcessNoise(15) | 0.3761 |
| AdditiveProcessNoise(29) | 0.3695 |
| AdditiveProcessNoise(43) | 0.3655 |
| AdditiveProcessNoise(57) | 0.3533 |
| AdditiveProcessNoise(71) | 0.3446 |
| AdditiveProcessNoise(85) | 0.3431 |
| AdditiveProcessNoise(99) | 0.3428 |
| AdditiveProcessNoise(113) | 0.3427 |
| AdditiveProcessNoise(127) | 0.3426 |
| AdditiveProcessNoise(141) | 0.3298 |
| AdditiveProcessNoise(155) | 0.3206 |
| AdditiveProcessNoise(169) | 0.3200 |
| AccelerometerNoise | 0.3199 |
| GyroscopeNoise | 0.3198 |
| AdditiveProcessNoise(1) | 0.3126 |
| AdditiveProcessNoise(15) | 0.3098 |
| AdditiveProcessNoise(29) | 0.3018 |
| AdditiveProcessNoise(43) | 0.2988 |
| AdditiveProcessNoise(57) | 0.2851 |
| AdditiveProcessNoise(71) | 0.2784 |
| AdditiveProcessNoise(85) | 0.2760 |
| AdditiveProcessNoise(99) | 0.2744 |
| AdditiveProcessNoise(113) | 0.2744 |
| AdditiveProcessNoise(127) | 0.2743 |
| AdditiveProcessNoise(141) | 0.2602 |
| AdditiveProcessNoise(155) | 0.2537 |
| AdditiveProcessNoise(169) | 0.2527 |
| AccelerometerNoise | 0.2524 |
| GyroscopeNoise | 0.2524 |
| AdditiveProcessNoise(1) | 0.2476 |
| AdditiveProcessNoise(15) | 0.2432 |
| AdditiveProcessNoise(29) | 0.2397 |
| AdditiveProcessNoise(43) | 0.2381 |
| AdditiveProcessNoise(57) | 0.2255 |
| AdditiveProcessNoise(71) | 0.2226 |
| AdditiveProcessNoise(85) | 0.2221 |
| AdditiveProcessNoise(99) | 0.2202 |
| AdditiveProcessNoise(113) | 0.2201 |
| AdditiveProcessNoise(127) | 0.2201 |
| AdditiveProcessNoise(141) | 0.2090 |
| AdditiveProcessNoise(155) | 0.2070 |
| AdditiveProcessNoise(169) | 0.2058 |
| AccelerometerNoise | 0.2052 |
| GyroscopeNoise | 0.2052 |
| AdditiveProcessNoise(1) | 0.2051 |
| AdditiveProcessNoise(15) | 0.2027 |
| AdditiveProcessNoise(29) | 0.2019 |
| AdditiveProcessNoise(43) | 0.2000 |
| AdditiveProcessNoise(57) | 0.1909 |
| AdditiveProcessNoise(71) | 0.1897 |
| AdditiveProcessNoise(85) | 0.1882 |
| AdditiveProcessNoise(99) | 0.1871 |
| AdditiveProcessNoise(113) | 0.1870 |
| AdditiveProcessNoise(127) | 0.1870 |
| AdditiveProcessNoise(141) | 0.1791 |
| AdditiveProcessNoise(155) | 0.1783 |
| AdditiveProcessNoise(169) | 0.1751 |


| 4 | AccelerometerNoise | 0.1748 |
| :---: | :---: | :---: |
| 4 | GyroscopeNoise | 0.1747 |
| 5 | AdditiveProcessNoise(1) | 0.1742 |
| 5 | AdditiveProcessNoise(15) | 0.1732 |
| 5 | AdditiveProcessNoise(29) | 0.1712 |
| 5 | AdditiveProcessNoise(43) | 0.1712 |
| 5 | AdditiveProcessNoise(57) | 0.1626 |
| 5 | AdditiveProcessNoise(71) | 0.1615 |
| 5 | AdditiveProcessNoise(85) | 0.1598 |
| 5 | AdditiveProcessNoise(99) | 0.1590 |
| 5 | AdditiveProcessNoise(113) | 0.1589 |
| 5 | AdditiveProcessNoise(127) | 0.1589 |
| 5 | AdditiveProcessNoise(141) | 0.1517 |
| 5 | AdditiveProcessNoise(155) | 0.1508 |
| 5 | AdditiveProcessNoise(169) | 0.1476 |
| 5 | AccelerometerNoise | 0.1473 |
| 5 | GyroscopeNoise | 0.1470 |
| 6 | AdditiveProcessNoise(1) | 0.1470 |
| 6 | AdditiveProcessNoise(15) | 0.1470 |
| 6 | AdditiveProcessNoise(29) | 0.1463 |
| 6 | AdditiveProcessNoise(43) | 0.1462 |
| 6 | AdditiveProcessNoise(57) | 0.1367 |
| 6 | AdditiveProcessNoise(71) | 0.1360 |
| 6 | AdditiveProcessNoise(85) | 0.1360 |
| 6 | AdditiveProcessNoise(99) | 0.1350 |
| 6 | AdditiveProcessNoise(113) | 0.1350 |
| 6 | AdditiveProcessNoise(127) | 0.1350 |
| 6 | AdditiveProcessNoise(141) | 0.1289 |
| 6 | AdditiveProcessNoise(155) | 0.1288 |
| 6 | AdditiveProcessNoise(169) | 0.1262 |
| 6 | AccelerometerNoise | 0.1253 |
| 6 | GyroscopeNoise | 0.1246 |
| 7 | AdditiveProcessNoise(1) | 0.1246 |
| 7 | AdditiveProcessNoise(15) | 0.1244 |
| 7 | AdditiveProcessNoise(29) | 0.1205 |
| 7 | AdditiveProcessNoise(43) | 0.1203 |
| 7 | AdditiveProcessNoise(57) | 0.1125 |
| 7 | AdditiveProcessNoise(71) | 0.1122 |
| 7 | AdditiveProcessNoise(85) | 0.1117 |
| 7 | AdditiveProcessNoise(99) | 0.1106 |
| 7 | AdditiveProcessNoise(113) | 0.1104 |
| 7 | AdditiveProcessNoise(127) | 0.1104 |
| 7 | AdditiveProcessNoise(141) | 0.1058 |
| 7 | AdditiveProcessNoise(155) | 0.1052 |
| 7 | AdditiveProcessNoise(169) | 0.1035 |
| 7 | AccelerometerNoise | 0.1024 |
| 7 | GyroscopeNoise | 0.1014 |
| 8 | AdditiveProcessNoise(1) | 0.1014 |
| 8 | AdditiveProcessNoise(15) | 0.1012 |
| 8 | AdditiveProcessNoise(29) | 0.1012 |
| 8 | AdditiveProcessNoise(43) | 0.1005 |
| 8 | AdditiveProcessNoise(57) | 0.0948 |
| 8 | AdditiveProcessNoise(71) | 0.0948 |
| 8 | AdditiveProcessNoise(85) | 0.0938 |
| 8 | AdditiveProcessNoise(99) | 0.0934 |
| 8 | AdditiveProcessNoise(113) | 0.0931 |
| 8 | AdditiveProcessNoise(127) | 0.0931 |
| 8 | AdditiveProcessNoise(141) | 0.0896 |


| 8 | AdditiveProcessNoise(155) | 0.0889 |
| :--- | :--- | :--- |
| 8 | AdditiveProcessNoise(169) | 0.0867 |
| 8 | AccelerometerNoise | 0.0859 |
| 8 | GyroscopeNoise | 0.0851 |
| 9 | AdditiveProcessNoise(1) | 0.0851 |
| 9 | AdditiveProcessNoise(15) | 0.0850 |
| 9 | AdditiveProcessNoise(29) | 0.0824 |
| 9 | AdditiveProcessNoise(43) | 0.0819 |
| 9 | AdditiveProcessNoise(57) | 0.0771 |
| 9 | AdditiveProcessNoise(71) | 0.0771 |
| 9 | AdditiveProcessNoise(85) | 0.0762 |
| 9 | AdditiveProcessNoise(99) | 0.0759 |
| 9 | AdditiveProcessNoise(113) | 0.0754 |
| 9 | AdditiveProcessNoise(127) | 0.0754 |
| 9 | AdditiveProcessNoise(141) | 0.0734 |
| 9 | AdditiveProcessNoise(155) | 0.0724 |
| 9 | AdditiveProcessNoise(169) | 0.0702 |
| 9 | AccelerometerNoise | 0.0697 |
| 9 | GyroscopeNoise | 0.0689 |
| 10 | AdditiveProcessNoise(1) | 0.0689 |
| 10 | AdditiveProcessNoise(15) | 0.0686 |
| 10 | AdditiveProcessNoise(29) | 0.0658 |
| 10 | AdditiveProcessNoise(43) | 0.0655 |
| 10 | AdditiveProcessNoise(57) | 0.0622 |
| 10 | AdditiveProcessNoise(71) | 0.0620 |
| 10 | AdditiveProcessNoise(85) | 0.0616 |
| 10 | AdditiveProcessNoise(99) | 0.0615 |
| 10 | AdditiveProcessNoise(113) | 0.0607 |
| 10 | AdditiveProcessNoise(127) | 0.0606 |
| 10 | AdditiveProcessNoise(141) | 0.0590 |
| 10 | AdditiveProcessNoise(155) | 0.0578 |
| 10 | AdditiveProcessNoise(169) | 0.0565 |
| 10 | AccelerometerNoise | 0.0562 |
| 10 | GyroscopeNoise | 0.0557 |
|  |  |  |

Estimate states again, this time using the tuned filter.

```
tunedEst = estimateStates(filt,ld.sensorData,tunedmn);
```

Compare the tuned and untuned estimates against the ground truth data.

```
times = ld.groundTruth.Properties.RowTimes;
duntuned = rad2deg(dist(untunedEst.Orientation,ld.groundTruth.Orientation));
dtuned = rad2deg(dist(tunedEst.Orientation,ld.groundTruth.Orientation));
plot(times,duntuned,times,dtuned);
xlabel("Time (sec)")
ylabel("Error (deg)")
legend("Untuned","Tuned")
title("Filter Orientation Error")
```

Filter Orientation Error


Print the root-mean-squared (RMS) error of both the untuned and the tuned filters.

```
untunedRMSError = sqrt(mean(duntuned.^2));
tunedRMSError = sqrt(mean(dtuned.^2));
fprintf("Untuned RMS error: %.2f degrees\n", ...
    untunedRMSError);
Untuned RMS error: 39.47 degrees
fprintf("Tuned RMS error: %.2f degrees\n", ...
    tunedRMSError);
Tuned RMS error: 6.39 degrees
```


## Input Arguments

filter - INS filter
insEKF object
INS filter, specified as an insEKF object.

## measureNoise - Measurement noise <br> structure

Measurement noise, specified as a structure. The function uses the measurement noise input as the initial guess for tuning the measurement noise. The structure should contain the measurement noise
for sensor models specified in the Sensors property of the INS filter. For example, if the insEKF filter object only contains an insAccelerometer object and an insGyroscope object, you should specify the structure like this:

| Field name | Description |
| :--- | :--- |
| AccelerometerNoise | Variance of accelerometer noise, specified as a <br> scalar in $\left(\mathrm{m}^{2} / \mathrm{s}\right)$. |
| GyroscopeNoise | Variance of gyroscope noise, specified as a scalar <br> in $(\mathrm{rad} / \mathrm{s})^{2}$. |

Tip Use the tunernoise function to obtain a representative structure for the measureNoise structure. For example:
filter = insEKF;
mNoise $=$ tunerNoise(filter)

## sensorData - Sensor data

## timetable

Sensor data, specified as a timetable. Each variable name (as a column) in the time table must match one of the sensor names specified in the SensorNames property of the filter. Each entry in the table is the measurement from the sensor at the corresponding row time.

If a sensor does not produce measurements at the row time, specify the corresponding entry as NaN .
If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the sensorData input based on your choice.

## groundTruth - Ground truth data

timetable
Ground truth data, specified as a timetable. In each row, the table contains the truth data for the row time. Each variable name (as a column) in the table must be one of the filter state names that you can obtain using the stateinfo object function.

The function processes each row of the sensorData and groundTruth tables sequentially to calculate the state estimate and RMS error from the ground truth. State variables not present in groundTruth input are ignored for the comparison. The sensorData and the groundTruth tables must have the same row times.

If you set the Cost property of the tuner configuration input, config, to Custom, then you can use other data types for the groundTruth input based on your choice.

## config - Tuner configuration

tunerconfig object
Tuner configuration, specified as a tunerconfig object.

## Output Arguments

## tunedMeasureNoise - Tuned measurement noise

structure
Tuned measurement noise, returned as a structure. The structure contains the same fields as the structure specified in the measureNoise input.

## References

[1] Abbeel, P., Coates, A., Montemerlo, M., Ng, A.Y. and Thrun, S. Discriminative Training of Kalman Filters. In Robotics: Science and systems, Vol. 2, pp. 1, 2005.

```
See Also
tunerconfig|tunernoise|predict|fuse| residual| correct|stateparts|
statecovparts|stateinfo|estimateStates|tune| createTunerCostTemplate|
tunerCostFcnParam
```

Introduced in R2022a

## createTunerCostTemplate

Create template of tuner cost function

## Syntax

createTunerCostTemplate(filter)

## Description

createTunerCostTemplate(filter) creates a template of a tuner cost function and shows it in an editor window. The created cost function computes the cost as the root-mean-squared (RMS) error between the estimated states and the ground truth. You can modify the cost function as desired.

When you tune the filter parameters of the insEKF object using its tune object function, use the function created by createTunerCostTemplate to specify the cost in the tunerconfig object as an input to the tune object function.

## Examples

## Tune insEKF with Custom Cost Function

Create an insEKF filter object and create a cost function using the createTunerCostTemplate object function.

```
filter = insEKF;
createTunerCostTemplate(filter);
```

Save the created function in an m-file.

```
doc = matlab.desktop.editor.getActive;
doc.saveAs(fullfile(pwd,"tunercost.m"));
```

Load prerecorded sensor data and ground truth data.

```
load("accelGyroINSEKFData.mat");
```

Specify an initial orientation state and its covariance.

```
stateparts(filter,"Orientation",compact(ld.initOrient));
statecovparts(filter,"Orientation",1e-2);
```

Create a measurement noise structure using the tunernoise function.

```
mnoise = tunernoise(filter);
```

Create a tunerconfig object using the created cost function.

```
cfg = tunerconfig(filter,MaxIterations=1, ...
    ObjectiveLimit=1e-4, ...
    Cost="custom", ...
    CustomCostFcn=@tunercost);
```

Tune the filter. Show the tuned measurement noise and process noise in the filter.

```
tunedmn = tune(filter,mnoise,ld.sensorData, ...
    ld.groundTruth,cfg)
\begin{tabular}{llll} 
Iteration & & Parameter & Metric \\
& & & AdditiveProcessNoise(1) \\
1 & & AdditiveProcessNoise(15) & 0.3413 \\
1 & & AdditiveProcessNoise(29) & 0.3381 \\
1 & & AdditiveProcessNoise(43) & 0.3334 \\
1 & & AdditiveProcessNoise(57) & 0.3214 \\
1 & & AdditiveProcessNoise(71) & 0.3121 \\
1 & & AdditiveProcessNoise(85) & 0.3110 \\
1 & & AdditiveProcessNoise(99) & 0.3107 \\
1 & & AdditiveProcessNoise(113) & 0.3106 \\
1 & AdditiveProcessNoise(127) & 0.3105 \\
1 & AdditiveProcessNoise(141) & 0.2972 \\
1 & AdditiveProcessNoise(155) & 0.2872 \\
1 & AdditiveProcessNoise(169) & 0.2855 \\
1 & AccelerometerNoise & 0.2852 \\
1 & GyroscopeNoise & 0.2851
\end{tabular}
tunedmn = struct with fields:
    AccelerometerNoise: 0.9000
        GyroscopeNoise: 0.9000
orientationNoise = statecovparts(filter,"Orientation")
orientationNoise = 4×4
\begin{tabular}{rrrr}
0.0100 & 0 & 0 & 0 \\
0 & 0.0100 & 0 & 0 \\
0 & 0 & 0.0100 & 0 \\
0 & 0 & 0 & 0.0100
\end{tabular}
```


## Input Arguments

filter - INS filter
insEKF object
INS filter, specified as an insEKF object.

## See Also

predict|fuse|residual|correct|stateparts | statecovparts| stateinfo| estimateStates|tune|tunerCostFcnParam

## Introduced in R2022a

## tunerCostFcnParam

First parameter example for tuning cost function

## Syntax

tunerCostFcnParam(filter)

## Description

tunerCostFcnParam(filter) creates a structure that has the fields required for tuning an insEKF filter with a custom cost function. The structure is useful when generating C code for a cost function using MATLAB Coder ${ }^{\mathrm{TM}}$.

## Examples

## Tune insEKF with MEX-Accelerated Custom Cost Function

Create an insEKF filter object. Then create a cost function using the createTunerCostTemplate object function.

```
filter = insEKF;
createTunerCostTemplate(filter);
doc = matlab.desktop.editor.getActive;
doc.saveAs(fullfile(pwd,"tunercost.m"));
```

Load prerecorded sensor data and ground truth data.

```
load("accelGyroINSEKFData.mat");
```

Create a MEX cost function using MATLAB Coder.

```
p = tunerCostFcnParam(filter);
disp("Generating MEX-accelerated cost function");
Generating MEX-accelerated cost function
codegen tunercost.m -args {p,ld.sensorData,ld.groundTruth};
Code generation successful.
```

Specify an initial orientation state and its covariance.

```
stateparts(filter,"Orientation",compact(ld.initOrient));
statecovparts(filter,"Orientation",1e-2);
```

Create a measurement noise structure using the tunernoise function.

```
mnoise = tunernoise(filter);
```

Create a tunerconfig object using the created MEX cost function.

```
cfg = tunerconfig(filter, MaxIterations=1, ...
```

    ObjectiveLimit=le-4, ...
    ```
Cost="custom", ...
CustomCostFcn=@tunercost_mex);
```

Tune the filter. Show the tuned measurement noise and process noise in the filter.

```
tunedmn = tune(filter,mnoise,ld.sensorData, ...
    ld.groundTruth,cfg)
    Iteration
    1
    1 AdditiveProcessNoise(15) 0.3381
    1 AdditiveProcessNoise(29) 0.3353
    1 AdditiveProcessNoise(43) 0.3334
    1 AdditiveProcessNoise(57) 0.3214
    1 AdditiveProcessNoise(71) 0.3121
    1 AdditiveProcessNoise(85) 0.3110
    1 AdditiveProcessNoise(99) 0.3107
    1 AdditiveProcessNoise(113) 0.3106
    1 AdditiveProcessNoise(127) 0.3105
    1 AdditiveProcessNoise(141) 0.2972
    1 AdditiveProcessNoise(155) 0.2872
    1 AdditiveProcessNoise(169) 0.2855
    1 AccelerometerNoise 0.2852
    1 GyroscopeNoise 0.2851
tunedmn = struct with fields:
    AccelerometerNoise: 0.9000
        GyroscopeNoise: 0.9000
orientationNoise = statecovparts(filter,"Orientation")
orientationNoise = 4×4
\begin{tabular}{rrrr}
0.0100 & 0 & 0 & 0 \\
0 & 0.0100 & 0 & 0 \\
0 & 0 & 0.0100 & 0 \\
0 & 0 & 0 & 0.0100
\end{tabular}
```


## Input Arguments

filter - INS filter
insEKF object
INS filter, specified as an insEKF object.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{Tm}}$.

## See Also

predict | fuse | residual|correct | stateparts | statecovparts | stateinfo| estimateStates|tune|createTunerCostTemplate

Introduced in R2022a

## insOptions

Options for configuration of insEKF object

## Description

The insOptions object specifies properties for an insEKF object.

## Creation

## Syntax

options = insOptions
options = insOptions(Name=Value)

## Description

options $=$ insOptions returns an insOptions object with default property values.
options = insOptions(Name=Value) specifies properties using one or more name-value arguments. For example, options = insOptions (ReferenceFrame="ENU") sets the reference frame used in the insEKF object as the east-north-up (ENU) frame. Unspecified properties have default values.

## Properties

## Datatype - Data type of insEKF variables

"double" (default)|"single"
Data type of insEKF variables, specified as "single" or "double". This data type applies to variables such as state, state covariance, and other internal variables.

Data Types: char|string

## SensorNamesSource - Source for names of sensors fused <br> "default" (default)| "property"

Source for the names of the sensors fused in the insEKF object, specified as "default" or "property".

- "default" - The insEKF object names the fused sensors using the default convention. See the SensorNames property of the insEKF object for details on the default names.
- "property" - Specify the names of sensors fused in the insEKF object using the SensorNames property of the insOptions object.

Data Types: char|string

## ReferenceFrame - Reference frame of insEKF object <br> "NED" (default) | "ENU"

Reference frame of the insEKF object, specified as "NED" for the north-east-down frame or "ENU" for the east-north-up frame.

Data Types: char|string

## SensorNames - Names of sensors fused in filter

\{ ' ' $\}$ (default) | cell array of character vectors
Names of sensors fused in the filter, specified as a cell array of character vectors.
Example: \{'Sensor1', 'Accelerometer2'\}
Data Types: cell

## Examples

## Create insOptions to Use with insEKF Object

Create an insOptions object, and specify the sensor names as Sensor1 and Sensor2. Specify the data type as single.

```
options = insOptions(SensorNamesSource="Property", ...
    SensorNames={'Sensor1','Sensor2'}, ...
    Datatype="single")
options =
    insOptions with properties:
            Datatype: 'single'
        SensorNamesSource: property
            ReferenceFrame: NED
                SensorNames: {'Sensor1' 'Sensor2'}
```

Create an insEKF filter object with one accelerometer and one magnetometer. Specify the properties of the filter using the insOptions object. In the created filter, the sensor names are Sensorl and Sensor2, respectively. The data type is single.

```
filter = insEKF(insAccelerometer,insMagnetometer,options)
```

filter =
insEKF with properties:
State: [16x1 single]
StateCovariance: [16x16 single]
AdditiveProcessNoise: [16x16 single]
MotionModel: [1x1 insMotionOrientation]
Sensors: \{[1x1 insAccelerometer] [1x1 insMagnetometer]\}
SensorNames: \{'Sensor1' 'Sensor2'\}
ReferenceFrame: 'NED'

## See Also

insEKF

Introduced in R2022a

## insAccelerometer

Model accelerometer readings for sensor fusion

## Description

The insAccelerometer object models accelerometer readings for sensor fusion. Passing an insAccelerometer object to an insEKF object enables the insEKF object to fuse accelerometer data. For details on the accelerometer model, see "Algorithms" on page 2-1671.

## Creation

## Syntax

sensor = insAccelerometer

## Description

sensor $=$ insAccelerometer creates an insAccelerometer object. Passing the created sensor to an insEKF object enables the insEKF object to fuse accelerometer data. When fusing data with the fuse object function of insEKF, pass sensor as the second argument to identify the data as obtained from an accelerometer.

## Examples

## Create insAccelerometer for Use in insEKF

Create two insAccelerometer objects and pass them to an insEKF object.

```
sensor1 = insAccelerometer;
sensor2 = insAccelerometer;
filterOrientation = insEKF(sensor1,sensor2,insMotionOrientation)
filterOrientation =
    insEKF with properties:
                            State: [13x1 double]
            StateCovariance: [13\times13 double]
        AdditiveProcessNoise: [13\times13 double]
            MotionModel: [1x1 insMotionOrientation]
            Sensors: {[1x1 insAccelerometer] [1x1 insAccelerometer]}
            SensorNames: {'Accelerometer' 'Accelerometer_1'}
            ReferenceFrame: 'NED'
```

Since the insMotionOrientation object does not model linear acceleration, the filter does not estimate acceleration.

```
stateinfo(filterOrientation)
```

```
ans = struct with fields:
                Orientation: [lllll
        AngularVelocity: [5 6 7]
        Accelerometer_Bias: [8 9 10]
    Accelerometer_1_Bias: [11 12 13]
```

Create another two insAccelerometer objects and pass them to a new insEKF object. Since the insMotionPose object models linear acceleration, the filter estimates acceleration.

```
sensor3 = insAccelerometer;
sensor4 = insAccelerometer;
filterPose = insEKF(sensor3,sensor4,insMotionPose)
filterPose =
    insEKF with properties:
                    State: [22x1 double]
            StateCovariance: [22x22 double]
        AdditiveProcessNoise: [22x22 double]
            MotionModel: [1x1 insMotionPose]
                    Sensors: {[1x1 insAccelerometer] [1x1 insAccelerometer]}
                SensorNames: {'Accelerometer' 'Accelerometer_1'}
            ReferenceFrame: 'NED'
stateinfo(filterPose)
ans = struct with fields:
            Orientation: [ll 2 3 4]
            AngularVelocity: [5 6 7]
            Position: [8 9 10]
            Velocity: [11 12 13]
            Acceleration: [14 15 16]
        Accelerometer Bias: [lllll}18\mathrm{ 19]
        Accelerometer_1_Bias: [20 21 22]
```

Fuse a measurement from sensor3.

```
fuse(filterPose,sensor3,[1 1 1],eye(3))
ans = 22\times1
    0.7759
    0.0506
    -0.0506
            0
            0
            0
            0
            0
            0
            0
        :
```


## Algorithms

The insAccelerometer object models the accelerometer reading as acceleration in the sensor frame. Depending on whether the insEKF object estimates linear acceleration in the state equations, the measurement equation takes one of two forms:

- If the insEKF object does not estimate the acceleration state, the measurement equation is:

$$
h(x)=g_{\text {sensor }}+\Delta
$$

where $h(x)$ is the three-dimensional measurement output, $g_{\text {sensor }}$ is the gravitational acceleration expressed in the sensor frame, and $\Delta$ is the three-dimensional bias of the sensor, modeled as a constant vector in the sensor frame.

- If the insEKF object estimates the acceleration state, the equation is:

$$
h(x)=g_{\text {sensor }}+a_{\text {sensor }}+\Delta
$$

where $a_{\text {sensor }}$ is the acceleration, excluding the gravity acceleration, expressed in the sensor frame.
Passing an insAccelerometer object to an insEKF filter object enables the filter object to additionally track the bias of the accelerometer. Internally, the insEKF object decides if the acceleration state is estimated by calling its stateparts object function.

## See Also

insEKF \| insOptions
Introduced in R2022a

## insGyroscope

Model gyroscope readings for sensor fusion

## Description

The insGyroscope object models gyroscope readings for sensor fusion. Passing an insGyroscope object to an insEKF object enables the insEKF object to fuse gyroscope data. For details on the gyroscope model, see "Algorithms" on page 2-1673.

## Creation

## Syntax

sensor = insGyroscope
Description
sensor = insGyroscope creates an insGyroscope object. Passing the created sensor to an insEKF object enables the insEKF object to fuse gyroscope data. When fusing data with the fuse object function of insEKF, pass sensor as the second argument to identify the data as obtained from a gyroscope.

## Examples

## Create insGyroscope for Use in insEKF

Create an insGyroscope object and pass it to an insEKF object.

```
sensor = insGyroscope;
filterOrientation = insEKF(sensor)
filterOrientation =
    insEKF with properties:
                            State: [10x1 double]
            StateCovariance: [10x10 double]
        AdditiveProcessNoise: [10x10 double]
            MotionModel: [1x1 insMotionOrientation]
            Sensors: {[1x1 insGyroscope]}
            SensorNames: {'Gyroscope'}
            ReferenceFrame: 'NED'
```

Show the state information of the filter. Notice that the state contains the gyroscope bias component.

```
stateinfo(filterOrientation)
ans = struct with fields:
    Orientation: [lllll
```

AngularVelocity: [5 6 7]
Gyroscope_Bias: [8 9 10]

Fuse a gyroscope measurement of [0.1 0.1 0.1] rad/s with measurement noise of diag([0.01 0.01 0.01]).

```
measure = [0.1 0.1 0.1];
measureNoise = diag([0.01 0.01 0.01]);
state = fuse(filterOrientation,sensor,measure,measureNoise)
state = 10\times1
    1.0000
            0
            0
            0
    0.0498
    0.0498
    0.0498
    0.0498
    0.0498
    0.0498
```


## Algorithms

The insGyroscope object models the angular velocity vector expressed in the sensor frame. The measurement equation is:

$$
h(x)=\omega_{\text {gyro }}+\Delta
$$

where $h(x)$ is the three-dimensional measurement output, $\omega_{\text {gyro }}$ is the angular velocity of the platform expressed in the sensor frame, and $\Delta$ is the three-dimensional bias of the sensor, modeled as a constant vector in the sensor frame.

Passing an insGyroscope object to an insEKF filter object enables the filter object to additionally track the bias of the gyroscope.

## See Also

insEKF|insOptions

Introduced in R2022a

## insGPS

Model GPS readings for sensor fusion

## Description

The insGPS object models GPS readings for sensor fusion. Passing an insGPS object to an insEKF object enables the insEKF object to fuse position and optional velocity data. For details on the GPS model, see "Algorithms" on page 2-1676.

## Creation

## Syntax

```
sensor = insGPS
```


## Description

sensor $=$ insGPS creates an insGPS object. Passing the created sensor to an insEKF object enables the insEKF object to fuse position and optional velocity data. When fusing data with the fuse object function of insEKF, pass sensor as the second argument to identify the data as obtained from a GPS.

To enable position and velocity estimation in insEKF, use a motion model that models position and velocity states, such as the insMotionPose object.

## Properties

## ReferenceLocation - Origin of local navigation reference frame

[0 0 0] (default)|three-element row vector of form [latitude longitude altitude]
Origin of the local navigation reference frame, specified as a three 3-element row vector in geodetic coordinates [latitude longitude altitude]. Altitude is the height above the reference ellipsoid model, WGS84, in meters. Latitude and longitude are in degrees.

The reference frame is a north-east-down (NED) or east-north-up (ENU) frame, based on the ReferenceFrame property of the insEKF object.
Data Types: single | double

## Examples

## Create insGPS for Use in insEKF

Create an insGPS object and pass it to an insEKF object.
sensor = insGPS;
filter = insEKF(sensor)

```
filter =
    insEKF with properties:
                            State: [16x1 double]
            StateCovariance: [16x16 double]
        AdditiveProcessNoise: [16x16 double]
            MotionModel: [1x1 insMotionPose]
            Sensors: {[1\times1 insGPS]}
            SensorNames: {'GPS'}
            ReferenceFrame: 'NED'
```

Show the state information of the filter. Since the GPS sensor reports position measurements, the filter by default models both rotational and translational motion.

```
stateinfo(filter)
ans = struct with fields:
    Orientation: [1 2 3 4]
    AngularVelocity: [5 6 7]
            Position: [8 9 10]
            Velocity: [11 12 13]
        Acceleration: [14 15 16]
```

Assume a GPS position measurement of 10 degrees in latitude, 10 degrees in longitude, and 10


```
lla = [10 10 10];
vel = [5 5 0];
llaNoise = eye(3);
velNoise = 0.1*eye(3);
```

Fuse the GPS position measurement.

```
state = fuse(filter,sensor,lla,llaNoise)
state = 16\times1
105 x
    0.0000
            0
            0
            0
            0
            0
            0
    5.5013
    5.4542
    0.9585
```

Fuse the GPS position measurement along with the velocity measurement.

```
measure = [lla vel];
measureNoise = blkdiag(llaNoise,velNoise);
state2 = fuse(filter,sensor,measure,measureNoise)
```

```
state2 = 16\times1
105 x
    0.0000
            0
            0
            0
            0
            0
            0
    7.3350
    7.2722
    1.2779
```


## Algorithms

The insGPS object models the GPS reading as the longitude, latitude, and altitude (LLA) position, and optional velocity data in the navigation frame.

Depending on whether you include the velocity data when using the fuse object function of insEKF, the measurement equation takes one of two forms:

- If you do not fuse velocity data, the measurement is the latitude in meters, longitude in degrees, and altitude in meters (LLA).
- If you fuse velocity data, the measurement is the LLA measurement, and the velocity of the platform in $\mathrm{m} / \mathrm{s}$, expressed in the reference frame defined by the ReferenceLoation property of the insGPS object and the ReferenceFrame property of the insEKF object.


## See Also

insEKF|insOptions
Introduced in R2022a

## insMagnetometer

Model magnetometer readings for sensor fusion

## Description

The insMagnetometer object models magnetometer readings for sensor fusion. Passing an insMagnetometer object to an insEKF object enables the insEKF object to fuse magnetometer data. For details on the magnetometer model, see "Algorithms" on page 2-1678.

## Creation

## Syntax

sensor $=$ insMagnetometer

## Description

sensor $=$ insMagnetometer creates an insMagnetometer object. Passing the created sensor to an insEKF object enables the insEKF object to fuse magnetometer data. When fusing data with the fuse object function of insEKF, pass sensor as the second argument to identify the data as obtained from a magnetometer.

## Examples

## Create insMagnetometer for Use in insEKF

Create an insMagnetometer object and pass it to an insEKF object.

```
sensor = insMagnetometer;
filterOrientation = insEKF(sensor)
filterOrientation =
    insEKF with properties:
                            State: [13x1 double]
            StateCovariance: [13\times13 double]
        AdditiveProcessNoise: [13x13 double]
            MotionModel: [1x1 insMotionOrientation]
                Sensors: {[1x1 insMagnetometer]}
                        SensorNames: {'Magnetometer'}
            ReferenceFrame: 'NED'
```

Show the state information of the filter. Notice that the state contains the geomagnetic vector component and the magnetometer bias component.

```
stateinfo(filterOrientation)
```

```
ans = struct with fields:
            Orientation: [lllll
    AngularVelocity: [5 6 7]
    GeomagneticVector: [8 9 10]
    Magnetometer_Bias: [11 12 13]
```

Fuse a magnetometer reading of $\left[\begin{array}{lll}27-2 & -16\end{array}\right] \mathrm{T}$ with a measurement noise of diag ([0.1 0.1 0.1]) $\mu \mathrm{T}^{2}$.

```
measure = [27 -2 -16];
measureNoise = diag([0.1 0.1 0.1]);
fuse(filterOrientation,sensor,measure,measureNoise)
ans = 13\times1
    0.9957
    -0.0032
    -0.0032
    -0.0050
            0
            0
            0
    27.5550
    -2.4168
    -16.0849
```


## Algorithms

The insMagnetometer object models the magnetometer reading as the geomagnetic vector in the sensor frame. The measurement equation is:

$$
h(x)=g_{\operatorname{mag}}+\Delta
$$

where $h(x)$ is the three-dimensional measurement output, $g_{\text {mag }}$ is the geomagnetic vector expressed in the sensor frame, and $\Delta$ is the three-dimensional bias of the sensor, which is modeled as a constant vector in the sensor frame.

Passing an insMagnetometer object to an insEKF filter object enables the filter object to additionally track the unique geomagnetic vector, as well as the bias of the magnetometer.

## See Also

insEKF |insOptions

## Introduced in R2022a

## insMotionOrientation

Motion model for 3-D orientation estimation

## Description

The insMotionOrientation object models orientation-only platform motion assuming a constant angular velocity. Passing an insMotionOrientation object to an insEKF object enables the estimation of 3-D orientation and angular velocity. For details on the motion model, see "Algorithms" on page 2-1680.

## Creation

## Syntax

model = insMotionOrientation

## Description

model = insMotionOrientation creates an insMotionOrientation object. Passing the created model to an insEKF object enables the estimation of:

- The orientation quaternion from the navigation frame to the body frame.
- The angular velocity of the platform, expressed in the body frame.


## Examples

## Create insMotionOrientation for Use in insEKF

Create an insMotionOrientation object and pass it to an insEKF object.

```
motionModel = insMotionOrientation
motionModel =
    insMotionOrientation with no properties.
filter = insEKF(motionModel)
filter =
    insEKF with properties:
                            State: [7x1 double]
            StateCovariance: [7x7 double]
        AdditiveProcessNoise: [7\times7 double]
            MotionModel: [1x1 insMotionOrientation]
                Sensors: {}
            SensorNames: {1\times0 cell}
```

```
ReferenceFrame: 'NED'
```

Show the state maintained in the filter.

```
stateinfo(filter)
ans = struct with fields:
    Orientation: [1 2 3 3 4]
    AngularVelocity: [5 6 7]
```


## Algorithms

The insMotionOrientation object models the orientation-only motion of platforms. The state equation of the motion model is:

$$
\begin{aligned}
& \dot{q}=\frac{1}{2} \omega q \\
& \dot{\omega}=0
\end{aligned}
$$

where:

- $q=\left(q_{0}, q_{1}, q_{2}, q_{3}\right)$ is the quaternion from the navigation frame to the body frame.
- $\omega$ is the angular velocity of the platform, expressed in the body frame.


## See Also

insEKF | insOptions | insMotionPose | positioning.insMotionModel
Introduced in R2022a

## insMotionPose

Model for 3-D motion estimation

## Description

The insMotionPose object models 3-D motion assuming constant angular velocity and constant linear acceleration. Passing an insMotionPose object to an insEKF object enables the estimation of 3-D motion, including orientation, angular velocity, position, linear velocity, and linear acceleration. For details on the motion model, see "Algorithms" on page 2-1682.

## Creation

## Syntax

model $=$ insMotionPose
Description
model = insMotionPose creates an insMotionPose object. Passing model to an insEKF object enables the estimation of:

- The orientation quaternion from the navigation frame to the body frame.
- The angular velocity of the platform, expressed in the body frame.
- The position of the platform, expressed in the navigation frame.
- The velocity of the platform, expressed in the navigation frame.
- The acceleration of the platform, expressed in the navigation frame.


## Examples

## Create insMotionPose for Use in insEKF

Create an insMotionPose object and pass it to an insEKF object.

```
motionModel = insMotionPose
motionModel =
    insMotionPose with no properties.
filter = insEKF(motionModel)
filter =
    insEKF with properties:
                            State: [16x1 double]
            StateCovariance: [16x16 double]
```

```
AdditiveProcessNoise: [16x16 double]
    MotionModel: [1x1 insMotionPose]
            Sensors: {}
        SensorNames: {1x0 cell}
    ReferenceFrame: 'NED'
```

Show the state maintained in the filter.

```
stateinfo(filter)
ans = struct with fields:
    Orientation: [lllll
    AngularVelocity: [5 6 7]
            Position: [8 9 10]
            Velocity: [11 12 13]
        Acceleration: [14 15 16]
```


## Algorithms

The insMotionPose object models the orientation-only motion of platforms. The state equation of the motion model is:

$$
\begin{aligned}
\dot{q} & =\frac{1}{2} \omega q \\
\dot{\omega} & =0 \\
\dot{p} & =v \\
\dot{v} & =a \\
\dot{a} & =0
\end{aligned}
$$

where:

- $q=\left(q_{0}, q_{1}, q_{2}, q_{3}\right)$ is the quaternion from the navigation frame to the body frame.
- $\omega$ is the angular velocity of the platform, expressed in the body frame.
- $\quad p$ is the position of the platform, expressed in the navigation frame.
- $v$ is the linear velocity of the platform, expressed in the navigation frame.
- $a$ is the linear acceleration of the platform, expressed in the navigation frame.


## See Also

insEKF |insOptions|insMotionOrientation| positioning.insMotionModel

## Introduced in R2022a

## positioning.INSMotionModel class

Package: positioning

Base class for defining motion models used with insEKF

## Description

The positioning. INSMotionModel class defines the base class for motion models used with INS filters. Derive from this class to define your own motion model.

To define a new motion model:

- Inherit from this class and implement at least two methods: modelstates and stateTransition.
- Optionally, if you want a higher fidelity simulation, you can implement a stateTransitionJacobian method that returns the Jacobian of the state transition function. If you do not implement this method, the object calculates the Jacobian numerically with lower accuracy and higher computation cost.

As an example of implementing this interface class, see the implementation details of insMotionOrientation by typing this in the Command Window:
edit insMotionOrientation
The positioning. INSMotionModel class is a handle class.

## Class Attributes

## Abstract true

For information on class attributes, see "Class Attributes".

## Creation

## Syntax

sensor = positioning.INSMotionModel()

## Description

sensor = positioning.INSMotionModel() creates an INS sensor model object. This constructor can only be called from a derived class.

## Methods

## Public Methods

modelstates
States for motion model
stateTransition
State transition of motion model
stateTransitionJacobian Jacobian of state transition function

## Examples

## Customize Motion Model Used with insEKF

Customize a 1-D constant velocity motion model used with an insEKF object. Customize the motion model by inheriting from the positioning. INSMotionModel interface class and implement the modelstates and stateTranistion methods. You can also optionally implement the stateTransitionJacobian method. These sections provide an overview of how the ConstantVelocityMotion class implements the positioning. INSMotionModel methods, but for more details on their implementation, see the attached ConstantVelocityMotion.m file.

## Implement modelstates method

To model 1-D constant velocity motion, you need to return only the 1-D position and velocity state as a structure. When you add a ConstantVelocityMotion object to an insEKF filter object, the filter adds the Position and Velocity components to the state vector of the filter.

## Implement stateTransition method

The stateTransition method returns the derivatives of the state defined by the motion model as a structure. The derivative of the Position is the Velocity, and the derivative of the Velocity is 0.

## Implement stateTransitionJacobian method

The stateTransitionJacobian method returns the partial derivatives of stateTransition method, with respect to the state vector of the filter, as a structure. All the partial derivatives are 0 , except the partial derivative of the derivative of the Position component, which is the Velocity, with respect to the Velocity state, is 1.

## Create and add inherited object

Create a ConstantVelocityMotion object.

```
cvModel = ConstantVelocityMotion
cvModel =
    ConstantVelocityMotion with no properties.
```

Create an insEKF object with the created cvModel object.

```
filter = insEKF(insAccelerometer,cvModel)
filter =
    insEKF with properties:
                            State: [5x1 double]
            StateCovariance: [5x5 double]
        AdditiveProcessNoise: [5x5 double]
            MotionModel: [1x1 ConstantVelocityMotion]
                Sensors: {[1x1 insAccelerometer]}
            SensorNames: {'Accelerometer'}
            ReferenceFrame: 'NED'
```

The filter state contains the Position and Velocity components.

```
stateinfo(filter)
ans = struct with fields:
    Position: 1
    Velocity: 2
    Accelerometer_Bias: [\begin{array}{lll}{3}&{4}&{5}\end{array}]
```


## Show customized ConstantVelocityMotion class

```
type ConstantVelocityMotion.m
classdef ConstantVelocityMotion < positioning.INSMotionModel
% CONSTANTVELOCITYMOTION Constant velocity motion in 1-D
% Copyright 2021 The MathWorks, Inc.
    methods
        function m = modelstates(~,~)
            % Return the state of motion model (added to the state of the
            % filter) as a structure.
            % Since the motion is 1-D constant velocity motion,
            % retrun only 1-D position and velocity state.
            m = struct('Position',0,'Velocity',0);
    end
    function sdot = stateTransition(~,filter,~, varargin)
            % Return the derivative of each state with respect to time as a
            % structure.
            % Deriviative of position = velocity.
            % Deriviative of velocity = 0 because this model assumes constant
            % velocity.
            % Find the current estimated velocity
            currentVelocityEstimate = stateparts(filter,'Velocity');
            % Return the derivatives
            sdot = struct( ...
                'Position',currentVelocityEstimate, ...
                'Velocity',0);
    end
    function dfdx = stateTransitionJacobian(~,filter,~,varargin)
            % Return the Jacobian of the stateTransition method with
            % respect to the state vector. The output is a structure with the
            % same fields as stateTransition but the value of each field is a
            % vector containing the derivative of that state relative to
            % all other states.
            % First, figure out the number of state components in the filter
            % and the corresponding indices
            N = numel(filter.State);
            idx = stateinfo(filter);
            % Compute the N partial derivatives of Position with respect to
            % the N states. The partial derivative of the derivative of the
            % Position stateTransition function with respect to Velocity is
```

```
                % just 1. All others are 0.
                dpdx = zeros(1,N);
                dpdx(1,idx.Velocity) = 1;
                % Compute the N partial derivatives of Velocity with respect to
                % the N states. In this case all the partial derivatives are 0.
                dvdx = zeros(1,N);
                % Return the partial derivatives as a structure.
                dfdx = struct('Position',dpdx,'Velocity',dvdx);
        end
    end
end
```


## See Also

insEKF|insOptions

Introduced in R2022a

## modelstates

Package: positioning
States for motion model

## Syntax

s = modelstates(filter,options)

## Description

s = modelstates(filter,options) returns a structure that describes the motion model states tracked by the insEKF filter object.

Tip After defining an insEKF object with a custom motion model, you can access the model states using the stateparts object function of insEKF.

## Examples

## Customize Motion Model Used with insEKF

Customize a 1-D constant velocity motion model used with an insEKF object. Customize the motion model by inheriting from the positioning. INSMotionModel interface class and implement the modelstates and stateTranistion methods. You can also optionally implement the stateTransitionJacobian method. These sections provide an overview of how the ConstantVelocityMotion class implements the positioning. INSMotionModel methods, but for more details on their implementation, see the attached ConstantVelocityMotion.m file.

## Implement modelstates method

To model 1-D constant velocity motion, you need to return only the 1-D position and velocity state as a structure. When you add a ConstantVelocityMotion object to an insEKF filter object, the filter adds the Position and Velocity components to the state vector of the filter.

## Implement stateTransition method

The stateTransition method returns the derivatives of the state defined by the motion model as a structure. The derivative of the Position is the Velocity, and the derivative of the Velocity is 0.

## Implement stateTransitionJacobian method

The stateTransitionJacobian method returns the partial derivatives of stateTransition method, with respect to the state vector of the filter, as a structure. All the partial derivatives are 0 , except the partial derivative of the derivative of the Position component, which is the Velocity, with respect to the Velocity state, is 1.

## Create and add inherited object

Create a ConstantVelocityMotion object.

```
cvModel = ConstantVelocityMotion
cvModel =
    ConstantVelocityMotion with no properties.
```

Create an insEKF object with the created cvModel object.

```
filter = insEKF(insAccelerometer,cvModel)
filter =
    insEKF with properties:
                            State: [5x1 double]
            StateCovariance: [5x5 double]
        AdditiveProcessNoise: [5x5 double]
            MotionModel: [1x1 ConstantVelocityMotion]
                            Sensors: {[1x1 insAccelerometer]}
                        SensorNames: {'Accelerometer'}
            ReferenceFrame: 'NED'
```

The filter state contains the Position and Velocity components.

```
stateinfo(filter)
ans = struct with fields:
    Position: 1
    Velocity: 2
    Accelerometer_Bias: [3 4 5]
```


## Show customized ConstantVelocityMotion class

```
type ConstantVelocityMotion.m
classdef ConstantVelocityMotion < positioning.INSMotionModel
% CONSTANTVELOCITYMOTION Constant velocity motion in 1-D
% Copyright 2021 The MathWorks, Inc.
    methods
        function m = modelstates(~,~)
            % Return the state of motion model (added to the state of the
            % filter) as a structure.
            % Since the motion is 1-D constant velocity motion,
            % retrun only 1-D position and velocity state.
            m = struct('Position',0,'Velocity',0);
        end
        function sdot = stateTransition(~,filter,~, varargin)
            % Return the derivative of each state with respect to time as a
                    % structure
            % Deriviative of position = velocity.
            % Deriviative of velocity = 0 because this model assumes constant
            % velocity.
            % Find the current estimated velocity
            currentVelocityEstimate = stateparts(filter,'Velocity');
```

```
            % Return the derivatives
            sdot = struct( ...
            'Position',currentVelocityEstimate, ...
            'Velocity',0);
        end
        function dfdx = stateTransitionJacobian(~,filter,~,varargin)
            % Return the Jacobian of the stateTransition method with
            % respect to the state vector. The output is a structure with the
            % same fields as stateTransition but the value of each field is a
            % vector containing the derivative of that state relative to
            % all other states.
                % First, figure out the number of state components in the filter
                    % and the corresponding indices
                    N = numel(filter.State);
                idx = stateinfo(filter);
                    % Compute the N partial derivatives of Position with respect to
                % the N states. The partial derivative of the derivative of the
                % Position stateTransition function with respect to Velocity is
                    % just 1. All others are 0.
            dpdx = zeros(1,N);
            dpdx(1,idx.Velocity) = 1;
            % Compute the N partial derivatives of Velocity with respect to
                % the N states. In this case all the partial derivatives are 0.
                    dvdx = zeros(1,N);
                        % Return the partial derivatives as a structure.
                    dfdx = struct('Position',dpdx,'Velocity',dvdx);
        end
    end
end
```


## Input Arguments

## filter - INS filter

insEKF object
INS filter, specified as an insEKF object.

## options - Options for INS filter

insOptions object
Options for the INS filter, specified as an insOptions object.

## Output Arguments

## s - State structure

structure
State structure, returned as a structure. The field names of the structure are the names of the states that you want estimate. The insEKF filter object uses the value of each field as the default value of its
corresponding state component, and uses the size of the value as the size of the corresponding state component.

Tip You can use the stateparts object function of the insEKF object to access the states, saved in the filter.

## See Also <br> stateTransition|stateTransitionJacobian <br> Introduced in R2022a

## stateTransition

Package: positioning
State transition of motion model

## Syntax

statedot = stateTransition(model,filter,dt,varargin)

## Description

statedot = stateTransition(model,filter, dt,varargin) returns the derivatives of the states of the motion model used with the INS filter.

## Examples

## Customize Motion Model Used with insEKF

Customize a 1-D constant velocity motion model used with an insEKF object. Customize the motion model by inheriting from the positioning. INSMotionModel interface class and implement the modelstates and stateTranistion methods. You can also optionally implement the stateTransitionJacobian method. These sections provide an overview of how the ConstantVelocityMotion class implements the positioning.INSMotionModel methods, but for more details on their implementation, see the attached ConstantVelocityMotion.m file.

## Implement modelstates method

To model 1-D constant velocity motion, you need to return only the 1-D position and velocity state as a structure. When you add a ConstantVelocityMotion object to an insEKF filter object, the filter adds the Position and Velocity components to the state vector of the filter.

## Implement stateTransition method

The stateTransition method returns the derivatives of the state defined by the motion model as a structure. The derivative of the Position is the Velocity, and the derivative of the Velocity is 0.

## Implement stateTransitionJacobian method

The stateTransitionJacobian method returns the partial derivatives of stateTransition method, with respect to the state vector of the filter, as a structure. All the partial derivatives are 0 , except the partial derivative of the derivative of the Position component, which is the Velocity, with respect to the Velocity state, is 1.

## Create and add inherited object

Create a ConstantVelocityMotion object.
cvModel $=$ ConstantVelocityMotion

```
cvModel =
    ConstantVelocityMotion with no properties.
```

Create an insEKF object with the created cvModel object.

```
filter = insEKF(insAccelerometer,cvModel)
filter =
    insEKF with properties:
                    State: [5x1 double]
            StateCovariance: [5x5 double]
        AdditiveProcessNoise: [5x5 double]
            MotionModel: [1x1 ConstantVelocityMotion]
                    Sensors: {[1x1 insAccelerometer]}
                    SensorNames: {'Accelerometer'}
                ReferenceFrame: 'NED'
```

The filter state contains the Position and Velocity components.

```
stateinfo(filter)
ans = struct with fields:
            Position: 1
            Velocity: 2
    Accelerometer Bias: [3 4 5]
```


## Show customized ConstantVelocityMotion class

```
type ConstantVelocityMotion.m
classdef ConstantVelocityMotion < positioning.INSMotionModel
% CONSTANTVELOCITYMOTION Constant velocity motion in 1-D
% Copyright 2021 The MathWorks, Inc.
    methods
        function m = modelstates(~,~)
            % Return the state of motion model (added to the state of the
            % filter) as a structure
            % Since the motion is 1-D constant velocity motion,
            % retrun only 1-D position and velocity state.
            m = struct('Position',0,'Velocity',0);
        end
        function sdot = stateTransition(~,filter,~, varargin)
            % Return the derivative of each state with respect to time as a
            % structure.
            % Deriviative of position = velocity.
            % Deriviative of velocity = 0 because this model assumes constant
            % velocity.
            % Find the current estimated velocity
            currentVelocityEstimate = stateparts(filter,'Velocity');
            % Return the derivatives
```

```
        sdot = struct( ...
            'Position',currentVelocityEstimate, ...
            'Velocity',0);
        end
        function dfdx = stateTransitionJacobian(~,filter,~,varargin)
            % Return the Jacobian of the stateTransition method with
            % respect to the state vector. The output is a structure with the
            % same fields as stateTransition but the value of each field is a
            % vector containing the derivative of that state relative to
            % all other states.
            % First, figure out the number of state components in the filter
            % and the corresponding indices
            N = numel(filter.State);
            idx = stateinfo(filter);
            % Compute the N partial derivatives of Position with respect to
            % the N states. The partial derivative of the derivative of the
            % Position stateTransition function with respect to Velocity is
            % just 1. All others are 0.
            dpdx = zeros(1,N);
            dpdx(1,idx.Velocity) = 1;
                        % Compute the N partial derivatives of Velocity with respect to
                    % the N states. In this case all the partial derivatives are 0.
                    dvdx = zeros(1,N);
                        % Return the partial derivatives as a structure.
                dfdx = struct('Position',dpdx,'Velocity',dvdx);
            end
    end
end
```


## Input Arguments

## model - Motion model used with INS filter

object inherited from positioning. INSMotionModel class
Motion model used with an INS filter, specified as an object inherited from the positioning. INSMotionModel abstract class.
filter - INS filter
insEKF object
INS filter, specified as an insEKF object.
dt - Filter time step
positive scalar
Filter time step, specified as a positive scalar.
Data Types: single|double

## varargin - Additional inputs

any data type

Additional inputs that are passed as the varargin inputs of the predict object function of the insEKF object.

## Output Arguments

## statedot - Derivatives of states

structure
Derivatives of the states, returned as a structure. The field names must be exactly the same as those of the structure returned by the modelstates method of model. The field values are the corresponding time derivatives of the sensor states.

## See Also <br> modelstates|stateTransitionJacobian

Introduced in R2022a

## stateTransitionJacobian

Package: positioning
Jacobian of state transition function

## Syntax

jac = stateTransitionJacobian(model,filter, dt, varargin)

## Description

jac = stateTransitionJacobian(model,filter, dt, varargin) returns the Jacobian matrix for the state transition function of the model object inherited from the positioning.INSMotionModel abstract class.

Note Implementing this method is optional for a subclass of the positioning.INSMotionModel abstract class. If you do not implement this method, the subclass uses a Jacobian matrix calculated by numerical differentiation.

## Examples

## Customize Motion Model Used with insEKF

Customize a 1-D constant velocity motion model used with an insEKF object. Customize the motion model by inheriting from the positioning. INSMotionModel interface class and implement the modelstates and stateTranistion methods. You can also optionally implement the stateTransitionJacobian method. These sections provide an overview of how the ConstantVelocityMotion class implements the positioning. INSMotionModel methods, but for more details on their implementation, see the attached ConstantVelocityMotion.m file.

## Implement modelstates method

To model 1-D constant velocity motion, you need to return only the 1-D position and velocity state as a structure. When you add a ConstantVelocityMotion object to an insEKF filter object, the filter adds the Position and Velocity components to the state vector of the filter.

## Implement stateTransition method

The stateTransition method returns the derivatives of the state defined by the motion model as a structure. The derivative of the Position is the Velocity, and the derivative of the Velocity is 0.

## Implement stateTransitionJacobian method

The stateTransitionJacobian method returns the partial derivatives of stateTransition method, with respect to the state vector of the filter, as a structure. All the partial derivatives are 0 , except the partial derivative of the derivative of the Position component, which is the Velocity, with respect to the Velocity state, is 1 .

## Create and add inherited object

Create a ConstantVelocityMotion object.
cvModel = ConstantVelocityMotion
cvModel =
ConstantVelocityMotion with no properties.

Create an insEKF object with the created cvModel object.

```
filter = insEKF(insAccelerometer,cvModel)
filter =
    insEKF with properties:
                    State: [5x1 double]
            StateCovariance: [5x5 double]
        AdditiveProcessNoise: [5x5 double]
            MotionModel: [1x1 ConstantVelocityMotion]
                    Sensors: {[1x1 insAccelerometer]}
                        SensorNames: {'Accelerometer'}
            ReferenceFrame: 'NED'
```

The filter state contains the Position and Velocity components.

```
stateinfo(filter)
ans = struct with fields:
    Position: 1
    Velocity: 2
    Accelerometer_Bias: [3 4 5]
```


## Show customized ConstantVelocityMotion class

```
type ConstantVelocityMotion.m
classdef ConstantVelocityMotion < positioning.INSMotionModel
% CONSTANTVELOCITYMOTION Constant velocity motion in 1-D
% Copyright 2021 The MathWorks, Inc.
    methods
        function m = modelstates(~,~)
            % Return the state of motion model (added to the state of the
            % filter) as a structure.
            % Since the motion is 1-D constant velocity motion,
            % retrun only l-D position and velocity state.
            m = struct('Position',0,'Velocity',0);
        end
        function sdot = stateTransition(~,filter,~, varargin)
            % Return the derivative of each state with respect to time as a
            % structure.
            % Deriviative of position = velocity.
            % Deriviative of velocity = 0 because this model assumes constant
```

```
            % velocity.
            % Find the current estimated velocity
            currentVelocityEstimate = stateparts(filter,'Velocity');
            % Return the derivatives
            sdot = struct( ...
            'Position',currentVelocityEstimate, ...
            'Velocity',0);
                end
                function dfdx = stateTransitionJacobian(~,filter,~,varargin)
            % Return the Jacobian of the stateTransition method with
            % respect to the state vector. The output is a structure with the
            % same fields as stateTransition but the value of each field is a
            % vector containing the derivative of that state relative to
            % all other states.
            % First, figure out the number of state components in the filter
            % and the corresponding indices
            N = numel(filter.State);
            idx = stateinfo(filter);
            % Compute the N partial derivatives of Position with respect to
            % the N states. The partial derivative of the derivative of the
            % Position stateTransition function with respect to Velocity is
            % just 1. All others are 0.
            dpdx = zeros(1,N);
            dpdx(1,idx.Velocity) = 1;
            % Compute the N partial derivatives of Velocity with respect to
            % the N states. In this case all the partial derivatives are 0.
            dvdx = zeros(1,N);
            % Return the partial derivatives as a structure.
            dfdx = struct('Position',dpdx,'Velocity',dvdx);
        end
    end
end
```


## Input Arguments

## model - Motion model used with INS filter

object inherited from positioning. INSMotionModel class
Motion model used with an INS filter, specified as an object inherited from the positioning. INSMotionModel abstract class.

## filter - INS filter

insEKF object
INS filter, specified as an insEKF object.

## dt - Filter time step

positive scalar
Filter time step, specified as a positive scalar.

Data Types: single | double
varargin - Additional inputs
any data type
Additional inputs that are passed as the varargin inputs of the predict object function of the insEKF object.

## Output Arguments

## jac - Jacobian matrix for state transition equation

$S$-by- $N$ real-valued matrix
Jacobian matrix for the state transition equation, returned as an $S$-by- $N$ real-valued matrix. $S$ is the number of fields in the returned structure of the modelstates method of the motion model, and $N$ is the dimension of the state maintained in the State property of the filter.

See Also<br>modelstates|stateTransition

Introduced in R2022a

## positioning.INSSensorModel class

Package: positioning

Base class for defining sensor models used with insEKF

## Description

The positioning.INSSensorModel class defines the base class for sensor models used with INS filters. Derive from this class to define your own sensor model.

To define a new sensor:

- Inherit from this class and implement at least the measurement method.
- Optionally, if you want a higher fidelity simulation, you can implement the measurementJacobian method that returns the Jacobian of the measurement function. If you do not implement this method, the object calculates a Jacobian numerically with lower accuracy and higher computation cost.

If the sensor model definition requires the use of the tracked state, you must additionally:

- Implement the sensorStates method to define the tracked state.
- Optionally, you can implement the stateTransition method if the state is not constant over time.
- Optionally, you can implement the stateTransitionJacobian method (that returns the Jacobian of the state transition function) for a higher fidelity simulation. If you do not implement this method, the object calculates the Jacobian numerically with lower accuracy and higher computation cost.

As an example of implementing this interface class, see the implementation details of insAccelerometer by typing this in the Command Window:

```
edit insGyroscope
```

The positioning. INSSensorModel class is a handle class.

## Class Attributes

```
Abstract true
```

For information on class attributes, see "Class Attributes".

## Creation

## Syntax

```
sensor = positioning.INSSensorModel()
```


## Description

sensor $=$ positioning.INSSensorModel() creates an INS sensor model object. This constructor can only be called from a derived class.

## Methods

## Public Methods

measurement measurementJacobian sensorStates stateTransition stateTransitionJacobian Jacobian of sensor state transition function

## Examples

## Customize Sensor Model Used with insEKF

Customize a sensor model used with the insEKF object. The sensor measures the velocity state, including a bias affected by random noise.

Customize the sensor model by inheriting from the positioning. INSSensorModel interface class and implementing its methods. Note that only the measurement method is required for implementation in the positioning. INSSensorModel interface class. These sections provide an overview of how the BiasSensor class implements the positioning. INSSensorModel methods, but for details on their implementation, see the details of the implementation are in the attached BiasSensor.m file.

## Implement sensorStates method

To model bias, the sensorStates method needs to return a state, Bias, as a structure. When you add a BiasSensor object to an insEKF filter object, the filter adds the bias component to the state vector of the filter.

## Implement measurement method

The measurement is the velocity component of the filter state, including the bias. Therefore, return the summation of the velocity component from the filter and the bias.

## Implement measurementJacobian method

The measurementJacobian method returns the partial derivative of the measurement method with respect to the state vector of the filter as a structure. All the partial derivatives are 0, except the partial derivatives of the measurement with respect to the velocity and bias state components.

## Implement stateTransition method

The stateTransiton method returns the derivative of the sensor state defined in the sensorStates method. Assume the derivative of the bias is affected by a white noise with a standard deviation of 0.01 . Return the derivative as a structure. Note that this only showcases how to set up the method, and does not correspond to any practical application.

## Implement stateTransitionJacobian method

Since the stateTransiton function does not depend on the state of the filter, the Jacobian matrix is 0.

## Create and add inherited object

Create a BiasSensor object.

```
biSensor = BiasSensor
biSensor =
    BiasSensor with no properties.
```

Create an insEKF object with the biSensor object.

```
filter = insEKF(biSensor,insMotionPose)
filter =
    insEKF with properties:
                    State: [17x1 double]
            StateCovariance: [17x17 double]
        AdditiveProcessNoise: [17x17 double]
                MotionModel: [1x1 insMotionPose]
                    Sensors: {[1x1 BiasSensor]}
                SensorNames: {'BiasSensor'}
            ReferenceFrame: 'NED'
```

The filter state contains the bias component.

```
stateinfo(filter)
ans = struct with fields:
    Orientation: [lllll
    AngularVelocity: [5 6 7]
            Position: [8 9 10]
            Velocity: [11 12 13]
        Acceleration: [14 15 16]
    BiasSensor Bias: 17
```


## Show customized BiasSensor class

```
type BiasSensor.m
classdef BiasSensor < positioning.INSSensorModel
%BIASSENSOR Sensor measuring velocity with bias
% Copyright 2021 The MathWorks, Inc.
    methods
        function s = sensorstates(~,~)
            % Assume the sensor has a bias. Define a Bias state to enable
            % the filter to estimate the bias.
            s = struct('Bias',0);
        end
```

```
    function z = measurement(sensor,filter)
        % Measurement is the summation of the velocity measurement and
        % the bias.
        velocity = stateparts(filter,'Velocity');
        bias = stateparts(filter,sensor,'Bias');
        z = velocity + bias;
end
function dzdx = measurementJacobian(sensor,filter)
    % Compute the Jacobian, which is the partial derivative of the
    % measurement (velocity plus bias) with respect to the filter
    % state vector.
    % Obtain the dimension of the filter state.
    N = numel(filter.State);
    % The partial derviative of the Bias with respect to all the
    % states is zero, except the Bias state itself.
    dzdx = zeros(1,N);
    % Obtain the index for the Bias state component in the filter.
    bidx = stateinfo(filter,sensor,'Bias');
    dzdx(:,bidx) = 1;
    % The partial derivative of the Velocity with respect to all the
    % states is zero, except the Velocity state itself.
    vidx = stateinfo(filter,'Velocity');
    dzdx(:,vidx) = 1;
end
    function dBias = stateTransition(~,~,dt,~)
        % Assume the derivative of the bias is affected by a zero-mean
        % white noise with a standard deviation of 0.01.
        noise = 0.01*randn*dt;
        dBias = struct('Bias',noise);
        end
        function dBiasdx = stateTransitonJacobian(~,filter,~,~)
        % Since the stateTransiton function does not depend on the
        % state of the filter, the Jacobian is all zero.
        N = numel(filter.State);
        dBiasdx = zeros(1,N);
        end
    end
```

end

## See Also

insEKF|insOptions

Introduced in R2022a

## measurement

Package: positioning
Sensor measurement from states

## Syntax

z = measurement(sensor,filter)

## Description

$z=$ measurement(sensor,filter) returns the measurement $z$ from the state maintained in the filter object. You must implement this method when you define a sensor object based on the positioning.INSSensorModel abstract class.

## Examples

## Customize Sensor Model Used with insEKF

Customize a sensor model used with the insEKF object. The sensor measures the velocity state, including a bias affected by random noise.

Customize the sensor model by inheriting from the positioning. INSSensorModel interface class and implementing its methods. Note that only the measurement method is required for implementation in the positioning. INSSensorModel interface class. These sections provide an overview of how the BiasSensor class implements the positioning. INSSensorModel methods, but for details on their implementation, see the details of the implementation are in the attached BiasSensor.m file.

## Implement sensorStates method

To model bias, the sensorStates method needs to return a state, Bias, as a structure. When you add a BiasSensor object to an insEKF filter object, the filter adds the bias component to the state vector of the filter.

## Implement measurement method

The measurement is the velocity component of the filter state, including the bias. Therefore, return the summation of the velocity component from the filter and the bias.

## Implement measurementJacobian method

The measurementJacobian method returns the partial derivative of the measurement method with respect to the state vector of the filter as a structure. All the partial derivatives are 0, except the partial derivatives of the measurement with respect to the velocity and bias state components.

## Implement stateTransition method

The stateTransiton method returns the derivative of the sensor state defined in the sensorStates method. Assume the derivative of the bias is affected by a white noise with a
standard deviation of 0.01 . Return the derivative as a structure. Note that this only showcases how to set up the method, and does not correspond to any practical application.

## Implement stateTransitionJacobian method

Since the stateTransiton function does not depend on the state of the filter, the Jacobian matrix is 0.

## Create and add inherited object

Create a BiasSensor object.
biSensor = BiasSensor
biSensor =
BiasSensor with no properties.

Create an insEKF object with the biSensor object.

```
filter = insEKF(biSensor,insMotionPose)
filter =
    insEKF with properties:
                            State: [17x1 double]
            StateCovariance: [17\times17 double]
        AdditiveProcessNoise: [17x17 double]
                MotionModel: [1x1 insMotionPose]
                    Sensors: {[1x1 BiasSensor]}
                SensorNames: {'BiasSensor'}
            ReferenceFrame: 'NED'
```

The filter state contains the bias component.

```
stateinfo(filter)
ans = struct with fields:
    Orientation: [lllll
    AngularVelocity: [5 6 7]
            Position: [8 9 10]
            Velocity: [11 12 13]
        Acceleration: [14 15 16]
    BiasSensor_Bias: 17
```


## Show customized BiasSensor class

```
type BiasSensor.m
classdef BiasSensor < positioning.INSSensorModel
%BIASSENSOR Sensor measuring velocity with bias
% Copyright 2021 The MathWorks, Inc.
    methods
        function s = sensorstates(~,~)
            % Assume the sensor has a bias. Define a Bias state to enable
```

```
    % the filter to estimate the bias.
    s = struct('Bias',0);
end
    function z = measurement(sensor,filter)
    % Measurement is the summation of the velocity measurement and
    % the bias.
    velocity = stateparts(filter,'Velocity');
    bias = stateparts(filter,sensor,'Bias');
    z = velocity + bias;
end
    function dzdx = measurementJacobian(sensor,filter)
    % Compute the Jacobian, which is the partial derivative of the
    % measurement (velocity plus bias) with respect to the filter
    % state vector.
    % Obtain the dimension of the filter state.
    N = numel(filter.State);
    % The partial derviative of the Bias with respect to all the
    % states is zero, except the Bias state itself.
    dzdx = zeros(1,N);
    % Obtain the index for the Bias state component in the filter.
    bidx = stateinfo(filter,sensor,'Bias');
    dzdx(:,bidx) = 1;
    % The partial derivative of the Velocity with respect to all the
    % states is zero, except the Velocity state itself.
    vidx = stateinfo(filter,'Velocity');
    dzdx(:,vidx) = 1;
    end
    function dBias = stateTransition(~,~,dt,~)
        % Assume the derivative of the bias is affected by a zero-mean
        % white noise with a standard deviation of 0.01.
        noise = 0.01*randn*dt;
        dBias = struct('Bias',noise);
    end
    function dBiasdx = stateTransitonJacobian(~,filter,~,~)
        % Since the stateTransiton function does not depend on the
        % state of the filter, the Jacobian is all zero.
        N = numel(filter.State);
        dBiasdx = zeros(1,N);
    end
    end
end
```


## Input Arguments

## sensor - Sensor model used with INS filter

object inherited from positioning. INSSensorModel class
Sensor model used with an INS filter, specified as an object inherited from the positioning. INSSensorModel abstract class.
filter - INS filter
insEKF object
INS filter, specified as an insEKF object.

## Output Arguments

z - Measurement
$M$-by-1 real-valued vector
Measurement, returned as an $M$-by- 1 real-valued vector.

## See Also

measurementJacobian | sensorStates| stateTransition| stateTransitionJacobian

Introduced in R2022a

# measurementJacobian 

Package: positioning
Jacobian of measurement function

## Syntax

jac = measurementJacobian(sensor,filter)

## Description

jac = measurementJacobian(sensor,filter) returns the Jacobian matrix for the measurement function of the sensor object, inherited from the positioning. INSSensorModel abstract class.

Note Implementing this method is optional for a subclass of the positioning.INSSensorModel abstract class. If you do not implement this method, the subclass uses a Jacobian matrix calculated by numerical differentiation.

## Examples

## Customize Sensor Model Used with insEKF

Customize a sensor model used with the insEKF object. The sensor measures the velocity state, including a bias affected by random noise.

Customize the sensor model by inheriting from the positioning. INSSensorModel interface class and implementing its methods. Note that only the measurement method is required for implementation in the positioning. INSSensorModel interface class. These sections provide an overview of how the BiasSensor class implements the positioning. INSSensorModel methods, but for details on their implementation, see the details of the implementation are in the attached BiasSensor.m file.

## Implement sensorStates method

To model bias, the sensorStates method needs to return a state, Bias, as a structure. When you add a BiasSensor object to an insEKF filter object, the filter adds the bias component to the state vector of the filter.

## Implement measurement method

The measurement is the velocity component of the filter state, including the bias. Therefore, return the summation of the velocity component from the filter and the bias.

## Implement measurementJacobian method

The measurementJacobian method returns the partial derivative of the measurement method with respect to the state vector of the filter as a structure. All the partial derivatives are 0, except the partial derivatives of the measurement with respect to the velocity and bias state components.

## Implement stateTransition method

The stateTransiton method returns the derivative of the sensor state defined in the sensorStates method. Assume the derivative of the bias is affected by a white noise with a standard deviation of 0.01 . Return the derivative as a structure. Note that this only showcases how to set up the method, and does not correspond to any practical application.

## Implement stateTransitionJacobian method

Since the stateTransiton function does not depend on the state of the filter, the Jacobian matrix is 0.

## Create and add inherited object

Create a BiasSensor object.
biSensor = BiasSensor
biSensor =
BiasSensor with no properties.

Create an insEKF object with the biSensor object.

```
filter = insEKF(biSensor,insMotionPose)
filter =
    insEKF with properties:
                    State: [17x1 double]
            StateCovariance: [17\times17 double]
        AdditiveProcessNoise: [17x17 double]
            MotionModel: [1x1 insMotionPose]
                    Sensors: {[1x1 BiasSensor]}
                        SensorNames: {'BiasSensor'}
            ReferenceFrame: 'NED'
```

The filter state contains the bias component.

```
stateinfo(filter)
ans = struct with fields:
            Orientation: [1 2 3 4]
        AngularVelocity: [5 6 7]
            Position: [8 9 10]
            Velocity: [11 12 13]
        Acceleration: [14 15 16]
    BiasSensor Bias: 17
```


## Show customized BiasSensor class

```
type BiasSensor.m
classdef BiasSensor < positioning.INSSensorModel
%BIASSENSOR Sensor measuring velocity with bias
% Copyright 2021 The MathWorks, Inc.
    methods
        function s = sensorstates(~,~)
            % Assume the sensor has a bias. Define a Bias state to enable
            % the filter to estimate the bias.
            s = struct('Bias',0);
    end
    function z = measurement(sensor,filter)
        % Measurement is the summation of the velocity measurement and
        % the bias.
        velocity = stateparts(filter,'Velocity');
        bias = stateparts(filter,sensor,'Bias');
        z = velocity + bias;
    end
    function dzdx = measurementJacobian(sensor,filter)
        % Compute the Jacobian, which is the partial derivative of the
        % measurement (velocity plus bias) with respect to the filter
        % state vector.
        % Obtain the dimension of the filter state.
        N = numel(filter.State);
        % The partial derviative of the Bias with respect to all the
        % states is zero, except the Bias state itself.
        dzdx = zeros(1,N);
        % Obtain the index for the Bias state component in the filter.
        bidx = stateinfo(filter,sensor,'Bias');
        dzdx(:,bidx) = 1;
        % The partial derivative of the Velocity with respect to all the
        % states is zero, except the Velocity state itself.
        vidx = stateinfo(filter,'Velocity');
        dzdx(:,vidx) = 1;
    end
    function dBias = stateTransition(~,~,dt,~)
        % Assume the derivative of the bias is affected by a zero-mean
        % white noise with a standard deviation of 0.01.
        noise = 0.01*randn*dt;
        dBias = struct('Bias',noise);
    end
    function dBiasdx = stateTransitonJacobian(~,filter,~,~)
        % Since the stateTransiton function does not depend on the
        % state of the filter, the Jacobian is all zero.
        N = numel(filter.State);
        dBiasdx = zeros(1,N);
    end
```

end
end

## Input Arguments

## sensor - Sensor model used with INS filter

object inherited from positioning. INSSensorModel class
Sensor model used with an INS filter, specified as an object inherited from the positioning.INSSensorModel abstract class.
filter - INS filter
insEKF object
INS filter, specified as an insEKF object.

## Output Arguments

## jac - Jacobian matrix for measurement equation

$M$-by- $N$ real-valued matrix
Jacobian matrix for the measurement equation, returned as an $M$-by- $N$ real-valued matrix. $M$ is the dimension of the sensor measurement, and $N$ is the dimension of the state maintained in the State property of the filter.

## See Also

measurement | sensorStates | stateTransition | stateTransitionJacobian
Introduced in R2022a

## sensorStates

Package: positioning
Sensor states

## Syntax

s = sensorStates(filter,options)

## Description

$\mathrm{s}=$ sensorStates(filter,options) returns a structure that describes the states used by the sensor model and tracked by the insEKF filter object.

Tip Implement this method only if you want to estimate sensor-specific states, such as biases, using the filter.

## Examples

## Customize Sensor Model Used with insEKF

Customize a sensor model used with the insEKF object. The sensor measures the velocity state, including a bias affected by random noise.

Customize the sensor model by inheriting from the positioning. INSSensorModel interface class and implementing its methods. Note that only the measurement method is required for implementation in the positioning. INSSensorModel interface class. These sections provide an overview of how the BiasSensor class implements the positioning. INSSensorModel methods, but for details on their implementation, see the details of the implementation are in the attached BiasSensor.m file.

## Implement sensorStates method

To model bias, the sensorStates method needs to return a state, Bias, as a structure. When you add a BiasSensor object to an insEKF filter object, the filter adds the bias component to the state vector of the filter.

## Implement measurement method

The measurement is the velocity component of the filter state, including the bias. Therefore, return the summation of the velocity component from the filter and the bias.

## Implement measurementJacobian method

The measurementJacobian method returns the partial derivative of the measurement method with respect to the state vector of the filter as a structure. All the partial derivatives are 0, except the partial derivatives of the measurement with respect to the velocity and bias state components.

## Implement stateTransition method

The stateTransiton method returns the derivative of the sensor state defined in the sensorStates method. Assume the derivative of the bias is affected by a white noise with a standard deviation of 0.01 . Return the derivative as a structure. Note that this only showcases how to set up the method, and does not correspond to any practical application.

## Implement stateTransitionJacobian method

Since the stateTransiton function does not depend on the state of the filter, the Jacobian matrix is 0.

## Create and add inherited object

Create a BiasSensor object.

```
biSensor = BiasSensor
biSensor =
    BiasSensor with no properties.
```

Create an insEKF object with the biSensor object.

```
filter = insEKF(biSensor,insMotionPose)
filter =
    insEKF with properties:
                            State: [17x1 double]
            StateCovariance: [17\times17 double]
        AdditiveProcessNoise: [17x17 double]
            MotionModel: [1x1 insMotionPose]
            Sensors: {[1x1 BiasSensor]}
                        SensorNames: {'BiasSensor'}
            ReferenceFrame: 'NED'
```

The filter state contains the bias component.

```
stateinfo(filter)
ans = struct with fields:
    Orientation: [lllll
    AngularVelocity: [5 6 7]
            Position: [8 9 10]
            Velocity: [11 12 13]
        Acceleration: [14 15 16]
    BiasSensor_Bias: 17
```


## Show customized BiasSensor class

```
type BiasSensor.m
classdef BiasSensor < positioning.INSSensorModel
%BIASSENSOR Sensor measuring velocity with bias
% Copyright 2021 The MathWorks, Inc.
```

```
    methods
        function s = sensorstates(~,~)
        % Assume the sensor has a bias. Define a Bias state to enable
        % the filter to estimate the bias.
        s = struct('Bias',0);
    end
    function z = measurement(sensor,filter)
        % Measurement is the summation of the velocity measurement and
        % the bias.
        velocity = stateparts(filter,'Velocity');
        bias = stateparts(filter,sensor,'Bias');
        z = velocity + bias;
    end
    function dzdx = measurementJacobian(sensor,filter)
        % Compute the Jacobian, which is the partial derivative of the
        % measurement (velocity plus bias) with respect to the filter
        % state vector.
        % Obtain the dimension of the filter state.
        N = numel(filter.State);
        % The partial derviative of the Bias with respect to all the
        % states is zero, except the Bias state itself.
        dzdx = zeros(1,N);
        % Obtain the index for the Bias state component in the filter.
        bidx = stateinfo(filter,sensor,'Bias');
        dzdx(:,bidx) = 1;
            % The partial derivative of the Velocity with respect to all the
            % states is zero, except the Velocity state itself.
            vidx = stateinfo(filter,'Velocity');
            dzdx(:,vidx) = 1;
    end
    function dBias = stateTransition(~,~,dt,~)
        % Assume the derivative of the bias is affected by a zero-mean
        % white noise with a standard deviation of 0.01.
        noise = 0.01*randn*dt;
        dBias = struct('Bias',noise);
    end
    function dBiasdx = stateTransitonJacobian(~,filter,~,~)
        % Since the stateTransiton function does not depend on the
        % state of the filter, the Jacobian is all zero.
        N = numel(filter.State);
        dBiasdx = zeros(1,N);
    end
end
```

end

## Input Arguments

filter - INS filter
insEKF object
INS filter, specified as an insEKF object.

```
options - Options for INS filter
insOptions object
```

Options for the INS filter, specified as an insOptions object.

## Output Arguments

## s - State structure <br> structure

State structure, returned as a structure. The field names of the structure are the names of the states that you want estimate. The filter uses the value of each field as the default value of the corresponding state component, and uses the size of the value as the size of the corresponding state component.

Tip You can use the stateparts object function of the insEKF filter object to access the states saved in the filter.

```
See Also
measurement | measurementJacobian| stateTransition| stateTransitionJacobian
Introduced in R2022a
```


## stateTransition

Package: positioning
State transition of sensor states

## Syntax

statedot = stateTransition(sensor,filter,dt,varargin)

## Description

statedot = stateTransition(sensor,filter, dt,varargin) returns the derivatives of the states of the sensor used in the INS filter.

Tip You only need to implement this method for the sensor object inherited from the positioning. INSSensorModel abstract class if you both of these two conditions are true:

- You have implemented the sensorStates method of the sensor.
- The states of the sensor are time-varying.


## Examples

## Customize Sensor Model Used with insEKF

Customize a sensor model used with the insEKF object. The sensor measures the velocity state, including a bias affected by random noise.

Customize the sensor model by inheriting from the positioning. INSSensorModel interface class and implementing its methods. Note that only the measurement method is required for implementation in the positioning. INSSensorModel interface class. These sections provide an overview of how the BiasSensor class implements the positioning. INSSensorModel methods, but for details on their implementation, see the details of the implementation are in the attached BiasSensor.m file.

## Implement sensorStates method

To model bias, the sensorStates method needs to return a state, Bias, as a structure. When you add a BiasSensor object to an insEKF filter object, the filter adds the bias component to the state vector of the filter.

## Implement measurement method

The measurement is the velocity component of the filter state, including the bias. Therefore, return the summation of the velocity component from the filter and the bias.

## Implement measurementJacobian method

The measurementJacobian method returns the partial derivative of the measurement method with respect to the state vector of the filter as a structure. All the partial derivatives are 0, except the partial derivatives of the measurement with respect to the velocity and bias state components.

## Implement stateTransition method

The stateTransiton method returns the derivative of the sensor state defined in the sensorStates method. Assume the derivative of the bias is affected by a white noise with a standard deviation of 0.01 . Return the derivative as a structure. Note that this only showcases how to set up the method, and does not correspond to any practical application.

## Implement stateTransitionJacobian method

Since the stateTransiton function does not depend on the state of the filter, the Jacobian matrix is 0.

## Create and add inherited object

Create a BiasSensor object.
biSensor = BiasSensor
biSensor =
BiasSensor with no properties.

Create an insEKF object with the biSensor object.

```
filter = insEKF(biSensor,insMotionPose)
filter =
    insEKF with properties:
                            State: [17x1 double]
            StateCovariance: [17x17 double]
        AdditiveProcessNoise: [17x17 double]
            MotionModel: [1x1 insMotionPose]
                    Sensors: {[1x1 BiasSensor]}
                        SensorNames: {'BiasSensor'}
                ReferenceFrame: 'NED'
```

The filter state contains the bias component.

```
stateinfo(filter)
ans = struct with fields:
    Orientation: [1 2 3 4]
        AngularVelocity: [5 6 7]
            Position: [8 9 10]
            Velocity: [11 12 13]
        Acceleration: [14 15 16]
    BiasSensor Bias: 17
```


## Show customized BiasSensor class

```
type BiasSensor.m
classdef BiasSensor < positioning.INSSensorModel
%BIASSENSOR Sensor measuring velocity with bias
% Copyright 2021 The MathWorks, Inc.
    methods
        function s = sensorstates(~,~)
            % Assume the sensor has a bias. Define a Bias state to enable
            % the filter to estimate the bias.
            s = struct('Bias',0);
    end
    function z = measurement(sensor,filter)
        % Measurement is the summation of the velocity measurement and
        % the bias.
        velocity = stateparts(filter,'Velocity');
        bias = stateparts(filter,sensor,'Bias');
        z = velocity + bias;
    end
    function dzdx = measurementJacobian(sensor,filter)
        % Compute the Jacobian, which is the partial derivative of the
        % measurement (velocity plus bias) with respect to the filter
        % state vector.
        % Obtain the dimension of the filter state.
        N = numel(filter.State);
        % The partial derviative of the Bias with respect to all the
        % states is zero, except the Bias state itself.
        dzdx = zeros(1,N);
        % Obtain the index for the Bias state component in the filter.
        bidx = stateinfo(filter,sensor,'Bias');
        dzdx(:,bidx) = 1;
        % The partial derivative of the Velocity with respect to all the
        % states is zero, except the Velocity state itself.
        vidx = stateinfo(filter,'Velocity');
        dzdx(:,vidx) = 1;
    end
    function dBias = stateTransition(~,~,dt,~)
        % Assume the derivative of the bias is affected by a zero-mean
        % white noise with a standard deviation of 0.01.
        noise = 0.01*randn*dt;
        dBias = struct('Bias',noise);
    end
    function dBiasdx = stateTransitonJacobian(~,filter,~,~)
        % Since the stateTransiton function does not depend on the
        % state of the filter, the Jacobian is all zero.
        N = numel(filter.State);
        dBiasdx = zeros(1,N);
    end
```

end
end

## Input Arguments

## sensor - Sensor model used with INS filter

object inherited from positioning. INSSensorModel class
Sensor model used with an INS filter, specified as an object inherited from the positioning.INSSensorModel abstract class.
filter - INS filter
insEKF object
INS filter, specified as an insEKF object.
dt - Filter time step
positive scalar
Filter time step, specified as a positive scalar.
Data Types: single | double
varargin - Additional inputs
any data type
Additional inputs that are passed as the varargin inputs of the predict object function of the insEKF object.

## Output Arguments

## statedot - Derivatives of sensor states

structure
Derivatives of the sensor states, returned as a structure. The field names must be exactly the same as those of the sensorStates method of sensor. The field values are the corresponding time derivatives of the sensor states.

```
See Also
measurement |measurementJacobian| sensorStates|stateTransitionJacobian
Introduced in R2022a
```


## stateTransitionJacobian

Package: positioning
Jacobian of sensor state transition function

## Syntax

```
jac = stateTransitionJacobian(sensor,filter,dt,varargin)
```


## Description

jac = stateTransitionJacobian(sensor,filter, dt, varargin) returns the Jacobian matrix for the state transition function of the sensor object inherited from the positioning. INSSensorModel abstract class.

Note Implementing this method is optional for a subclass of the positioning.INSSensorModel abstract class. If you do not implement this method, the subclass uses a Jacobian matrix calculated by numerical differentiation.

## Examples

## Customize Sensor Model Used with insEKF

Customize a sensor model used with the insEKF object. The sensor measures the velocity state, including a bias affected by random noise.

Customize the sensor model by inheriting from the positioning. INSSensorModel interface class and implementing its methods. Note that only the measurement method is required for implementation in the positioning. INSSensorModel interface class. These sections provide an overview of how the BiasSensor class implements the positioning. INSSensorModel methods, but for details on their implementation, see the details of the implementation are in the attached BiasSensor.m file.

## Implement sensorStates method

To model bias, the sensorStates method needs to return a state, Bias, as a structure. When you add a BiasSensor object to an insEKF filter object, the filter adds the bias component to the state vector of the filter.

## Implement measurement method

The measurement is the velocity component of the filter state, including the bias. Therefore, return the summation of the velocity component from the filter and the bias.

## Implement measurementJacobian method

The measurementJacobian method returns the partial derivative of the measurement method with respect to the state vector of the filter as a structure. All the partial derivatives are 0, except the partial derivatives of the measurement with respect to the velocity and bias state components.

## Implement stateTransition method

The stateTransiton method returns the derivative of the sensor state defined in the sensorStates method. Assume the derivative of the bias is affected by a white noise with a standard deviation of 0.01 . Return the derivative as a structure. Note that this only showcases how to set up the method, and does not correspond to any practical application.

## Implement stateTransitionJacobian method

Since the stateTransiton function does not depend on the state of the filter, the Jacobian matrix is 0.

## Create and add inherited object

Create a BiasSensor object.
biSensor = BiasSensor
biSensor =
BiasSensor with no properties.

Create an insEKF object with the biSensor object.

```
filter = insEKF(biSensor,insMotionPose)
filter =
    insEKF with properties:
                            State: [17x1 double]
            StateCovariance: [17x17 double]
        AdditiveProcessNoise: [17x17 double]
            MotionModel: [1x1 insMotionPose]
                    Sensors: {[1x1 BiasSensor]}
                        SensorNames: {'BiasSensor'}
                ReferenceFrame: 'NED'
```

The filter state contains the bias component.

```
stateinfo(filter)
ans = struct with fields:
    Orientation: [1 2 3 4]
        AngularVelocity: [5 6 7]
            Position: [8 9 10]
            Velocity: [11 12 13]
        Acceleration: [14 15 16]
    BiasSensor Bias: 17
```


## Show customized BiasSensor class

```
type BiasSensor.m
classdef BiasSensor < positioning.INSSensorModel
%BIASSENSOR Sensor measuring velocity with bias
% Copyright 2021 The MathWorks, Inc.
    methods
        function s = sensorstates(~,~)
            % Assume the sensor has a bias. Define a Bias state to enable
            % the filter to estimate the bias.
            s = struct('Bias',0);
    end
    function z = measurement(sensor,filter)
        % Measurement is the summation of the velocity measurement and
        % the bias.
        velocity = stateparts(filter,'Velocity');
        bias = stateparts(filter,sensor,'Bias');
        z = velocity + bias;
    end
    function dzdx = measurementJacobian(sensor,filter)
        % Compute the Jacobian, which is the partial derivative of the
        % measurement (velocity plus bias) with respect to the filter
        % state vector.
        % Obtain the dimension of the filter state.
        N = numel(filter.State);
        % The partial derviative of the Bias with respect to all the
        % states is zero, except the Bias state itself.
        dzdx = zeros(1,N);
        % Obtain the index for the Bias state component in the filter.
        bidx = stateinfo(filter,sensor,'Bias');
        dzdx(:,bidx) = 1;
        % The partial derivative of the Velocity with respect to all the
        % states is zero, except the Velocity state itself.
        vidx = stateinfo(filter,'Velocity');
        dzdx(:,vidx) = 1;
    end
    function dBias = stateTransition(~,~,dt,~)
        % Assume the derivative of the bias is affected by a zero-mean
        % white noise with a standard deviation of 0.01.
        noise = 0.01*randn*dt;
        dBias = struct('Bias',noise);
    end
    function dBiasdx = stateTransitonJacobian(~,filter,~,~)
        % Since the stateTransiton function does not depend on the
        % state of the filter, the Jacobian is all zero.
        N = numel(filter.State);
        dBiasdx = zeros(1,N);
    end
```

end
end

## Input Arguments

## sensor - Sensor model used with INS filter

object inherited from positioning. INSSensorModel class
Sensor model used with an INS filter, specified as an object inherited from the positioning.INSSensorModel abstract class.
filter - INS filter
insEKF object
INS filter, specified as an insEKF object.
dt - Filter time step
positive scalar
Filter time step, specified as a positive scalar.
Data Types: single | double
varargin - Additional inputs
any data type
Additional inputs that are passed as the varargin inputs of the predict object function of the insEKF object.

## Output Arguments

## jac - Jacobian matrix for state transition equation

$S$-by- $N$ real-valued matrix
Jacobian matrix for the state transition equation, returned as an $N S$-by- $N$ real-valued matrix. $S$ is the number of fields in the returned structure of the sensorState method of sensor, and $N$ is the dimension of the state maintained in the State property of the filter.

```
See Also
measurement | measurementJacobian| sensorStates| stateTransition
Introduced in R2022a
```


## Methods

## addPlanner

Add path planner for benchmarking

## Syntax

addPlanner(plannerBM, planFcn)
addPlanner(plannerBM, planFcn,initializationFcn)
addPlanner( $\qquad$ ,Name=Value)

## Description

addPlanner ( $\mathrm{plannerBM}, \mathrm{planFcn}$ ) adds the plan function of a planner as a function handle planFcn to the plannerBenchmark object.
addPlanner (plannerBM, planFcn, initializationFcn) also adds the initialization function of a planner as a function handle initializationFen to the plannerBenchmark object.
addPlanner( $\qquad$ ,Name=Value) specifies options using one or more name-value arguments in addition to any combination of input arguments from previous syntaxes.

## Examples

## Benchmark 2-D Path Planners

Create an occupancy map from an example map.

```
load("exampleMaps.mat","simpleMap");
map = occupancyMap(simpleMap);
```

Create a state validator with stateSpaceSE2 using the map.
sv = validatorOccupancyMap(stateSpaceSE2,Map=map);
Specify the start and goal states.

```
start = [5 8 pi/2];
goal = [7 18 pi/2];
```

Create a plannerBenchmark object.

```
pbo = plannerBenchmark(sv,start,goal);
```

Define the function handles for the initialization functions of the planners.

```
plannerHAFcn = @(sv)plannerHybridAStar(sv);
plannerRRTSFcn = @(sv)plannerRRTStar(sv.StateSpace,sv);
```

Define the function handle for the plan function, which is common for both planners.

```
plnFcn = @(initOut,s,g)plan(initOut,s,g);
```

Add the path planners for benchmarking.

```
addPlanner(pbo,plnFcn,plannerHAFcn);
addPlanner(pbo,plnFcn,plannerRRTSFcn,PlannerName="ppRRTStar");
```

Set the rng for repetitive results.

```
rng('default')
```

Run the path planners for the number of times specified in runCount to collect metrics.

```
runCount = 5;
runPlanner(pbo,runCount)
```

Initializing plannerHAFcn_plnFcn ...
Done.
Planning with plannerHAFcn plnFcn for start pose (5 81.5708 ) and goal pose ( 7181.5708 ) at run
Planning with plannerHAFcn_plnFcn for start pose (5 81.5708 ) and goal pose ( 718 1.5708) at run
Planning with plannerHAFcn_plnFcn for start pose (5 81.5708 ) and goal pose ( 718 1.5708) at run
Planning with plannerHAFcn_plnFcn for start pose ( 581.5708 ) and goal pose ( 7181.5708 ) at run
Planning with plannerHAFcn_plnFcn for start pose (5 81.5708 ) and goal pose ( 7181.5708 ) at run
Initializing ppRRTStar ...
Done.
Planning with ppRRTStar for start pose (5 81.5708 ) and goal pose ( 7181.5708 ) at run count 1.
Planning with ppRRTStar for start pose ( 581.5708 ) and goal pose ( 7181.5708 ) at run count 2.
Planning with ppRRTStar for start pose ( 581.5708 ) and goal pose ( 7181.5708 ) at run count 3.
Planning with ppRRTStar for start pose (5 81.5708 ) and goal pose ( 7181.5708 ) at run count 4.
Planning with ppRRTStar for start pose ( 581.5708 ) and goal pose ( 7181.5708 ) at run count 5 .

Access path length metric for all the runs on the environment.

|  | Mean | Median | StdDev | sampleSize |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| plannerHAFcn_plnFcn ppRRTStar | $\begin{array}{r} 10.349 \\ 12.84 \end{array}$ | $\begin{array}{r} 10.349 \\ 12.9 \end{array}$ | $\begin{array}{r} 0 \\ 0.67112 \end{array}$ | 5 5 |  |
| pLenData=2×5 table | Run1 | Run2 | Run3 | Run4 | Run5 |
| plannerHAFcn_plnFcn | 10.349 | 10.349 | 10.349 | 10.349 | 10.349 |
| ppRRTStar - | 13.8 | 12.9 | 12.2 | 12 | 13.3 |

Visualize all the metrics.

```
show(pbo)
```



Closely inspect the clearance metric.
figure
show(pbo,"clearance")


## Input Arguments

## plannerBM - Path planner benchmark

plannerBenchmark object
Path planner benchmark, specified as a plannerBenchmark object.

## planFen - Plan function of path planner

function handle
Plan function of path planner, specified as a function handle.
The function handle should be of the form, @(init0ut, start, goal) planFcn(...), where initOut is the output of the initialization function.

If the initializationFcn input is not specified, the function handle should be @(env, start, goal)planFcn(...), where env is the Environment property of plannerBenchmark object.

The first output of $p l a n F c n$ must be either a navPath object, $m$-by- 2 , or $m$-by- 3 matrix.

## Data Types: function_handle

## initializationFcn - Initialization function of path planner <br> function handle

Initialization function of path planner, specified as a function handle.
The function handle should be of the form, @(env)initializationFcn(...), where env is the Environment property of plannerBenchmark object.

The output of initializationFcn is the first input to the planFcn function handle.

## Data Types: function_handle

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: addPlanner (pbo,plnFcn,plannerRRTSFcn,PlannerName="ppRRTStar")

## PlannerName - Name of planner

character vector | string scalar
Name of planner, specified as character vector or string scalar.
The default planner name depends on one of the following,

- If workspace variable name of initializationFcn and planFcn are initVar and planVar, respectively, the default planner name will be "initVar_planVar".
- If the optional initializationFcn input is not specified then the default planner name will be "planVar".
- If the function handles are specified as anonymous functions directly inside the addPlanner function, the default planner name will be "CustomInitFcn_CustomPlanFcn".
- If the optional initializationFcn input is not specified and the planFen function handle is specified as an anonymous function directly then the default planner name will be "CustomPlanFcn".

Data Types: char | string

## NumPlanOutput - Number of expected output from plan function

1 (default) | positive scalar
Number of expected output from plan function, specified as a positive scalar.
Data Types: single | double

## See Also

## Objects

plannerBenchmark

## Functions

copy | metric | runPlanner | show

## Introduced in R2022a

## copy

Create deep copy of plannerBenchmark object

## Syntax

plannerBM2 $=$ copy (plannerBM1)

## Description

plannerBM2 = copy (plannerBM1) creates a deep copy of the plannerBenchmark object with the same properties.

## Examples

## Create Copy of plannerBenchmark Object

Create an occupancy map from an example map.

```
load("exampleMaps.mat","simpleMap");
map = occupancyMap(simpleMap);
Specify the start and goal states.
start = [5 8 pi/2];
goal = [7 18 pi/2];
Create a plannerBenchmark object using the map.
pbo = plannerBenchmark(map,start,goal)
pbo =
    plannerBenchmark with properties:
        Environment: [1x1 occupancyMap]
            Start: [5 8 1.5708]
                Goal: [7 18 1.5708]
        PlannerOutput: [1x1 struct]
```

Create a copy of plannerBenchmark object.
pboNew $=$ copy (pbo)
pboNew =
plannerBenchmark with properties:
Environment: [1x1 occupancyMap]
Start: [5 8 1.5708]
Goal: [7 18 1.5708]
PlannerOutput: [1x1 struct]

## Input Arguments

plannerBM1 - Path planner benchmark
plannerBenchmark object
Path planner benchmark, specified as a plannerBenchmark object.

## Output Arguments

plannerBM2 - Copy of path planner benchmark
plannerBenchmark object
Copy of path planner benchmark, returned as a plannerBenchmark object.

## See Also

## Objects

plannerBenchmark
Functions
addPlanner | metric| runPlanner | show
Introduced in R2022a

## metric

Return path planner metrics

## Syntax

```
metricSummary = metric(plannerBM)
metricSummary = metric(plannerBM,metricName)
[metricSummary,metricData] = metric(plannerBM)
[metricSummary,metricData] = metric(plannerBM,metricName)
```


## Description

metricSummary $=$ metric( $p l a n n e r B M$ ) returns the summary of all the path planner metrics as a table.
metricSummary $=$ metric(plannerBM, metricName) returns the summary of a specific metric.
[metricSummary,metricData] = metric(plannerBM) returns the metricData table with the metric values across each run for all metrics and metricSummary table with the summary of all metrics.
[metricSummary,metricData] = metric(plannerBM, metricName) returns the summary and the values of a specific metric.

## Examples

## Benchmark 2-D Path Planners

Create an occupancy map from an example map.

```
load("exampleMaps.mat","simpleMap");
map = occupancyMap(simpleMap);
```

Create a state validator with stateSpaceSE2 using the map.

```
sv = validatorOccupancyMap(stateSpaceSE2,Map=map);
```

Specify the start and goal states.

```
start = [5 8 pi/2];
goal = [7 18 pi/2];
```

Create a plannerBenchmark object.
pbo = plannerBenchmark(sv,start,goal);
Define the function handles for the initialization functions of the planners.

```
plannerHAFcn = @(sv)plannerHybridAStar(sv);
plannerRRTSFcn = @(sv)plannerRRTStar(sv.StateSpace,sv);
```

Define the function handle for the plan function, which is common for both planners.

```
plnFcn = @(initOut,s,g)plan(initOut,s,g);
```

Add the path planners for benchmarking.

```
addPlanner(pbo,plnFcn,plannerHAFcn);
addPlanner(pbo,plnFcn,plannerRRTSFcn,PlannerName="ppRRTStar");
```

Set the rng for repetitive results.

```
rng('default')
```

Run the path planners for the number of times specified in runCount to collect metrics.

```
runCount = 5;
runPlanner(pbo,runCount)
```

Initializing plannerHAFcn_plnFcn ...
Done.
Planning with plannerHAFcn_plnFcn for start pose (5 81.5708 ) and goal pose ( 7181.5708 ) at run
Planning with plannerHAFcn_plnFcn for start pose (5 81.5708 ) and goal pose ( 718 1.5708) at run
Planning with plannerHAFcn_plnFcn for start pose (5 81.5708 ) and goal pose ( 7181.5708 ) at run
Planning with plannerHAFcn_plnFcn for start pose (5 81.5708 ) and goal pose ( 7181.5708 ) at run
Planning with plannerHAFcn_plnFcn for start pose (5 81.5708 ) and goal pose ( 7181.5708 ) at run
Initializing ppRRTStar ...
Done.
Planning with ppRRTStar for start pose (5 81.5708 ) and goal pose ( 7181.5708 ) at run count 1.
Planning with ppRRTStar for start pose (5 81.5708 ) and goal pose ( 7181.5708 ) at run count 2.
Planning with ppRRTStar for start pose ( 581.5708 ) and goal pose ( 7181.5708 ) at run count 3.
Planning with ppRRTStar for start pose ( 581.5708 ) and goal pose ( 7181.5708 ) at run count 4.
Planning with ppRRTStar for start pose (5 81.5708 ) and goal pose ( 7181.5708 ) at run count 5.

Access path length metric for all the runs on the environment.

```
[pLenSummary,pLenData] = metric(pbo,"pathLength")
```

|  | Mean | Median | StdDev | sampleSize |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| plannerHAFcn_plnFcn ppRRTStar | $\begin{array}{r} 10.349 \\ 12.84 \end{array}$ | $\begin{array}{r} 10.349 \\ 12.9 \end{array}$ | $\begin{array}{r} 0 \\ 0.67112 \end{array}$ | 5 5 |  |
| pLenData=2×5 table | Run1 | Run2 | Run3 | Run4 | Run5 |
| plannerHAFcn_plnFcn ppRRTStar | $\begin{array}{r} 10.349 \\ 13.8 \end{array}$ | $\begin{array}{r} 10.349 \\ 12.9 \end{array}$ | $\begin{array}{r} 10.349 \\ 12.2 \end{array}$ | $\begin{array}{r} 10.349 \\ 12 \end{array}$ | $\begin{array}{r} 10.349 \\ 13.3 \end{array}$ |

Visualize all the metrics.
show(pbo)


Closely inspect the clearance metric.
figure
show(pbo,"clearance")


## Input Arguments

## plannerBM - Path planner benchmark

plannerBenchmark object
Path planner benchmark, specified as a plannerBenchmark object.
metricName - Metric name
"clearance" | "executionTime" | "initializationTime" | "isPathValid" | "pathLength"
| "smoothness"
Metric name, specified as "clearance", "executionTime", "initializationTime", "isPathValid", "pathLength", or "smoothness".
Data Types: char|string

## Output Arguments

metricSummary - Metric summary
table
Metric summary, returned as table. The summary includes Mean, Median, Standard Deviation, and sampleSize for metrics of numeric type. For the metrics of logical type, the summary includes the TrueCount, FalseCount, and SuccessRate. TrueCount is the number of times the metric value is true.

FalseCount is the number of times the metric value is false. SuccessRate is the ratio of TrueCount to total runs of planner expressed in percentage.

Data Types: table

## metricData - Metric value

table
Metric value, returned as table. The table contains the metric values across each run for all metrics.
Data Types: table

## Tips

- If the metric value can not be computed due to empty states in path output or error during plan function execution, NaN will be displayed for corresponding values in metric data tables. The show function will not display any value for metrics with NaN value.
- If the path output is navPath, metrics are calculated using the state space in navPath.
- If the path output is a m-by-2 matrix, state space is assumed as stateSpaceSE2 with theta as 0 for all poses.
- If the path output is a m-by-3 matrix, the third column in the path output is assumed as theta and subsequently stateSpaceSE2 is assumed as the state space.
- If environment is validator0ccupancyMap, the metric isPathValid is computed using the specified environment.
- If environment is occupancyMap or binary0ccupancyMap, default validator0ccupancyMap is created using the specified environment as Map and state space is derived as above.
- The value of ValidationDistance property is assumed as $0.1^{*}(1 / r e s o l u t i o n ~ o f ~ m a p) . ~$


## See Also

## Objects

plannerBenchmark
Functions
addPlanner | copy | runPlanner | show
Introduced in R2022a

## runPlanner

Run path planners

## Syntax

runPlanner(plannerBM)
runPlanner(plannerBM, runCount)
runPlanner ( $\qquad$ , Verbose=Value)

## Description

runPlanner(plannerBM) runs all the path planners once.
runPlanner (plannerBM, runCount) specifies the number of times to run all the path planners. The function collects outputs of initialization function and plan function. The function also calculates the metric, executionTime for the plan function and the metric, initializationTime for the initialization function.
runPlanner( $\qquad$ ,Verbose=Value) specifies verbose which display function progress. Value of verbose is specified as "on" or "off". The default value of verbose is "on".

## Examples

## Benchmark 2-D Path Planners

Create an occupancy map from an example map.

```
load("exampleMaps.mat","simpleMap");
map = occupancyMap(simpleMap);
```

Create a state validator with stateSpaceSE2 using the map.
sv = validator0ccupancyMap(stateSpaceSE2,Map=map);
Specify the start and goal states.

```
start = [5 8 pi/2];
goal = [7 18 pi/2];
```

Create a plannerBenchmark object.
pbo = plannerBenchmark(sv,start,goal);
Define the function handles for the initialization functions of the planners.
plannerHAFcn = @(sv)plannerHybridAStar(sv);
plannerRRTSFcn = @(sv)plannerRRTStar(sv.StateSpace,sv);
Define the function handle for the plan function, which is common for both planners.

```
plnFcn = @(initOut,s,g)plan(initOut,s,g);
```

Add the path planners for benchmarking.

```
addPlanner(pbo,plnFcn,plannerHAFcn);
addPlanner(pbo,plnFcn,plannerRRTSFcn,PlannerName="ppRRTStar");
```

Set the rng for repetitive results.

```
rng('default')
```

Run the path planners for the number of times specified in runCount to collect metrics.

```
runCount = 5;
runPlanner(pbo,runCount)
```

Initializing plannerHAFcn_plnFcn ...
Done.
Planning with plannerHAFcn_plnFcn for start pose (5 81.5708 ) and goal pose ( 7181.5708 ) at run
Planning with plannerHAFcn_plnFcn for start pose ( 581.5708 ) and goal pose ( 7181.5708 ) at run
Planning with plannerHAFcn_plnFcn for start pose (5 81.5708 ) and goal pose ( 7181.5708 ) at run
Planning with plannerHAFcn_plnFcn for start pose (5 81.5708 ) and goal pose ( 7181.5708 ) at run
Planning with plannerHAFcn_plnFcn for start pose (5 81.5708 ) and goal pose ( 7181.5708 ) at run
Initializing ppRRTStar ...
Done.
Planning with ppRRTStar for start pose (5 8 1.5708) and goal pose ( 7181.5708 ) at run count 1.
Planning with ppRRTStar for start pose ( 581.5708 ) and goal pose ( 7181.5708 ) at run count 2.
Planning with ppRRTStar for start pose ( 581.5708 ) and goal pose ( 7181.5708 ) at run count 3.
Planning with ppRRTStar for start pose (5 81.5708 ) and goal pose ( 7181.5708 ) at run count 4.
Planning with ppRRTStar for start pose (5 81.5708 ) and goal pose ( 7181.5708 ) at run count 5.

Access path length metric for all the runs on the environment.

```
[pLenSummary,pLenData] = metric(pbo,"pathLength")
```

pLenSummary=2×4 table

|  | Mean | Median | StdDev | sampleSize |
| :---: | :---: | :---: | :---: | :---: |
| plannerHAFcn_plnFcn | 10.349 | 10.349 | 0 | 5 |
| ppRRTStar | 12.84 | 12.9 | 0.67112 | 5 |


| pLenData=2×5 table |  |  |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  | Run1 |  | Run2 |  | Run3 |  | Run4 |

Visualize all the metrics.
show(pbo)


Closely inspect the clearance metric.
figure
show(pbo,"clearance")


## Input Arguments

plannerBM - Path planner benchmark
plannerBenchmark object
Path planner benchmark, specified as a plannerBenchmark object.
runCount - Number of times of execution of plan functions
1 (default) | positive scalar
Number of times of execution of plan functions, specified as a positive scalar.
Data Types: single | double

## See Also

Objects
plannerBenchmark

## Functions

addPlanner | copy | metric | show
Introduced in R2022a

## show

Visualize path planner metrics

## Syntax

show(plannerBM)
axHandle $=\operatorname{show}(p l a n n e r B M)$
$\qquad$ ] = show(plannerBM,metricName)

## Description

show ( $p l a n n e r B M$ ) visualizes all the path planner metrics in a figure as box plots and bar graphs. axHandle $=$ show( plannerBM ) returns the axes handle of the figure used to plot all the metrics.
[ $\qquad$ ] = show(plannerBM, metricName) visualizes a specific metric.

## Examples

## Benchmark 2-D Path Planners

Create an occupancy map from an example map.

```
load("exampleMaps.mat","simpleMap");
map = occupancyMap(simpleMap);
```

Create a state validator with stateSpaceSE2 using the map.

```
sv = validatorOccupancyMap(stateSpaceSE2,Map=map);
```

Specify the start and goal states.

```
start = [5 8 pi/2];
goal = [7 18 pi/2];
```

Create a plannerBenchmark object.
pbo = plannerBenchmark(sv,start,goal);
Define the function handles for the initialization functions of the planners.

```
plannerHAFcn = @(sv)plannerHybridAStar(sv);
```

plannerRRTSFcn = @(sv)plannerRRTStar(sv.StateSpace,sv);

Define the function handle for the plan function, which is common for both planners.

```
plnFcn = @(initOut,s,g)plan(initOut,s,g);
```

Add the path planners for benchmarking.
addPlanner(pbo,plnFcn,plannerHAFcn) ;
addPlanner(pbo,plnFcn,plannerRRTSFcn,PlannerName="ppRRTStar");

Set the rng for repetitive results.

```
rng('default')
```

Run the path planners for the number of times specified in runCount to collect metrics.

```
runCount = 5;
runPlanner(pbo,runCount)
```

Initializing plannerHAFcn_plnFcn ...
Done.
Planning with plannerHAFcn plnFcn for start pose ( 581.5708 ) and goal pose ( 7181.5708 ) at run
Planning with plannerHAFcn_plnFcn for start pose (5 81.5708 ) and goal pose ( 7181.5708 ) at run
Planning with plannerHAFcn_plnFcn for start pose (5 81.5708 ) and goal pose ( 718 1.5708) at run
Planning with plannerHAFcn_plnFcn for start pose ( 581.5708 ) and goal pose ( 7181.5708 ) at run
Planning with plannerHAFcn_plnFcn for start pose (5 81.5708 ) and goal pose ( 7181.5708 ) at run
Initializing ppRRTStar ...
Done.
Planning with ppRRTStar for start pose (5 81.5708 ) and goal pose ( 7181.5708 ) at run count 1.
Planning with ppRRTStar for start pose ( 581.5708 ) and goal pose ( 7181.5708 ) at run count 2.
Planning with ppRRTStar for start pose ( 581.5708 ) and goal pose ( 7181.5708 ) at run count 3.
Planning with ppRRTStar for start pose ( 581.5708 ) and goal pose ( 7181.5708 ) at run count 4.
Planning with ppRRTStar for start pose (5 81.5708 ) and goal pose ( 7181.5708 ) at run count 5.

Access path length metric for all the runs on the environment.

```
[pLenSummary,pLenData] = metric(pbo,"pathLength")
```

pLenSummary=2×4 table

|  | Mean | Median | StdDev | sampleSize |
| :---: | :---: | :---: | :---: | :---: |
| plannerHAFcn_plnFcn | 10.349 | 10.349 | 0 | 5 |
| ppRRTStar | 12.84 | 12.9 | 0.67112 | 5 |


| pLenData=2×5 table |  |  |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  | Run1 |  | Run2 |  | Run3 |  | Run4 |

Visualize all the metrics.

```
show(pbo)
```



Closely inspect the clearance metric.
figure
show(pbo,"clearance")


## Input Arguments

## plannerBM - Path planner benchmark

plannerBenchmark object
Path planner benchmark, specified as a plannerBenchmark object.

```
metricName - Metric name
"clearance" | "executionTime" | "initializationTime"| "isPathValid"| "pathLength"
| "smoothness"
```

Metric name, specified as "clearance", "executionTime", "initializationTime", "isPathValid", "pathLength", or "smoothness".

Data Types: char | string

## Output Arguments

## axHandle - Axes used to plot metrics

axes object | uiaxes object
Axes used to plot path, returned as either an axes or uiaxes object.

## See Also

Objects
plannerBenchmark
Functions
addPlanner |copy|metric|runPlanner
Introduced in R2022a

## copy

Create deep copy of plannerPRM object

## Syntax

planner2 $=$ copy (planner1)

## Description

planner2 = copy(planner1) creates a deep copy of the plannerPRM object with the same properties.

## Examples

## Create Copy of plannerPRM Object

Create an occupancy map from an example map and set the map resolution as 10 cells/meter.

```
map = load("exampleMaps.mat").simpleMap;
map = occupancyMap(map,10);
```

Create a state space and update the state space bounds to be the same as the map limits.

```
ss = stateSpaceSE2;
ss.StateBounds = [map.XWorldLimits; map.YWorldLimits; [-pi pi]];
```

Create a state validator with stateSpaceSE2 using the map and set the validation distance.

```
sv = validatorOccupancyMap(ss,Map=map);
sv.ValidationDistance = 0.01;
Create a plannerPRM object.
planner = plannerPRM(ss,sv)
planner =
    plannerPRM with properties:
                            StateSpace: [1x1 stateSpaceSE2]
            StateValidator: [1x1 validatorOccupancyMap]
        MaxConnectionDistance: Inf
                        MaxNumNodes: 50
```

Create a copy of the plannerPRM object.

```
plannerNew = copy(planner)
```

plannerNew =
plannerPRM with properties:
StateSpace: [1x1 stateSpaceSE2]

```
StateValidator: [1x1 validatorOccupancyMap] MaxConnectionDistance: Inf
MaxNumNodes: 50
```


## Input Arguments

planner1 - Path planner
plannerPRM object
Path planner, specified as a plannerPRM object.

## Output Arguments

planner2 - Copy of path planner
plannerPRM object
Copy of path planner, returned as a plannerPRM object.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

Objects
plannerPRM
Functions
graphData|plan
Introduced in R2022a

## graphData

Retrieve graph as digraph object

## Syntax

graph = graphData(planner)

## Description

graph $=$ graphData(planner) retrieves graph as a digraph object. The digraph object is created when the plannerPRM object is created with default or user specified values for the MaxNumNodes and MaxConnectionDistance properties.

## Examples

## Retrieve Graph from Probabilistic Roadmap Path Planner

Load an example map into the workspace, and use it to create an occupancy map with a resolution of 10 cells/meter.

```
load("exampleMaps.mat","simpleMap");
map = occupancyMap(simpleMap,10);
```

Create a state space object and update the state space bounds to match the map limits.

```
ss = stateSpaceSE2;
ss.StateBounds = [map.XWorldLimits; map.YWorldLimits; [-pi pi]];
```

Create a state validator for the occupancy map using the state space object and set the validation distance.

```
sv = validatorOccupancyMap(ss,Map=map);
```

sv.ValidationDistance = 0.01;

Create a probabilistic roadmap path planner object.

```
planner = plannerPRM(ss,sv);
```

Retrieve the network graph as a digraph object.

```
graph = graphData(planner);
```

Extract the nodes and edges from the graph.

```
edges = table2array(graph.Edges);
nodes = table2array(graph.Nodes);
```

Plot the map and graph.

```
show(sv.Map)
```

hold on

```
plot(nodes(:,1),nodes(:,2),"*",Color=[0 0 1],LineWidth=2)
for i = 1:size(edges,1)
    % Samples states at distance 0.02 meters.
    states = interpolate(ss,nodes(edges(i,1),:), ...
                                    nodes(edges(i,2),:),0:0.02:1);
    plot(states(:,1),states(:,2),Color=[0 0 1])
end
```



## Input Arguments

## planner - Path planner

plannerPRM object
Path planner, specified as a plannerPRM object.

## Output Arguments

## graph - Graph data

digraph object
Graph data, returned as a digraph object.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

## Objects

plannerPRM|digraph

## Functions

copy | plan
Introduced in R2022a

## plan

Plan path between start and goal states on roadmap

## Syntax

path = plan(planner,startState, goalState)
[path,solutionInfo] = plan(planner,startState,goalState)

## Description

path $=p l a n(p l a n n e r$, startState, goalState) returns an obstacle-free path as a navPath object between the start state and the goal state within a roadmap that contains a network graph of connected nodes.
[path,solutionInfo] = plan(planner,startState,goalState) also returns solutionInfo as a structure that contains the solution information of the path planning.

## Examples

## Plan Obstacle-Free Path Using Probabilistic Roadmap Path Planner

Create an occupancy map from an example map and set the map resolution as 10 cells/meter.

```
map = load("exampleMaps.mat").simpleMap;
map = occupancyMap(map,10);
```

Create a state space and update the state space bounds to be the same as the map limits.

```
ss = stateSpaceSE2;
ss.StateBounds = [map.XWorldLimits; map.YWorldLimits; [-pi pi]];
```

Create a state validator with stateSpaceSE2 using the map and set the validation distance.

```
sv = validatorOccupancyMap(ss,Map=map);
sv.ValidationDistance = 0.01;
```

Create a plannerPRM object.
planner = plannerPRM(ss,sv);
Retrieve graph as a digraph object.

```
graph = graphData(planner);
```

Extract nodes and edges from graph.

```
edges = table2array(graph.Edges);
nodes = table2array(graph.Nodes);
```

Specify the start and goal states.

```
start = [0.5 0.5 0];
goal = [2.5 0.2 0];
```

Plot map and graph.

```
show(sv.Map)
hold on
plot(nodes(:,1),nodes(:,2),"*","Color","b","LineWidth",2)
for i = 1:size(edges,1)
    % Samples states at distance 0.02 meters.
    states = interpolate(ss,nodes(edges(i,1),:), ...
                                    nodes(edges(i,2),:),0:0.02:1);
    plot(states(:,1),states(:,2),"Color","b")
end
plot(start(1),start(2),"*","Color","g","LineWidth",3)
plot(goal(1),goal(2),"*","Color","r","LineWidth",3)
```

Plan a path with default settings. Set the rng seed for repeatability.
rng(100,"twister");
[pthObj, solnInfo] = plan(planner,start,goal);

Visualize the results.

```
if solnInfo.IsPathFound
    interpolate(pthObj,1000);
    plot(pth0bj.States(:,1),pth0bj.States(:,2), ...
            "Color",[0.85 0.325 0.098],"LineWidth",2)
else
    disp("Path not found")
end
hold off
```



## Input Arguments

## planner - Path planner

plannerPRM object
Path planner, specified as a plannerPRM object.

## startState - Start state of the path

$N$-element real-valued row vector
Start state of the path, specified as an $N$-element real-valued row vector. $N$ is the dimension of the state space.
Example: [1 1 pi/6]
Data Types: single | double

## goalState - Goal state of the path

$N$-element real-valued row vector
Goal state of the path, specified as an $N$-element real-valued row vector. $N$ is the dimension of the state space.
Example: [2 2 pi/3]
Data Types: single | double

## Output Arguments

## path - Planned path information

navPath object
Planned path information, returned as a navPath object.
solutionInfo - Solution information
structure
Solution information, returned as a structure. The structure contains the field:

| Field | Description |
| :--- | :--- |
| IsPathFound | Indicates whether a path is found. It returns as 1 <br> if a path is found. Otherwise, it returns 0. |

## Data Types: struct

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

## Objects

plannerPRM | navPath

## Functions

copy | graphData

## Introduced in R2022a

## Blocks

## AHRS

Orientation from accelerometer, gyroscope, and magnetometer readings


Navigation Toolbox / Multisensor Positioning / Navigation Filters
Sensor Fusion and Tracking Toolbox / Multisensor Positioning / Navigation Filters

## Description

The AHRS Simulink ${ }^{\circledR}$ block fuses accelerometer, magnetometer, and gyroscope sensor data to estimate device orientation.

## Ports

## Input

## Accel - Accelerometer readings in sensor body coordinate system (m/s ${ }^{\mathbf{2}}$ )

N -by-3 matrix of real scalar
Accelerometer readings in the sensor body coordinate system in $\mathrm{m} / \mathrm{s}^{2}$, specified as an N -by- 3 matrix of real scalars. $N$ is the number of samples, and the three columns of Accel represent the $[x y z$ ] measurements, respectively.
Data Types: single | double
Gyro - Gyroscope readings in sensor body coordinate system (rad/s)
$N$-by-3 matrix of real scalar
Gyroscope readings in the sensor body coordinate system in rad/s, specified as an $N$-by- 3 matrix of real scalars. $N$ is the number of samples, and the three columns of Gyro represent the [ $x y z$ ] measurements, respectively.

Data Types: single | double

## Mag - Magnetometer readings in sensor body coordinate system ( $\mu \mathrm{T}$ )

## N -by-3 matrix of real scalar

Magnetometer readings in the sensor body coordinate system in $\mu \mathrm{T}$, specified as an $N$-by- 3 matrix of real scalars. $N$ is the number of samples, and the three columns of magReadings represent the [ $x y$ $z]$ measurements, respectively.

## Data Types: single | double

## Output

Orientation - Orientation of sensor body frame relative to navigation frame
$M$-by-4 array of scalar | 3-by-3-by-M-element rotation matrix

Orientation of the sensor body frame relative to the navigation frame, return as an $M$-by-4 array of scalars or a 3 -by-3-by- $M$ array of rotation matrices. Each row the of the $N$-by- 4 array is assumed to be the four elements of a quaternion. The number of input samples, $N$, and the Decimation Factor parameter determine the output size $M$.
Data Types: single | double

## Angular Velocity - Angular velocity in sensor body coordinate system (rad/s) <br> M-by-3 array of real scalar (default)

Angular velocity with gyroscope bias removed in the sensor body coordinate system in rad/s, returned as an $M$-by-3 array of real scalars. The number of input samples, $N$, and the Decimation Factor parameter determine the output size $M$.
Data Types: single | double

## Parameters

Main
Reference frame - Navigation reference frame
NED (default) | ENU
Navigation reference frame, specified as NED (North-East-Down) or ENU (East-North-Up).

## Decimation factor - Decimation factor

1 (default) | positive integer
Decimation factor by which to reduce the input sensor data rate, specified as a positive integer.
The number of rows of the inputs -- Accel, Gyro , and Mag -- must be a multiple of the decimation factor.

Data Types: single | double

## Initial process noise - Initial process noise

ahrsfilter.defaultProcessNoise (default) | 12-by-12 matrix of real scalar
Initial process noise, specified as a 12-by-12 matrix of real scalars. The default value, ahrsfilter.defaultProcessNoise, is a 12-by-12 diagonal matrix as:

| Columns 1 through 6 |  |  |  |
| ---: | ---: | ---: | ---: |
|  |  | 0 | 0 |
| 0.000006092348396 | 0 | 0 | 0 |
| 0 | 0.000006092348396 | 0 |  |
| 0 | 0 | 0.000006092348396 | 0 |
| 0 | 0 | 0 | 0.000076154354947 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
|  | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |

Columns 7 through 12

| 0 | 0 | 0 | 0 |
| ---: | ---: | ---: | ---: |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0.00962361000000 | 0 | 0 | 0 |
| 0 | 0.009623610000000 | 0 | 0 |
| 0 | 0 | 0.009623610000000 | 0 |
| 0 | 0 | 0 | 0.600000000000000 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |

Data Types: single | double
Orientation format - Orientation output format
'quaternion' (default)|'Rotation matrix'
Output orientation format, specified as 'quaternion' or 'Rotation matrix':

- 'quaternion ' -- Output is an M-by-4 array of real scalars. Each row of the array represents the four components of a quaternion.
- 'Rotation matrix' -- Output is a 3-by-3-by-M rotation matrix.

The output size $M$ depends on the input dimension $N$ and the Decimation Factor parameter.
Data Types: char | string

## Simulate using - Type of simulation to run

## Interpreted Execution (default)|Code Generation

- Interpreted execution - Simulate the model using the MATLAB interpreter. This option shortens startup time. In Interpreted execution mode, you can debug the source code of the block.
- Code generation - Simulate the model using generated C code. The first time you run a simulation, Simulink generates C code for the block. The C code is reused for subsequent simulations as long as the model does not change. This option requires additional startup time.


## Measurement Noise

Accelerometer noise ( $\left.\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}\right)$ - Variance of accelerometer signal noise ((m/s $\left.\left.{ }^{2}\right)^{2}\right)$
0.00019247 (default) | positive real scalar

Variance of accelerometer signal noise in $\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}$, specified as a positive real scalar.
Data Types: single | double

## Gyroscope noise ((rad/s) ${ }^{2}$ ) - Variance of gyroscope signal noise ((rad/s) ${ }^{\mathbf{2}}$ )

9.1385e-5 (default) | positive real scalar

Variance of gyroscope signal noise in (rad/s) ${ }^{2}$, specified as a positive real scalar.
Data Types: single | double
Magnetometer noise $\left(\mu T^{2}\right)$ - Variance of magnetometer signal noise ( $\mu \mathrm{T}^{2}$ )
0.1 (default) | positive real scalar

Variance of magnetometer signal noise in $\mu \mathrm{T}^{2}$, specified as a positive real scalar.
Data Types: single | double
Gyroscope drift noise (rad/s) - Variance of gyroscope offset drift ((rad/s) ${ }^{2}$ )
3.0462e-13 (default) | positive real scalar

Variance of gyroscope offset drift in (rad/s) ${ }^{2}$, specified as a positive real scalar.
Data Types: single | double

## Environmental Noise

Linear acceleration noise ( $\left.\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}\right)$ - Variance of linear acceleration noise $\left(\mathrm{m} / \mathrm{s}^{2}\right)^{\mathbf{2}}$
0.0096236 (default) | positive real scalar

Variance of linear acceleration noise in $\left(\mathrm{m} / \mathrm{s}^{2}\right)^{2}$, specified as a positive real scalar. Linear acceleration is modeled as a lowpass-filtered white noise process.
Data Types: single | double
Magnetic disturbance noise ( $\mu \mathrm{T}^{2}$ ) - Variance of magnetic disturbance noise ( $\mu \mathrm{T}^{2}$ )
0.5 (default) | real finite positive scalar

Variance of magnetic disturbance noise in $\mu \mathrm{T}^{2}$, specified as a real finite positive scalar.
Data Types: single | double
Linear acceleration decay factor - Decay factor for linear acceleration drift
0.5 (default) | scalar in the range [0,1)

Decay factor for linear acceleration drift, specified as a scalar in the range [0,1). If linear acceleration changes quickly, set this parameter to a lower value. If linear acceleration changes slowly, set this parameter to a higher value. Linear acceleration drift is modeled as a lowpass-filtered white noise process.
Data Types: single | double
Magnetic disturbance decay factor - Decay factor for magnetic disturbance
0.5 (default) | positive scalar in the range [0,1]

Decay factor for magnetic disturbance, specified as a positive scalar in the range [0,1]. Magnetic disturbance is modeled as a first order Markov process.
Data Types: single | double
Magnetic field strength ( $\mu \mathrm{T}$ ) - Magnetic field strength ( $\mu \mathrm{T}$ )
50 (default) | real positive scalar
Magnetic field strength in $\mu \mathrm{T}$, specified as a real positive scalar. The magnetic field strength is an estimate of the magnetic field strength of the Earth at the current location.
Data Types: single | double

## Algorithms

Note: The following algorithm only applies to an NED reference frame.

The AHRS block uses the nine-axis Kalman filter structure described in [1]. The algorithm attempts to track the errors in orientation, gyroscope offset, linear acceleration, and magnetic disturbance to output the final orientation and angular velocity. Instead of tracking the orientation directly, the indirect Kalman filter models the error process, $x$, with a recursive update:

$$
x_{k}=\left[\begin{array}{l}
\theta_{k} \\
b_{k} \\
a_{k} \\
d_{k}
\end{array}\right]=F_{k}\left[\begin{array}{l}
\theta_{k}-1 \\
b_{k-1} \\
a_{k-1} \\
d_{k-1}
\end{array}\right]+w_{k}
$$

where $\chi_{\mathrm{k}}$ is a 12-by- 1 vector consisting of:

- $\theta_{k}$-- 3-by-1 orientation error vector, in degrees, at time $k$
- $b_{k}$-- 3-by-1 gyroscope zero angular rate bias vector, in deg/s, at time $k$
- $a_{k}--3$-by-1 acceleration error vector measured in the sensor frame, in $g$, at time $k$
- $d_{k}--3$-by-1 magnetic disturbance error vector measured in the sensor frame, in $\mu \mathrm{T}$, at time $k$ and where $w_{\mathrm{k}}$ is a 12-by-1 additive noise vector, and $F_{\mathrm{k}}$ is the state transition model.

Because $\chi_{\mathrm{k}}$ is defined as the error process, the a priori estimate is always zero, and therefore the state transition model, $F_{k}$, is zero. This insight results in the following reduction of the standard Kalman equations:

Standard Kalman equations:

$$
\begin{aligned}
& x_{k}^{-}=F_{k} x_{k}^{+}-1 \\
& P_{k}^{-}=F_{k} P_{k-1}^{+} F_{k}^{T}+Q_{k} \\
& y_{k}=z_{k}-H_{k} x_{k}^{-} \\
& S_{k}=R_{k}+H_{k} P_{k}^{-} H_{k} T \\
& K_{k}=P_{k}^{-} H_{k}^{T}\left(S_{k}\right)^{-1} \\
& x_{k}^{+}=x_{\bar{k}}^{-}+K_{k} y_{k} \\
& P_{k}^{+}=P_{k}^{-}-K_{k} H_{k} P_{k}^{-}
\end{aligned}
$$

Kalman equations used in this algorithm:

$$
\begin{aligned}
& x_{k}^{-}=0 \\
& P_{k}^{-}=Q_{k} \\
& y_{k}=z_{k} \\
& S_{k}=R_{k}+H_{k} P_{k}^{-} H_{k} T \\
& K_{k}=P_{k}^{-} H_{k}^{T}\left(S_{k}\right)^{-1} \\
& x_{k}^{+}=K_{k} Y_{k} \\
& P_{k}^{+}=P_{k}^{-}-K_{k} H_{k} P_{k}^{-}
\end{aligned}
$$

where:

- ${x_{k}}^{-}$-- predicted (a priori) state estimate; the error process
- $P_{k}{ }^{-}$-- predicted (a priori) estimate covariance
- $y_{k}$-- innovation
- $S_{k}$-- innovation covariance
- $K_{k}-$ Kalman gain
- $x_{k}{ }^{+}$-- updated (a posteriori) state estimate
- $P_{k}{ }^{+}$-- updated (a posteriori) estimate covariance
$k$ represents the iteration, the superscript + represents an a posteriori estimate, and the superscript represents an a priori estimate.

The graphic and following steps describe a single frame-based iteration through the algorithm.


Before the first iteration, the accelReadings, gyroReadings, and magReadings inputs are chunked into DecimationFactor-by-3 frames. For each chunk, the algorithm uses the most current accelerometer and magnetometer readings corresponding to the chunk of gyroscope readings.

## Detailed Overview

Walk through the algorithm for an explanation of each stage of the detailed overview.


## Model

The algorithm models acceleration and angular change as linear processes.

gyroOffset

## Predict Orientation

The orientation for the current frame is predicted by first estimating the angular change from the previous frame:

$$
\Delta \varphi_{N \times 3}=\frac{\left(\text { gyroReadings }_{N \times 3}-\text { gyroOffset }_{1 \times 3}\right)}{f s}
$$

where $N$ is the decimation factor specified by the Decimation factor and $f s$ is the sample rate.
The angular change is converted into quaternions using the rotvec quaternion construction syntax:

$$
\Delta Q_{N \times 1}=\text { quaternion }\left(\Delta \varphi_{N \times 3}, \text { 'rotvec' }\right)
$$

The previous orientation estimate is updated by rotating it by $\Delta Q$ :

$$
q_{1}^{-} \times 1=\left(q_{1}^{+} \times 1\right)\left(\prod_{n=1}^{N} \Delta Q_{n}\right)
$$

During the first iteration, the orientation estimate, $q^{-}$, is initialized by ecompass.

## Estimate Gravity from Orientation

The gravity vector is interpreted as the third column of the quaternion, $q^{-}$, in rotation matrix form:

$$
g_{1 \times 3}=(r \operatorname{Prior}(:, 3))^{T}
$$

## Estimate Gravity from Acceleration

A second gravity vector estimation is made by subtracting the decayed linear acceleration estimate of the previous iteration from the accelerometer readings:

$$
\text { gAccel }_{1 \times 3}=\text { accelReadings }_{1 \times 3}-\text { linAccelprior }_{1 \times 3}
$$

## Estimate Earth's Magnetic Vector

Earth's magnetic vector is estimated by rotating the magnetic vector estimate from the previous iteration by the a priori orientation estimate, in rotation matrix form:

$$
\text { mGyro }_{1 \times 3}=\left((\text { rPrior })\left(m^{T}\right)\right)^{T}
$$

## Error Model



The error model combines two differences:

- The difference between the gravity estimate from the accelerometer readings and the gravity estimate from the gyroscope readings: $z_{g}=g-g A c c e l$
- The difference between the magnetic vector estimate from the gyroscope readings and the magnetic vector estimate from the magnetometer: $z_{m}=m G y r o-$ magReadings


## Magnetometer Correct

The magnetometer correct estimates the error in the magnetic vector estimate and detects magnetic jamming.


## Magnetometer Disturbance Error

The magnetic disturbance error is calculated by matrix multiplication of the Kalman gain associated with the magnetic vector with the error signal:

$$
\text { mError }_{3 \times 1}=\left(\left(K(10: 12,:)_{3 \times 6}\right)\left(z_{1 \times 6}\right)^{T}\right)^{T}
$$

The Kalman gain, $K$, is the Kalman gain calculated in the current iteration.

## Magnetic Jamming Detection

Magnetic jamming is determined by verifying that the power of the detected magnetic disturbance is less than or equal to four times the power of the expected magnetic field strength:

$$
t f=\left\{\begin{array}{l}
\text { true if } \\
\text { false else }
\end{array} \sum|m E r r o r|^{2}>(4)(\text { ExpectedMagneticFieldStrength })^{2}\right.
$$

ExpectedMagneticFieldStrength is a property of ahrsfilter.

## Kalman Equations

The Kalman equations use the gravity estimate derived from the gyroscope readings, $g$, the magnetic vector estimate derived from the gyroscope readings, mGyro, and the observation of the error process, $z$, to update the Kalman gain and intermediary covariance matrices. The Kalman gain is applied to the error signal, $z$, to output an a posteriori error estimate, $x^{+}$.


## Observation Model

The observation model maps the 1-by-3 observed states, $g$ and mGyro, into the 6-by-12 true state, $H$.
The observation model is constructed as:

$$
H_{3 \times 9}=\left[\begin{array}{cccccccccccc}
0 & g_{z} & -g_{y} & 0 & -\kappa g_{z} & \kappa g_{y} & 1 & 0 & 0 & 0 & 0 & 0 \\
-g_{z} & 0 & g_{x} & \kappa g_{z} & 0 & -\kappa g_{x} & 0 & 1 & 0 & 0 & 0 & 0 \\
g_{y} & -g_{x} & 0 & -\kappa g_{y} & \kappa g_{x} & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\
0 & m_{z} & -m_{y} & 0 & -\kappa m_{z} & -\kappa m_{y} & 0 & 0 & 0 & -1 & 0 & 0 \\
-m_{z} & 0 & m_{x} & \kappa m_{z} & 0 & -\kappa m_{\chi} & 0 & 0 & 0 & 0 & -1 & 0 \\
m_{y} & -m_{x} & 0 & -\kappa m_{y} & \kappa m_{x} & 0 & 0 & 0 & 0 & 0 & 0 & -1
\end{array}\right]
$$

where $g_{\mathrm{x}}, g_{\mathrm{y}}$, and $g_{\mathrm{z}}$ are the $x$-, $y$-, and $z$-elements of the gravity vector estimated from the a priori orientation, respectively. $m_{x}, m_{y}$, and $m_{z}$ are the $x$-, $y$-, and $z$-elements of the magnetic vector estimated from the a priori orientation, respectively. K is a constant determined by the Sample rate and Decimation factor properties: $\kappa=$ Decimation factor/Sample rate.

## Innovation Covariance

The innovation covariance is a 6 -by- 6 matrix used to track the variability in the measurements. The innovation covariance matrix is calculated as:

$$
S_{6 \times 6}=R_{6 \times 6}+\left(H_{6 \times 12}\right)\left(P_{12 \times 12}^{-}\right)\left(H_{6 \times 12}\right)^{T}
$$

where

- $H$ is the observation model matrix
- $P^{-}$is the predicted (a priori) estimate of the covariance of the observation model calculated in the previous iteration
- $R$ is the covariance of the observation model noise, calculated as:

$$
R_{6 \times 6}=\left[\begin{array}{cccccc}
a c c e l_{\text {noise }} & 0 & 0 & 0 & 0 & 0 \\
0 & a c c e l_{\text {noise }} & 0 & 0 & 0 & 0 \\
0 & 0 & a c c e l_{\text {noise }} & 0 & 0 & 0 \\
0 & 0 & 0 & \text { mag }_{\text {noise }} & 0 & 0 \\
0 & 0 & 0 & 0 & \text { mag }_{\text {noise }} & 0 \\
0 & 0 & 0 & 0 & 0 & \text { mag }_{\text {noise }}
\end{array}\right]
$$

where

$$
\begin{aligned}
& \text { accel }_{\text {noise }}=\text { AccelerometerNoise }+ \text { LinearAccelerationNoise }+\kappa^{2} \\
& (\text { GyroscopeDriftNoise }+ \text { GyroscopeNoise })
\end{aligned}
$$

and

$$
\begin{aligned}
& \text { mag }_{\text {noise }}=\text { MagnetometerNoise }+ \text { MagneticDisturbanceNoise }+\kappa^{2} \\
& (\text { GyroscopeDriftNoise }+ \text { GyroscopeNoise })
\end{aligned}
$$

## Update Error Estimate Covariance

The error estimate covariance is a 12-by-12 matrix used to track the variability in the state.
The error estimate covariance matrix is updated as:

$$
P_{12 \times 12}^{+}=P_{12 \times 12}^{-}-\left(K_{12 \times 6}\right)\left(H_{6 \times 12}\right)\left(P_{12 \times 12}^{-}\right)
$$

where $K$ is the Kalman gain, $H$ is the measurement matrix, and $P^{-}$is the error estimate covariance calculated during the previous iteration.

## Predict Error Estimate Covariance

The error estimate covariance is a 12 -by- 12 matrix used to track the variability in the state. The $a$ priori error estimate covariance, $P^{-}$, is set to the process noise covariance, $Q$, determined during the previous iteration. $Q$ is calculated as a function of the a posteriori error estimate covariance, $P^{+}$. When calculating $Q$, it is assumed that the cross-correlation terms are negligible compared to the autocorrelation terms, and are set to zero:

$$
Q=
$$

$\left[\begin{array}{ccccc}P^{+}(1)+K^{2} P^{+}(40)+\beta+\eta & 0 & 0 & -K\left(P^{+}(40)+\beta\right) & 0 \\ 0 & P^{+}(14)+K^{2} P^{+}(53)+\beta+\eta & 0 & 0 & -K\left(P^{+}(53)+\right. \\ 0 & 0 & P^{+}(27)+K^{2} P^{+}(66)+\beta+\eta & 0 & 0 \\ -K\left(P^{+}(40)+\beta\right) & 0 & 0 & P^{+}(40)+\beta & 0 \\ 0 & -K\left(P^{+}(53)+\beta\right) & 0 & 0 & P^{+}(53)+\beta \\ 0 & 0 & -K\left(P^{+}(66)+\beta\right) & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0\end{array}\right.$
where

- $P^{+}$-- is the updated (a posteriori) error estimate covariance
- $\kappa$-- Decimation factor divided by sample rate.
- $\beta$-- Gyroscope drift noise.
- $\eta$-- Gyroscope noise.
- $\quad \nu$-- Linear acceleration decay factor.
- $\xi$-- Linear acceleration noise.
- $\sigma$-- Magnetic disturbance decay factor.
- $\gamma$-- Magnetic disturbance noise.


## Kalman Gain

The Kalman gain matrix is a 12-by-6 matrix used to weight the innovation. In this algorithm, the innovation is interpreted as the error process, $z$.

The Kalman gain matrix is constructed as:

$$
K_{12 \times 6}=\left(P_{12 \times 12}^{-}\right)\left(H_{6 \times 12}\right)^{T}\left(\left(S_{6 \times 6}\right)^{T}\right)^{-1}
$$

where

- $P^{-}$-- predicted error covariance
- $H$-- observation model
- $S$-- innovation covariance


## Update a Posteriori Error

The a posterior error estimate is determined by combining the Kalman gain matrix with the error in the gravity vector and magnetic vector estimations:

$$
x_{12 \times 1}=\left(K_{12 \times 6}\right)\left(z_{1 \times 6}\right)^{T}
$$

If magnetic jamming is detected in the current iteration, the magnetic vector error signal is ignored, and the a posterior error estimate is calculated as:

$$
x_{9 \times 1}=\left(K(1: 9,1: 3)\left(z_{g}\right)^{T}\right.
$$

## Correct



## Estimate Orientation

The orientation estimate is updated by multiplying the previous estimation by the error:

$$
q^{+}=\left(q^{-}\right)\left(\theta^{+}\right)
$$

## Estimate Linear Acceleration

The linear acceleration estimation is updated by decaying the linear acceleration estimation from the previous iteration and subtracting the error:

$$
\text { linAccelPrior }=\left(\text { linAccelPrior }_{k-1}\right) \nu-b^{+}
$$

where

- $\quad \nu$-- Linear acceleration decay factor


## Estimate Gyroscope Offset

The gyroscope offset estimation is updated by subtracting the gyroscope offset error from the gyroscope offset from the previous iteration:

$$
\text { gyroOffset }=\text { gyroOffset }_{k-1}-a^{+}
$$

## Compute Angular Velocity

To estimate angular velocity, the frame of gyroReadings are averaged and the gyroscope offset computed in the previous iteration is subtracted:

$$
\text { angularVelocity }_{1 \times 3}=\frac{\sum \text { gyroReadings }_{N \times 3}}{N}-\text { gyroOffset }_{1 \times 3}
$$

where $N$ is the decimation factor specified by the DecimationFactor property.
The gyroscope offset estimation is initialized to zeros for the first iteration.

## Update Magnetic Vector

If magnetic jamming was not detected in the current iteration, the magnetic vector estimate, $m$, is updated using the a posteriori magnetic disturbance error and the a posteriori orientation.

The magnetic disturbance error is converted to the navigation frame:

$$
m E r r o r N E D_{1 \times 3}=\left(\left(\text { Post }_{3 \times 3}\right)^{T}\left(m E r r o r_{1 \times 3}\right)^{T}\right)^{T}
$$

The magnetic disturbance error in the navigation frame is subtracted from the previous magnetic vector estimate and then interpreted as inclination:

$$
M=m-m E r r o r N E D
$$

$$
\text { inclination }=\operatorname{atan2}(M(3), M(1))
$$

The inclination is converted to a constrained magnetic vector estimate for the next iteration:

```
m(1) = (ExpectedMagneticFieldStrength)(cos(inclination))
m(2)}=
m(3)=(ExpectedMagneticFieldStrength)(sin(inclination))
```


## References

[1] Open Source Sensor Fusion. https://github.com/memsindustrygroup/Open-Source-Sensor-Fusion/ tree/master/docs
[2] Roetenberg, D., H.J. Luinge, C.T.M. Baten, and P.H. Veltink. "Compensation of Magnetic Disturbances Improves Inertial and Magnetic Sensing of Human Body Segment Orientation." IEEE Transactions on Neural Systems and Rehabilitation Engineering. Vol. 13. Issue 3, 2005, pp. 395-405.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using Simulink ${ }^{\circledR}$ Coder ${ }^{\mathrm{TM}}$.

See Also<br>ahrsfilter|ecompass|imufilter|imuSensor|gpsSensor<br>Introduced in R2020a

## Coordinate Transformation Conversion

Convert to a specified coordinate transformation representation


Robotics System Toolbox / Utilities<br>Navigation Toolbox / Utilities<br>ROS Toolbox / Utilities<br>UAV Toolbox / Utilities

## Description

The Coordinate Transformation Conversion block converts a coordinate transformation from the input representation to a specified output representation. The input and output representations use the following forms:

- Axis-Angle (AxAng) - [x y z theta]
- Euler Angles (Eul) - [ $\left.\begin{array}{l}z \\ y\end{array}\right]$ ], [ $\left.\begin{array}{ll}z & y \\ z\end{array}\right]$, or [ $x$ y $\left.z\right]$
- Homogeneous Transformation (TForm) - 4-by-4 matrix
- Quaternion (Quat) - [w x y z]
- Rotation Matrix (RotM) - 3-by-3 matrix
- Translation Vector (TrVec) - [x y z]

All vectors must be column vectors.
To accommodate representations that only contain position or orientation information (TrVec or Eul, for example), you can specify two inputs or outputs to handle all transformation information. When you select the Homogeneous Transformation as an input or output, an optional Show TrVec input/ output port parameter can be selected on the block mask to toggle the multiple ports.

## Ports

Input

## Input transformation - Coordinate transformation <br> column vector | 3-by-3 matrix | 4-by-4 matrix

Input transformation, specified as a coordinate transformation. The following representations are supported:

- Axis-Angle (AxAng) - [x y z theta]
- Euler Angles (Eul) - [ $\left.\begin{array}{ll}z & y \\ x\end{array}\right]$, [ $\left.\begin{array}{lll}z & y & z\end{array}\right]$, or [ $x$ y $z$ ]
- Homogeneous Transformation (TForm) - 4-by-4 matrix
- Quaternion (Quat) - [w x y z]
- Rotation Matrix (RotM) - 3-by-3 matrix
- Translation Vector (TrVec) - [x y z]

All vectors must be column vectors.
To accommodate representations that only contain position or orientation information (TrVec or Eul, for example), you can specify two inputs or outputs to handle all transformation information. When you select the Homogeneous Transformation as an input or output, an optional Show TrVec input/ output port parameter can be selected on the block mask to toggle the multiple ports.

## TrVec - Translation vector

3-element column vector
Translation vector, specified as a 3-element column vector, $\left[\begin{array}{lll}x & y & z\end{array}\right]$, which corresponds to a translation in the $x, y$, and $z$ axes respectively. This port can be used to input or output the translation information separately from the rotation vector.

## Dependencies

You must select Homogeneous Transformation (TForm) for the opposite transformation port to get the option to show the additional TrVec port. Enable the port by clicking Show TrVec input/ output port.

## Output Arguments

## Output transformation - Coordinate transformation

column vector | 3-by-3 matrix | 4-by-4 matrix
Output transformation, specified as a coordinate transformation with the specified representation. The following representations are supported:

- Axis-Angle (AxAng) - [x y z theta]
- Euler Angles (Eul) - [z y x], [z y z], or [x y z]
- Homogeneous Transformation (TForm) - 4-by-4 matrix
- Quaternion (Quat) - [w x y z]
- Rotation Matrix (RotM) - 3-by-3 matrix
- Translation Vector (TrVec) - [lllll

To accommodate representations that only contain position or orientation information (TrVec or Eul, for example), you can specify two inputs or outputs to handle all transformation information. When you select the Homogeneous Transformation as an input or output, an optional Show TrVec input/ output port parameter can be selected on the block mask to toggle the multiple ports.

## TrVec - Translation vector

three-element column vector
Translation vector, specified as a three-element column vector, $\left[\begin{array}{lll}x & y & z\end{array}\right]$, which corresponds to a translation in the $x, y$, and $z$ axes respectively. This port can be used to input or output the translation information separately from the rotation vector.

## Dependencies

You must select Homogeneous Transformation (TForm) for the opposite transformation port to get the option to show the additional TrVec port. Enable the port by clicking Show TrVec input/ output port.

## Parameters

## Representation - Input or output representation

Axis-Angle|Euler Angles|Homogeneous Transformation|Rotation Matrix| Translation Vector|Quaternion

Select the representation for both the input and output port for the block. If you are using a transformation with only orientation information, you can also select the Show TrVec input/ output port when converting to or from a homogeneous transformation.

## Axis rotation sequence - Order of Euler angle axis rotations

ZYX (default) | ZYZ|XYZ
Order of the Euler angle axis rotations, specified as $Z Y X, Z Y Z$, or $X Y Z$. The order of the angles in the input or output port Eul must match this rotation sequence. The default order $Z Y X$ specifies an orientation by:

- Rotating about the initial $z$-axis
- Rotating about the intermediate $y$-axis
- Rotating about the second intermediate $x$-axis


## Dependencies

You must select Euler Angles for the Representation input or output parameter. The axis rotation sequence only applies to Euler angle rotations.

## Show TrVec input/output port - Toggle TrVec port off (default) | on

Toggle the TrVec input or output port when you want to specify or receive a separate translation vector for position information along with an orientation representation.

## Dependencies

You must select Homogeneous Transformation (TForm) for the opposite transformation port to get the option to show the additional TrVec port.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using Simulink ${ }^{\circledR}$ Coder ${ }^{\mathrm{TM}}$.

## See Also

axang2quat|eul2tform|trvec2tform
Introduced in R2017b

## IMU

IMU simulation model


## Description

The IMU Simulink block models receiving data from an inertial measurement unit (IMU) composed of accelerometer, gyroscope, and magnetometer sensors.

## Ports

Input

## Linear Acceleration - Acceleration of IMU in local navigation coordinate system (m/s ${ }^{\mathbf{2}}$ )

$N$-by-3 matrix of real scalar
Acceleration of the IMU in the local navigation coordinate system, specified as an $N$-by- 3 matrix of real scalars in meters per second squared. $N$ is the number of samples in the current frame.
Data Types: single | double

## Angular Velocity - Angular velocity of IMU in local navigation coordinate system (rad/s) <br> $N$-by-3 matrix of real scalar

Angular velocity of the IMU sensor body frame in the local navigation coordinate system, specified as an $N$-by-3 matrix of scalars in radians per second. $N$ is the number of samples in the current frame.
Data Types: single | double

## Orientation - Orientation of IMU in local navigation coordinate system

$N$-by-4 array of real scalar | 3-by-3-by- $N$-element rotation matrix
Orientation of the IMU sensor body frame with respect to the local navigation coordinate system, specified as an $N$-by- 4 array of real scalars or a 3-by-3-by- $N$ rotation matrix. Each row the of the $N$ -by- 4 array is assumed to be the four elements of a quaternion. $N$ is the number of samples in the current frame.

Data Types: single|double
Output
Accel - Accelerometer measurement of IMU in sensor body coordinate system ( $\mathbf{m} / \mathbf{s}^{\mathbf{2}}$ )
$N$-by-3 matrix of real scalar

Accelerometer measurement of the IMU in the sensor body coordinate system, returned as an N -by- 3 matrix of real scalars in meters per second squared. $N$ is the number of samples in the current frame.
Data Types: single | double

## Gyro - Gyroscope measurement of IMU in sensor body coordinate system (rad/s) <br> N -by-3 matrix of real scalar

Gyroscope measurement of the IMU in the sensor body coordinate system, returned as an $N$-by-3 matrix of real scalars in radians per second. $N$ is the number of samples in the current frame.
Data Types: single | double
Mag - Magnetometer measurement of IMU in sensor body coordinate system ( $\mu \mathrm{T}$ )
N -by-3 matrix of real scalar
Magnetometer measurement of the IMU in the sensor body coordinate system, returned as an N -by- 3 matrix of real scalars in microtesla. $N$ is the number of samples in the current frame.
Data Types: single | double

## Parameters

## Parameters

Reference frame - Navigation reference frame
NED (default) | ENU
Navigation reference frame, specified as NED (North-East-Down) or ENU (East-North-Up).
Temperature $\left({ }^{\circ} \mathrm{C}\right)-$ Operating temperature of $\mathrm{IMU}\left({ }^{\circ} \mathrm{C}\right)$
25 (default) | real scalar
Operating temperature of the IMU in degrees Celsius, specified as a real scalar.
When the block calculates temperature scale factors and environmental drift noises, $25^{\circ} \mathrm{C}$ is used as the nominal temperature.
Data Types: single | double
Magnetic field (NED) - Magnetic field vector expressed in NED navigation frame ( $\mu \mathrm{T}$ ) [27.5550, -2.4169, -16.0849] (default) | 1-by-3 vector of scalar

Magnetic field vector expressed in the NED navigation frame, specified as a 1-by-3 vector of scalars.
The default magnetic field corresponds to the magnetic field at latitude zero, longitude zero, and altitude zero.

## Dependencies

To enable this parameter, set Reference frame to NED.
Data Types: single | double
MagneticField (ENU) - Magnetic field vector expressed in ENU navigation frame ( $\mu \mathrm{T}$ ) [-2.4169, 27.5550, 16.0849] (default)| 1-by-3 vector of scalar

Magnetic field vector expressed in the ENU navigation frame, specified as a 1-by-3 vector of scalars.

The default magnetic field corresponds to the magnetic field at latitude zero, longitude zero, and altitude zero.

## Dependencies

To enable this parameter, set Reference frame to ENU.
Data Types: single | double

## Seed - Initial seed for randomization

67 (default) | nonnegative integer
Initial seed of a random number generator algorithm, specified as a nonnegative integer.

## Data Types: single | double

## Simulate using - Type of simulation to run

## Interpreted Execution (default) |Code Generation

- Interpreted execution - Simulate the model using the MATLAB interpreter. This option shortens startup time. In Interpreted execution mode, you can debug the source code of the block.
- Code generation - Simulate the model using generated C code. The first time that you run a simulation, Simulink generates C code for the block. The C code is reused for subsequent simulations if the model does not change. This option requires additional startup time.


## Accelerometer

Maximum readings ( $\mathrm{m} / \mathrm{s}^{2}$ ) - Maximum sensor reading ( $\mathrm{m} / \mathrm{s}^{2}$ )
inf (default) | real positive scalar
Maximum sensor reading in $\mathrm{m} / \mathrm{s}^{2}$, specified as a real positive scalar.
Data Types: single | double
Resolution ( $\left.\left(\mathrm{m} / \mathrm{s}^{2}\right) / \mathrm{LSB}\right)$ - Resolution of sensor measurements (( $\left.\mathrm{m} / \mathrm{s}^{\mathbf{2}}\right) / \mathrm{LSB}$ )
0 (default) | real nonnegative scalar
Resolution of sensor measurements in $\left(\mathrm{m} / \mathrm{s}^{2}\right) / \mathrm{LSB}$, specified as a real nonnegative scalar.
Data Types: single | double
Constant offset bias ( $\mathrm{m} / \mathrm{s}^{2}$ ) - Constant sensor offset bias ( $\mathrm{m} / \mathrm{s}^{\mathbf{2}}$ )
[0000] (default) | real scalar | real 3-element row vector
Constant sensor offset bias in $\mathrm{m} / \mathrm{s}^{2}$, specified as a real scalar or 3 -element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

## Data Types: single | double

Axis skew (\%) - Sensor axes skew (\%)
$\left[\begin{array}{lll}0 & 0 & 0\end{array}\right]$ (default) | real scalar in the range $[0,100] \mid$ real 3 -element row vector in the range $[0,100]$
Sensor axes skew in a percentage, specified as a real scalar or 3-element row vector with values ranging from 0 to 100. Any scalar input is converted into a real 3 -element row vector where each element has the input scalar value.
Data Types: single | double

Velocity random walk ( $\mathrm{m} / \mathrm{s}^{2} / \sqrt{ } \mathrm{Hz}$ ) - Velocity random walk ( $\mathrm{m} / \mathrm{s}^{2} / \sqrt{\mathrm{Hz}}$ )
[0 0 0] (default) | real scalar | real 3-element row vector
Velocity random walk in ( $\mathrm{m} / \mathrm{s}^{2} / \sqrt{ } \mathrm{Hz}$ ), specified as a real scalar or 3 -element row vector. This property corresponds to the power spectral density of sensor noise. Any scalar input is converted into a real 3element row vector where each element has the input scalar value.

Data Types: single | double
Bias Instability ( $\mathrm{m} / \mathrm{s}^{\mathbf{2}}$ ) - Instability of the bias offset ( $\mathrm{m} / \mathrm{s}^{\mathbf{2}}$ )
[0 0 0] (default) | real scalar | real 3-element row vector
Instability of the bias offset in $\mathrm{m} / \mathrm{s}^{2}$, specified as a real scalar or 3 -element row vector. Any scalar input is converted into a real 3 -element row vector where each element has the input scalar value.
Data Types: single | double
Acceleration random walk ((m/s $\left.\left.{ }^{2}\right)(\sqrt{ } \mathrm{Hz})\right)$ - Acceleration random walk ((m/s $\left.{ }^{2}\right)(\sqrt{ } \mathrm{Hz})$ ) [0 0 0] (default) |real scalar | real 3-element row vector

Acceleration random walk of sensor in $\left(\mathrm{m} / \mathrm{s}^{2}\right)(\sqrt{\mathrm{Hz}})$, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3 -element row vector where each element has the input scalar value.

Data Types: single | double
Bias from temperature ( $\left.\left(\mathrm{m} / \mathrm{s}^{2}\right) /{ }^{\circ} \mathrm{C}\right)$ - Sensor bias from temperature $\left(\left(\mathrm{m} / \mathrm{s}^{2}\right) /{ }^{\circ} \mathrm{C}\right)$
[0 0 0] (default)|real scalar | real 3-element row vector
Sensor bias from temperature in $\left(\mathrm{m} / \mathrm{s}^{2}\right) /{ }^{\circ} \mathrm{C}$, specified as a real scalar or 3 -element row vector. Any scalar input is converted into a real 3 -element row vector where each element has the input scalar value.

Data Types: single | double
Temperature scale factor ( $\% /{ }^{\circ} \mathrm{C}$ ) - Scale factor error from temperature (\%/ ${ }^{\circ} \mathrm{C}$ )
$\left[\begin{array}{lll}0 & 0 & 0\end{array}\right]$ (default) | real scalar in the range $[0,100] \mid$ real 3 -element row vector in the range $[0,100]$
Scale factor error from temperature in $\% /{ }^{\circ} \mathrm{C}$, specified as a real scalar or real 3 -element row vector with values ranging from 0 to 100 . Any scalar input is converted into a real 3 -element row vector where each element has the input scalar value.

Data Types: single | double

## Gyroscope

Maximum readings (rad/s) - Maximum sensor reading (rad/s)
inf (default) | real positive scalar
Maximum sensor reading in rad/s, specified as a real positive scalar.
Data Types: single | double
Resolution ( (rad/s)/LSB) - Resolution of sensor measurements ((rad/s)/LSB)
0 (default) | real nonnegative scalar
Resolution of sensor measurements in (rad/s)/LSB, specified as a real nonnegative scalar.

## Data Types: single |double

Constant offset bias (rad/s) - Constant sensor offset bias (rad/s)
$\left.\begin{array}{lll}0 & 0 & 0\end{array}\right]$ (default) | real scalar | real 3-element row vector
Constant sensor offset bias in rad/s, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3 -element row vector where each element has the input scalar value.
Data Types: single | double

## Axis skew (\%) - Sensor axes skew (\%)

$\left[\begin{array}{lll}0 & 0 & 0\end{array}\right]$ (default) | real scalar in the range $[0,100] \mid$ real 3 -element row vector in the range $[0,100]$
Sensor axes skew in a percentage, specified as a real scalar or 3-element row vector with values ranging from 0 to 100. Any scalar input is converted into a real 3 -element row vector where each element has the input scalar value.
Data Types: single | double
Bias from acceleration ((rad/s)/(m/s2) - Sensor bias from linear acceleration (rad/s)/(m/s $\left.{ }^{2}\right)$
[0 0 0 ] (default) | real scalar | real 3-element row vector
Sensor bias from linear acceleration in $(\mathrm{rad} / \mathrm{s}) /\left(\mathrm{m} / \mathrm{s}^{2}\right)$, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3 -element row vector where each element has the input scalar value.

Data Types: single | double
Angle random walk ((rad/s)/(VHz)) - Acceleration random walk ((rad/s)/(VHz))
[0 0 0] (default) |real scalar | real 3-element row vector
Acceleration random walk of sensor in (rad/s)/( $\sqrt{ } \mathrm{Hz}$ ), specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3 -element row vector where each element has the input scalar value.

Data Types: single | double

## Bias Instability (rad/s) - Instability of the bias offset (rad/s)

[0 0 0] (default) | real scalar | real 3-element row vector
Instability of the bias offset in rad/s, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3 -element row vector where each element has the input scalar value.

Data Types: single | double
Rate random walk ((rad/s)( $\sqrt{ } \mathrm{Hz}))$ - Integrated white noise of sensor ((rad/s)( $\sqrt{ } \mathrm{Hz})$ ) [0000] (default) | real scalar | real 3-element row vector

Integrated white noise of sensor in $(\mathrm{rad} / \mathrm{s})(\sqrt{ } \mathrm{Hz})$, specified as a real scalar or 3 -element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double
Bias from temperature ( $\left.(\mathrm{rad} / \mathrm{s}) /{ }^{\circ} \mathrm{C}\right)$ - Sensor bias from temperature ( $(\mathrm{rad} / \mathrm{s}) /{ }^{\circ} \mathrm{C}$ )
[0 0 0 0 ] (default) |real scalar | real 3-element row vector

Sensor bias from temperature in (rad $/ \mathrm{s}$ ) $/{ }^{\circ} \mathrm{C}$, specified as a real scalar or 3 -element row vector. Any scalar input is converted into a real 3 -element row vector where each element has the input scalar value.
Data Types: single | double
Temperature scale factor ( $\% /{ }^{\circ} \mathrm{C}$ ) - Scale factor error from temperature (\%/ ${ }^{\circ} \mathrm{C}$ )
[0000] (default) | real scalar in the range [0,100] | real 3-element row vector in the range [0,100]
Scale factor error from temperature in $\% /{ }^{\circ} \mathrm{C}$, specified as a real scalar or real 3 -element row vector with values ranging from 0 to 100. Any scalar input is converted into a real 3 -element row vector where each element has the input scalar value.

Data Types: single | double
Magnetometer
Maximum readings ( $\mu \mathrm{T}$ ) - Maximum sensor reading ( $\mu \mathrm{T}$ )
inf (default) | real positive scalar
Maximum sensor reading in $\mu \mathrm{T}$, specified as a real positive scalar.
Data Types: single | double
Resolution ( $(\mu \mathrm{T}) / \mathrm{LSB}$ ) - Resolution of sensor measurements ( $(\mu \mathrm{T}) / \mathrm{LSB}$ )
0 (default) | real nonnegative scalar
Resolution of sensor measurements in ( $\mu \mathrm{T}$ )/LSB, specified as a real nonnegative scalar.
Data Types: single | double
Constant offset bias ( $\mu \mathrm{T}$ ) - Constant sensor offset bias ( $\mu \mathrm{T}$ )
[0 0 0 ] (default) | real scalar | real 3-element row vector
Constant sensor offset bias in $\mu \mathrm{T}$, specified as a real scalar or 3 -element row vector. Any scalar input is converted into a real 3 -element row vector where each element has the input scalar value.

Data Types: single | double

## Axis skew (\%) - Sensor axes skew (\%)

$\left[\begin{array}{lll}0 & 0 & 0\end{array}\right]$ (default) | real scalar in the range $[0,100] \mid$ real 3 -element row vector in the range $[0,100]$
Sensor axes skew in a percentage, specified as a real scalar or 3 -element row vector with values ranging from 0 to 100. Any scalar input is converted into a real 3 -element row vector where each element has the input scalar value.
Data Types: single | double
White noise PSD ( $\mu \mathrm{T} / \sqrt{ } \mathrm{Hz}$ ) - Power spectral density of sensor noise ( $\mu \mathrm{T} / \sqrt{ } \mathrm{Hz}$ )
[0 0 0] (default) | real scalar | real 3-element row vector
Power spectral density of sensor noise in $\mu \mathrm{T} / \sqrt{ } \mathrm{Hz}$, specified as a real scalar or 3 -element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double
Bias Instability ( $\mu \mathrm{T}$ ) - Instability of the bias offset ( $\mu \mathrm{T}$ )
[0 0 0] (default)|real scalar |real 3-element row vector

Instability of the bias offset in $\mu \mathrm{T}$, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single|double
Random walk ( $(\mu \mathrm{T}) * \sqrt{ } \mathrm{~Hz})$ - Integrated white noise of sensor $((\mu \mathrm{T}) * \sqrt{ } \mathrm{~Hz})$
[0 0 0 ] (default) | real scalar | real 3-element row vector
Integrated white noise of sensor in $(\mu \mathrm{T})^{*} \sqrt{ } \mathrm{~Hz}$, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double
Bias from temperature ( $\mu \mathrm{T} /{ }^{\circ} \mathrm{C}$ ) - Sensor bias from temperature ( $\mu \mathrm{T} /{ }^{\circ} \mathrm{C}$ )
[0 0 0 0 ] (default) |real scalar |real 3-element row vector
Sensor bias from temperature in $\mu \mathrm{T} /{ }^{\circ} \mathrm{C}$, specified as a real scalar or 3-element row vector. Any scalar input is converted into a real 3-element row vector where each element has the input scalar value.

Data Types: single | double
Temperature scale factor $\left(\% /{ }^{\circ} \mathrm{C}\right)$ - Scale factor error from temperature ( $\% /{ }^{\circ} \mathrm{C}$ )
$\left[\begin{array}{lll}0 & 0 & 0\end{array}\right]$ (default) | real scalar in the range $[0,100]$ | real 3-element row vector in the range [0,100]
Scale factor error from temperature in $\% /{ }^{\circ} \mathrm{C}$, specified as a real scalar or real 3 -element row vector with values ranging from 0 to 100 . Any scalar input is converted into a real 3 -element row vector where each element has the input scalar value.

Data Types: single | double

## Algorithms

## Accelerometer

The following algorithm description assumes an NED navigation frame. The accelerometer model uses the ground-truth orientation and acceleration inputs and the imuSensor and accelparams properties to model accelerometer readings.


## Obtain Total Acceleration

To obtain the total acceleration (totalAcc), the acceleration is preprocessed by negating and adding the gravity constant vector ( $g=[0 ; 0 ; 9.8] \mathrm{m} / \mathrm{s}^{2}$ assuming an NED frame) as:

$$
\text { totalAcc }=- \text { acceleration }+g
$$

The acceleration term is negated to obtain zero total acceleration readings when the accelerometer is in a free fall. The acceleration term is also known as the specific force.

## Convert to Sensor Frame

Then the total acceleration is converted from the local navigation frame to the sensor frame using:

$$
a=(\text { orientation })(\text { totalAcc })^{T}
$$

If the orientation is input in quaternion form, it is converted to a rotation matrix before processing.

## Bulk Model

The ground-truth acceleration in the sensor frame, $a$, passes through the bulk model, which adds axes misalignment and bias:

$$
b=\left(\left[\begin{array}{ccc}
1 & \frac{\alpha_{2}}{100} & \frac{\alpha_{3}}{100} \\
\frac{\alpha_{1}}{100} & 1 & \frac{\alpha_{3}}{100} \\
\frac{\alpha_{1}}{100} & \frac{\alpha_{2}}{100} & 1
\end{array}\right]\left(a^{T}\right)\right)^{T}+\text { ConstantBias }
$$

where ConstantBias is a property of accelparams, and $\alpha_{1}, \alpha_{2}$, and $\alpha_{3}$ are given by the first, second, and third elements of the AxesMisalignment property of accelparams.

## Bias Instability Drift

The bias instability drift is modeled as white noise biased and then filtered:

$$
\beta_{1}=h_{1} *(w)(\text { BiasInstability })
$$

where BiasInstability is a property of accelparams, and $h_{1}$ is a filter defined by the SampleRate property:

$$
H_{1}(z)=\frac{1}{1-\frac{1}{2} z^{-1}}
$$

## White Noise Drift

White noise drift is modeled by multiplying elements of the white noise random stream by the standard deviation:

$$
\beta_{2}=(w)\left(\sqrt{\frac{\text { SampleRate }}{2}}\right)(\text { NoiseDensity })
$$

where SampleRate is an imuSensor property, and NoiseDensity is an accelparams property. Elements of $w$ are random numbers given by settings of the imuSensor random stream.

## Random Walk Drift

The random walk drift is modeled by biasing elements of the white noise random stream and then filtering:

$$
\beta_{3}=h_{2} *(w)\left(\frac{\text { RandomWalk }}{\sqrt{\frac{\text { SampleRate }}{2}}}\right)
$$

where RandomWalk is a property of accelparams, SampleRate is a property of imuSensor, and $h_{2}$ is a filter defined as:

$$
H_{2}(z)=\frac{1}{1-z^{-1}}
$$

## Environmental Drift Noise

The environmental drift noise is modeled by multiplying the temperature difference from a standard with the temperature bias:

$$
\Delta_{e}=(\text { Temperature - 25)(TemperatureBias) }
$$

where Temperature is a property of imuSensor, and TemperatureBias is a property of accelparams. The constant 25 corresponds to a standard temperature.

## Scale Factor Error Model

The temperature scale factor error is modeled as:

$$
\text { scaleFactorError }=1+\left(\frac{\text { Temperature }-25}{100}\right) \text { (TemperatureScaleFactor) }
$$

where Temperature is a property of imuSensor, and TemperatureScaleFactor is a property of accelparams. The constant 25 corresponds to a standard temperature.

## Quantization Model

The quantization is modeled by first saturating the continuous signal model:

$$
e=\left\{\begin{array}{cc}
\text { MeasurementRange } & \text { if } d>\text { MeasurementRange } \\
- \text { MeasurementRange } & \text { if }-d>\text { MeasurementRange } \\
d & \text { else }
\end{array}\right.
$$

and then setting the resolution:

$$
\text { accelReadings }=(\text { Resolution })\left(\operatorname{round}\left(\frac{e}{\text { Resolution }}\right)\right)
$$

where MeasurementRange is a property of accelparams.

## Gyroscope

The following algorithm description assumes an NED navigation frame. The gyroscope model uses the ground-truth orientation, acceleration, and angular velocity inputs, and the imuSensor and gyroparams properties to model accelerometer readings.


## Convert to Sensor Frame

The ground-truth angular velocity is converted from the local frame to the sensor frame using the ground-truth orientation:

$$
a=(\text { orientation })(\text { angularVelocity })^{T}
$$

If the orientation is input in quaternion form, it is converted to a rotation matrix before processing.

## Bulk Model

The ground-truth angular velocity in the sensor frame, $a$, passes through the bulk model, which adds axes misalignment and bias:

$$
b=\left(\left[\begin{array}{ccc}
1 & \frac{\alpha_{2}}{100} & \frac{\alpha_{3}}{100} \\
\frac{\alpha_{1}}{100} & 1 & \frac{\alpha_{3}}{100} \\
\frac{\alpha_{1}}{100} & \frac{\alpha_{2}}{100} & 1
\end{array}\right]\left(a^{T}\right)\right)^{T}+\text { ConstantBias }
$$

where ConstantBias is a property of gyroparams, and $\alpha_{1}, \alpha_{2}$, and $\alpha_{3}$ are given by the first, second, and third elements of the AxesMisalignment property of gyroparams.

## Bias Instability Drift

The bias instability drift is modeled as white noise biased and then filtered:

$$
\beta_{1}=h_{1} *(w)(\text { BiasInstability })
$$

where BiasInstability is a property of gyroparams and $h_{1}$ is a filter defined by the SampleRate property:

$$
H_{1}(z)=\frac{1}{1-\frac{1}{2} z^{-1}}
$$

## White Noise Drift

White noise drift is modeled by multiplying elements of the white noise random stream by the standard deviation:

$$
\beta_{2}=(w)\left(\sqrt{\frac{\text { SampleRate }}{2}}\right) \text { (NoiseDensity) }
$$

where SampleRate is an imuSensor property, and NoiseDensity is an gyroparams property. The elements of $w$ are random numbers given by settings of the imuSensor random stream.

## Random Walk Drift

The random walk drift is modeled by biasing elements of the white noise random stream and then filtering:

$$
\beta_{3}=h_{2} *(w)\left(\frac{\text { RandomWalk }}{\sqrt{\frac{\text { SampleRate }}{2}}}\right)
$$

where RandomWalk is a property of gyroparams, SampleRate is a property of imuSensor, and $h_{2}$ is a filter defined as:

$$
H_{2}(z)=\frac{1}{1-z^{-1}}
$$

## Environmental Drift Noise

The environmental drift noise is modeled by multiplying the temperature difference from a standard with the temperature bias:

$$
\Delta_{e}=(\text { Temperature }-25)(\text { TemperatureBias })
$$

where Temperature is a property of imuSensor, and TemperatureBias is a property of gyroparams. The constant 25 corresponds to a standard temperature.

## Scale Factor Error Model

The temperature scale factor error is modeled as:

$$
\text { scaleFactorError }=1+\left(\frac{\text { Temperature }-25}{100}\right) \text { (TemperatureScaleFactor) }
$$

where Temperature is a property of imuSensor, and TemperatureScaleFactor is a property of gyroparams. The constant 25 corresponds to a standard temperature.

## Quantization Model

The quantization is modeled by first saturating the continuous signal model:

$$
e=\left\{\begin{array}{cc}
\text { MeasurementRange } & \text { if } d>\text { MeasurementRange } \\
- \text { MeasurementRange } & \text { if }-d>\text { MeasurementRange } \\
d & \text { else }
\end{array}\right.
$$

and then setting the resolution:

$$
\text { gyroReadings }=(\text { Resolution })\left(\text { round }\left(\frac{e}{\text { Resolution }}\right)\right)
$$

where MeasurementRange is a property of gyroparams.

## Magnetometer

The following algorithm description assumes an NED navigation frame. The magnetometer model uses the ground-truth orientation and acceleration inputs, and the imuSensor and magparams properties to model magnetometer readings.


## Convert to Sensor Frame

The ground-truth acceleration is converted from the local frame to the sensor frame using the ground-truth orientation:

$$
a=(\text { orientation })(\text { totalAcc })^{T}
$$

If the orientation is input in quaternion form, it is converted to a rotation matrix before processing.

## Bulk Model

The ground-truth acceleration in the sensor frame, $a$, passes through the bulk model, which adds axes misalignment and bias:

$$
b=\left(\left[\begin{array}{ccc}
1 & \frac{\alpha_{2}}{100} & \frac{\alpha_{3}}{100} \\
\frac{\alpha_{1}}{100} & 1 & \frac{\alpha_{3}}{100} \\
\frac{\alpha_{1}}{100} & \frac{\alpha_{2}}{100} & 1
\end{array}\right]\left(a^{T}\right)\right)^{T}+\text { ConstantBias }
$$

where ConstantBias is a property of magparams, and $\alpha_{1}, \alpha_{2}$, and $\alpha_{3}$ are given by the first, second, and third elements of the AxesMisalignment property of magparams.

## Bias Instability Drift

The bias instability drift is modeled as white noise biased and then filtered:

$$
\beta_{1}=h_{1} *(w)(\text { BiasInstability })
$$

where BiasInstability is a property of magparams and $h_{1}$ is a filter defined by the SampleRate property:

$$
H_{1}(z)=\frac{1}{1-\frac{1}{2} z^{-1}}
$$

## White Noise Drift

White noise drift is modeled by multiplying elements of the white noise random stream by the standard deviation:

$$
\beta_{2}=(w)\left(\sqrt{\frac{\text { SampleRate }}{2}}\right)(\text { NoiseDensity })
$$

where SampleRate is an imuSensor property, and NoiseDensity is an magparams property. The elements of $w$ are random numbers given by settings of the imuSensor random stream.

## Random Walk Drift

The random walk drift is modeled by biasing elements of the white noise random stream and then filtering:

$$
\beta_{3}=h_{2} *(w)\left(\frac{\text { RandomWalk }}{\sqrt{\frac{\text { SampleRate }}{2}}}\right)
$$

where RandomWalk is a property of magparams, SampleRate is a property of imuSensor, and $h_{2}$ is a filter defined as:

$$
H_{2}(z)=\frac{1}{1-z^{-1}}
$$

## Environmental Drift Noise

The environmental drift noise is modeled by multiplying the temperature difference from a standard with the temperature bias:

$$
\Delta_{e}=\text { (Temperature - 25)(TemperatureBias) }
$$

where Temperature is a property of imuSensor, and TemperatureBias is a property of magparams. The constant 25 corresponds to a standard temperature.

## Scale Factor Error Model

The temperature scale factor error is modeled as:

$$
\text { scaleFactorError }=1+\left(\frac{\text { Temperature-25 }}{100}\right) \text { (TemperatureScaleFactor) }
$$

where Temperature is a property of imuSensor, and TemperatureScaleFactor is a property of magparams. The constant 25 corresponds to a standard temperature.

## Quantization Model

The quantization is modeled by first saturating the continuous signal model:

$$
e=\left\{\begin{array}{cc}
\text { MeasurementRange } & \text { if } d>\text { MeasurementRange } \\
- \text { MeasurementRange if }-d>\text { MeasurementRange } \\
d & \text { else }
\end{array}\right.
$$

and then setting the resolution:

$$
\text { magReadings }=(\text { Resolution })\left(\text { round }\left(\frac{e}{\text { Resolution }}\right)\right)
$$

where MeasurementRange is a property of magparams.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using Simulink ${ }^{\circledR}$ Coder ${ }^{\mathrm{TM}}$.

## See Also

## Classes

accelparams | gyroparams | magparams

## Objects

imuSensor|gpsSensor

## Topics

"Model IMU, GPS, and INS/GPS"

## Introduced in R2020a

## INS

Simulate INS sensor

Library: Navigation Toolbox / Multisensor Positioning / Sensor Models<br>Automated Driving Toolbox / Driving Scenario and Sensor<br>Modeling<br>Sensor Fusion and Tracking Toolbox / Multisensor<br>Positioning / Sensor Models<br>UAV Toolbox / UAV Scenario and Sensor Modeling



## Description

The block simulates an INS sensor, which outputs noise-corrupted position, velocity, and orientation based on the corresponding inputs. The block can also optionally output acceleration and angular velocity based on the corresponding inputs. To change the level of noise present in the output, you can vary the roll, pitch, yaw, position, velocity, acceleration, and angular velocity accuracies. The accuracy is defined as the standard deviation of the noise.

## Ports

## Input

Position - Position of INS sensor
$N$-by-3 real-valued matrix
Position of the INS sensor relative to the navigation frame, in meters, specified as an $N$-by- 3 realvalued matrix. $N$ is the number of samples.

Data Types: single | double

## Velocity - Velocity of INS sensor

N -by-3 real-valued matrix of scalar
Velocity of the INS sensor relative to the navigation frame, in meters per second, specified as an $N$ -by-3 real-valued matrix. $N$ is the number of samples.

## Data Types: single | double

## Orientation - Orientation of INS sensor

3 -by-3-by- $N$ real-valued array | $N$-by-4 real-valued matrix | $N$-by-3 matrix of Euler angles
Orientation of the INS sensor relative to the navigation frame, specified as one of these formats:

- A 3-by-3-by- $N$ real-valued array, where each page of the array (3-by-3 matrix) is a rotation matrix.
- An $N$-by- 4 real-valued matrix, where each row of the matrix is the four elements of a quaternion.
- An $N$-by-3 matrix of Euler angles, where each row of the matrix is the three Euler angles corresponding to the $z-y-x$ rotation convention.
$N$ is the number of samples.


## Data Types: single | double

## Acceleration - Acceleration of INS sensor

$N$-by-3 real-valued matrix
Acceleration of the INS sensor relative to the navigation frame, in meters per second squared, specified as an $N$-by- 3 real-valued matrix. $N$ is the number of samples.

## Dependencies

To enable this input port, select Use acceleration and angular velocity.
Data Types: single | double

## AngularVelocity - Angular velocity of INS sensor

$N$-by-3 real-valued matrix
Angular velocity of the INS sensor relative to the navigation frame, in degrees per second, specified as an $N$-by-3 real-valued matrix. $N$ is the number of samples.

## Dependencies

To enable this input port, select Use acceleration and angular velocity.

## Data Types: single | double

## HasGNSSFix - Enable GNSS fix

$N$-by-1 logical vector
Enable GNNS fix, specified as an $N$-by-1 logical vector. $N$ is the number of samples. Specify this input as false to simulate the loss of a GNSS receiver fix. When a GNSS receiver fix is lost, position measurements drift at a rate specified by the Position error factor parameter.

## Dependencies

To enable this input port, select Enable HasGNSSFix port.

## Data Types: single|double

## Output

## Position - Position of INS sensor

$N$-by-3 real-valued matrix
Position of the INS sensor relative to the navigation frame, in meters, returned as an $N$-by-3 realvalued matrix. $N$ is the number of samples in the input.
Data Types: single|double

## Velocity - Velocity of INS sensor

$N$-by-3 real-valued matrix
Velocity of the INS sensor relative to the navigation frame, in meters per second, returned as an $N$ -by-3 real-valued matrix. $N$ is the number of samples in the input.

## Data Types: single|double

## Orientation - Orientation of INS sensor

3-by-3-by- $N$ real-valued array | $N$-by-4 real-valued matrix
Orientation of the INS sensor relative to the navigation frame, returned as one of the formats:

- A 3-by-3-by- $N$ real-valued array, where each page of the array (3-by-3 matrix) is a rotation matrix.
- An $N$-by-4 real-valued matrix, where each row of the matrix is the four elements of a quaternion.
- An $N$-by-3 matrix of Euler angles, where each row of the matrix is the three Euler angles corresponding to the z - y -x rotation convention.
$N$ is the number of samples in the input.
Data Types: single | double


## Acceleration - Acceleration of INS sensor

$N$-by-3 real-valued matrix
Acceleration of the INS sensor relative to the navigation frame, in meters per second squared, returned as an $N$-by- 3 real-valued matrix. $N$ is the number of samples.

## Dependencies

To enable this output port, select Use acceleration and angular velocity.

## Data Types: single | double

## AngularVelocity - Angular velocity of INS sensor <br> $N$-by-3 real-valued matrix

Angular velocity of the INS sensor relative to the navigation frame, in degrees per second, returned as an $N$-by- 3 real-valued matrix. $N$ is the number of samples.

## Dependencies

To enable this output port, select Use acceleration and angular velocity.

## Data Types: single | double

## Parameters

Mounting location (m) - Location of sensor on platform (m)
$\left[\begin{array}{lll}0 & 0 & 0\end{array}\right]$ (default)| three-element real-valued vector of form $[x y z]$
Location of the sensor on the platform, in meters, specified as a three-element real-valued vector of the form $[x y z]$. The vector defines the offset of the sensor origin from the origin of the platform.
Data Types: single | double
Roll (X-axis) accuracy (deg) - Accuracy of roll measurement (deg)
0.2 (default) | nonnegative real scalar

Accuracy of the roll measurement of the sensor body in degrees, specified as a nonnegative real scalar.

Roll is defined as rotation around the $x$-axis of the sensor body. Roll noise is modeled as white process noise with standard deviation equal to the specified Roll accuracy in degrees.
Data Types: single | double
Pitch (Y-axis) accuracy (deg) - Accuracy of pitch measurement (deg)
0.2 (default) | nonnegative real scalar

Accuracy of the pitch measurement of the sensor body in degrees, specified as a nonnegative real scalar.

Pitch is defined as rotation around the $y$-axis of the sensor body. Pitch noise is modeled as white process noise with standard deviation equal to the specified Pitch accuracy in degrees.
Data Types: single | double
Yaw (Z-axis) accuracy (deg) - Accuracy of yaw measurement (deg)
1 (default) | nonnegative real scalar
Accuracy of the yaw measurement of the sensor body in degrees, specified as a nonnegative real scalar.

Yaw is defined as rotation around the $z$-axis of the sensor body. Yaw noise is modeled as white process noise with standard deviation equal to the specified Yaw accuracy in degrees.
Data Types: single | double
Position accuracy (m) - Accuracy of position measurement (m)
1 (default) | nonnegative real scalar | 1-by-3 vector of nonnegative values
Accuracy of the position measurement of the sensor body in meters, specified as a nonnegative real scalar or a 1-by-3 vector of nonnegative values. If you specify the parameter as a scalar value, then the block sets the accuracy of all three position components to this value.

Position noise is modeled as white process noise with a standard deviation equal to the specified Position accuracy in meters.
Data Types: single | double
Velocity accuracy ( $\mathrm{m} / \mathrm{s}$ ) - Accuracy of velocity measurement (m/s)
1 (default) | nonnegative real scalar
Accuracy of the velocity measurement of the sensor body in meters per second, specified as a nonnegative real scalar.

Velocity noise is modeled as white process noise with a standard deviation equal to the specified Velocity accuracy in meters per second.
Data Types: single | double
Use acceleration and angular velocity - Use acceleration and angular velocity off (default) | on
Select this check box to enable the block inputs of acceleration and angular velocity through the Acceleration and AngularVelocity input ports, respectively. Meanwhile, the block outputs the acceleration and angular velocity measurements through the Acceleration and AngularVelocity output ports, respectively. Additionally, selecting this parameter enables you to specify the Acceleration accuracy and Angular velocity accuracy parameters.

## Acceleration accuracy ( $\mathrm{m} / \mathrm{s}^{2}$ ) - Accuracy of acceleration measurement (m/s ${ }^{2}$ ) <br> 0 (default) | nonnegative real scalar

Accuracy of the acceleration measurement of the sensor body in meters, specified as a nonnegative real scalar.

Acceleration noise is modeled as white process noise with a standard deviation equal to the specified Acceleration accuracy in meters per second squared.

## Dependencies

To enable this parameter, select Use acceleration and angular velocity.

## Data Types: single | double

## Angular velocity accuracy (deg/s) - Accuracy of angular velocity measurement (deg/s) <br> 0 (default) | nonnegative real scalar

Accuracy of the angular velocity measurement of the sensor body in meters, specified as a nonnegative real scalar.

Angular velocity noise is modeled as white process noise with a standard deviation equal to the specified Angular velocity accuracy in degrees per second.

## Dependencies

To enable this parameter, select Use acceleration and angular velocity.
Data Types: single | double
Enable HasGNSSFix port - Enable HasGNSSFix input port
off (default) | on
Select this check box to enable the HasGNSSFix input port. When the HasGNSSFix input is specified as false, position measurements drift at a rate specified by the Position error factor parameter.

Position error factor ( $m$ ) - Position error factor (m)
[0 0 0] (default) | nonnegative scalar | 1-by-3 real-valued vector
Position error factor without GNSS fix, specified as a scalar or a 1-by-3 real-valued vector. If you specify the parameter as a scalar value, then the block sets the position error factors of all three position components to this value.

When the HasGNSSFix input is specified as false, the position error grows at a quadratic rate due to constant bias in the accelerometer. The position error for a position component $E(t)$ can be expressed as $E(t)=1 / 2 \alpha t^{2}$, where $\alpha$ is the position error factor for the corresponding component and $t$ is the time since the GNSS fix is lost. The computed $E(t)$ values for the $x, y$, and $z$ components are added to the corresponding position components of the Position output.

## Dependencies

To enable this parameter, select Enable HasGNSSFix port.
Data Types: double

## Intial Seed - Initial seed for randomization

67 (default) | nonnegative integer
Initial seed of a random number generator algorithm, specified as a nonnegative integer.
Data Types: single | double

## Simulate using - Type of simulation to run

Interpreted Execution (default)|Code Generation

- Interpreted execution - Simulate the model using the MATLAB interpreter. This option shortens startup time. In Interpreted execution mode, you can debug the source code of the block.
- Code generation - Simulate the model using generated C code. The first time that you run a simulation, Simulink generates $C$ code for the block. The $C$ code is reused for subsequent simulations if the model does not change. This option requires additional startup time.


## See Also

IMU | insSensor

## Topics

"Model IMU, GPS, and INS/GPS"
Introduced in R2020b

## GPS

Simulate GPS sensor readings with noise

| Library: | UAV Toolbox / UAV Scenario and Sensor Modeling |
| :--- | :--- |
|  | Navigation Toolbox / Multisensor Positioning / Sensor |
|  | Models |
|  | Sensor Fusion and Tracking Toolbox / Multisensor |
|  | Positioning / Sensor Models |



## Description

The block outputs noise-corrupted GPS measurements based on the input position and velocity in the local coordinate frame or geodetic frame. It uses the WGS84 earth model to convert local coordinates to latitude-longitude-altitude LLA coordinates.

## Ports

Input

## Position - Position of GPS receiver in navigation coordinate system

matrix
Specify the input position of the GPS receiver in the navigation coordinate system as a real, finite N -by-3 matrix. $N$ is the number of samples in the current frame. The format of the matrix rows differs depending on the value of the Position input format parameter.

- If the value of the Position input format parameter is Local, specify each row of the Position as Cartesian coordinates in meters with respect to the local navigation reference frame, specified by the Reference frame parameter, with the origin specified by the Reference location parameter.
- If the value of the Position input format parameter is Geodetic, specify each row of the Position input as geodetic coordinates of the form [latitude longitude altitude]. The values of latitude and longitude are in degrees. Altitude is the height above the WGS84 ellipsoid model in meters.


## Data Types: single | double

Velocity - Velocity in local navigation coordinate system (m/s)
matrix
Specify the input velocity of the GPS receiver in the navigation coordinate system in meters per second as a real, finite $N$-by- 3 matrix. $N$ is the number of samples in the current frame. The format of the matrix rows differs depending on the value of the Position input format parameter.

- If the value of the Position input format parameter is Local, specify each row of the Velocity with respect to the local navigation reference frame (NED or ENU), specified by the Reference frame parameter, with the origin specified by the Reference location parameter.
- If the value of the Position input format parameter is Geodetic, specify each row of the Velocity with respect to the navigation reference frame (NED or ENU), specified by the Reference frame parameter, with the origin specified by Position.

Data Types: single | double

## Output

LLA - Position in LLA coordinate system
matrix
Position of the GPS receiver in the geodetic latitude, longitude, and altitude (LLA) coordinate system, returned as a real, finite $N$-by-3 array. Latitude and longitude are in degrees with North and East being positive. Altitude is in meters.
$N$ is the number of samples in the current frame.
Data Types: single|double

## Velocity - Velocity in local navigation coordinate system (m/s) <br> matrix

Velocity of the GPS receiver in the local navigation coordinate system in meters per second, returned as a real, finite $N$-by- 3 matrix. $N$ is the number of samples in the current frame. The format of the matrix rows differs depending on the value of the Position input format parameter.

- If the value of the Position input format parameter is Local, the Velocity output is with respect to the local navigation reference frame (NED or ENU), specified by the Reference frame parameter, with the origin specified by the Reference location parameter.
- If the value of the Position input format parameter is Geodetic, the Velocity output is with respect to the navigation reference frame (NED or ENU), specified by the Reference frame parameter, with the origin specified by LLA.

Data Types: single | double

## Groundspeed - Magnitude of horizontal velocity in local navigation coordinate system (m/s) <br> vector

Magnitude of the horizontal velocity of the GPS receiver in the local navigation coordinate system in meters per second, returned as a real, finite $N$-element column vector.
$N$ is the number of samples in the current frame.
Data Types: single | double

## Course - Direction of horizontal velocity in local navigation coordinate system ( ${ }^{\circ}$ )

 vectorDirection of the horizontal velocity of the GPS receiver in the local navigation coordinate system, in degrees, returned as a real, finite $N$-element column vector of values from 0 to 360 . North corresponds to 0 degrees and East corresponds to 90 degrees.
$N$ is the number of samples in the current frame.
Data Types: single | double

## Parameters

## Reference frame - Reference frame

NED (default) | ENU
Specify the reference frame as NED (North-East-Down) or ENU(East-North-Up).

## Position input format - Position coordinate input format

Local (default) | Geodetic
Specify the position coordinate input format as Local or Geodetic.

- If you set this parameter to Local, then the input to the Position port must be in the form of Cartesian coordinates with respect to the local navigation frame, specified by the Reference Frame parameter, with the origin fixed and defined by the Reference location parameter. The input to the Velocity input port must also be with respect to this local navigation frame.
- If you set this parameter to Geodetic, then the input to the Position port must be geodetic coordinates in [latitude longitude altitude]. The input to the Velocity input port must also be with respect to the navigation frame specified by the Reference frame parameter, with the origin corresponding to the Position port.


## Reference location - Origin of local navigation reference frame

[0, 0, 0] (default) | three-element vector
Specify the origin of the local reference frame as a three-element row vector in geodetic coordinates [latitude longitude altitude], where altitude is the height above the reference ellipsoid model WGS84. The reference location values are in degrees, degrees, and meters, respectively. The degree format is decimal degrees (DD).

## Dependencies

To enable this parameter, set the Position input format parameter to Local.

## Horizontal position accuracy - Horizontal position accuracy (m)

1.6 (default) | nonnegative real scaler

Specify horizontal position accuracy as a nonnegative real scalar in meters. The horizontal position accuracy specifies the standard deviation of the noise in the horizontal position measurement. Increasing this value adds noise to the measurement, decreasing its accuracy.

Tunable: Yes

## Vertical position accuracy - Vertical position accuracy (m) <br> 3 (default) | nonnegative real scaler

Specify vertical position accuracy as a nonnegative real scalar in meters. The vertical position accuracy specifies the standard deviation of the noise in the vertical position measurement. Increasing this value adds noise to the measurement, decreasing its accuracy.

Tunable: Yes

## Velocity accuracy - Velocity accuracy (m/s)

## 0.1 (default) | nonnegative real scalar

Specify velocity accuracy per second as a nonnegative real scalar in meters. The velocity accuracy specifies the standard deviation of the noise in the velocity measurement. Increasing this value adds noise to the measurement, decreasing its accuracy.

Tunable: Yes

## Decay factor - Global position noise decay factor

0.999 (default) | scalar in range [0, 1]

Specify the global position noise decay factor as a numeric scalar in the range [0, 1]. A decay factor of 0 models the global position noise as a white noise process. A decay factor of 1 models the global position noise as a random walk process.

Tunable: Yes

## Seed - Initial seed

67 (default) | nonnegative integer
Specify the initial seed of an mt19937ar random number generator algorithm as a nonnegative integer.

## Simulate using - Type of simulation to run

Interpreted execution (default) | Code generation
Select the type of simulation to run from these options:

- Interpreted execution - Simulate the model using the MATLAB interpreter. For more information, see "Simulation Modes".
- Code generation - Simulate the model using generated C code. The first time you run a simulation, Simulink generates C code for the block. The C code is reused for subsequent simulations, as long as the model does not change.


## See Also

## Objects

gpsSensor
Topics
"Model IMU, GPS, and INS/GPS"

## Introduced in R2021b

## Pure Pursuit

Linear and angular velocity control commands

Library:<br>Robotics System Toolbox / Mobile Robot Algorithms<br>Navigation Toolbox / Control Algorithms



## Description

The Pure Pursuit block computes linear and angular velocity commands for following a path using a set of waypoints and the current pose of a differential drive vehicle. The block takes updated poses to update velocity commands for the vehicle to follow a path along a desired set of waypoints. Use the Max angular velocity and Desired linear velocity parameters to update the velocities based on the performance of the vehicle.

The Lookahead distance parameter computes a look-ahead point on the path, which is an instantaneous local goal for the vehicle. The angular velocity command is computed based on this point. Changing Lookahead distance has a significant impact on the performance of the algorithm. A higher look-ahead distance results in a smoother trajectory for the vehicle, but can cause the vehicle to cut corners along the path. Too low of a look-ahead distance can result in oscillations in tracking the path, causing unstable behavior. For more information on the pure pursuit algorithm, see "Pure Pursuit Controller".

## Input/Output Ports

## Input

## Pose - Current vehicle pose

```
[x y theta] vector
```

Current vehicle pose, specified as an [x y theta] vector, which corresponds to the $x-y$ position and orientation angle, theta. Positive angles are measured counterclockwise from the positive $x$-axis.

## Waypoints - Waypoints <br> [ ] (default) | $n$-by-2 array

Waypoints, specified as an $n$-by- 2 array of [ $\mathrm{x} y$ ] pairs, where $n$ is the number of waypoints. You can generate the waypoints using path planners like mobileRobotPRM or specify them as an array in Simulink.

## Output

## LinVel - Linear velocity

scalar in meters per second
Linear velocity, specified as a scalar in meters per second.
Data Types: double

## AngVel - Angular velocity

scalar in radians per second
Angular velocity, specified as a scalar in radians per second.
Data Types: double
TargetDir - Target direction for vehicle
scalar in radians

Target direction for the vehicle, specified as a scalar in radians. The forward direction of the vehicle is considered zero radians, with positive angles measured counterclockwise. This output can be used as the input to the TargetDir port for the Vector Field Histogram block.

## Dependencies

To enable this port, select the Show TargetDir output port parameter.

## Parameters

Desired linear velocity (m/s) - Linear velocity
0.1 (default) | scalar

Desired linear velocity, specified as a scalar in meters per second. The controller assumes that the vehicle drives at a constant linear velocity and that the computed angular velocity is independent of the linear velocity.

## Maximum angular velocity (rad/s) - Angular velocity

1.0 (default) | scalar

Maximum angular velocity, specified as a scalar in radians per second. The controller saturates the absolute angular velocity output at the given value.

## Lookahead distance (m) - Look-ahead distance

1.0 (default) | scalar

Look-ahead distance, specified as a scalar in meters. The look-ahead distance changes the response of the controller. A vehicle with a higher look-ahead distance produces smooth paths but takes larger turns at corners. A vehicle with a smaller look-ahead distance follows the path closely and takes sharp turns, but oscillate along the path. For more information on the effects of look-ahead distance, see "Pure Pursuit Controller".

## Show TargetDir output port - Target direction indicator <br> off (default) | on

Select this parameter to enable the TargetDir out port. This port gives the target direction as an angle in radians from the forward position, with positive angles measured counterclockwise.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using Simulink ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

## Blocks

Vector Field Histogram

## Classes <br> binary0ccupancyMap | occupancyMap | binary0ccupancyMap | occupancyMap | controllerVFH

## Topics

"Plan Path for a Differential Drive Robot in Simulink" (Robotics System Toolbox)
"Path Following with Obstacle Avoidance in Simulink®"
"Pure Pursuit Controller"

Introduced in R2019b

## Vector Field Histogram

Avoid obstacles using vector field histogram
Library: Navigation Toolbox / Control Algorithms


## Description

The Vector Field Histogram (VFH) block enables your vehicle to avoid obstacles based on range sensor data. Given a range sensor reading in terms of ranges and angles, and a target direction to drive toward, the VFH controller computes an obstacle-free steering direction.

For more information on the algorithm details, see "Vector Field Histogram" on page 4-51 under Algorithms.

## Limitations

- The Ranges and Angles inputs are limited to 4000 elements when generating code for models that use this block.


## Input/Output Ports

## Input

## Ranges - Range values from scan data

vector of scalars
Range values from scan data, specified as a vector of scalars in meters. These range values are distances from a sensor at specified angles. The vector must be the same length as the corresponding Angles vector.

## Angles - Angle values from scan data

vector of scalars
Angle values from scan data, specified as a vector of scalars in radians. These angle values are the specific angles of the specified ranges. The vector must be the same length as the corresponding Ranges vector.

## TargetDir - Target direction for vehicle <br> scalar

Target direction for the vehicle, specified as a scalar in radians. The forward direction of the vehicle is considered zero radians, with positive angles measured counterclockwise. You can use the TargetDir output from the Pure Pursuit block when generating controls from a set of waypoints.

## Output <br> steeringDir - Steering direction for vehicle <br> scalar

Steering direction for the vehicle, specified as a scalar in radians. This obstacle-free direction is calculated based on the VFH+ algorithm. The forward direction of the vehicle is considered zero radians, with positive angles measured counterclockwise.

## Parameters

## Main

## Number of angular sectors - Number of bins used to create the histograms 180 (default) | scalar

Number of bins used to create the histograms, specified as a scalar. This parameter is nontunable. You can set this parameter only when the object is initialized.

## Range distance limits ( m ) - Limits for range readings

[0.05 2] (default)|two-element vector of scalars
Limits for range readings in meters, specified as a two-element vector of scalars. The range readings input are only considered if they fall within the distance limits. Use the lower distance limit to ignore false positives from poor sensor performance at lower ranges. Use the upper limit to ignore obstacles that are too far away from the vehicle.

## Histogram thresholds - Thresholds for computing binary histogram <br> [3 10] (default) | two-element vector of scalars

Thresholds for computing binary histogram, specified as a two-element vector of scalars. The algorithm uses these thresholds to compute the binary histogram from the polar obstacle density. Polar obstacle density values higher than the upper threshold are represented as occupied space (1) in the binary histogram. Values smaller than the lower threshold are represented as free space (0). Values that fall between the limits are set to the values of a previous computed binary histogram if one exists from previous iterations. If a previous histogram does not exist, the value is set as free space (0).

```
vehicle radius (m) - Radius of the vehicle
```


## 0.1 (default) | scalar

Radius of the vehicle, specified as a scalar in meters. This dimension defines the smallest circle that can circumscribe your vehicle. The vehicle radius is used to account for vehicle size when computing the obstacle-free direction.

## Safety distance (m) - Safety distance around the vehicle <br> 0.1 (default) | scalar

Safety distance left around the vehicle position in addiction to vehicle radius, specified as a scalar in meters. The vehicle radius and safety distance are used to compute the obstacle-free direction.

## Minimum turning radius (m) - Minimum turning radius at current speed 0.1 (default) | scalar

Minimum turning radius for the vehicle moving at its current speed, specified as a scalar in meters.

## Simulate using - Specify type of simulation to run <br> Code generation (default)| Interpreted execution

- Code generation - Simulate model using generated C code. The first time you run a simulation, Simulink generates $C$ code for the block. The $C$ code is reused for subsequent simulations, as long as the model does not change. This option requires additional startup time but the speed of the subsequent simulations is comparable to Interpreted execution.
- Interpreted execution - Simulate model using the MATLAB interpreter. This option shortens startup time but has a slower simulation speed than Code generation. In this mode, you can debug the source code of the block.

Tunable: No

## Cost Function Weights

Target direction weight - Cost function weight for target direction
5 (default) | scalar
Cost function weight for moving toward the target direction, specified as a scalar. To follow a target direction, set this weight to be higher than the sum of Current direction weight and Previous direction weight. To ignore the target direction cost, set this weight to 0 .

## Current direction weight - Cost function weight for current direction <br> 2 (default) | scalar

Cost function weight for moving the vehicle in the current heading direction, specified as a scalar. Higher values of this weight produce efficient paths. To ignore the current direction cost, set this weight to 0.

## Previous direction weight - Cost function weight for previous direction <br> 2 (default) | scalar

Cost function weight for moving in the previously selected steering direction, specified as a scalar. Higher values of this weight produce smoother paths. To ignore the previous direction cost, set this weight to 0 .

## Algorithms

## Vector Field Histogram

The block uses the VFH+ algorithm to compute the obstacle-free direction. First, the algorithm takes the ranges and angles from range sensor data and builds a polar histogram for obstacle locations. Then, it uses the input histogram thresholds to calculate a binary histogram that indicates occupied and free directions. Finally, the algorithm computes a masked histogram, which is computed from the binary histogram based on the minimum turning radius of the vehicle.

The algorithm selects multiple steering directions based on the open space and possible driving directions. A cost function, with weights corresponding to the previous, current, and target directions, calculates the cost of different possible directions. The algorithm then returns an obstaclefree direction with minimal cost. Using the obstacle-free direction, you can input commands to move your vehicle in that direction.

To use this block for your own application and environment, you must tune the algorithm parameters. Parameter values depend on the type of vehicle, the range sensor, and the hardware you use. For more information on the VFH algorithm, see cont rollerVFH.

## See Also

## Blocks

Pure Pursuit | Publish | Subscribe
Classes
controllerVFH

## Topics

"Vector Field Histogram"
Introduced in R2019b

$$
5
$$

Apps

## SLAM Map Builder

Build 2-D grid maps using lidar-based SLAM

## Description

The SLAM Map Builder app loads recorded lidar scans and odometry sensor data to build a 2-D occupancy grid using simultaneous localization and mapping (SLAM) algorithms. Incremental scan matching aligns and overlays scans to build the map. Loop closure detection adjusts for drift of the vehicle odometry by detecting previously visited locations and adjusting the overall map. Sometimes, the scan matching algorithm and loop closure detection require manual adjustment. Use the app to manually align scans and modify loop closures to improve the overall map accuracy. You can also tune the SLAM algorithm settings to improve the automatic map building.

## To use the app:

| $\sqrt{3}$ <br> Import | To load rosbag log files, select Import > Import from rosbag. Select the rosbag file and click Open. This opens the Import tab. For more information, see Import and Filter a rosbag on page 5-13. <br> To load data from the workspace, Import > Import from workspace. Select your Scans and Poses variables using the drop downs provided. You can also specify the variables in the slamMapBuilder function. See Programmatic Use on page 5-12. |
| :---: | :---: |
| SLAM Settings | Use SLAM Settings to adjust the SLAM algorithm settings. Default values are provided, but your specific sensors and data may require tuning of these settings. The most important value to tune is the Loop Closure Threshold. For more information, see Tune SLAM Settings on page 5-13. |
| Build | Click Build to begin the SLAM map building process. The building process aligns scans in the map using incremental scan matching, identifies loop closures when visiting previous locations, and adjusts poses. Click Pause at any time during the map building process to manually align incremental scans or modify loop closures. |
| $\begin{array}{\|cc}  & \\ \begin{array}{cc} \text { Incremental } \\ \text { Match } & \text { Loop } \\ \text { Closure } \end{array} \end{array}$ | Click Incremental Match to modify the relative pose of the currently selected frame and align the scan with the previous scan. Click Loop Closure to modify or ignore the detected loop closure for the current frame. Use the slider on the bottom to scroll back to areas where scan matching or loop closures are not accurate. You can modify any number of scans or loop closures. For more information, see Modify Increment Scans and Loop Closures on page 5-14. |
| 气 <br> Sync | After modifying your map, click Sync to update all the poses in the scan map. The two options under Sync are Sync, which searches for new loop closures, or Sync Fast, which skips loop closure searching and just updates the scan map. For more information, see Sync the Map on page 5-15. |
| Export Occupancy Grid | When you are satisfied with how the map looks, click Export to OccupancyGrid to either export the map to an m-file or save the map in the workspace. The map is output as a 2-D probabilistic occupancy grid in an occupancyMap object. |
|  | You can open existing app sessions you have saved using Open Session. When you are in the Map Builder tab, you can save your progress to an m-file using Save Session. |



## Open the SLAM Map Builder App

- 

MATLAB Toolstrip: On the Apps tab, under Control System Design and Analysis, click SLAM Map Builder.

- MATLAB Command Window: Enter slamMapBuilder


## Examples

## Build and Tune a Map Using Lidar Scans with SLAM

The SLAM Map Builder app helps you build an occupancy grid from lidar scans using simultaneous localization and mapping (SLAM) algorithms. The map is built by estimating poses through scan matching and using loop closures for pose graph optimization. This example shows you the workflow for loading a rosbag of lidar scan data, filtering the data, and building the map. Tune the scan map by adjusting incremental scan matches and modifying loop closures.

## Load Lidar Scan Data

Load the example .mat file into the workspace, which contains a variable, scans, as a cell array of lidarScan objects.
load slamLidarScans.mat

## Open the App

In the Apps tab, under Control System Design and Analysis, click SLAM Map Builder.
Also, you can call the slamMapBuilder function:
slamMapBuilder

## Import Lidar Scans

Click Import > Import from workspace to load the scans. Data stored as a rosbag can be loaded with a ROS Toolbox license.


Select the scans variable in the Scans drop down.


In the tool bar, set Downsample to (\%) to 10. Downsampling evenly samples from the data to reduce computation time for the SLAM algorithm. For this example, $10 \%$ is every 5th scan. Click Apply.

Use the slider or arrow keys at the bottom to preview the scans.


Once you are done importing, click Close.

## Tune SLAM Settings

The SLAM algorithm can be tuned using the SLAM Settings dialog. The parameters should be adjusted based on your sensor specifications, the environment, and your application. For this example, increase Loop Closure Threshold from 200 to 300. This increased threshold decreases the likelihood of accepting and using a detected loop closure. Set the Optimization Interval to 10. With every 10th loop closure accepted, the pose graph is optimized to account for drift.

| 4 SLAM Map Builder - SLAM Settings | - |  | $\square$ | $\times$ |
| :---: | :---: | :---: | :---: | :---: |
| Lidar SLAM Parameters NLP Solver Parameters |  |  |  |  |
| Map Resolution (cells/m) | 8 |  |  |  |
| Lidar Range [min,max] (m) | 020 |  |  |  |
| Loop Closure Threshold | 300 |  |  |  |
| Loop Closure Search Radius (m) | 8 |  |  |  |
| Loop Closure Max Attempts | 1 |  |  |  |
| Loop Closure Auto Rollback | on |  |  |  |
| Optimization Interval (\# of Loop Closures) | 10 |  |  |  |
| Movement Threshold [Linear,Angular] (m,rad) | 00 |  |  |  |
|  | OK | Cancel |  |  |

## Build the Map

After filtering your data and setting the SLAM algorithm settings, click Build. The app begins processing scans to build the map. You should see the slider progressing and scans being overlaid in the map. The estimated robot trajectory is plotted on the same scan map. Incremental scan matches are shown in the Incremental Match pane. Whenever a loop closure is detected, the Loop Closure pane shows the two scans overlaid on each other.


## Adjust Scan Matches or Loop Closures

At any time during the build process, if you notice the map is distorted or an incremental match or loop closure looks off, click Pause to select scans for adjustment. You can modify scans at the end of the build process as well. Navigate using the arrow keys or slider to the point in the file where the distortion first occurs. Click the Incremental Match or Loop Closure buttons to adjust the currently displayed scan poses. In this section, the bad loop closure is artificial and only for illustration purposes.

Click the Loop Closure button. This opens a tab for modifying the loop closure relative pose.


To ignore the loop closure completely, click Ignore. Otherwise, manually modify the relative scan pose until the scans line up.

Click Pan Scan or Rotate Scan, then click and drag in the figure to align the two scans. Click Accept when you are done. You can do this for multiple scans.


After you modify your scan poses for incremental matches and loop closures, click Sync to apply changes. SyncFast updates the map without searching for new loop closures and reduces computation time if you have already processed all the scans.


## Export Occupancy Grid

Once you have synced your changes and finished building the map, you should see a fully overlaid scan map with a robot trajectory.


Click Export Occupancy Grid to get a final occupancy map of your environment as a occupancyMap object. Specify the variable name to export the map to the workspace. You can create a map from a subset of scans by scrolling back to the desired frame before exporting and selecting Up to currently selected scan.

Call show on the stored map to visualize the occupancy map.
show(my0ccMap)


You can also save a SLAM Map Builder app session using the Save Session button. The app writes the current state of the app to a . mat file that can be loaded later using Open Session.

- "Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
- "Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"


## Programmatic Use

slamMapBuilder (bag) opens the SLAM Map Builder app and imports the rosbag log file specified in bag, a BagSelection object created using the rosbag function. The app opens to the Import tab to filter the sensor data in your rosbag.
slamMapBuilder(sessionFile) opens the SLAM Map Builder app from a saved session file name, sessionFile. An app session file is created through the Save Session button in the app toolstrip.
slamMapBuilder (scans) opens the SLAM Map Builder app and imports the scans specified in scans, a cell array of lidarScan objects. The app assumes you have prefiltered your scans and skips the import process. Click Build to start building the map.
slamMapBuilder(scans, poses) opens the SLAM Map Builder app and imports the scans and poses. scans is specified as a cell array of lidarScan objects. poses is a matrix of [ $x$ y theta] vectors that correspond to the poses of scans. The app assumes you have prefiltered your scans and skips the import process. Click Build to start building the map.

## More About

## Import and Filter a rosbag

When you click the Import button, specify the parameters for your rosbag and how you want to filter the data in the toolstrip. You must Apply your settings to see the scans updated in the figures.

- Select the ROS topic for the lidar scans and odometry (if available).
- In Odom Topic, if you select Use TF, specify the frame of the lidar scan sensor, Lidar Frame, and the base fixed frame of the vehicle, Fixed Frame. The items in the drop down menu are generated based on the available frames in the tf transformation tree of the rosbag.
- Specify the Start Time and End Time if you want to trim data from rosbag. You can use the sliders or manually type in your time values.
- Select the desired downsample percentage of scans in Downsample Scans. This evenly downsamples the scans based on the percentage. For example, a value of $25 \%$ would only select every fourth scan.
- Click Apply to see the new filtered scans and apply all settings. Close the tab when you are done.

If you'd like more control over filtering scans in the rosbag, import your rosbag into MATLAB using rosbag. Filter the rosbag using select. To open the app using your custom filtered rosbag, see Programmatic Use on page 5-12.

## Tune SLAM Settings

To improve the automatic map building process, the SLAM algorithm has tunable parameters. Click SLAM Settings to tune the parameters. Use Lidar SLAM Parameters to affect different aspects of the scan alignment and loop closure detection processes. Also, tune the NLP Solver Parameters to change how the map optimization algorithm improves the overall map based on loop closures.

## Lidar SLAM Parameters:

- Map Resolution (cells/m) -- Resolution of the map. The resolution affects the location accuracy of the scan alignment and defines the output size of the occupancy grid.
- Lidar Range [min, max] (m) -- Range of lidar sensor readings. When processing the lidar scans, readings outside of the lidar range are ignored.
- Loop Closure Threshold -- Unitless threshold for accepting loop closures. Depending on your lidar scans, the average loop closure score varies. If the build process does not find loop closures and the vehicle revisits locations in the map, consider lowering this threshold.
- Loop Closure Search Radius (m) -- Radius to search for loop closures. Based on the odometry pose, the algorithm searches for loop closures in the existing map within the given radius in meters.
- Loop Closure Max Attempts -- Number of attempts at finding loop closures. When this number increases, the algorithm makes more attempts to find loop closures in the map but increases computation time.
- Loop Closure Auto Rollback -- Allow automatic rejection of loop closures. The algorithm tracks the residual error from the map optimization. If it detects a sudden change in the error and this parameter is set to on, the loop closure is rejected.
- Optimization Interval (\# of Loop Closures) -- Number of detected loop closures accepted to trigger optimization. By default, the map is optimized with every loop closure found.
- Movement Threshold [Linear,Angular] (m,rad) -- Minimum change in pose required to accept a new scan. If the pose of the vehicle does not exceed this threshold, the next scan is discarded from the map building process.


## NLP Solver Parameters:

- Max Iterations -- Maximum number of iterations for map optimization. Increasing this value may improve map accuracy but increases computation time.
- Max Time (s) -- Maximum time allowed for map optimization specified in seconds. Increasing this value may improve map accuracy but increases computation time.
- Gradient Tolerance -- Lower bound on the norm of the gradient of the cost function for optimization. Lowering this value causes the optimization to run longer to search for a local minimum but increases the computation time.
- Function Tolerance -- Lower bound on the change in the cost function for optimization. Lowering this value causes the optimization to run longer to search for a local minimum but increases the computation time.
- Step Tolerance -- Lower bound on the step size for optimization. Lowering this value causes the optimization to run longer to search for a local minimum but increases the computation time.
- First Node Pose [x,y,theta] (m,rad) -- Pose of the first node in the graph. If you need to offset the position of the scans in the map, specify the position, $[x y]$, in meters and orientation, theta, in radians.

After changing any of these settings, the map building process must be restarted to rebuild the map with the new parameters.

## Modify Incremental Matches and Loop Closures

This app allows you to manually modify incremental scans and adjust detected loop closures. If you notice scans are not properly aligned after you build the map, use the Incremental Match and Loop Closure buttons to open their modification tabs. Use the modification toolstrip buttons to adjust the relative pose between scans.


- Ignore -- When modifying loop closures, you can simply ignore loop closures if they are inaccurate. The algorithm always discards ignored loop closure if detected in the same app session. You cannot ignore incremental scan matches.
- Pan Scan -- Click this button to manually shift the pose. After selecting, click and drag inside the map to shift the scans and overlay them properly. Align all the points of the scans until you are satisfied. You can manually specify the $\mathbf{X}, \mathbf{Y}$ location in the Relative Pose section as well.
- Rotate Scan -- Click this button to manually rotate the pose. After selecting, click and drag inside the map to rotate the scans and overlay them properly. Align all the points of the scans until you are satisfied. You can manually specify the Theta location in the Relative Pose section as well.


## Sync the Map

After making modifications to the map building process using Incremental Scans and Loop
Closures, you must sync the map to apply the changes. Based on the changes you make to properly align scans, the overall map shifts and alignments change for every scan after your modification. You have two options after making your modifications, Sync or Sync Fast. If you click Sync Fast, the changes to the poses are automatically applied and no other changes to the map occur. Sync restarts the entire map building and loop closure detection processes starting at the first modification. The specified modifications are applied, but the algorithm attempts to realign other scans and search for new loop closures as well.

## See Also

## Functions

buildMap | matchScans | matchScansGrid| rosbag|optimizePoseGraph

## Objects

lidarSLAM| lidarScan | occupancyMap | poseGraph

## Topics

"Implement Simultaneous Localization And Mapping (SLAM) with Lidar Scans"
"Implement Online Simultaneous Localization And Mapping (SLAM) with Lidar Scans"

## Introduced in R2019b


[^0]:    "trust-region" (default) |"fminunc"

[^1]:    You can identify the attribute letter given a channel or code and a satellite system.

[^2]:    sensorData - Sensor data
    table

